

Graph Drawing Through the Lens of a Framework for Analyzing Visualization Methods

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<http://www.cs.ubc.ca/~tmm/talks.html#gd13>

Why?...
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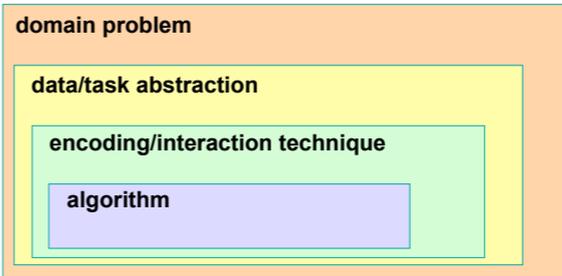
Outline

- Levels of visualization design
- Abstraction for data
- Principles of marks and channels
- Using space
- Further analysis examples
- Conclusions

Levels of visualization design

Separating vis design into four levels

- connecting all the way from real-world problems of target users to algorithms



– covered elsewhere: validation
[A Nested Model for Visualization Design and Validation. Munzner. IEEE Trans. Visualization and Computer Graphics (Proc. InfoVis 09), 15(6):921-928, 2009.]

Emphasis: Technique level

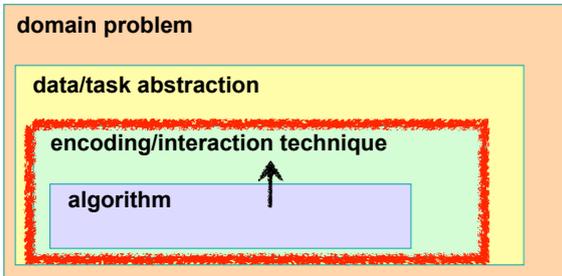
- just above familiar algorithm level, connects directly
- plus a bit of background on abstraction



[A Nested Model for Visualization Design and Validation. Munzner. IEEE Trans. Visualization and Computer Graphics (Proc. InfoVis 09), 15(6):921-928, 2009.]

Goal: More upwards characterization

- map from algorithms up to techniques they support



[A Nested Model for Visualization Design and Validation. Munzner. IEEE Trans. Visualization and Computer Graphics (Proc. InfoVis 09), 15(6):921-928, 2009.]

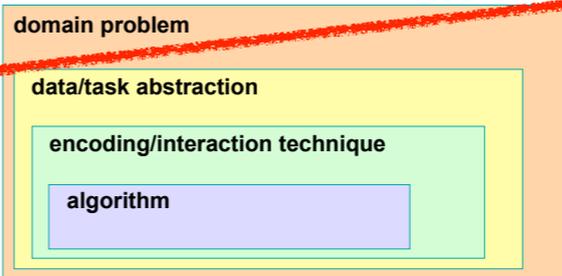
Characterize how?

- focus here on one major issue
 - how is space used?
- explicit consideration in visualization
 - trickier to see from purely graph drawing perspective
 - common cases not trivial to analyze!
 - node-link diagrams, compound graphs

Covered elsewhere: Downwards from real users

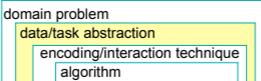
- design study methodology paper
 - problem-driven work: building for specific people to use

[Design Study Methodology: Reflections from the Trenches and the Stacks. Sedlmair, Meyer, and Munzner. IEEE Trans. Visualization and Computer Graphics (Proc. InfoVis 2012), 18(12):2431-2440, 2012.]



Abstraction for data

Abstraction: data types



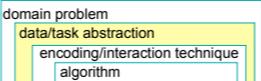
Dataset Types

- Tables
 - attributes
 - items
- Networks
 - node = item
 - link
- Trees
- Text/Logs
 - The quick brown fox...

Attribute Types

- Categorical
 - ★ ○ +
- Ordered
- Quantitative
 - |||||

Abstraction: data types



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Attribute Types

- Categorical
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–covered elsewhere: task abstraction
[A Multi-Level Typology of Abstract Visualization Tasks. Brehmer and Munzner. IEEE Trans. Visualization and Computer Graphics (Proc. InfoVis), to appear 2013.]

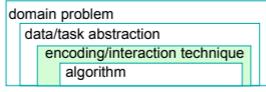
Deriving new data: Common case

- example: Strahler number for graphs
 - centrality metric: node importance
 - new per-node quantitative attrib
 - result of global calculation
- visualization uses
 - fast interactive rendering: draw nodes in order of importance
 - draw small subset: structure far more understandable than w/ random sampling



–more detail in Auber02
[Using Strahler numbers for real time visual exploration of huge graphs. Auber. Intl. Conf. Computer Vision and Graphics, 2002, p. 56-69.]

