

# CPSC 427

## Video Game Programming

### Rendering and Transformations



Helge Rhodin

# Today

---

- What is rendering?
- How to represent our game world, graphically!

## Outcome:

- Learning about different rendering approaches
- Understanding affine transformations

# Our game loop (A1, main.cpp)

```
// Set all states to default
world.restart();
auto t = Clock::now();
// Variable timestep loop
while (!world.is_over())
{
    // Processes system messages, if this wasn't present the window would become unresponsive
    glfwPollEvents();

    // Calculating elapsed times in milliseconds from the previous iteration
    auto now = Clock::now();
    float elapsed_ms = static_cast<float>((std::chrono::duration_cast<std::chrono::microseconds>(now - t)).count()) / 1000.f;
    t = now;

    DebugSystem::clearDebugComponents();
    ai.step(elapsed_ms, window_size_in_game_units);
    world.step(elapsed_ms, window_size_in_game_units);
    physics.step(elapsed_ms, window_size_in_game_units);
    world.handle_collisions();

    renderer.draw(window_size_in_game_units);
}

return EXIT_SUCCESS;
```

# CPSC 427

## Video Game Programming

### Rendering basics



Helge Rhodin

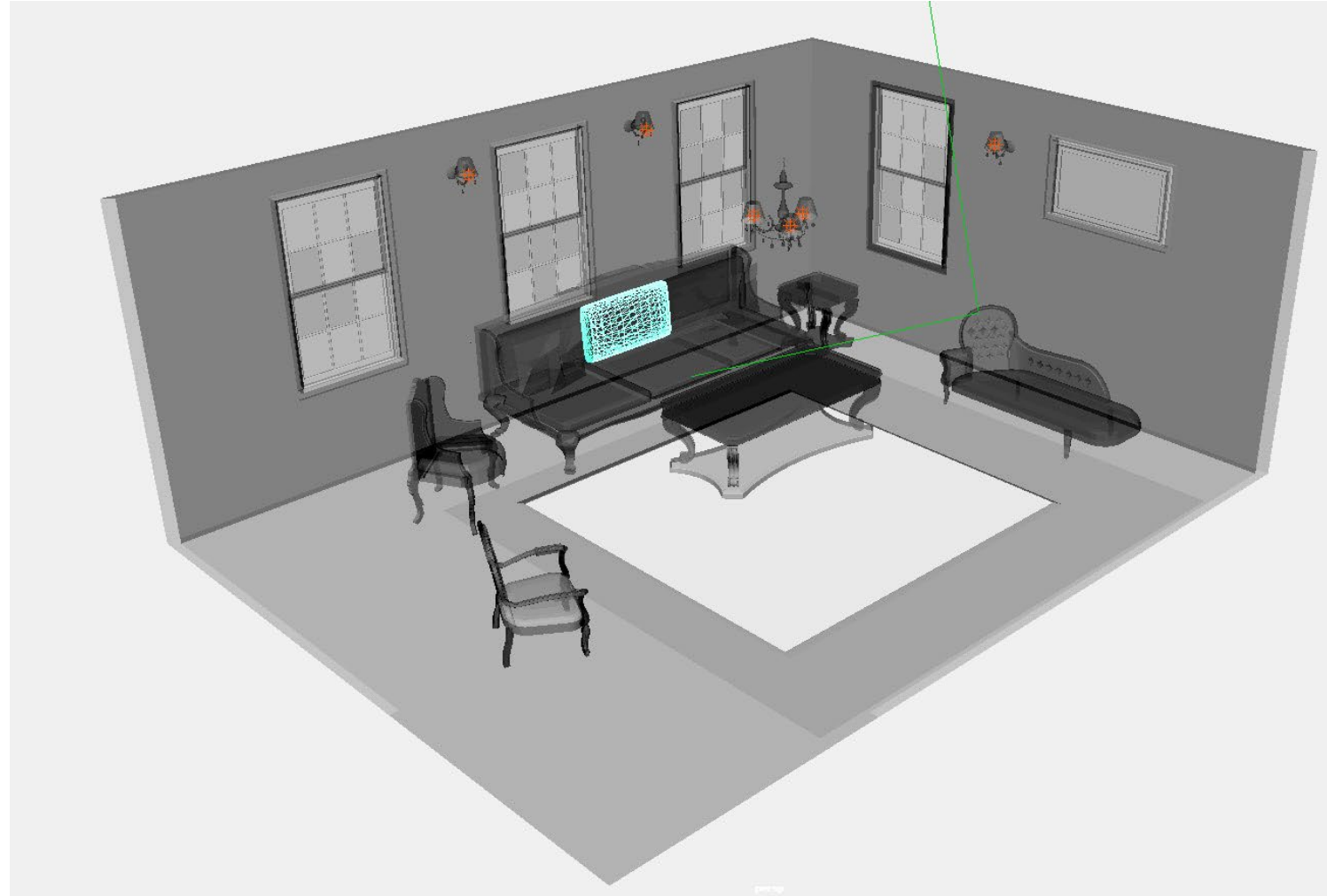
# What is rendering?

*Generating an image from a (3D) scene*

*Let's think how!*

# Scene

- A coordinate frame
- Objects
- Their materials
- (Lights)
- (Camera)



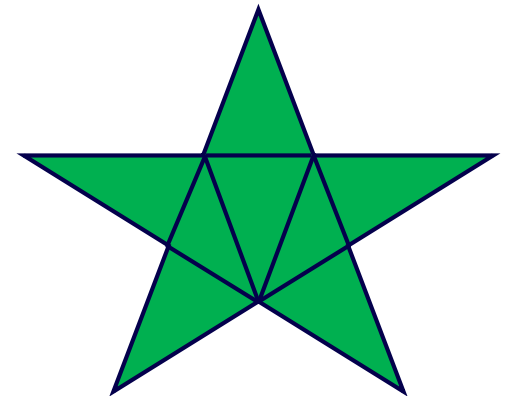
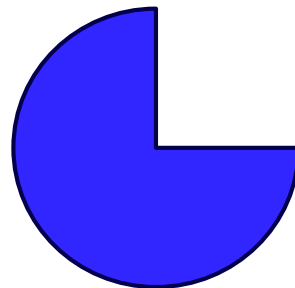
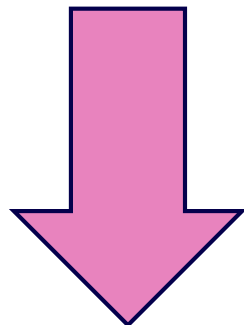
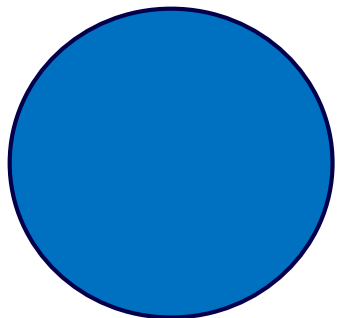


# SINGLE OBJECT

*How to describe a single piece of geometry?*

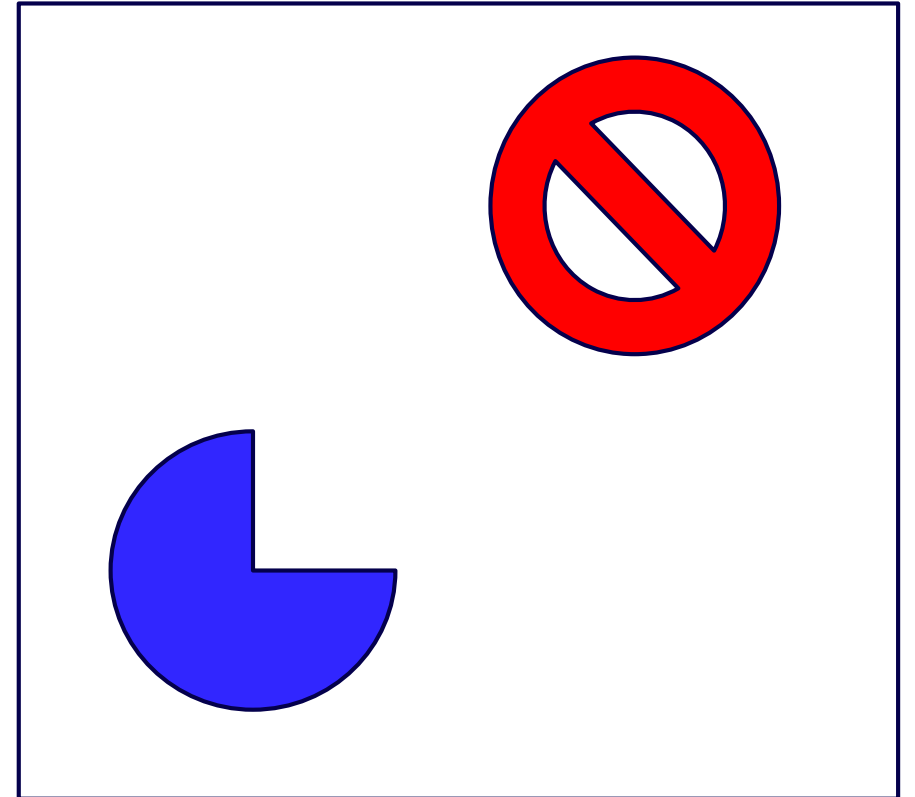
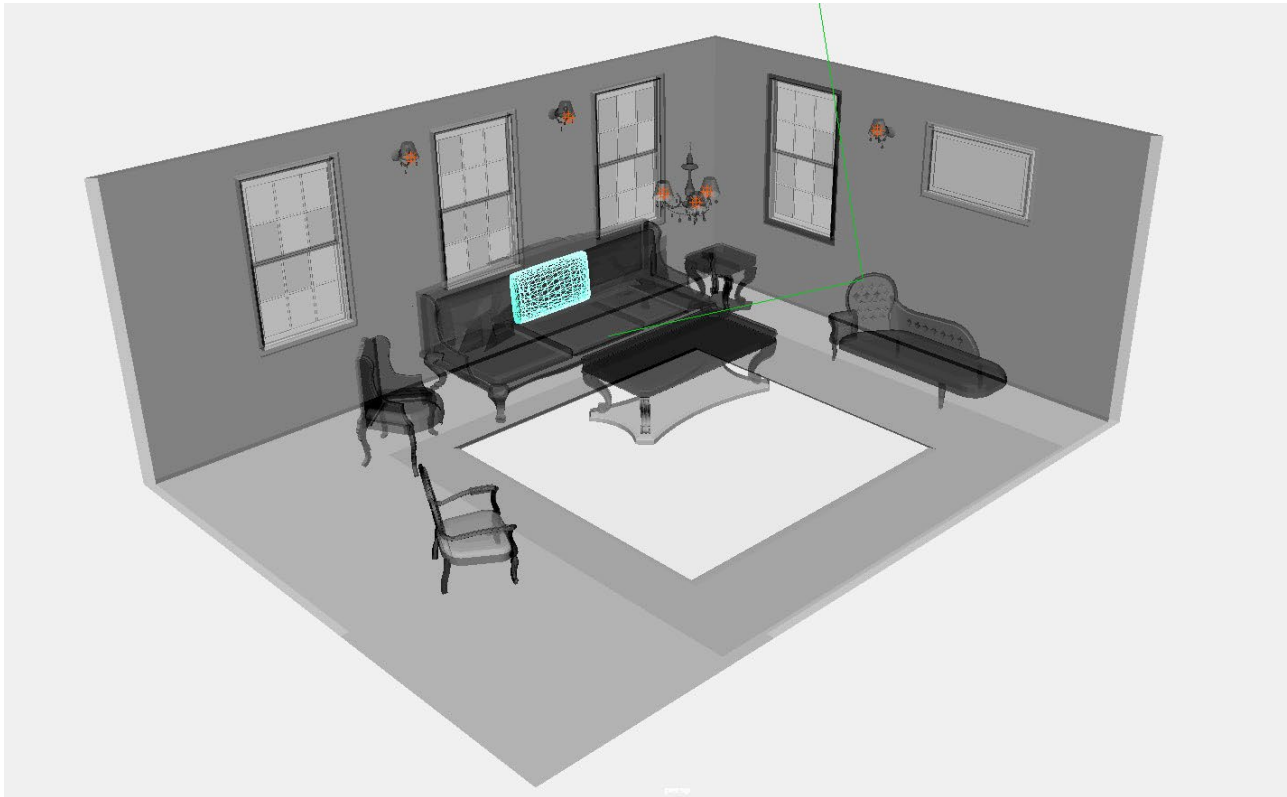
**2D**

