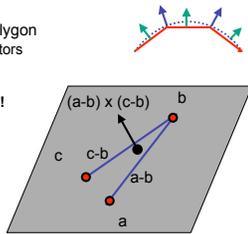


Computing Normals

- per-vertex normals by interpolating per-facet normals
 - OpenGL supports both
- computing normal for a polygon
 - three points form two vectors
 - cross: normal of plane gives direction
 - normalize to unit length!**
- which side is up?
 - convention: points in counterclockwise order



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Specifying Normals

- OpenGL state machine
 - uses last normal specified
 - if no normals specified, assumes all identical
- per-vertex normals


```
glNormal3f(1,1,1);
glVertex3f(3,4,5);
glNormal3f(1,1,0);
glVertex3f(10,5,2);
```
- per-face normals


```
glNormal3f(1,1,1);
glVertex3f(3,4,5);
glVertex3f(10,5,2);
```
- normal interpreted as direction from vertex location
- can automatically normalize (computational cost)


```
glEnable(GL_NORMALIZE);
```

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Global Illumination Models

- simple lighting/shading methods simulate local illumination models
 - no object-object interaction
- global illumination models
 - more realism, more computation
 - leaving the pipeline for these two lectures!
- approaches
 - ray tracing
 - radiosity
 - photon mapping
 - subsurface scattering

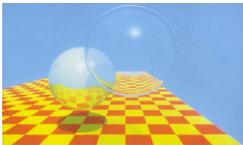
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Advanced Rendering

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Ray Tracing

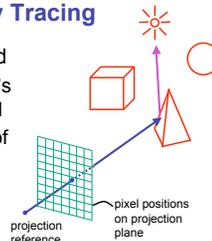
- simple basic algorithm
- well-suited for software rendering
- flexible, easy to incorporate new effects
 - Turner Whitted, 1990



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Simple Ray Tracing

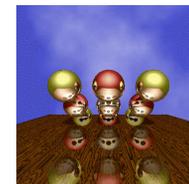
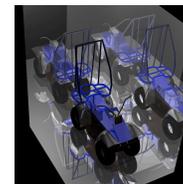
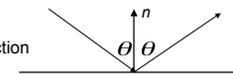
- view dependent method
 - cast a ray from viewer's eye through each pixel
 - compute intersection of ray with first object in scene
 - cast ray from intersection point on object to light sources



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Reflection

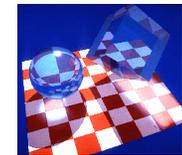
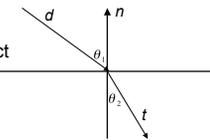
- mirror effects
 - perfect specular reflection



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Refraction

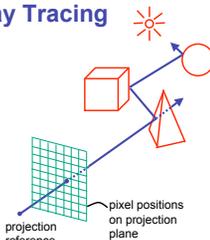
- happens at interface between transparent object and surrounding medium
 - e.g. glass/air boundary
- Snell's Law
 - $c_1 \sin \theta_1 = c_2 \sin \theta_2$
 - light ray bends based on refractive indices c_1, c_2



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Recursive Ray Tracing

- ray tracing can handle
 - reflection (chrome/mirror)
 - refraction (glass)
 - shadows
- spawn secondary rays
 - reflection, refraction
 - if another object is hit, recurse to find its color
 - shadow
 - cast ray from intersection point to light source, check if intersects another object



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Basic Algorithm

```
for every pixel pi {
  generate ray r from camera position through pixel pi
  for every object o in scene {
    if ( r intersects o )
      compute lighting at intersection point, using local
      normal and material properties; store result in pi
    else
      pi = background color
  }
}
```

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Basic Ray Tracing Algorithm

```
RayTrace(r,scene)
obj := FirstIntersection(r,scene)
if (no obj) return BackgroundColor;
else begin
  if ( Reflect(obj) ) then
    reflect_color := RayTrace(ReflectRay(r,obj));
  else
    reflect_color := Black;
  if ( Transparent(obj) ) then
    refract_color := RayTrace(RefractRay(r,obj));
  else
    refract_color := Black;
  return Shade(reflect_color,refract_color,obj);
end;
```

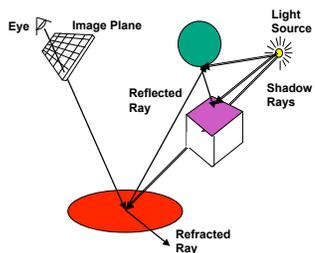
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Algorithm Termination Criteria

