



University of British Columbia  
CPSC 314 Computer Graphics  
Jan-Apr 2010

Tamara Munzner

**Vision/Color II, Rasterization**

**Week 6, Mon Feb 8**

<http://www.ugrad.cs.ubc.ca/~cs314/Vjan2010>

## Events this week

### Schlumberger Info Session

Date: **Mon., Feb 8**  
Time: **5:30 pm**  
Location: **HENN Rm 201**

### Finding a Summer Job or Internship Info Session

Date: **Wed., Feb 10**  
Time: **12 pm**  
Location: **X836**

### Masters of Digital Media Program Info Session

Date: **Thurs., Feb 11**  
Time: **12:30 – 1:30 pm**  
Location: **DMP 201**

### Reminder: Co-op Deadline

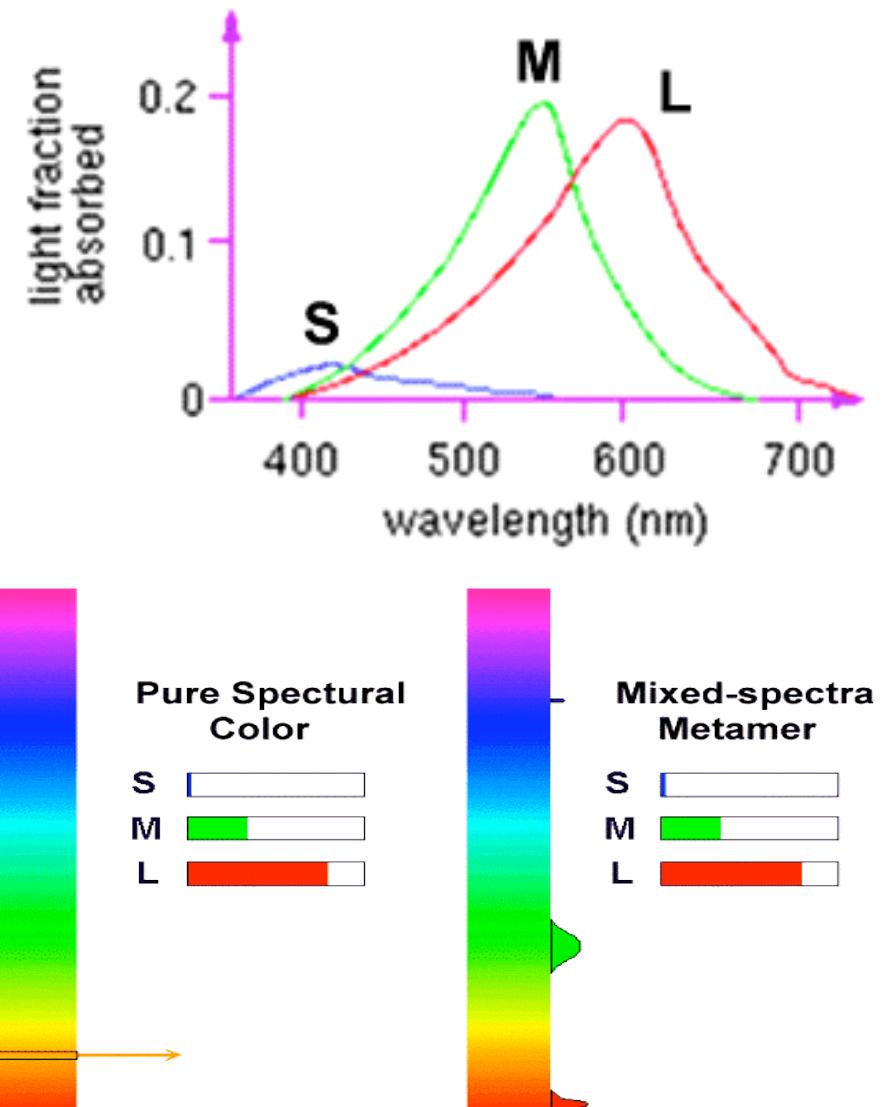
Date: **Fri., Feb 12**  
**Submit application to Fiona at Rm X241 by 4:30 pm**

# News

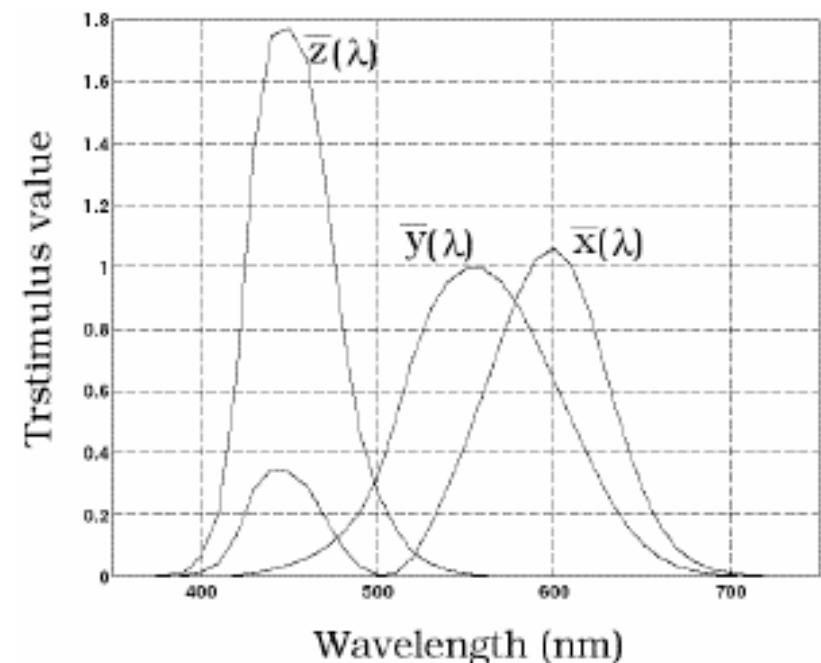
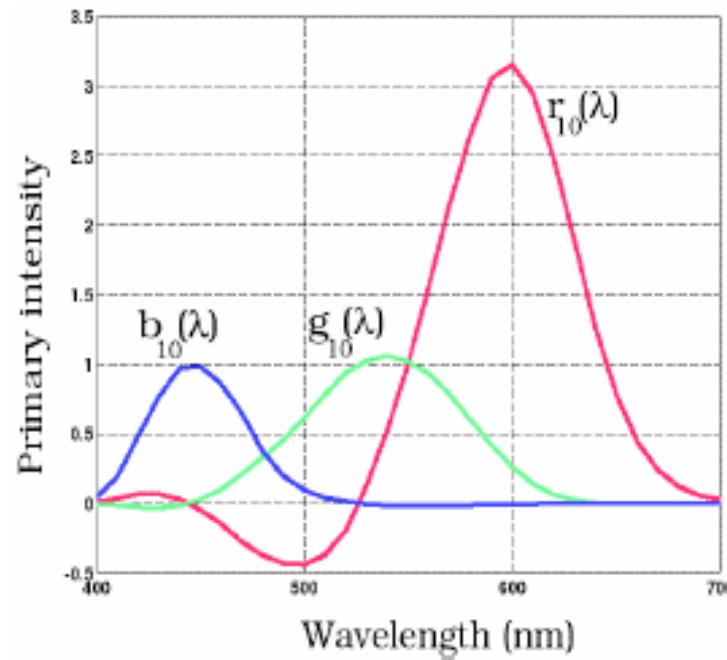
- TA office hours in lab for P2/H2 questions this week
  - Mon 3-5 (Shailen)
  - Tue 3:30-5 (Kai)
  - Wed 3-5 (Shailen)
  - Thu 3-5 (Kai)
  - Fri 2-4 (Garrett)
- again - start **now**, do not put off until late in break!

# Review: Trichromacy and Metamers

- three types of cones
- color is combination of cone stimuli
  - metamer: identically perceived color caused by very different spectra



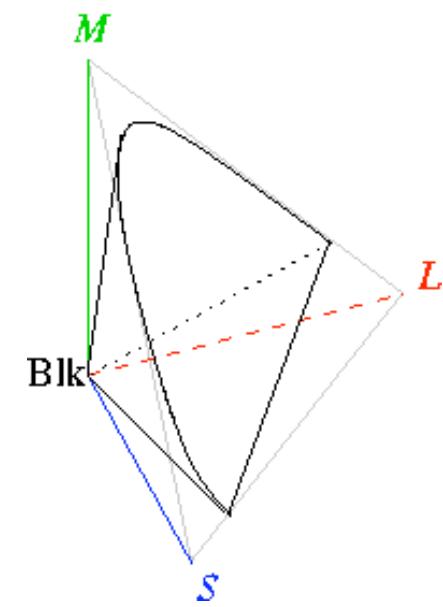
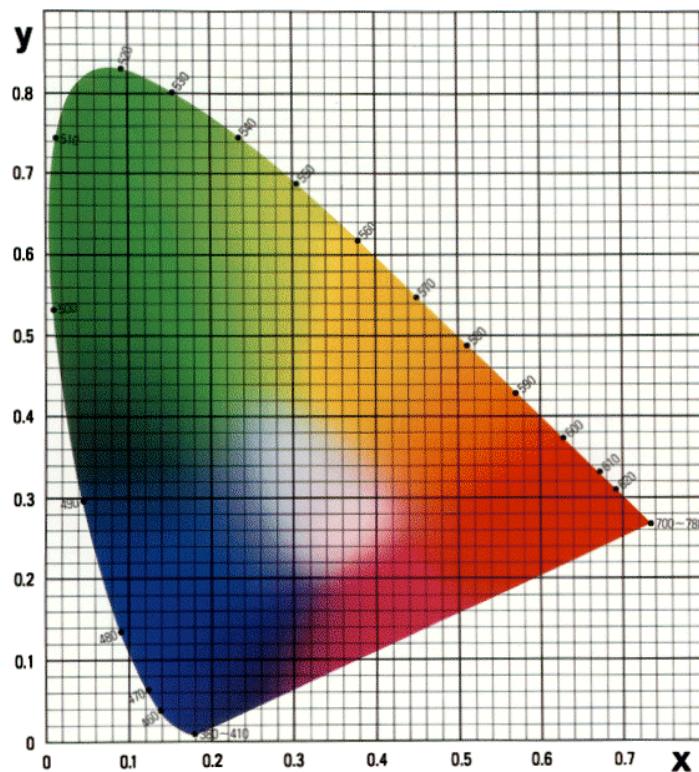
# Review: Measured vs. CIE Color Spaces



- measured basis
  - monochromatic lights
  - physical observations
  - negative lobes
- transformed basis
  - “imaginary” lights
  - all positive, unit area
  - Y is luminance

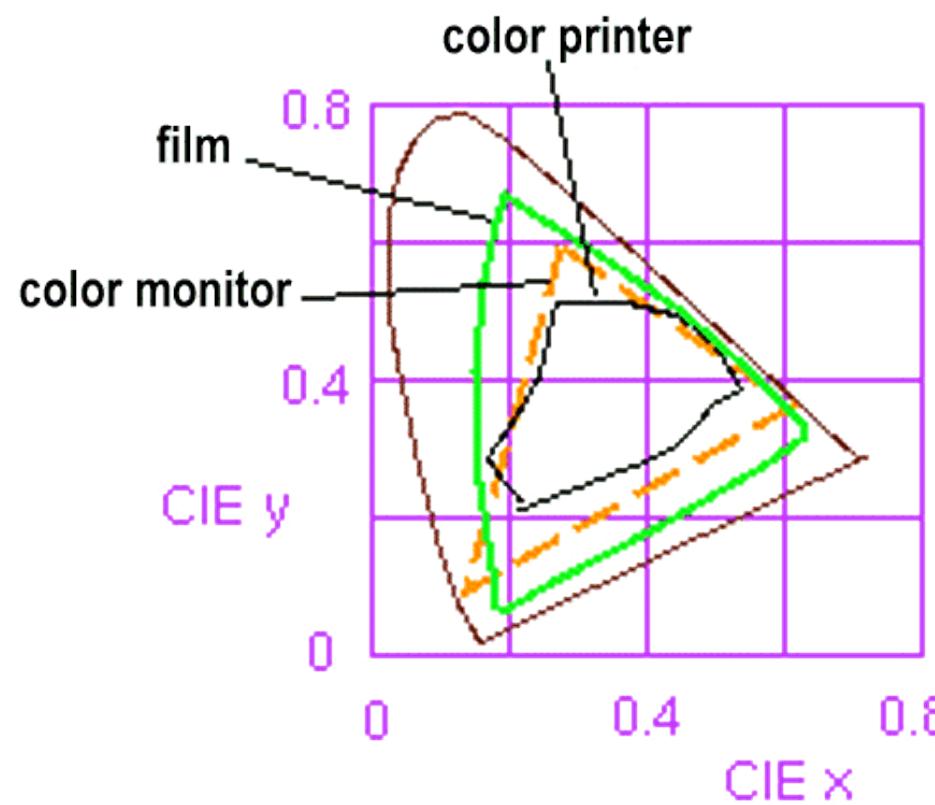
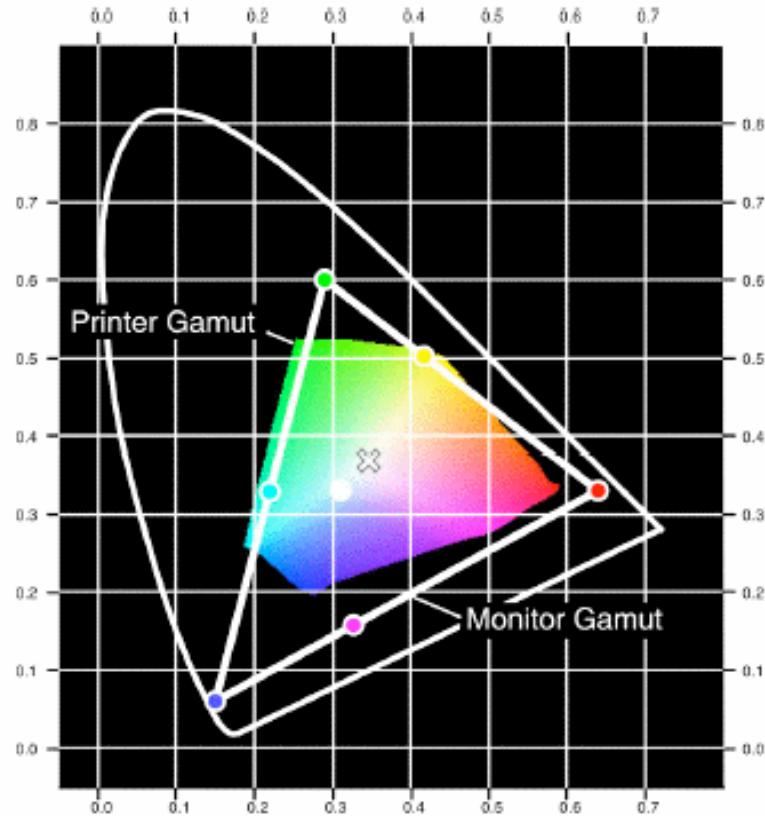
# Review: Chromaticity Diagram