- Triangulated polygon
- Smooth geometry => **discretized/triangulated at render time**
  - *Closed curve (implicit)*
  - *Boolean combination of simple shapes*



# SCENE

## *How to describe a scene?*

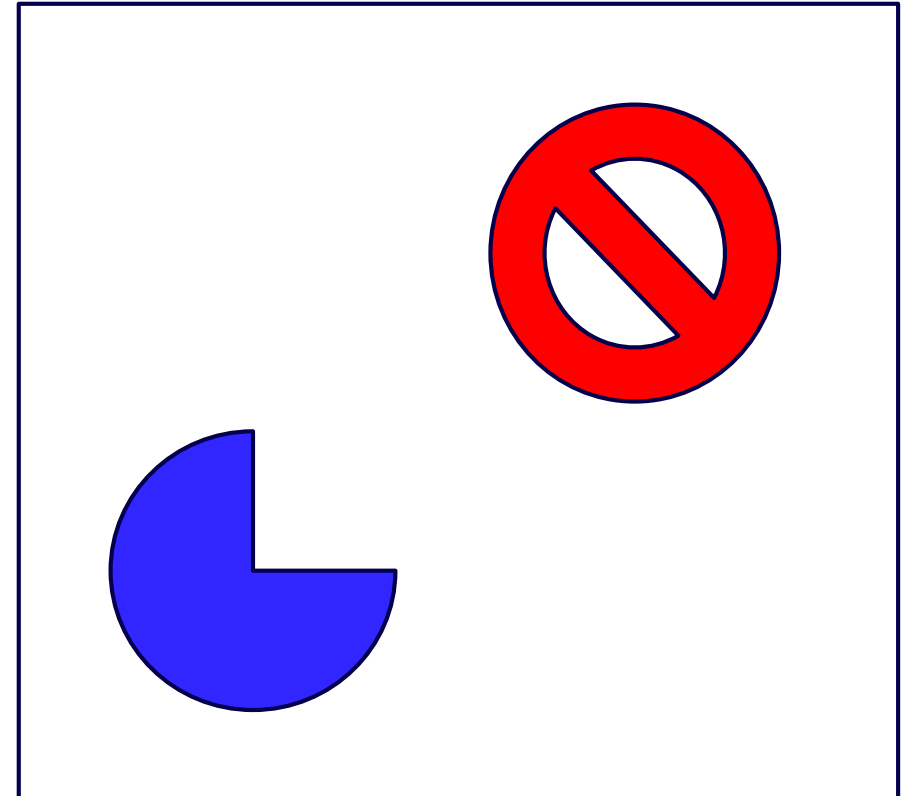




# SCENE

*How to describe a scene?*

*Local Coordinate Systems joined via Transformations*



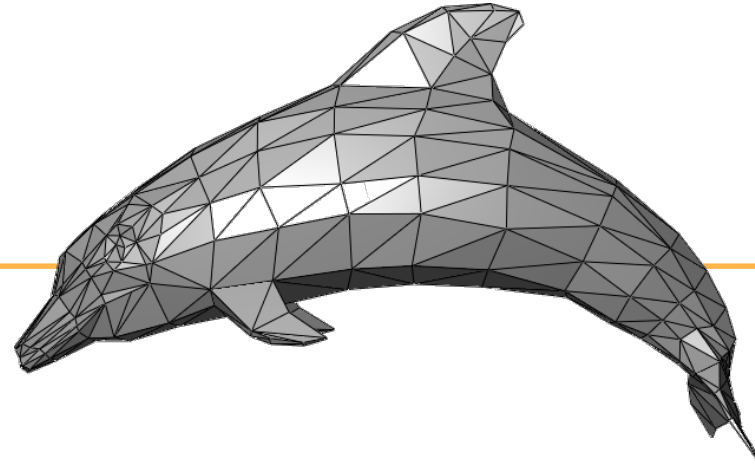
# Object

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***Most common:***

- ***surface representation using a (textured) mesh***

# GEOMETRY



## Triangle meshes

- List of vertices
- Connectivity defined by indices

- `uint16_t indices[] = {vertex_index1, vertex_index2, vertex_index3, ...}`

three indices make one triangle

### OpenGL resources

- vertex buffer
- index buffer

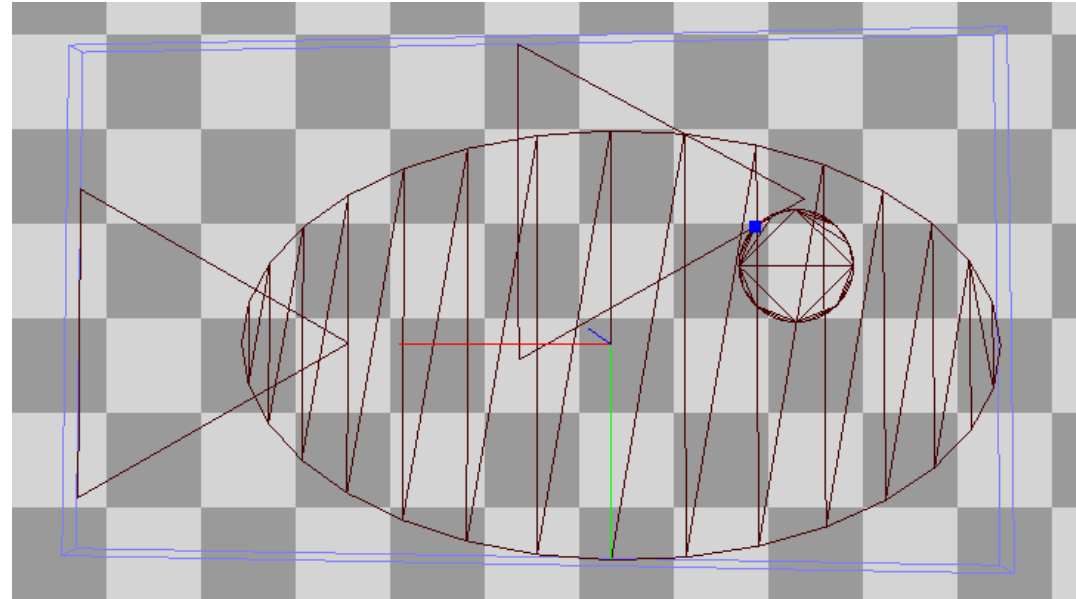
### Creation

```
Guint vbo;  
glGenBuffers (vbo) ;
```

```
Guint ibo;  
glGenBuffers (ibo) ;
```

# Programmatic geometry definition

```
vec3 vertices[153];  
vertices[0].position = { -0.54, +1.34, -0.01 };  
vertices[1].position = { +0.75, +1.21, -0.01 };  
...  
vertices[152].position = { -1.22, +3.59, -0.01 };  
  
uint16_t indices[] = { 0,3,1, 0,4,1,... , 151,152,150 };  
  
GLuint vbo;  
glGenBuffers (vbo);  
glBindBuffer (vbo);  
glBufferData (vbo, vertices);  
  
GLuint ibo;  
glGenBuffers (ibo);  
glBindBuffer (ibo);  
glBufferData (ibo, indices);
```



