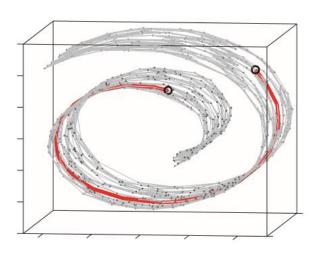
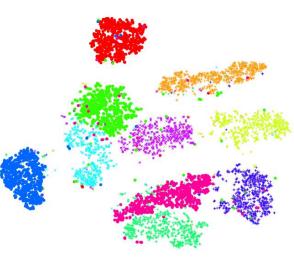
## CPSC 340: Machine Learning and Data Mining

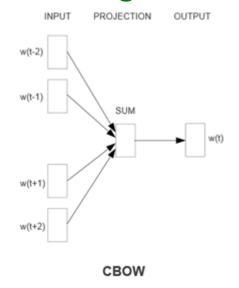
Deep Learning Fall 2019

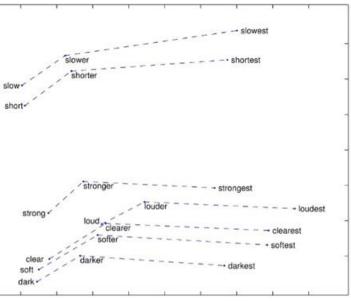
## Last Time: Multi-Dimensional Scaling

- Modern multi-dimensional scaling (MDS) methods:
  - ISOMAP uses geodesic distance in data manifold.
  - T-SNE tends to reveal clusters and manifold structures.
  - Word2vec gives continuous alternative to bag of words.









http://wearables.cc.gatech.edu/paper\_of\_week/isomap.pdf http://lvdmaaten.github.io/publications/papers/JMLR\_2008.pdf http://sebastianruder.com/secret-word2vec http://sebastianruder.com/secret-word2vec

## Word2Vec

#### • Subtracting word vectors to find related vectors.

Table 8: Examples of the word pair relationships, using the best word vectors from Table 4 (Skipgram model trained on 783M words with 300 dimensionality).

Relationship	Example 1	Example 2	Example 3
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee
big - bigger	small: larger	cold: colder	quick: quicker
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter
Sarkozy - France	Berlusconi: Italy	Merkel: Germany	Koizumi: Japan
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza

Table 8 shows words that follow various relationships. We follow the approach described above: the relationship is defined by subtracting two word vectors, and the result is added to another word. Thus for example, *Paris - France + Italy = Rome*. As it can be seen, accuracy is quite good, although

Word vectors for 157 languages <u>here</u>.

## End of Part 4: Key Concepts

• We discussed linear latent-factor models:

$$f(W,z) = \hat{z} \hat{z} (\langle w_{j}z_{j} \rangle - x_{ij})^{2}$$
$$= \hat{z} ||W^{T}z_{i} - x_{i}||^{2}$$
$$= ||ZW - X||_{F}^{2}$$

- Represent 'X' as linear combination of latent factors 'w<sub>c</sub>'.
  - Latent features ' $z_i$ ' give a lower-dimensional version of each ' $x_i$ '.
  - When k=1, finds direction that minimizes squared orthogonal distance.
- Applications:
  - Outlier detection, dimensionality reduction, data compression, features for linear models, visualization, factor discovery, filling in missing entries.

## End of Part 4: Key Concepts

• We discussed linear latent-factor models:

$$f(W_{j}z) = \hat{z} \hat{z} \hat{z} (\langle w_{j}z \rangle - x_{ij})^{2}$$

- Principal component analysis (PCA):
  - Often uses orthogonal factors and fits them sequentially (via SVD).
- Non-negative matrix factorization:
  - Uses non-negative factors giving sparsity.
  - Can be minimized with projected gradient.
- Many variations are possible:
  - Different regularizers (sparse coding) or loss functions (robust/binary PCA).
  - Missing values (recommender systems) or change of basis (kernel PCA).

## End of Part 4: Key Concepts

- We discussed multi-dimensional scaling (MDS):
  - Non-parametric method for high-dimensional data visualization.
  - Tries to match distance/similarity in high-/low-dimensions.
    - "Gradient descent on scatterplot points".
- Main challenge in MDS methods is "crowding" effect:
  - Methods focus on large distances and lose local structure.
- Common solutions:
  - Sammon mapping: use weighted cost function.
  - ISOMAP: approximate geodesic distance using via shortest paths in graph.
     T-SNE: give up on large distances and focus on neighbour distances.
- Word2vec is a recent MDS method giving better "word features".

## Supervised Learning Roadmap

- Part 1: "Direct" Supervised Learning.
  - We learned parameters 'w' based on the original features  $x_i$  and target  $y_i$ .
- Part 3: Change of Basis.
  - We learned parameters 'v' based on a change of basis  $z_i$  and target  $y_i$ .
- Part 4: Latent-Factor Models.
  - We learned parameters 'W' for basis  $z_i$  based on only on features  $x_i$ .

