

# Information Visualization

## Networks & Trees 1/2

**Tamara Munzner**

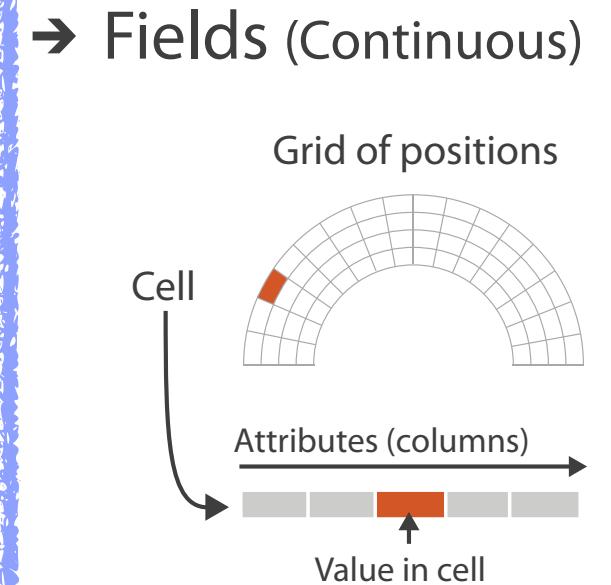
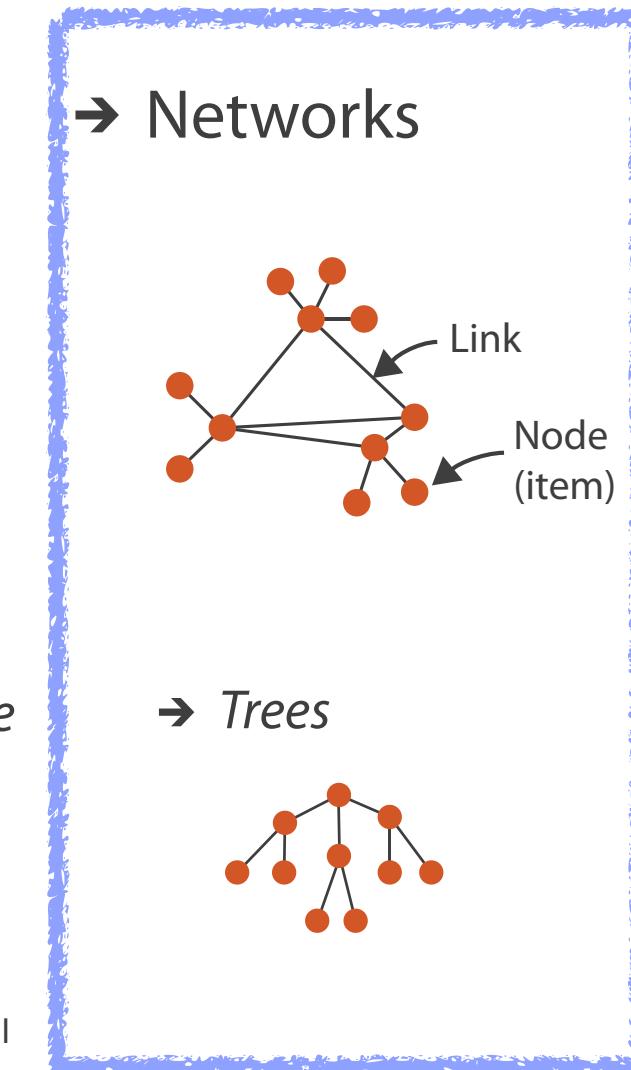
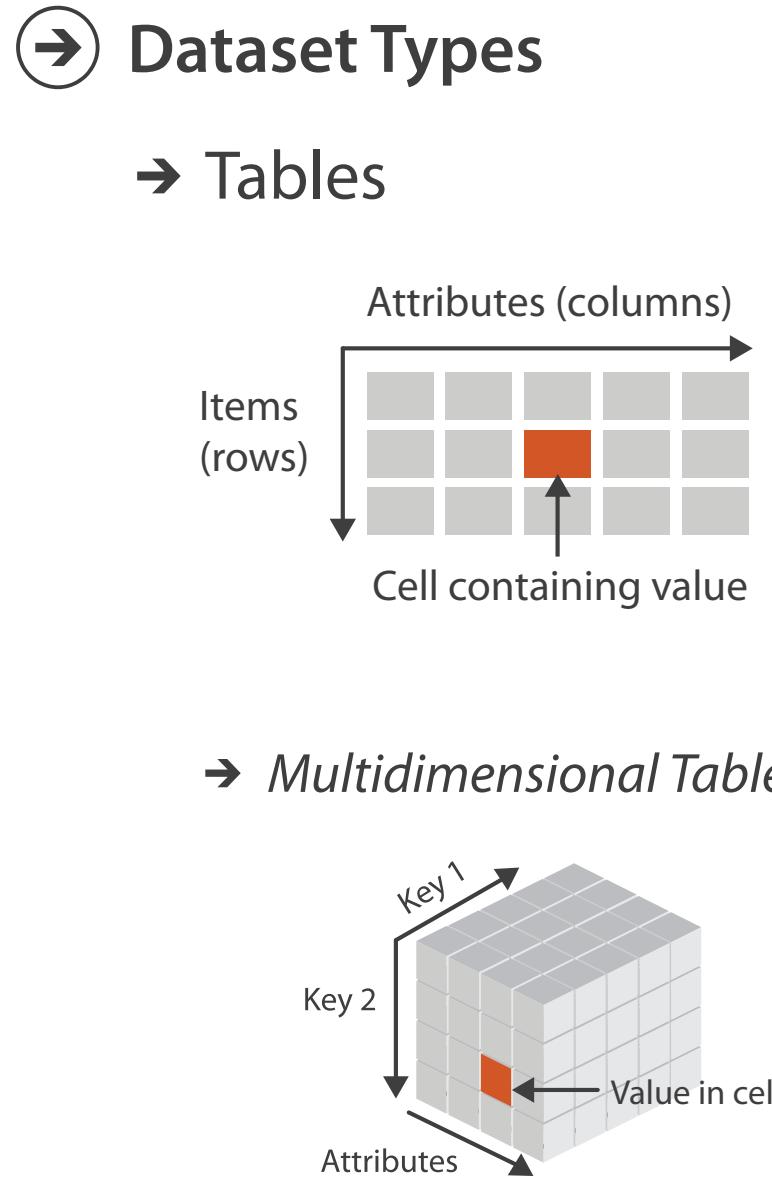
Department of Computer Science  
University of British Columbia

**Lect 14/15, Feb 27 & Mar 3 2020**

**<https://www.cs.ubc.ca/~tmm/courses/436V-20>**

# Network data

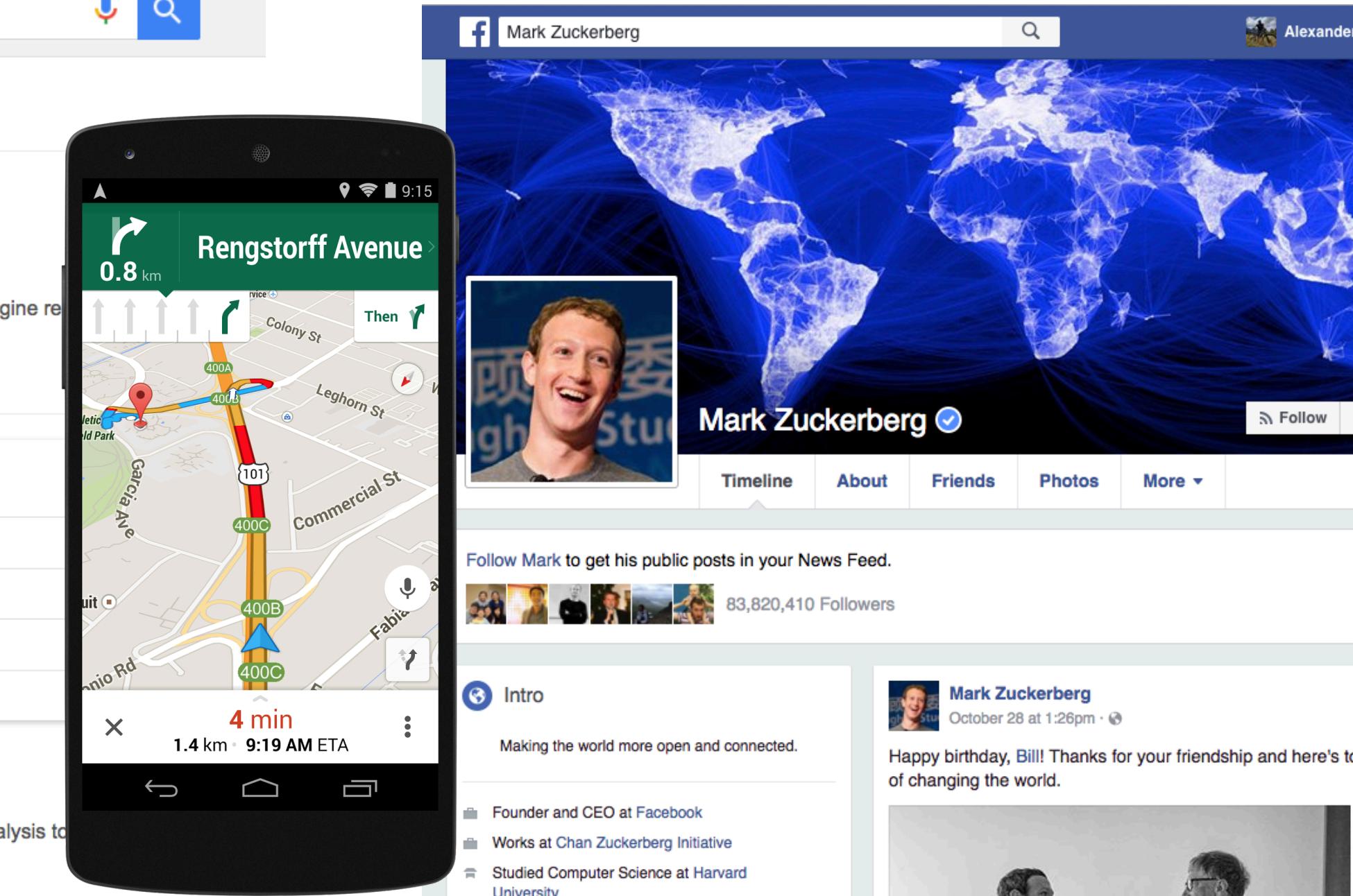
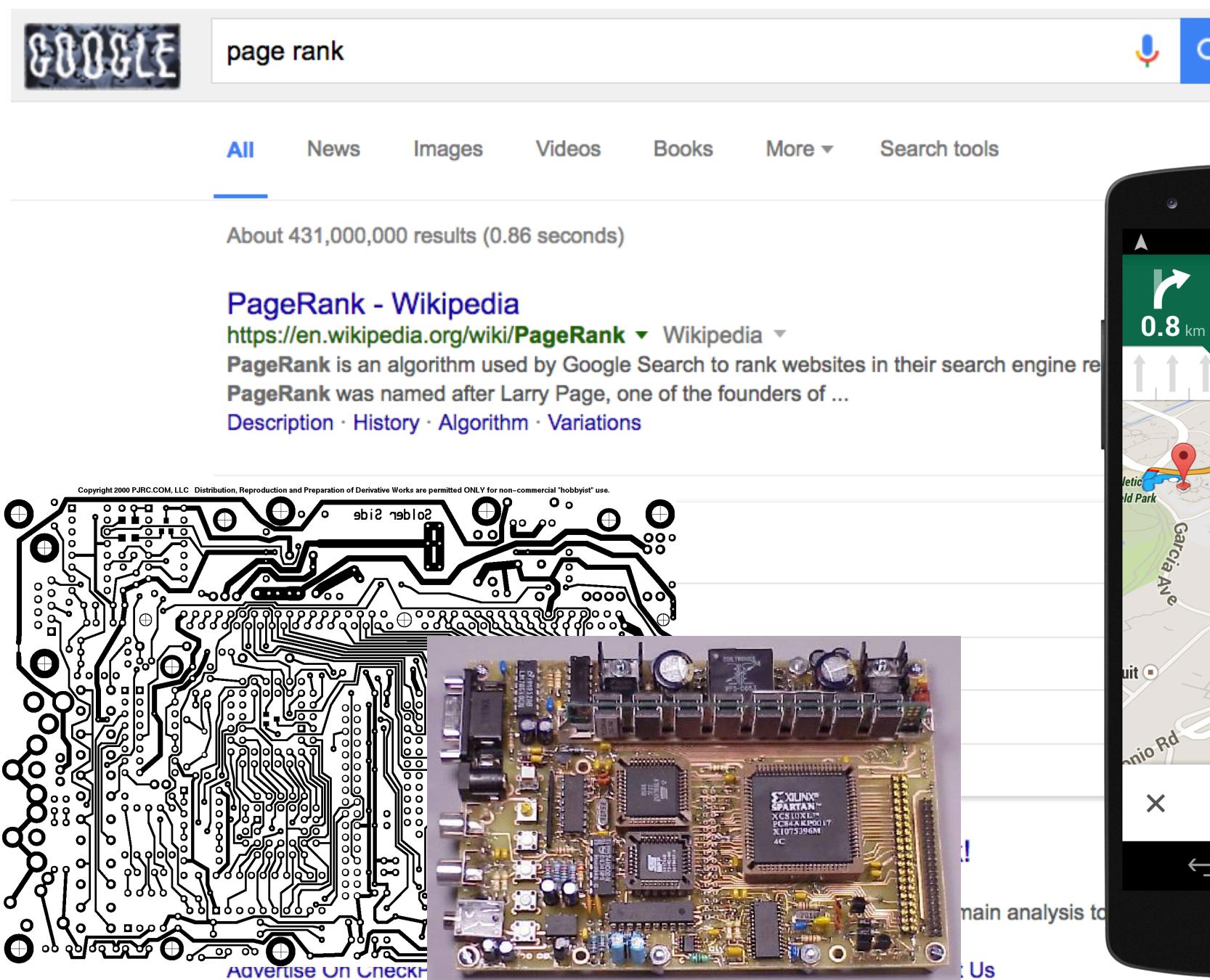
- networks
  - model relationships between things
    - aka graphs
  - two kinds of items, both can have attributes
    - nodes
    - links
- tree
  - special case
  - no cycles
    - one parent per node



# **Networks**

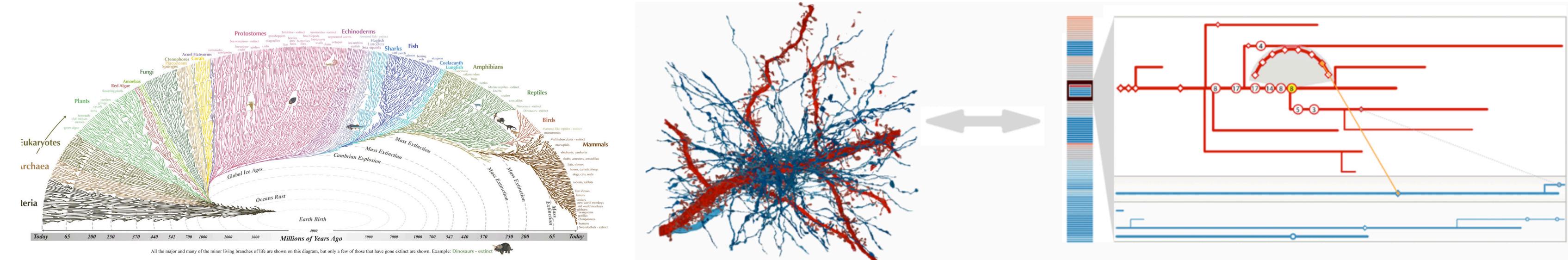
# Applications of networks

- without networks, couldn't have any of these:

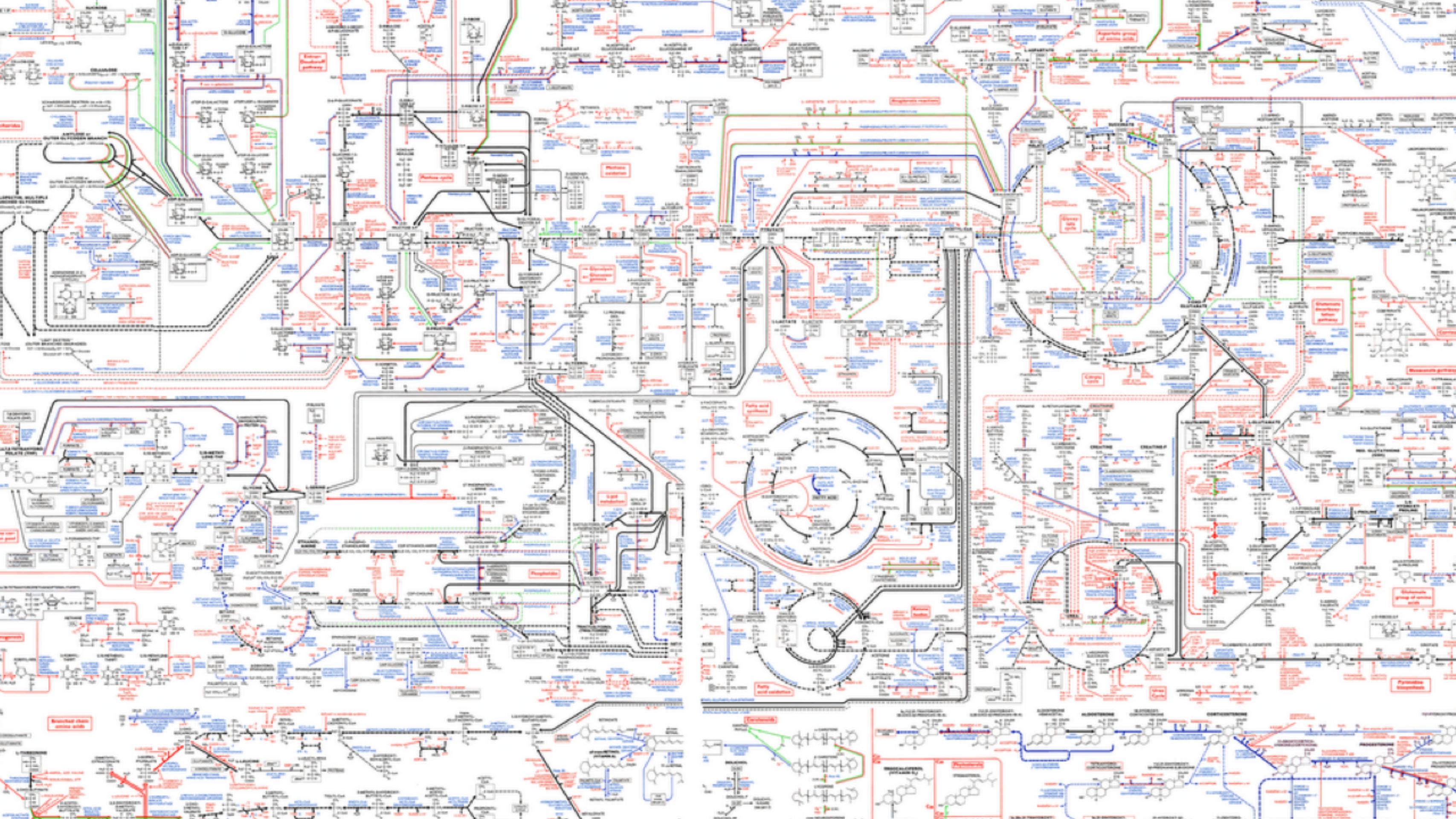


# Applications of networks: biological networks

- interactions between genes, proteins, and chemical products
- the brain: connections between neurons
- your ancestry: the relations between you and your family
- phylogeny: the evolutionary relationships of life



[Beyer 2014]

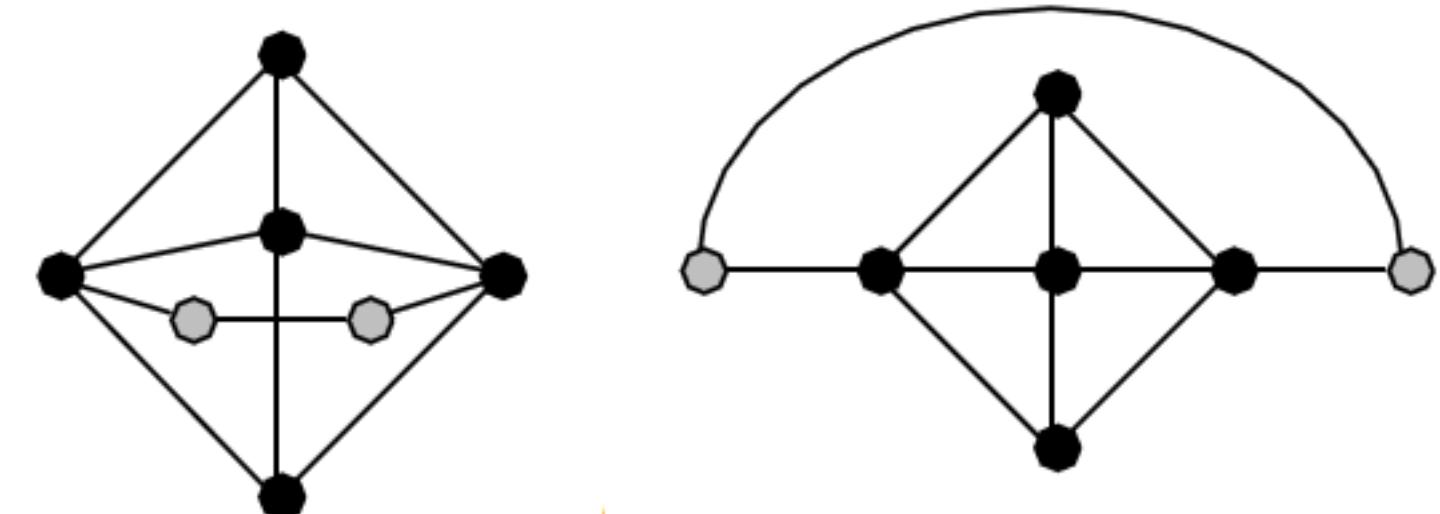
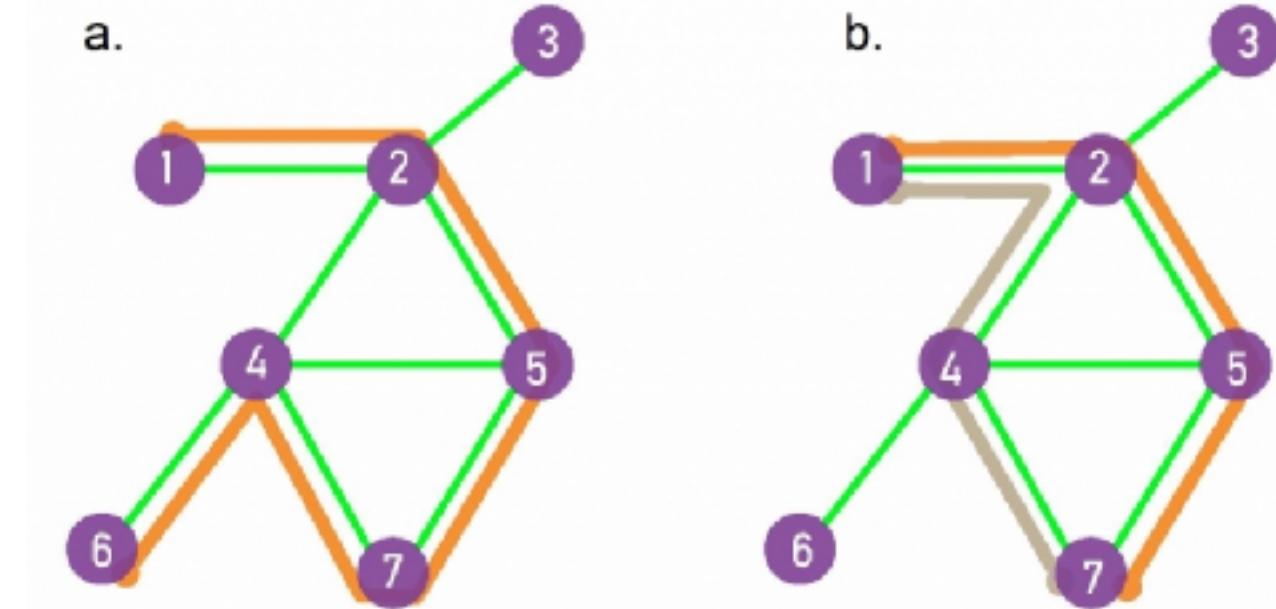


