



Tamara Munzner

## Collision II, Antialiasing

Week 11, Mon Mar 26

<http://www.ugrad.cs.ubc.ca/~cs314/V/jan2007>

## News

- Homework 4 out today
  - due Wed 11 Apr, 10am
- extra TA office hours in lab for midterm Q&A
  - Tuesday 4pm Gordon
- H3 solutions, graded H3 handed back
- P4 proposal email feedback out to all who turned in
  - some were missing real email, used ugrad accounts

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## Midterm 2: Wed Mar 26

- covering through Homework 3 material
  - MT1: transformations, some viewing
  - MT2 emphasis
    - some viewing
    - projections
    - color
    - rasterization
    - lighting/shading
    - advanced rendering (incl raytracing)
- graded H3 + solutions out Monday

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## Midterm 2: Wed Mar 26

- closed book
- allowed to have
  - calculator
  - one side of 8.5"x11" paper, handwritten
    - write your name on it
    - turn it in with exam, you'll get it back
- have ID out and face up

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## Review: Select/Hit Picking

- assign (hierarchical) integer key/name(s)
- small region around cursor as new viewport



- redraw in selection mode
  - equivalent to casting pick "tube"
  - store keys, depth for drawn objects in hit list
- examine hit list
  - usually use frontmost, but up to application

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## Correction/Review: Hit List

- glSelectBuffer(bufferSize, \*buffer)
  - where to store hit list data
- on hit, copy entire contents of name stack to output buffer.
- hit record
  - number of names on stack
  - minimum and **maximum** depth of object vertices
    - depth lies in the z-buffer range [0,1]
    - multiplied by  $2^{32} - 1$  then rounded to nearest int

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## Review: Collision Detection

- boundary check
  - perimeter of world vs. viewpoint or objects
    - 2D/3D absolute coordinates for bounds
    - simple point in space for viewpoint/objects
- set of fixed barriers
  - walls in maze game
    - 2D/3D absolute coordinate system
- set of moveable objects
  - one object against set of items
    - missile vs. several tanks
  - multiple objects against each other
    - punching game: arms and legs of players
    - room of bouncing balls

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## Reading for Collision/Acceleration

- FCG Sect 10.9 Sub-Linear

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## Collision/Acceleration II

### Accelerating Collision Detection

- two kinds of approaches (many others also)
  - collision proxies / bounding volumes
  - spatial data structures to localize
- used for both 2D and 3D
- used to accelerate many things, not just collision detection
  - raytracing
  - culling geometry before using standard rendering pipeline

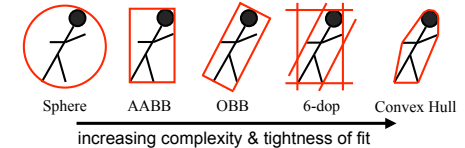
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### Collision Proxies

- **proxy**: something that takes place of real object
  - cheaper than general mesh-mesh intersections
- **collision proxy (bounding volume)** is piece of geometry used to represent complex object for purposes of finding collision
  - if proxy collides, object is said to collide
  - collision points mapped back onto original object
- good proxy: cheap to compute collisions for, tight fit to the real geometry
- common proxies: sphere, cylinder, box, ellipsoid
  - consider: fat player, thin player, rocket, car ...

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### Trade-off in Choosing Proxies



← decreasing cost of (overlap tests + proxy update)

- AABB: axis aligned bounding box
- OBB: oriented bounding box, arbitrary alignment
- k-dops – shapes bounded by planes at fixed orientations
  - discrete orientation polytope

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## Pair Reduction

- want proxy for any moving object requiring collision detection
- before pair of objects tested in any detail, quickly test if proxies intersect
- when lots of moving objects, even this quick bounding sphere test can take too long:  $N^2$  times if there are  $N$  objects
- reducing this  $N^2$  problem is called *pair reduction*
- pair testing isn't a big issue until  $N > 50$  or so...