Wn

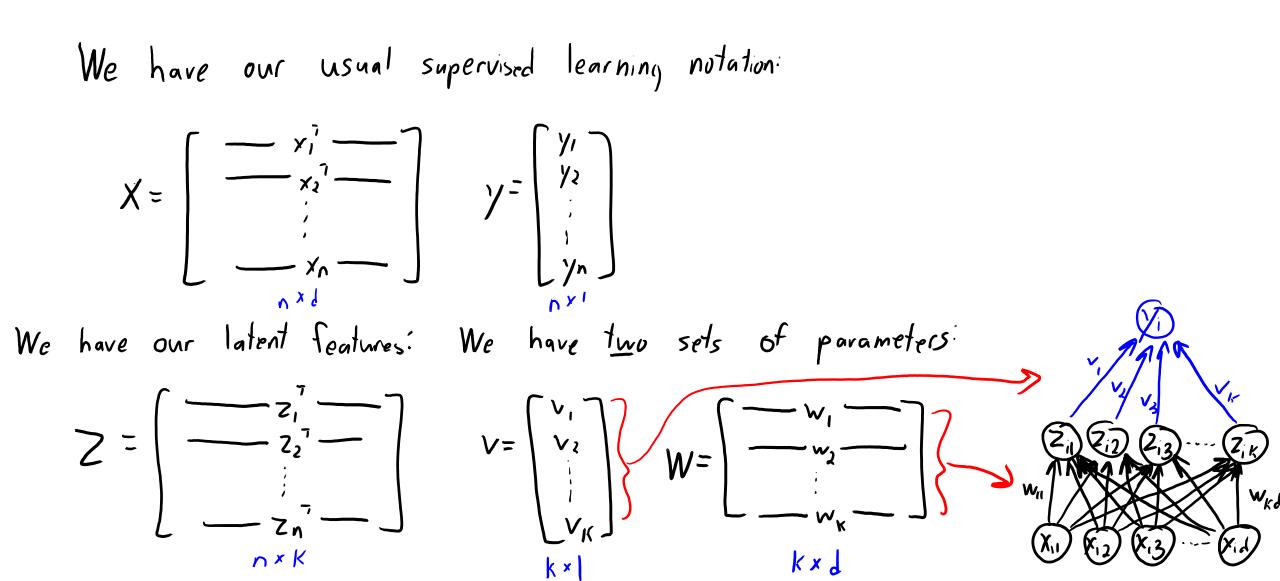
WK

- You can then learn 'v' based on change of basis  $z_i$  and target  $y_i$ .
- Part 5: Neural Networks.
  - Jointly learn 'W' and 'v' based on  $x_i$  and  $y_i$ .
  - Learn basis z<sub>i</sub> that is good for supervised learning.

#### A Graphical Summary of CPSC 340 Parts 1-5

Part 1: "I have features xi" Part 3: Change of basis Part 4: basis from latent-factor Port 5: Neural networks model (Zik)  $(2_{12})$ (Z13) -- (Z15) "PCA will give me good fectures" TI think this Part 2." What is the group of x,?" basis will work (X,n)  $(X, V) \times V \times V$  $(\mathbf{x}_{i})$   $(\mathbf{x}_{i})$ - - (X, ) Learn features "What are the 'parts' of x,?" classifier at Traine separatel Same Time.

#### **Notation for Neural Networks**



#### Linear-Linear Model

• Obvious choice: linear latent-factor model with linear regression.

Use features from latent-factor model: 
$$z_i = Wx_i$$
  
Make predictions using a linear model:  $y_i = v^7 z_i$ 

• We want to train 'W' and 'v' jointly, so we could minimize:

$$f(W,v) = \frac{1}{2} \sum_{i=1}^{n} (\sqrt{z_i} - \gamma_i)^2 = \frac{1}{2} \sum_{i=1}^{n} (\sqrt{W_{x_i}} - \gamma_i)^2$$

$$\lim_{\substack{i \text{ near regression with } z_i \text{ as features}} \int_{\substack{i = 1 \\ i = 1$$

## Introducing Non-Linearity

- To increase flexibility, something needs to be non-linear.
- Typical choice: transform z<sub>i</sub> by non-linear function 'h'.

$$z_i = W_{x_i} \qquad y_i = v^T h(z_i)$$

- Here the function 'h' transforms 'k' inputs to 'k' outputs.

• Common choice for 'h': applying sigmoid function element-wise:

$$h(z_{ic}) = \frac{1}{1 + exp(-z_{ic})}$$

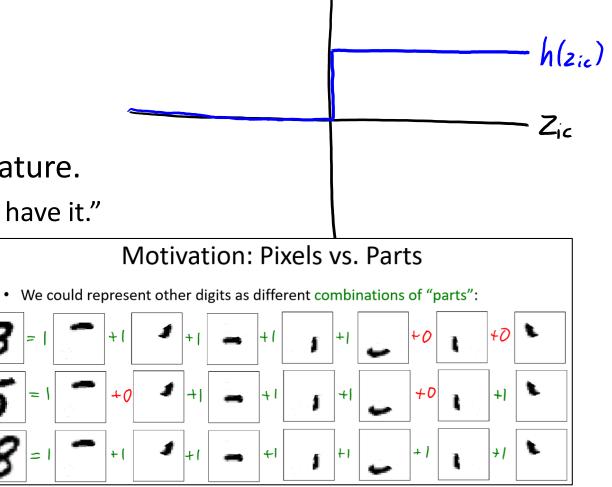
- So this takes the  $z_{ic}$  in  $(-\infty,\infty)$  and maps it to (0,1).
- This is called a "multi-layer perceptron" or a "neural network".

