



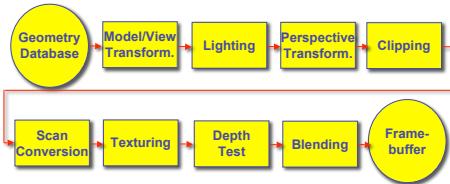
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## OpenGL, GLUT, Transformations I

Week 2, Wed Jan 16

<http://www.ugrad.cs.ubc.ca/~cs314/Vjan2008>

## Review: Rendering Pipeline



## OpenGL (briefly)

- API to graphics hardware
  - based on IRIS\_GL by SGI
- designed to exploit hardware optimized for display and manipulation of 3D graphics
- implemented on many different platforms
- low level, powerful flexible
- pipeline processing
  - set state as needed

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## Graphics State

- set the state once, remains until overwritten
  - glColor3f(1.0, 1.0, 0.0) → set color to yellow
  - glClearColor(0.0, 0.0, 0.2) → dark blue bg
  - glEnable(GL\_LIGHT0) → turn on light
  - glEnable(GL\_DEPTH\_TEST) → hidden surf.

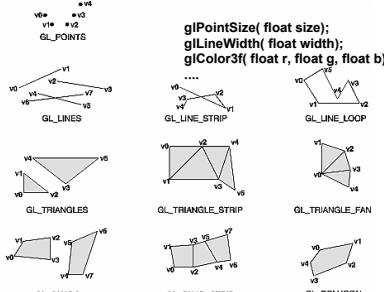
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## Geometry Pipeline

- tell it how to interpret geometry
  - glBegin(<mode of geometric primitives>)
  - mode = GL\_TRIANGLES, GL\_POLYGON, etc.
- feed it vertices
  - glVertex3f(-1.0, 0.0, -1.0)
  - glVertex3f(1.0, 0.0, -1.0)
  - glVertex3f(0.0, 1.0, -1.0)
- tell it you're done
  - glEnd()

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## OpenGL: Geometric Primitives



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## Code Sample

```
void display()
{
    glClearColor(0.0, 0.0, 0.0, 0.0);
    glClear(GL_COLOR_BUFFER_BIT);
    glColor3f(0.0, 1.0, 0.0);
    glBegin(GL_POLYGON);
    glVertex3f(0.25, 0.25, -0.5);
    glVertex3f(0.75, 0.25, -0.5);
    glVertex3f(0.75, 0.75, -0.5);
    glVertex3f(0.25, 0.75, -0.5);
    glEnd();
    glFlush();
}
```

- more OpenGL as course continues

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## GLUT

## GLUT: OpenGL Utility Toolkit

- developed by Mark Kilgard (also from SGI)
- simple, portable window manager
  - opening windows
    - handling graphics contexts
    - handling input with callbacks
      - keyboard, mouse, window reshape events
      - timing
      - idle processing, idle events
  - designed for small/medium size applications
  - distributed as binaries
    - free, but not open source

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## Event-Driven Programming

- main loop not under your control
  - vs. batch mode where you control the flow
- control flow through event callbacks
  - redraw the window now
  - key was pressed
  - mouse moved
- callback functions called from main loop when events occur
  - mouse/keyboard state setting vs. redrawing

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## GLUT Callback Functions

```
// you supply these kind of functions
void reshape(int w, int h);
void keyboard(unsigned char key, int x, int y);
void mouse(int button, int state, int x, int y);
void idle();
void display();

// register them with glut
	glutReshapeFunc(reshape);
	glutKeyboardFunc(keyboard);
	glutMouseFunc(mouse);
	glutIdleFunc(idle);
	glutDisplayFunc(display);

void glutDisplayFunc (void (*func)(void));
void glutKeyboardFunc (void (*func)(unsigned char key, int x, int y));
void glutIdleFunc (void (*func) ());
void glutReshapeFunc (void (*func)(int width, int height));
```

