

Last Time

factor analysis

- similar to probabilistic PCA

PCA noise: (Gaussian, isotropic)

FA noise: different entries on diag (not isotropic)

On PCA

$$D \begin{bmatrix} X \\ N \end{bmatrix} \xRightarrow{\text{PCA}} D \begin{bmatrix} H \\ M \end{bmatrix} \begin{bmatrix} W \\ N \end{bmatrix}$$

H eigenvectors W coefficients
 M N

- finding these matrices that approximates the full data set
- difference ideally as close as possible

PCA: columns of H orthonormal

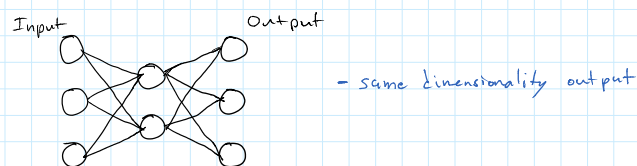
NMF: H, W no negative elements Non-Negative Matrix Factorization

Sparse Coding: coefficients have sparsity

- requires iterative optimizer
why? - represent as additive sum of 'templates'

Auto encoders

- neural network for unsupervised learning



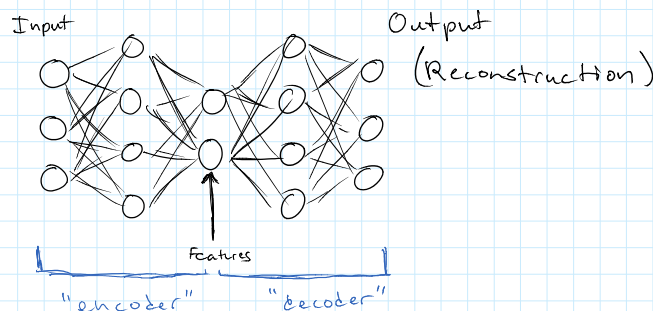
- same dimensionality output

↑ "Information Bottleneck"

- 3d worth of info, 2d squeeze, recover as close as possible in output

- multiple layers allows for a more rich representation
- Linear version (one hidden layer) performs PCA

Alternative Picture:



Specific Models:

- sparse auto encoder (sparse feature vectors)
- penalty on hidden layer (ie. L_1 penalty)

$$\min_{\{w_j\}} \frac{1}{N} \sum_{n=1}^N \|x_n - \tilde{x}_n\|_2^2 + L_1 \text{ makes it sparse}$$

- De-noising auto encoder

- corrupt input with noise
- try to reconstruct original
- features shouldn't be sensitive to small variations
- robustness

Information Theory angle ("information bottleneck")

- imagine discrete: started with '3' bits, brought it to '2' bits, and back to '3'
- "Fit this thing into some size"
 - JPEG encoding
- "Lossy Compression"

Analogy to brain: only firing sparse subset of neurons for some given input.