## Why Sigmoid?

• Consider setting 'h' to define binary features z<sub>i</sub> using:

$$h(z_{ic}) = \begin{cases} 1 & \text{if } z_{ic} = 70 \\ 20 & \text{if } z_{ic} < 0 \end{cases}$$

- Each h(zi) can be viewed as binary feature.
  - "You either have this 'part' or you don't have it."
- We can make 2<sup>k</sup> objects by all the possible "part combinations".



## Why Sigmoid?

Zic

• Consider setting 'h' to define binary features z<sub>i</sub> using:

$$h(z_{ic}) = \begin{cases} 1 & \text{if } z_{ic} = 70 \\ 20 & \text{if } z_{ic} < 0 \end{cases}$$

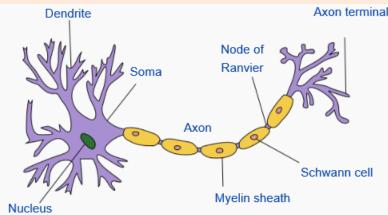
- Each h(zi) can be viewed as binary feature.
  - "You either have this 'part' or you don't have it."
- But this is hard to optimize (non-differentiable/discontinuous).
- Sigmoid is a smooth approximation to these binary features.
  - Non-parametric version is a universal approximator:
    - If 'k' grows appropriately with 'n', can model any continuous function.

#### Supervised Learning Roadmap

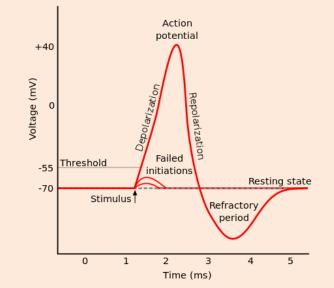
Hund-engineered features Learn a latent-factor model: Learn 'n' and W' together. Neural network. w<sub>a</sub> | WKd V  $(2_{12})$ (Z.) (x12) (x13) ···-(X.) Use latent features "I think this W<sub>II</sub> in supervised model: WKd basis will work " (K12) (X13) ····· (X14) w<sub>a</sub> | WKd But still gives a (×13) linear model  $(\mathbf{X}_{1})$   $(\mathbf{X}_{1})$   $(\mathbf{X}_{1})$   $(\mathbf{X}_{1})$   $(\mathbf{X}_{1})$ ··-- (Zik) Good representation of Requires domain knowledge and can be time- consuming Extra non-linear transformation 'h' X; might be bad for predicting y:

## Why "Neural Network"?

• Cartoon of "typical" neuron:

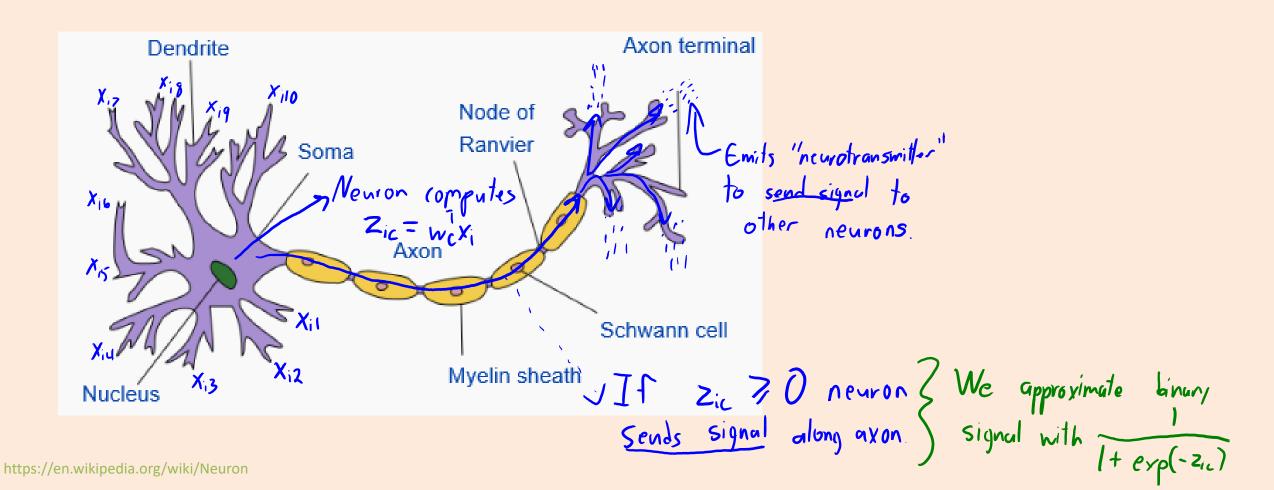


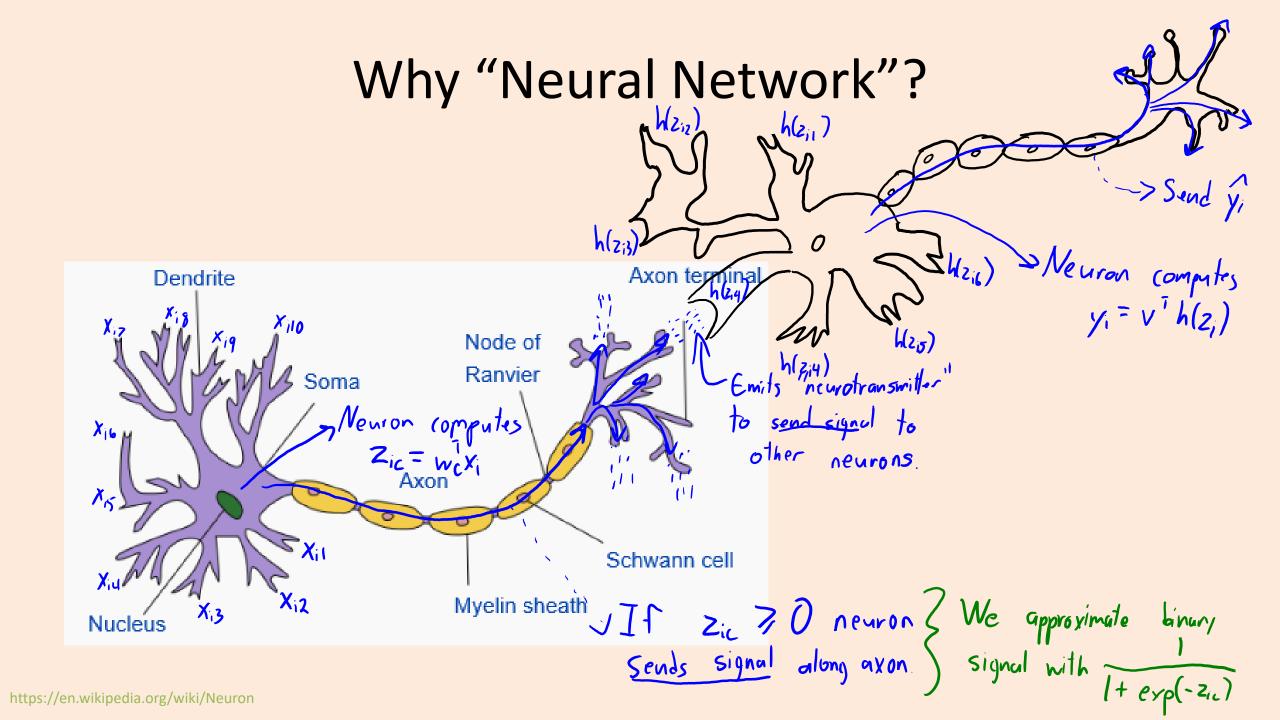
- Neuron has many "dendrites", which take an input signal.
- Neuron has a single "axon", which sends an output signal.
- With the right input to dendrites:
  - "Action potential" along axon (like a binary signal):



https://en.wikipedia.org/wiki/Neuron https://en.wikipedia.org/wiki/Action\_potential

#### Why "Neural Network"?



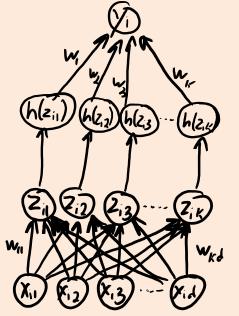


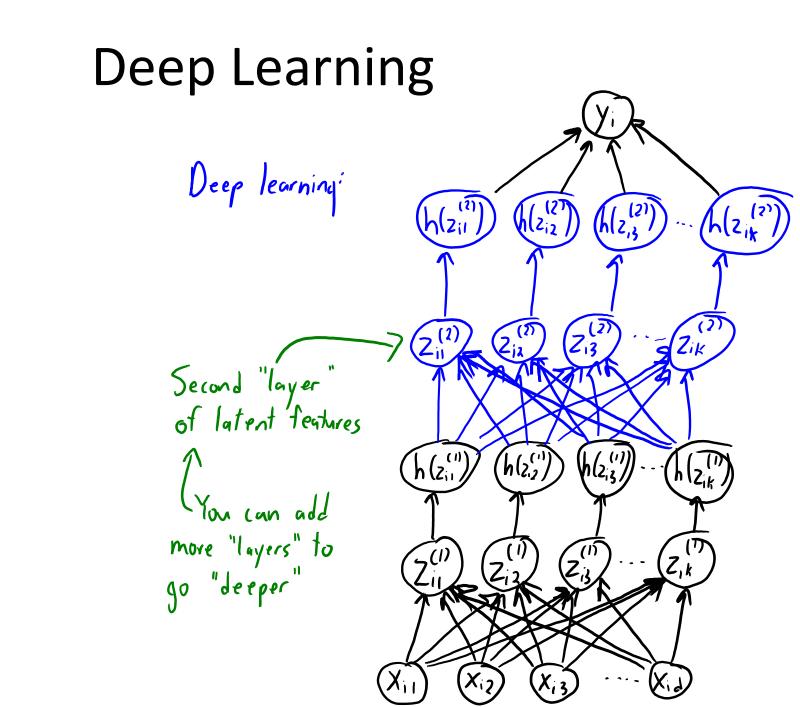
#### Why "Neural Network"?

