



Tamara Munzner

Hidden Surfaces

<http://www.ugrad.cs.ubc.ca/~cs314/Vjan2013>

Clarification: Blinn-Phong Model

- only change vs Phong model is to have the specular calculation to use $(\mathbf{h} \cdot \mathbf{n})$ instead of $(\mathbf{v} \cdot \mathbf{r})$
- full Blinn-Phong lighting model equation has ambient, diffuse, specular terms

$$\mathbf{I}_{\text{total}} = k_a \mathbf{I}_{\text{ambient}} + \sum_{i=1}^{\#lights} \mathbf{I}_i (k_d (\mathbf{n} \cdot \mathbf{l}_i) + k_s (\mathbf{n} \cdot \mathbf{h}_i)^{n_{shiny}})$$

- just like full Phong model equation

$$\mathbf{I}_{\text{total}} = k_a \mathbf{I}_{\text{ambient}} + \sum_{i=1}^{\#lights} \mathbf{I}_i (k_d (\mathbf{n} \cdot \mathbf{l}_i) + k_s (\mathbf{v} \cdot \mathbf{r}_i)^{n_{shiny}})$$

2

Reading for Hidden Surfaces

- FCG Sect 8.2.3 Z-Buffer
- FCG Sect 12.4 BSP Trees
 - (8.1, 8.2 2nd ed)
- FCG Sect 3.4 Alpha Compositing
 - (N/A 2nd ed)

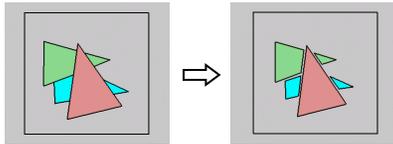
3

Hidden Surface Removal

4

Occlusion

- for most interesting scenes, some polygons overlap

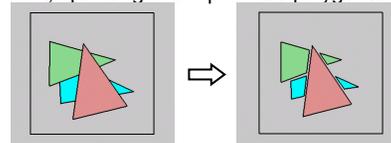


- to render the correct image, we need to determine which polygons occlude which

5

Painter's Algorithm

- simple: render the polygons from back to front, "painting over" previous polygons



- draw blue, then green, then orange
- will this work in the general case?

6

Painter's Algorithm: Problems

- intersecting polygons* present a problem
- even non-intersecting polygons can form a cycle with no valid visibility order:



7

Analytic Visibility Algorithms

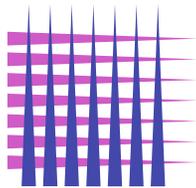
- early visibility algorithms computed the set of visible polygon *fragments* directly, then rendered the fragments to a display:



8

Analytic Visibility Algorithms

- what is the minimum worst-case cost of computing the fragments for a scene composed of n polygons?*
- answer:
 $O(n^2)$



9

Analytic Visibility Algorithms

- so, for about a decade (late 60s to late 70s) there was intense interest in finding efficient algorithms for *hidden surface removal*
- we'll talk about one:
 - Binary Space Partition (BSP) Trees*

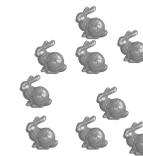
10

Binary Space Partition Trees (1979)

- BSP Tree: partition space with binary tree of planes
 - idea: divide space recursively into half-spaces by choosing splitting planes that separate objects in scene
 - preprocessing: create binary tree of planes
 - runtime: correctly traversing this tree enumerates objects from back to front

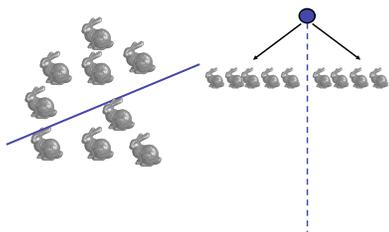
11

Creating BSP Trees: Objects



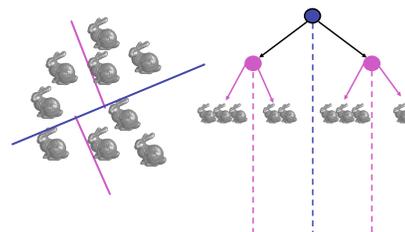
12

Creating BSP Trees: Objects



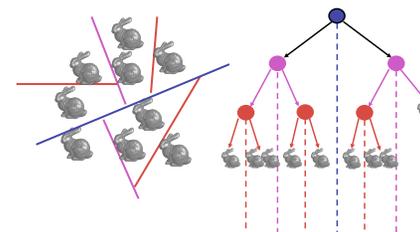
13

Creating BSP Trees: Objects



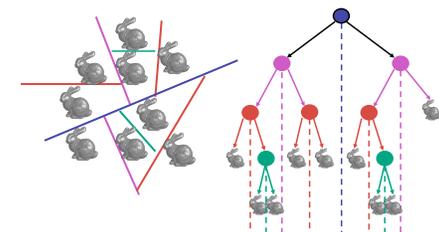
14

Creating BSP Trees: Objects



15

Creating BSP Trees: Objects



16

Splitting Objects

- no bunnies were harmed in previous example
- but what if a splitting plane passes through an object?
 - split the object; give half to each node



17

Traversing BSP Trees

- tree creation independent of viewpoint
 - preprocessing step
- tree traversal uses viewpoint
 - runtime, happens for many different viewpoints
- each plane divides world into near and far
 - for given viewpoint, decide which side is near and which is far
 - check which side of plane viewpoint is on independently for each tree vertex
 - tree traversal differs depending on viewpoint!
- recursive algorithm
 - recurse on far side
 - draw object
 - recurse on near side

18

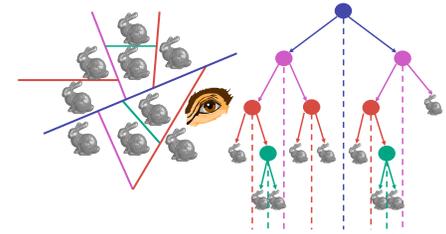
Traversing BSP Trees

query: given a viewpoint, produce an ordered list of (possibly split) objects from back to front:

```
renderBSP(BSPtree *T)
BSPtree *near, *far;
if (eye on left side of T->plane)
    near = T->left; far = T->right;
else
    near = T->right; far = T->left;
renderBSP(far);
if (T is a leaf node)
    renderObject(T)
renderBSP(near);
```

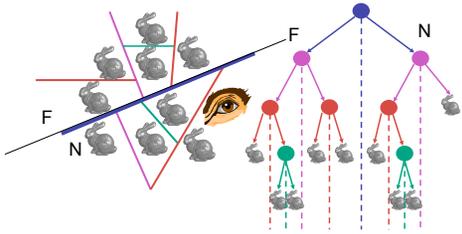
19

BSP Trees : Viewpoint A



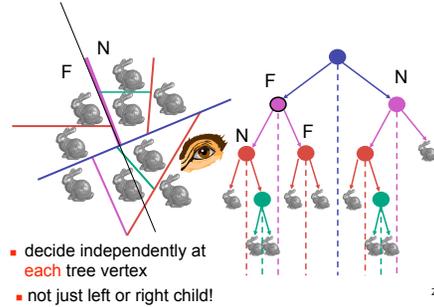
20

BSP Trees : Viewpoint A



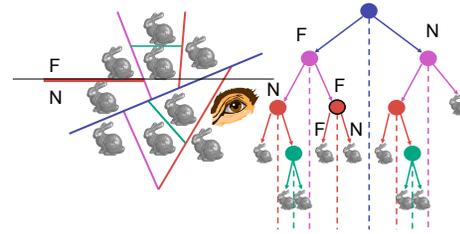
21

BSP Trees : Viewpoint A



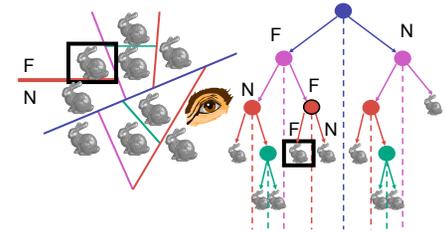
22

BSP Trees : Viewpoint A



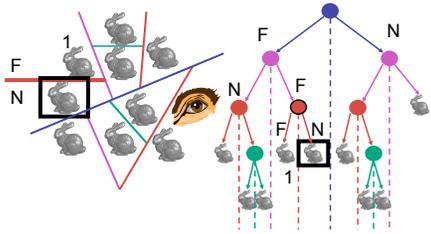
23

BSP Trees : Viewpoint A



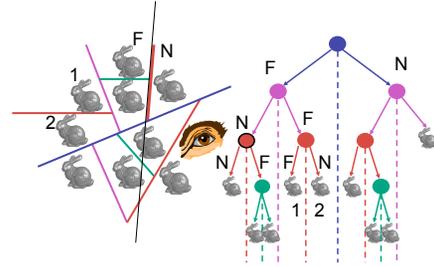
24

BSP Trees : Viewpoint A



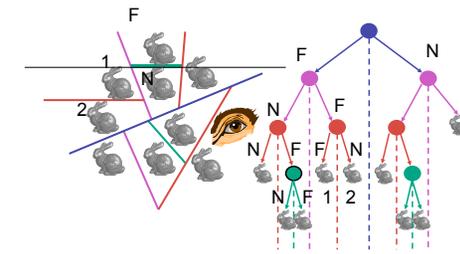
25

BSP Trees : Viewpoint A



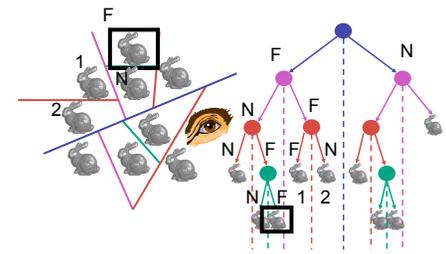
26

BSP Trees : Viewpoint A



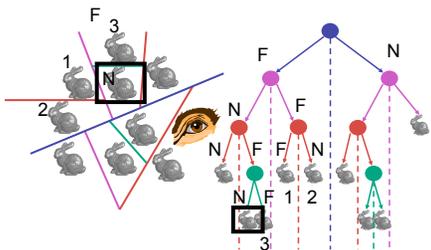
27

BSP Trees : Viewpoint A



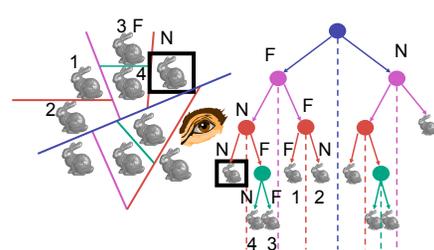
28

BSP Trees : Viewpoint A



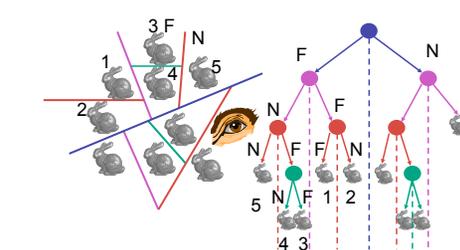
29

BSP Trees : Viewpoint A



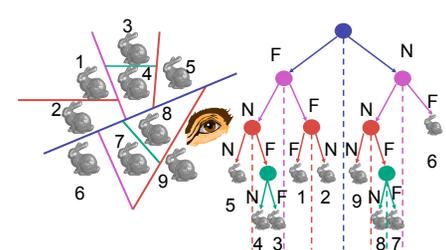
30

BSP Trees : Viewpoint A



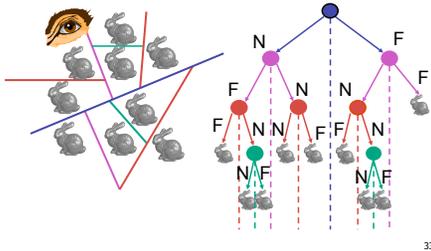
31

BSP Trees : Viewpoint A



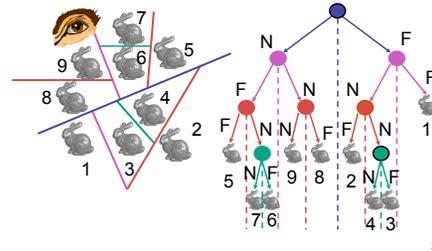
32

BSP Trees : Viewpoint B



33

BSP Trees : Viewpoint B



34

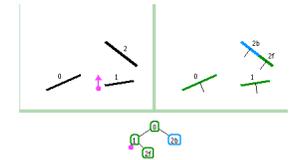
BSP Tree Traversal: Polygons

- split along the plane defined by any polygon from scene
- classify all polygons into positive or negative half-space of the plane
 - if a polygon intersects plane, split polygon into two and classify them both
- recurse down the negative half-space
- recurse down the positive half-space

35

BSP Demo

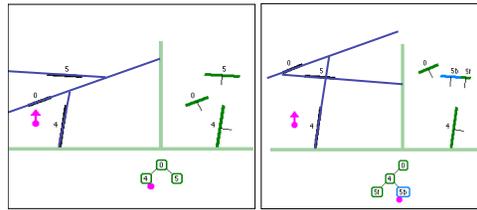
- useful demo: <http://symbolcraft.com/graphics/bsp>



36

BSP Demo

- order of insertion can affect half-plane extent



37

Summary: BSP Trees

- pros:
 - simple, elegant scheme
 - correct version of painter's algorithm back-to-front rendering approach
 - was very popular for video games (but getting less so)
- cons:
 - slow to construct tree: $O(n \log n)$ to split, sort
 - splitting increases polygon count: $O(n^2)$ worst-case
 - computationally intense preprocessing stage restricts algorithm to static scenes

38

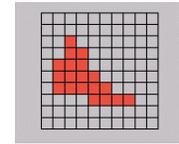
The Z-Buffer Algorithm (mid-70's)

- BSP trees proposed when memory was expensive
 - first 512x512 framebuffer was >\$50,000!
- Ed Catmull proposed a radical new approach called **z-buffering**
- the big idea:
 - resolve visibility **independently at each pixel**

39

The Z-Buffer Algorithm

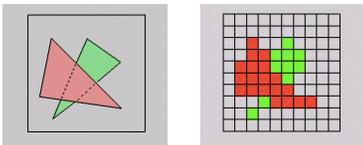
- we know how to rasterize polygons into an image discretized into pixels:



40

The Z-Buffer Algorithm

- what happens if multiple primitives occupy the same pixel on the screen?
 - which is allowed to paint the pixel?



41

The Z-Buffer Algorithm

- idea: retain depth after projection transform
 - each vertex maintains z coordinate
 - relative to eye point
 - can do this with canonical viewing volumes

42

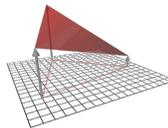
The Z-Buffer Algorithm

- augment color framebuffer with **Z-buffer** or **depth buffer** which stores Z value at each pixel
 - at frame beginning, initialize all pixel depths to ∞
 - when rasterizing, interpolate depth (Z) across polygon
 - check Z-buffer before storing pixel color in framebuffer and storing depth in Z-buffer
 - don't write pixel if its Z value is more distant than the Z value already stored there

43

Interpolating Z

- barycentric coordinates
 - interpolate Z like other planar parameters



44

Z-Buffer

- store (r,g,b,z) for each pixel
- typically 8+8+8+24 bits, can be more

```

for all i,j {
  Depth[i,j] = MAX_DEPTH
  Image[i,j] = BACKGROUND_COLOUR
}
for all polygons P {
  for all pixels in P {
    if (Z_pixel < Depth[i,j]) {
      Image[i,j] = C_pixel
      Depth[i,j] = Z_pixel
    }
  }
}
    
```

45

Depth Test Precision

- reminder: perspective transformation maps eye-space (view) z to NDC z

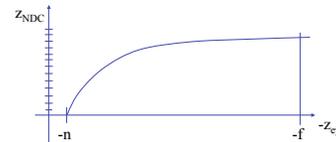
$$\begin{bmatrix} E & 0 & A & 0 \\ 0 & F & B & 0 \\ 0 & 0 & C & D \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} Ex + Az \\ Fy + Bz \\ Cz + D \\ -z \end{bmatrix} = \begin{bmatrix} -\left(\frac{Ex}{z} + Az\right) \\ -\left(\frac{Fy}{z} + Bz\right) \\ -\left(C + \frac{D}{z}\right) \\ 1 \end{bmatrix}$$

- thus: $z_{NDC} = -\left(C + \frac{D}{z_{eye}}\right)$

46

Depth Test Precision

- therefore, depth-buffer essentially stores $1/z$, rather than z!
- issue with integer depth buffers
 - high precision for near objects
 - low precision for far objects



47

Depth Test Precision

- low precision can lead to **depth fighting** for far objects
 - two different depths in eye space get mapped to same depth in framebuffer
 - which object "wins" depends on drawing order and scan-conversion
- gets worse for larger ratios $f:n$
 - *rule of thumb*: $f:n < 1000$ for 24 bit depth buffer
- with 16 bits cannot discern millimeter differences in objects at 1 km distance
- demo: sjbaker.org/steve/omniv/love_your_z_buffer.html

48

More: Integer Depth Buffer

- reminder from picking discussion
 - depth lies in the NDC z range [0,1]
 - format: multiply by $2^n - 1$ then round to nearest int
 - where n = number of bits in depth buffer
- 24 bit depth buffer = $2^{24} = 16,777,216$ possible values
 - small numbers near, large numbers far
- consider depth from VCS: $(1 < N) * (a + b / z)$
 - N = number of bits of Z precision
 - $a = zFar / (zFar - zNear)$
 - $b = zFar * zNear / (zNear - zFar)$
 - z = distance from the eye to the object

49

Z-Buffer Algorithm Questions

- how much memory does the Z-buffer use?
- does the image rendered depend on the drawing order?
- does the time to render the image depend on the drawing order?
- how does Z-buffer load scale with visible polygons? with framebuffer resolution?

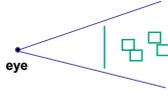
50

Z-Buffer Pros

- simple!!!
- easy to implement in hardware
 - hardware support in all graphics cards today
- polygons can be processed in arbitrary order
- easily handles polygon interpenetration
- enables **deferred shading**
 - rasterize shading parameters (e.g., surface normal) and only shade final visible fragments

51

Z-Buffer Cons

- poor for scenes with high depth complexity
 - need to render all polygons, even if most are invisible
- 
- shared edges are handled inconsistently
 - ordering dependent**

52

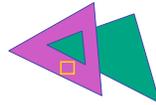
Z-Buffer Cons

- requires lots of memory
 - (e.g. 1280x1024x32 bits)
- requires fast memory
 - Read-Modify-Write in inner loop
- hard to simulate translucent polygons
 - we throw away color of polygons behind closest one
 - works if polygons ordered back-to-front
 - extra work throws away much of the speed advantage

53

Hidden Surface Removal

- two kinds of visibility algorithms
 - object space methods
 - image space methods



54

Object Space Algorithms

- determine visibility on object or polygon level
 - using camera coordinates
- resolution independent
 - explicitly compute visible portions of polygons
- early in pipeline
 - after clipping
- requires depth-sorting
 - painter's algorithm
 - BSP trees

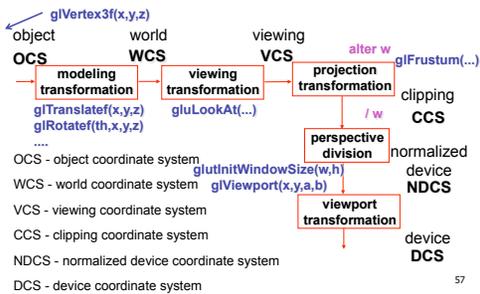
55

Image Space Algorithms

- perform visibility test for in screen coordinates
 - limited to resolution of display
 - Z-buffer: check every pixel independently
- performed late in rendering pipeline

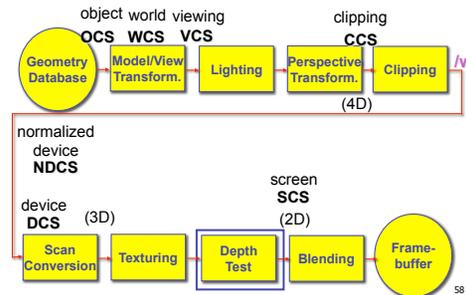
56

Projective Rendering Pipeline



57

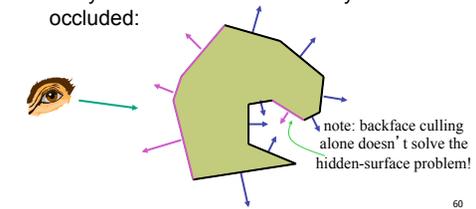
Rendering Pipeline



58

Back-Face Culling

- on the surface of a closed orientable manifold, polygons whose normals point away from the camera are always occluded:



60

Backface Culling

59

Back-Face Culling

- not rendering backfacing polygons improves performance
 - by how much?
 - reduces by about half the number of polygons to be considered for each pixel
 - optimization when appropriate

61

Back-Face Culling

- most objects in scene are typically "solid"
- rigorously: **orientable closed manifolds**
 - orientable**: must have two distinct sides
 - cannot self-intersect
 - a sphere is orientable since has two sides, 'inside' and 'outside'.
 - a Mobius strip or a Klein bottle is not orientable
 - closed**: cannot "walk" from one side to the other
 - sphere is closed manifold
 - plane is not



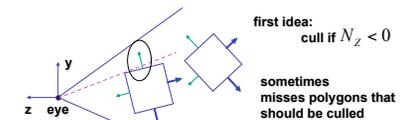
Back-Face Culling

- examples of non-manifold objects:
 - a single polygon
 - a terrain or height field
 - polyhedron w/ missing face
 - anything with cracks or holes in boundary
 - one-polygon thick lampshade