- termination criteria
 - no intersection
 - reach maximal depth
 - number of bounces
 - contribution of secondary ray attenuated below threshold
 - each reflection/refraction attenuates ray

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Ray Tracing Algorithm



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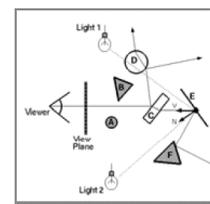
Ray-Tracing Terminology

- terminology:
 - primary ray: ray starting at camera
 - shadow ray
 - reflected/refracted ray
 - ray tree: all rays directly or indirectly spawned off by a single primary ray
- note:
 - need to limit maximum depth of ray tree to ensure termination of ray-tracing process!

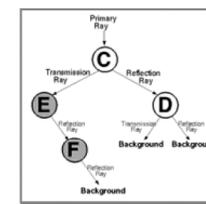
30

Ray Trees

- all rays directly or indirectly spawned off by a single primary ray



Ray traced through scene



Ray tree

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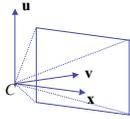
Ray Tracing

- issues:
 - generation of rays
 - intersection of rays with geometric primitives
 - geometric transformations
 - lighting and shading
 - efficient data structures so we don't have to test intersection with every object

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Ray Generation

- camera coordinate system
 - origin: C (camera position)
 - viewing direction: \mathbf{v}
 - up vector: \mathbf{u}
 - x direction: $\mathbf{x} = \mathbf{v} \times \mathbf{u}$
- note:
 - corresponds to viewing transformation in rendering pipeline
 - like gluLookAt



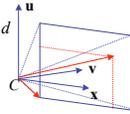
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Ray Generation

- other parameters:
 - distance of camera from image plane: d
 - image resolution (in pixels): w, h
 - left, right, top, bottom boundaries in image plane: l, r, t, b
- then:
 - lower left corner of image: $O = C + d \cdot \mathbf{v} + l \cdot \mathbf{x} + b \cdot \mathbf{u}$
 - pixel at position i, j ($i=0..w-1, j=0..h-1$):

$$P_{i,j} = O + i \cdot \frac{r-l}{w-1} \cdot \mathbf{x} - j \cdot \frac{t-b}{h-1} \cdot \mathbf{u}$$

$$= O + i \cdot \Delta x \cdot \mathbf{x} - j \cdot \Delta y \cdot \mathbf{y}$$



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Ray Generation

- ray in 3D space:

$$R_{i,j}(t) = C + t \cdot (P_{i,j} - C) = C + t \cdot \mathbf{v}_{i,j}$$

where $t = 0 \dots \infty$

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Ray Tracing

- issues:
 - generation of rays
 - intersection of rays with geometric primitives
 - geometric transformations
 - lighting and shading
 - efficient data structures so we don't have to test intersection with every object

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Ray - Object Intersections

- inner loop of ray-tracing
 - must be extremely efficient
- task: given an object o, find ray parameter t , such that $R_{i,j}(t)$ is a point on the object
 - such a value for t may not exist
- solve a set of equations
- intersection test depends on geometric primitive
 - ray-sphere
 - ray-triangle
 - ray-polygon

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Ray Intersections: Spheres

- spheres at origin
 - implicit function

$$S(x, y, z) : x^2 + y^2 + z^2 = r^2$$
 - ray equation

$$R_{i,j}(t) = C + t \cdot \mathbf{v}_{i,j} = \begin{pmatrix} c_x \\ c_y \\ c_z \end{pmatrix} + t \cdot \begin{pmatrix} v_x \\ v_y \\ v_z \end{pmatrix} = \begin{pmatrix} c_x + t \cdot v_x \\ c_y + t \cdot v_y \\ c_z + t \cdot v_z \end{pmatrix}$$

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Ray Intersections: Spheres

- to determine intersection:
 - insert ray $R_{i,j}(t)$ into $S(x, y, z)$:

$$(c_x + t \cdot v_x)^2 + (c_y + t \cdot v_y)^2 + (c_z + t \cdot v_z)^2 = r^2$$
 - solve for t (find roots)
 - simple quadratic equation

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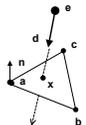
Ray Intersections: Other Primitives

- implicit functions
 - spheres at arbitrary positions
 - same thing
 - conic sections (hyperboloids, ellipsoids, paraboloids, cones, cylinders)
 - same thing (all are quadratic functions!)
- polygons
 - first intersect ray with plane
 - linear implicit function
 - then test whether point is inside or outside of polygon (2D test)
 - for convex polygons
 - suffices to test whether point is on the correct side of every boundary edge
 - similar to computation of outcodes in line clipping (upcoming)