- plane of equal brightness showing chromaticity

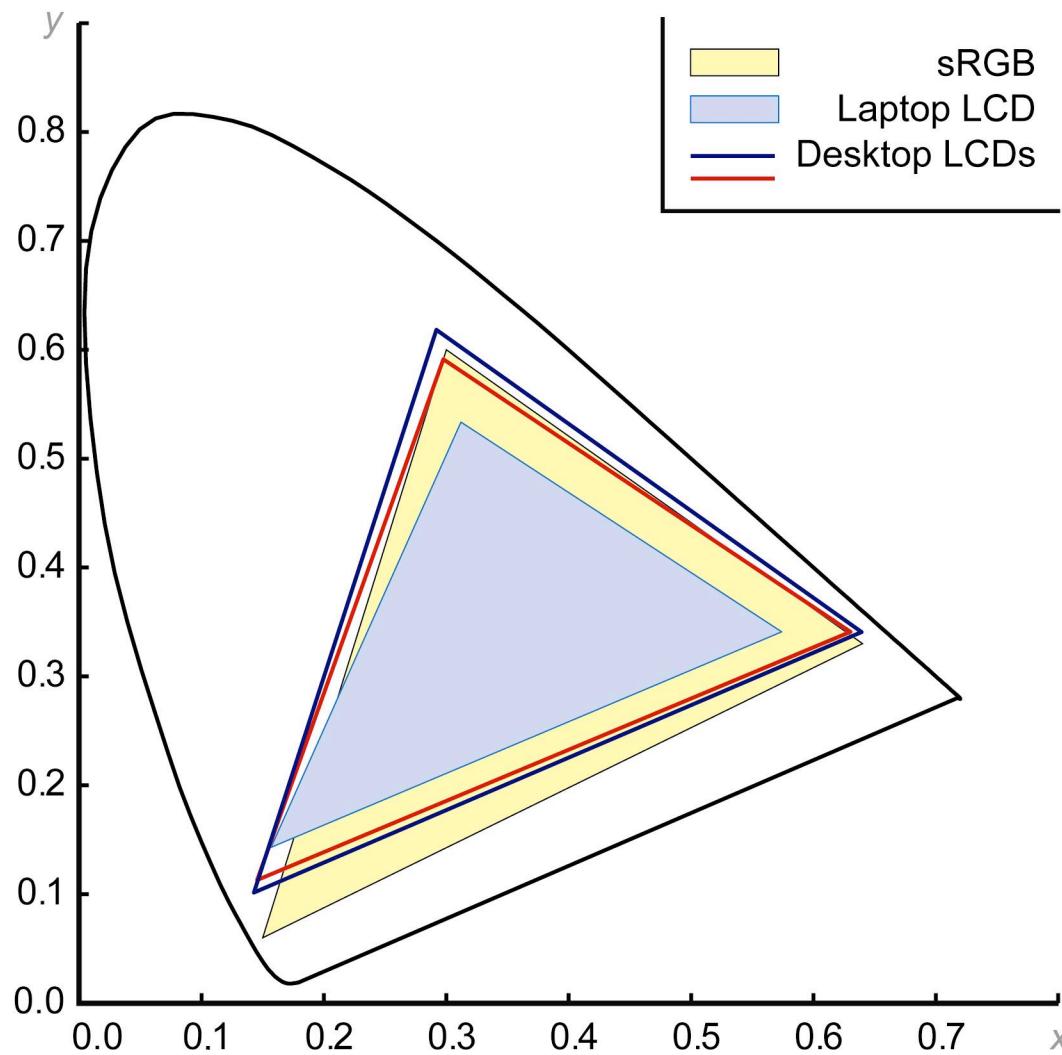


# Device Color Gamuts

- gamut is polygon, device primaries at corners
  - defines reproducible color range
  - X, Y, and Z are hypothetical light sources, no device can produce entire gamut

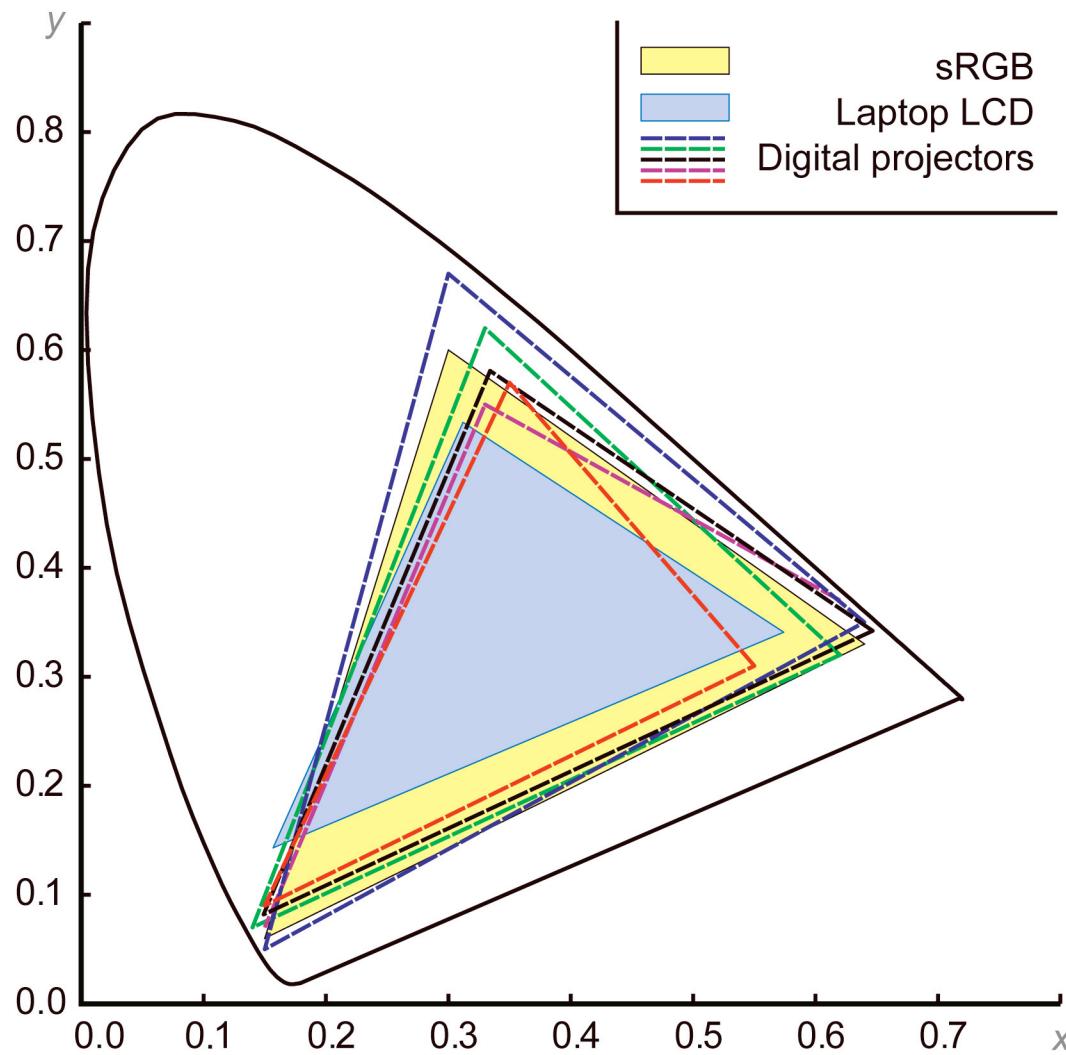


# Display Gamuts



From A Field Guide to Digital Color, © A.K. Peters, 2003

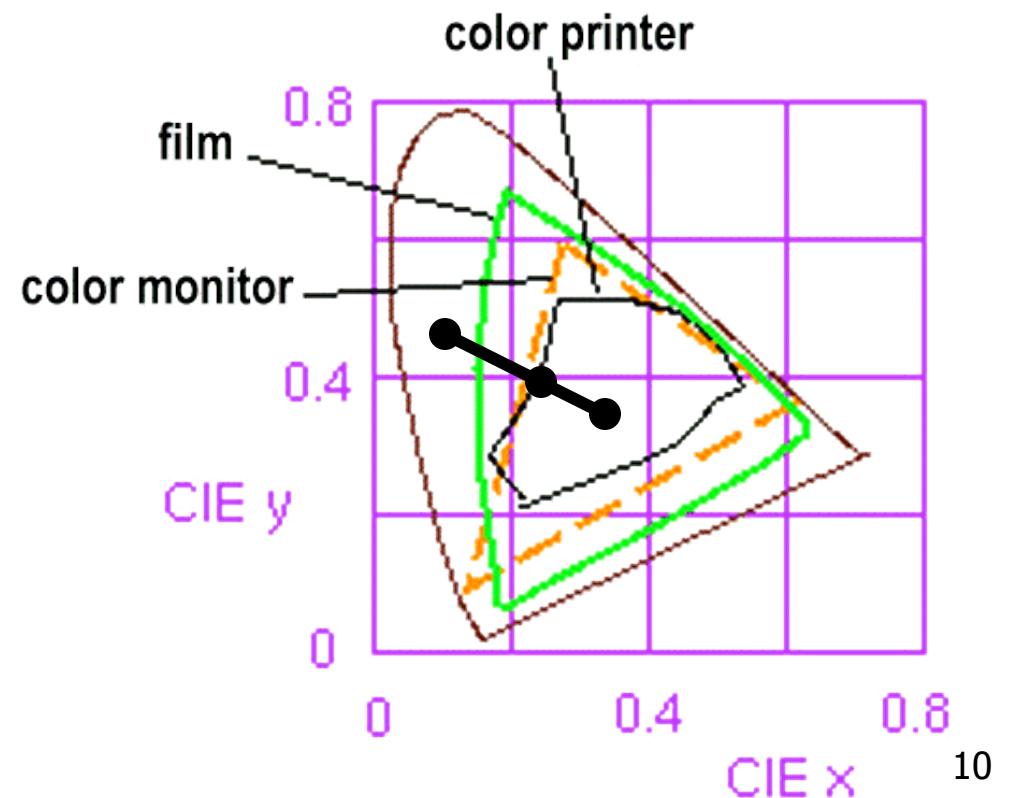
# Projector Gamuts



*From A Field Guide to Digital Color, © A.K. Peters, 2003*

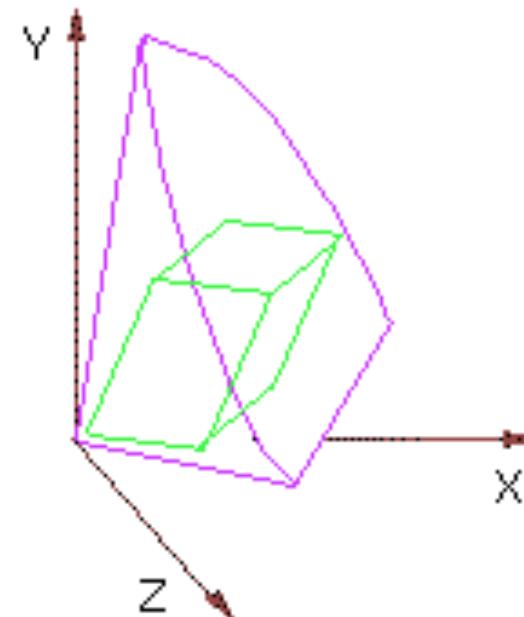
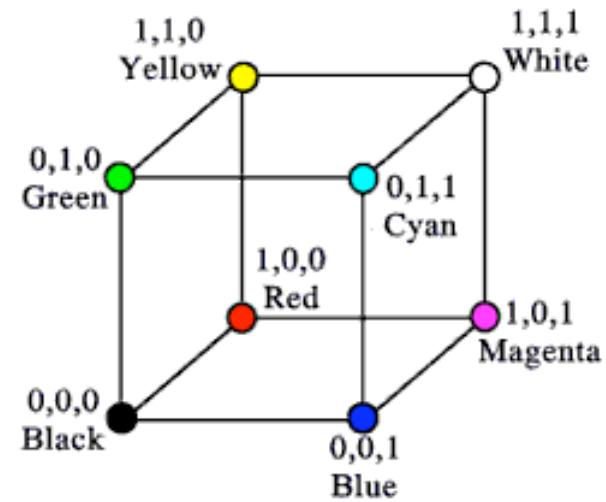
# Gamut Mapping