Principles of marks and channels



Techniques: Visual encoding

- how to analyze?
 - start with easy cases from statistical graphics



Marks and channels

- marks: geometric primitives
 - points
 - lines
 - areas
- visual channels: control appearance of marks
 - position
 - horizontal, vertical, both
 - color
 - tilt
 - size
 - shape

Techniques: Visual encoding analysis principles

- analyze as combination of marks and channels showing abstract data



Techniques: Visual encoding analysis principles

- analyze as combination of marks and channels showing abstract data



1: vertical position

mark: line

Techniques: Visual encoding analysis principles

- analyze as combination of marks and channels showing abstract data



1: vertical position
2: vertical position, horizontal position

mark: line mark: point

Techniques: Visual encoding analysis principles

- analyze as combination of marks and channels showing abstract data



1: vertical position
2: vertical position, horizontal position
3: vertical position, horizontal position, color

mark: line mark: point mark: point

Techniques: Visual encoding analysis principles

- analyze as combination of marks and channels showing abstract data



1: vertical position
2: vertical position, horizontal position
3: vertical position, horizontal position, color
4: vertical position, horizontal position, color, size

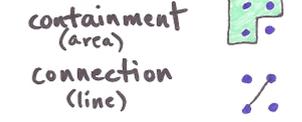
mark: line mark: point mark: point mark: point

Marks as links

Marks as Items/Nodes



Marks as Links



- we implicitly perceive some properties as indicating relationships between items
 - containment
 - connection
 - also, proximity
 - use of space

Channel types

- channels also have implicit perceptual types
 - match them with attribute types
 - avoid losing information or implying incorrect properties
 - how much: ordered
 - example: spatial position along a common scale
 - example: length of line mark
 - what: categorical
 - example: spatial region
- spatial channels have strongest perceptual impact
 - reason for focus on use of space here
- many other channels: color, size, orientation, ...
 - we know types and ranking in terms of impact (roughly)

Channel rankings

Ordered: Ordinal/Quantitative
How much

- position on common scale
- position on unaligned scale
- length (1D size)
- tilt/angle
- area (2D size)
- curvature
- volume (3D size)
- lightness black/white
- color saturation
- stipple density

Categorical
What

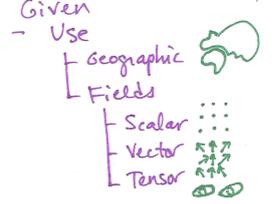
- region
- color hue
- shape
- stipple pattern

• covered elsewhere: [Visualization Principles] <http://www.cs.ubc.ca/~tmm/talks.htm#vizbi11>

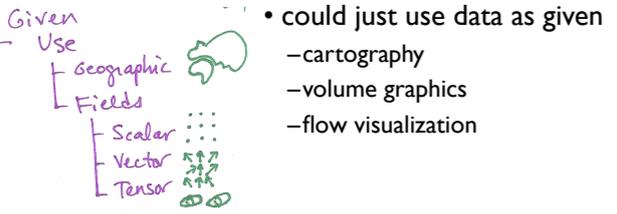
• focus here: implications of these rankings!

Using space

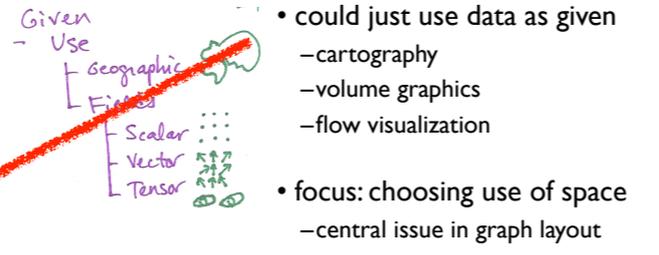
Using space: Channel choices



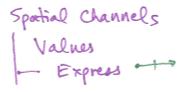
Using space: Channel choices



Using space: Channel choices



Using space: Channel choices



Using space: Channel choices

- values expressed spatially
 - encode quantitative attribute using spatial position of mark
 - example: scatterplots



Using space: Channel choices

Spatial Channels

- Values
 - Express
 - Regions
 - Separate
 - order
 - Align
- 1D list
- 2D matrix
- 3D vol. grid
- 3+D recursive subdivision