-> Predictions based on aggregation vTh(Wx;) at y: "neuron" -> Synapse between Zik and yi neuron Spinory signal h(wcx,) sent along "axon" h(zk , Neuron aggregates signals: w.x. "dendrites" for Zik "neuron" are reciving xij values W<sub>(1</sub> WKd

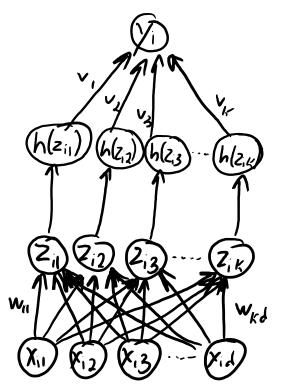
#### "Artificial" Neural Nets vs. "Real" Networks Nets

- Artificial neural network:
  - $x_i$  is measurement of the world.
  - $z_i$  is internal representation of world.
  - $y_i$  is output of neuron for classification/regression.
- Real neural networks are more complicated:
  - Timing of action potentials seems to be important.
    - "Rate coding": frequency of action potentials simulates continuous output.
  - Neural networks don't reflect sparsity of action potentials.
  - How much computation is done inside neuron?
  - Brain is highly organized (e.g., substructures and cortical columns).
  - Connection structure changes.
  - Different types of neurotransmitters.



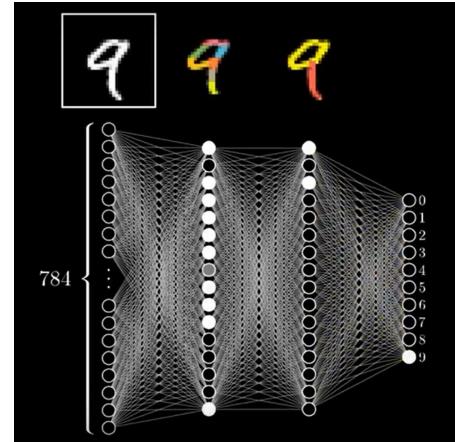


Neural network.



## "Hierarchies of Parts" Motivation for Deep Learning

- Each "neuron" might recognize
  - a "part" of a digit.
  - "Deeper" neurons might recognize combinations of parts.
  - Represent complex objects as hierarchical combinations of re-useable parts (a simple "grammar").
- Watch the full video here:
  - <u>https://www.youtube.com/watch?v=aircAruvnKk</u>



- Theory:
  - 1 big-enough hidden layer already gives universal approximation.
  - But some functions require exponentially-fewer parameters to approximate with more layers (can fight curse of dimensionality).

#### Deep Learning Linear model: $\hat{y}_i = w^T x_i$ Deep learning (h(z,z)) (h(z (2))) h(212) Neural network with I hidden layer: $\gamma_i = v^{T} h(W_{x_i})$ (2) g Zik Neural network with 2 hidden layers $y_i = v^2 h(W^{(2)}h(W^{(1)}x_i))$ Second "layer" of latent features $h(z_{ii}^{(n)})$ ₩(2;3))· (h(z,2)) $h(z_{ik}^{(n)})$ You can add Neural network with 3 hidden layers $\hat{\gamma}_i = v^T h(W^{(3)}h(W^{(2)}h(W^{(1)}x_i)))$ more "layers" to go "deeper"

#### **Deep Learning**

• For 4 layers, we could write the prediction as:

$$\gamma_{i} = \sqrt{h} \left( W^{(4)} h(W^{(3)} h(W^{(2)} h(W^{(2)} x_{i}))) \right)$$

• For 'm' layers, we could use:

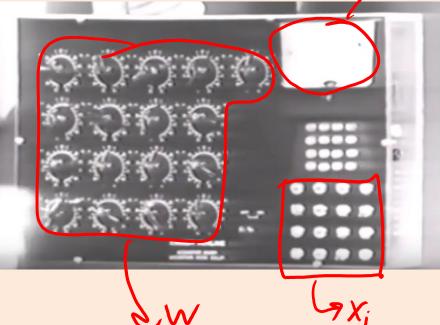
$$\frac{\text{Symbol}:}{\text{Meaning:}} \quad \prod_{k=0}^{n} f_{k}(t)$$

$$\frac{\text{Meaning:}}{\text{f}_{n} \circ f_{h-1} \circ f_{h-2} \circ \dots \circ f_{2} \circ f_{1} \circ f_{0}(t)}$$

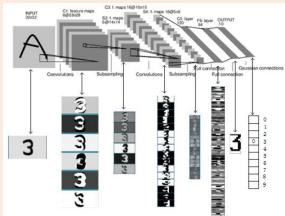
$$\hat{y}_{i} = \sqrt{T} \left( \frac{T}{L} h(W^{(l)}x_{i}) \right)$$

https://mathwithbaddrawings.com/2016/04/27/symbols-that-math-urgently-needs-to-adopt

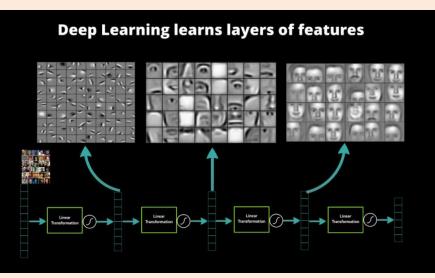
- 1950 and 1960s: Initial excitement.
  - Perceptron: linear classifier and stochastic gradient (roughly).
  - "the embryo of an electronic computer that [the Navy] expects will be able to walk, talk, see, write, reproduce itself and be conscious of its existence." w X; New York Times (1958).
    - https://www.youtube.com/watch?v=IEFRtz68m-8
  - Object recognition
     assigned to students as a summer project
- Then drop in popularity:
  - Quickly realized limitations of linear models.