- how to handle colors outside gamut?
  - one way: construct ray to white point, find closest displayable point within gamut



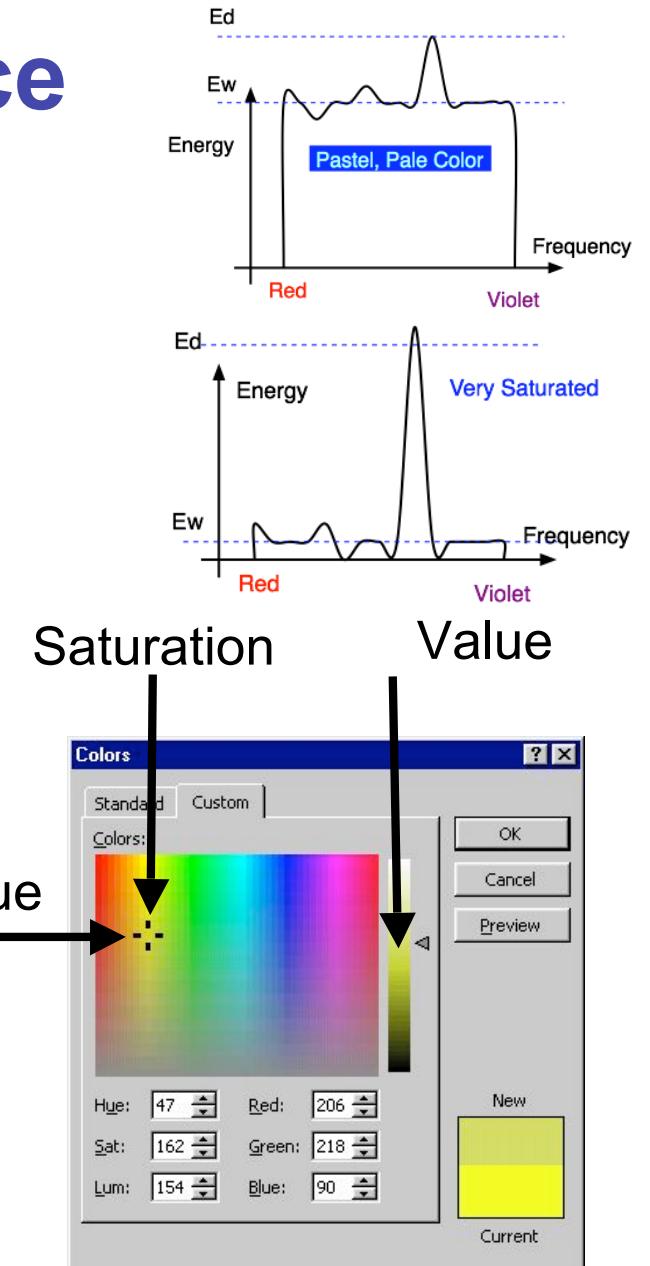
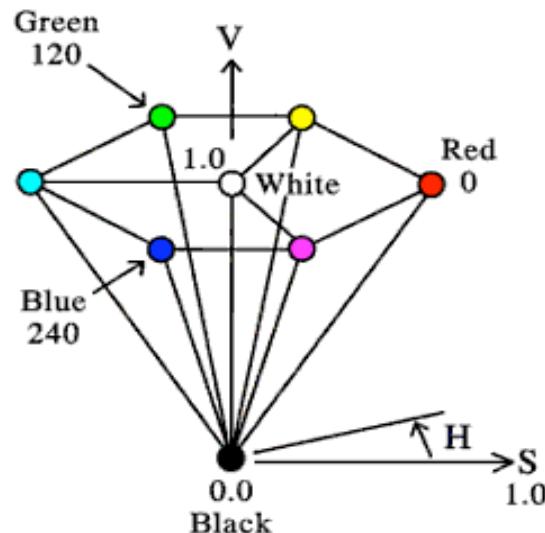
# RGB Color Space (Color Cube)

- define colors with  $(r, g, b)$  amounts of red, green, and blue
  - used by OpenGL
  - hardware-centric
- RGB color cube sits within CIE color space
  - subset of perceivable colors
  - scale, rotate, shear cube



# HSV Color Space

- more intuitive color space for people
  - $H$  = Hue
    - dominant wavelength, “color”
  - $S$  = Saturation
    - how far from grey/white
  - $V$  = Value
    - how far from black/white
    - also: brightness B, intensity I, lightness L



# HSI/HSV and RGB

- HSV/HSI conversion from RGB not expressible in matrix
  - H=hue same in both
  - V=value is max, I=intensity is average

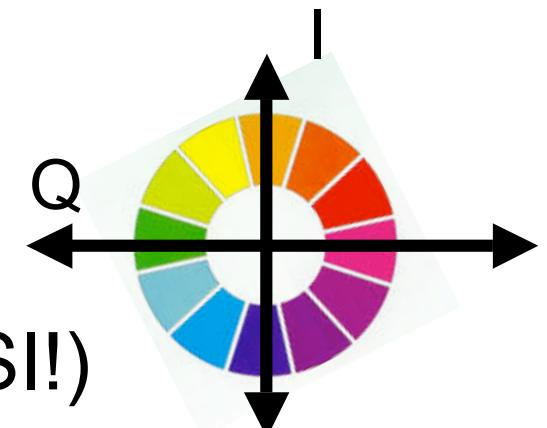
$$H = \cos^{-1} \left[ \frac{\frac{1}{2}[(R - G) + (R - B)]}{\sqrt{(R - G)^2 + (R - B)(G - B)}} \right] \text{ if } (B > G), \\ H = 360 - H$$

$$\text{HSI: } S = 1 - \frac{\min(R, G, B)}{I} \quad I = \frac{R + G + B}{3}$$

$$\text{HSV: } S = 1 - \frac{\min(R, G, B)}{V} \quad V = \max(R, G, B)$$

# YIQ Color Space

- color model used for color TV
  - Y is luminance (same as CIE)
  - I & Q are color (not same I as HSI!)
  - using Y backwards compatible for B/W TVs
  - conversion from RGB is linear



- expressible with matrix multiply

$$\begin{bmatrix} Y \\ I \\ Q \end{bmatrix} = \begin{bmatrix} 0.30 & 0.59 & 0.11 \\ 0.60 & -0.28 & -0.32 \\ 0.21 & -0.52 & 0.31 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

- green is much lighter than red, and red lighter than blue

# Luminance vs. Intensity

- luminance
  - Y of YIQ
  - $0.299R + 0.587G + 0.114B$
  - captures important factor
- intensity/brightness
  - I/V/B of HSI/HSV/HSB
  - $0.333R + 0.333G + 0.333B$
  - not perceptually based



(a) Colour Image



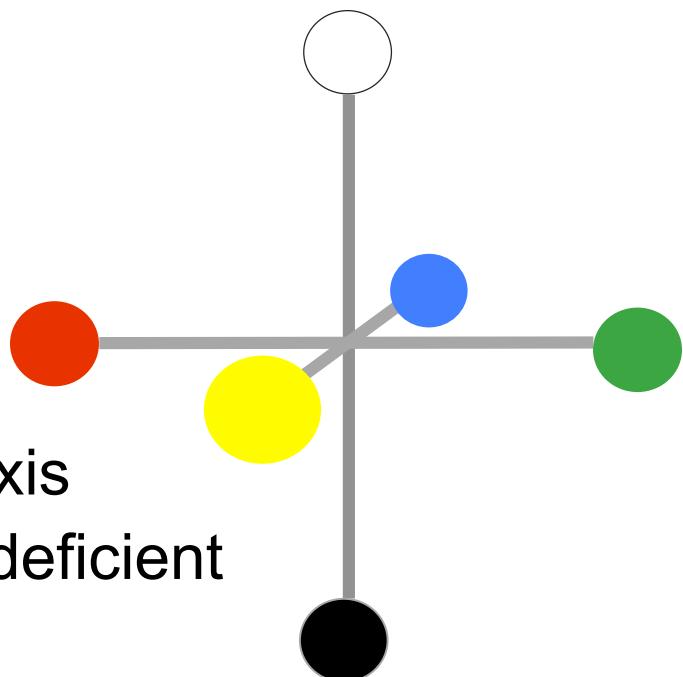
(b) Intensity Image



(c) Luminance Image

# Opponent Color

- definition
  - achromatic axis
  - R-G and Y-B axis
  - separate lightness from chroma channels
- first level encoding
  - linear combination of LMS
  - before optic nerve
  - basis for perception
  - “color blind” = color deficient
    - degraded/no acuity on one axis
    - 8%-10% men are red/green deficient



- simulates color vision deficiencies



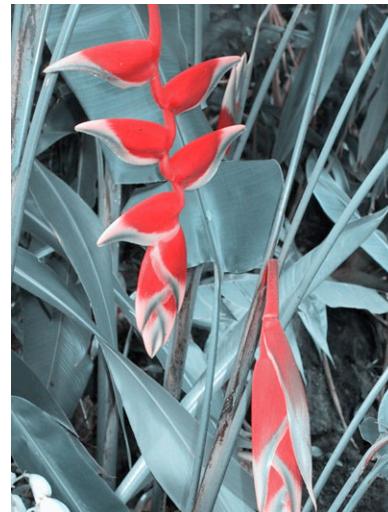
Normal vision



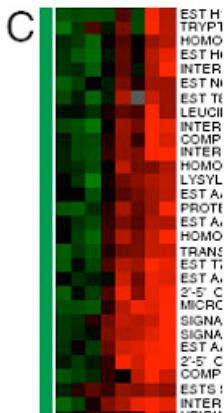
Deutanope



Protanope

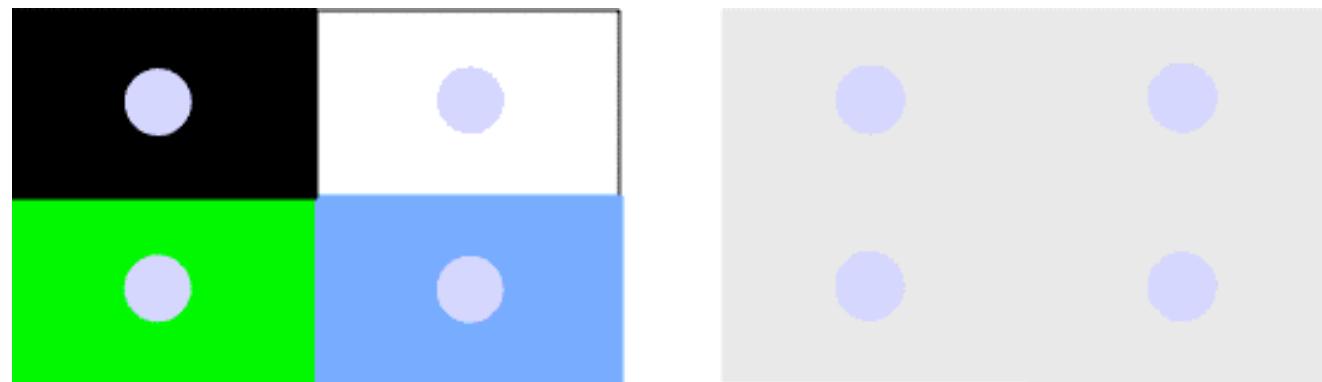


Tritanope



# Color/Lightness Constancy

- color perception depends on surrounding
  - colors in close proximity
    - simultaneous contrast effect



