University of British Columbia
CPSC 314 Computer Graphics
Jan-Apr 2008

Tamara Munzner

Viewing/Projections I

Week 3, Fri Jan 25

http://www.ugrad.cs.ubc.ca/~cs314/Vjan2008

Reading for This and Next 2 Lectures

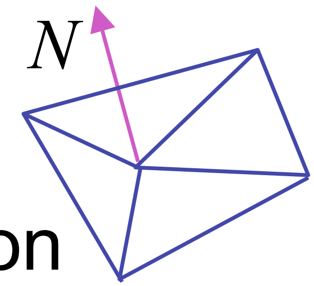
- FCG Chapter 7 Viewing
- FCG Section 6.3.1 Windowing Transforms

- RB rest of Chap Viewing
- RB rest of App Homogeneous Coords

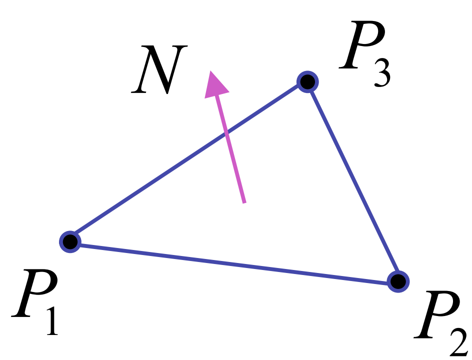
Review: Display Lists

- precompile/cache block of OpenGL code for reuse
  - usually more efficient than immediate mode
    - exact optimizations depend on driver
  - good for multiple instances of same object
    - but cannot change contents, not parametrizable
  - good for static objects redrawn often
    - display lists persist across multiple frames
    - interactive graphics: objects redrawn every frame from new viewpoint from moving camera
  - can be nested hierarchically
- snowman example: 3x performance improvement, 36K polys

Review: Computing Normals



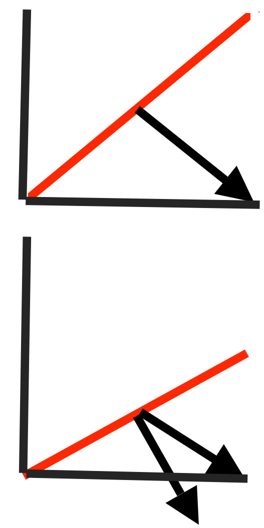
- normal
  - direction specifying orientation of polygon
    - w=0 means direction with homogeneous coords
    - vs. w=1 for points/vectors of object vertices
  - used for lighting
    - must be normalized to unit length
  - can compute if not supplied with object



$$N = (P_2 - P_1) \times (P_3 - P_1)$$

Review: Transforming Normals

- cannot transform normals using same matrix as points
  - nonuniform scaling would cause to be not perpendicular to desired plane!



$$P \longrightarrow P' = MP$$
$$N \longrightarrow N' = QN$$

given M,
what should Q be?

$$\mathbf{Q} = \left(\mathbf{M}^{-1}\right)^{\mathrm{T}}$$

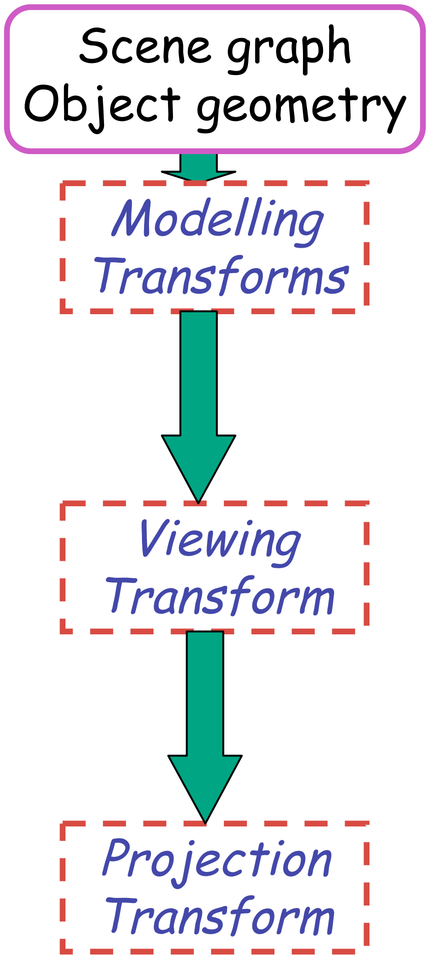
inverse transpose of the modelling transformation

Viewing

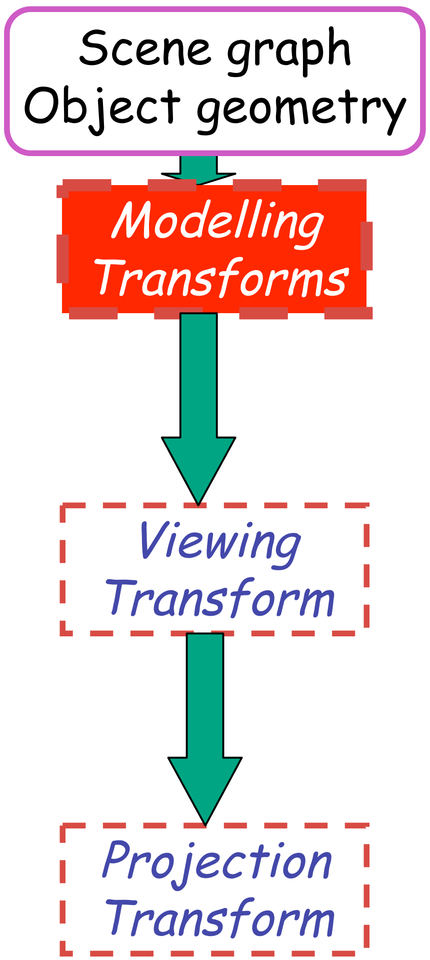
Using Transformations

- three ways
  - modelling transforms
    - place objects within scene (shared world)
    - affine transformations
  - viewing transforms
    - place camera
    - rigid body transformations: rotate, translate
  - projection transforms
    - change type of camera
    - projective transformation