# Image

## *A grid of color values*



# Screen

*Displays what's in frame buffer*

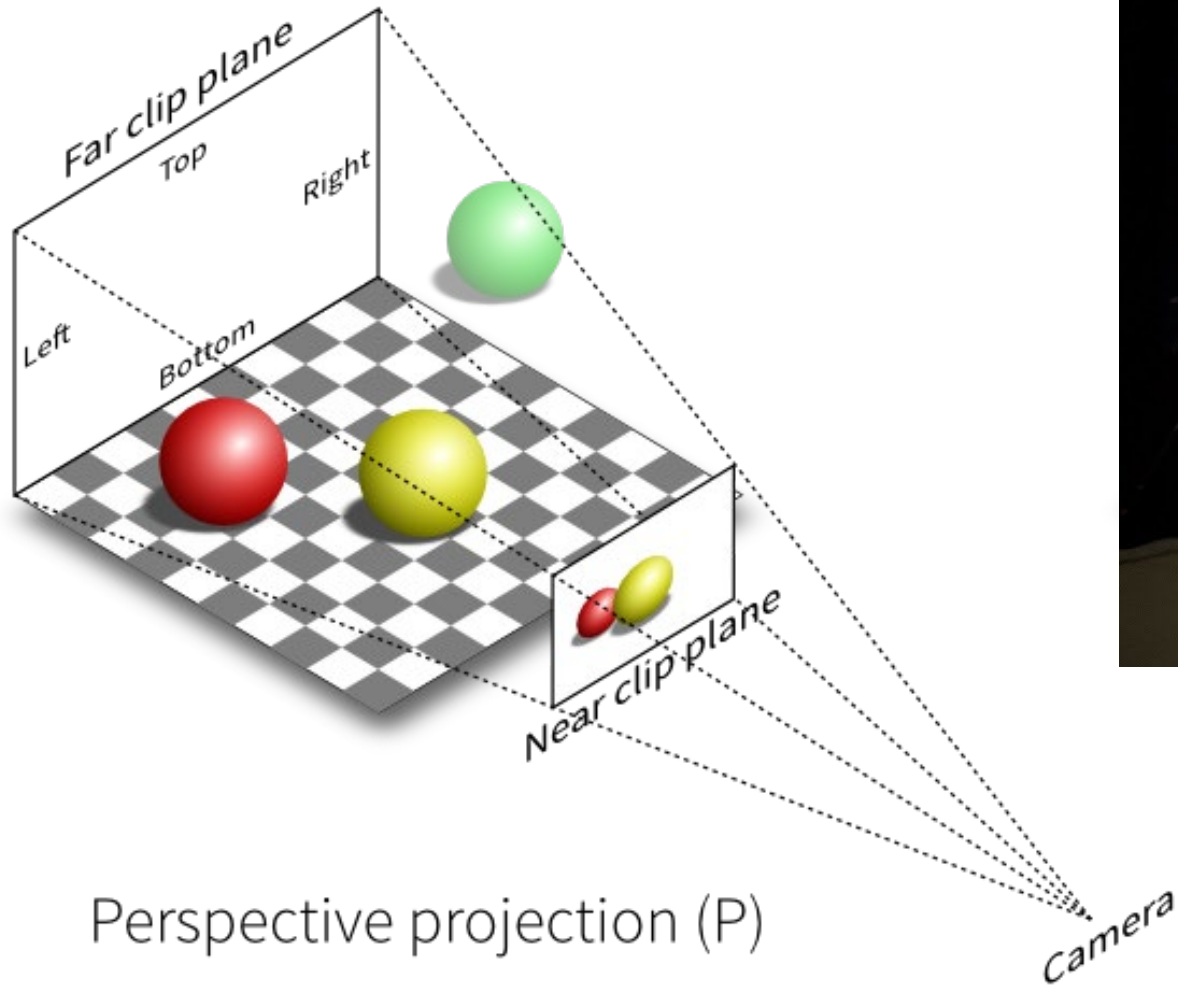
*Terminology:*

**Pixel:** basic element on device

**Resolution:** number of rows & columns in device



# Virtual Camera



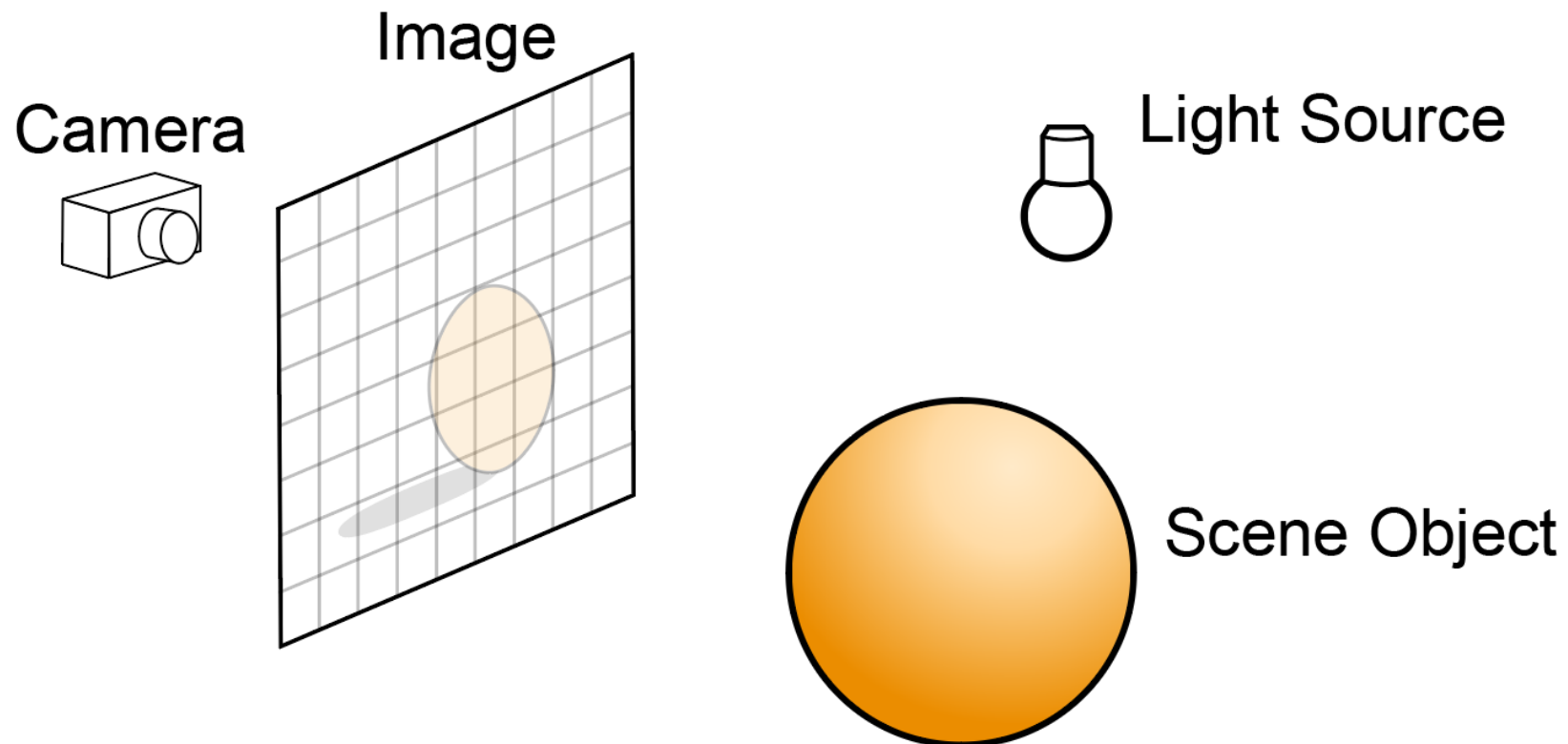
Virtual camera registered in the real world  
(using marker-based motion capture)

Perspective projection (P)



# Rendering?

- ***Simulating light transport***
  - How to simulate light efficiently?



# Rendering – Photon Tracing

- ***simulate physical light transport from a source to the camera***

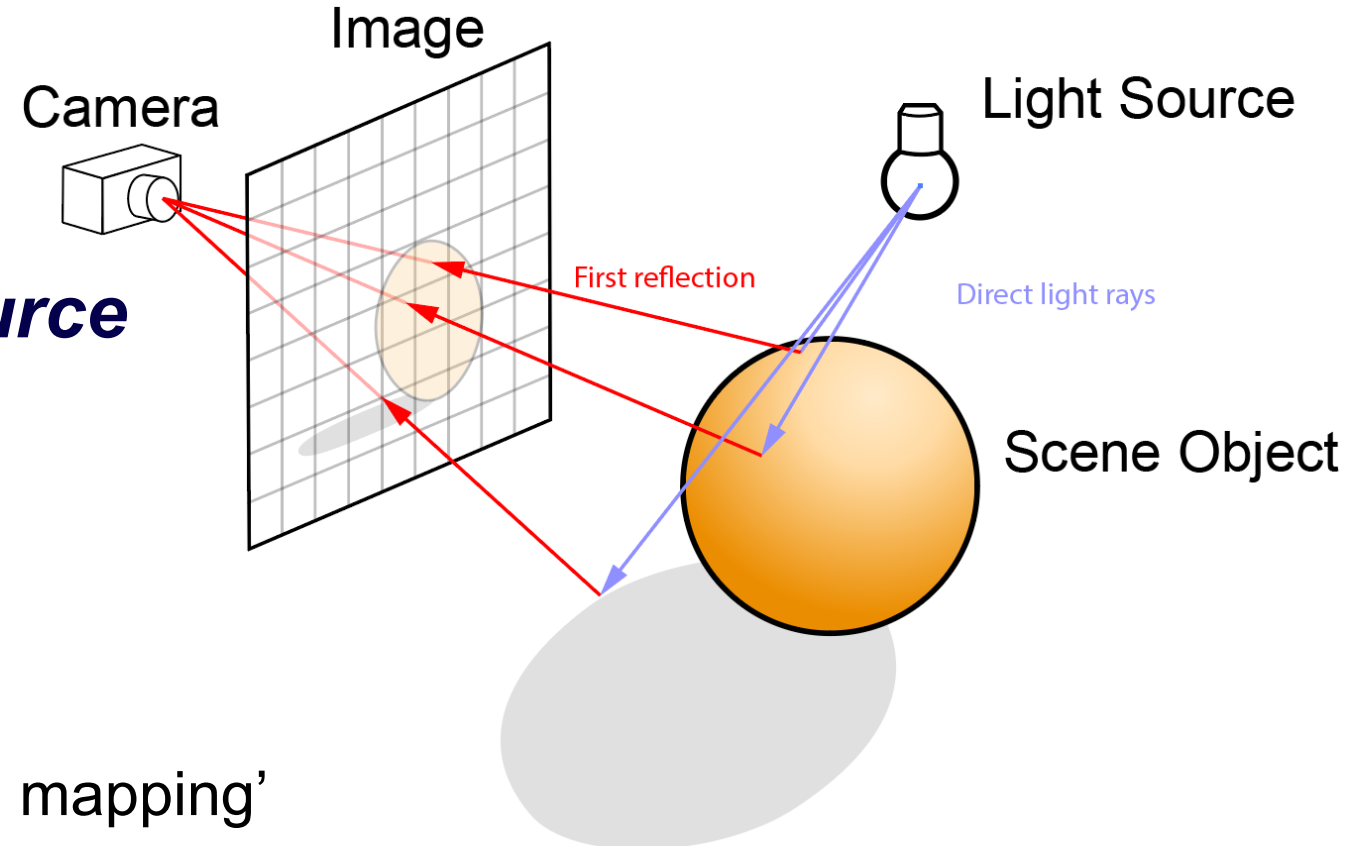
- *the paths of photons*

- ***shoot rays from the light source***

- *random direction*

- ***compute first intersection***

- *continue towards the camera*

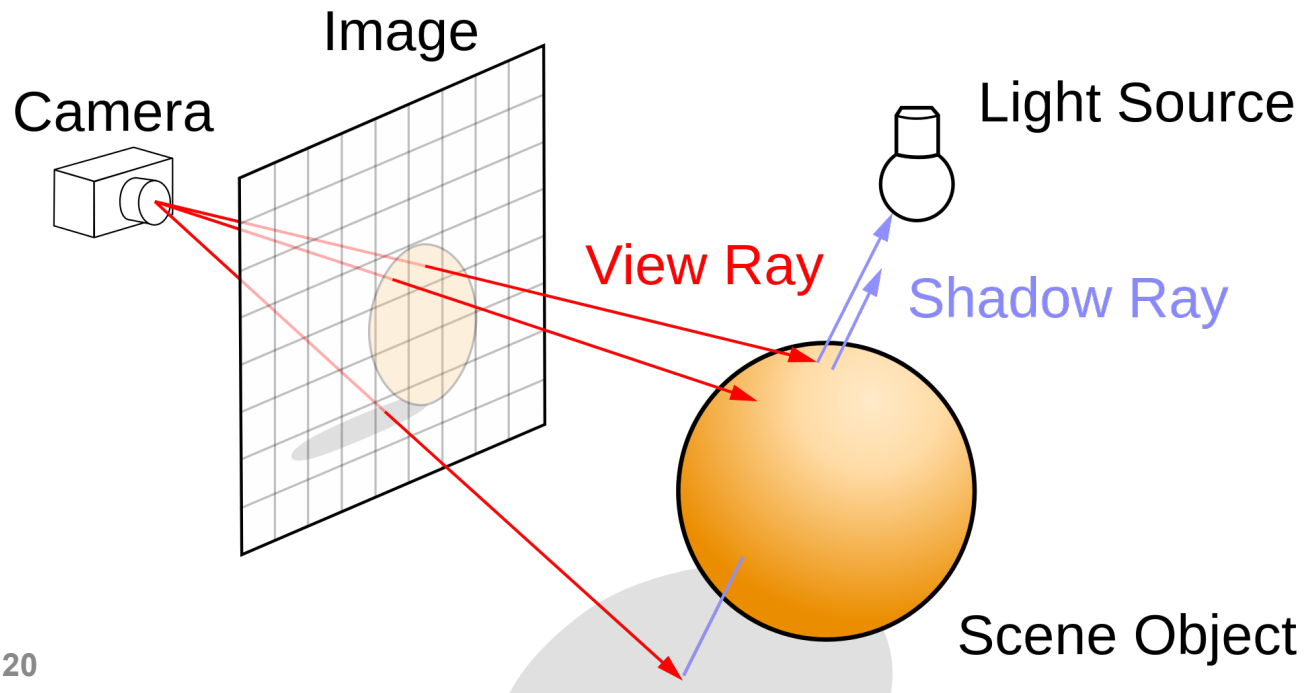


- used for indirect illumination: 'photon mapping'