- illumination under which the scene is viewed

# Color/Lightness Constancy

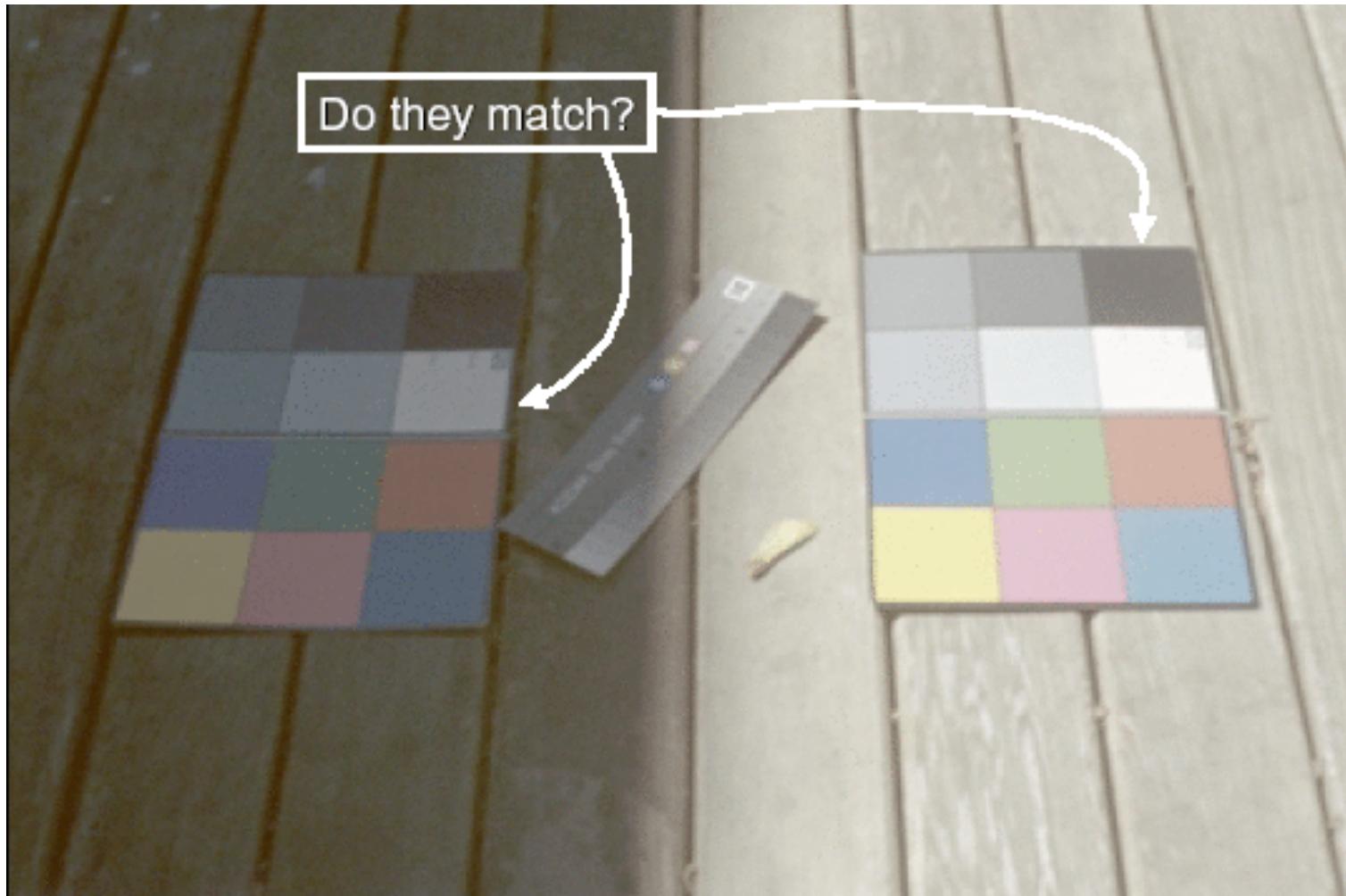


Image courtesy of John McCann

# Color/Lightness Constancy

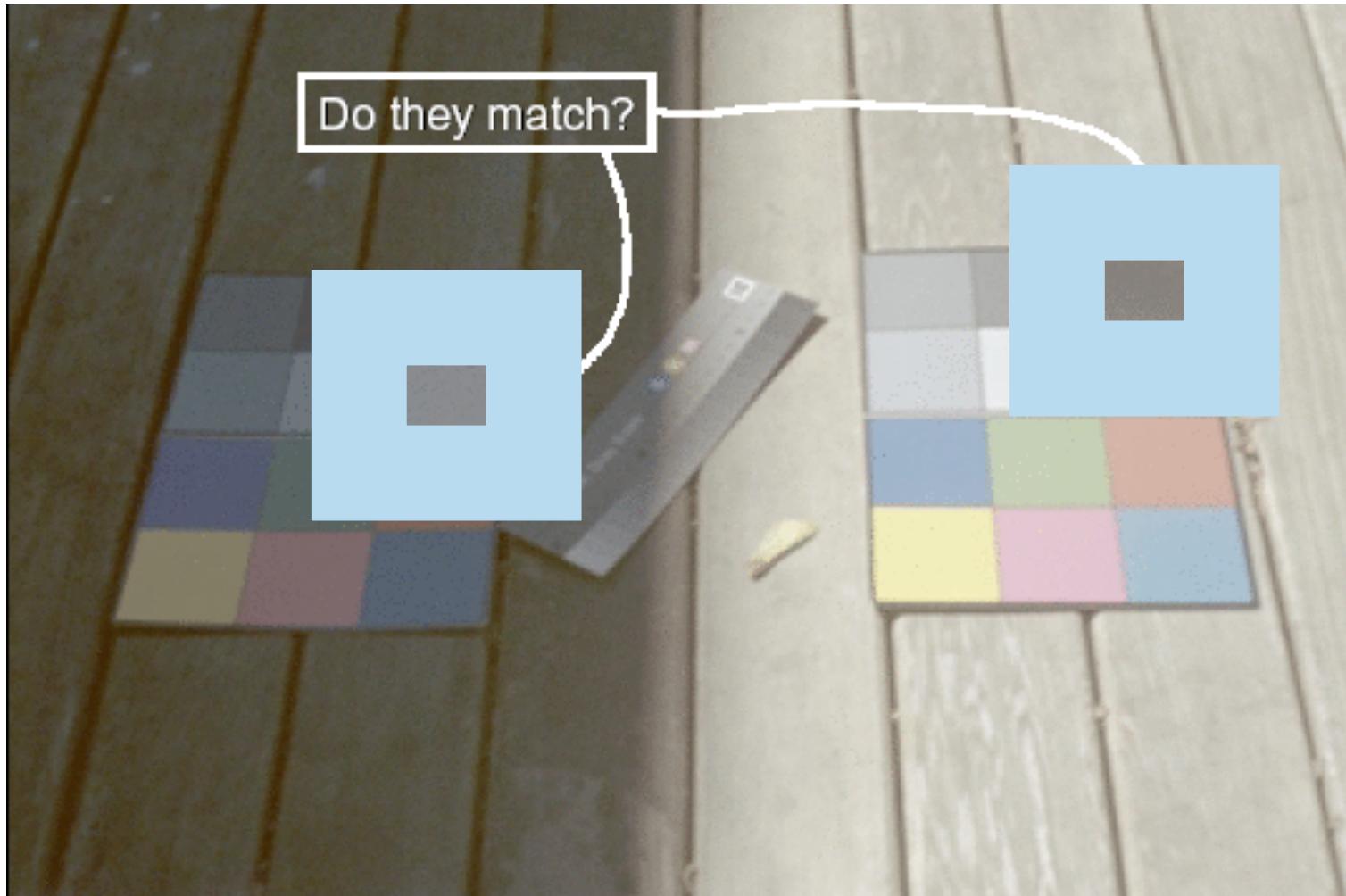


Image courtesy of John McCann

# Color Constancy

- automatic “white balance” from change in illumination
- vast amount of processing behind the scenes!
- colorimetry vs. perception



From Color Appearance Models, fig 8-1

# Stroop Effect

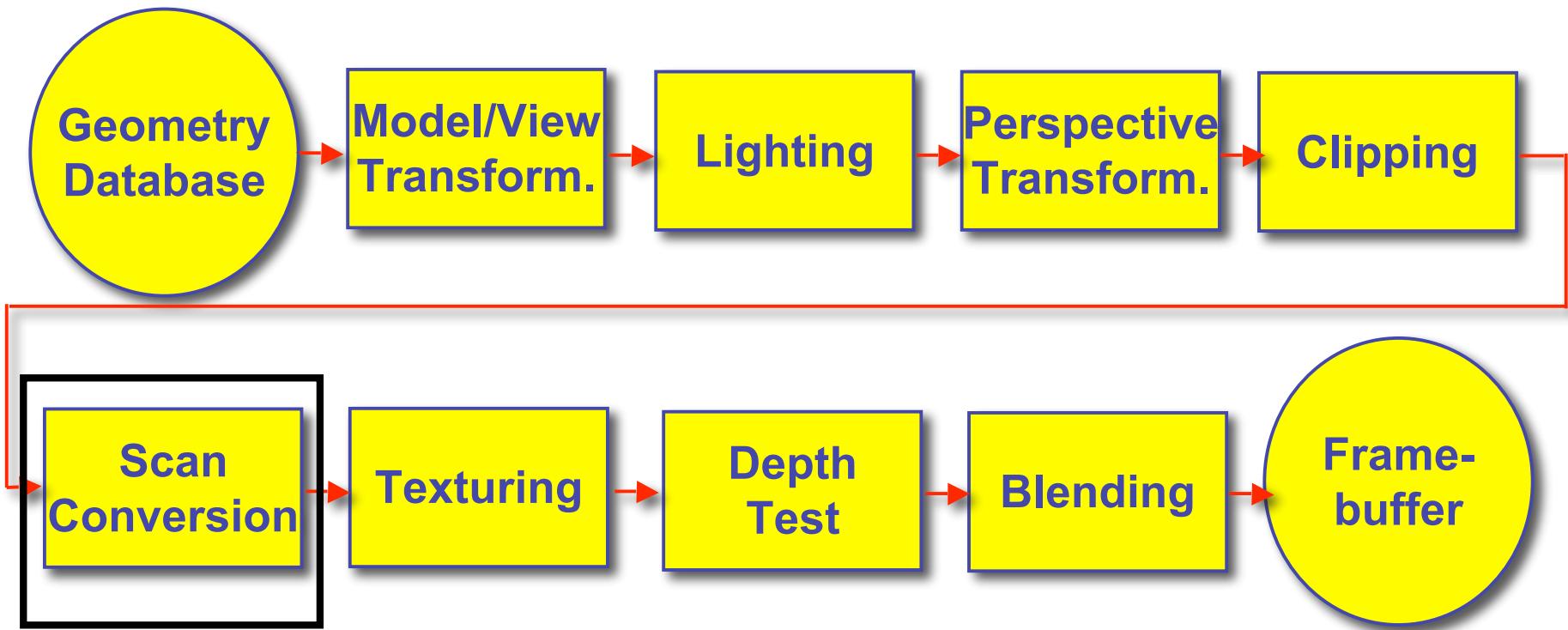
- **red**
- **blue**
- **orange**
- **purple**
- **green**

# Stroop Effect

- blue
- green
- purple
- red
- orange
  
- interplay between cognition and perception

# Rasterization

# Rendering Pipeline

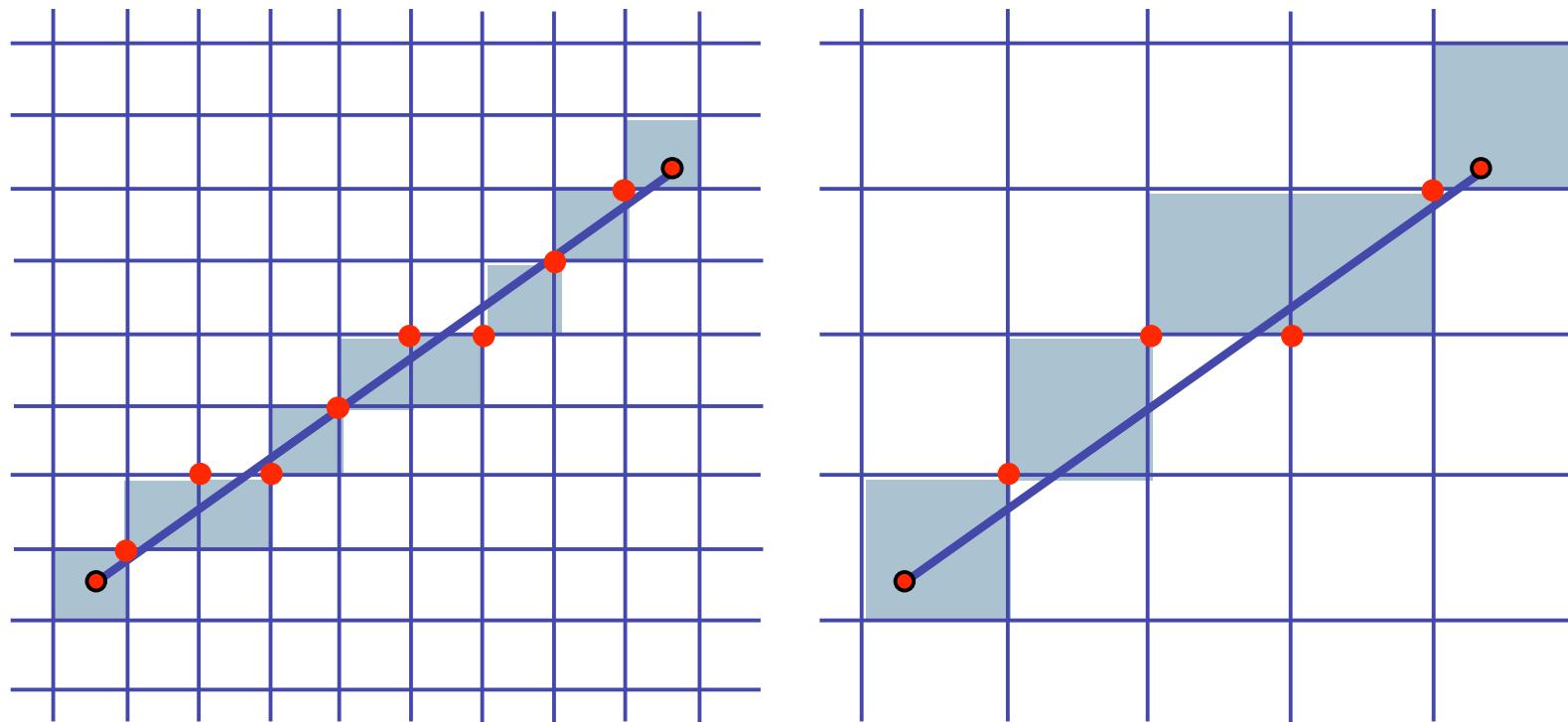


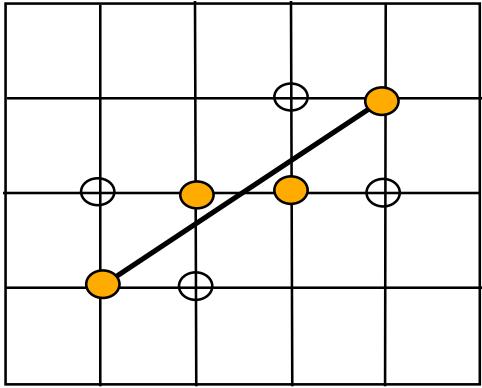
# Scan Conversion - Rasterization

- convert continuous rendering primitives into discrete fragments/pixels
  - lines
    - midpoint/Bresenham
  - triangles
    - flood fill
    - scanline
    - implicit formulation
  - interpolation

# Scan Conversion

- given vertices in DCS, fill in the pixels
- display coordinates required to provide scale for discretization
  - [demo]





# Basic Line Drawing

$$y = mx + b$$

$$y = \frac{(y_1 - y_0)}{(x_1 - x_0)}(x - x_0) + y_0$$

- goals
  - integer coordinates
  - thinnest line with no gaps
- assume
  - $x_0 < x_1$  slope  $0 < \frac{dy}{dx} < 1$
  - one octant, other cases symmetric
- how can we do this more quickly?