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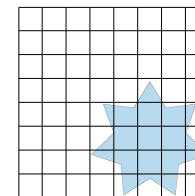
## Spatial Data Structures

- can only hit something that is close
- spatial data structures tell you what is close to object
  - uniform grid, octrees, kd-trees, BSP trees
  - bounding volume hierarchies
    - OBB trees
  - for player-wall problem, typically use same spatial data structure as for rendering
    - BSP trees most common

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## Uniform Grids

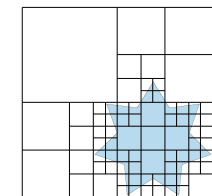
- axis-aligned
- divide space uniformly



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## Quadtrees/Octrees

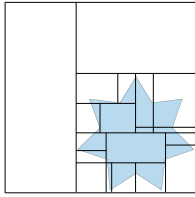
- axis-aligned
- subdivide until no points in cell



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## KD Trees

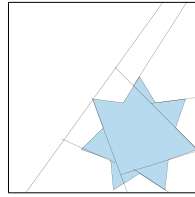
- axis-aligned
- subdivide in alternating dimensions



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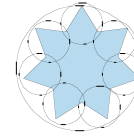
## BSP Trees

- planes at arbitrary orientation



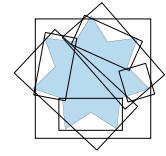
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## Bounding Volume Hierarchies



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## OBB Trees



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## Related Reading

- Real-Time Rendering
  - Tomas Moller and Eric Haines
  - on reserve in CICS reading room

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## Acknowledgement

- slides borrow heavily from
  - Stephen Chenney, (UWisc CS679)
    - <http://www.cs.wisc.edu/~schenney/courses/cs679-f2003/lectures/cs679-22.ppt>
- slides borrow lightly from
  - Steve Rotenberg, (UCSD CSE169)
    - [http://graphics.ucsd.edu/courses/cse169\\_w05/CSE169\\_17.ppt](http://graphics.ucsd.edu/courses/cse169_w05/CSE169_17.ppt)
- further reading: Real-Time Rendering
  - Tomas Moller and Eric Haines
  - on reserve in CICS reading room

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## Antialiasing

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## Reading for Antialiasing

- FCG Sec 3.7 Simple Antialiasing
- FCG Sec 10.11.1 Antialiasing
- FCG Chap 4 Signal Processing (optional)

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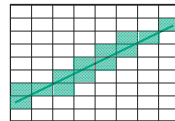
## Samples

- most things in the real world are **continuous**
- everything in a computer is **discrete**
- the process of mapping a continuous function to a discrete one is called **sampling**
- the process of mapping a discrete function to a continuous one is called **reconstruction**
- the process of mapping a continuous variable to a discrete one is called **quantization**
- rendering an image requires sampling and quantization
- displaying an image involves reconstruction

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## Jaggy Line Segments

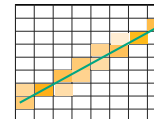
- we tried to sample a line segment so it would map to a 2D raster display
- we quantized the pixel values to 0 or 1
- we saw stairsteps / jaggies



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## Less Jaggy Line Segments

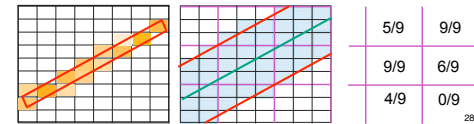
- better if quantize to many shades
  - image is less visibly jaggy
- find color for area, not just single point at center of pixel
  - **supersampling**: sample at higher frequency than intended display size



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## Supersample and Average

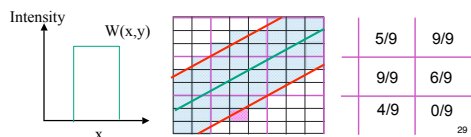
- supersample: create image at higher resolution
  - e.g. 768x768 instead of 256x256
  - shade pixels wrt area covered by thick line/rectangle
- average across many pixels
  - e.g. 3x3 small pixel block to find value for 1 big pixel
  - rough approximation divides each pixel into a finer grid of pixels



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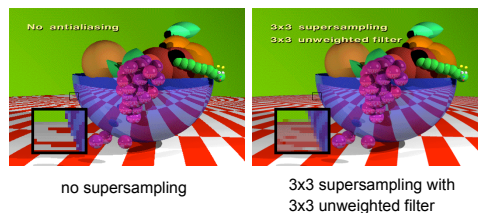
## Supersample and Average

- supersample: jaggies less obvious, but still there
  - small pixel center check still misses information
  - unweighted area sampling
    - equal areas cause equal intensity, regardless of distance from pixel center to area
    - aka box filter