Rendering Pipeline

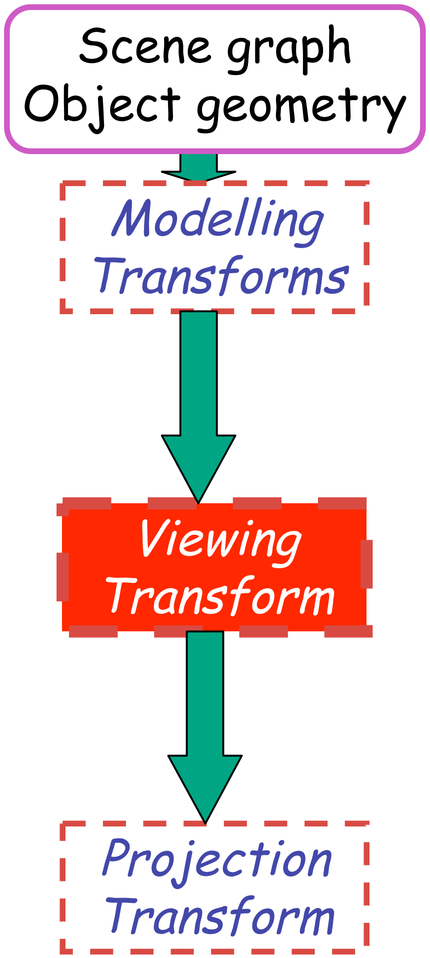


Rendering Pipeline



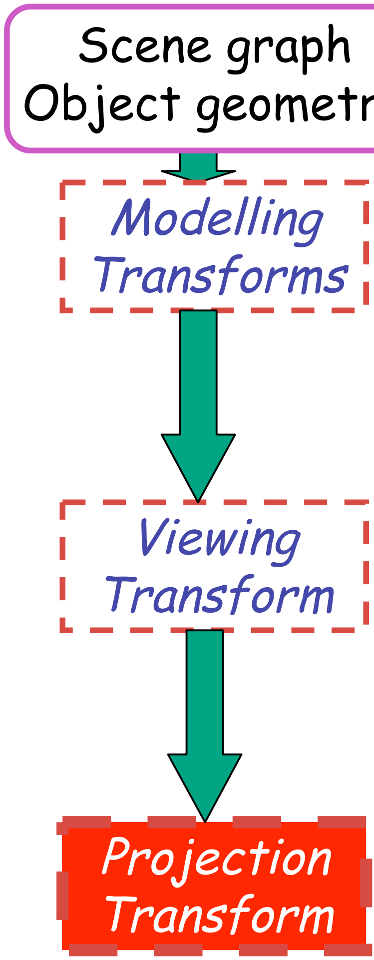
- result
  - all vertices of scene in shared 3D world coordinate system