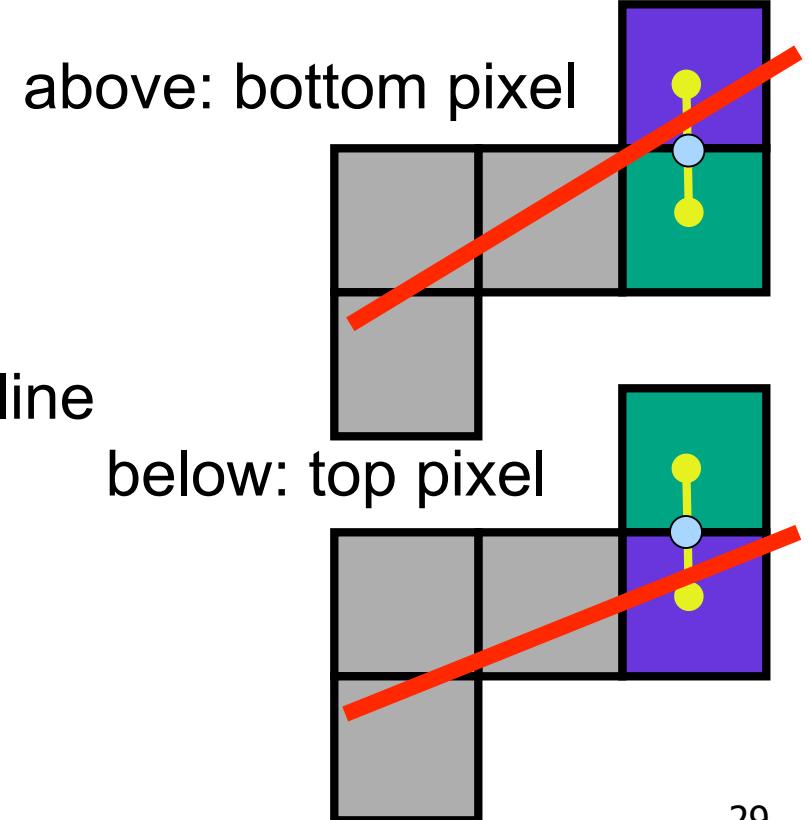
```

Line(  $x_0, y_0, x_1, y_1$  )
begin
  float  $dx, dy, x, y, slope$ ;
   $dx \Leftarrow x_1 - x_0$ ;
   $dy \Leftarrow y_1 - y_0$ ;
   $slope \Leftarrow \frac{dy}{dx}$ ;
   $y \Leftarrow y_0$ 
  for  $x$  from  $x_0$  to  $x_1$  do
    begin
      PlotPixel(  $x, \textbf{Round}(y)$  );
       $y \Leftarrow y + slope$ ;
    end;
  end;

```

# Midpoint Algorithm

- we're moving horizontally along x direction
  - only two choices: draw at current y value, or move up vertically to  $y+1$ ?
    - check if midpoint between two possible pixel centers above or below line
- candidates
  - top pixel:  $(x+1, y+1)$
  - bottom pixel:  $(x+1, y)$
- midpoint:  $(x+1, y+.5)$
- check if midpoint above or below line
  - below: pick top pixel
  - above: pick bottom pixel
- key idea behind Bresenham
  - [demo]



# Making It Fast: Reuse Computation

- midpoint: if  $f(x+1, y+.5) < 0$  then  $y = y+1$
- on previous step evaluated  $f(x-1, y-.5)$  or  $f(x-1, y+.05)$
- $f(x+1, y) = f(x,y) + (y_0-y_1)$
- $f(x+1, y+1) = f(x,y) + (y_0-y_1) + (x_1-x_0)$

```
y=y0
d = f(x0+1, y0+.5)
for (x=x0; x <= x1; x++) {
    draw(x,y);
    if (d<0) then {
        y = y + 1;
        d = d + (x1 - x0) + (y0 - y1)
    } else {
        d = d + (y0 - y1)
    }
}
```

# Making It Fast: Integer Only

- avoid dealing with non-integer values by doubling both sides

```
y=y0  
d = f(x0+1, y0+.5)  
for (x=x0; x <= x1; x++)  
{  
    draw(x,y);  
    if (d<0) then {  
        y = y + 1;  
        d = d + (x1 - x0) +  
             (y0 - y1)  
    } else {  
        d = d + (y0 - y1)  
    }  
}
```

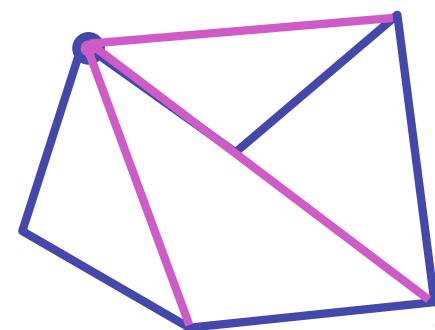
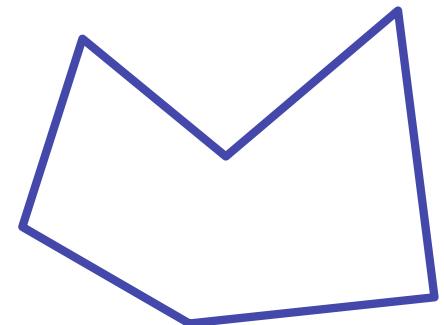
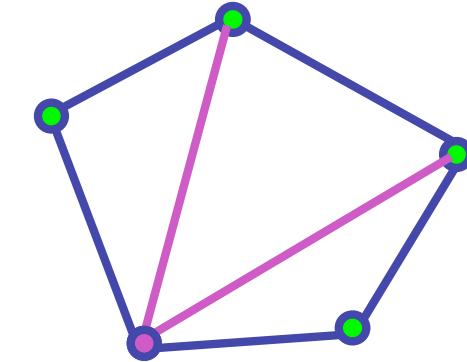
```
y=y0  
2d = 2*(y0-y1)(x0+1) +  
(x1-x0)(2y0+1) +  
2x0y1 - 2x1y0  
for (x=x0; x <= x1; x++) {  
    draw(x,y);  
    if (d<0) then {  
        y = y + 1;  
        d = d + 2(x1 - x0) +  
              2(y0 - y1)  
    } else {  
        d = d + 2(y0 - y1)  
    }  
}
```

# Rasterizing Polygons/Triangles

- basic surface representation in rendering
- why?
  - lowest common denominator
    - can approximate any surface with arbitrary accuracy
      - all polygons can be broken up into triangles
    - guaranteed to be:
      - planar
      - triangles - convex
    - simple to render
      - can implement in hardware

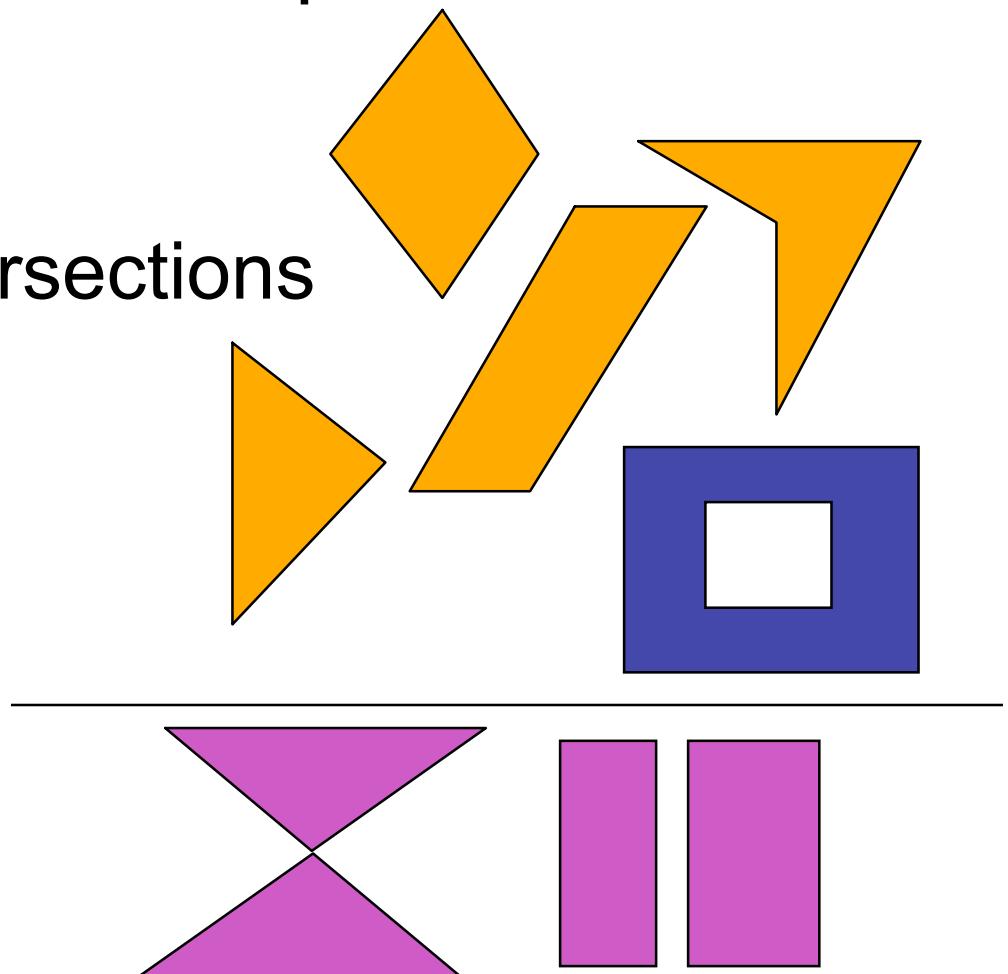
# Triangulating Polygons

- simple convex polygons
  - trivial to break into triangles
  - pick one vertex, draw lines to all others not immediately adjacent
  - OpenGL supports automatically
    - glBegin(GL\_POLYGON) ... glEnd()
- concave or non-simple polygons
  - more effort to break into triangles
  - simple approach may not work
  - OpenGL can support at extra cost
    - gluNewTess(), gluTessCallback(), ...