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## GLUT Example 1

```
#include <GLUT/glut.h>
void display()
{
    int main(argc, argv)
    {
        glClearColor(0,0,0,1);
        glClear(GL_COLOR_BUFFER_BIT);
        glColor4f(0,1,0,1);
        glBegin(GL_POLYGON);
        GLUT_RGB(GLUT_DOUBLE);
        glVertex3f(0.25, 0.25, -0.5);
        glutInitWindowSize(640,480);
        glVertex3f(0.75, 0.25, -0.5);
        glutCreateWindow("glut1");
        glVertex3f(0.75, 0.75, -0.5);
        glutDisplayFunc(display);
        glVertex3f(0.25, 0.75, -0.5);
        glutMainLoop();
        glEnd();
        return 0; // never reached
    }
    glutSwapBuffers();
}
```

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## GLUT Example 2

```
#include <GLUT/glut.h>
void display()
{
    glRotatef(0.1, 0,0,1);
    int main(argc, argv)
    {
        glutInit(&argc, argv);
        glClearColor(0,0,0,1);
        glClear(GL_COLOR_BUFFER_BIT);
        glutInitDisplayMode(
        GL_RGB|GLUT_DOUBLE);
        glBegin(GL_POLYGON);
        glutInitWindowSize(640,480);
        glVertex3f(0.25, 0.25, -0.5);
        glutCreateWindow("glut2");
        glVertex3f(0.75, 0.25, -0.5);
        glutDisplayFunc(display);
        glVertex3f(0.75, 0.75, -0.5);
        glutMainLoop();
        glVertex3f(0.25, 0.75, -0.5);
        return 0; // never reached
    }
    glutSwapBuffers();
}
```

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## Redrawing Display

- display only redrawn by explicit request
  - glutPostRedisplay() function
  - default window resize callback does this
- idle called from main loop when no user input
  - good place to request redraw
  - will call display next time through event loop
- should return control to main loop quickly
- continues to rotate even when no user action

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## GLUT Example 3

```
#include <GLUT/glut.h>
void idle()
{
    glutPostRedisplay();
}
int main(argc, argv)
{
    glRotatef(0.1, 0,0,1);
    glClearColor(0,0,0,1);
    glClear(GL_COLOR_BUFFER_BIT);
    glutInit(&argc, argv);
    glColor4f(0,1,0,1);
    glutInitDisplayMode(
    GL_RGB|GLUT_DOUBLE);
    glBegin(GL_POLYGON);
    glutInitWindowSize(640,480);
    glVertex3f(0.25, 0.25, -0.5);
    glutCreateWindow("glut1");
    glVertex3f(0.75, 0.25, -0.5);
    glutDisplayFunc(display);
    glVertex3f(0.75, 0.75, -0.5);
    glutMainLoop();
    glutIdleFunc(idle);
    glutSwapBuffers();
    return 0; // never reached
}
```

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## Keyboard/Mouse Callbacks

- again, do minimal work
- consider keypress that triggers animation
  - do not have loop calling display in callback!
    - what if user hits another key during animation?
  - instead, use shared/global variables to keep track of state
    - yes, OK to use globals for this!
  - then display function just uses current variable value

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## GLUT Example 4

```
#include <GLUT/glut.h>
void doKey(unsigned char key,
           int x, int y) {
    bool animToggle = true;
    float angle = 0.1;
    if ('t' == key) {
        animToggle = !animToggle;
        if (!animToggle)
            glutIdleFunc(NULL);
        else
            glutIdleFunc(idle);
    } else if ('r' == key) {
        angle = -angle;
    }
    glutPostRedisplay();
}
int main(int argc,char**argv) {
    ...
    glutKeyboardFunc( doKey );
    ...
}
```

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## Transformations

## Transformations

- transforming an object = transforming all its points
- transforming a polygon = transforming its vertices



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## Matrix Representation

- represent 2D transformation with matrix
  - multiply matrix by column vector  $\Leftrightarrow$  apply transformation to point

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \quad x' = ax + by \\ y' = cx + dy$$

- transformations combined by multiplication

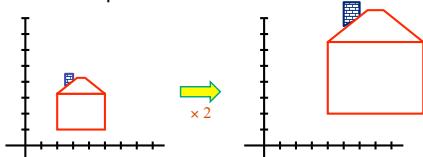
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} d & e \\ f & g \end{bmatrix} \begin{bmatrix} h & i \\ j & k \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

- matrices are efficient, convenient way to represent sequence of transformations!