Rendering Pipeline

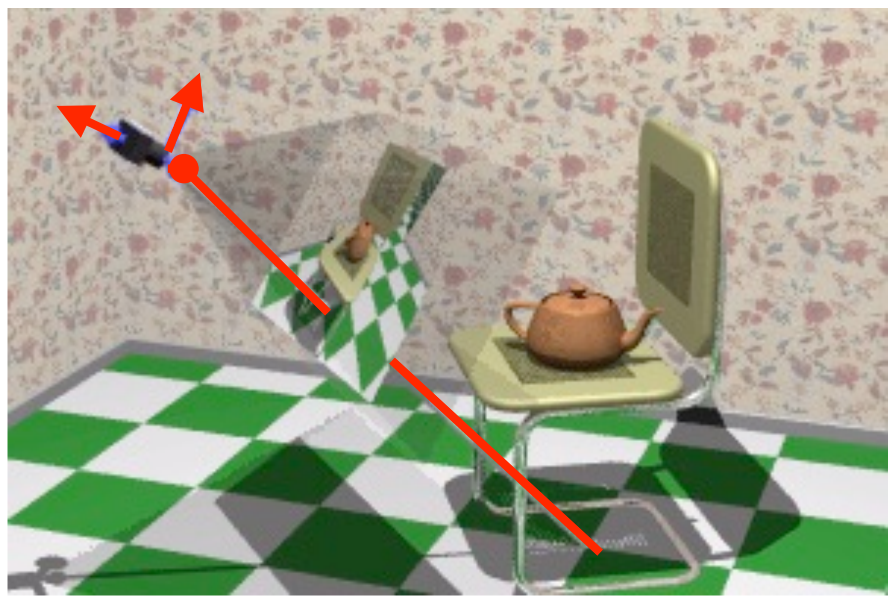


- result
  - scene vertices in 3D view (camera) coordinate system

Rendering Pipeline



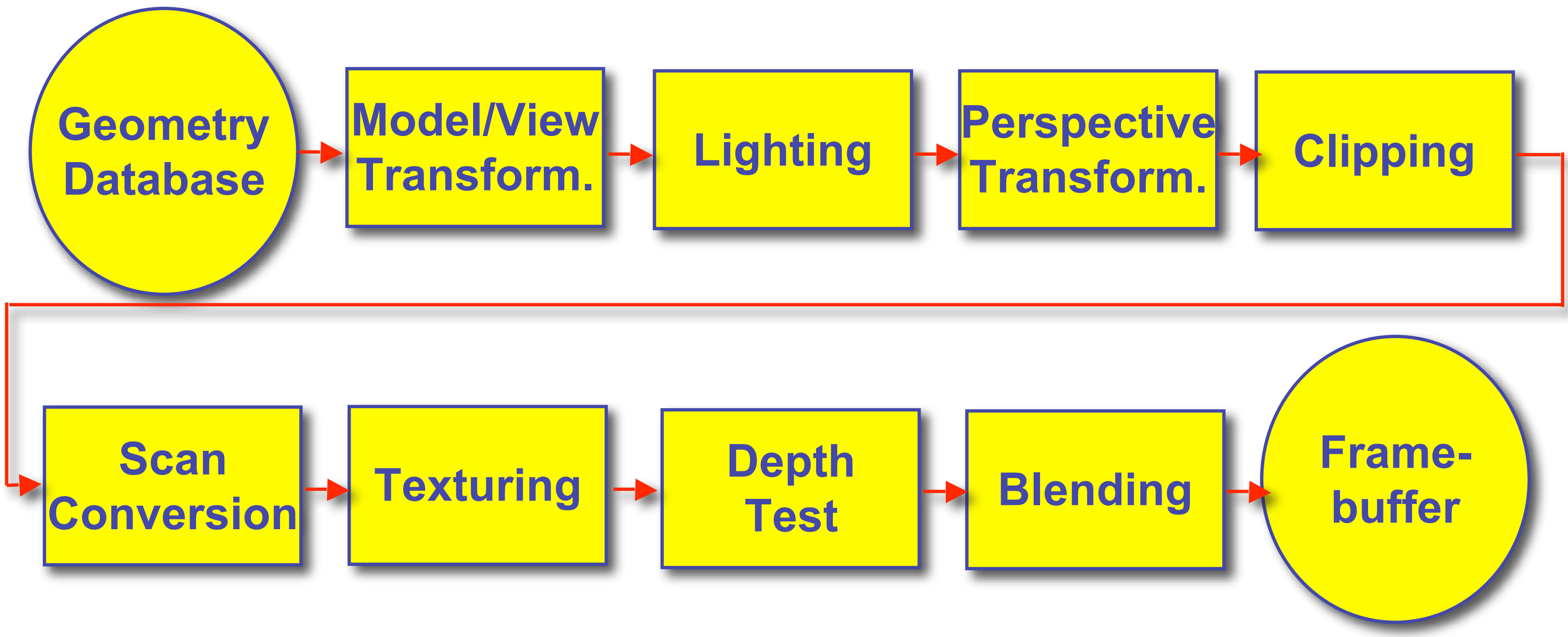
- result
  - 2D screen coordinates of clipped vertices



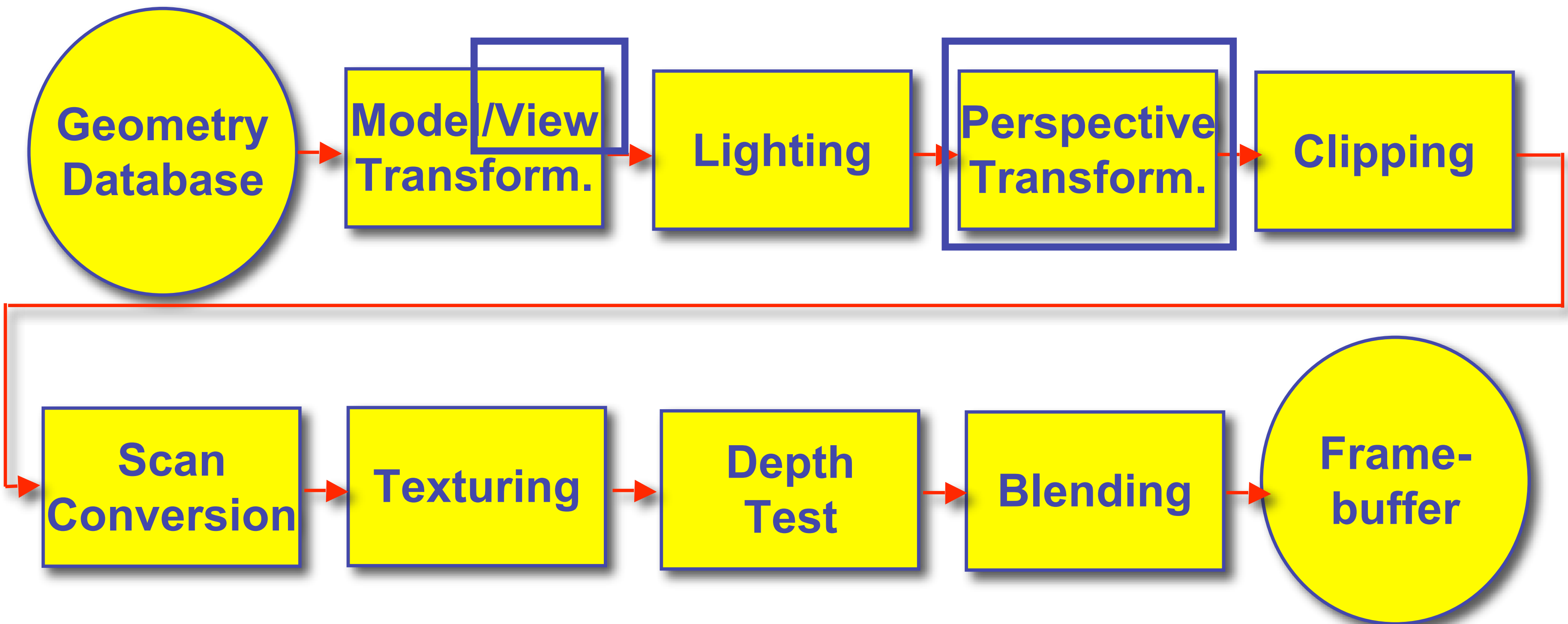
Viewing and Projection

- need to get from 3D world to 2D image
- projection: geometric abstraction
  - what eyes or cameras do
- two pieces
  - viewing transform:
    - where is the camera, what is it pointing at?
  - perspective transform: 3D to 2D
    - flatten to image

Rendering Pipeline



Rendering Pipeline



OpenGL Transformation Storage

- modeling and viewing stored together
  - possible because no intervening operations
- perspective stored in separate matrix