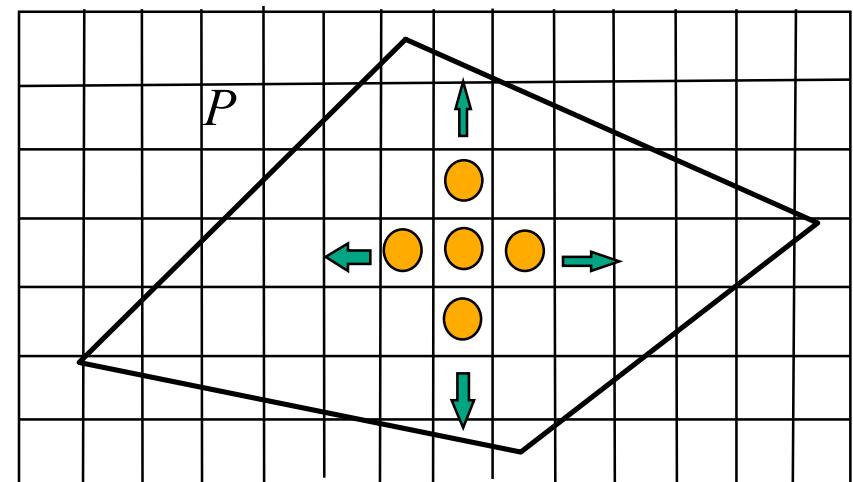
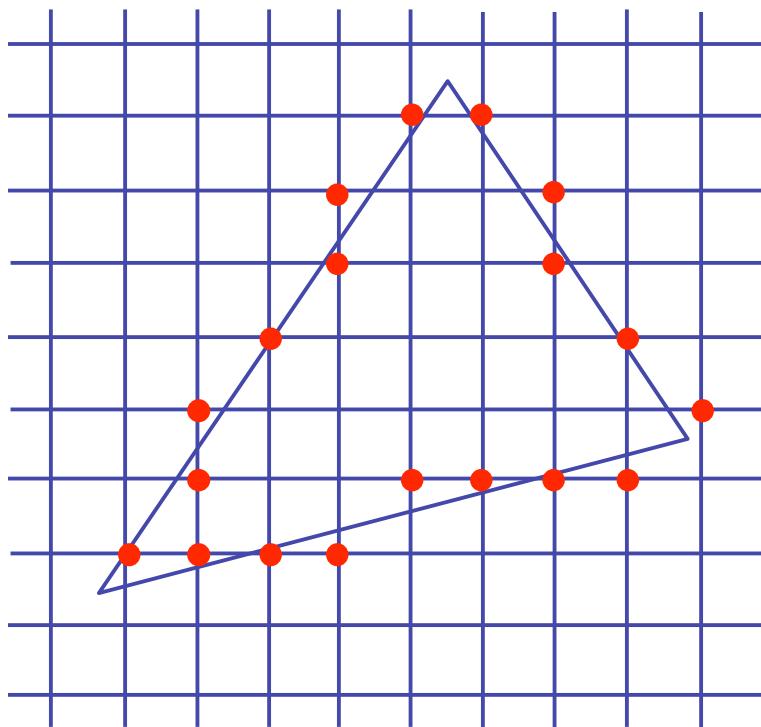
# Problem

- input: closed 2D polygon
- problem: fill its interior with specified color on graphics display
- assumptions
  - simple - no self intersections
  - simply connected
- solutions
  - flood fill
  - edge walking



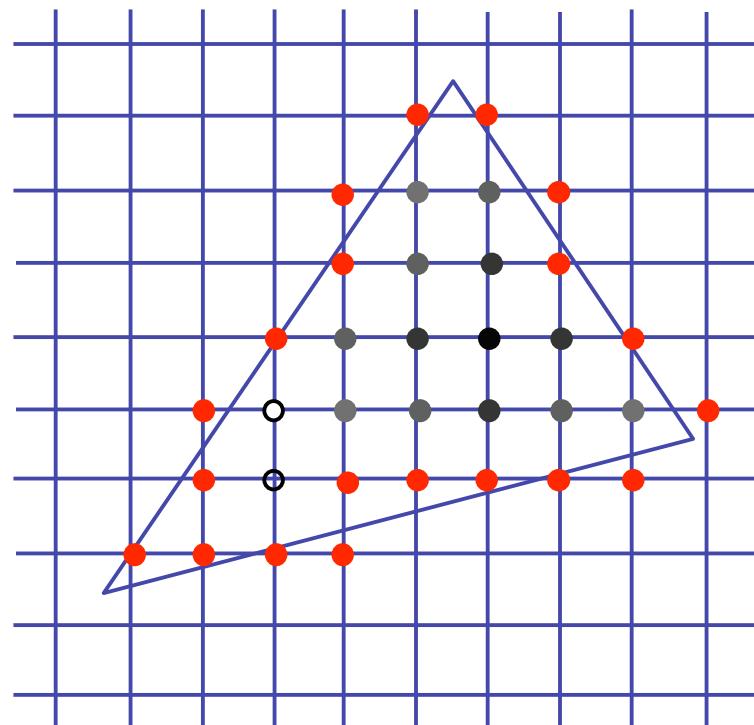
# Flood Fill

- simple algorithm
  - draw edges of polygon
  - use flood-fill to draw interior



# Flood Fill

- start with **seed point**
    - recursively set all neighbors until boundary is hit



# Flood Fill

- draw edges

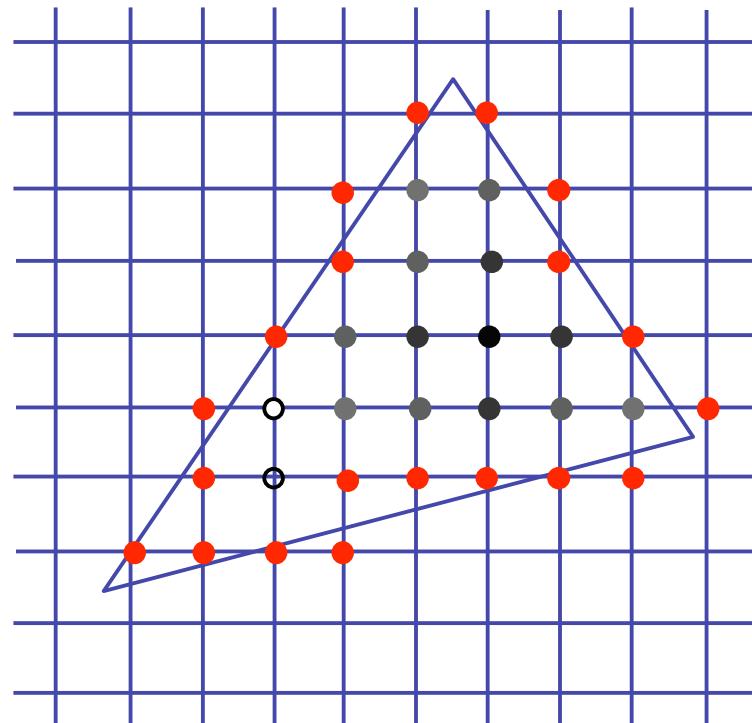
- run:

```
FloodFill(Polygon P, int x, int y, Color C)
  if not (OnBoundary(x,y,P) or Colored(x,y,C))
    begin
      PlotPixel(x,y,C);
      FloodFill(P,x + 1,y,C);
      FloodFill(P,x,y + 1,C);
      FloodFill(P,x,y - 1,C);
      FloodFill(P,x - 1,y,C);
    end ;
```

- drawbacks?

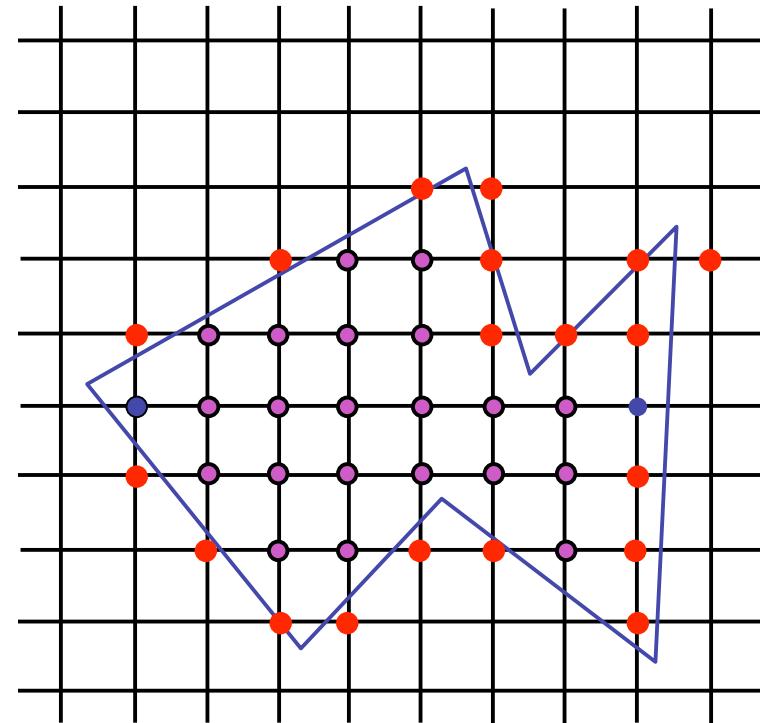
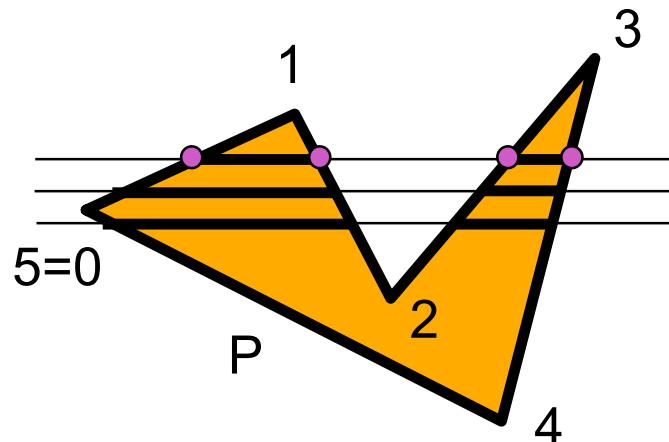
# Flood Fill Drawbacks

- pixels visited up to 4 times to check if already set
- need per-pixel flag indicating if set already
  - must clear for every polygon!



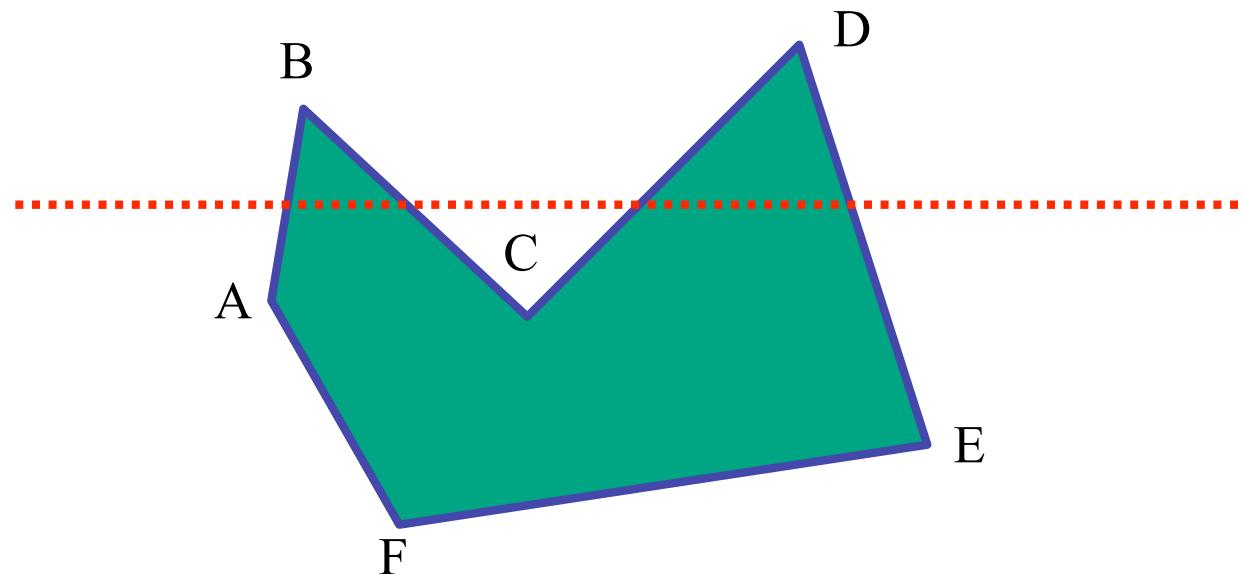
# Scanline Algorithms

- **scanline**: a line of pixels in an image
  - set pixels inside polygon boundary along horizontal lines one pixel apart vertically



# General Polygon Rasterization

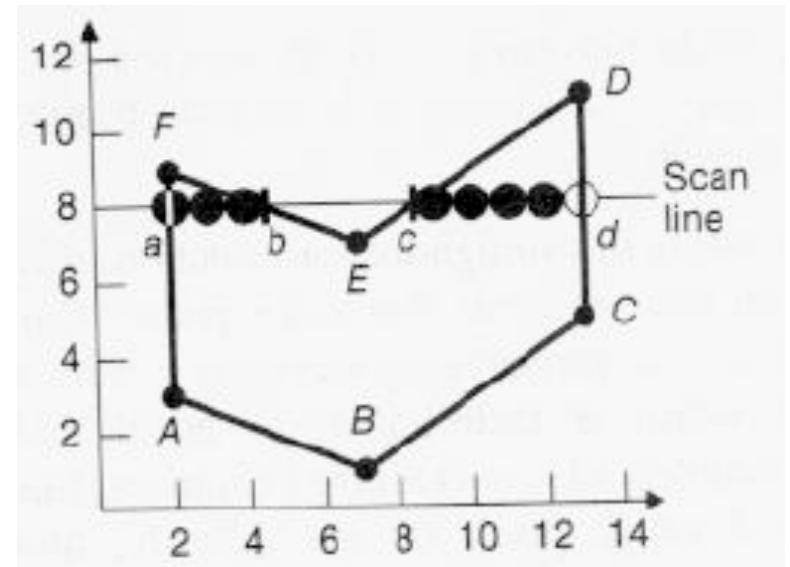
- how do we know whether given pixel on scanline is inside or outside polygon?



# General Polygon Rasterization

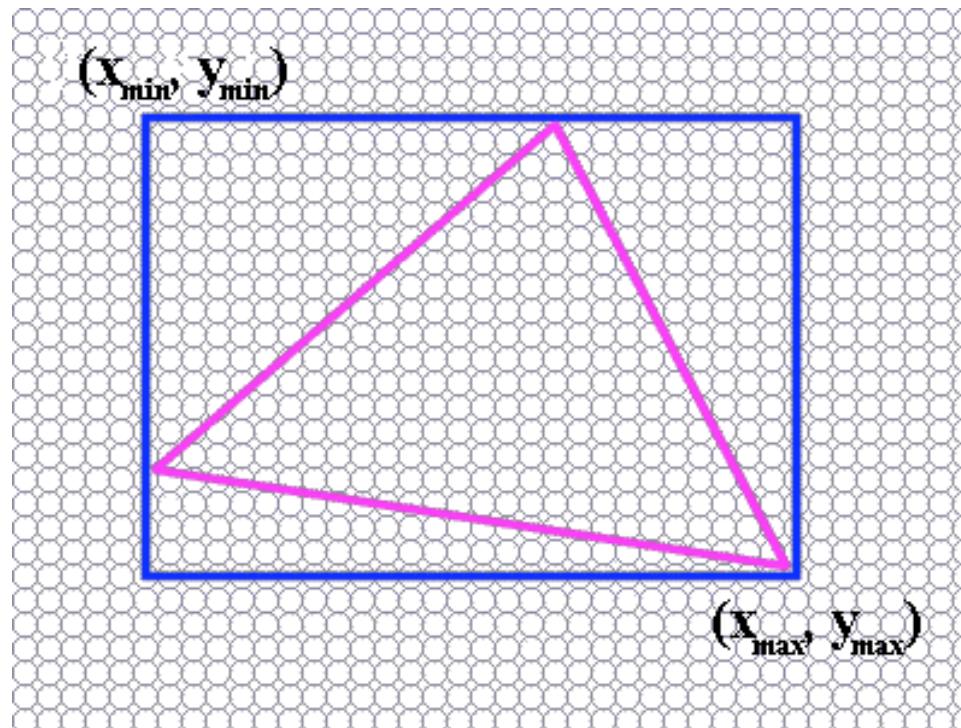
- idea: use a **parity test**

```
for each scanline
    edgeCnt = 0;
    for each pixel on scanline (1 to r)
        if (oldpixel->newpixel crosses edge)
            edgeCnt++;
        // draw the pixel if edgeCnt odd
        if (edgeCnt % 2)
            setPixel(pixel);
```



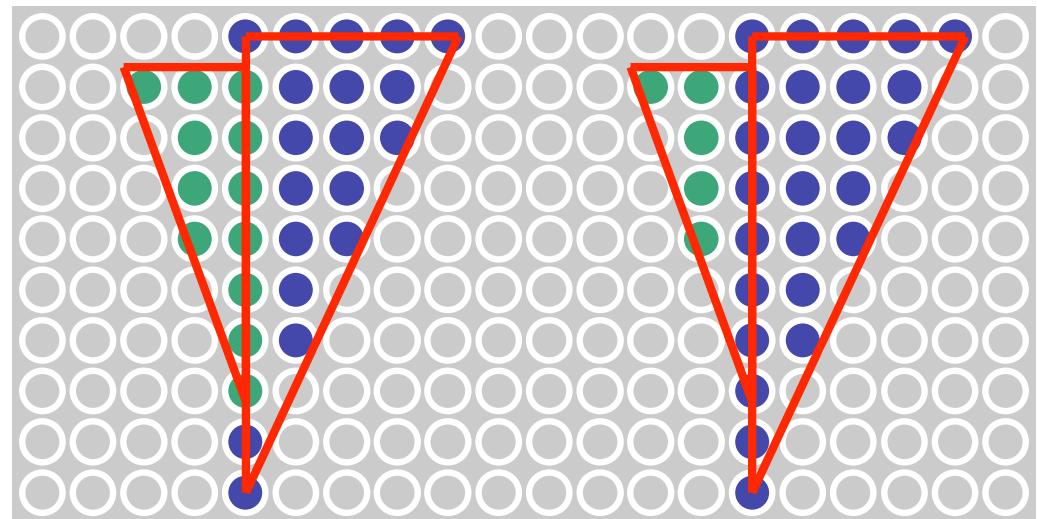
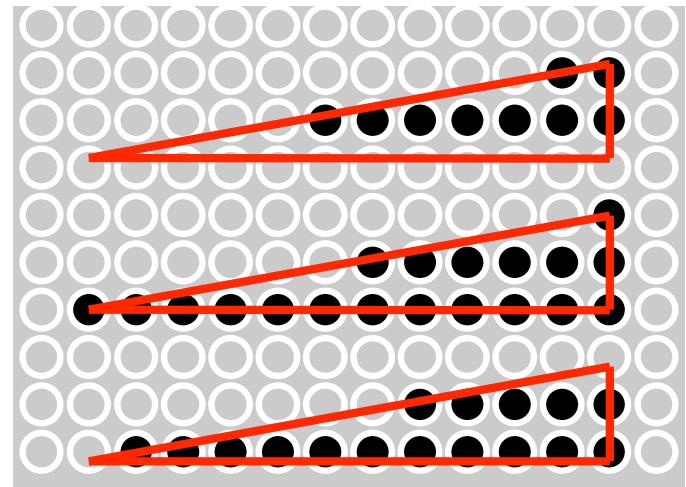
# Making It Fast: Bounding Box

- smaller set of candidate pixels
  - loop over  $x_{\min}$ ,  $x_{\max}$  and  $y_{\min}, y_{\max}$  instead of all  $x$ , all  $y$



# Triangle Rasterization Issues

- moving slivers
- shared edge ordering



# Triangle Rasterization Issues

- *exactly which pixels should be lit?*
  - pixels with centers inside triangle edges
- *what about pixels exactly on edge?*
  - draw them: order of triangles matters (it shouldn't)
  - don't draw them: gaps possible between triangles
- need a consistent (if arbitrary) rule
  - example: draw pixels on left or top edge, but not on right or bottom edge
  - example: check if triangle on same side of edge as offscreen point

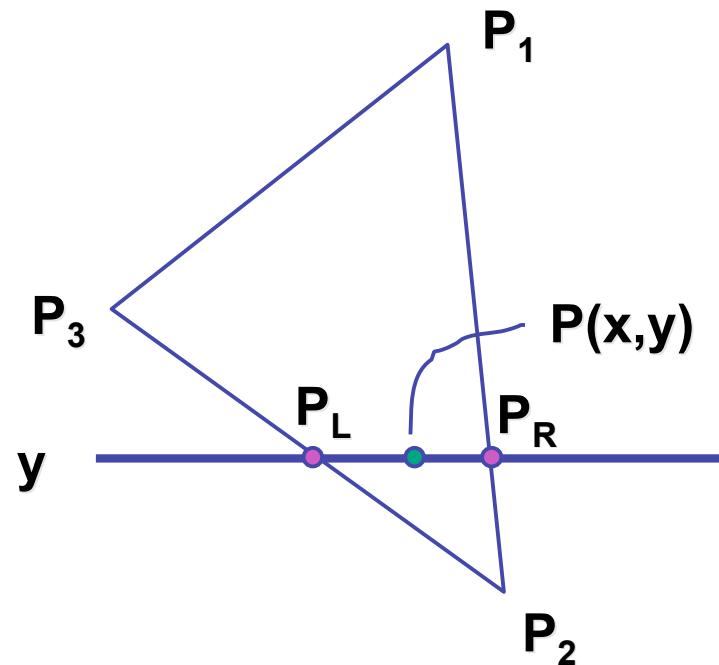
# Interpolation

# Interpolation During Scan Conversion

- drawing pixels in polygon requires interpolating many values between vertices
  - r,g,b colour components
    - use for shading
  - z values
  - u,v texture coordinates
  - $N_x, N_y, N_z$  surface normals
- equivalent methods (for triangles)
  - bilinear interpolation
  - barycentric coordinates

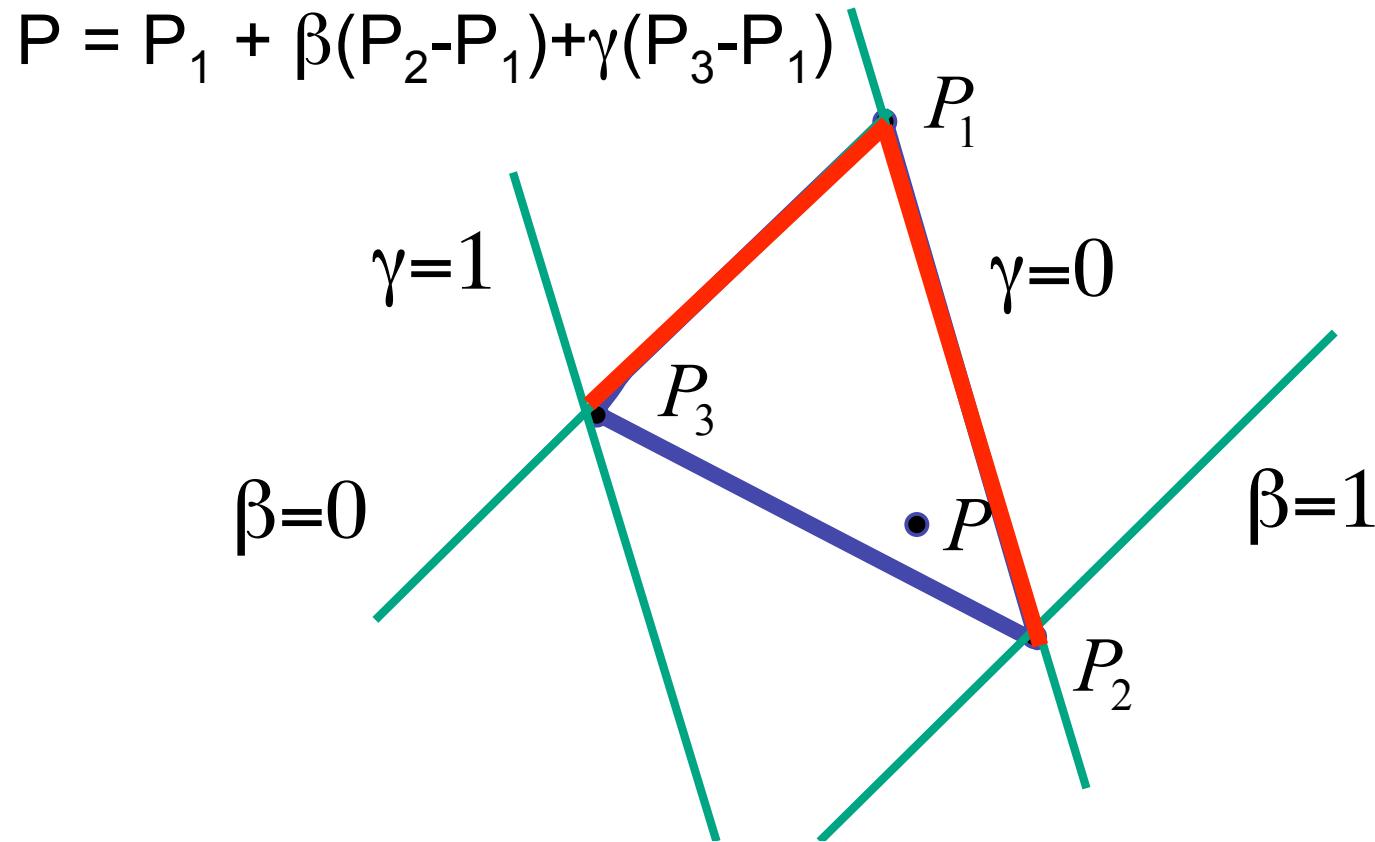
# Bilinear Interpolation

- interpolate quantity along  $L$  and  $R$  edges,  
as a function of  $y$ 
  - then interpolate quantity as a function of  $x$

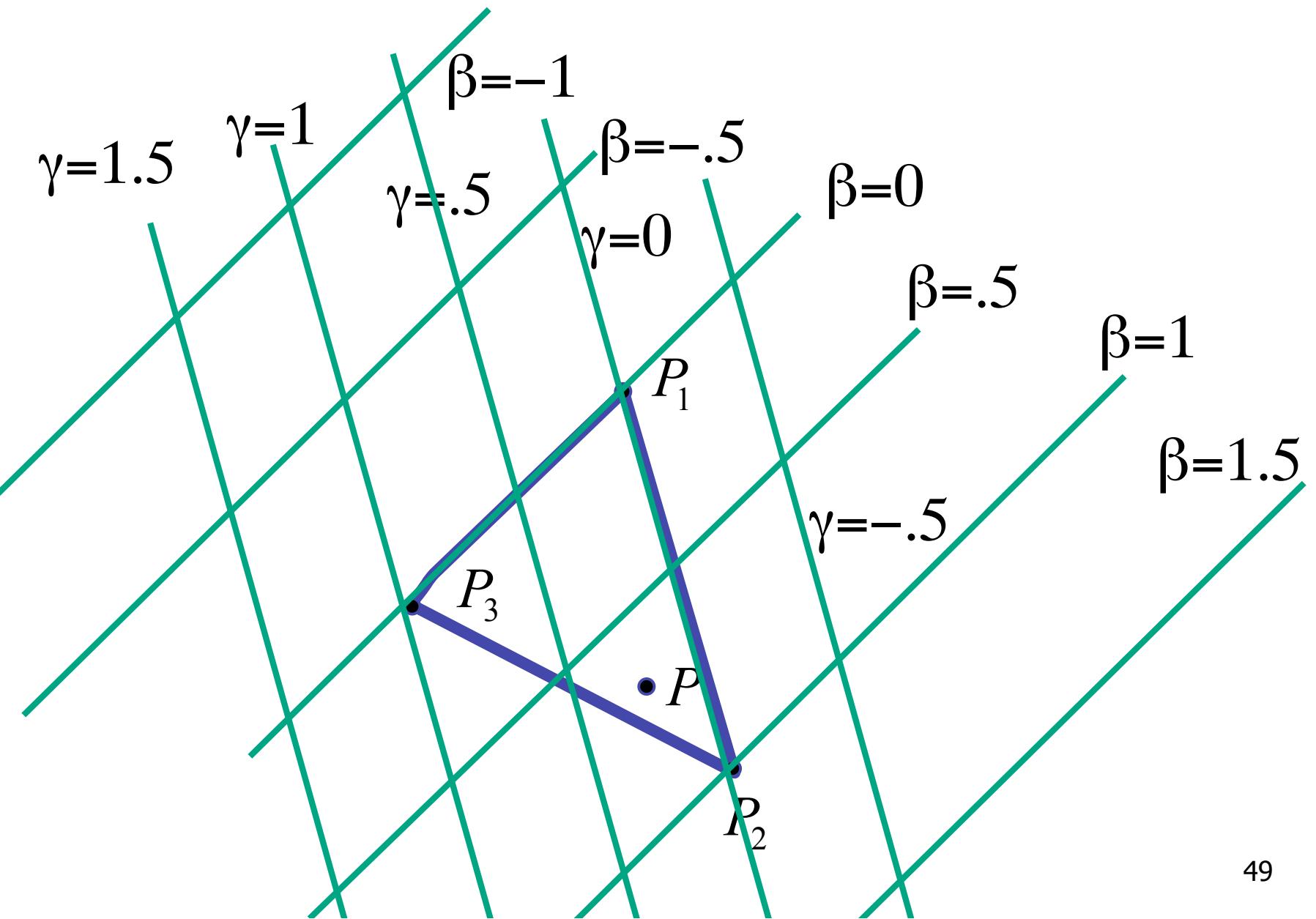


# Barycentric Coordinates

- non-orthogonal coordinate system based on triangle itself
  - origin:  $P_1$ , basis vectors:  $(P_2-P_1)$  and  $(P_3-P_1)$