# Rendering – Ray Tracing

*Start rays from the camera (opposes physics, an optimization)*

- *View rays: trace **from every pixel** to the first occlude*
- *Shadow ray: test light visibility*



Nvidia RTX does ray tracing

# Problems of ray tracing

- ***the collision detection is costly***
  - ray-object intersection
    - *n objects*
    - *k rays*
    - *naïve:  $O(n*k)$  complexity*

# Rendering – Splatting

*Approximate scene with spheres*

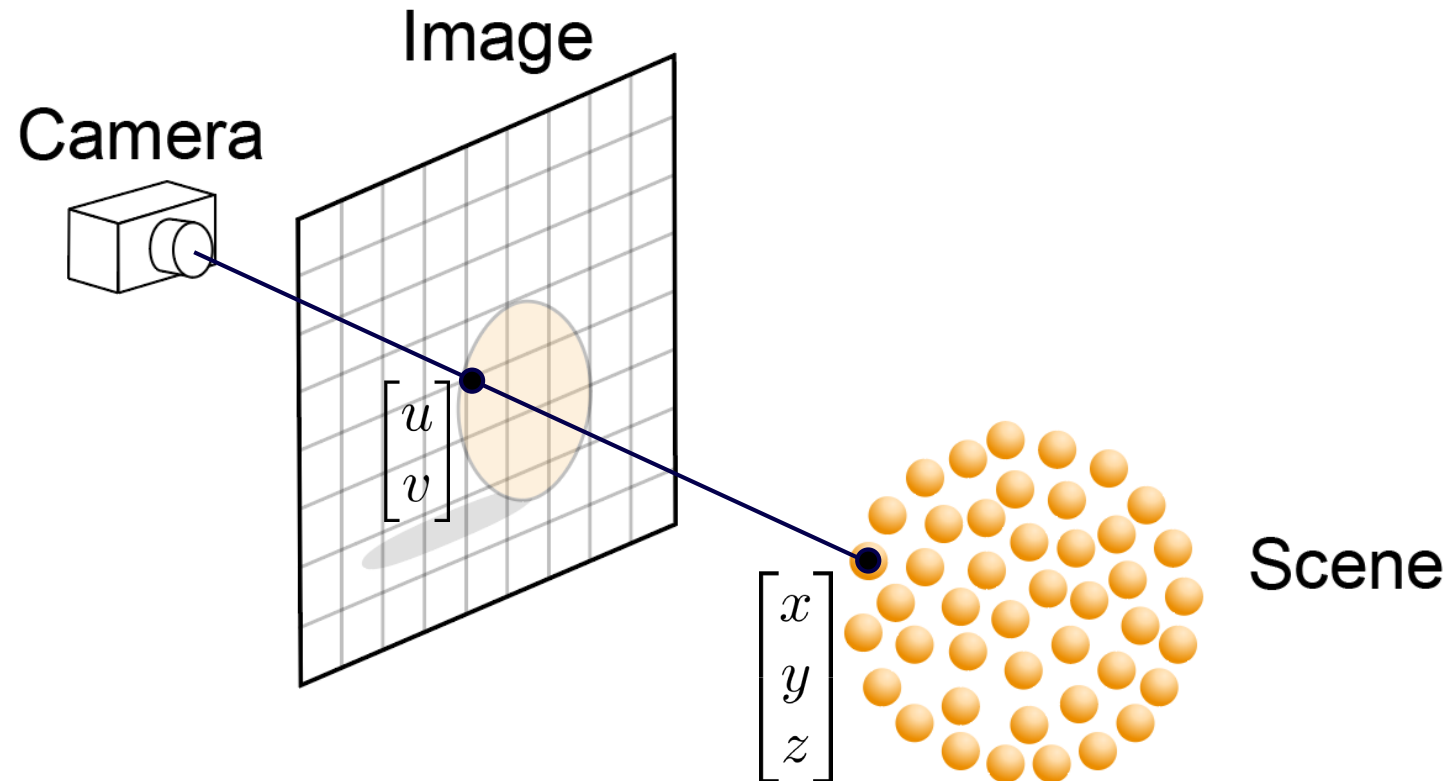
- *sort spheres back-to front*
- *project each sphere*
- simple equation

$$\begin{bmatrix} u \\ v \end{bmatrix} = \frac{1}{z} \begin{bmatrix} x \\ y \end{bmatrix}$$

- $O(n)$  for  $n$  spheres

*Many spheres needed!*

*Shadows?*



# Rendering – Rasterization

*Approximate objects with triangles*

## 1. Project each corner/vertex

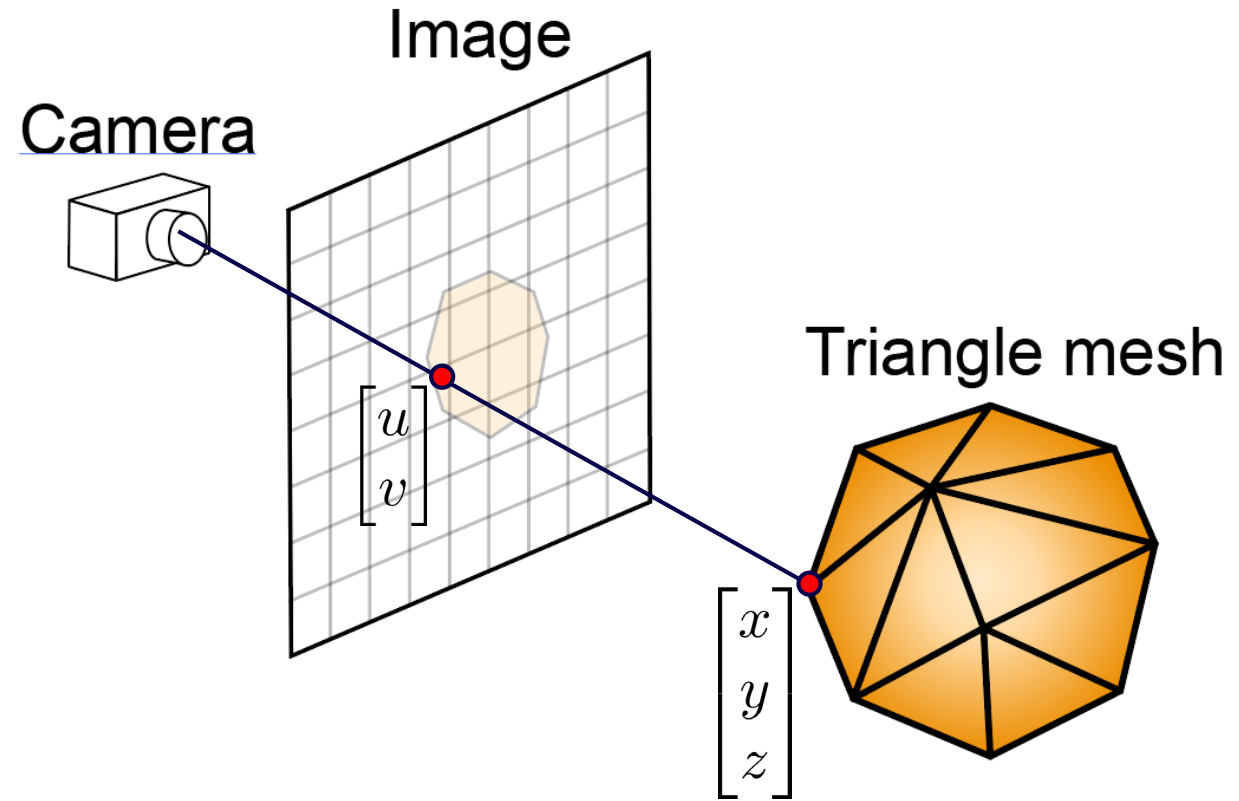
- projection of triangle stays a triangle

$$\begin{bmatrix} u \\ v \end{bmatrix} = \frac{1}{z} \begin{bmatrix} x \\ y \end{bmatrix}$$

- $O(n)$  for  $n$  vertices

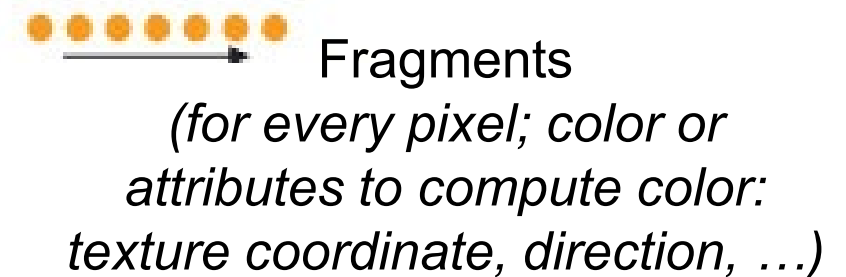
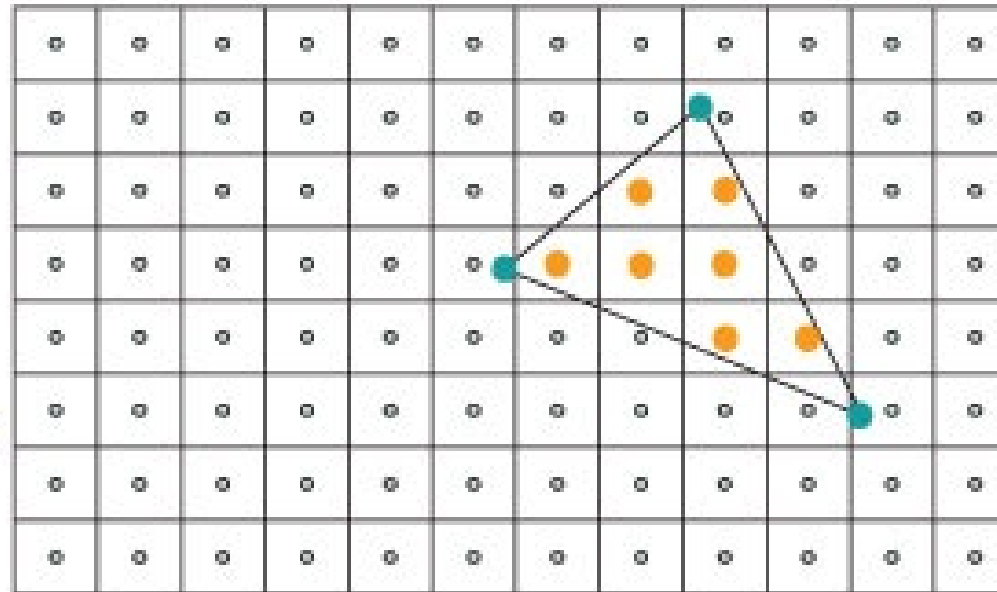
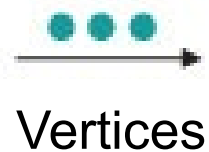
## 2. Fill pixels enclosed by triangle

- e.g., scan-line algorithm



# Rasterizing a Triangle

- *Determine pixels enclosed by the triangle*
- *Interpolate vertex properties linearly*

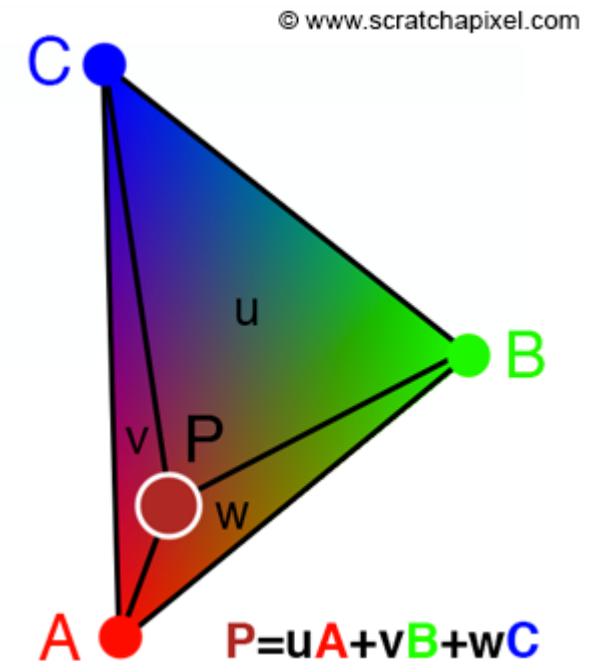




# Self study:

## Interpolation with barycentric coordinates

- *linear combination of vertex properties*
  - *e.g., color, texture coordinate, surface normal/direction*
- *weights are proportional to the areas spanned by the sides to query point P*



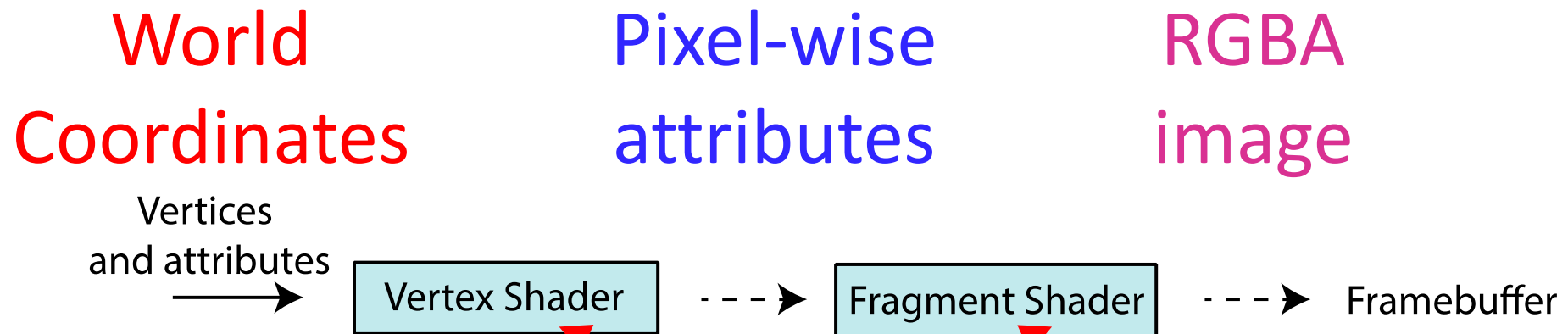


# Backup

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# OpenGL Rendering Pipeline (simplified)

1. *Vertex shader: geometric transformations*
2. *Fragment shader: pixel-wise color computation*

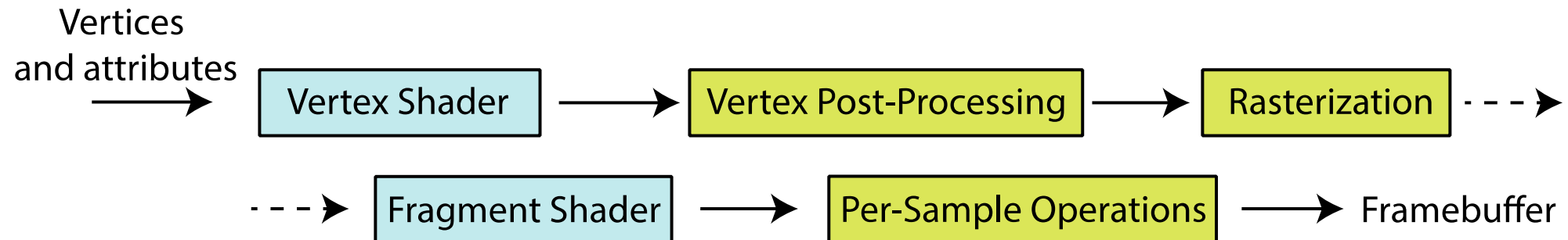


Shader: Programmable functions to define object appearance locally (vertex wise or fragment wise)

# OpenGL Rendering Pipeline

## *Input:*

- *3D vertex position*
- *Optional vertex attributes: color, texture coordinates, ...*



## *Output:*

- **Frame Buffer** : GPU video memory, holds image for display
- **RGBA pixel color** (**R**ed, **G**reen, **B**lue, **A**lpha / opacity)

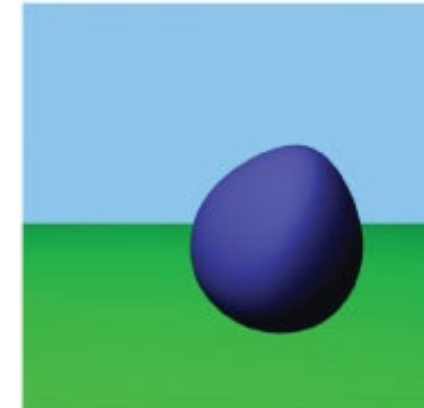
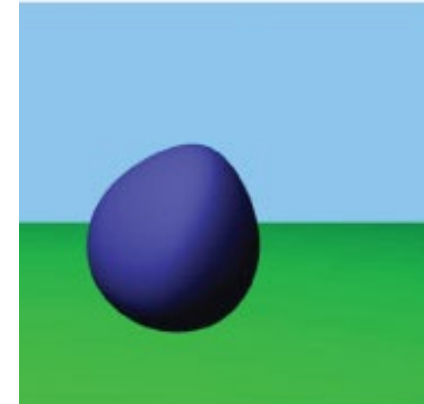
# Vertex shader examples

## *Object motion & transformation*

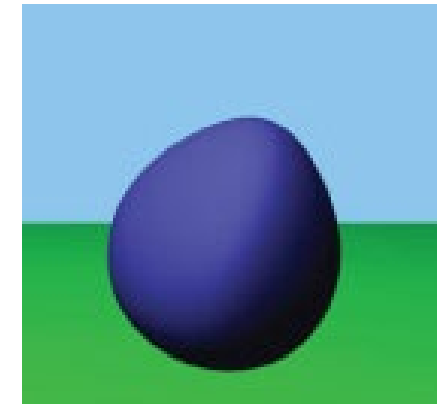
- translation
- rotation
- scaling

## *Projection*

- Orthographic
  - *simple, without perspective effects*
- Perspective
  - *pinhole projection model*



Translation



Scaling

# GLSL Vertex shader

## The OpenGL Shading Language (GLSL)

- Syntax similar to the C programming language
- Build-in vector operations
- functionality as the GLM library (used in the assignment template)

```
void main ()
{
    // Transforming The Vertex
    vec3 out_pos = projection * transform * vec3(in_pos.xy, 1.0);
    gl_Position = vec4(out_pos.xy, in_pos.z, 1.0);
}
```

**x and y coordinates  
of a vec2, vec3 or vec4**

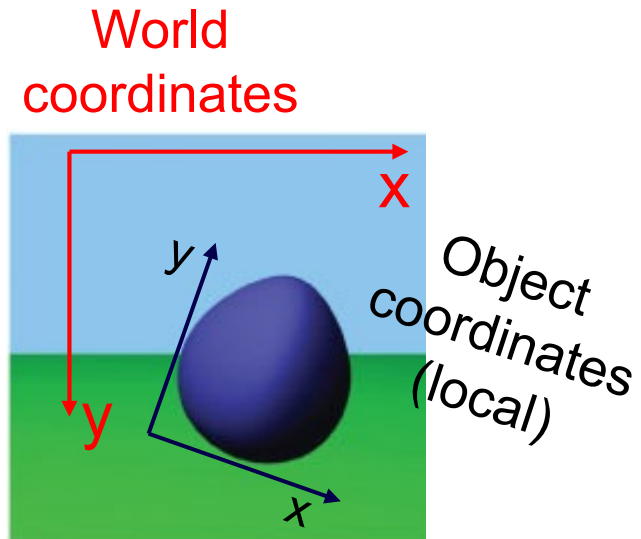
**world  
-> camera**

**object  
-> world**

**float  
(32 bit)**

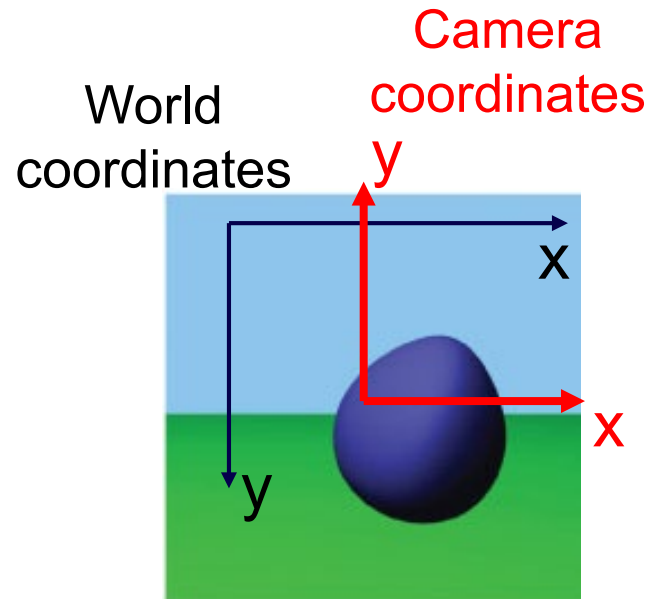
**vector of 3 (vec3) and 4 (vec4) floats**