# Exercise: Friend networks, two ways

- Imagine a network of friends
  - you want to visualize if and how often the friends have met each other
  - for each friend you have age, gender, and origin info
- Create two different sketches that visualize this friendship relation
- In Socrative quiz, click on true when done  
[~5 min]

# Network tasks: topology-based

- topological structure of network
  - path following
    - path is route along links
      - hops from one node to another
    - path length is number of links along route
      - shortest path connects nodes i & j with smallest # of hops
- topology vs geometry
  - topological hops different from geometric distance given specific layout
    - topology does not depend on layout
    - geometry does

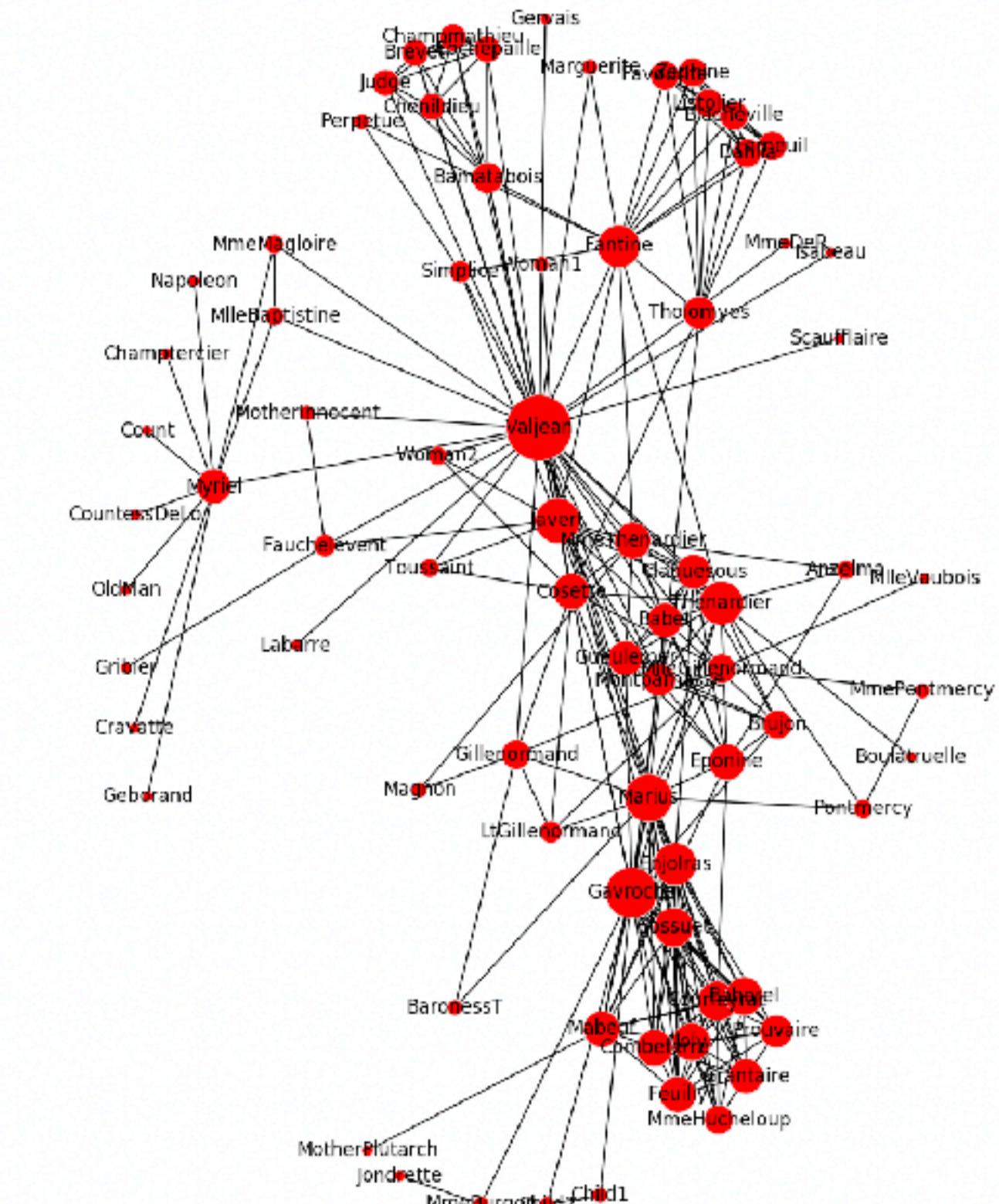
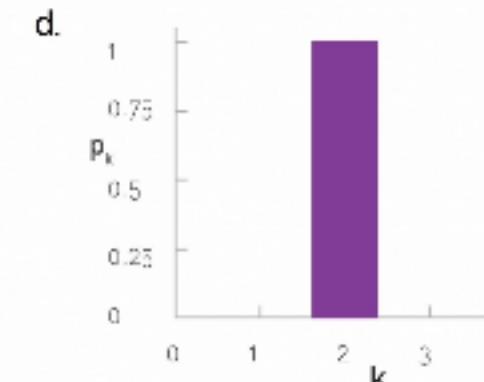
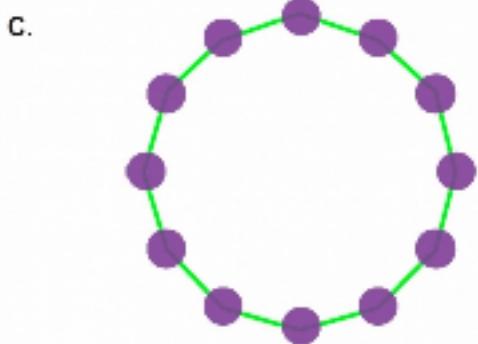
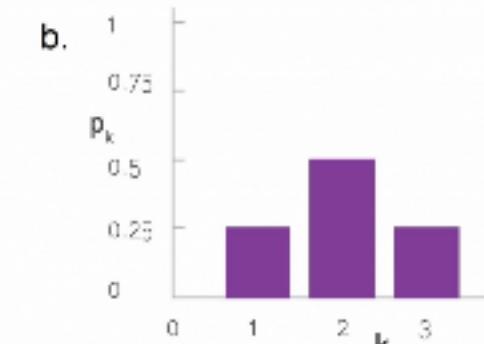
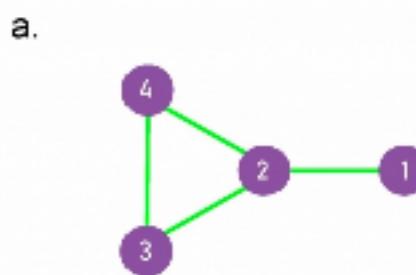


# Network tasks: topology-based

- topological structure of network

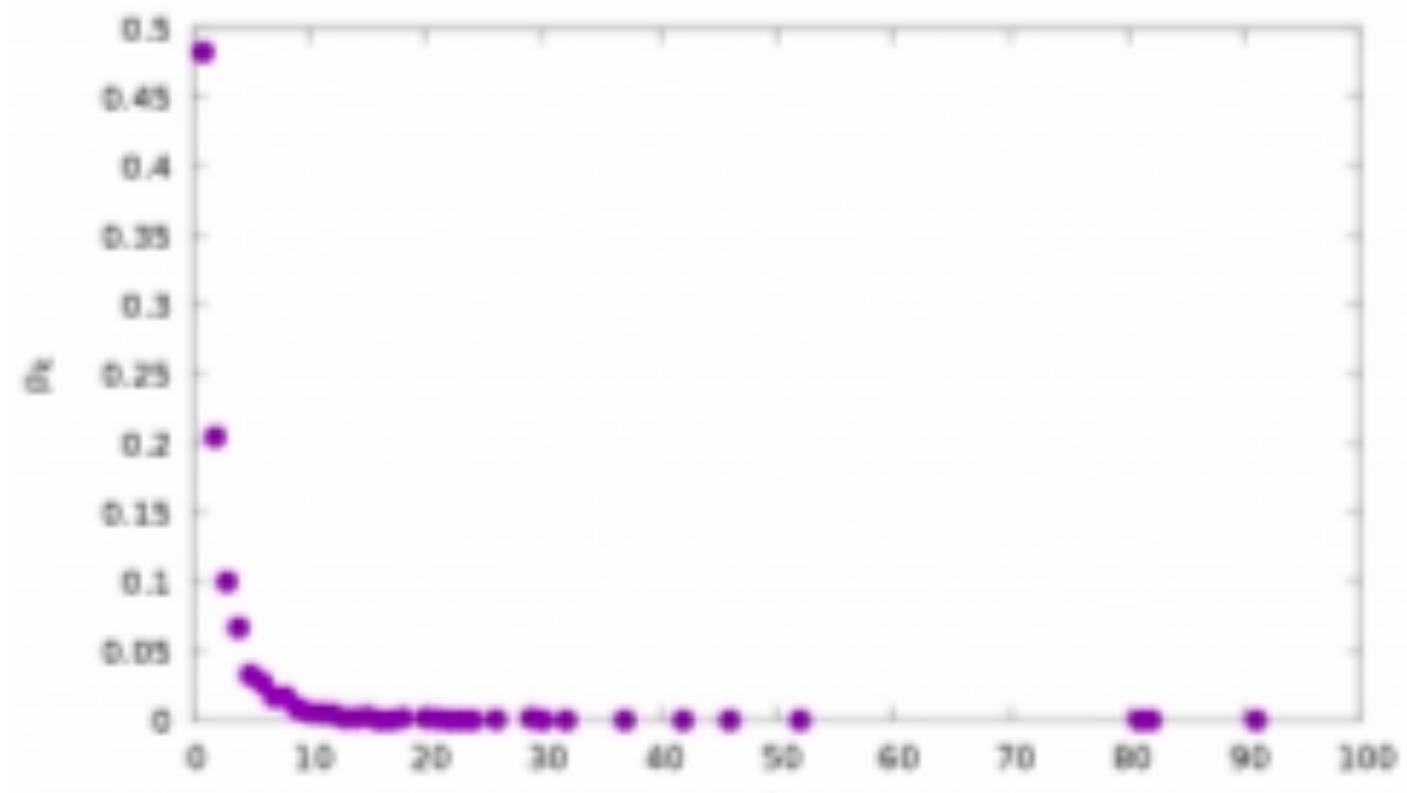
- node importance metrics

- node degree: attribute on nodes
      - number of links connected to a node
      - local measure of importance
      - average degree, degree distribution

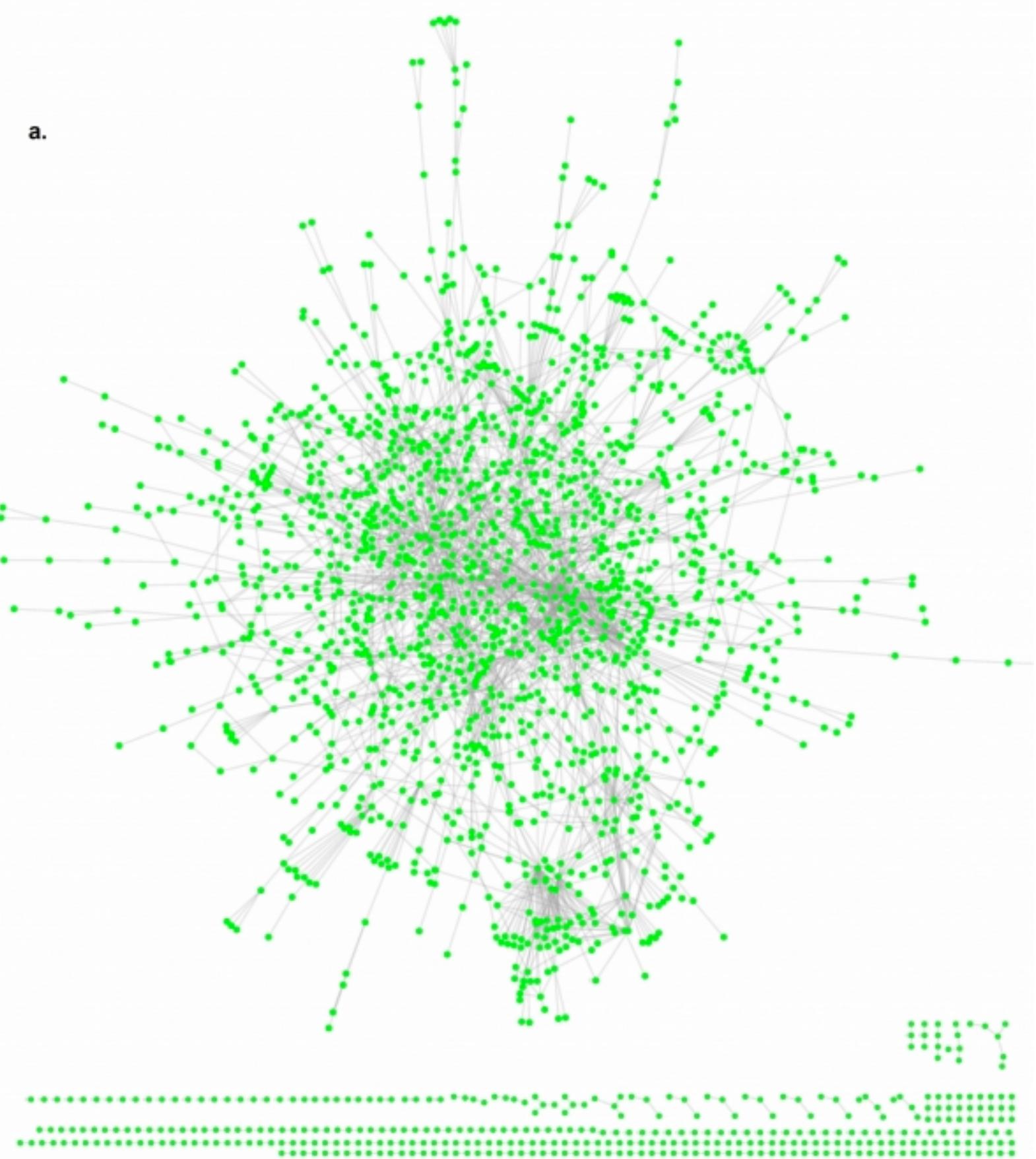


# Degree distribution

- real network
  - power law distributions are common

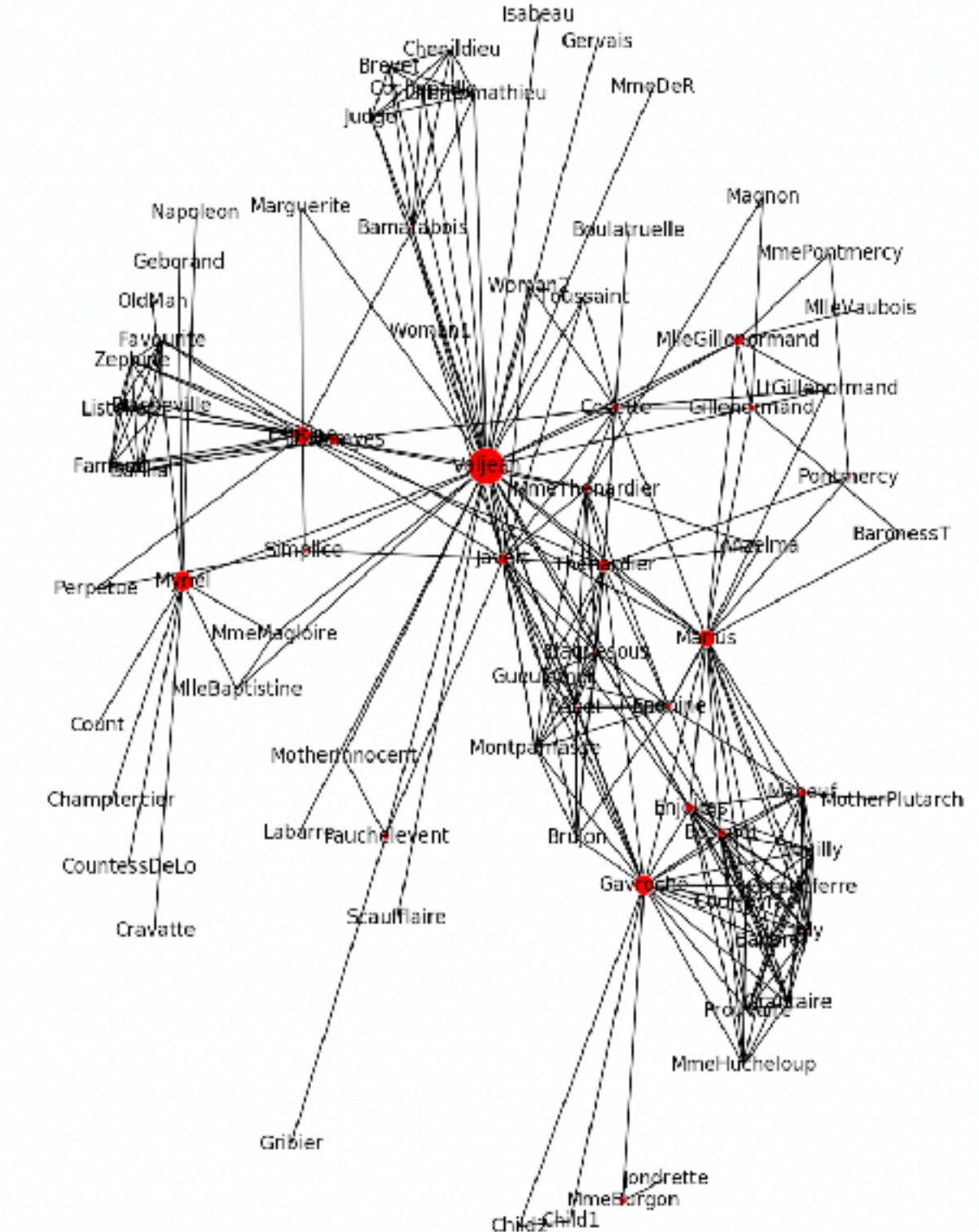


Protein interaction network, Barabasi

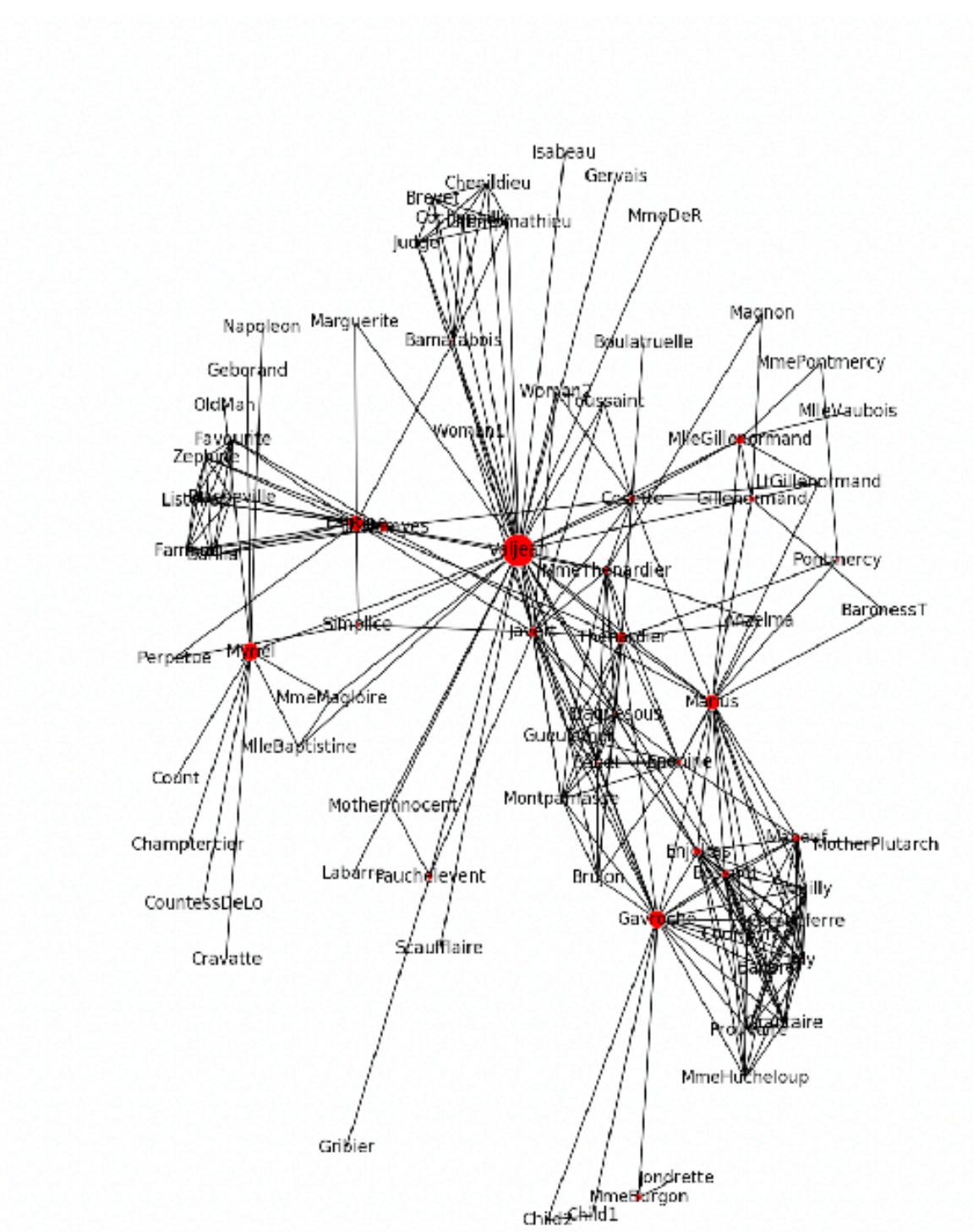
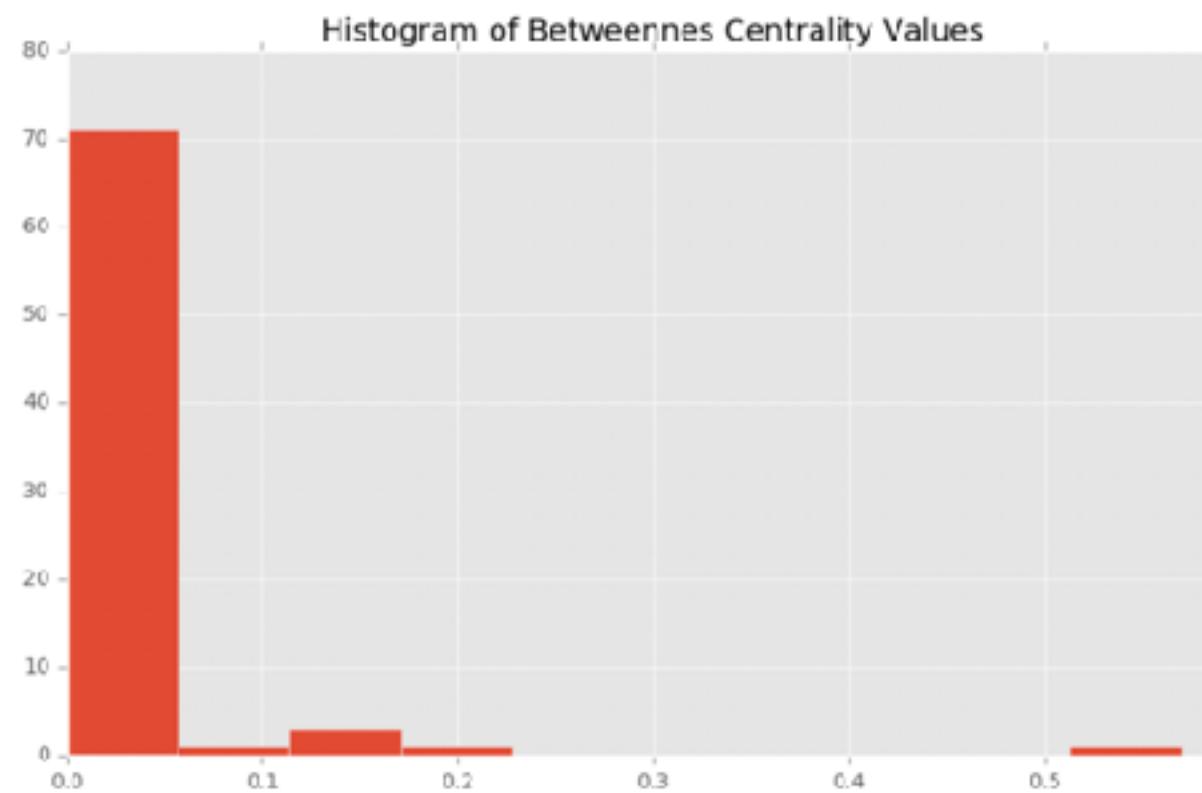
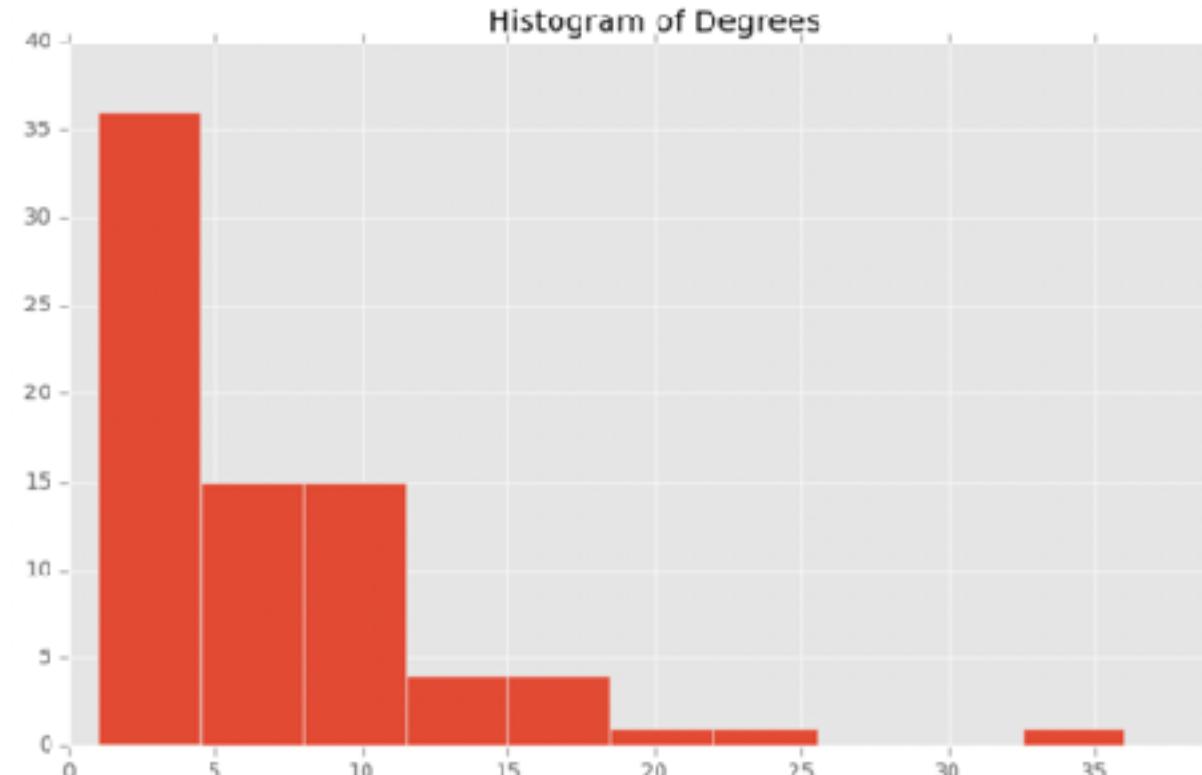