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Ray-Triangle Intersection

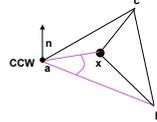
- method in book is elegant but a bit complex
- easier approach: triangle is just a polygon
 - intersect ray with plane
 - normal: $\mathbf{n} = (\mathbf{b} - \mathbf{a}) \times (\mathbf{c} - \mathbf{a})$
 - ray: $\mathbf{x} = \mathbf{e} + t\mathbf{d}$
 - plane: $(\mathbf{p} - \mathbf{x}) \cdot \mathbf{n} = 0 \Rightarrow \mathbf{x} = \frac{\mathbf{p} \cdot \mathbf{n}}{\mathbf{n} \cdot \mathbf{n}}$
 - $\frac{\mathbf{p} \cdot \mathbf{n}}{\mathbf{n} \cdot \mathbf{n}} = \mathbf{e} + t\mathbf{d} \Rightarrow t = -\frac{(\mathbf{e} - \mathbf{p}) \cdot \mathbf{n}}{\mathbf{d} \cdot \mathbf{n}}$
 - \mathbf{p} is a or b or c
- check if ray inside triangle



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Ray-Triangle Intersection

- check if ray inside triangle
 - check if point counterclockwise from each edge (to its left)
 - check if cross product points in same direction as normal (i.e. if dot is positive)
- $$(\mathbf{b} - \mathbf{a}) \times (\mathbf{x} - \mathbf{a}) \cdot \mathbf{n} \geq 0$$
- $$(\mathbf{c} - \mathbf{b}) \times (\mathbf{x} - \mathbf{b}) \cdot \mathbf{n} \geq 0$$
- $$(\mathbf{a} - \mathbf{c}) \times (\mathbf{x} - \mathbf{c}) \cdot \mathbf{n} \geq 0$$
- more details at <http://www.cs.cornell.edu/courses/cs465/2003fa/homeworks/raytri.pdf>



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Ray Tracing

- issues:
 - generation of rays
 - intersection of rays with geometric primitives
 - geometric transformations
 - lighting and shading
 - efficient data structures so we don't have to test intersection with every object

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Geometric Transformations

- similar goal as in rendering pipeline:
 - modeling scenes more convenient using different coordinate systems for individual objects
- problem
 - not all object representations are easy to transform
 - problem is fixed in rendering pipeline by restriction to polygons, which are affine invariant
 - ray tracing has different solution
 - ray itself is always affine invariant
 - thus: transform ray into object coordinates!

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Geometric Transformations

- ray transformation
 - for intersection test, it is only important that ray is in same coordinate system as object representation
 - transform all rays into object coordinates
 - transform camera point and ray direction by inverse of model/view matrix
 - shading has to be done in world coordinates (where light sources are given)
 - transform object space intersection point to world coordinates
 - thus have to keep both world and object-space ray

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Ray Tracing

- issues:
 - generation of rays
 - intersection of rays with geometric primitives
 - geometric transformations
 - lighting and shading
 - efficient data structures so we don't have to test intersection with every object

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Local Lighting

- local surface information (normal...)
 - for implicit surfaces $F(x, y, z) = 0$: normal $\mathbf{n}(x, y, z)$ can be easily computed at every intersection point using the gradient

$$\mathbf{n}(x, y, z) = \begin{pmatrix} \partial F(x, y, z) / \partial x \\ \partial F(x, y, z) / \partial y \\ \partial F(x, y, z) / \partial z \end{pmatrix}$$
 - example:

$$F(x, y, z) = x^2 + y^2 + z^2 - r^2$$

$$\mathbf{n}(x, y, z) = \begin{pmatrix} 2x \\ 2y \\ 2z \end{pmatrix} \quad \text{needs to be normalized!}$$

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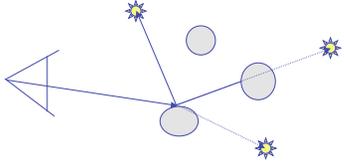
Local Lighting

- local surface information
 - alternatively: can interpolate per-vertex information for triangles/meshes as in rendering pipeline
 - now easy to use Phong shading!
 - as discussed for rendering pipeline
 - difference with rendering pipeline:
 - interpolation cannot be done incrementally
 - have to compute barycentric coordinates for every intersection point (e.g plane equation for triangles)