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## Scaling

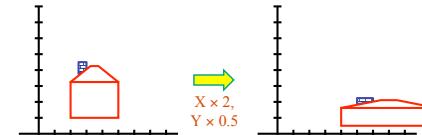
- scaling** a coordinate means multiplying each of its components by a scalar
- uniform scaling** means this scalar is the same for all components:



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## Scaling

- non-uniform scaling**: different scalars per component:



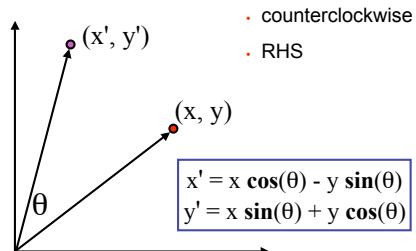
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## Scaling

- scaling operation:  $\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} ax \\ by \end{bmatrix}$
  - or, in matrix form:  $\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$
- scaling matrix

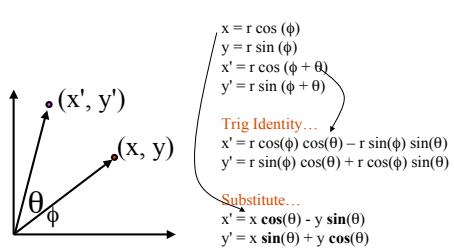
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## 2D Rotation



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## 2D Rotation From Trig Identities



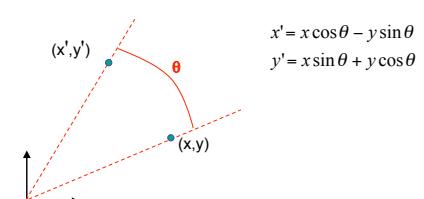
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## 2D Rotation Matrix

- easy to capture in matrix form:
- $$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$
- even though  $\sin(\theta)$  and  $\cos(\theta)$  are nonlinear functions of  $\theta$ ,
  - $x'$  is a linear combination of  $x$  and  $y$
  - $y'$  is a linear combination of  $x$  and  $y$

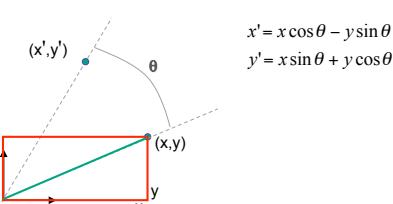
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## 2D Rotation: Another Derivation



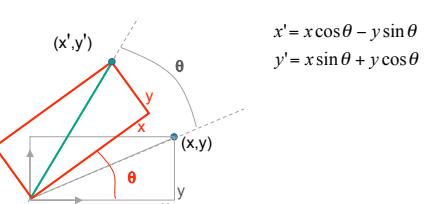
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## 2D Rotation: Another Derivation



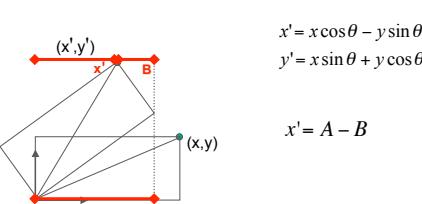
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## 2D Rotation: Another Derivation



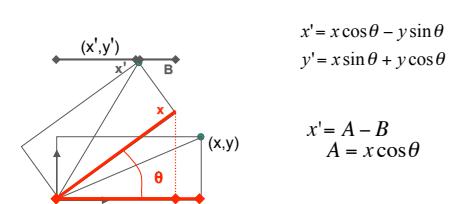
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## 2D Rotation: Another Derivation