# Network tasks: topology-based

- topological structure of network
  - node importance metrics
    - betweenness centrality: attribute on nodes
      - how many shortest paths pass through a node
      - global measure of importance
      - good measure for overall relevance of node in network

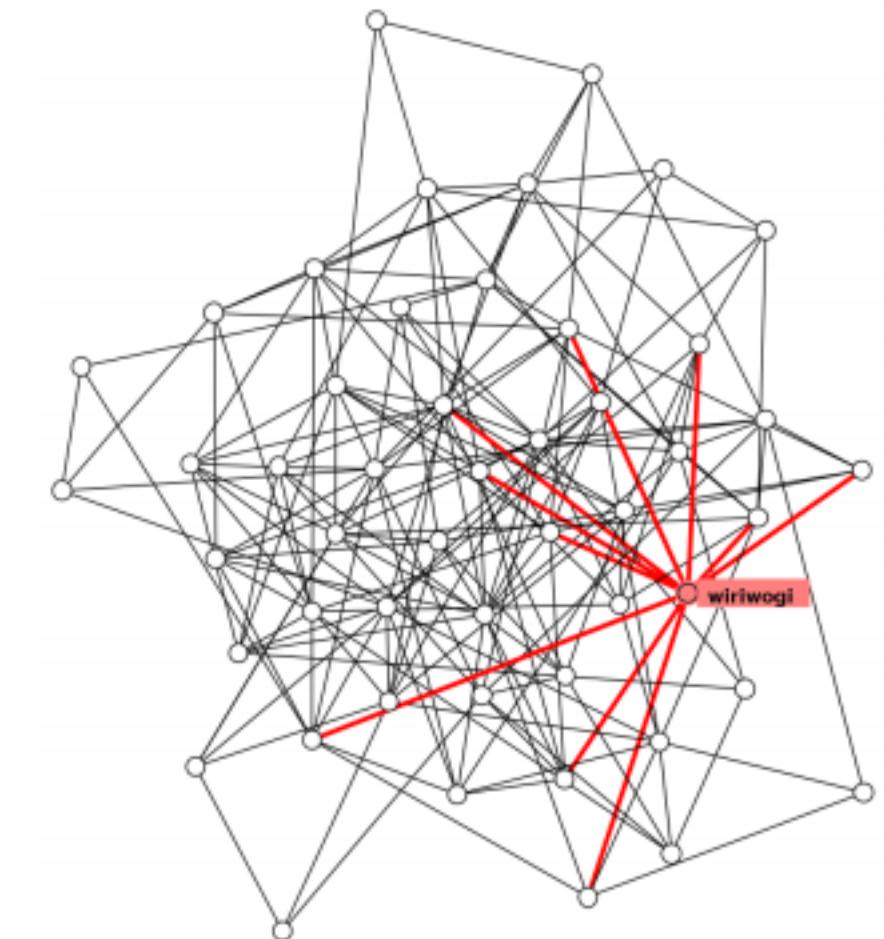


# Centrality measures: Degree vs betweenness centrality



# Network tasks: attribute-based vs topology-based

- topology based tasks
  - find paths
  - find (topological) neighbors
  - compare centrality/importance measures
  - identify clusters / communities
- attribute based tasks (similar to table data)
  - find extreme values, ...
- combination tasks - incorporating both
- example: locate - find single or multiple nodes/links with a given property
  - topology: find all adjacent nodes of given node
  - attributes: find edges with maximum edge weight



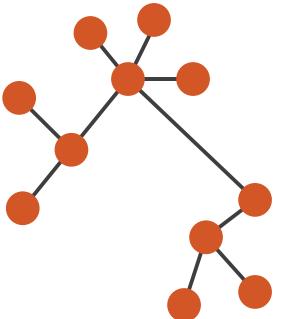
# Three kinds of network visual encodings

## → Node–Link Diagrams

Connection Marks

NETWORKS

TREES



## → Adjacency Matrix

Derived Table

NETWORKS

TREES

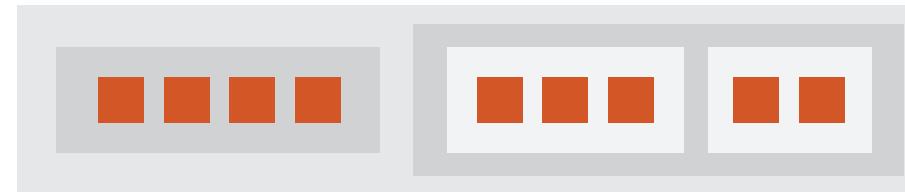
■	■	■	■	■
■	■	■	■	■
■	■	■	■	■
■	■	■	■	■
■	■	■	■	■

## → Enclosure

Containment Marks

NETWORKS

TREES



# Node-link diagrams

- nodes: point marks
- links: line marks
  - straight lines or arcs
  - connections between nodes
- intuitive & familiar
  - most common
  - many, many variants

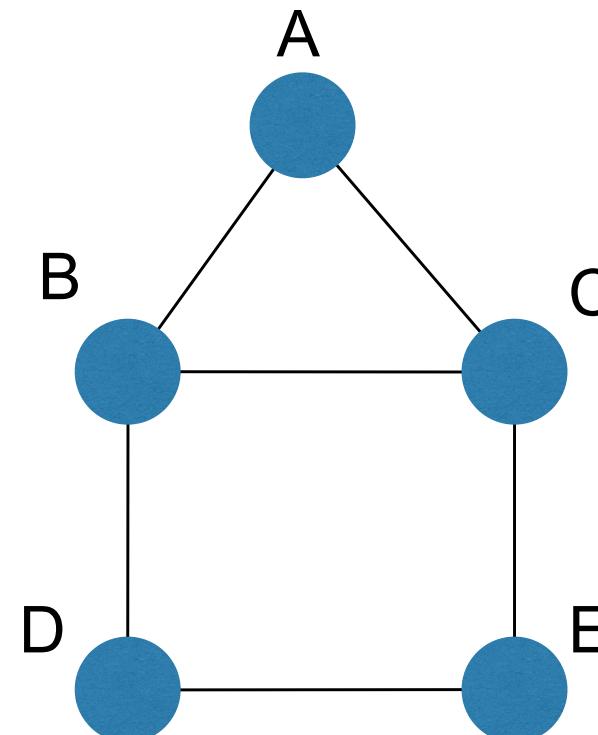
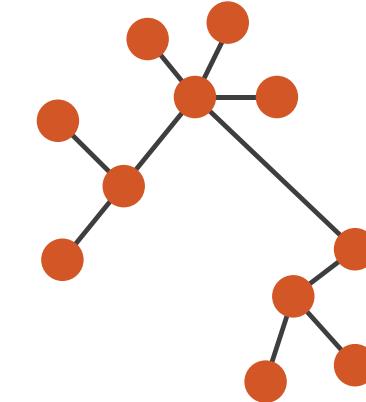


## Node-Link Diagrams

Connection Marks

NETWORKS

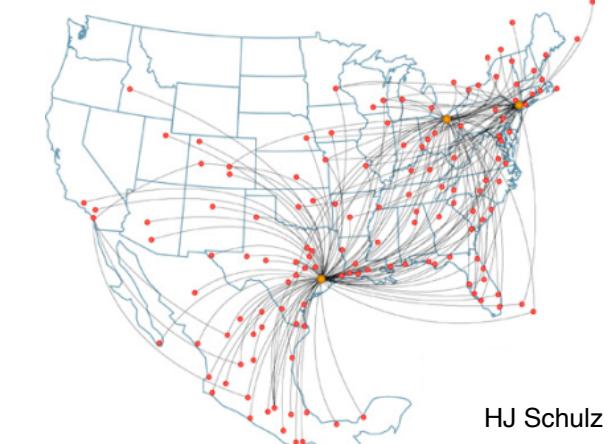
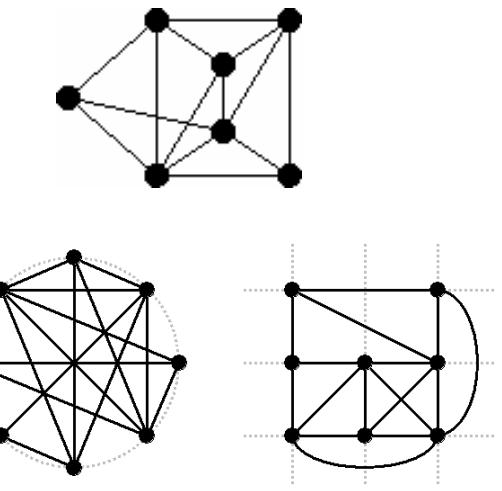
TREES



Free

Styled

Fixed



HJ Schulz 2006

## Exercise

- sketch an aesthetically pleasing node-link diagram of this network
  - there are five nodes: A, B, C, D, E
  - each row in the table describes an edge

A B

C D

C B

A D

A C

B D

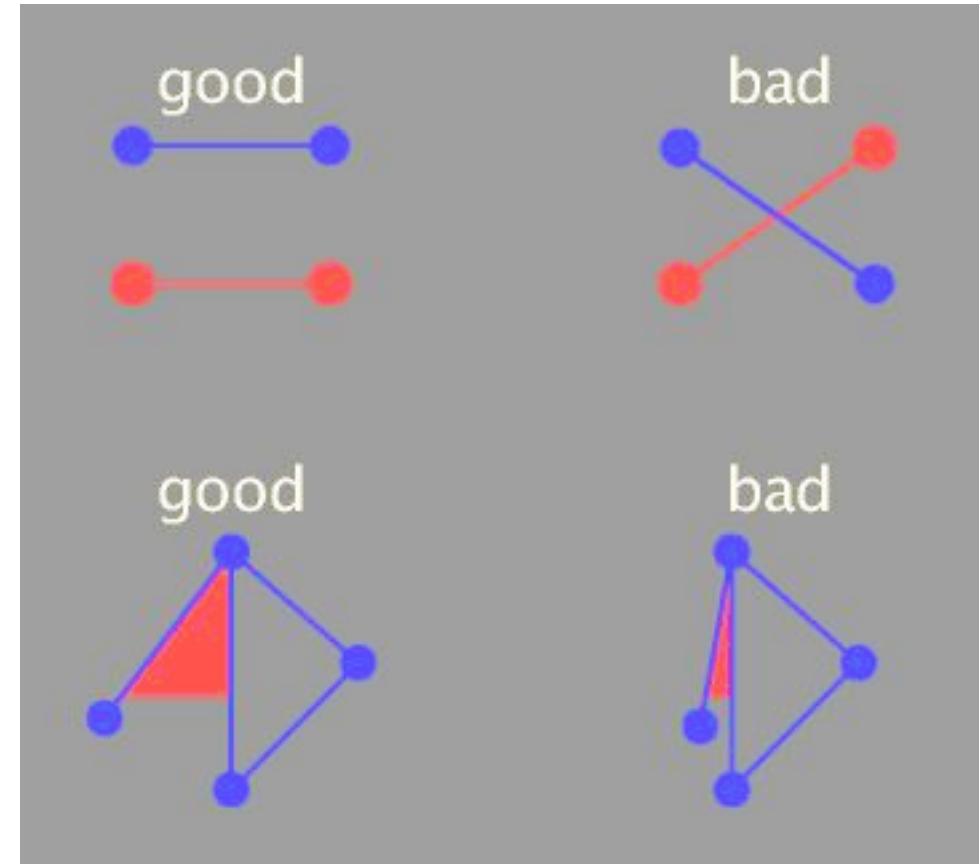
D E

A E

- Socrative quiz: pick true when done [~5 min]

# Criteria for good node-link layouts

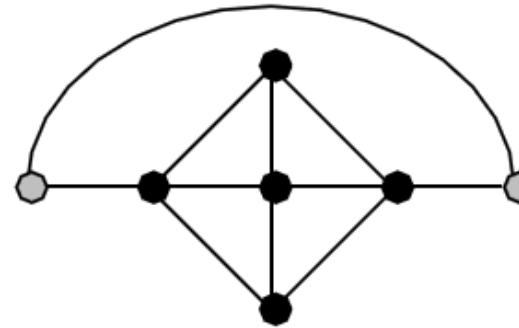
- minimize
  - edge crossings
  - distances between topological neighbor nodes
  - total drawing area
  - edge bends
  - edge length disparities (sometimes)
- maximize
  - angular distance between different edges
  - aspect ratio disparities
- emphasize symmetry
  - similar graph structures should look similar in layout



# Criteria conflict

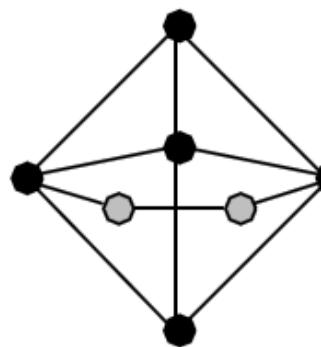
- most criteria NP-hard individually
- many criteria directly conflict with each other

Minimum number  
of edge crossings

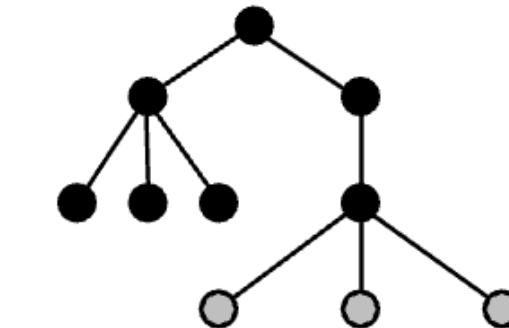


vs.

Uniform edge  
length

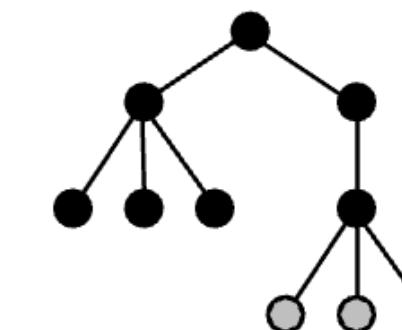


Space utilization



vs.

Symmetry

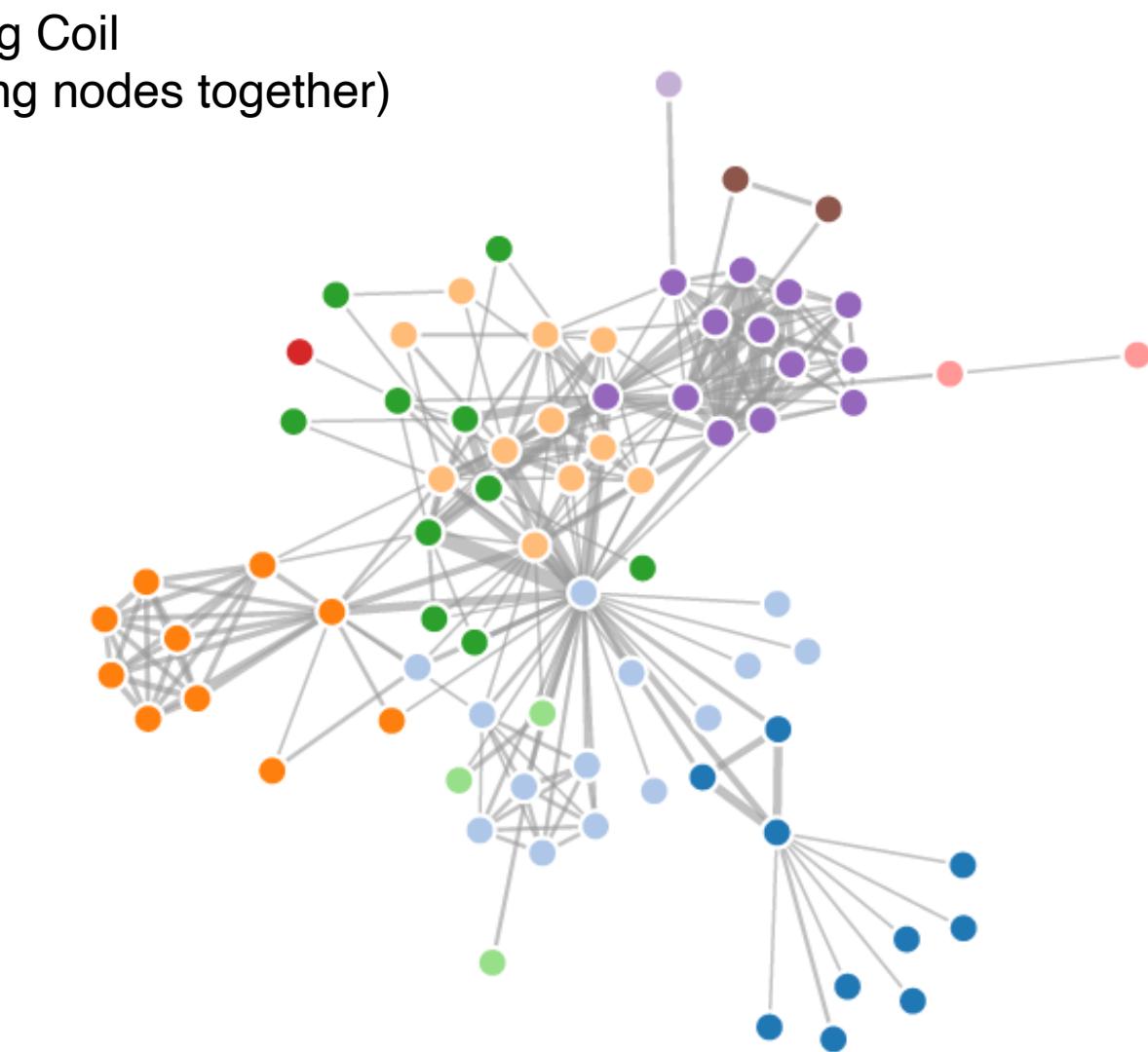
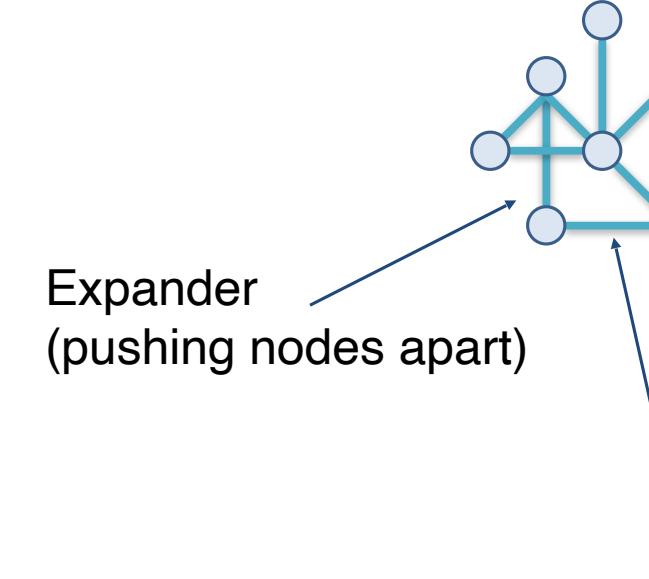


# Optimization-based layouts

- formulate layout problem as optimization problem
- convert criteria into weighted cost function
  - $F(\text{layout}) = a * [\text{crossing counts}] + b * [\text{drawing space used}] + \dots$
- use known optimization techniques to find layout at minimal cost
  - energy-based physics models
  - force-directed placement
  - spring embedders