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Global Shadows

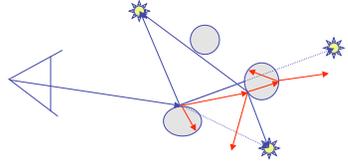
- approach
 - to test whether point is in shadow, send out **shadow rays** to all light sources
 - if ray hits another object, the point lies in shadow



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Global Reflections/Refractions

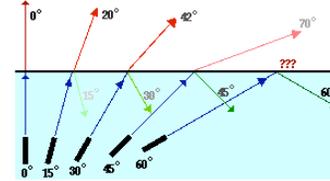
- approach
 - send rays out in reflected and refracted direction to gather incoming light
 - that light is multiplied by local surface color and added to result of local shading



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Total Internal Reflection

As the angle of incidence increases from 0 to greater angles ...



...the refracted ray becomes dimmer (there is less refraction)
 ...the reflected ray becomes brighter (there is more reflection)
 ...the angle of refraction approaches 90 degrees until finally a refracted ray can no longer be seen.

<http://www.physicsclassroom.com/Class/refrn/U14L3b.html>

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Ray Tracing

- issues:
 - generation of rays
 - intersection of rays with geometric primitives
 - geometric transformations
 - lighting and shading
 - **efficient data structures so we don't have to test intersection with every object**

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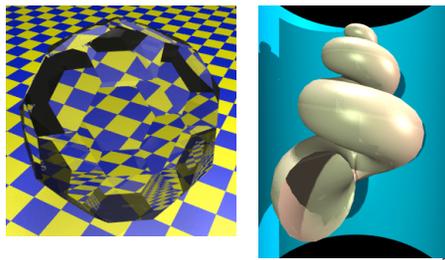
Optimized Ray-Tracing

- basic algorithm simple but **very** expensive
- optimize by reducing:
 - number of rays traced
 - number of ray-object intersection calculations
- methods
 - bounding volumes: boxes, spheres
 - spatial subdivision
 - uniform
 - BSP trees
- (more on this later with collision)



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Example Images



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Radiosity

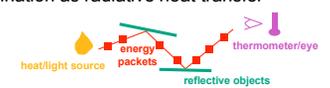
- radiosity definition
 - rate at which energy emitted or reflected by a surface
- radiosity methods
 - capture diffuse-diffuse bouncing of light
 - indirect effects difficult to handle with raytracing



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Radiosity

- illumination as radiative heat transfer
 - conserve light energy in a volume
 - model light transport as packet flow until convergence
 - solution captures diffuse-diffuse bouncing of light
- view-independent technique
 - calculate solution for entire scene offline
 - browse from any viewpoint in realtime



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Radiosity

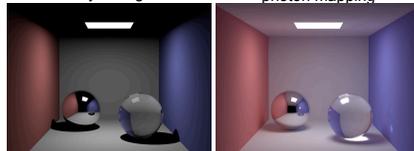
- divide surfaces into small patches
- loop: check for light exchange between all pairs
 - form factor: orientation of one patch wrt other patch (n x n matrix)



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Better Global Illumination

- ray-tracing: great specular, approx. diffuse
 - view dependent
- radiosity: great diffuse, specular ignored
 - view independent, mostly-enclosed volumes
- photon mapping: superset of raytracing and radiosity
 - view dependent, handles both diffuse and specular well

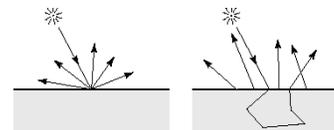


graphics.ucsd.edu/~henrik/images/cbox.html

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Subsurface Scattering: Translucency

- light enters and leaves at *different* locations on the surface
 - bounces around inside
- technical Academy Award, 2003
 - Jensen, Marschner, Hanrahan



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Subsurface Scattering: Marble



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Subsurface Scattering: Milk vs. Paint



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Subsurface Scattering: Skin



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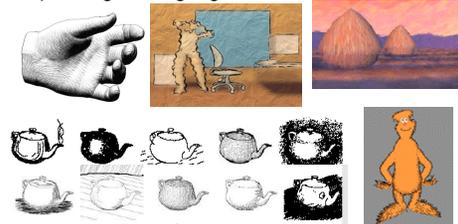
Subsurface Scattering: Skin



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Non-Photorealistic Rendering

- simulate look of hand-drawn sketches or paintings, using digital models



www.red3d.com/cwr/npr/

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