# From local object to camera coordinates



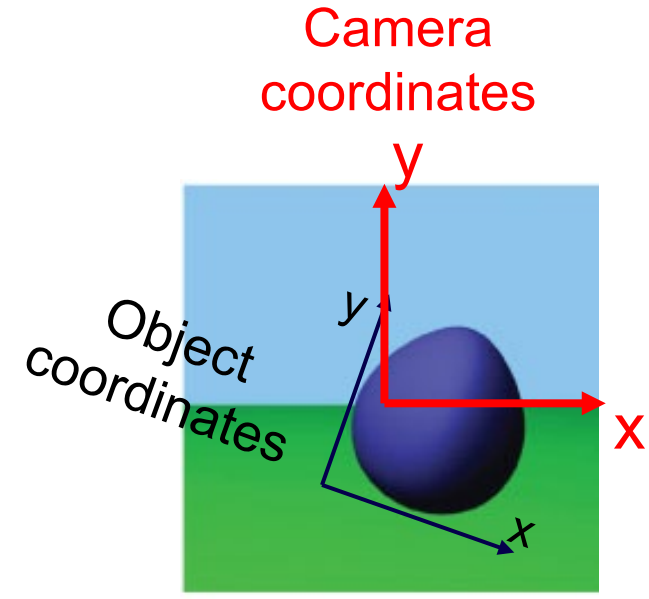
**object -> world**

**transform**



**world -> camera**

**projection**



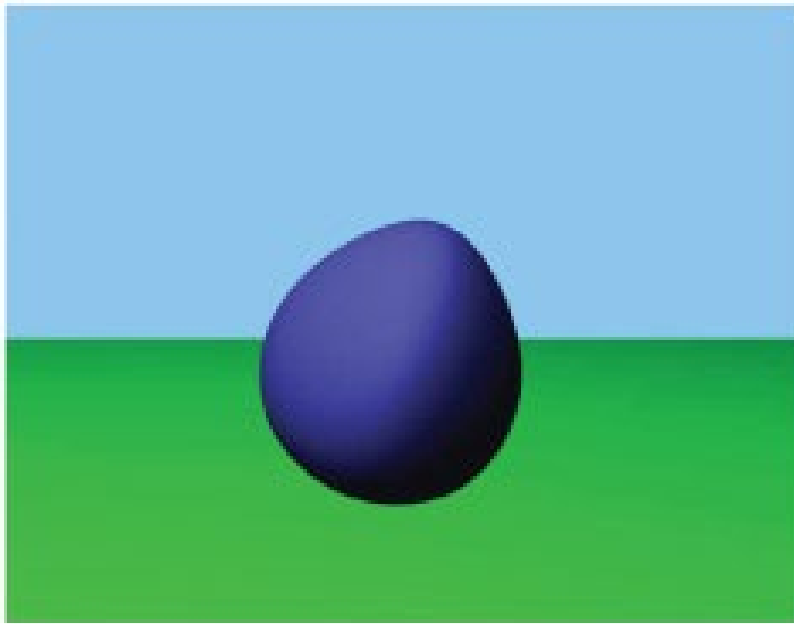
**object -> camera**

**projection \* transform**

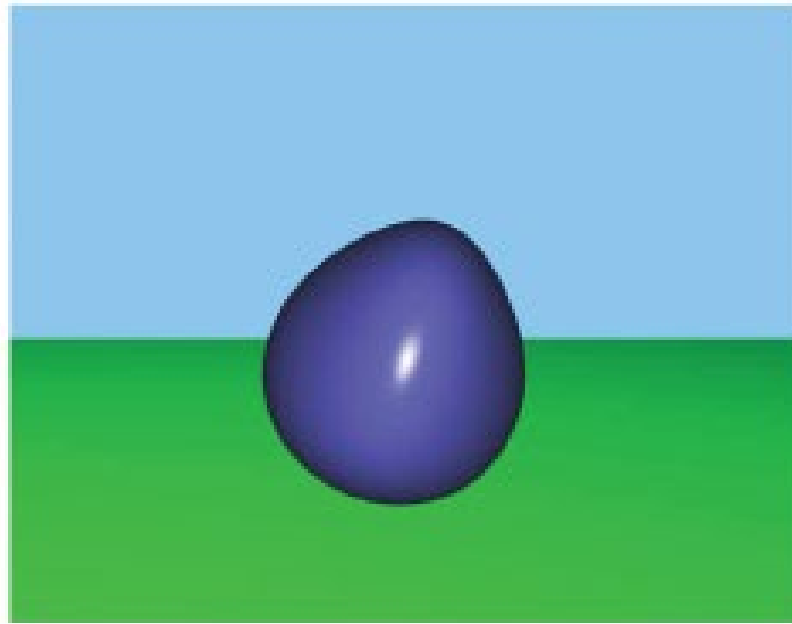


# Fragment shader examples

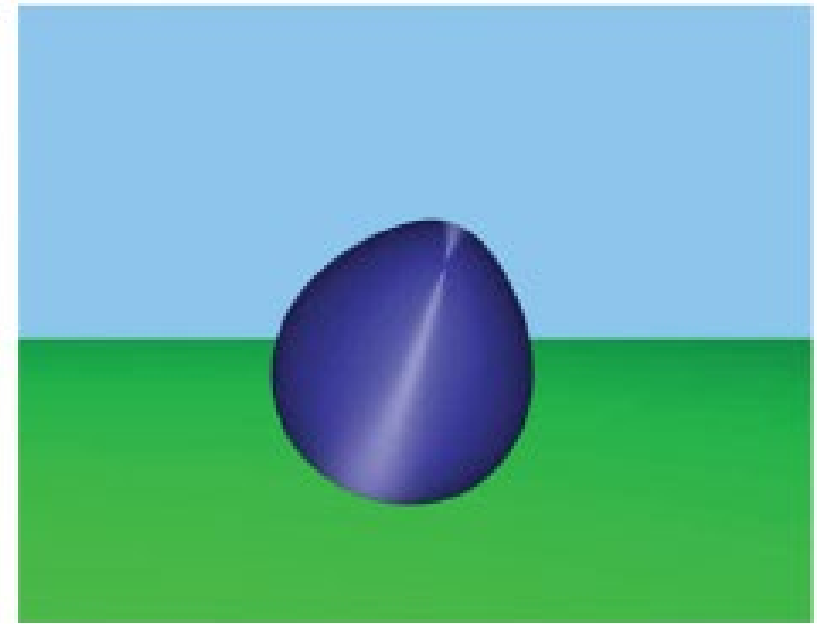
- *simulates materials and lights*
- *can read from textures*



**Diffuse**

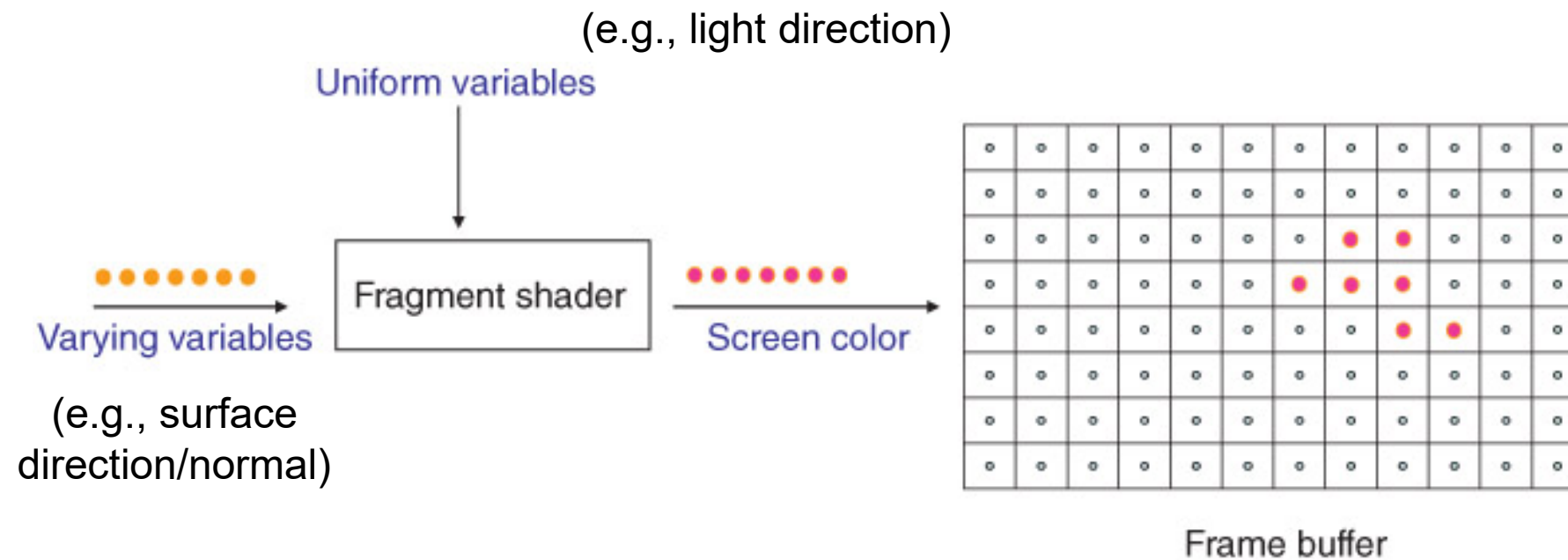


**Specular**



**Directional**

# Fragment shader overview



# GLSL fragment shader examples

## *Minimal:*

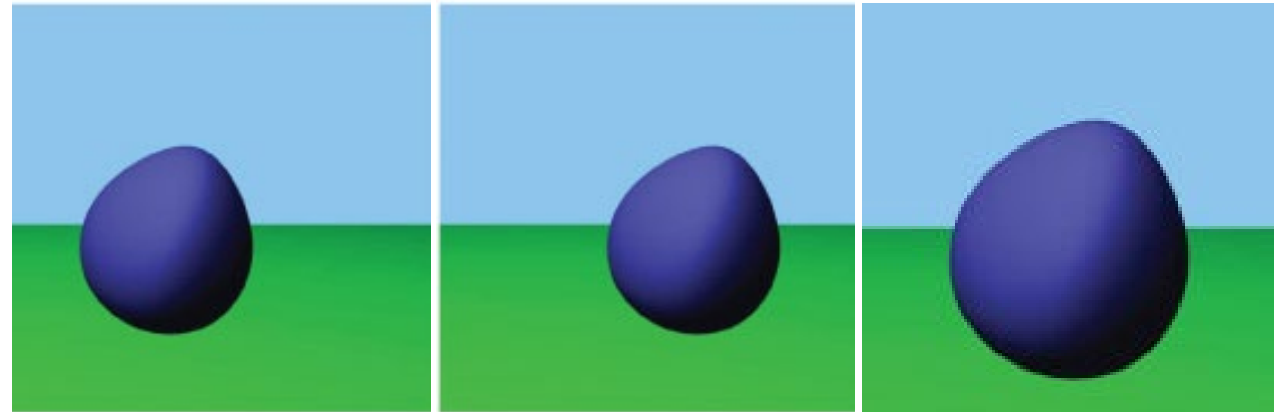
```
out vec4 out_color; Specify color output
void main()
{
    // Setting Each Pixel To ???
    out_color = vec4(1.0, 0.0, 0.0, 1.0);
}
```

Red, Green, Blue, Alpha

# CPSC 427

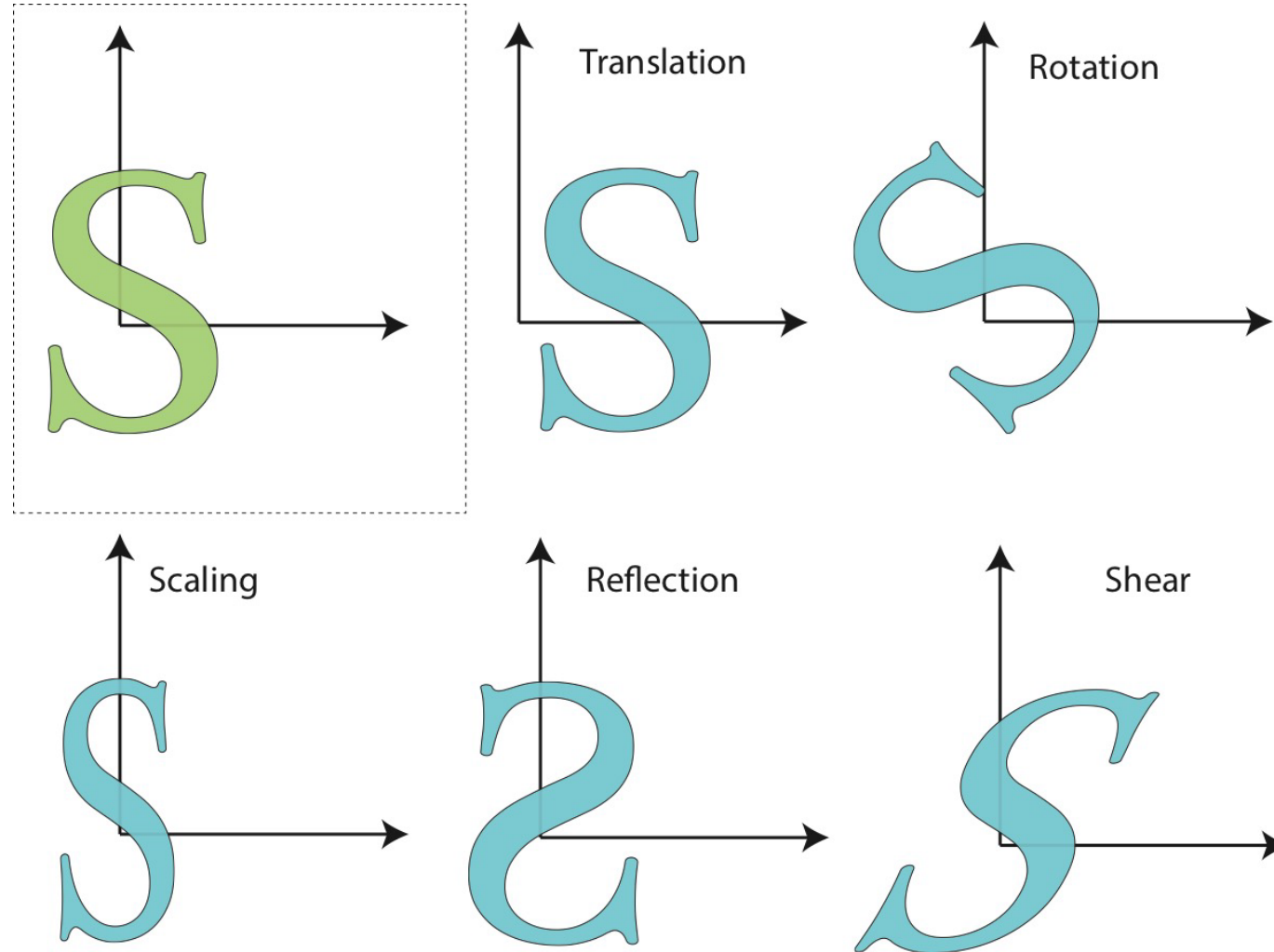
## Video Game Programming

### Transformations

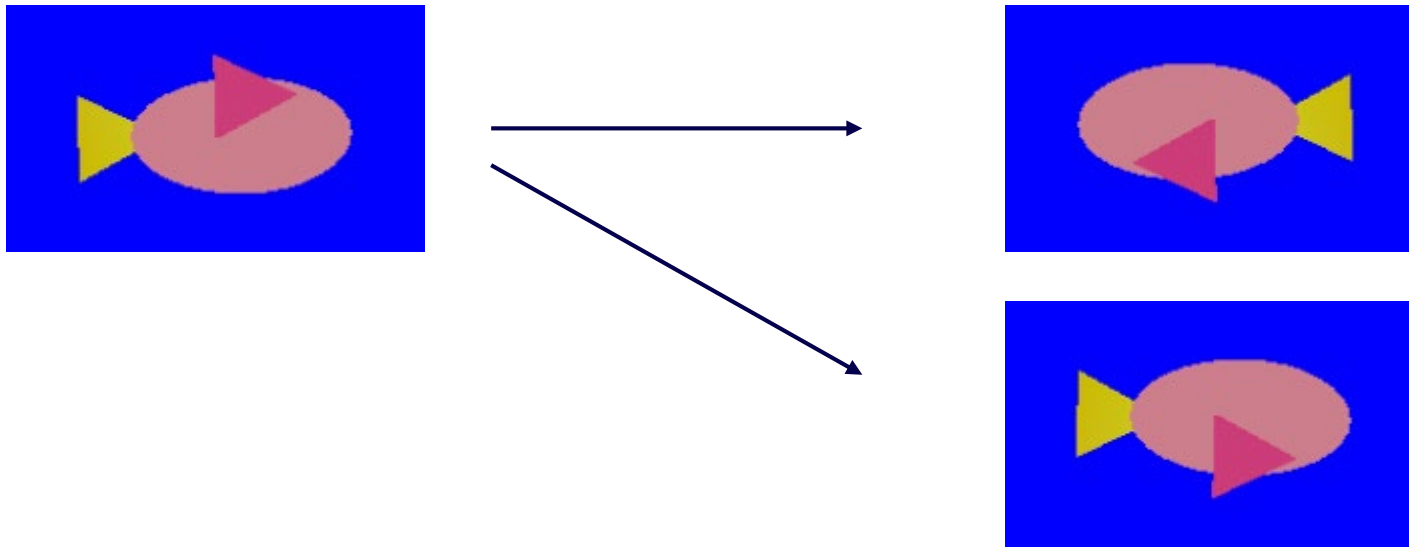


Helge Rhodin

# Modeling Transformations



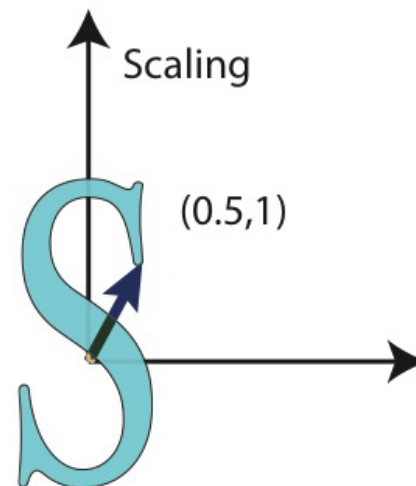
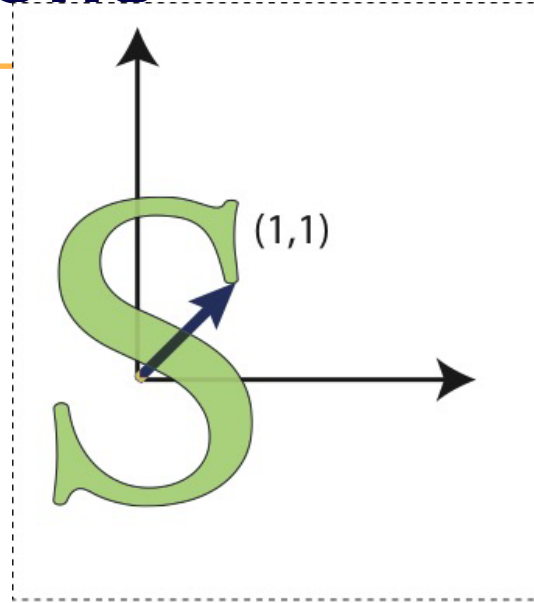
# How to turn the fish?



**Both versions are fine for Assignment 1 (A1)!**

# Matrix representations

**Scale:**





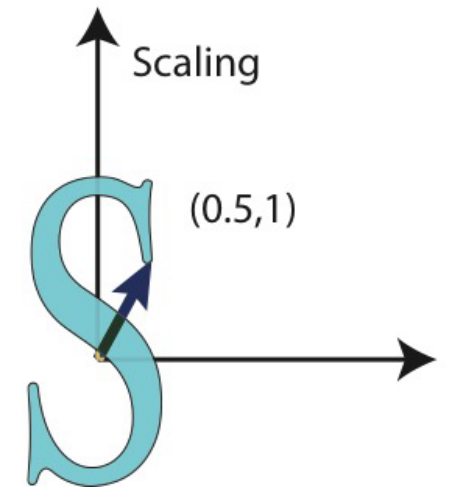
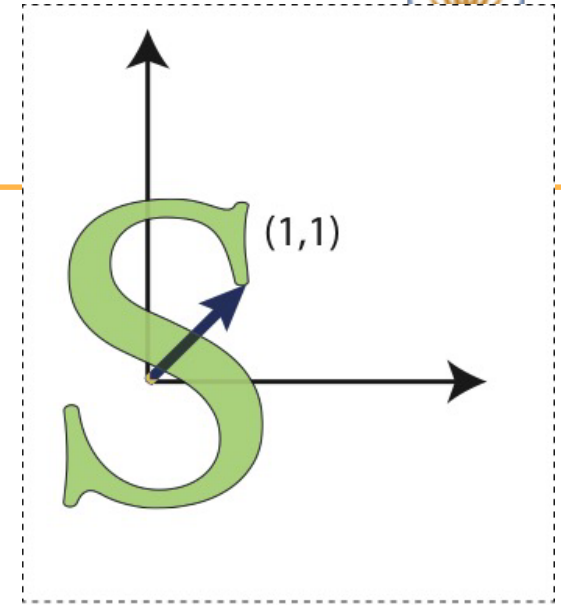
# Matrix representations

## Scale:

$$M = \begin{bmatrix} \alpha & 0 \\ 0 & \beta \end{bmatrix}$$

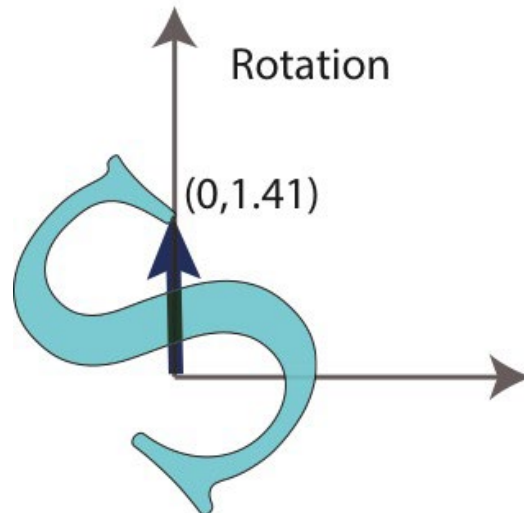
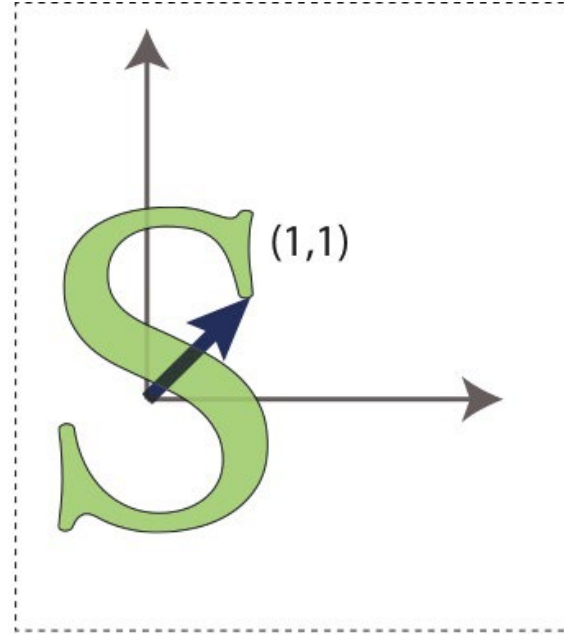
Example:

$$\begin{bmatrix} \alpha & 0 \\ 0 & \beta \end{bmatrix} \begin{pmatrix} 1 \\ 2 \end{pmatrix} = \begin{pmatrix} \alpha \\ 2\beta \end{pmatrix}$$



