



Tamara Munzner

**Collision II**

**Week 11, Mon Mar 29**

<http://www.ugrad.cs.ubc.ca/~cs314/Vjan2010>

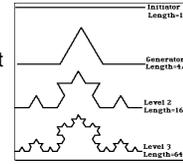
**News**

- P3 demos started today
  - signup sheet posted if you need to check time
- P4 proposals due Wed 1pm
  - give me hardcopy in class, not in box
  - electronic also ok, 'handin proj4.prop'

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**Review: Language-Based Generation**

- L-Systems
  - F: forward, R: right, L: left
- Koch snowflake:
  - F = FLFRRFLF
- Mariano's Bush:
  - F=FF-[-F+F+F]+[+F-F-F]
  - angle 16



<http://spanky.triumf.ca/www/fractint/lsys/plants.html>

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**Review: Fractal Terrain**

- 1D: midpoint displacement
  - divide in half, randomly displace
  - scale variance by half
- 2D: diamond-square
  - generate new value at midpoint
  - average corner values + random displacement
    - scale variance by half each time



<http://www.gameprogrammer.com/fractal.html>

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**Review: Particle Systems**

- changeable/fluid stuff
  - fire, steam, smoke, water, grass, hair, dust, waterfalls, fireworks, explosions, flocks
- life cycle
  - generation, dynamics, death
- rendering tricks
  - avoid hidden surface computations



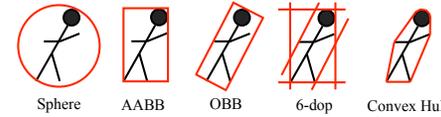
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**Review: Collision Detection**

- boundary check
  - perimeter of world vs. viewpoint or objects
    - 2D/3D absolute coordinates for bounds
    - simple point in space for viewpoint/objects
- set of fixed barriers
  - walls in maze game
    - 2D/3D absolute coordinate system
- set of moveable objects
  - one object against set of items
    - missile vs. several tanks
  - multiple objects against each other
    - punching game: arms and legs of players
    - room of bouncing balls

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**Review: Trade-off in Choosing Proxies**



increasing complexity & tightness of fit  
 decreasing cost of (overlap tests + proxy update)

- AABB: axis aligned bounding box
- OBB: oriented bounding box, arbitrary alignment
- k-dops – shapes bounded by planes at fixed orientations
  - discrete orientation polytope

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**Pair Reduction**

- want proxy for any moving object requiring collision detection
- before pair of objects tested in any detail, quickly test if proxies intersect
- when lots of moving objects, even this quick bounding sphere test can take too long:  $N^2$  times if there are  $N$  objects
- reducing this  $N^2$  problem is called *pair reduction*
- pair testing isn't a big issue until  $N > 50$  or so...

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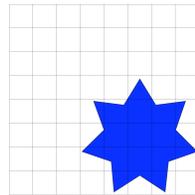
**Spatial Data Structures**

- can only hit something that is close
- spatial data structures tell you what is close to object
  - uniform grid, octrees, kd-trees, BSP trees
  - bounding volume hierarchies
    - OBB trees
  - for player-wall problem, typically use same spatial data structure as for rendering
    - BSP trees most common

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**Uniform Grids**

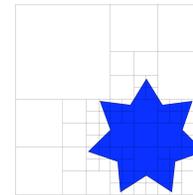
- axis-aligned
- divide space uniformly



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**Quadtrees/Octrees**

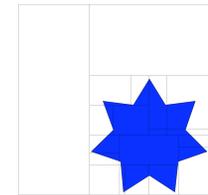
- axis-aligned
- subdivide until no points in cell



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**KD Trees**

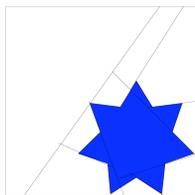
- axis-aligned
- subdivide in alternating dimensions



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**BSP Trees**

- planes at arbitrary orientation



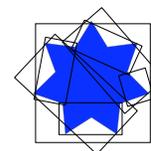
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**Bounding Volume Hierarchies**



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**OBB Trees**



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**Related Reading**

- Real-Time Rendering
  - Tomas Moller and Eric Haines
  - on reserve in CICS reading room

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## Acknowledgement

- slides borrow heavily from
  - Stephen Chenney, (UWisc CS679)
    - <http://www.cs.wisc.edu/~schenney/courses/cs679-f2003/lectures/cs679-22.ppt>
- slides borrow lightly from
  - Steve Rotenberg, (UCSD CSE169)
    - [http://graphics.ucsd.edu/courses/cse169\\_w05/CSE169\\_17.ppt](http://graphics.ucsd.edu/courses/cse169_w05/CSE169_17.ppt)

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## Antialiasing

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## Reading for Antialiasing

- FCG Sec 8.3 Simple Antialiasing
  - 2nd ed: 3.7
- FCG Sec 13.4.1 Antialiasing
  - 2nd ed: 10.11.1
- FCG Chap 9 Signal Processing (optional)
  - 2nd ed: Chap 4 (optional)

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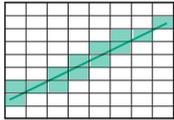
## Samples

- most things in the real world are **continuous**
- everything in a computer is **discrete**
- the process of mapping a continuous function to a discrete one is called **sampling**
- the process of mapping a discrete function to a continuous one is called **reconstruction**
- the process of mapping a continuous variable to a discrete one is called **quantization**
- rendering an image requires sampling and quantization
- displaying an image involves reconstruction

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## Jaggy Line Segments

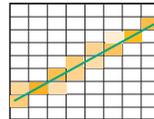
- we tried to sample a line segment so it would map to a 2D raster display
- we quantized the pixel values to 0 or 1
- we saw stairsteps / jaggies



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## Less Jaggy Line Segments

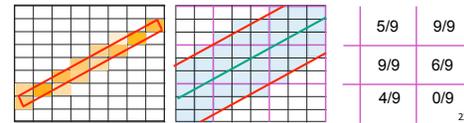
- better if quantize to many shades
  - image is less visibly jaggy
- find color for area, not just single point at center of pixel
  - supersampling**: sample at higher frequency than intended display size



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## Supersample and Average

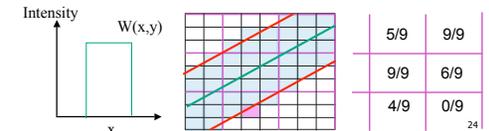
- supersample: create image at higher resolution
  - e.g. 768x768 instead of 256x256
  - shade pixels wrt area covered by thick line/rectangle
- average across many pixels
  - e.g. 3x3 small pixel block to find value for 1 big pixel
  - rough approximation divides each pixel into a finer grid of pixels



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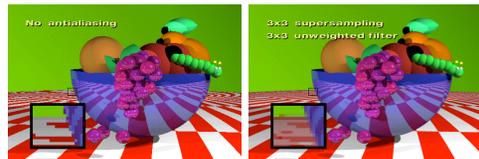
## Supersample and Average

- supersample: jaggies less obvious, but still there
  - small pixel center check still misses information
  - unweighted area sampling
    - equal areas cause equal intensity, regardless of distance from pixel center to area
    - aka box filter



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## Supersampling Example: Image



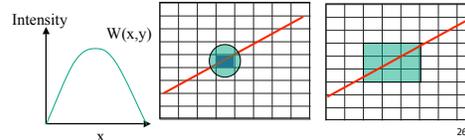
no supersampling

3x3 supersampling with 3x3 unweighted filter

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## Weighted Area Sampling

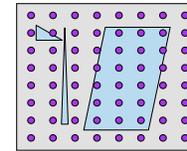
- intuitively, pixel cut through the center should be more heavily weighted than one cut along corner
- weighting function,  $W(x,y)$ 
  - specifies the contribution of primitive passing through the point  $(x, y)$  from pixel center
  - Gaussian filter (or approximation) commonly used



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## Sampling Errors

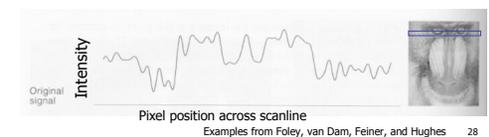
- some objects missed entirely, others poorly sampled
  - could try unweighted or weighted area sampling
  - but how can we be sure we show everything?
- need to think about entire class of solutions!
  - brief taste of signal processing (Chap 4 FCG)



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## Image As Signal

- image as spatial signal
- 2D raster image
  - discrete sampling of 2D spatial signal
- 1D slice of raster image
  - discrete sampling of 1D spatial signal



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## Sampling Frequency

- if don't sample often enough, resulting signal misinterpreted as lower-frequency one
  - we call this **aliasing**

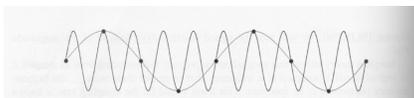


Fig. 14.17 Sampling below the Nyquist rate. (Courtesy of George Wolberg, Columbia University.)

Examples from Foley, van Dam, Feiner, and Hughes

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## Sampling Theorem

continuous signal can be completely recovered from its samples

iff

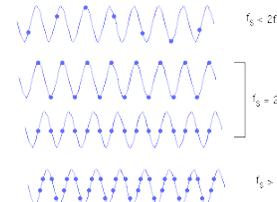
sampling rate greater than twice maximum frequency present in signal

- Claude Shannon

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## Nyquist Rate

- lower bound on sampling rate
  - twice the highest frequency component in the image's spectrum



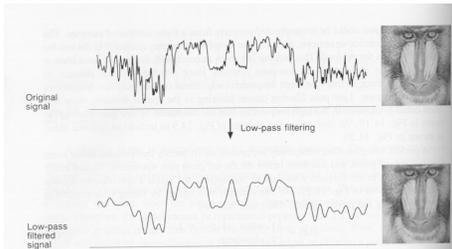
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## Aliasing

- incorrect appearance of high frequencies as low frequencies
- to avoid: **antialiasing**
  - supersample
    - sample at higher frequency
  - low pass filtering
    - remove high frequency function parts
    - aka prefiltering, band-limiting

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## Low-Pass Filtering



Examples from Foley, van Dam, Feiner, and Hughes 33

## Low-Pass Filtering

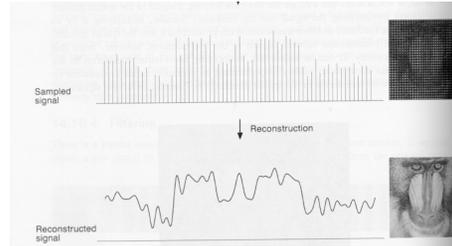
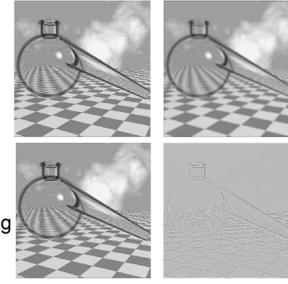


Fig. 14.20 The sampling pipeline with filtering. (Courtesy of George Wolberg Columbia University.)

Examples from Foley, van Dam, Feiner, and Hughes 34

## Filtering

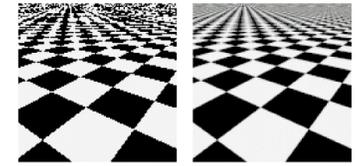
- low pass
  - blur
- high pass
  - edge finding



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## Texture Antialiasing

- texture mipmapping: low pass filter



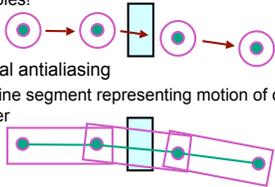
(a)

(b)

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## Temporal Antialiasing

- subtle point: collision detection about algorithms for finding collisions *in time* as much as space
- temporal sampling
  - aliasing: can miss collision completely with point samples!
- temporal antialiasing
  - test line segment representing motion of object center



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