- values expressed spatially
 - encode quantitative attribute using spatial position of mark
 - example: scatterplots
- regions of space
 - separate into regions
 - proximity implies grouping
 - order regions
 - could be data-driven
 - align for more precise judgements
 - can subdivide recursively

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Using space: Examples

Spatial Channels

- Values
 - Express
 - Regions
 - Separate
 - order
 - Align
- 1D list
- 2D matrix
- 3D vol. grid
- 3+D recursive subdivision

- multiple bar charts
 - data: table, 3 attribs
 - 1 quant, 2 categ
 - marks: line
 - spatial channels
 - within each region
 - express value w/ vert spatial pos
 - align vert
 - order by quant attrib
 - one choice: separate views
 - separate into 2 regions by categ attrib
 - another choice: interleaved view
 - separate into 4 regions, 1 per item
 - draw both attribs within region

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Using space: Examples

Spatial Channels

- Values
 - Express
 - Regions
 - Separate
 - order
 - Align
- 1D list
- 2D matrix
- 3D vol. grid
- 3+D recursive subdivision

- heatmap
 - data: same!
 - 1 quant, 2 categ
 - marks: area
 - (color by quant attrib)
 - spatial channels
 - separate and align in 2D matrix
 - indexed by 2 categ attribs
 - order: many choices
 - matrix reordering algs

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Using space: Examples

Spatial Channels

- Values
 - Express
 - Regions
 - Separate
 - order
 - Align
- 1D list
- 2D matrix
- 3D vol. grid
- 3+D recursive subdivision

- matrix graph view
 - data, channels: same!
 - derived data: table from network
 - 1 quant attrib
 - weighted edge between nodes
 - 2 categ attribs: node list x 2
 - spatial channels:
 - cell shows presence/absence of edge

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Using space: Links

Link Marks

- Connection
- Containment

- marks as links (vs. nodes)
 - common case in graph drawing
 - 1D case: connection
 - ex: all node-link diagrams
 - emphasizes topology, path tracing
 - 2D case: containment
 - ex: all treemap variants
 - emphasizes attribute values at leaves (size coding)

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Using space: Layout orientation

Spatial Layout

- Rectilinear
- Parallel
- Radial

- spatial layout
 - orientation of spatial axes

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Using space: Layout orientation

Spatial Layout

- Rectilinear
- Parallel
- Radial

- spatial layout
 - orientation of spatial axes

29

Using space: Layout orientation

Spatial Layout

- Rectilinear
- Parallel
- Radial

- spatial layout
 - orientation of spatial axes
- limitations studied
 - rectilinear: scalability wrt #axes
 - 2 axes best
 - 3 problematic
 - see Visualization Principles talk
 - 4+ impossible
 - radial: perceptual limits
 - angles lower precision than lengths

[Uncovering Strengths and Weaknesses of Radial Visualizations - an Empirical Approach. Diehl, Beck and Burch. IEEE TVCG (Proc. InfoVis) 16(6):935-942, 2010.]

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Analysis examples: Tree drawing

- data shown
 - link relationships
 - tree depth
 - sibling order
- methods
 - connection vs containment link marks
 - rectilinear vs radial layout
 - spatial position channels
- considerations
 - redundant? arbitrary?
 - information density?
 - avoid wasting space

[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees. McGuffin and Robert. Information Visualization 9:2 (2010), 115-140.]

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Analysis example: force-directed placement

- visual encoding
 - link connection marks
 - node point marks
- considerations
 - spatial position: no meaning directly encoded
 - left free to minimize crossings
 - proximity semantics?
 - sometimes meaningful
 - sometimes arbitrary, artifact of layout algorithm
 - tension with length
 - long edges more visually salient than short

[http://mbostock.github.com/d3/text/force.html]

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Analysis example: multi-level FDP (sfdp)

- data
 - original: network
 - derived: cluster hierarchy atop it
- visual encoding
 - same: link connection marks
- considerations
 - better algorithm for same encoding technique
 - same: fundamental use of space
 - hierarchy used in algorithm but not shown explicitly

[Efficient and high quality force-directed graph drawing. Hu. The Mathematica Journal 10:37-71, 2005.]

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Analysis example: GrouseFlocks

- data: compound graphs
 - network
 - cluster hierarchy atop it
 - derived or interactively chosen
- visual encoding
 - connection marks for network links
 - containment marks for hierarchy
 - point marks for nodes
- dynamic interaction
 - select individual metanodes in hierarchy to expand/contract

[GrouseFlocks: Steerable Exploration of Graph Hierarchy Space. Archambault, Munzner, and Auber. IEEE TVCG 14(4): 900-913, 2008.]