# Matrix representations

## *Rotation*



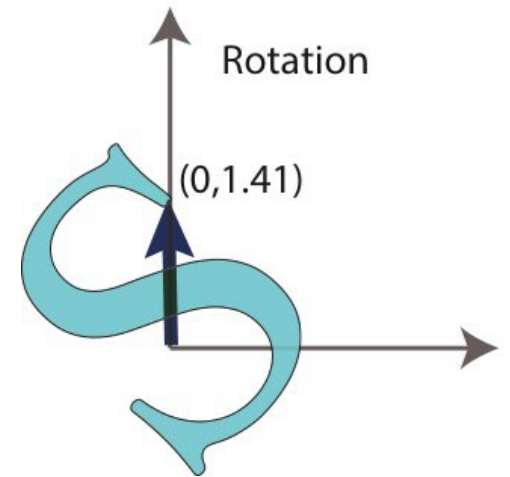
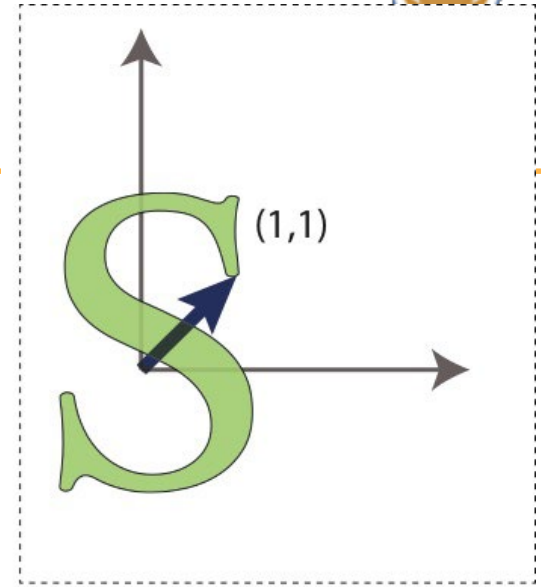
# Matrix representations

## Rotation

$$R(\alpha) = \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{bmatrix}$$

Example:

$$\begin{bmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{bmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix} = \begin{pmatrix} \cos(\alpha) - \sin(\alpha) \\ \cos(\alpha) + \sin(\alpha) \end{pmatrix}$$



## ***What does this 2D transformation do?***

- A. Rotates by 90 deg
- B. Scales by a factor of 2
- C. Rotates by -90 deg
- D. Nothing

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

## ***What does this 2D transformation do?***

- A. Rotates by 90 deg
- B. Reflects the object
- C. Rotates by -90 deg
- D. Scales the object

$$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix},$$

# TRANSLATION

---

*There's a minor glitch.*

- Translation: can't be represented as  $2 \times 2$  matrix multiplication

# general transformations

---

*We need to represent all the  
linear transformations + translation.*

*Ideas?*

$$T(\mathbf{v}) = M\mathbf{v} + \mathbf{b}$$

# AUGMENTED MATRIX

$$M_{2 \times 2} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

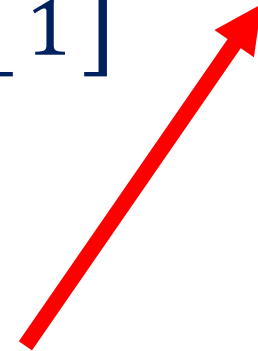
$$\begin{bmatrix} M_{2 \times 2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$

**Haven't changed much, have we?**

# AUGMENTED MATRIX

$$\begin{bmatrix} M_{2 \times 2} & \begin{matrix} b_x \\ b_y \end{matrix} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x' + b_x \\ y' + b_y \\ 1 \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} + \mathbf{b}$$

**Translation**





# Affine transformations

---

- Linear (rotation, scaling, shear, reflections) +  
TRANSLATION

# Affine transformations

---

- Linear (rotation, scaling, shear, reflections) + TRANSLATION
- How to convert a linear transformation matrix into affine matrix?

# AFFINE Transformations

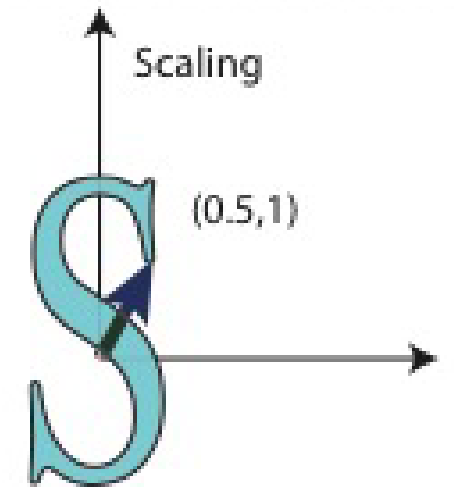
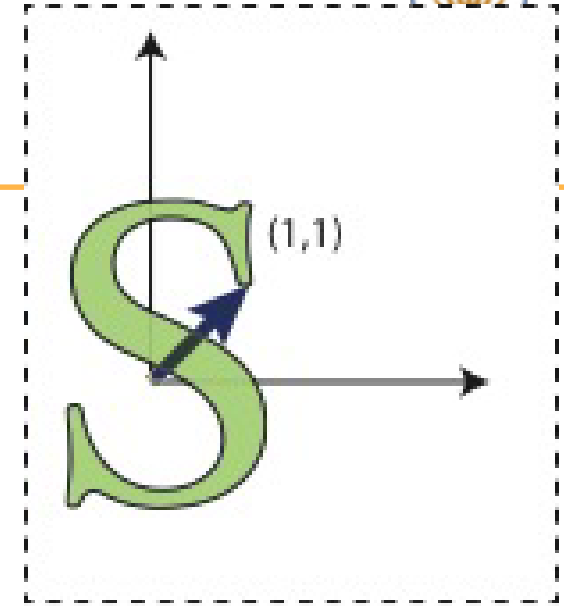
## Scale:

$$M = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}$$

$$M = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Example:

$$\begin{pmatrix} a \cdot 1 \\ b \cdot 2 \\ 1 \end{pmatrix} = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}$$



# AFFINE Transformations

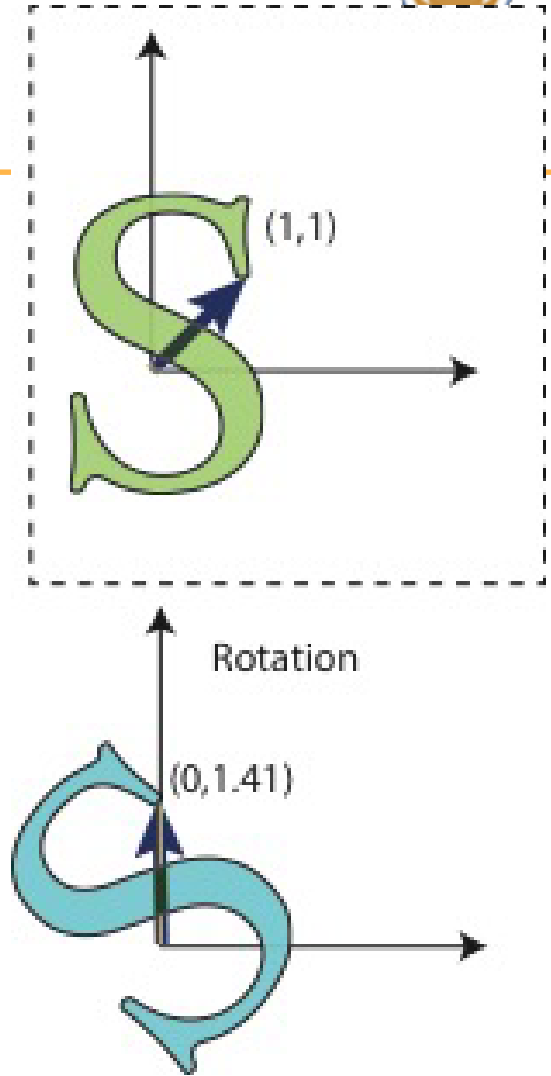
## Rotation

$$M = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}$$

$$M = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Example:

$$\begin{pmatrix} a \cdot 1 \\ b \cdot 2 \\ 1 \end{pmatrix} = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}$$



# AFFINE Transformations

## *Translation*

$$M = \begin{bmatrix} 1 & 0 & C_x \\ 0 & 1 & C_y \\ 0 & 0 & 1 \end{bmatrix}$$

Example:

$$\begin{bmatrix} 1 & 0 & C_x \\ 0 & 1 & C_y \\ 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} = \begin{pmatrix} x + C_x \\ y + C_y \\ 1 \end{pmatrix}$$

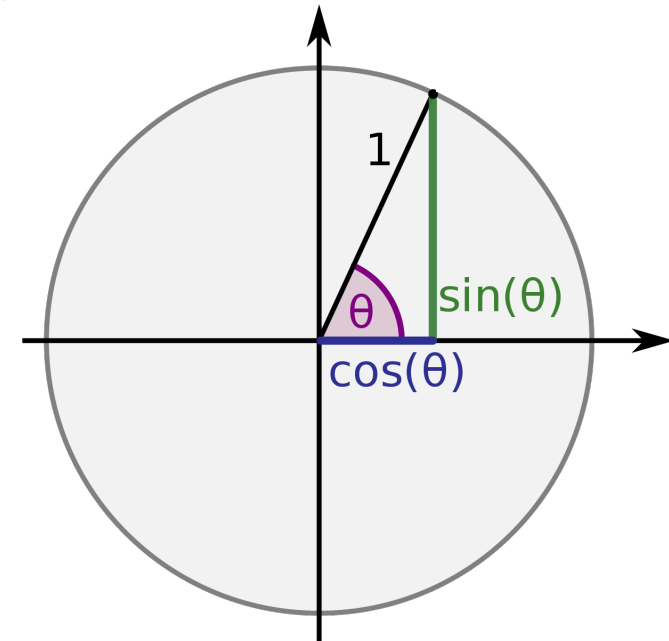
# Linear transformations

- Rotations, scaling, shearing
- Can be expressed as 2x2 matrix (for 2D points)
- E.g.

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

- or a rotation

$$\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$



Rotation angle  $\theta$ ,  $\cos$ , and  $\sin$

[https://en.wikipedia.org/wiki/Trigonometric\\_functions](https://en.wikipedia.org/wiki/Trigonometric_functions)

# Affine transformations

- Linear transformations + translations
- Can be expressed as 2x2 matrix + 2 vector
- E.g. scale + translation:

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \end{pmatrix}$$

# Modeling Transformation

## *Adding a third coordinate*

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \end{pmatrix} \quad \rightarrow \quad \begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \\ 0 \end{pmatrix}$$
$$= \begin{pmatrix} 2 & 0 & t_x \\ 0 & 2 & t_y \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$

Affine transformations are now linear

- one 3x3 matrix can express: 2D rotation, scale, shear, and translation



# Combination of Transformations?

---

- ***How can we combine***
  - translation
  - rotation
  - scaling
- ***... into one matrix?***

## Self study: Homogeneous coordinates

- Homogeneous coordinates are defined as vectors, with equivalence

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} x/z \\ y/z \\ 1 \end{pmatrix} = \begin{pmatrix} x\lambda \\ y\lambda \\ z\lambda \end{pmatrix}$$

- Can also represent projective equations
- homogeneous matrix becomes 4x4

$$\begin{pmatrix} x' \\ y' \\ z' \\ 1 \end{pmatrix} = \begin{pmatrix} 2 & 0 & 0 & t_x \\ 0 & 2 & 0 & t_y \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$