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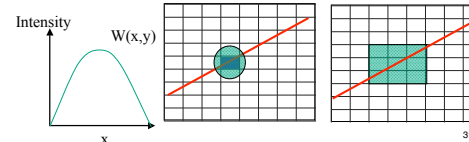
## Supersampling Example: Image



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## Weighted Area Sampling

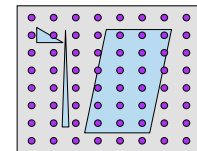
- intuitively, pixel cut through the center should be more heavily weighted than one cut along corner
- weighting function,  $W(x,y)$ 
  - specifies the contribution of primitive passing through the point  $(x, y)$  from pixel center
  - Gaussian filter (or approximation) commonly used



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## Sampling Errors

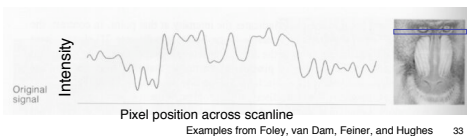
- some objects missed entirely, others poorly sampled
  - could try unweighted or weighted area sampling
  - but how can we be sure we show everything?
- need to think about entire class of solutions!
  - brief taste of signal processing (Chap 4 FCG)



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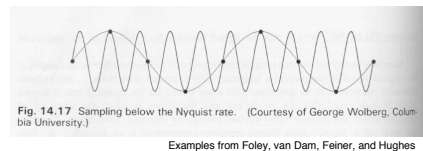
## Image As Signal

- image as spatial signal
- 2D raster image
  - discrete sampling of 2D spatial signal
- 1D slice of raster image
  - discrete sampling of 1D spatial signal



## Sampling Frequency

- if don't sample often enough, resulting signal misinterpreted as lower-frequency one
  - we call this **aliasing**



## Sampling Theorem

continuous signal can be completely recovered from its samples

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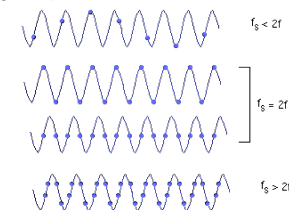
sampling rate greater than twice maximum frequency present in signal

- Claude Shannon

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## Nyquist Rate

- lower bound on sampling rate
  - twice the highest frequency component in the image's spectrum

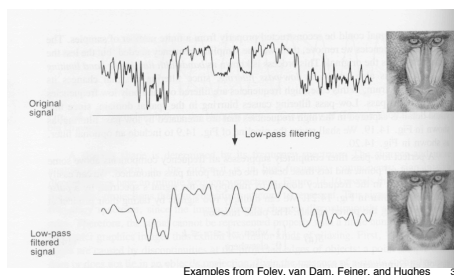


## Aliasing

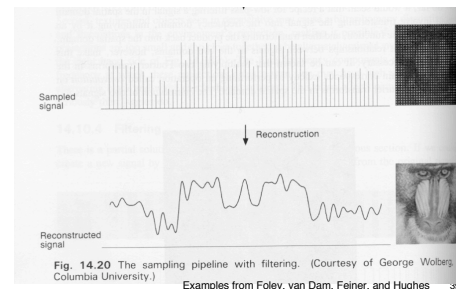
- incorrect appearance of high frequencies as low frequencies
- to avoid: **antialiasing**
  - supersample
    - sample at higher frequency
  - low pass filtering
    - remove high frequency function parts
    - aka prefiltering, band-limiting

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## Low-Pass Filtering

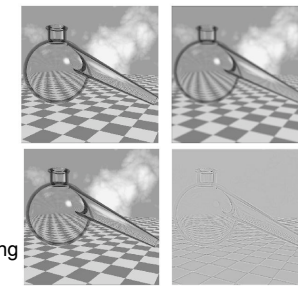


## Low-Pass Filtering



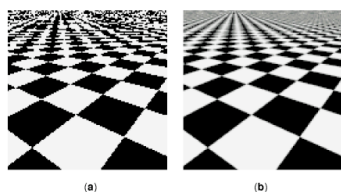
## Filtering

- low pass
  - blur
- high pass
  - edge finding



## Texture Antialiasing

- texture mipmapping: low pass filter



## Temporal Antialiasing

- subtle point: collision detection about algorithms for finding collisions *in time* as much as space
- temporal sampling
  - aliasing: can miss collision completely with point samples!
- temporal antialiasing
  - test line segment representing motion of object center