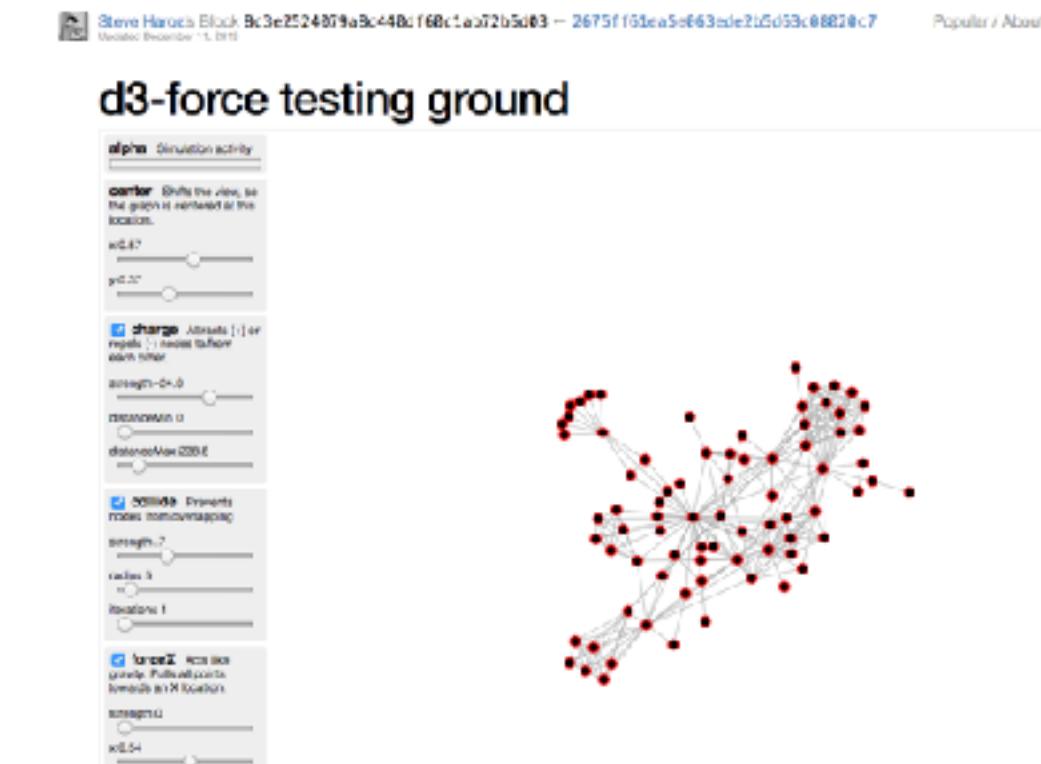
# Force-directed placement

- physics model
  - links = springs pull together
  - nodes = magnets repulse apart
- algorithm
  - place vertices in random locations
  - while not equilibrium
    - calculate force on vertex
      - sum of
        - » pairwise repulsion of all nodes
        - » attraction between connected nodes
    - move vertex by  $c * \text{vertex\_force}$



# Force-directed placement properties

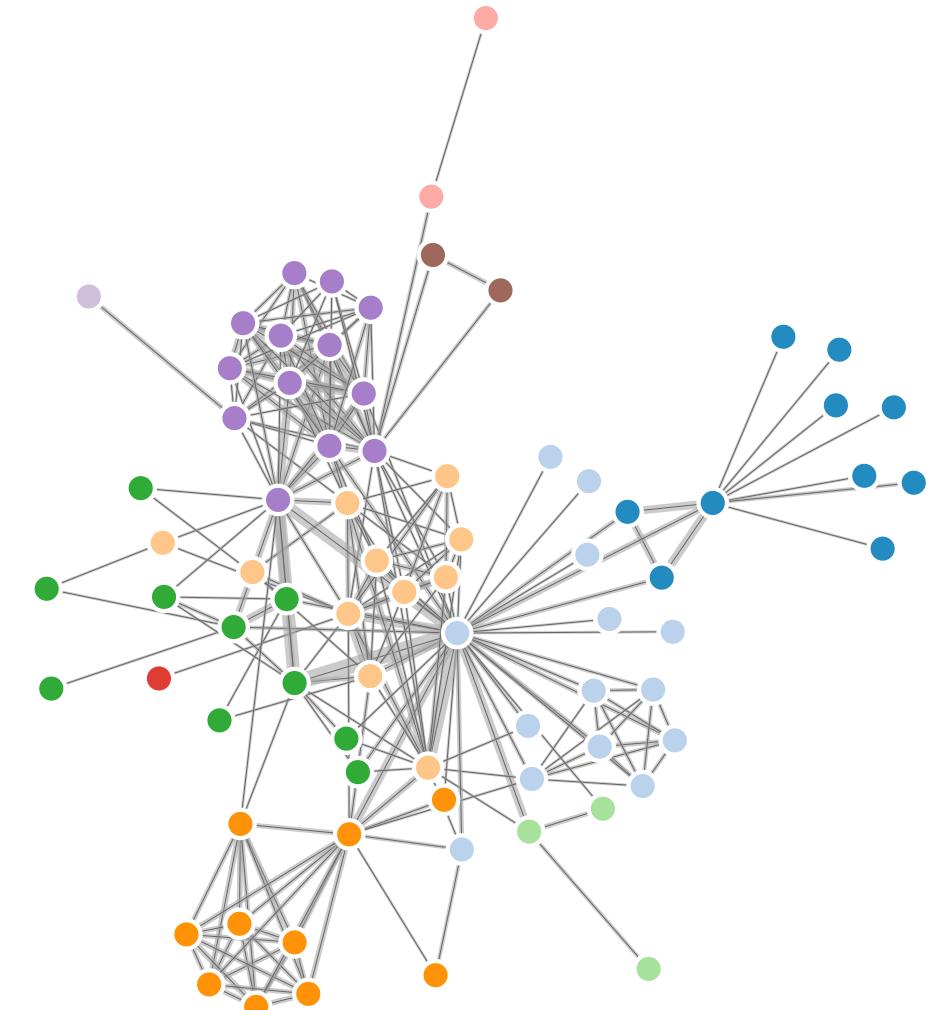
- strengths
  - reasonable layout for small, sparse graphs
  - clusters typically visible
  - edge length uniformity
- weaknesses
  - nondeterministic
  - computationally expensive:  $O(n^3)$  for  $n$  nodes
    - each step is  $n^2$ , takes  $\sim n$  cycles to reach equilibrium
  - naive FD doesn't scale well beyond 1K nodes
  - iterative progress: engaging but distracting



<https://bl.ocks.org/steveharoz/8c3e2524079a8c440df60c1ab72b5d03>

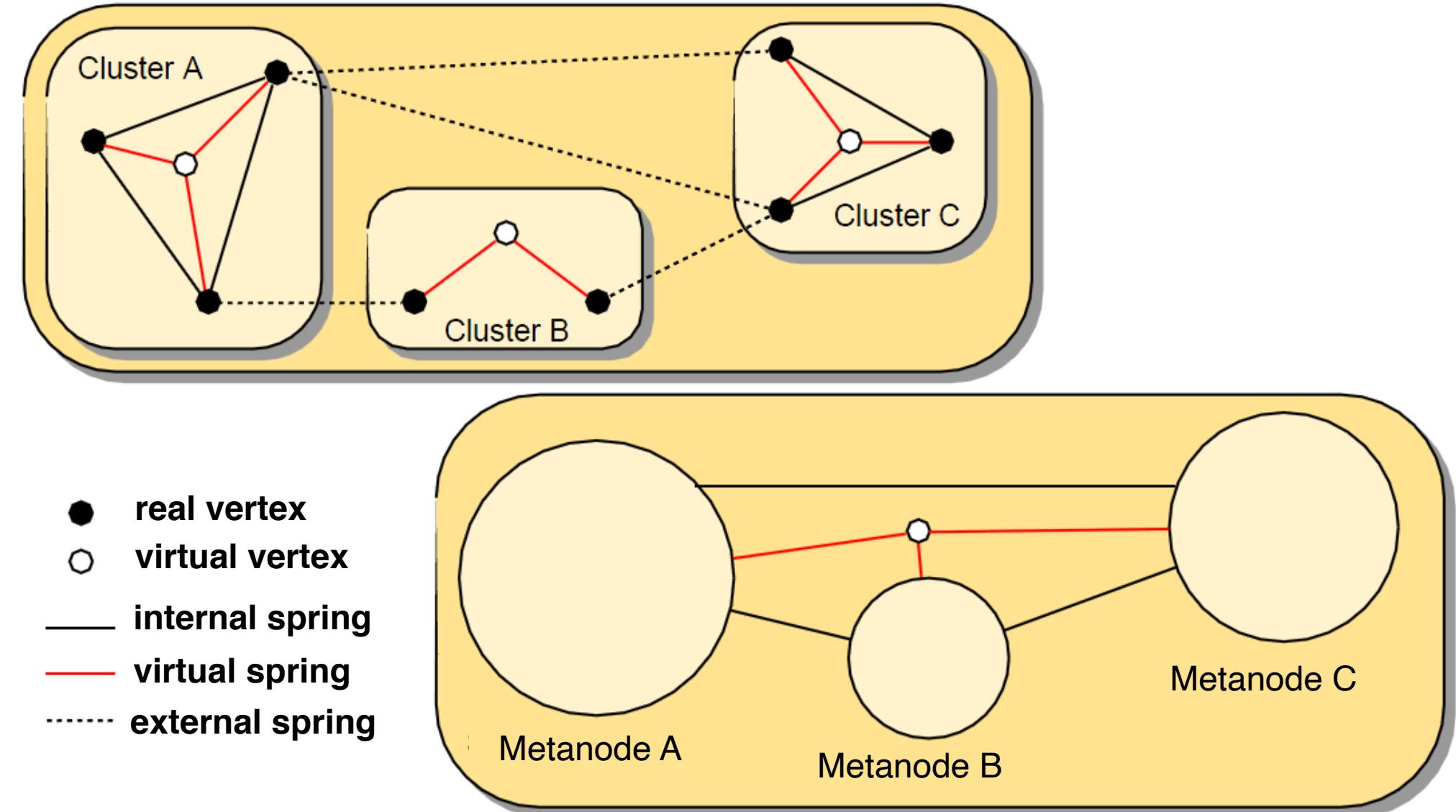
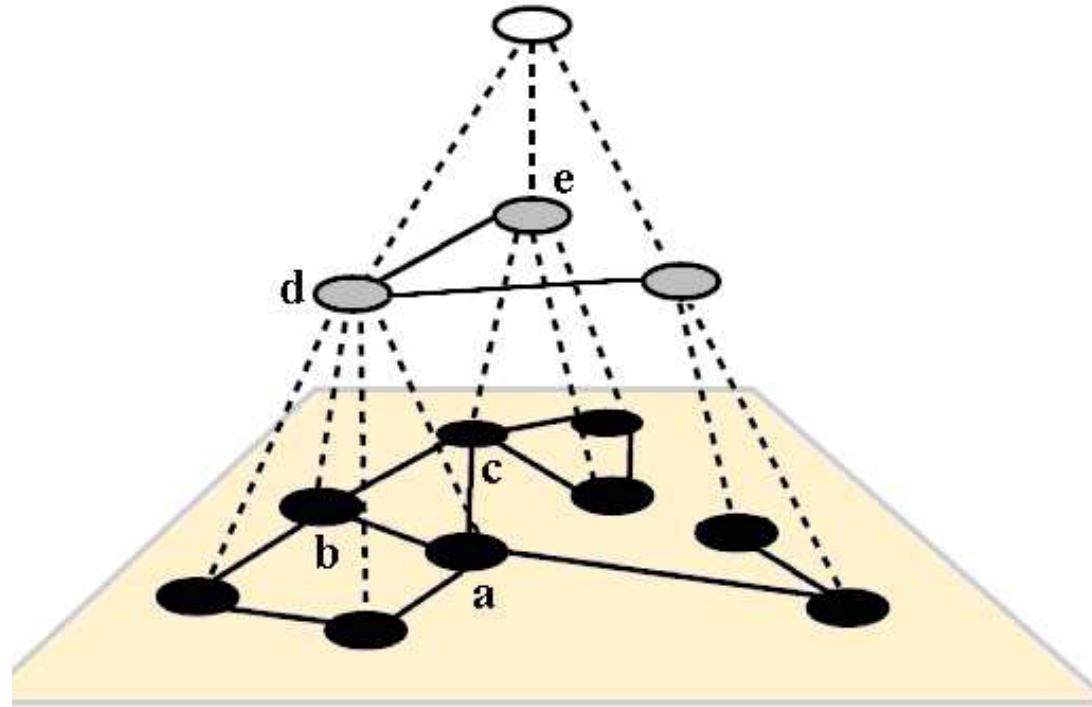
# Idiom: force-directed placement

- visual encoding
  - link connection marks, node point marks
- considerations
  - spatial position: no meaning directly encoded
    - left free to minimize crossings
  - proximity semantics?
    - sometimes meaningful
    - sometimes arbitrary, artifact of layout algorithm
    - tension with length
      - long edges more visually salient than short
- tasks
  - explore topology; locate paths, clusters
- scalability
  - node/edge density  $E < 4N$



# Multilevel approaches

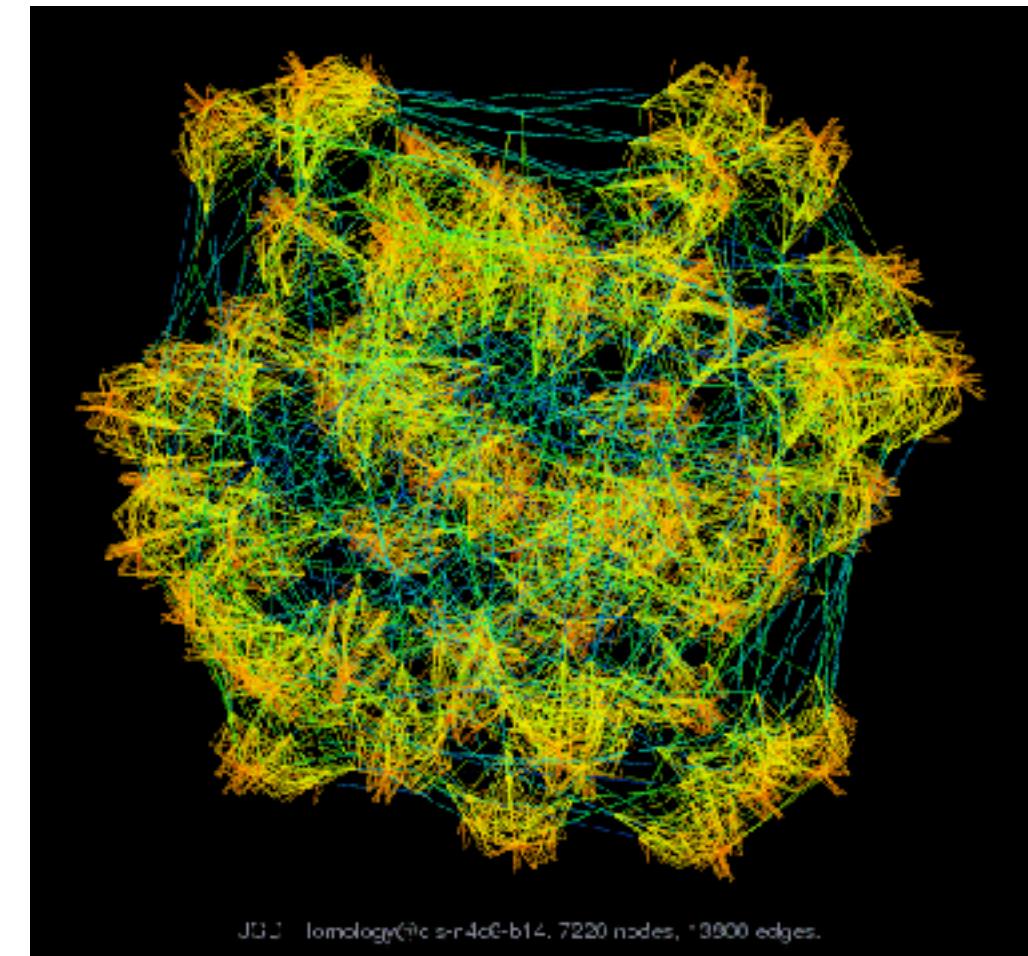
- derive cluster hierarchy of metanodes on top of original graph nodes



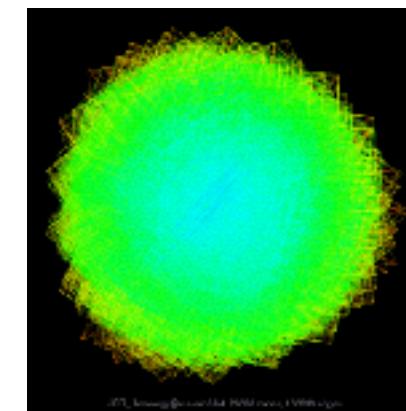
[Schulz 2004]

# Idiom: **sfdp** (multi-level force-directed placement)

- data
  - original: network
  - derived: cluster hierarchy atop it
- considerations
  - better algorithm for same encoding technique
    - same: fundamental use of space
    - hierarchy used for algorithm speed/quality but not shown explicitly
- scalability
  - nodes, edges: 1K-10K
  - hairball problem eventually hits

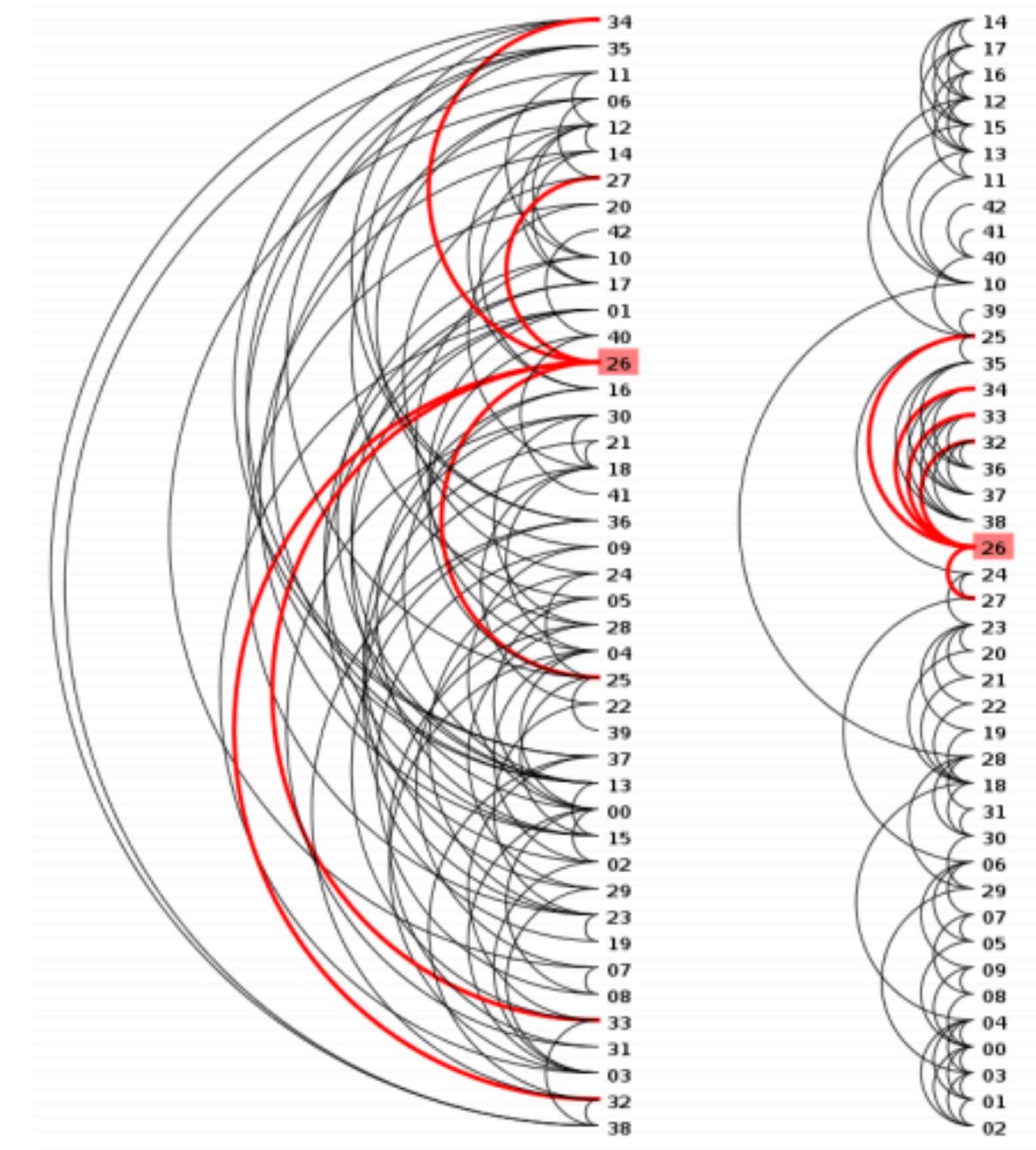
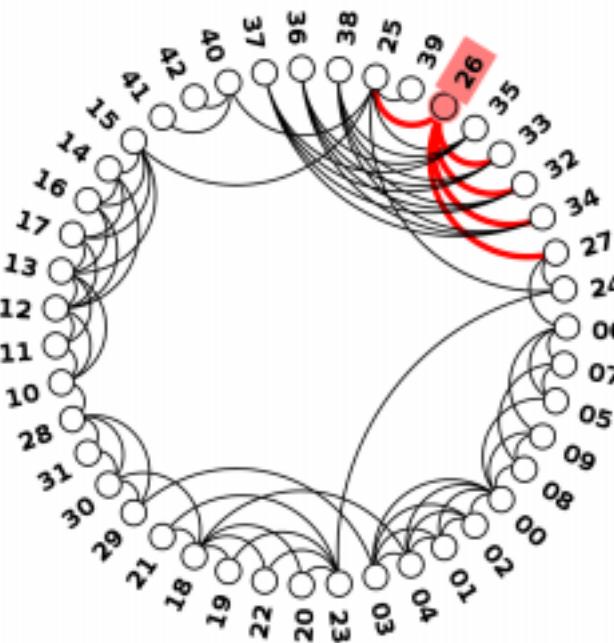
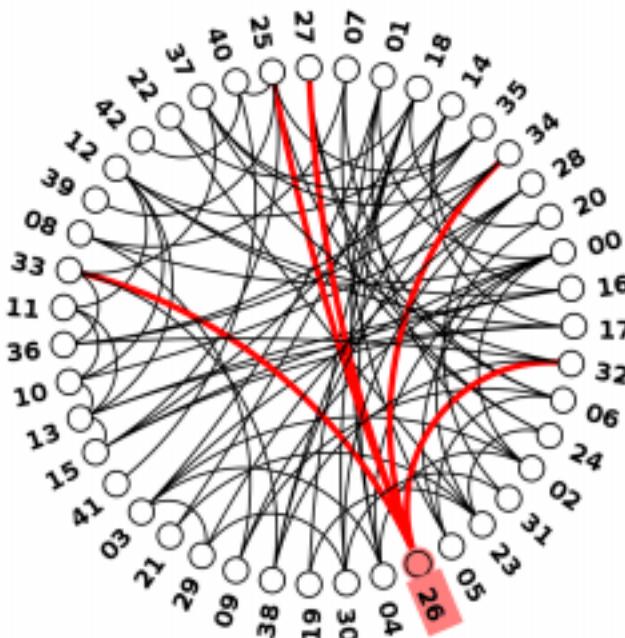


[Efficient and high quality force-directed graph drawing.  
Hu. *The Mathematica Journal* 10:37–71, 2005.]

