

Outline

- ▷ Radioactivity
- ▷ Alpha decay
- ▷ Beta decay
- ▷ Gamma decay
- ▷ Rate of decay
- ▷ Half-life
- ▷ Activity
- ▷ Radioactive dating
- ▷ End

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UBC Physics 102 Lecture 2

Rik Blok

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Radioactivity [Text: Sect. 42-3]

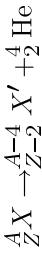
- **Definition:** Radioactivity
 - Decay of an unstable nucleus.
- **Discussion: 3 common types of decay**

Type	Particle emitted	Charge	Mass
α (alpha)	${}^4\text{He}$ (2 p + 2 n)	+2	heavy
β (beta)	electron	-1	light
γ (gamma)	photon	none	very light

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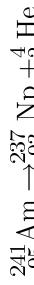
Alpha decay [Text: Sect. 42-3]

- **Definition:** α decay



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- **Example: Smoke detectors**



- Emitted α particle used to generate current between two plates.

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Beta decay [Text: Sect. 42-5]

- **Definition: β decay**



- $\beta = e^-$ (electron).
- Mass (A) and charge (Z) conserved.
- Electron comes from nucleus, not orbit.
- Produced by decay of neutron:



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Gamma decay [Text: Sect. 42-6]

- **Definition: Excited state**

- Nucleus with surplus energy (often result of α or β decay).
- Denoted by $*$, as in $\frac{A}{Z}X^*$.

- **Definition: γ decay**



- Produces photon (γ particle).
- Mass (A) and charge (Z) conserved.

- **Interactive Quiz: PRS 02a**



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Rate of decay [Text: Sect. 42-8]

- **Derivation: Radioactive decay law**

- Radioactive decay is unpredictable, quantum process.
- Average rate of decay is proportional to amount present,

$$\frac{dN}{dt} = -\lambda N.$$

- λ (lambda) is proportionality constant that sets rate.
- Can integrate to find how much material remains after time t ,

$$N(t) = N_0 e^{-\lambda t}.$$

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Half-life [Text: Sect. 42-8]

- **Derivation: Half-life, $T_{1/2}$**

- The time it takes for half the original amount of isotope to decay. Is solution to

$$\frac{N_0}{2} = N_0 e^{-\lambda T_{1/2}}.$$

- **Interactive Quiz: PRS 02b**

- **Definition: Half-life, $T_{1/2}$**

$$T_{1/2} = \frac{\ln 2}{\lambda}$$

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Activity [Text: Sect. 42-8]

• Definition: Activity, $\left| \frac{dN}{dt} \right|$

- Rate of decay, or number of decays per second of a sample.

$$\left| \frac{dN}{dt} \right| = \lambda N.$$

• Example:

- ^{31}Si has a half-life of 2.62 hr. What will the activity of a 1 g sample be after 1 week?



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Activity, contd

• Solution:

- We know $N(t) = N_0 e^{-\lambda t}$. Then

$$\left| \frac{dN}{dt} \right| = \lambda N_0 e^{-\lambda t}.$$

- Need to calculate N_0 , λ , and t . First, t (in hours) is $t = 1 \text{ wk} = 168 \text{ hr}$.

- Now, use half-life, $T_{1/2} = \frac{\ln 2}{\lambda}$ to get λ ,

$$\begin{aligned}\lambda &= \frac{\ln 2}{T_{1/2}} = \frac{0.693}{2.62 \text{ hr}} \\ &= 0.265 \text{ hr}^{-1}.\end{aligned}$$

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Activity, contd

• Solution: contd

- Finally, need to find number of particles, N_0 .
- Use atomic mass, 1 particle = 31 u,

$$\begin{aligned}N_0 &= 10^{-3} \text{ kg} \times \frac{1 \text{ u}}{1.66 \times 10^{-27} \text{ kg}} \times \frac{1 \text{ particle}}{31 \text{ u}} \\ &= 1.94 \times 10^{22} \text{ particles}.\end{aligned}$$

- So activity is

$$\begin{aligned}\left| \frac{dN}{dt} \right| &= \lambda N_0 e^{-\lambda t} \\ &= (0.265 \text{ hr}^{-1})(1.94 \times 10^{22} \text{ part.}) e^{-(0.265 \text{ hr}^{-1})(168 \text{ hr})} \\ &= 238 \text{ particles/hr. } \square\end{aligned}$$

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Radioactive dating [Text: Sect. 42-10]

• Discussion: Carbon dating

- Unstable ^{14}C isotope occurs naturally.
- About $1.3 \times 10^{-10}\%$ of carbon in the environment is ^{14}C .
- Absorbed during life (eating, breathing, etc.).
- No longer absorbed after death so ^{14}C decays.
- Can estimate how long ago specimen died by using $N(t) = N_0 e^{-\lambda t}$ to determine time needed to get N down to current value,

$$t = \frac{1}{\lambda} \ln \frac{N_0}{N}.$$

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Radioactive dating, contd

- **Discussion: Carbon dating, contd**

- λ can be calculated from half-life, $T_{1/2} = 5730$ yr.
- N_0 can be determined from total number of carbon atoms in sample.

- Measure activity to get current N , from $\left| \frac{dN}{dt} \right| = \lambda N$.



End

- **Practice Problems:**

- Ch. 42: Q. 7, 13, 19, 21, 25
 - Ch. 42: Pr. 35, 37, 39, 43, 45, 47, 49, 55, 63, 65
- **Interactive Quiz: Feedback**
 - **Tutorial Question: tut02**