# Barycentric Coordinates



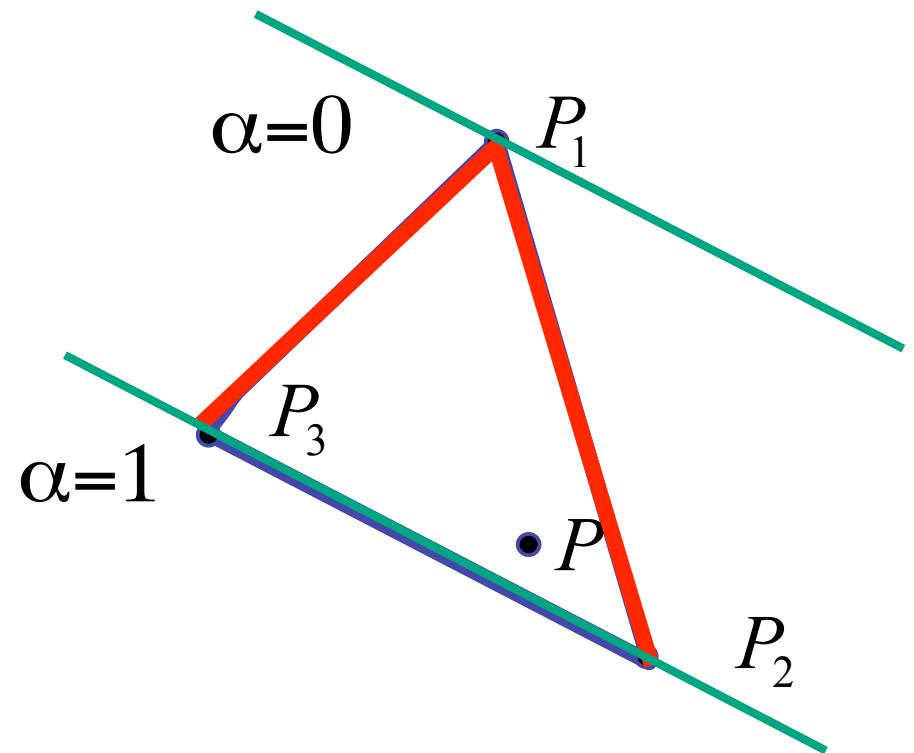
# Barycentric Coordinates

- non-orthogonal coordinate system based on triangle itself
  - origin:  $P_1$ , basis vectors:  $(P_2-P_1)$  and  $(P_3-P_1)$

$$P = P_1 + \beta(P_2 - P_1) + \gamma(P_3 - P_1)$$

$$P = (1-\beta-\gamma)P_1 + \beta P_2 + \gamma P_3$$

$$P = \alpha P_1 + \beta P_2 + \gamma P_3$$

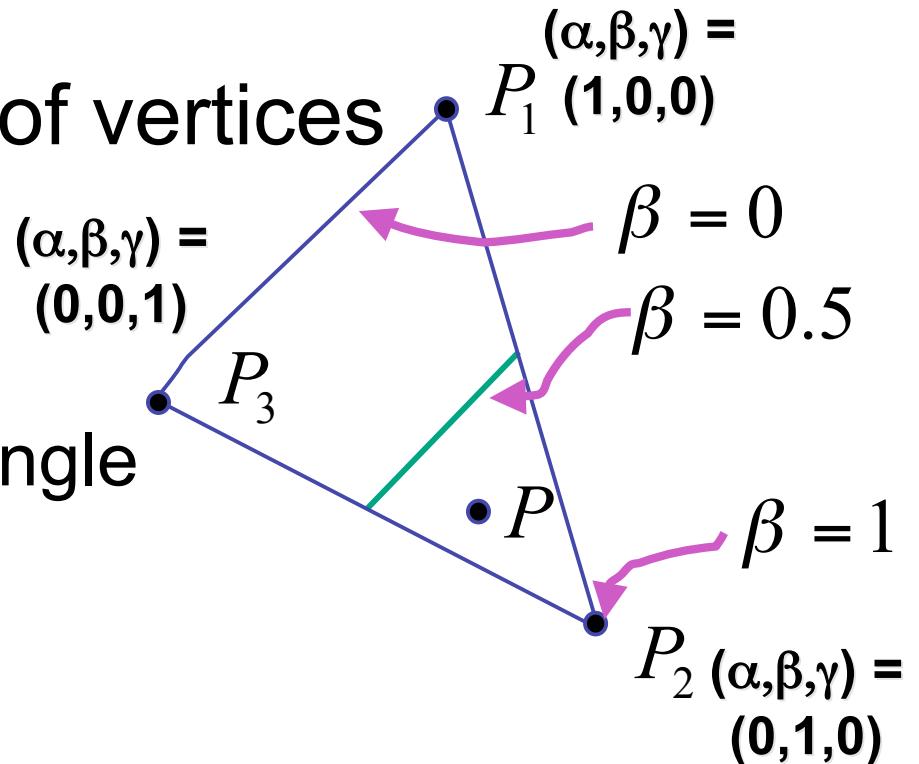


# Using Barycentric Coordinates

- weighted combination of vertices
  - smooth mixing
  - speedup
    - compute once per triangle

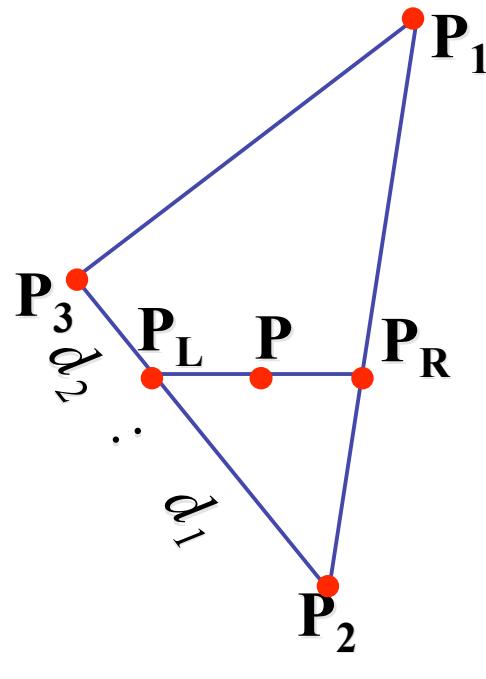
$$\left\{ \begin{array}{l} P = \alpha \cdot P_1 + \beta \cdot P_2 + \gamma \cdot P_3 \\ \alpha + \beta + \gamma = 1 \\ 0 \leq \alpha, \beta, \gamma \leq 1 \text{ for points inside triangle} \end{array} \right.$$

“convex combination  
of points”



# Deriving Barycentric From Bilinear

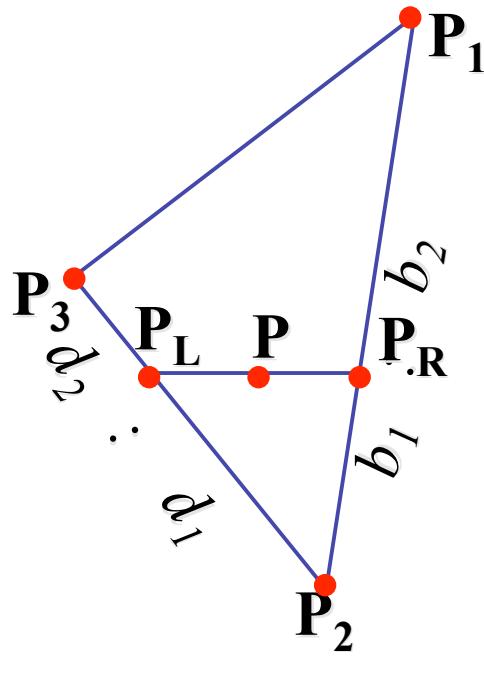
- from bilinear interpolation of point P on scanline



$$\begin{aligned}P_L &= P_2 + \frac{d_1}{d_1 + d_2}(P_3 - P_2) \\&= \left(1 - \frac{d_1}{d_1 + d_2}\right)P_2 + \frac{d_1}{d_1 + d_2}P_3 = \\&= \frac{d_2}{d_1 + d_2}P_2 + \frac{d_1}{d_1 + d_2}P_3\end{aligned}$$

# Deriving Barycentric From Bilinear

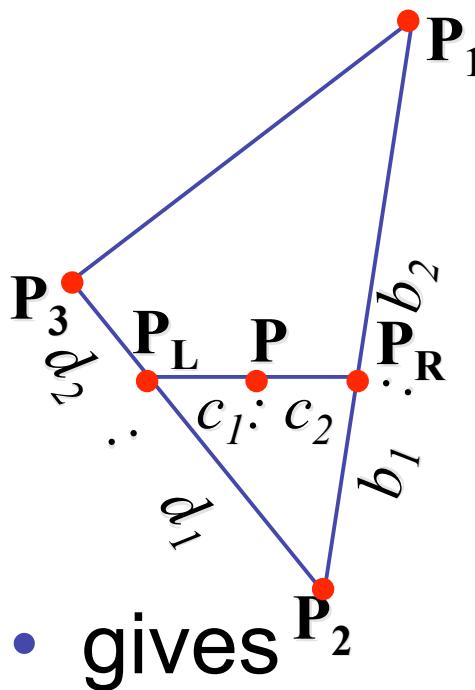
- similarly



$$\begin{aligned}P_R &= P_2 + \frac{b_1}{b_1 + b_2} (P_1 - P_2) \\&= \left(1 - \frac{b_1}{b_1 + b_2}\right) P_2 + \frac{b_1}{b_1 + b_2} P_1 = \\&= \frac{b_2}{b_1 + b_2} P_2 + \frac{b_1}{b_1 + b_2} P_1\end{aligned}$$

# Deriving Barycentric From Bilinear

- combining



- gives

$$P = \frac{c_2}{c_1 + c_2} \cdot P_L + \frac{c_1}{c_1 + c_2} \cdot P_R$$

$$P_L = \frac{d_2}{d_1 + d_2} P_2 + \frac{d_1}{d_1 + d_2} P_3$$

$$P_R = \frac{b_2}{b_1 + b_2} P_2 + \frac{b_1}{b_1 + b_2} P_1$$

$$P = \frac{c_2}{c_1 + c_2} \left( \frac{d_2}{d_1 + d_2} P_2 + \frac{d_1}{d_1 + d_2} P_3 \right) + \frac{c_1}{c_1 + c_2} \left( \frac{b_2}{b_1 + b_2} P_2 + \frac{b_1}{b_1 + b_2} P_1 \right)$$

# Deriving Barycentric From Bilinear

- thus  $P = \alpha P_1 + \beta P_2 + \gamma P_3$  with

$$\alpha = \frac{c_1}{c_1 + c_2} \frac{b_1}{b_1 + b_2}$$

$$\beta = \frac{c_2}{c_1 + c_2} \frac{d_2}{d_1 + d_2} + \frac{c_1}{c_1 + c_2} \frac{b_2}{b_1 + b_2}$$

$$\gamma = \frac{c_2}{c_1 + c_2} \frac{d_1}{d_1 + d_2}$$

- can verify barycentric properties

$$\alpha + \beta + \gamma = 1, \quad 0 \leq \alpha, \beta, \gamma \leq 1$$

# Computing Barycentric Coordinates

- 2D triangle area
  - half of parallelogram area
    - from cross product

$$A = A_{P1} + A_{P2} + A_{P3}$$

$$\alpha = A_{P1} / A$$

$$\beta = A_{P2} / A$$

$$\gamma = A_{P3} / A$$