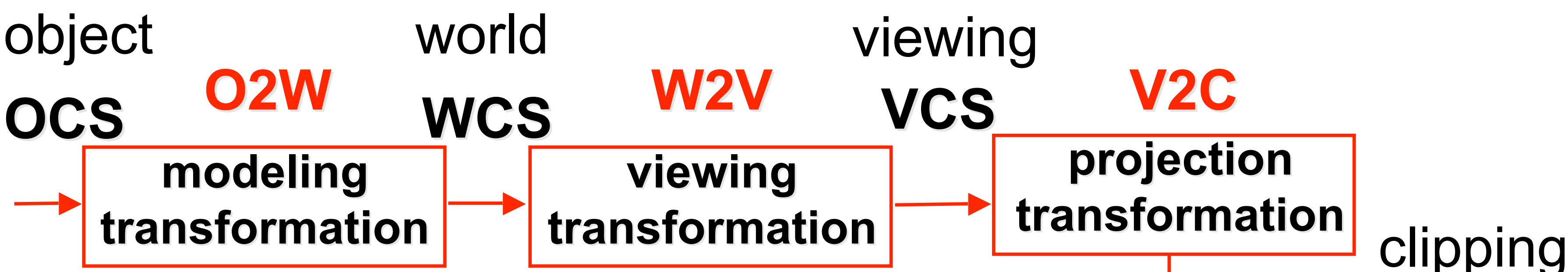
- specify which matrix is target of operations
  - common practice: return to default modelview mode after doing projection operations

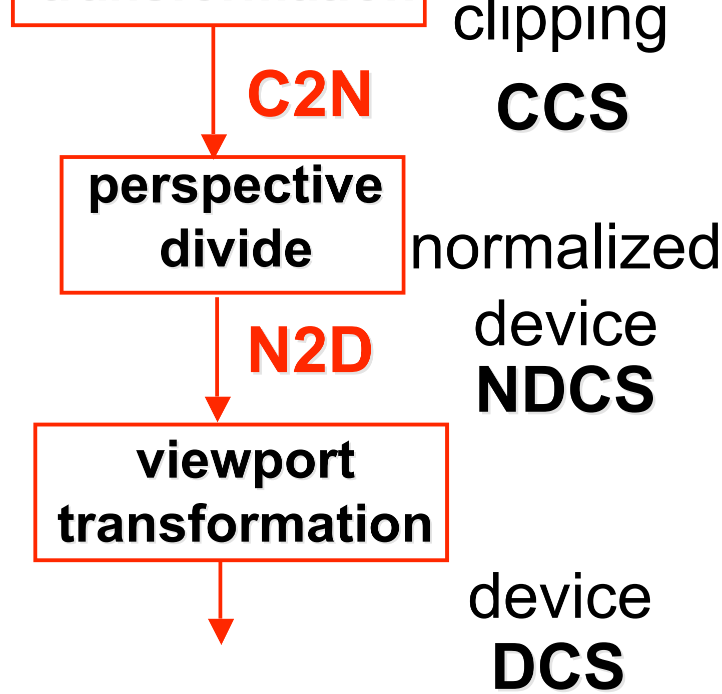
```
glMatrixMode(GL_MODELVIEW);
glMatrixMode(GL_PROJECTION);
```

Coordinate Systems

- result of a transformation
- names
  - convenience
    - mouse: leg, head, tail
  - standard conventions in graphics pipeline
    - object/modelling
    - world
    - camera/viewing/eye
    - screen/window
    - raster/device

Projective Rendering Pipeline





OCS - object/model coordinate system

WCS - world coordinate system

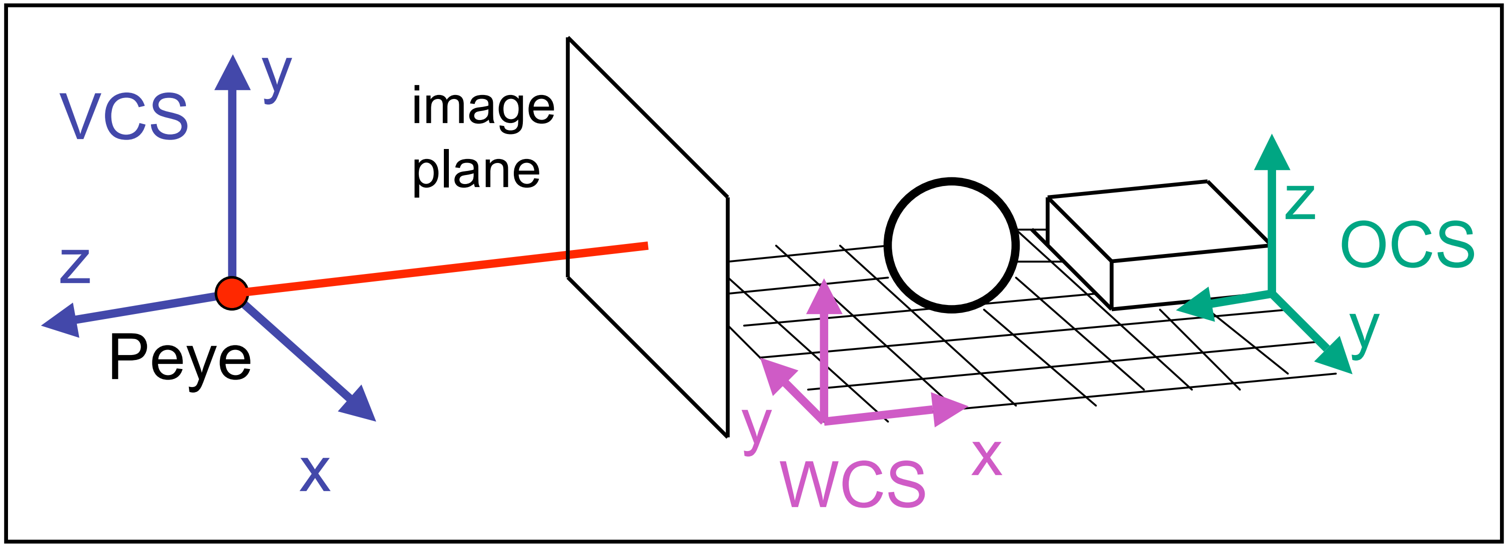
VCS - viewing/camera/eye coordinate system

CCS - clipping coordinate system

NDCS - normalized device coordinate system

DCS - device/display/screen coordinate system

Viewing Transformation



object	world	viewing
OCS	**WCS**	**VCS**

→ **modeling transformation** → **viewing transformation** →

$\mathbf{M}_{\mathbf{mod}}$ $\mathbf{M}_{\mathbf{cam}}$

OpenGL ModelView matrix

Basic Viewing

- starting spot - OpenGL
  - camera at world origin
    - probably inside an object
  - y axis is up
  - looking down negative z axis
    - why? RHS with x horizontal, y vertical, z out of screen
- translate backward so scene is visible
  - move distance d = focal length

- where is camera in P1 template code?
  - 5 units back, looking down -z axis

Convenient Camera Motion

- rotate/translate/scale versus
  - eye point, gaze/lookat direction, up vector
  - demo: Robins transformation, projection

OpenGL Viewing Transformation

```
gluLookAt(ex,ey,ez,lx,ly,lz,ux,uy,uz)
```

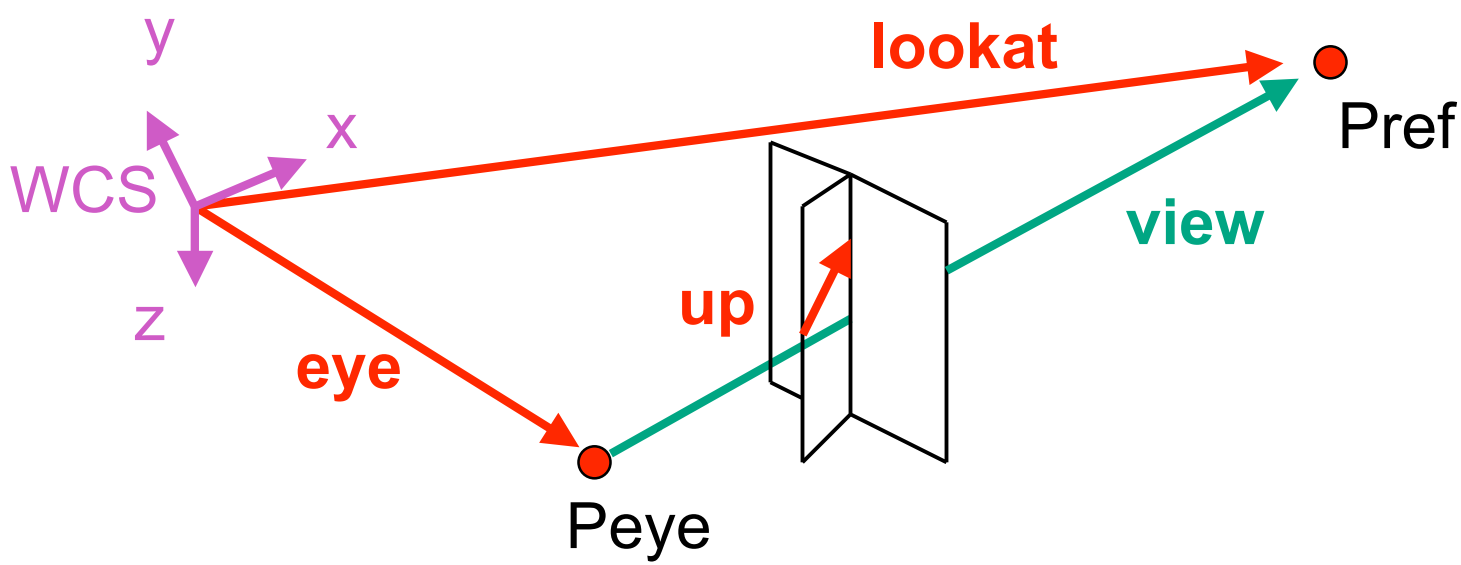
- postmultiplies current matrix, so to be safe:

```
glMatrixMode(GL_MODELVIEW);
glLoadIdentity();
gluLookAt(ex,ey,ez,lx,ly,lz,ux,uy,uz)
// now ok to do model transformations
```

- demo: Nate Robins tutorial *projection*

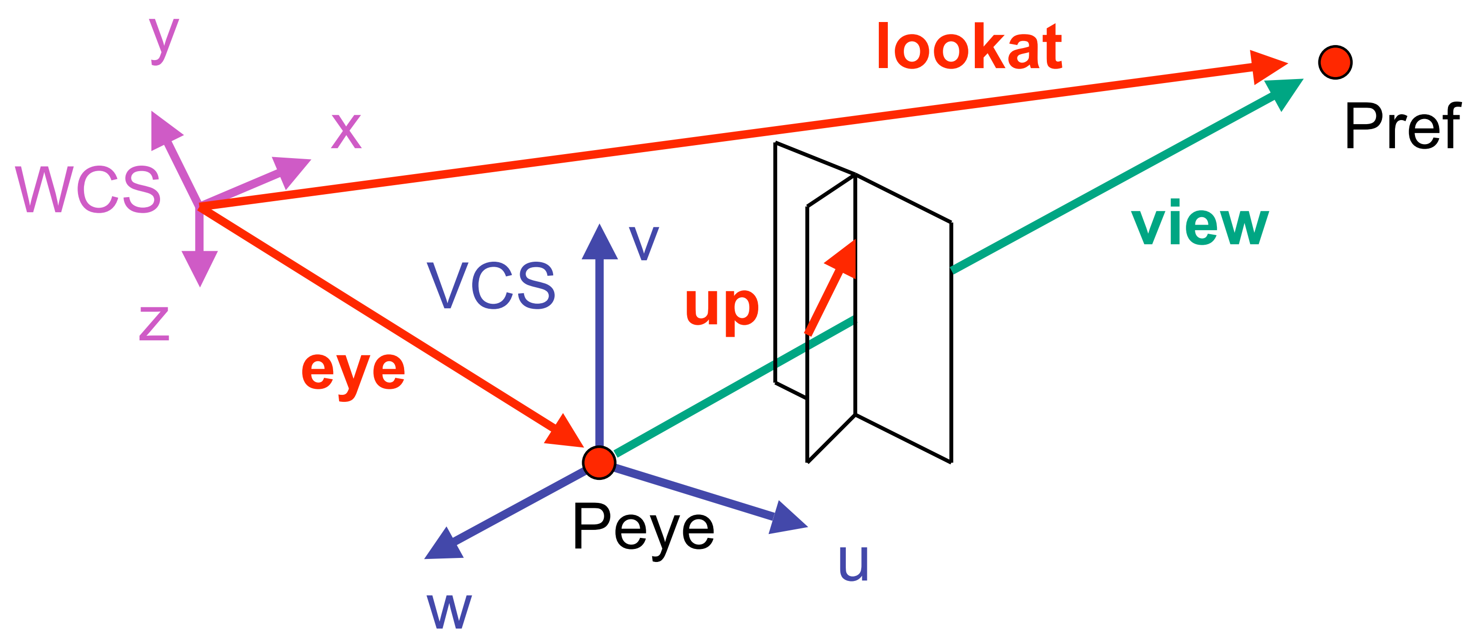
Convenient Camera Motion

- rotate/translate/scale versus
  - eye point, gaze/lookat direction, up vector



From World to View Coordinates: W2V

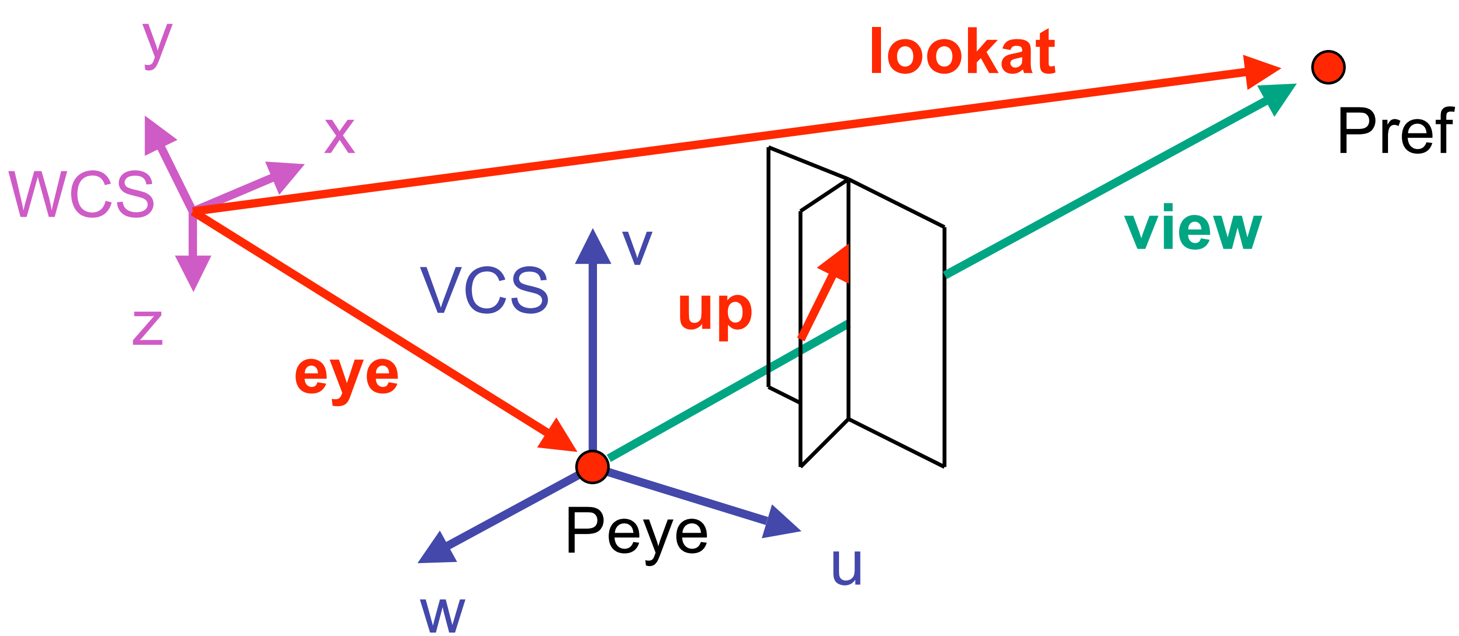
- translate **eye** to origin
- rotate **view** vector (**lookat** – **eye**) to **w** axis
- rotate around **w** to bring **up** into **vw**-plane