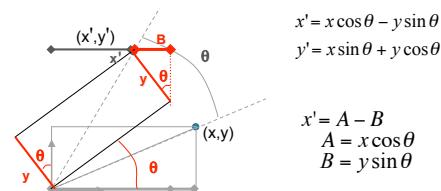
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## 2D Rotation: Another Derivation



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## 2D Rotation: Another Derivation



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## Shear

- shear along x axis
- push points to right in proportion to height

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} ? & ? \\ ? & ? \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} ? \\ ? \end{bmatrix}$$

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## Shear

- shear along x axis
- push points to right in proportion to height

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & sh_x \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

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## Reflection

- reflect across x axis
- mirror

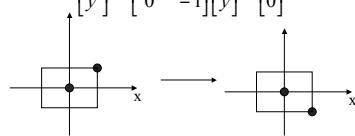
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} ? & ? \\ ? & ? \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} ? \\ ? \end{bmatrix}$$

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## Reflection

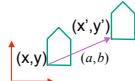
- reflect across x axis

- mirror
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$



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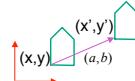
## 2D Translation



$$\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} x+a \\ y+b \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

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## 2D Translation



$$\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} x+a \\ y+b \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

scaling matrix

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

rotation matrix

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## 2D Translation



$$\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} x+a \\ y+b \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

vector addition

$$\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} x+a \\ y+b \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

matrix multiplication

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

scaling matrix

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

rotation matrix

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## 2D Translation

vector addition

$$\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} x+a \\ y+b \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

matrix multiplication

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

scaling matrix

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

rotation matrix

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

translation multiplication matrix??

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## Linear Transformations

- linear transformations are combinations of
  - shear
  - scale
  - rotate
  - reflect
- properties of linear transformations
  - satisfies  $T(sx+ty) = s T(x) + t T(y)$
  - origin maps to origin
  - lines map to lines
  - parallel lines remain parallel
  - ratios are preserved
  - closed under composition

## Challenge

- matrix multiplication
  - for everything except translation
  - how to do everything with multiplication?
  - then just do composition, no special cases
- homogeneous coordinates trick
  - represent 2D coordinates  $(x,y)$  with 3-vector  $(x,y,1)$

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## Homogeneous Coordinates

- our 2D transformation matrices are now  $3 \times 3$ :

$$\text{Rotation} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad \text{Scale} = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

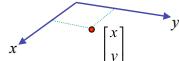
$$\text{Translation} = \begin{bmatrix} 1 & 0 & T_x \\ 0 & 1 & T_y \\ 0 & 0 & 1 \end{bmatrix} \quad \text{use rightmost column}$$

$$\begin{bmatrix} 1 & 0 & a \\ 0 & 1 & b \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x+a \\ y+b \\ 1 \end{bmatrix} = \begin{bmatrix} x+a \\ y+b \\ 1 \end{bmatrix}$$

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## Homogeneous Coordinates Geometrically

- point in 2D cartesian



## Homogeneous Coordinates Geometrically

homogeneous

$$(x, y, w) \xrightarrow{lw} \left( \frac{x}{w}, \frac{y}{w} \right)$$

cartesian

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## Homogeneous Coordinates Geometrically

homogeneous

$$(x, y, w) \xrightarrow{lw} \left( \frac{x}{w}, \frac{y}{w} \right)$$

cartesian

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## Affine Transformations

- affine transforms are combinations of
  - linear transformations
  - translations

$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

- properties of affine transformations
  - origin does not necessarily map to origin
  - lines map to lines
  - parallel lines remain parallel
  - ratios are preserved
  - closed under composition

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## Homogeneous Coordinates Summary

- may seem unintuitive, but they make graphics operations much easier
- allow all affine transformations to be expressed through matrix multiplication
  - we'll see even more later...
- use 3x3 matrices for 2D transformations
  - use 4x4 matrices for 3D transformations