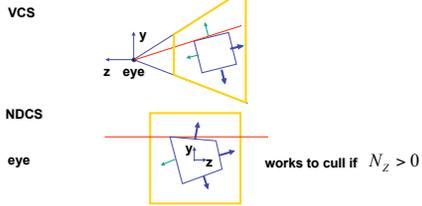
63

Back-face Culling: VCS



64

Back-face Culling: NDCS



65

Invisible Primitives

- why might a polygon be invisible?
 - polygon outside the *field of view / frustum*
 - solved by **clipping**
 - polygon is **backfacing**
 - solved by **backface culling**
 - polygon is **occluded** by object(s) nearer the viewpoint
 - solved by **hidden surface removal**

66

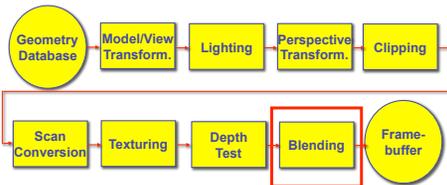


67

Blending

68

Rendering Pipeline



69

Alpha and Premultiplication

- specify opacity with alpha channel α
 - $\alpha=1$: opaque, $\alpha=.5$: translucent, $\alpha=0$: transparent
- how to express a pixel is half covered by a red object?
 - obvious way: store color independent from transparency (r,g,b, α)
 - intuition: alpha as transparent colored glass
 - 100% transparency can be represented with many different RGB values
 - pixel value is (1,0,0,.5)
 - upside: easy to change opacity of image, very intuitive
 - downside: compositing calculations are more difficult - not associative
 - elegant way: premultiply by α so store (cr, cg, cb, α)
 - intuition: alpha as screen/mesh
 - RGB specifies how much color object contributes to scene
 - alpha specifies how much object obscures whatever is behind it (coverage)
 - alpha of .5 means half the pixel is covered by the color, half completely transparent
 - only one 4-tuple represents 100% transparency: (0,0,0,0)
 - pixel value is (.5, 0, 0, .5)
 - upside: compositing calculations easy (& additive blending for glowing!)
 - downside: less intuitive

70

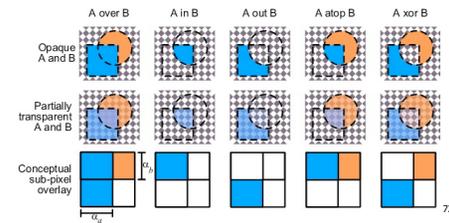
Alpha and Simple Compositing

- F is foreground, B is background, F over B
- premultiply math: uniform for each component, simple, linear
 - $R' = R_F + (1-A_F)R_B$
 - $G' = G_F + (1-A_F)G_B$
 - $B' = B_F + (1-A_F)B_B$
 - $A' = A_F + (1-A_F)A_B$
 - associative: easy to chain together multiple operations
- non-premultiply math: trickier
 - $R' = (R_F A_F + (1-A_F)R_B A_B) / A'$
 - $G' = (G_F A_F + (1-A_F)G_B A_B) / A'$
 - $B' = (B_F A_F + (1-A_F)B_B A_B) / A'$
 - $A' = A_F + (1-A_F)A_B$
 - don't need divide if F or B is opaque. but still... oof!
 - chaining difficult, must avoid double-counting with intermediate ops

71

Alpha and Complex Compositing

- foreground color **A**, background color **B**
- how might you combine multiple elements?
 - Compositing Digital Images, Porter and Duff, Siggraph '84
 - pre-multiplied alpha allows all cases to be handled simply



72

Alpha Examples

- blend white and clear equally (50% each)
 - white is (1,1,1), clear is (0,0,0,0), black is (0,0,0,1)
 - premultiplied: multiply componentwise by 50% and just add together
 - (.5, .5, .5, .5) is indeed half-transparent white in premultiply format
 - 4-tuple would mean half-transparent grey in non-premultiply format
- premultiply allows both conventional blend and additive blend
 - alpha 0 and RGB nonzero: glowing/luminescent
 - (nice for particle systems, stay tuned)
- for more: see nice writeup from Alvy Ray Smith
 - technical academy award for Smith, Catmull, Porter, Duff
 - <http://www.alvyray.com/Awards/AwardsAcademy96.htm>

73