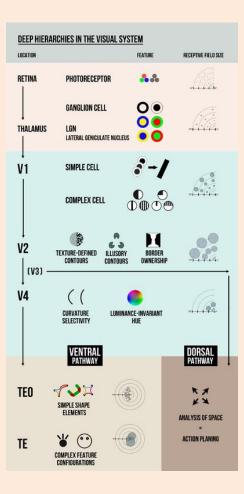


- 1970 and 1980s: Connectionism (brain-inspired ML)
  - Want "connected networks of simple units".
    - Use parallel computation and distributed representations.
  - Adding hidden layers z<sub>i</sub> increases expressive power.
    - With 1 layer and enough sigmoid units, a universal approximator.
  - Success in optical character recognition.



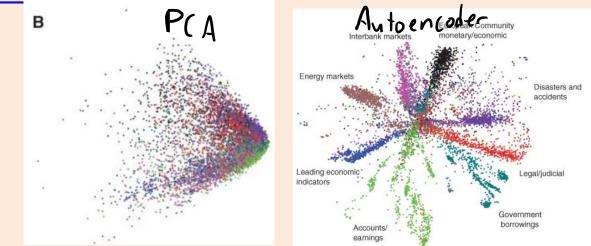
https://en.wikibooks.org/wiki/Sensory\_Systems/Visual\_Signal\_Processing http://www.datarobot.com/blog/a-primer-on-deep-learning/ http://blog.csdn.net/strint/article/details/44163869





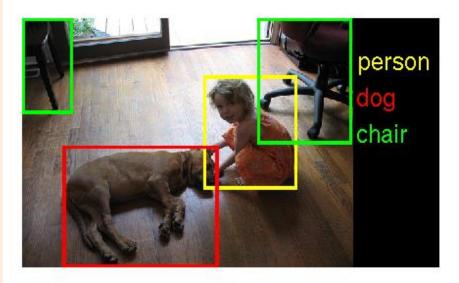
- 1990s and early-2000s: drop in popularity.
  - It proved really difficult to get multi-layer models working robustly.
  - We obtained similar performance with simpler models:
    - Rise in popularity of logistic regression and SVMs with regularization and kernels.
  - Lots of internet successes (spam filtering, web search, recommendation).
  - ML moved closer to other fields like numerical optimization and statistics.

- Late 2000s: push to revive connectionism as "deep learning".
  - Canadian Institute For Advanced Research (CIFAR) NCAP program:
    - "Neural Computation and Adaptive Perception".
    - Led by Geoff Hinton, Yann LeCun, and Yoshua Bengio ("Canadian mafia").
  - Unsupervised successes: "deep belief networks" and "autoencoders".
    - Could be used to initialize deep neural networks.
    - <u>https://www.youtube.com/watch?v=KuPai0ogiHk</u>



## 2010s: DEEP LEARNING!!!

- Bigger datasets, bigger models, parallel computing (GPUs/clusters).
   And some tweaks to the models from the 1980s.
- Huge improvements in automatic speech recognition (2009).
  - All phones now have deep learning.
- Huge improvements in computer vision (2012).
  - Changed computer vision field almost instantly.
  - This is now finding its way into products.



http://www.image-net.org/challenges/LSVRC/2014/

## 2010s: DEEP LEARNING!!!

- Media hype:
  - "How many computers to identify a cat? 16,000"

New York Times (2012).

- "Why Facebook is teaching its machines to think like humans" Wired (2013).
- "What is 'deep learning' and why should businesses care?"
   Forbes (2013).
- "Computer eyesight gets a lot more accurate"

New York Times (2014).

• 2015: huge improvement in language understanding.

## Summary

- Neural networks learn features z<sub>i</sub> for supervised learning.
- Sigmoid function avoids degeneracy by introducing non-linearity.
   Universal approximator with large-enough 'k'.
- Biological motivation for (deep) neural networks.
- Deep learning considers neural networks with many hidden layers.
   Can more-efficiently represent some functions.
- Unprecedented performance on difficult pattern recognition tasks.