Deriving W2V Transformation

- translate **eye** to origin

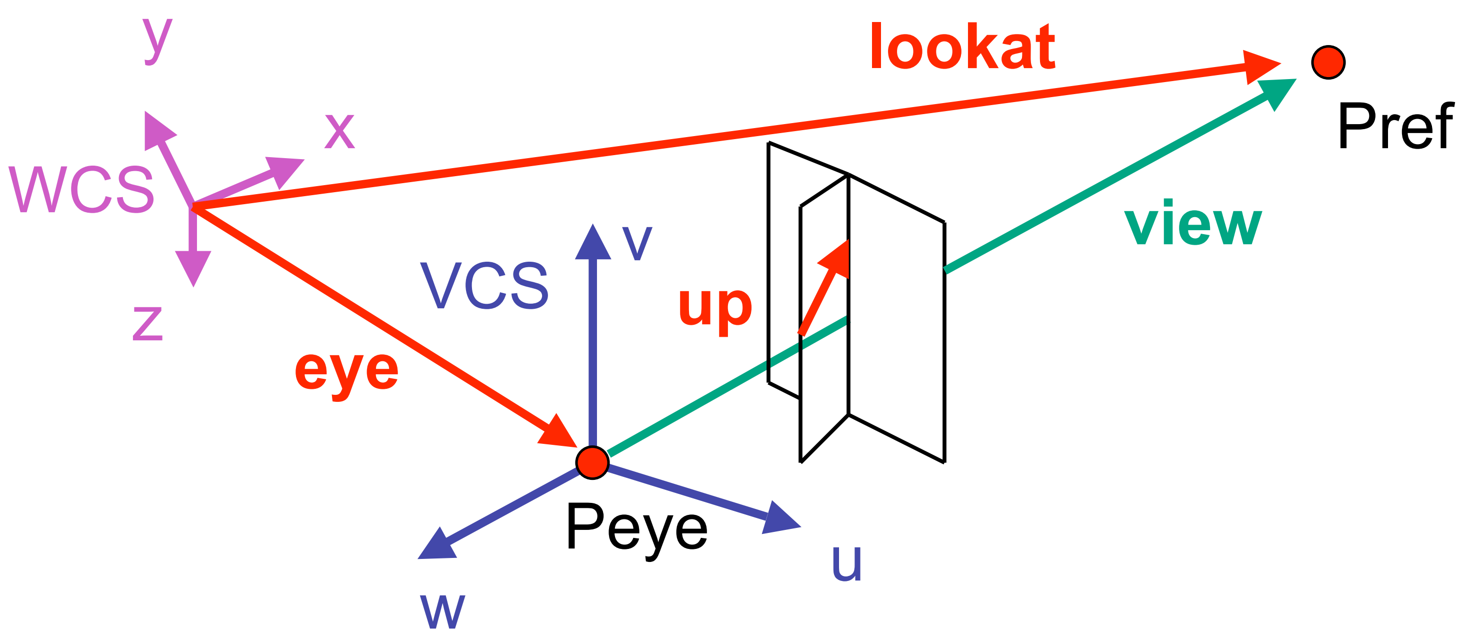
$$\mathbf{T} = \begin{bmatrix} 1 & 0 & 0 & e_x \\ 0 & 1 & 0 & e_y \\ 0 & 0 & 1 & e_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Deriving W2V Transformation

- rotate **view** vector (**lookat** – **eye**) to **w** axis
  - **w**: normalized opposite of **view/gaze** vector **g**

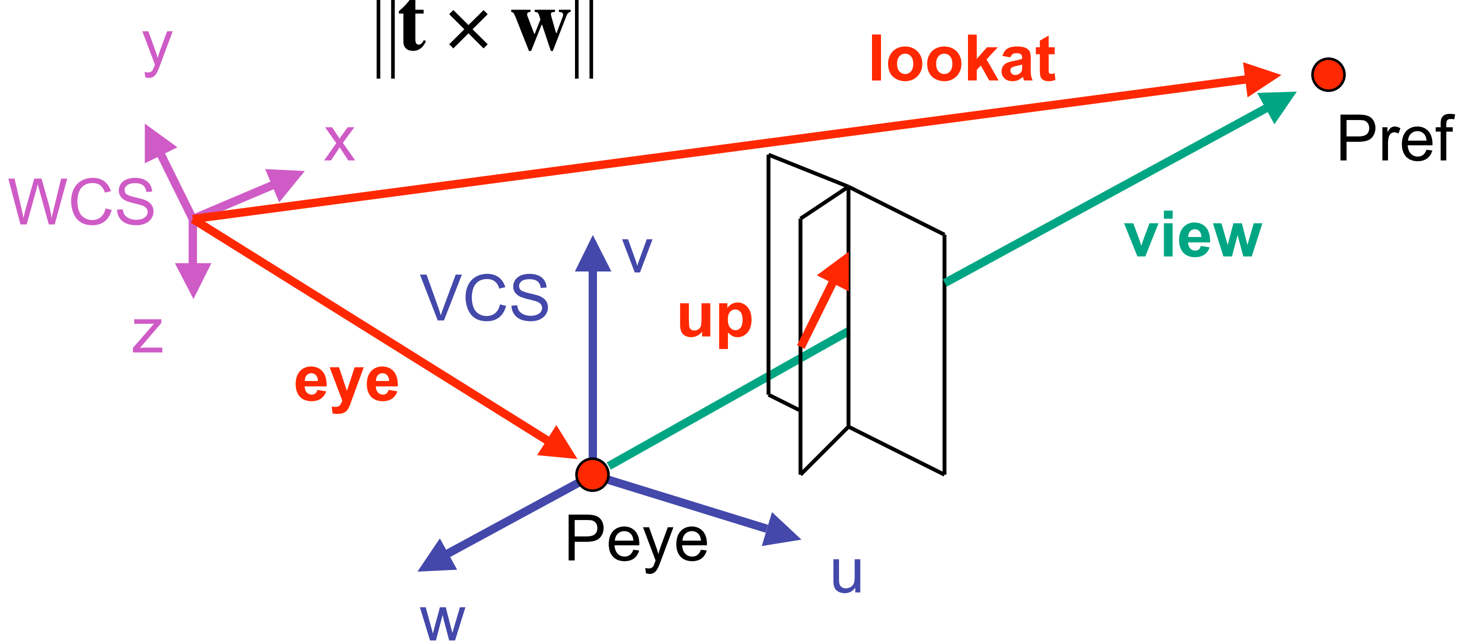
$$\mathbf{w} = -\hat{\mathbf{g}} = -\frac{\mathbf{g}}{\|\mathbf{g}\|}$$



Deriving W2V Transformation

- rotate around **w** to bring **up** into **vw**-plane
  - **u** should be perpendicular to **vw**-plane, thus perpendicular to **w** and **up** vector **t**
  - **v** should be perpendicular to **u** and **w**

$$\mathbf{u} = \frac{\mathbf{t} \times \mathbf{w}}{\left\| \mathbf{t} \times \mathbf{w} \right\|} \qquad \mathbf{v} = \mathbf{w} \times \mathbf{u}$$



Deriving W2V Transformation

- rotate from WCS **xyz** into **uvw** coordinate system with matrix that has columns **u**, **v**, **w**

$$\mathbf{u} = \frac{\mathbf{t} \times \mathbf{w}}{\left\|\mathbf{t} \times \mathbf{w}\right\|} \qquad \mathbf{v} = \mathbf{w} \times \mathbf{u} \qquad \mathbf{w} = -\hat{\mathbf{g}} = -\frac{\mathbf{g}}{\left\|\mathbf{g}\right\|}$$

$$\mathbf{R} = \begin{bmatrix} u_x & v_x & w_x & 0 \\ u_y & v_y & w_y & 0 \\ u_z & v_z & w_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad \mathbf{T} = \begin{bmatrix} 1 & 0 & 0 & e_x \\ 0 & 1 & 0 & e_y \\ 0 & 0 & 1 & e_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad M_{W2V} = TR$$

- reminder: rotate from **uvw** to **xyz** coord sys with matrix **M** that has columns **u,v,w**

W2V vs. V2W

- $M_{W2V}=TR$

$$\mathbf{T}=\begin{bmatrix}1 & 0 & 0 & e_x\\ 0 & 1 & 0 & e_y\\ 0 & 0 & 1 & e_z\\ 0 & 0 & 0 & 1\end{bmatrix}\quad \mathbf{R}=\begin{bmatrix}u_x & v_x & w_x & 0\\ u_y & v_y & w_y & 0\\ u_z & v_z & w_z & 0\\ 0 & 0 & 0 & 1\end{bmatrix}$$

- we derived position of camera in world
  - invert for world with respect to camera
- $M_{V2W}=(M_{W2V})^{-1}=R^{-1}T^{-1}$

$$\mathbf{R}^{-1}=\begin{bmatrix}u_x & u_y & u_z & 0\\ v_x & v_y & v_z & 0\\ w_x & w_y & w_z & 0\\ 0 & 0 & 0 & 1\end{bmatrix}\quad \mathbf{T}^{-1}=\begin{bmatrix}1 & 0 & 0 & -e_x\\ 0 & 1 & 0 & -e_y\\ 0 & 0 & 1 & -e_z\\ 0 & 0 & 0 & 1\end{bmatrix}$$

  - inverse is transpose for orthonormal matrices
  - inverse is negative for translations

W2V vs. V2W

- M_{W2V}=TR

$$\mathbf{T} = \begin{bmatrix} 1 & 0 & 0 & e_x \\ 0 & 1 & 0 & e_y \\ 0 & 0 & 1 & e_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \mathbf{R} = \begin{bmatrix} u_x & v_x & w_x & 0 \\ u_y & v_y & w_y & 0 \\ u_z & v_z & w_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

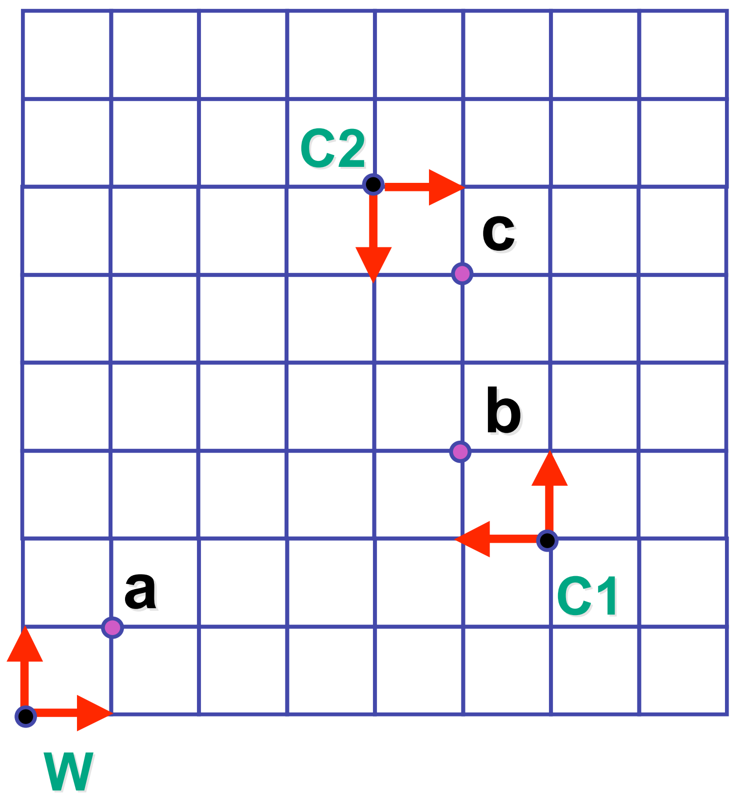
- we derived position of camera in world
  - invert for world with respect to camera
- $M_{V2W}=(M_{W2V})^{-1}=R^{-1}T^{-1}$

$$\mathbf{M}_{view2world} = \begin{bmatrix} u_x & u_y & u_z & 0 \\ v_x & v_y & v_z & 0 \\ w_x & w_y & w_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -e_x \\ 0 & 1 & 0 & -e_y \\ 0 & 0 & 1 & -e_z \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} u_x & u_y & u_z & -e_x \\ v_x & v_y & v_z & -e_y \\ w_x & w_y & w_z & -e_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Moving the Camera or the World?

- two equivalent operations
  - move camera one way vs. move world other way
- example
  - initial OpenGL camera: at origin, looking along -z axis
  - create a unit square parallel to camera at z = -10
  - translate in z by 3 possible in two ways
    - camera moves to z = -3
      - Note OpenGL models viewing in left-hand coordinates
    - camera stays put, but world moves to -7
  - resulting image same either way
    - possible difference: are lights specified in world or view coordinates?

World vs. Camera Coordinates Example



$a = (1,1)_W$

$b = (1,1)_{C1} = (5,3)_W$

$c = (1,1)_{C2} = (1,3)_{C1} = (5,5)_W$