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Multiple views vs single views

Combining Views

- Side By Side
- Superimposed
- Changing

- powerful method: use multiple views side by side
 - vs. superimposing multiple views as layers atop each other
 - all must have shared spatial layout
 - vs. single view that changes over time
 - as with interactive navigation
- principle: eyes beat memory
 - easy to compare by moving eyes between side-by-side views
 - harder to compare visible item to memory of what you saw
 - external cognition vs. internal working memory limits

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Further analysis examples

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Analysis example: Cerebral

- data
 - network
 - nodes: genes, links: known interaction
 - per-node attribs
 - location within cell where interaction occurs
 - biological function
 - table
 - 1 quant attrib: gene expression level
 - indexed by 2 categ attribs: node/gene, experimental condition

[Cerebral: Visualizing Multiple Experimental Conditions on a Graph with Biological Context. Barsky, Munzner, Gardy, and Kincaid. IEEE TVCG (Proc. InfoVis) 14(6): 1253-1260, 2008.]

[Cerebral: a Cytoscape plugin for layout of and interaction with biological networks using subcellular localization annotation. Barsky, Gardy, Hancock, and Munzner. Bioinformatics 23(8):1040-1042, 2007.]

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Use of space: Cerebral

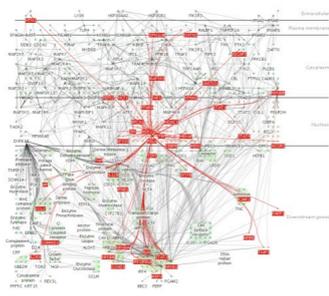
- side by side views
 - small multiples
 - same encoding, different data
 - separate into regions
 - each shows entire network
 - color nodes by quant attrib for condition

[Cerebral: Visualizing Multiple Experimental Conditions on a Graph with Biological Context. Barsky, Munzner, Gardy, and Kincaid. IEEE TVCG (Proc. InfoVis) 14(6):1253-1260, 2008.]

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Use of space: Cerebral

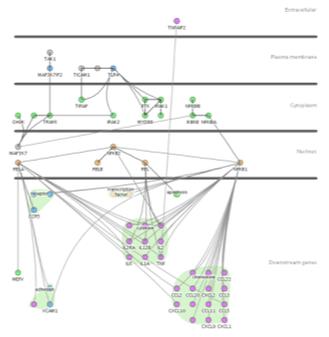
- superimposed layers within each view
 - dynamic interaction technique
- highlight 1-hop neighbors on mouseover
 - foreground layer distinguished by color



Cerebral: a Cytoscape plugin for layout of and interaction with biological networks using subcellular localization annotation. Barsky, Gardy, Hancock, and Munzner. *Bioinformatics* 23(8):1040-1042, 2007.]

Use of space: Cerebral

- network visual encoding
 - consideration
 - mimic stylized spatial semantics of hand-drawn diagrams
 - marks: connection for links
 - spatial channels
 - separate into regions according to subcellular location attrib
 - order regions vert by attrib
 - in bottom region: also separate into subregions by function attrib



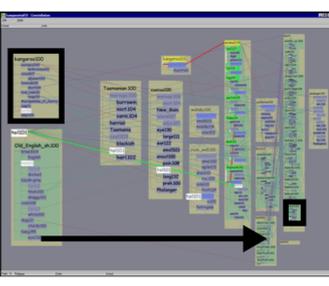
Cerebral: a Cytoscape plugin for layout of and interaction with biological networks using subcellular localization annotation. Barsky, Gardy, Hancock, and Munzner. *Bioinformatics* 23(8):1040-1042, 2007.]

Considerations: Cerebral

- explicit discussion of choices for use of space
 - design motivated by analysis of previous work
 - justified as more suitable than characterized alternatives
 - changing single view with animation: avoided
 - cognitive load
 - hard to track changes across many conditions and many nodes
 - separating into one region per gene: avoided
 - information density
 - not enough space to show multiple attribs within node for big networks
 - enough space to show multiple networks with single mark per node
 - » separating into one region per condition: chosen
 - spatial position: partially constrained

Analysis example: Constellation

- data
 - multi-level network
 - node: word
 - link: words used in same dictionary definition
 - subgraph for each definition
 - not just hierarchical clustering
 - paths through network
 - query for high-weight paths between 2 nodes
 - quant attrib: plausibility

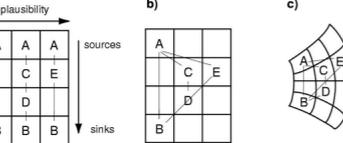
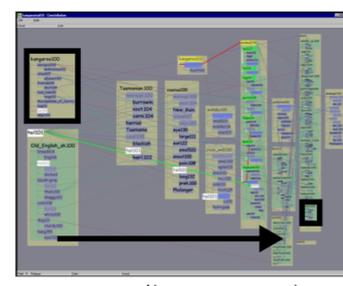


[Interactive Visualization of Large Graphs and Networks. Munzner. Ph.D. Dissertation, Stanford University, June 2000.]

[Constellation: A Visualization Tool For Linguistic Queries from MindNet. Munzner, Guimbretière and Robertson. *Proc. IEEE Symp. InfoVis* 1999, p. 132-135.]

Using space: Constellation

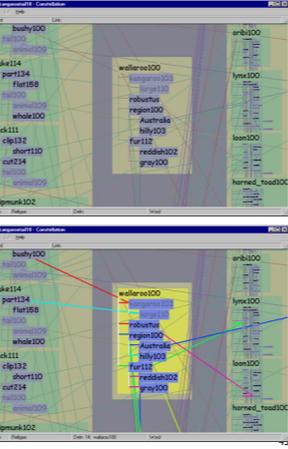
- visual encoding
 - link connection marks between words
 - link containment marks to indicate subgraphs
 - encode plausibility with horiz spatial position
 - encode source/sink for query with vert spatial position
- spatial layout
 - curvilinear grid: more room for longer low-plausibility paths



[Interactive Visualization of Large Graphs and Networks. Munzner. Ph.D. Dissertation, Stanford University, June 2000.]

Using space: Constellation

- edge crossings
 - cannot easily minimize instances, since position constrained by spatial encoding
 - instead: minimize perceptual impact
- views: superimposed layers
 - dynamic foreground/background layers on mouseover, using color
 - four kinds of constellations
 - definition, path, link type, word
 - not just 1-hop neighbors



[Interactive Visualization of Large Graphs and Networks. Munzner. Ph.D. Dissertation, Stanford University, June 2000.]

Considerations: Constellation

- another example of design motivated by analysis
 - explicit discussion of choices using space
 - spatial position: highly constrained
 - tradeoffs
 - information density vs spatial encoding semantics
 - » covered elsewhere: iterative refinement of layout
 - crossings: instances vs salience

Analysis example: Noack LinLog

- energy model designed to reveal clusters in data
 - requires that edges between clusters longer than those within
 - visual encoding technique
 - using same minimization algorithms as previous work
- considerations
 - also design motivated by prior analysis
 - explicit discussion of technique-level issues in GD literature
 - encourage more papers like this!



[An Energy Model for Visual Graph Clustering. Noack. *Proc. Graph Drawing* 2003, p. 425-436.]

Conclusions

Framework goals

- guide development of new algorithms/techniques
 - in same spirit as examples shown
 - Cerebral, Constellation, LinLog Energy
- characterize existing algorithms/techniques
 - can guide adoption
 - in what context are they suitable?
 - context here: previous design levels
- vis methods analysis only one possible route!
 - many others
 - benchmarks, computational complexity, user studies...

Vis methods analysis framework

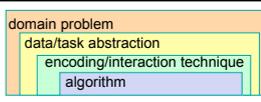
- characterize techniques in terms of methods for using space
 - marks and channels
 - marks for nodes vs marks for links
 - space channel: express, separate, order, align
 - position, proximity, partitioning into groups
- general way to analyze visualizations systematically
 - applied to graph drawing examples in particular

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Mapping upwards

- from algorithms to techniques
 - sometimes trivial
 - discussion in paper itself
 - direct citation of previous work for framing context
 - sometimes tricky indeed
 - when algorithm description does not facilitate analysis of resulting visual encoding
 - use for space, or other channels
 - line between algorithm and technique can be blurry
 - does new algorithm support existing technique, or new one?
 - » trivial when speed increase for identical visual results
- from techniques to abstractions to domain problems
 - equally important questions, but beyond scope for today...



More information

- this talk
 - <http://www.cs.ubc.ca/~tmm/talks.html#gd13>
- more on analysis
 - techniques/methods in more depth
 - also, principles and abstractions!
- single chapter in 2009 Fundamentals of Graphics textbook *Visualization*
 - <http://www.cs.ubc.ca/~tmm/papers.html#akpchapter>
- full vis textbook: to appear, 2014, AK Peters
 - *Visualization Analysis and Design: Principles, Abstractions, and Methods*