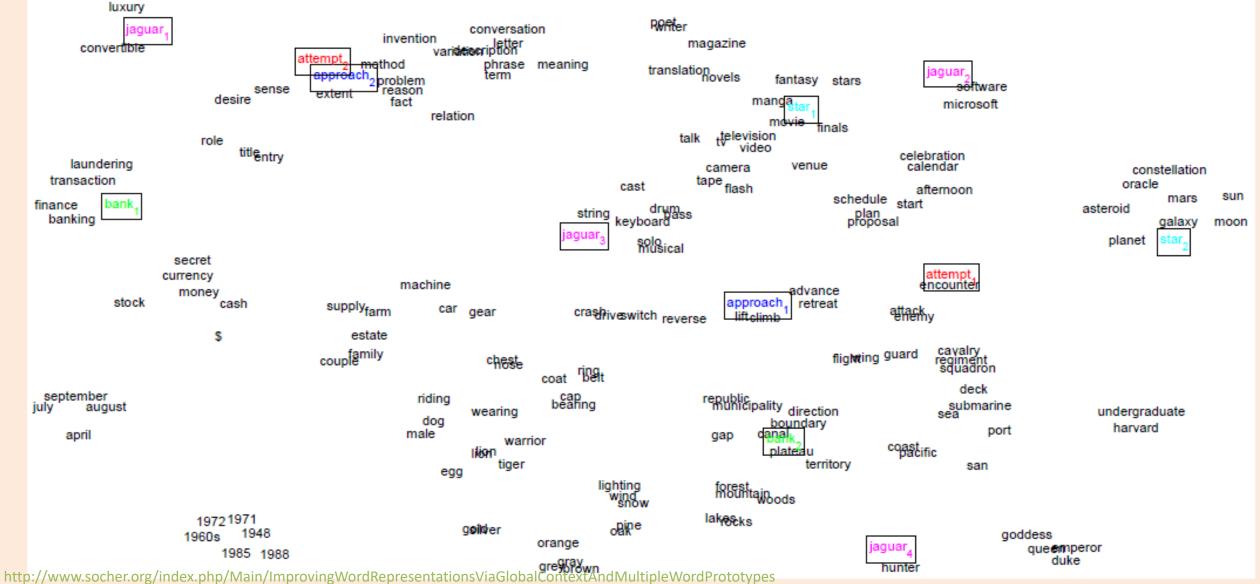
- Next time:
  - Training deep networks.

## **Multiple Word Prototypes**

- What about homonyms and polysemy?
  - The word vectors would need to account for all meanings.
- More recent approaches:
  - Try to cluster the different contexts where words appear.
  - Use different vectors for different contexts.



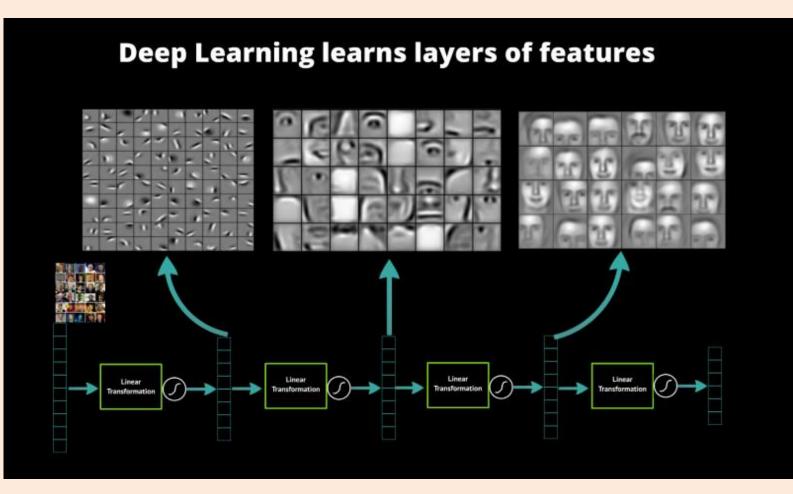
#### Multiple Word Prototypes



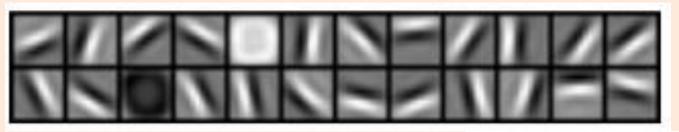
# Why $z_i = Wx_i$ ?

- In PCA we had that the optimal  $Z = XW^T(WW^T)^{-1}$ .
- If W had normalized+orthogonal rows,  $Z = XW^T$  (since  $WW^T = I$ ).
  - So  $z_i = Wx_i$  in this normalized+orthogonal case.
- Why we would use  $z_i = Wx_i$  in neural networks?
  - We didn't enforce normalization or orthogonality.
- Well, the value W<sup>T</sup>(WW<sup>T</sup>)<sup>-1</sup> is just "some matrix".
  - You can think of neural networks as just directly learning this matrix.

• Faces might be composed of different "parts":

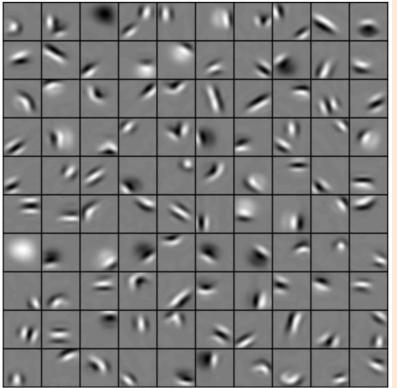


• First layer of z<sub>i</sub> trained on 10 by 10 image patches:

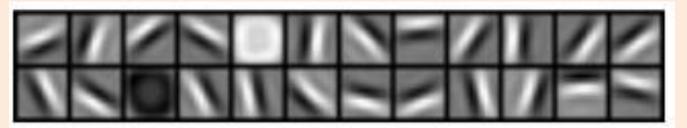


( "Gabor filters"

- Attempt to visualize second layer:
  - Corners, angles, surface boundaries?
- Models require many tricks to work.
   We'll discuss these next time.