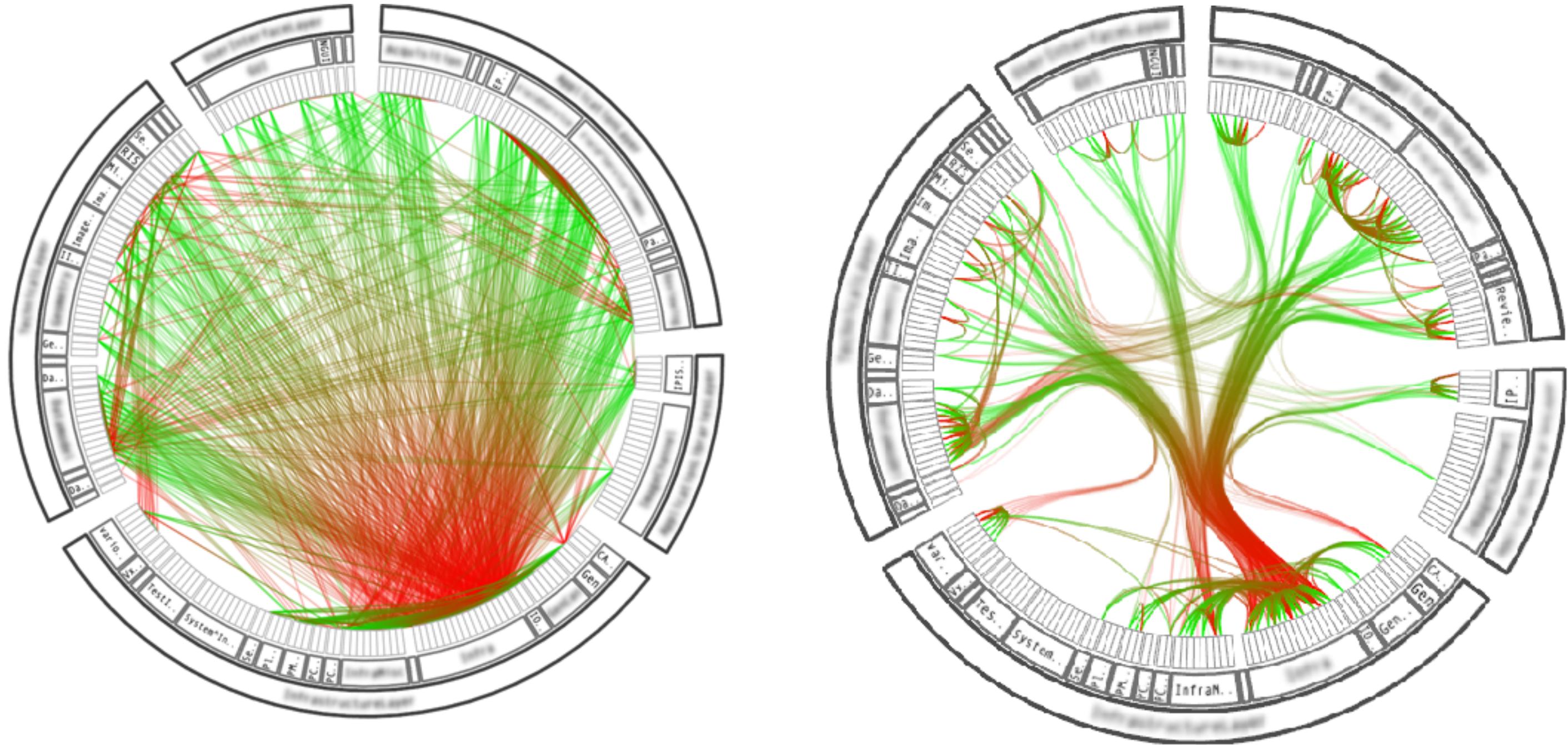


# Restricted layouts: Circular, arc

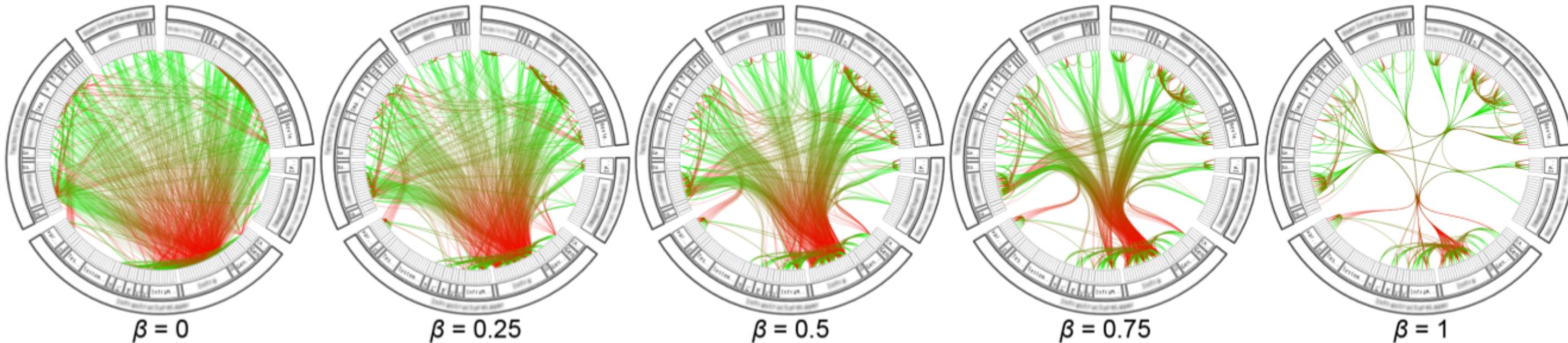
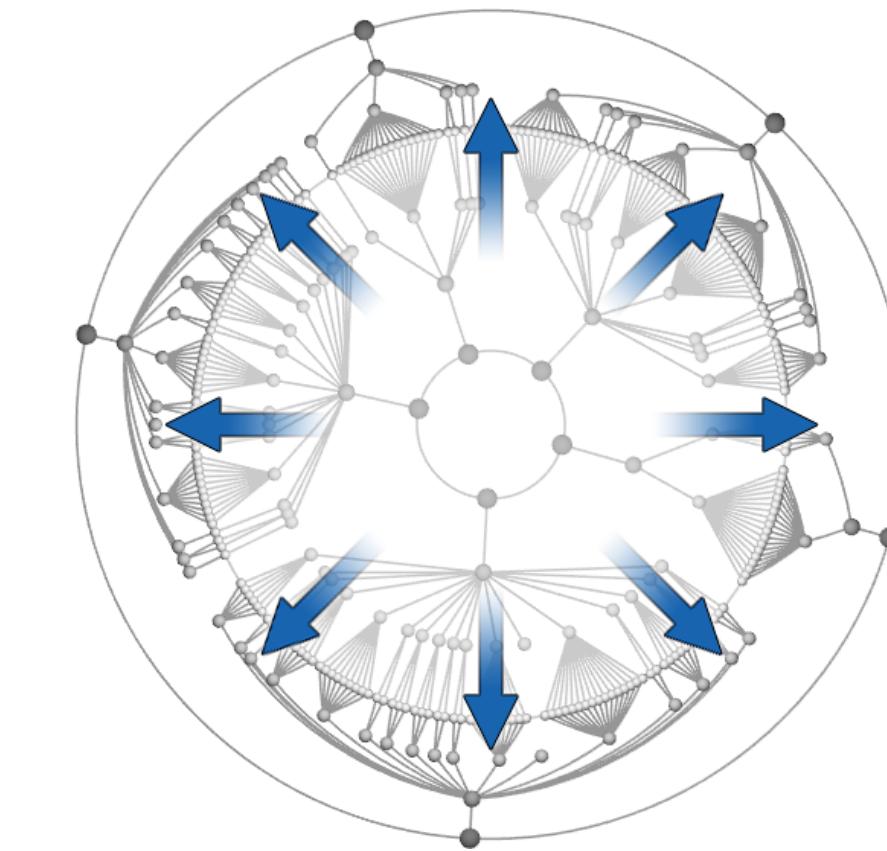
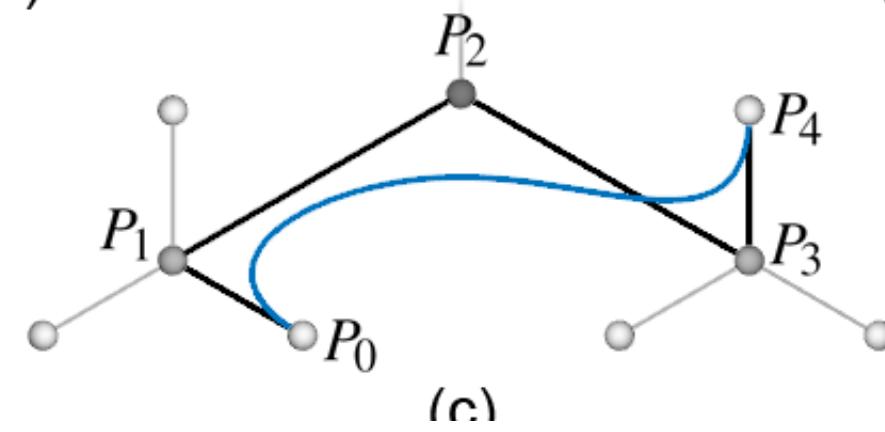
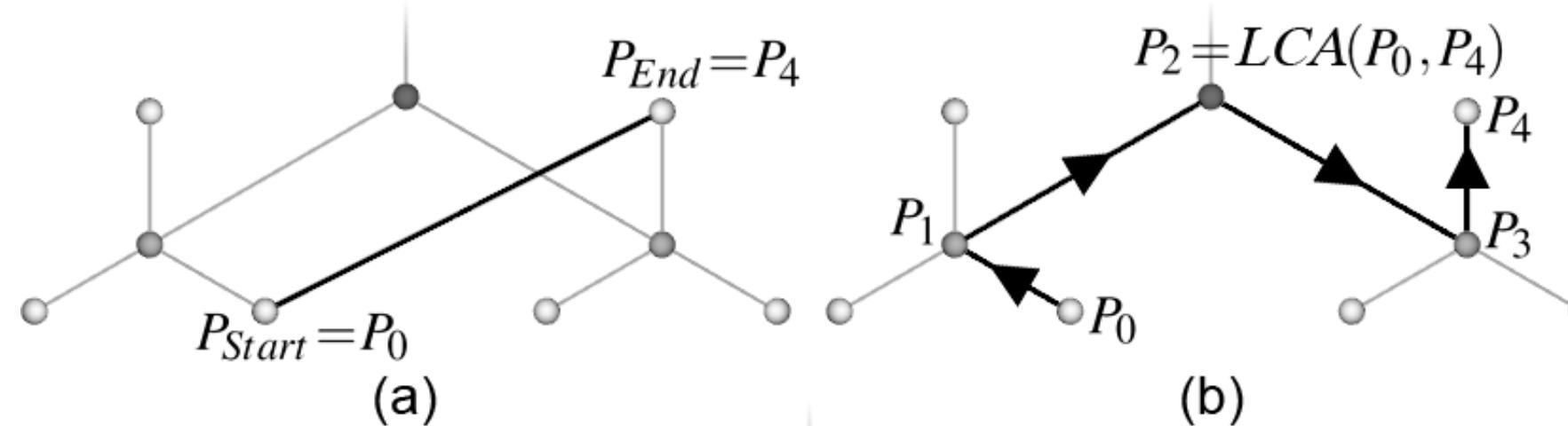
- lay out nodes around circle or along line
  - circular layouts
  - arc diagrams
- node ordering crucial to avoid excessive clutter from edge crossings
  - barycentric ordering before & after
  - derived attribute: global computation



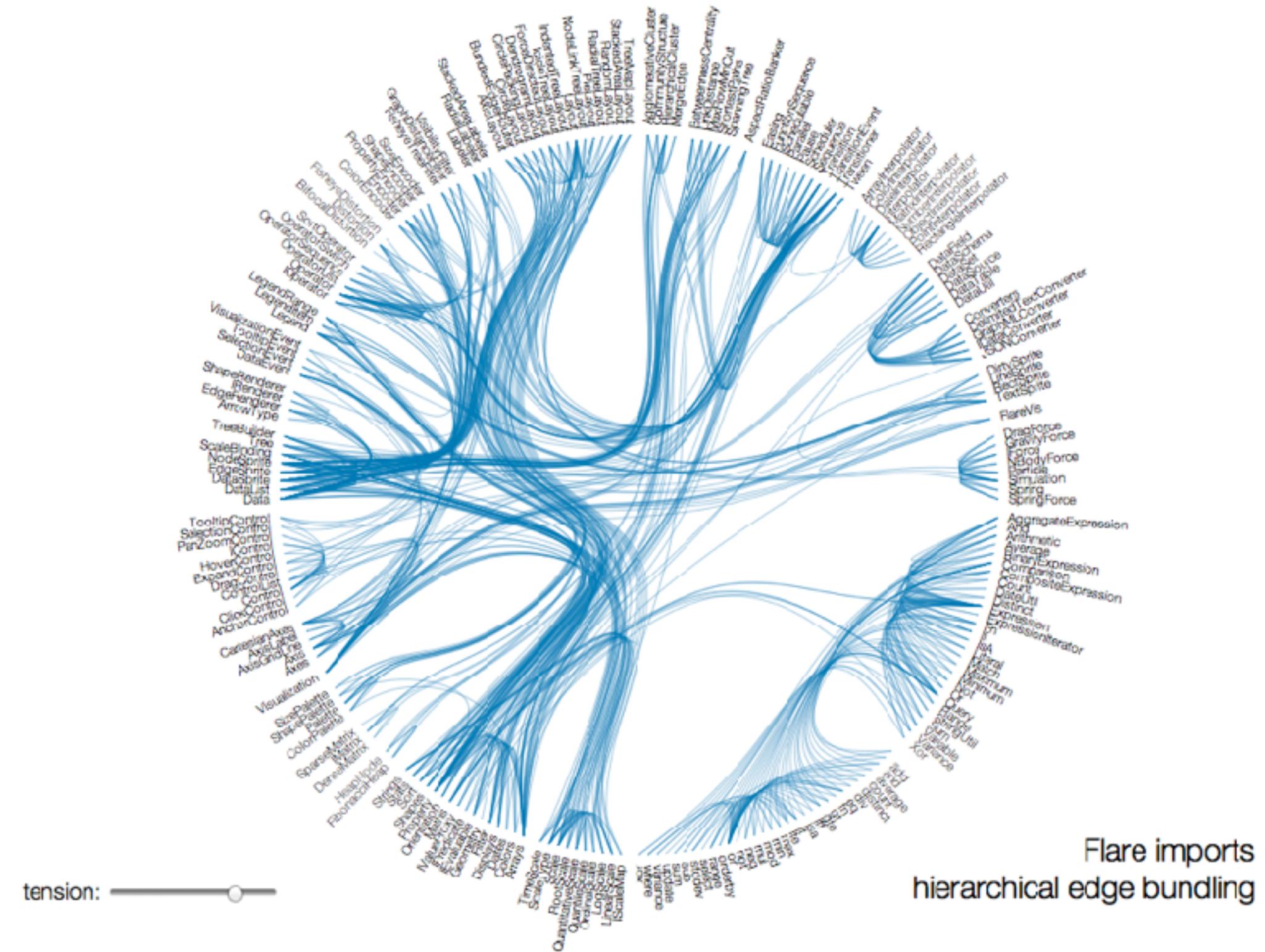
# Edge clutter reduction: hierarchical edge bundling



# Hierarchical edge bundling



# Bundle strength



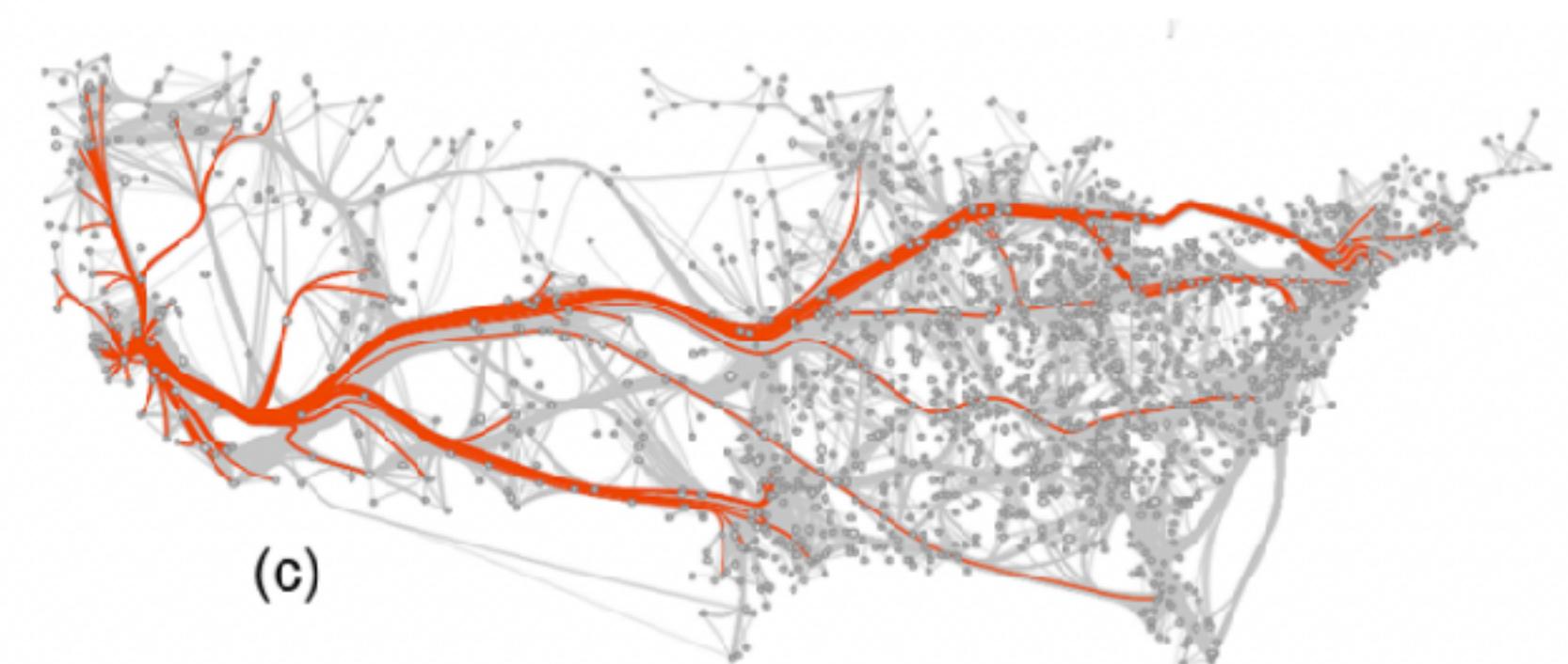
<http://mbostock.github.io/d3/talk/20111116/bundle.html>

# Fixed layouts: Geographic

- lay out network nodes using given/fixed spatial data
  - route edges accordingly
  - edge bundling also applicable

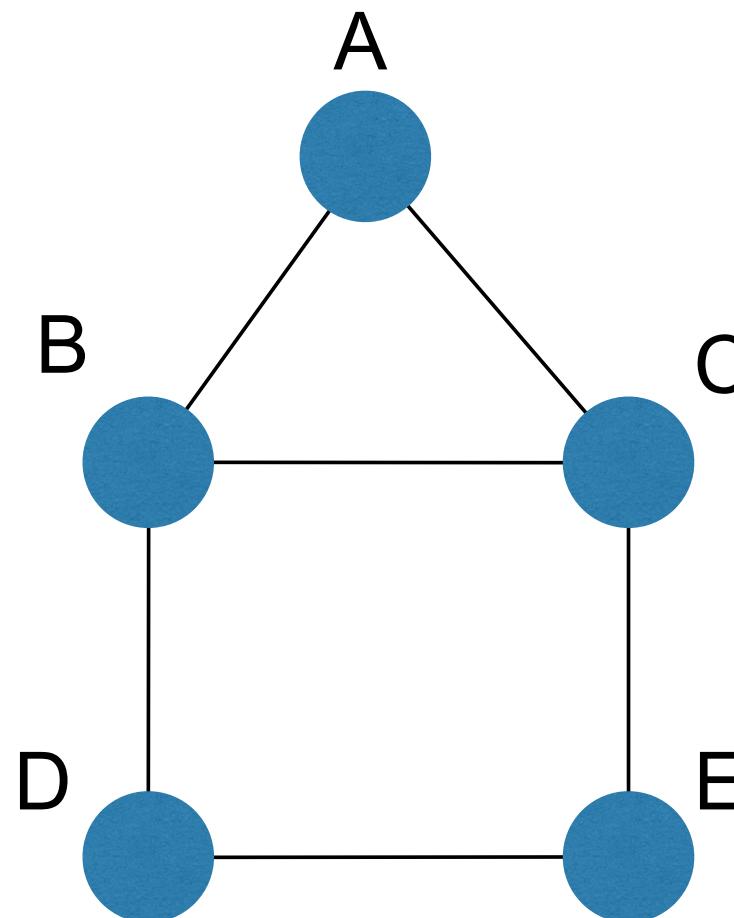


<https://www.facebook.com/notes/facebook-engineering/visualizing-friendships/469716398919>



# Adjacency matrix representations

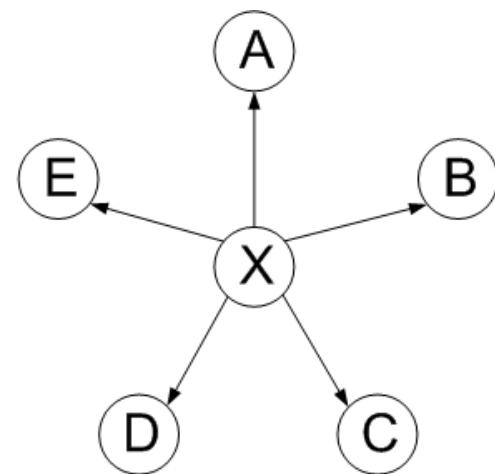
- derive adjacency matrix from network



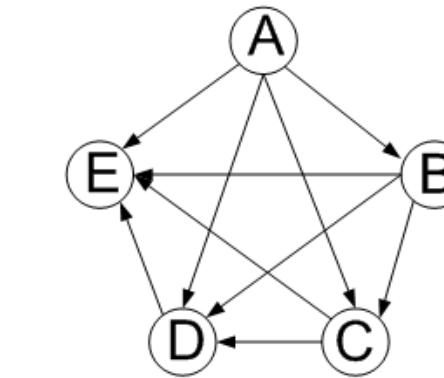
A	B	C	D	E
A				
B				
C				
D				
E				

# Adjacency matrix examples

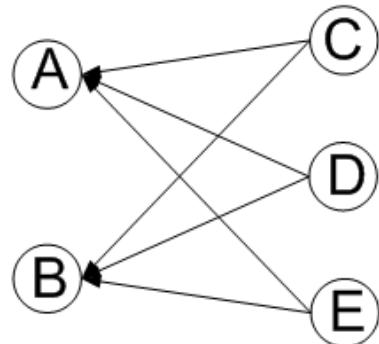
A					
D					
C					
B					
E					
...	X	Y	Z	...	



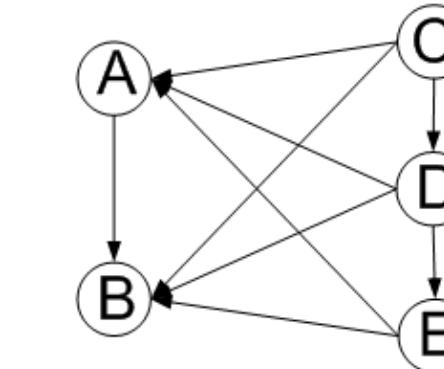
A					
B					
C					
D					
E					
...	A	B	C	D	E



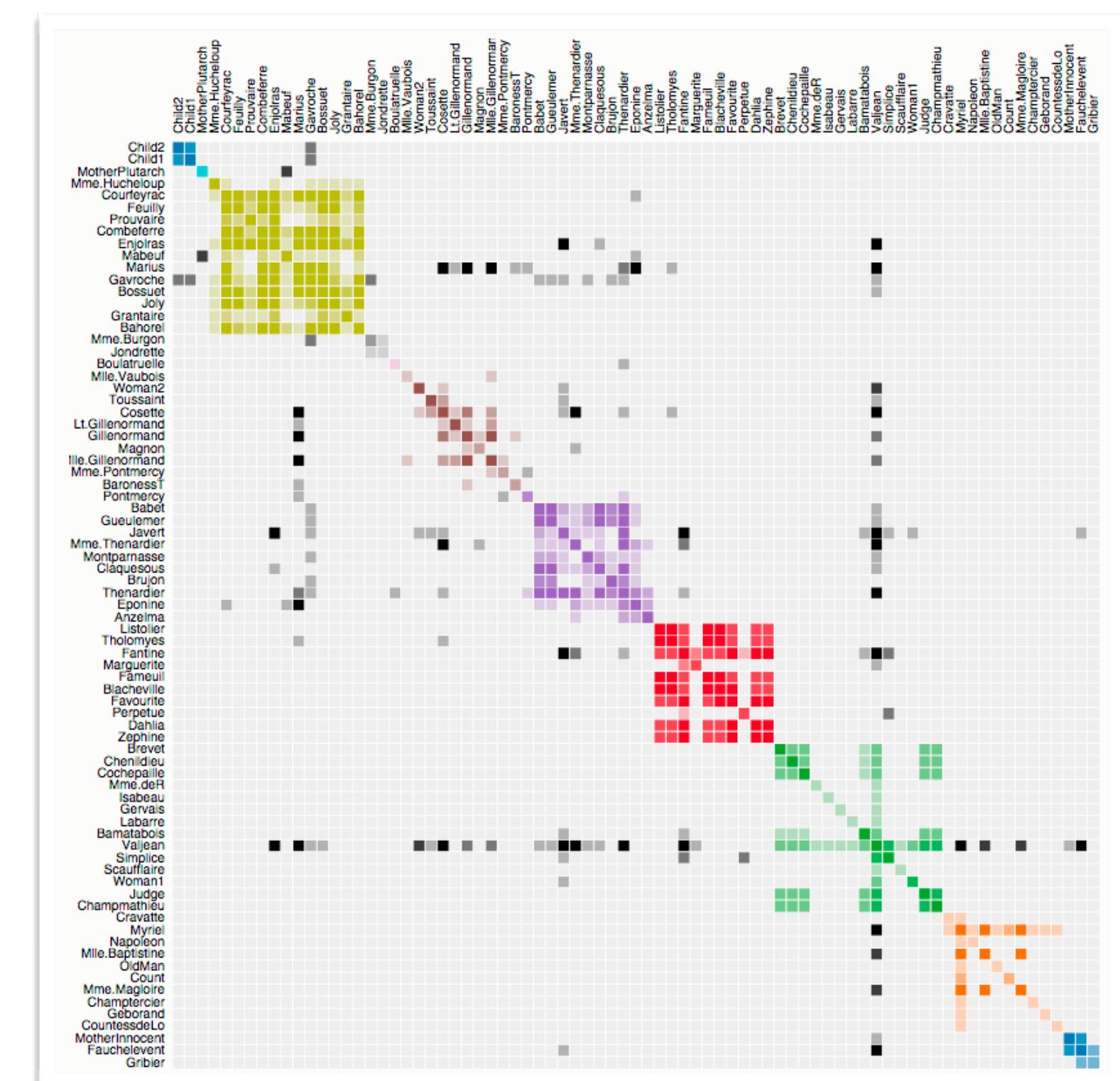
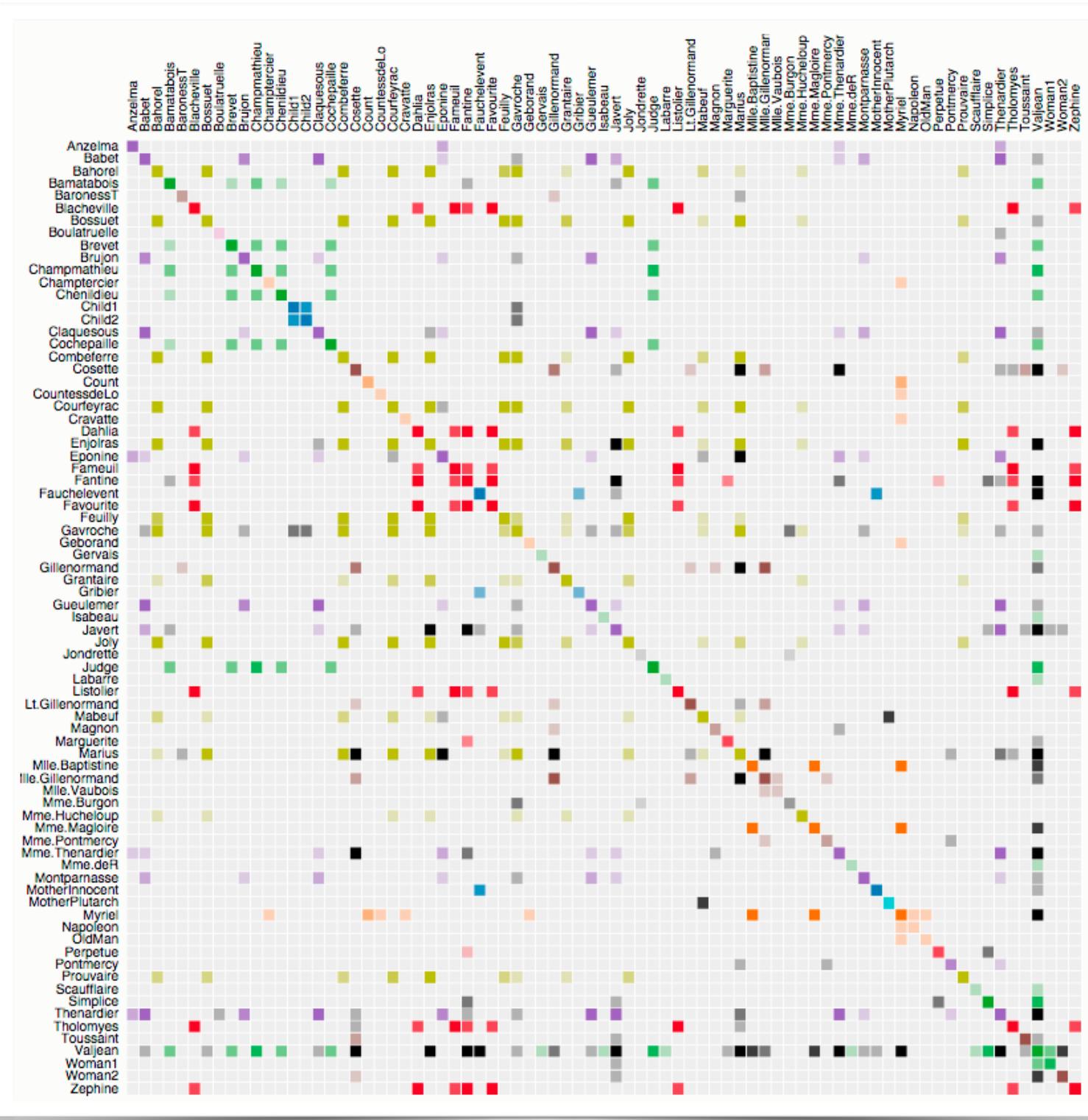
A					
B					
C					
D					
E					
...	A	B	C	D	E



A					
B					
C					
D					
E					
...	A	B	C	D	E



# Node order is crucial: Reordering

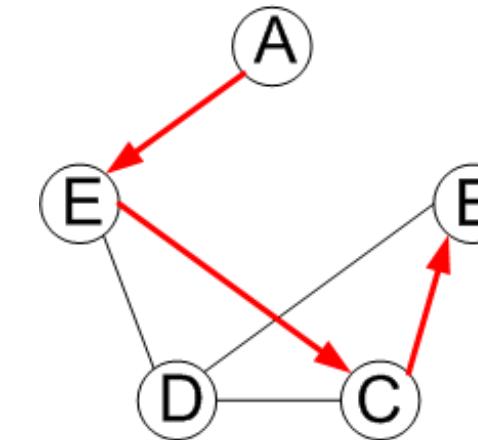


<https://bostocks.org/mike/miserables/>

# Adjacency matrix

	A	B	C	D	E	F	G	H
A								
B								
C								
D								
E								
F								
R								
O								
M								
E								
D								
C								
B								
A								

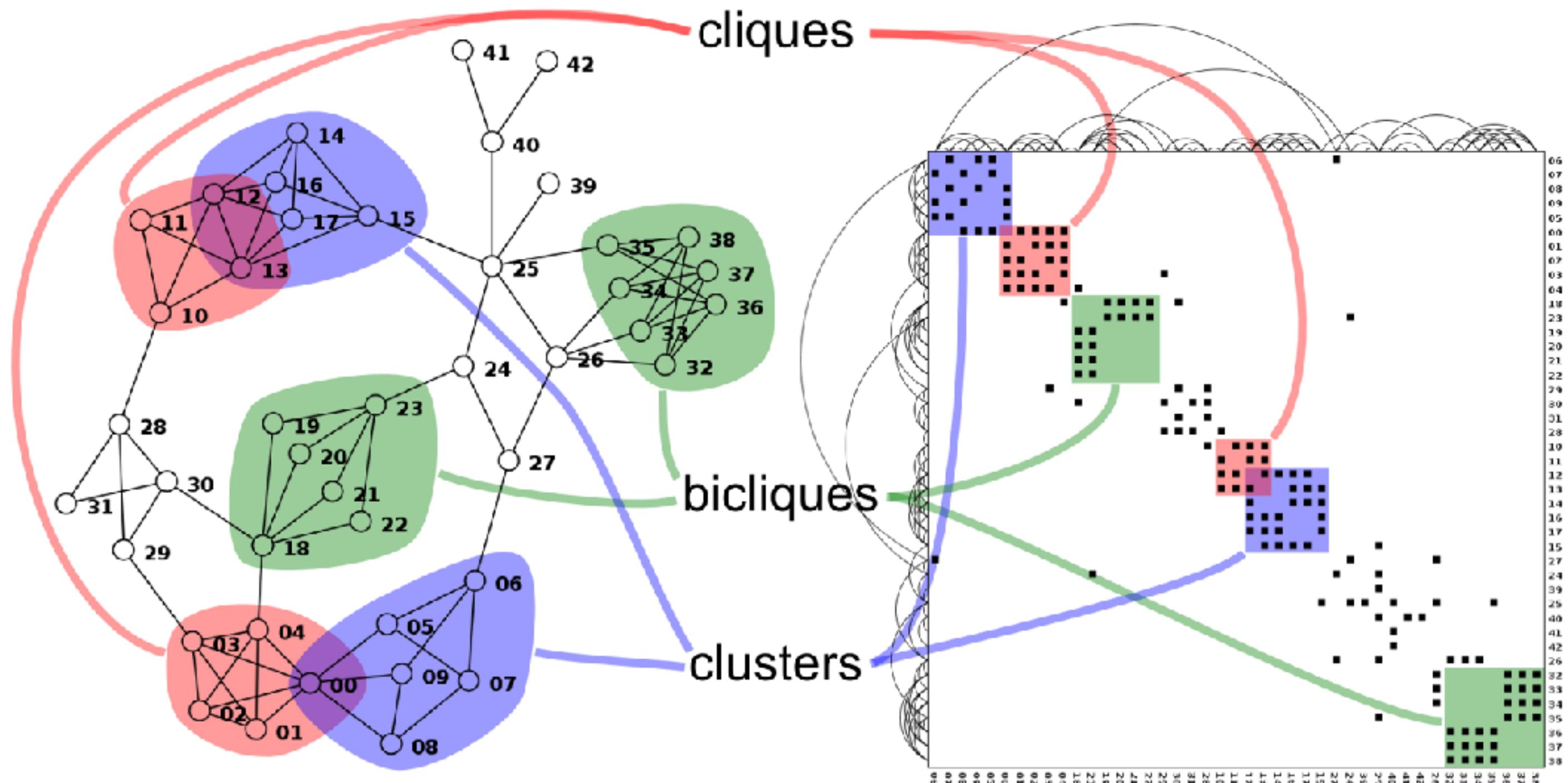
good for topology tasks  
related to neighborhoods  
(node 1-hop neighbors)



	A	B	C	D	E
E				red	
D				blue	
C					red
B				red	
A				blue	

bad for topology tasks  
related to paths

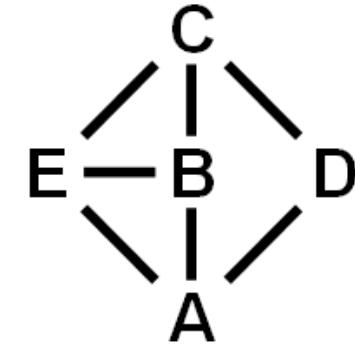
# Structures visible in both



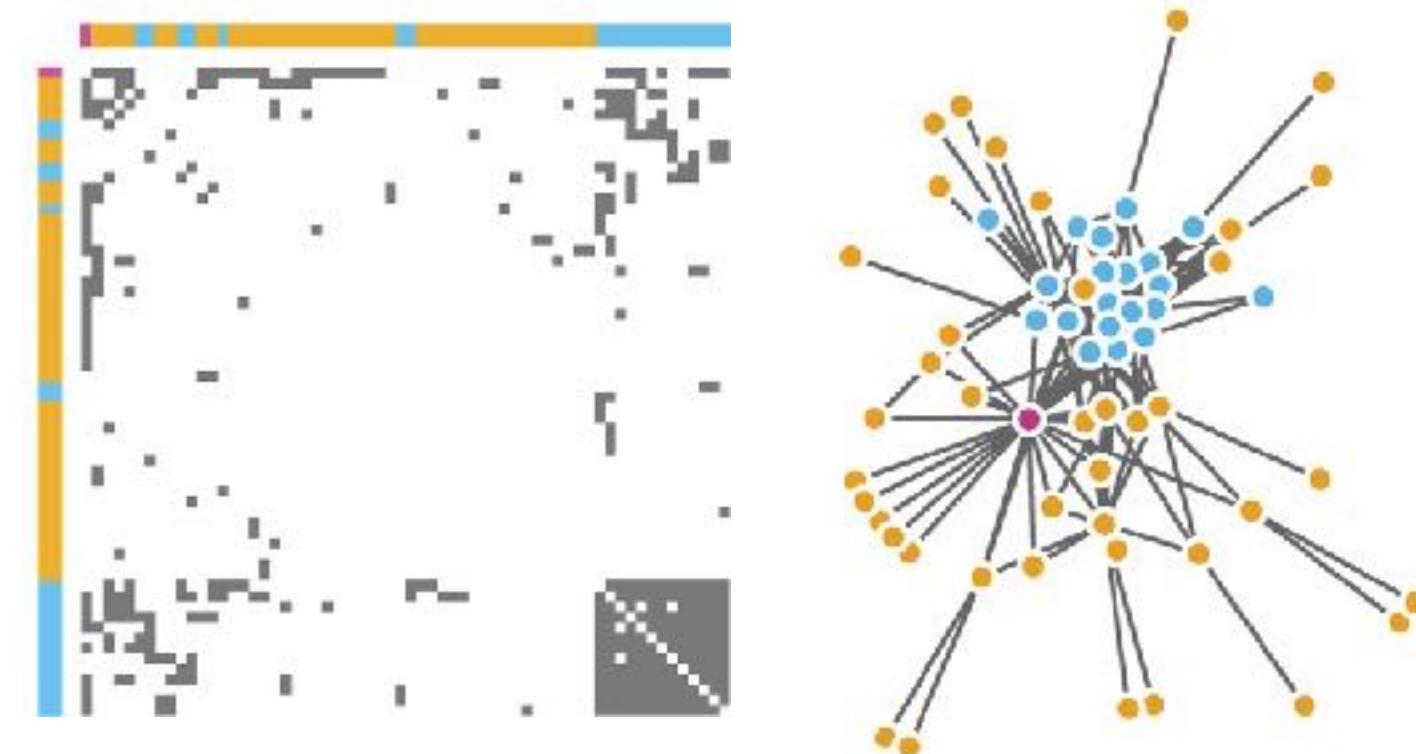
# Idiom: adjacency matrix view

- data: network
  - transform into same data/encoding as heatmap
- derived data: table from network
  - 1 quant attrib
    - weighted edge between nodes
  - 2 categ attribs: node list x 2
- visual encoding
  - cell shows presence/absence of edge
- scalability
  - 1K nodes, 1M edges

	A	B	C	D	E
A	A				
B		B			
C			C		
D				D	
E					E



[NodeTrix: a Hybrid Visualization of Social Networks.  
Henry, Fekete, and McGuffin. IEEE TVCG (Proc. InfoVis)  
13(6):1302-1309, 2007.]



[Points of view: Networks. Gehlenborg and Wong. Nature Methods 9:115.]

# Node-link vs. matrix comparison

- node-link diagram strengths

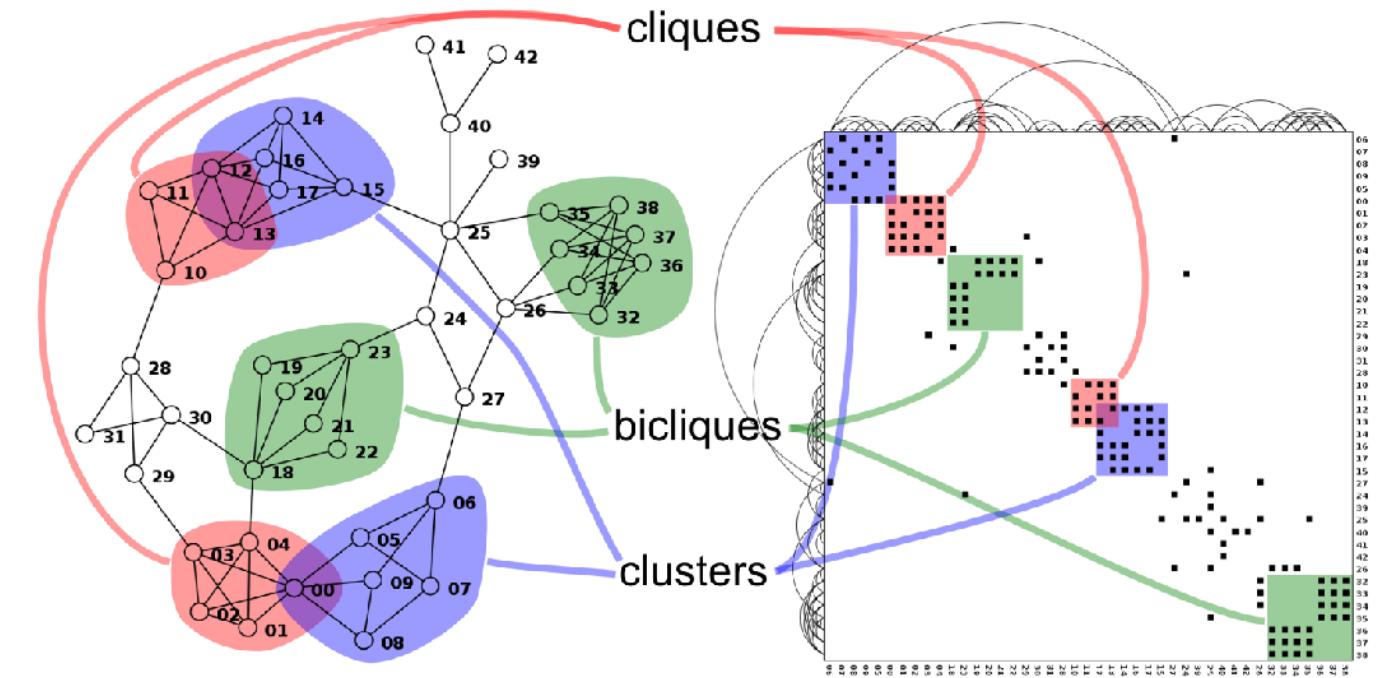
- topology understanding, path tracing
  - intuitive, flexible, no training needed

- adjacency matrix strengths

- focus on edges rather than nodes
  - layout straightforward (reordering needed)
  - predictability, scalability
  - some topology tasks trainable

- empirical study

- node-link best for small networks
  - matrix best for large networks
    - if tasks don't involve path tracing!

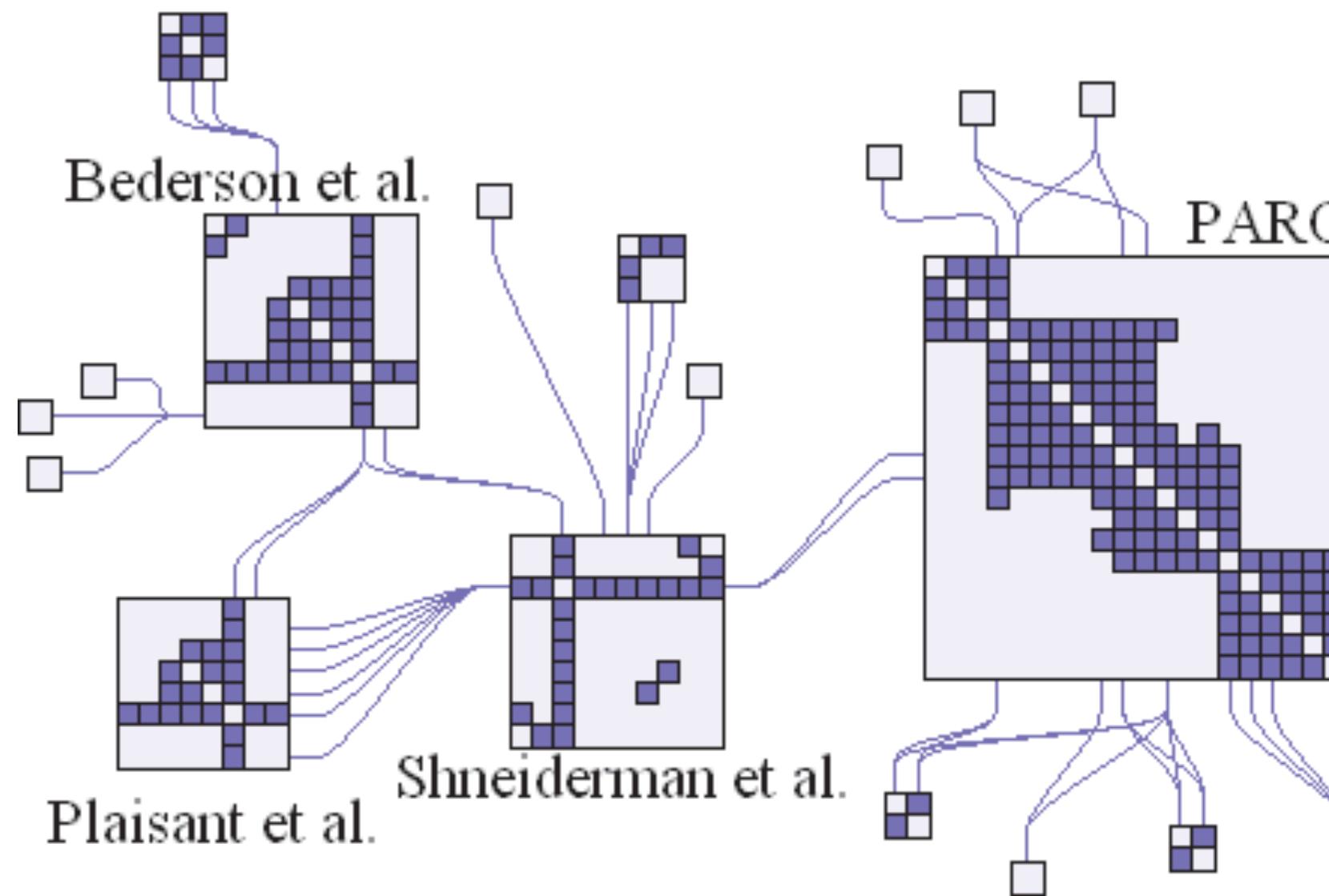


<http://www.michaelmcguffin.com/courses/vis/patternsInAdjacencyMatrix.png>

[On the readability of graphs using node-link and matrix-based representations: a controlled experiment and statistical analysis. Ghoniem, Fekete, and Castagliola. *Information Visualization* 4:2 (2005), 114–135.]

# Idiom: NodeTrix

- hybrid nodelink/matrix
- capture strengths of both



# Trees

# Tree exercise

Here is part of a directory structure used for the material for this class and the relative file size.

datavis-17/

lectures/

    Intro.key (110 MB)

    perception/

        Perception.key (113 MB)

        Blindness.mov (15MB)

    Data.key (12 MB)

    Graphs.key (180 MB)

exams/

    Exam1-solution.doc (5MB)

    Exam1.doc (1MB)

exercise/

    Graph.doc (3MB)

    Graph-video.doc (210MB)

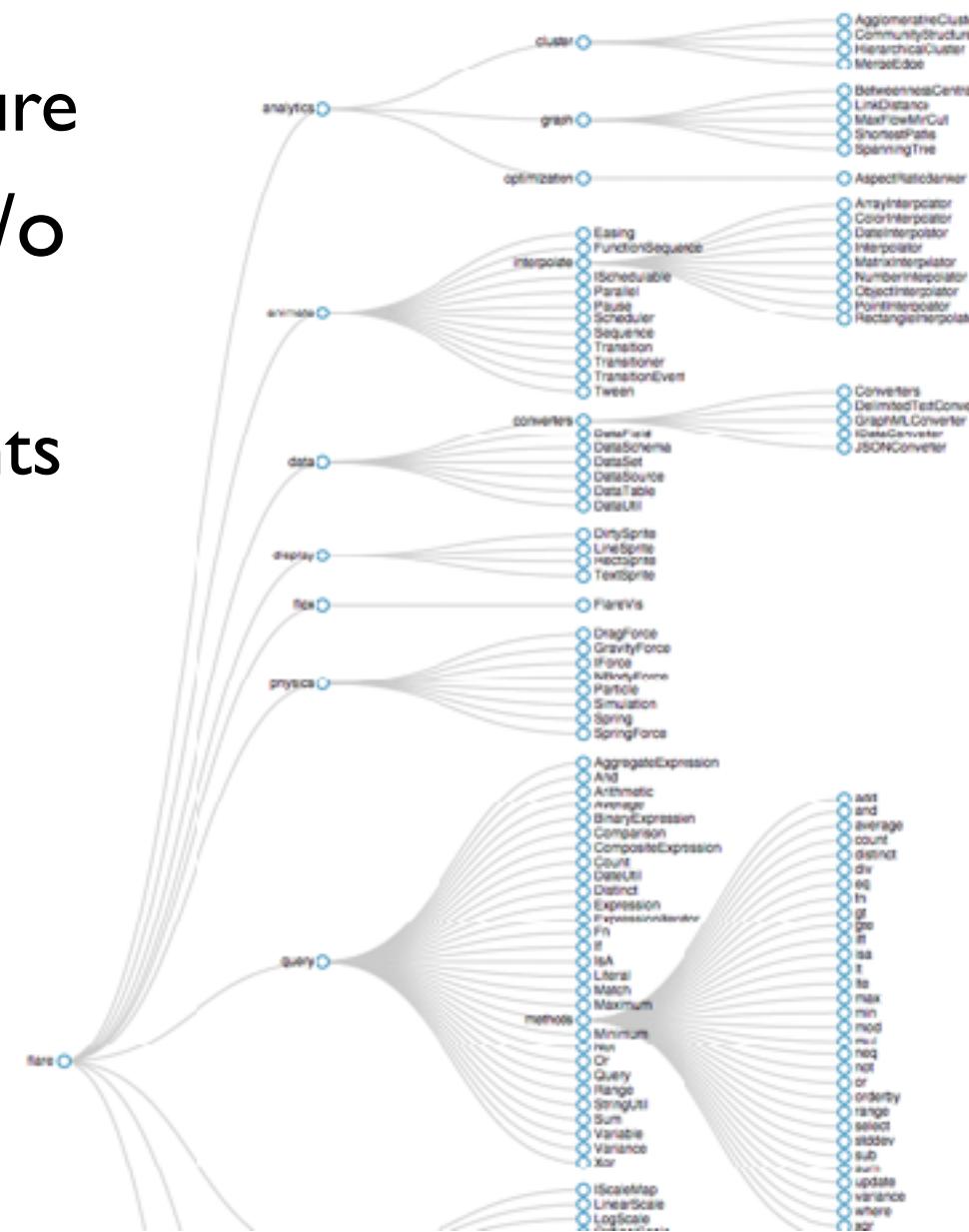
Sketch two different visualizations that show both, the directory structure and the size of the directories and the contained files.

- **socrative: true when done with both**

# Node-link trees

- Reingold-Tilford
  - tidy drawings of trees
    - exploit parent/child structure
  - allocate space: compact w/o overlap
    - rectilinear and radial variants
  - nice algorithm writeup

<http://billmill.org/pymag-trees/>



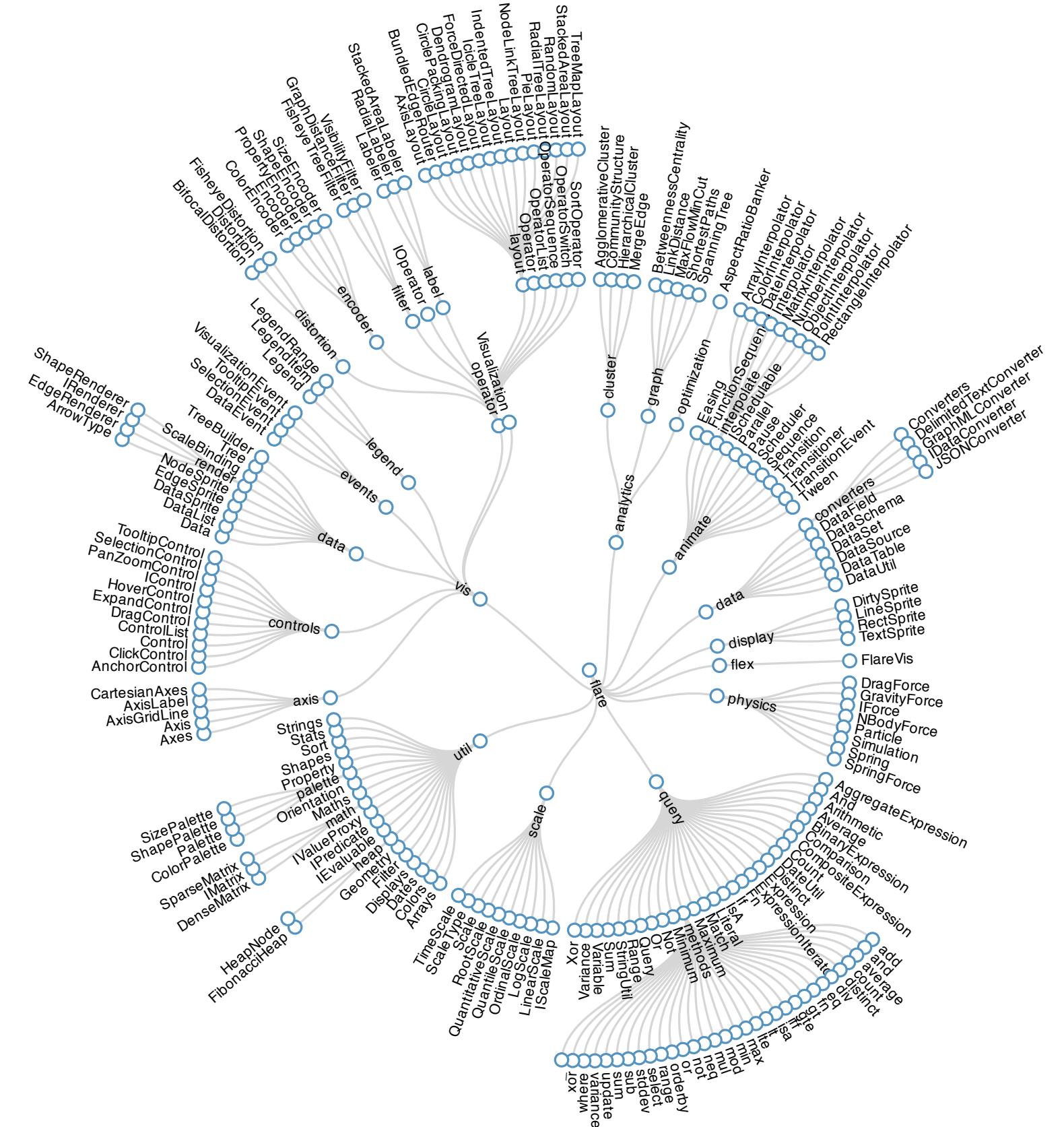
<http://blocks.org/mbostock/4339184>



<http://blocks.org/mbostock/4063550>

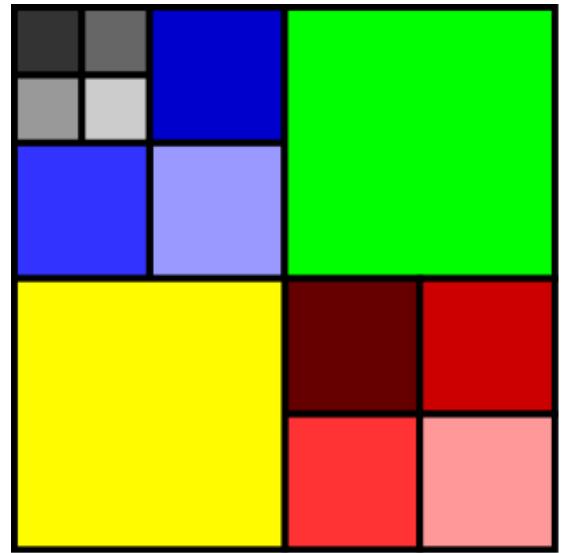
# Idiom: radial node-link tree

- data
  - tree
- encoding
  - link connection marks
  - point node marks
  - radial axis orientation
    - angular proximity: siblings
    - distance from center: depth in tree
- tasks
  - understanding topology, following paths
- scalability
  - IK - 10K nodes

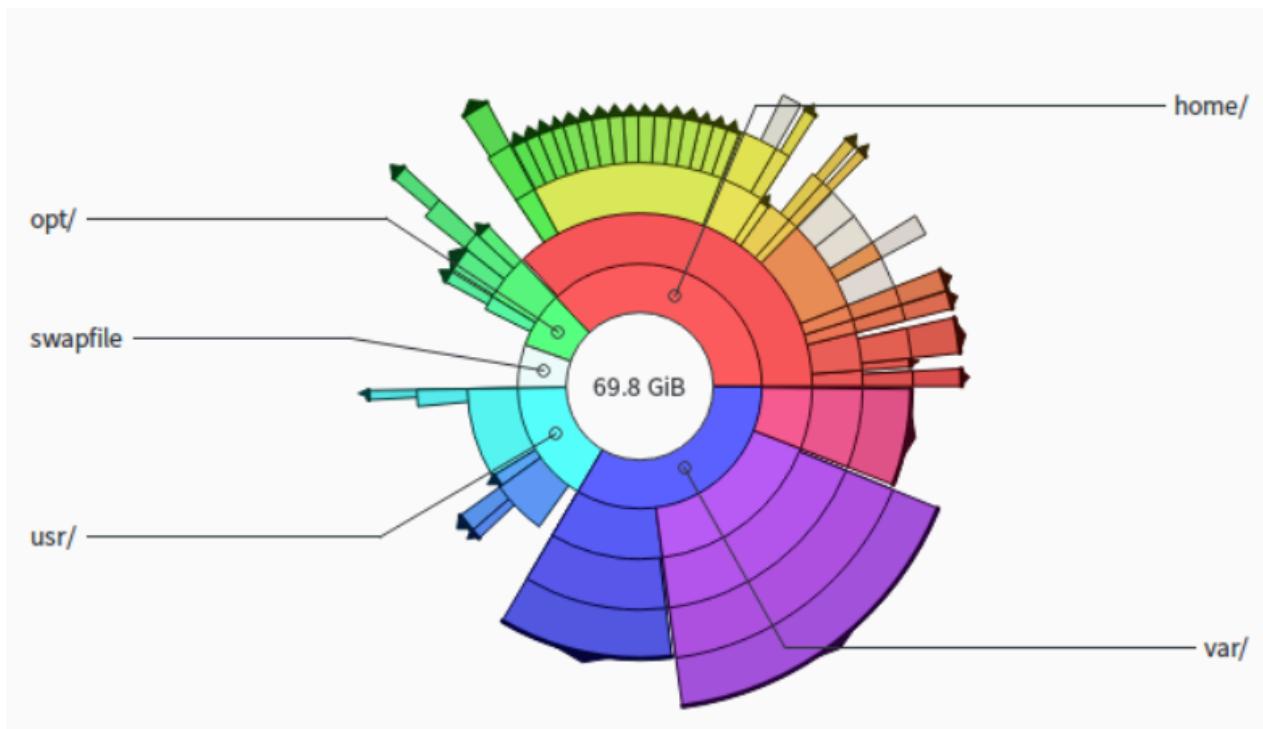


# Containment (implicit) layouts

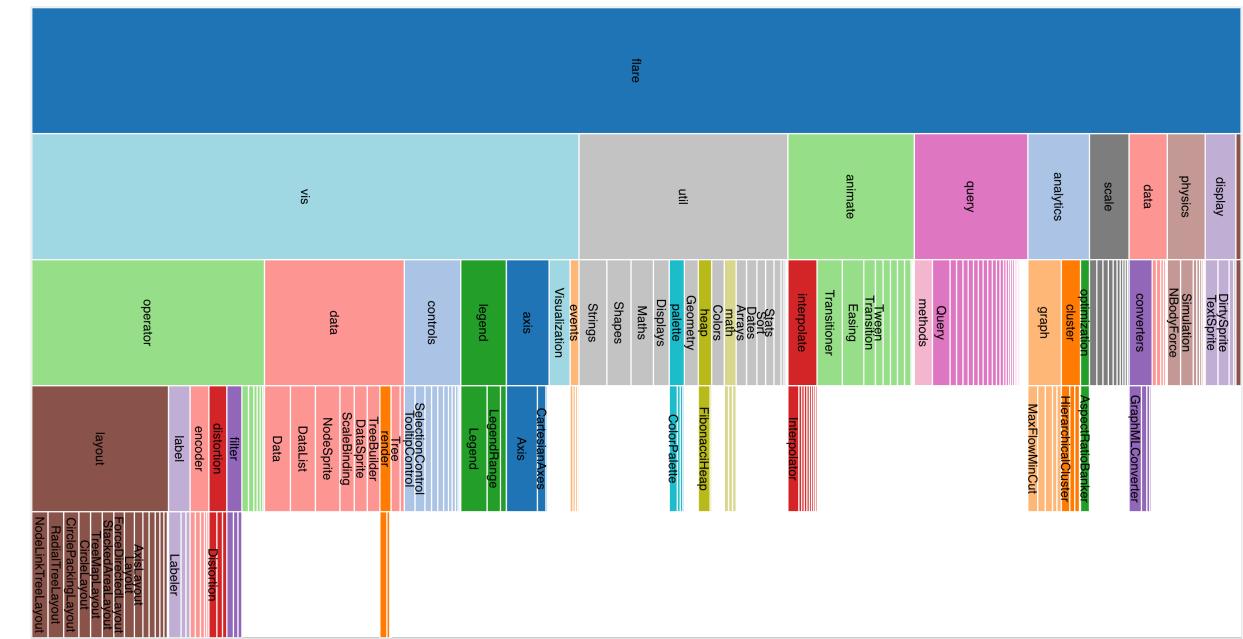
Treemap



Sunburst

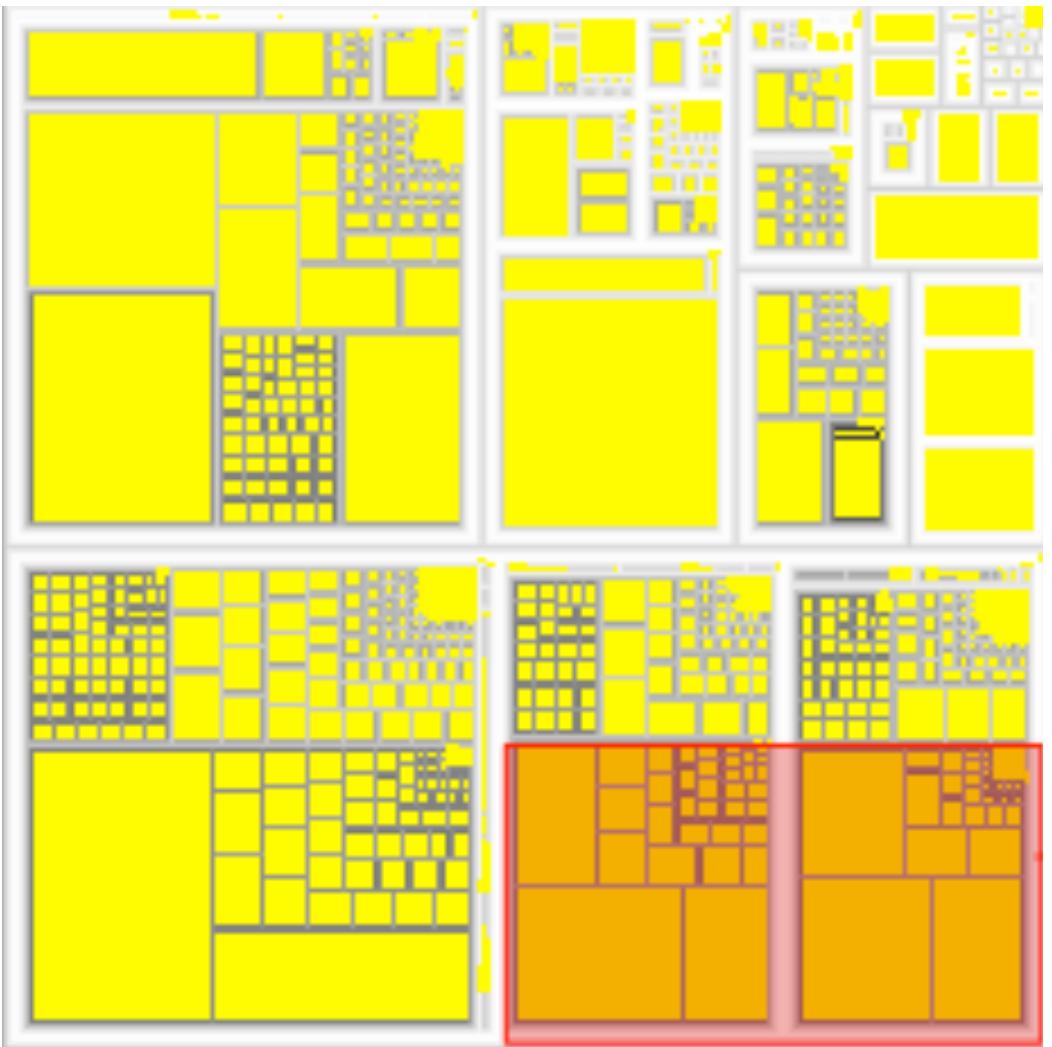


Icicle Plot



# Idiom: treemap

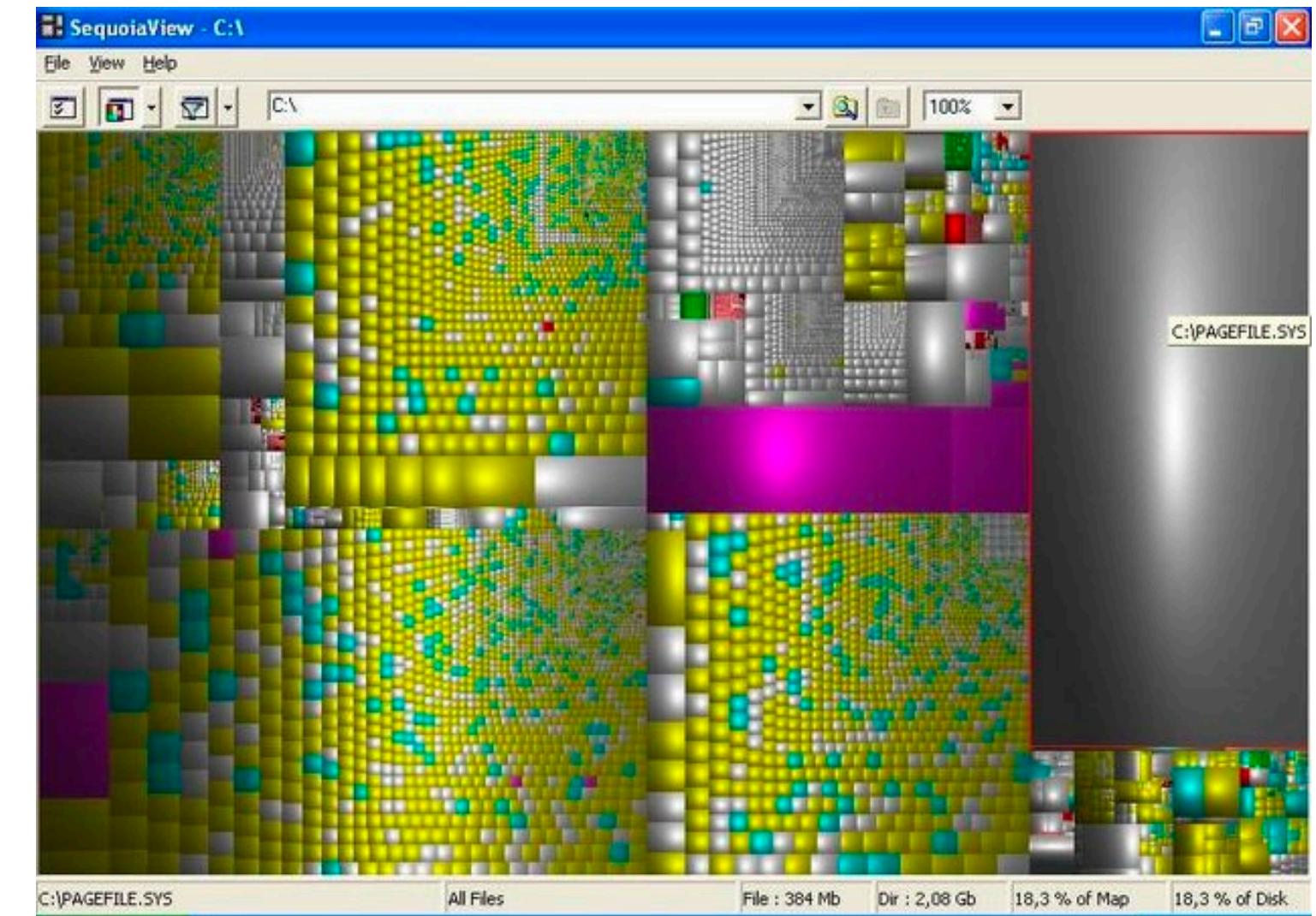
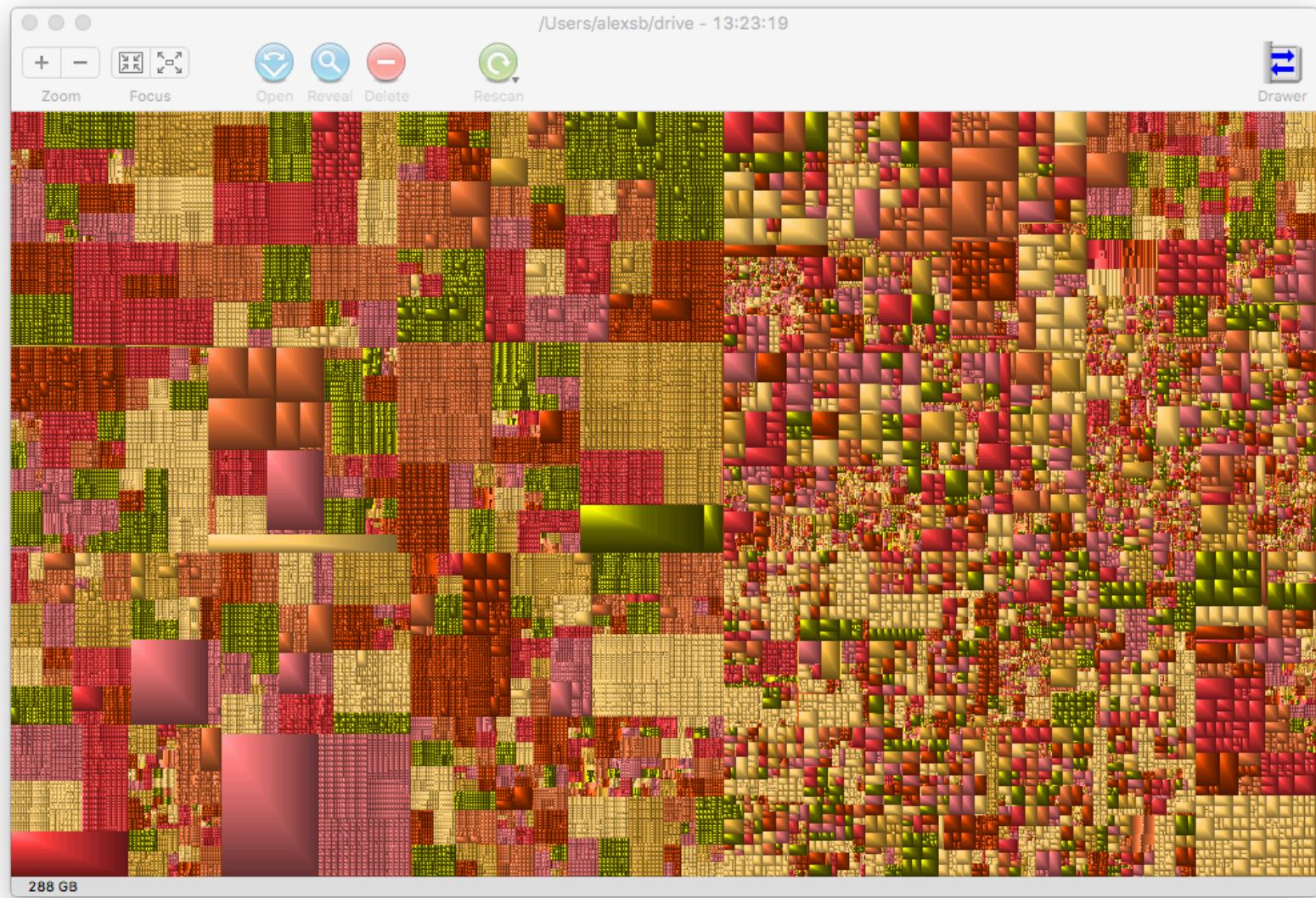
- data
  - tree
  - 1 quant attrib at leaf nodes
- encoding
  - area containment marks for hierarchical structure
  - rectilinear orientation
  - size encodes quant attrib
- tasks
  - query attribute at leaf nodes
- scalability
  - 1M leaf nodes



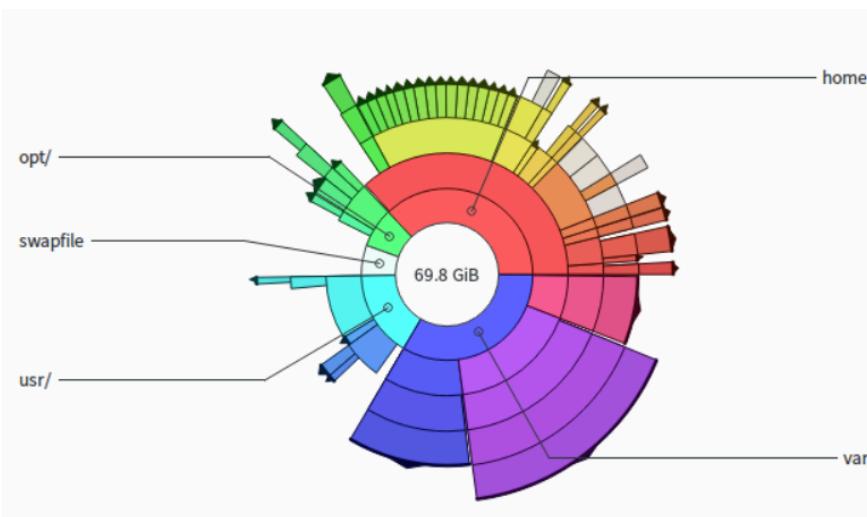
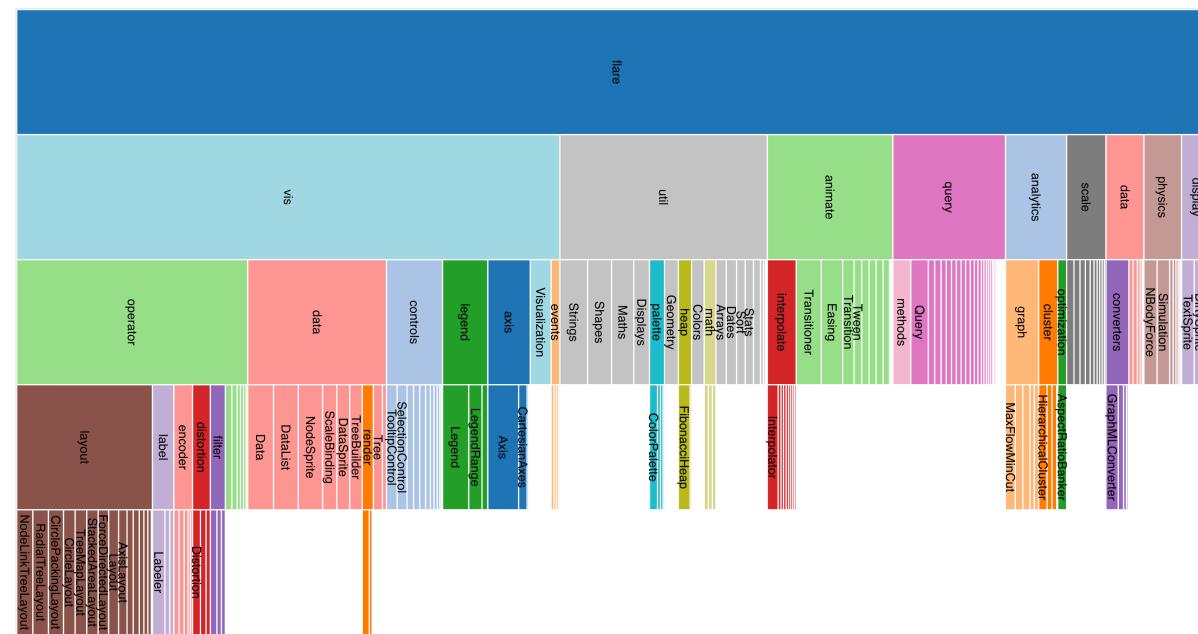
[http://tulip.labri.fr/Documentation/3\\_7/userHandbook/html/ch06.html](http://tulip.labri.fr/Documentation/3_7/userHandbook/html/ch06.html)

# Treemap software: disk space

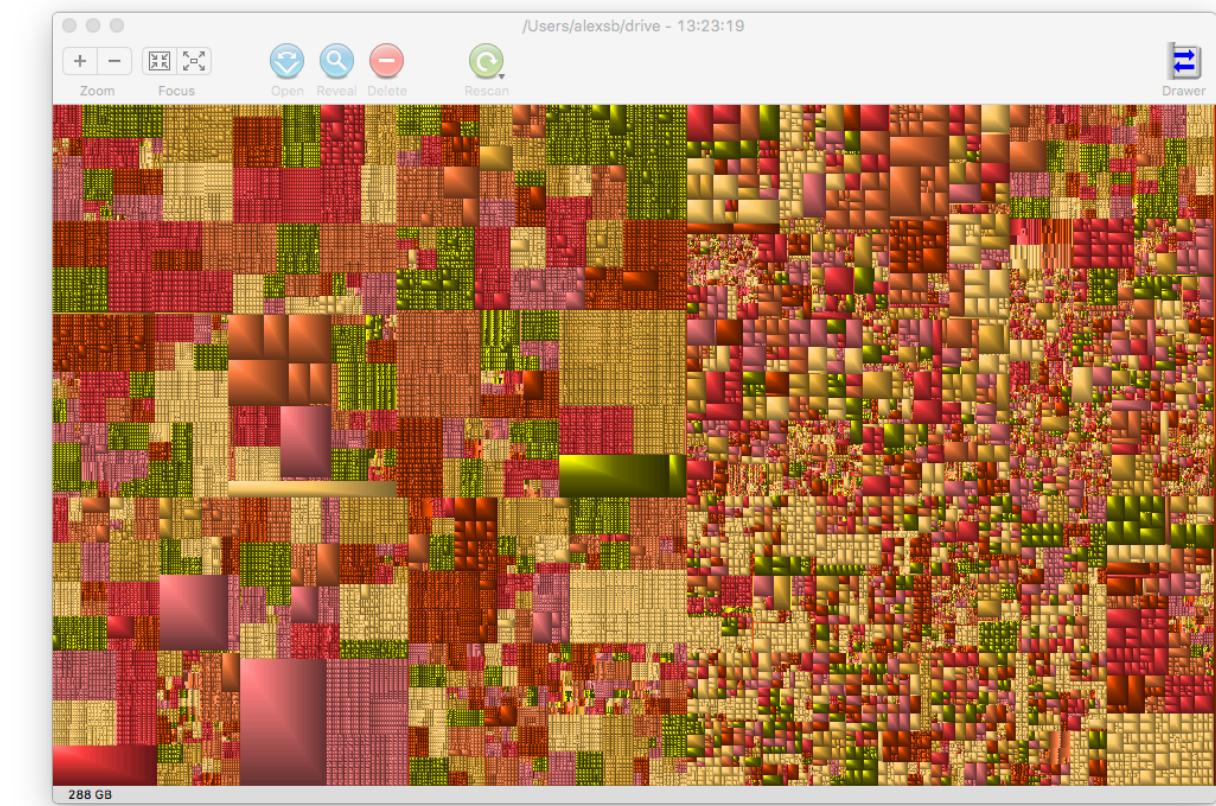
Mac: GrandPerspective   Windows: Sequoia View



# Containment: Approaches compared



Inner Nodes and Leaves Visible

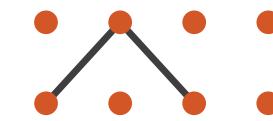


Only Leaves Visible

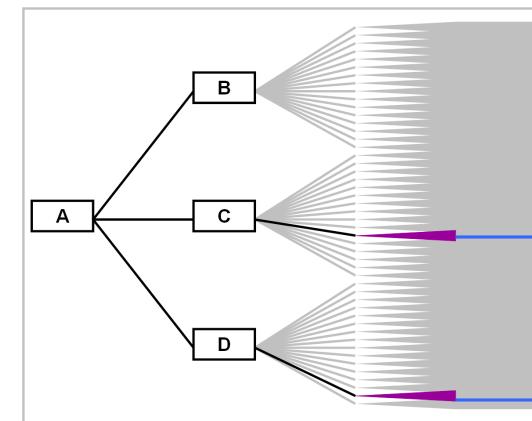
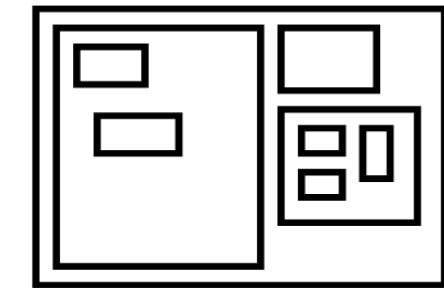
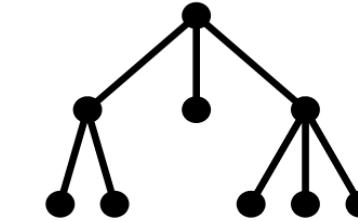
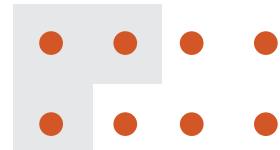
# Link marks: Connection and containment

- marks as links (vs. nodes)
  - common case in network drawing
  - 1D case: connection
    - ex: all node-link diagrams
    - emphasizes topology, path tracing
    - networks and trees
  - 2D case: containment
    - ex: all treemap variants
    - emphasizes attribute values at leaves (size coding)
    - only trees

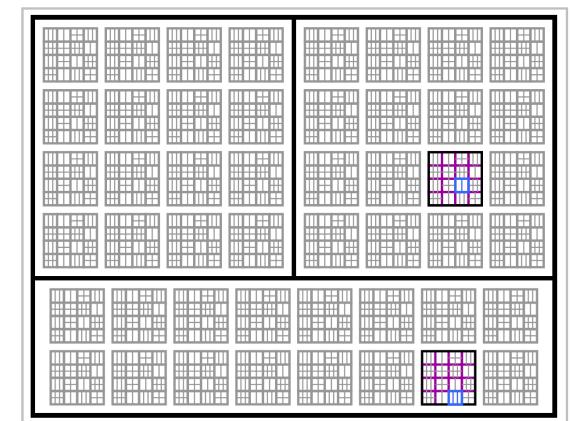
→ Connection



→ Containment



Node-Link Diagram

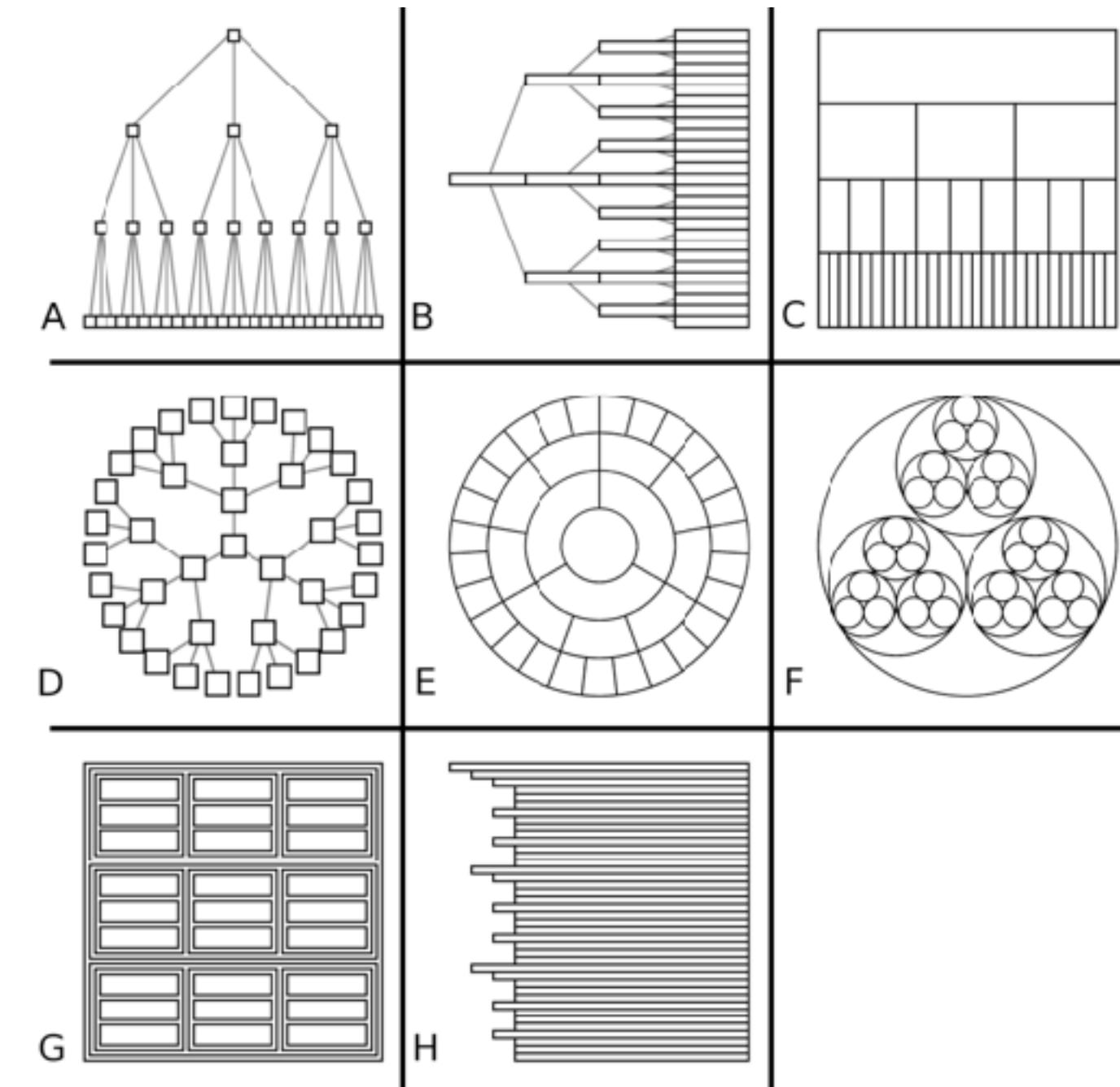


Treemap

[*Elastic Hierarchies: Combining Treemaps and Node-Link Diagrams*. Dong, McGuffin, and Chignell. Proc. InfoVis 2005, p. 57-64.]

# Tree drawing idioms comparison

- data shown
  - link relationships
  - tree depth
  - sibling order
- design choices
  - connection vs containment link marks
  - rectilinear vs radial layout
  - spatial position channels
- considerations
  - redundant? arbitrary?
  - information density?
    - avoid wasting space
    - consider where to fit labels!



[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees. McGuffin and Robert. Information Visualization 9:2 (2010), 115–140.]

# treevis.net: many, many options

<https://treevis.net/>

How to cite this site?  
Check out other surveys! (3)

treevis.net - A Visual Bibliography of Tree Visualization 2.0 by Hans-Jörg Schulz

v.21-OCT-2014

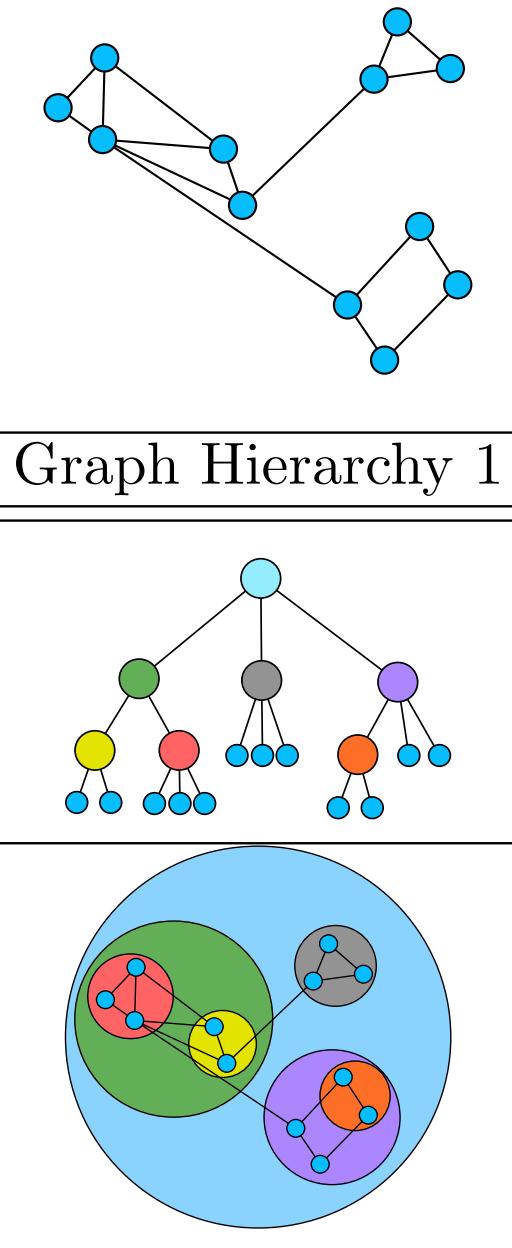
Dimensionality      Representation      Alignment      Fulltext Search      Techniques Shown  x **277**

Dimensionality: All, 2D, 3D, 4D  
Representation: All, Node-link, Chord, Circular  
Alignment: All, Circular, Radial, Circular-Radial  
Techniques Shown: 277

The screenshot displays a grid of 25 rows, each containing 12 small images representing different tree visualization techniques. The techniques include various layouts like circular, radial, and hierarchical, often with color coding or 3D effects. The first row shows a search bar and navigation links. The second row contains a 'Fulltext Search' input field and a 'Techniques Shown' counter set at 277.

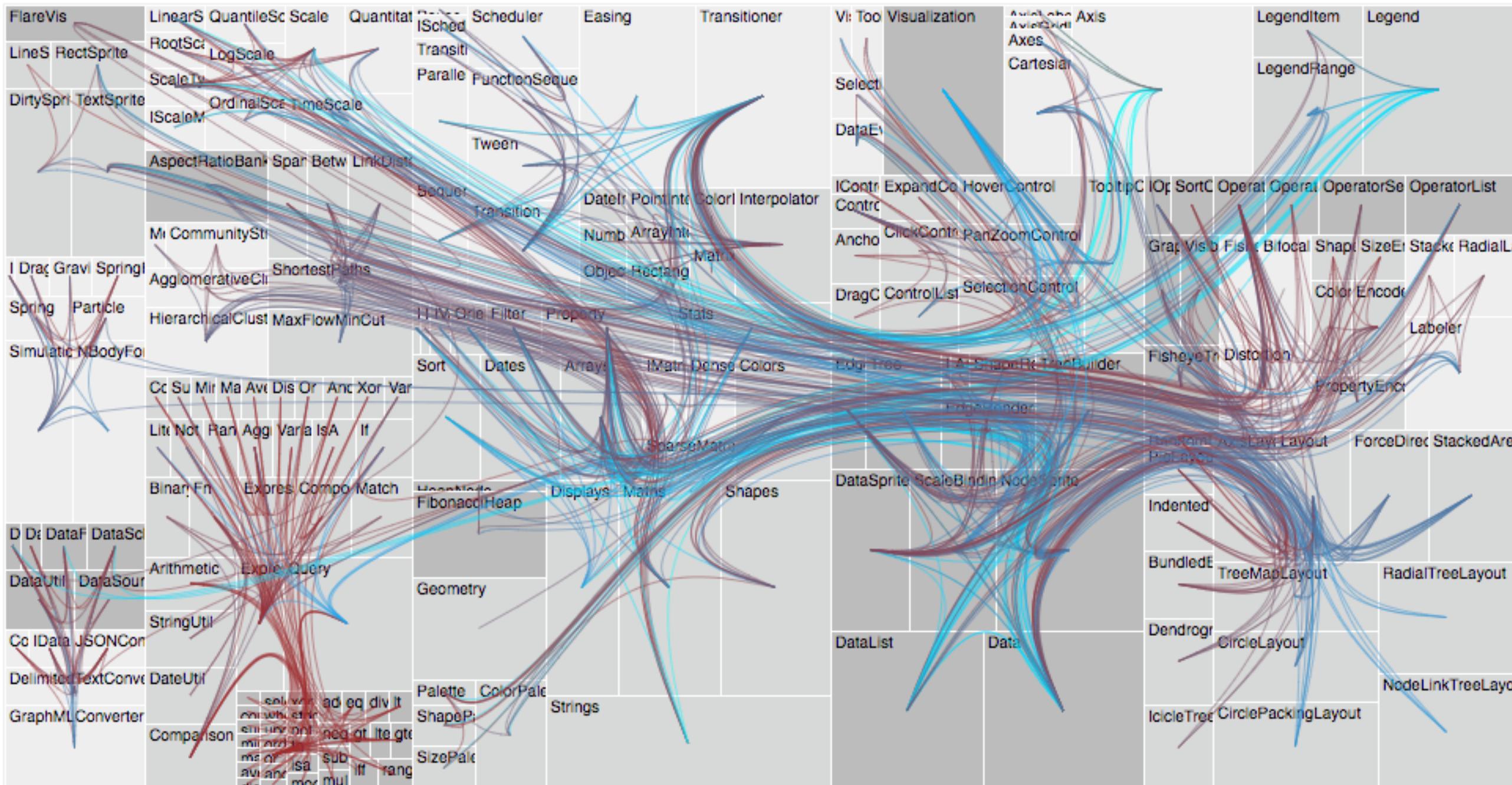
# Idiom: GrouseFlocks

- data: compound graphs
  - network
  - cluster hierarchy atop it
    - derived or interactively chosen
- visual encoding
  - connection marks for network links
  - containment marks for hierarchy
  - point marks for nodes
- dynamic interaction
  - select individual metanodes in hierarchy to expand/contract



[*GrouseFlocks: Steerable Exploration of Graph Hierarchy Space*. Archambault, Munzner, and Auber. *IEEE TVCG* 14(4): 900-913, 2008.]

# Hierarchical edge bundling: treemap vs radial



# Credits

- Visualization Analysis and Design (Ch 9)
- Alex Lex & Miriah Meyer, <http://dataviscourse.net/>