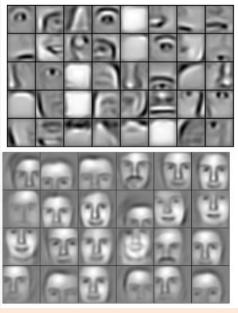


• First layer of z<sub>i</sub> trained on 10 by 10 image patches:



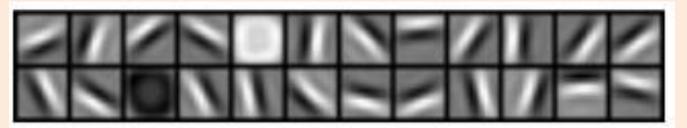
{ "Gabor filters"

 Visualization of second and third layers trained on specific objects: faces



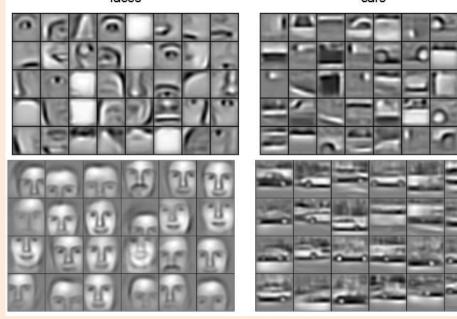
http://www.cs.toronto.edu/~rgrosse

• First layer of z<sub>i</sub> trained on 10 by 10 image patches:

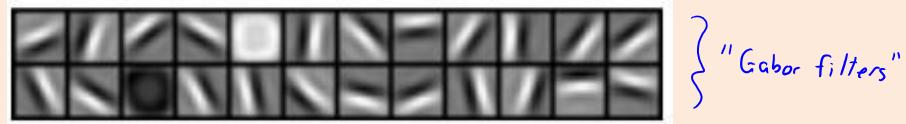


& "Gabor filters"

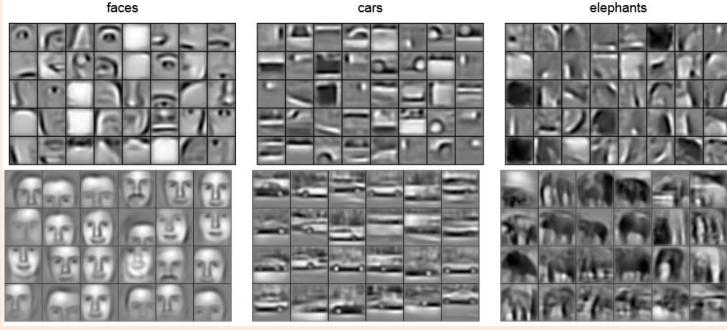
Visualization of second and third layers trained on specific objects:



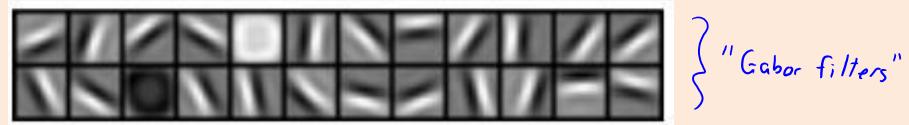
• First layer of z<sub>i</sub> trained on 10 by 10 image patches:



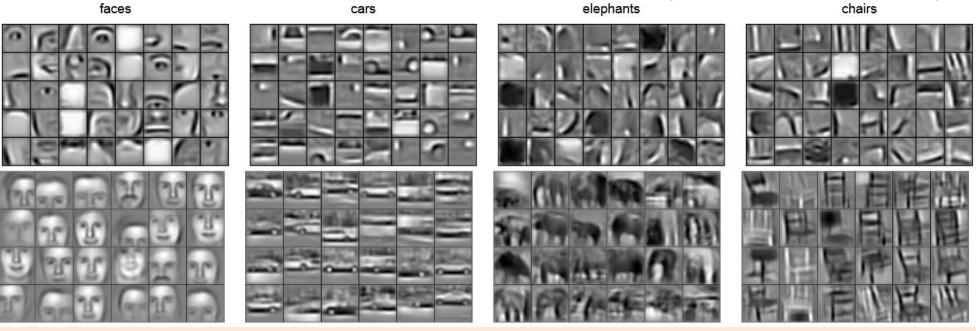
• Visualization of second and third layers trained on specific objects:



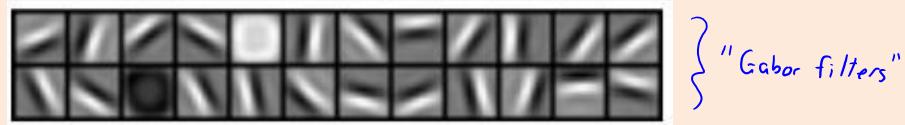
• First layer of z<sub>i</sub> trained on 10 by 10 image patches:



• Visualization of second and third layers trained on specific objects:



• First layer of z<sub>i</sub> trained on 10 by 10 image patches:



• Visualization of second and third layers trained on specific objects:

