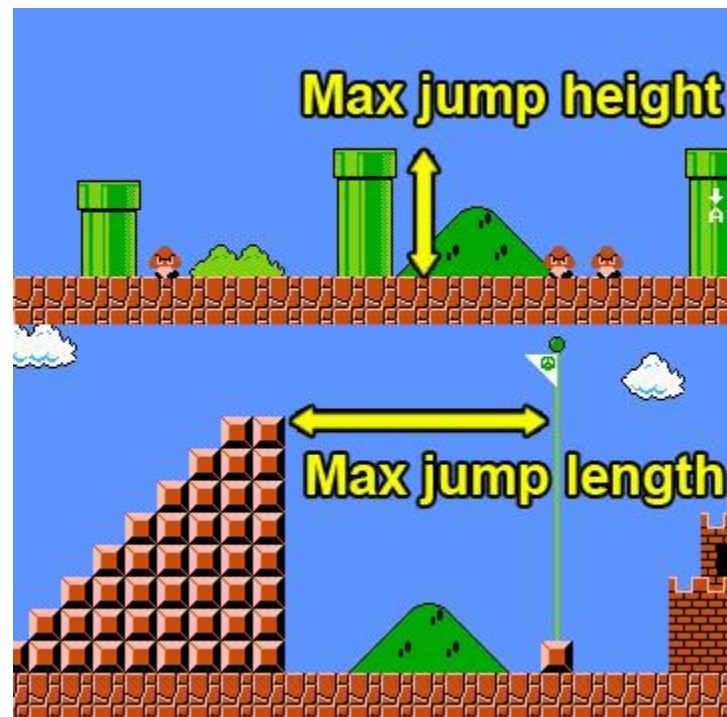


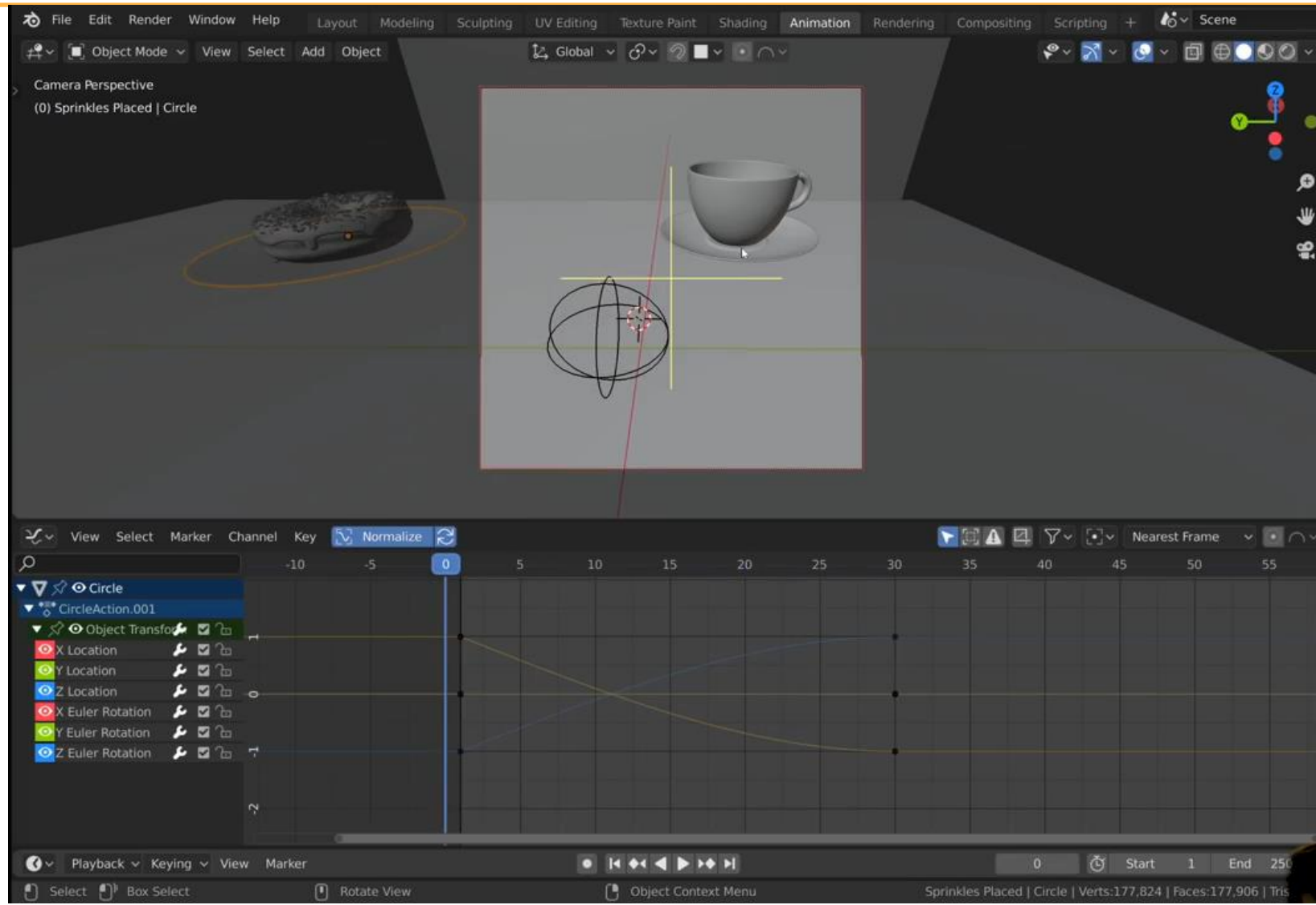
CPSC 427

Video Game Programming

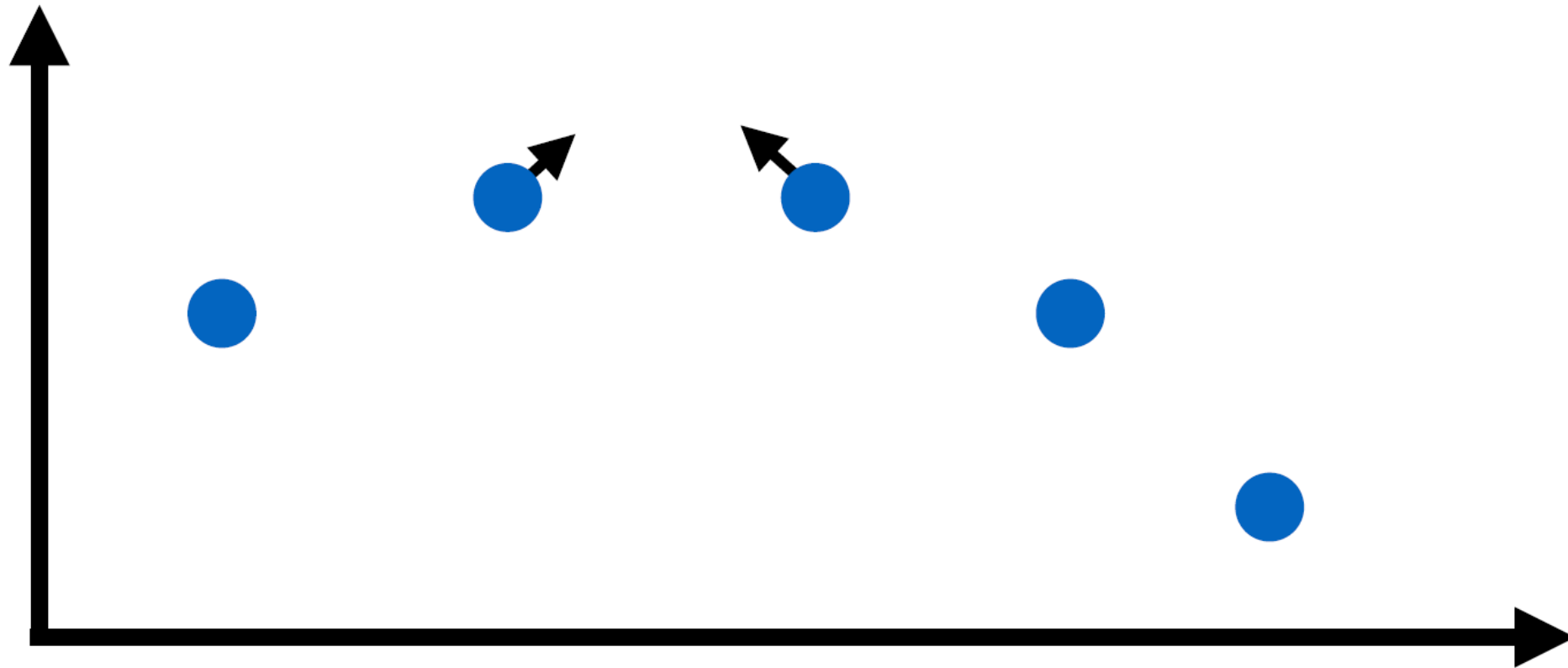
Game Balancing



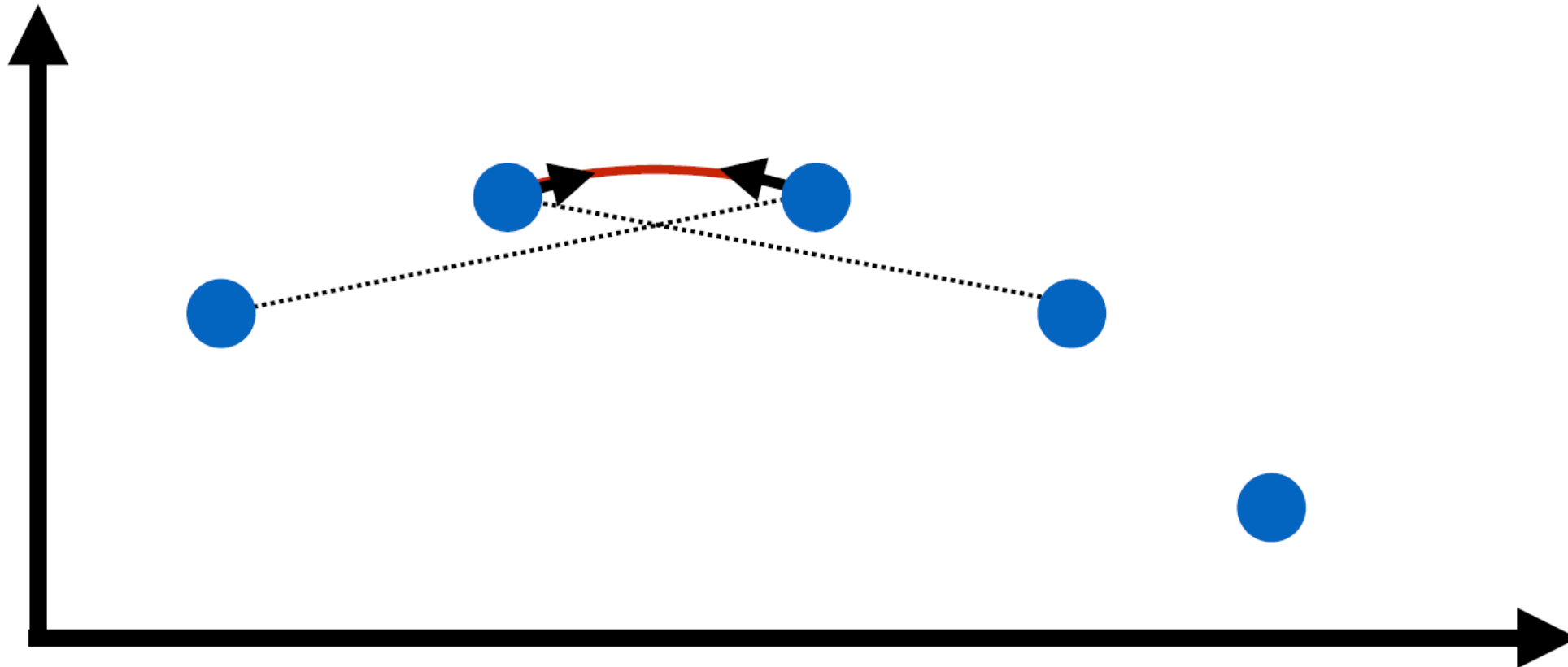
Recap: Keyframe animation & mesh creation



Smooth curve



Smooth curve

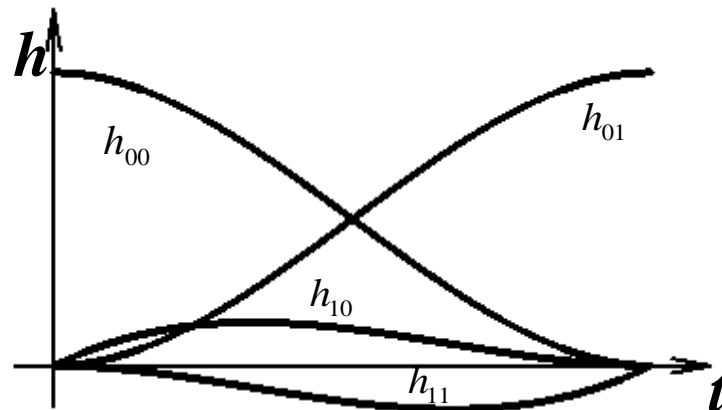


Hermite Cubic Basis

Four cubic polynomials that satisfy the conditions

$$h_{00}(t) = t^2(2t - 3) + 1 \quad h_{01}(t) = -t^2(2t - 3)$$

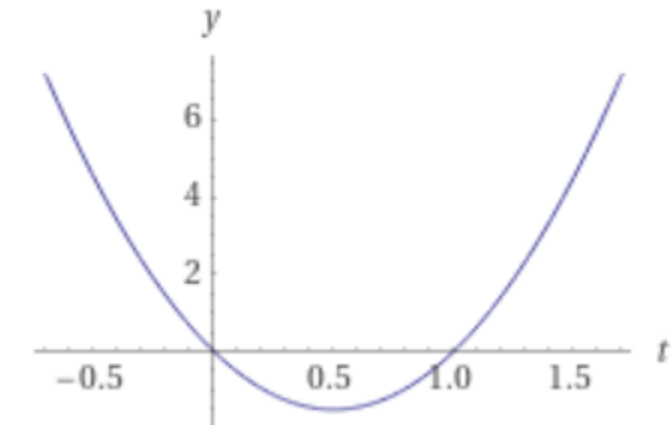
$$h_{10}(t) = t(t - 1)^2 \quad h_{11}(t) = t^2(t - 1)$$



Derivative of h00

$$6(-1 + t)t$$

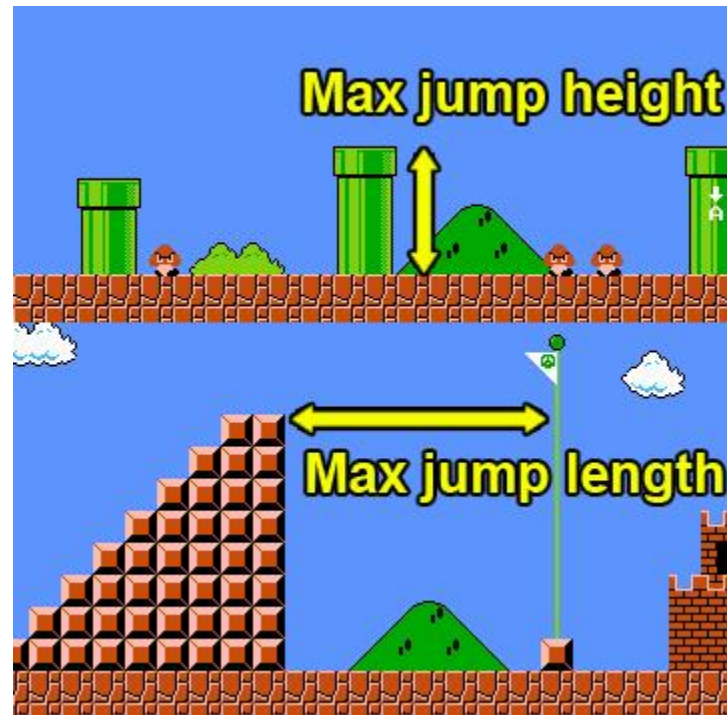
Plots:



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Video Game Programming

Game Balancing



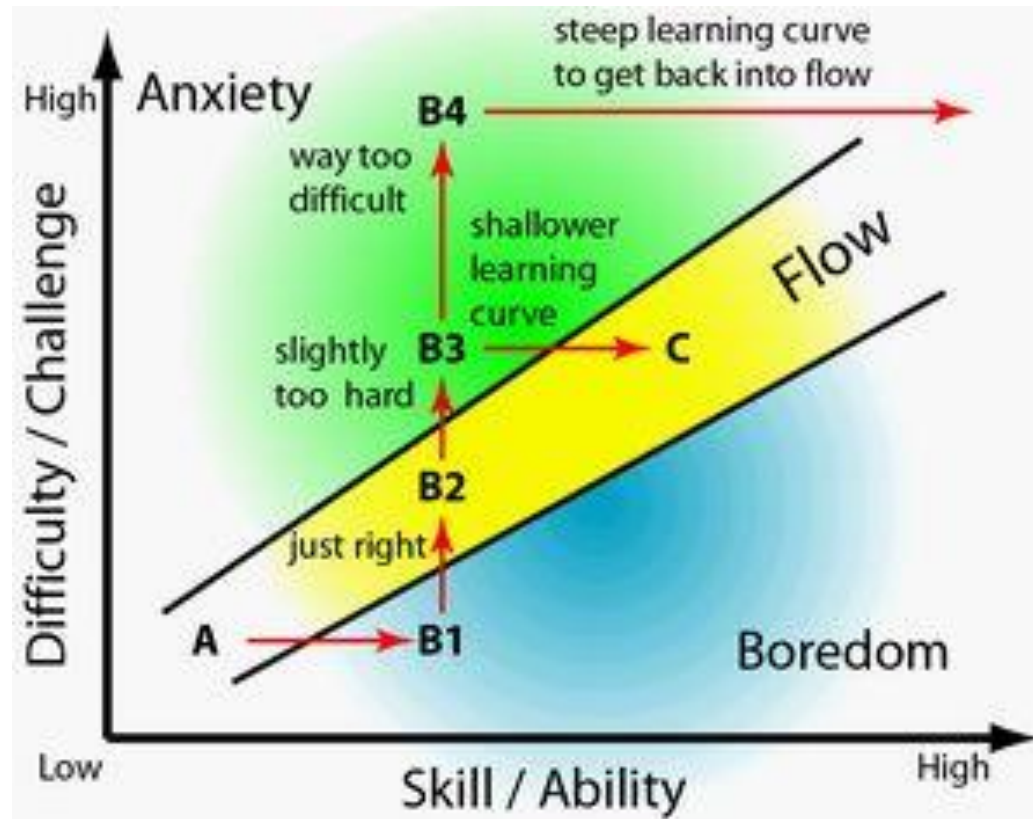


Resources on Balancing

<https://gamebalanceconcepts.wordpress.com/2010/07/07/level-1-intro-to-game-balance/>

by Ian Schreiber

Fun to play?



<https://www.androidauthority.com/level-design-mobile-games-developers-make-games-fun-661877/>

What does balanced mean?

- *Is chess balanced*
- *Settlers of Catan?*
- *Is Tetris balanced?*
- *Is your game balanced?*



Game Theory

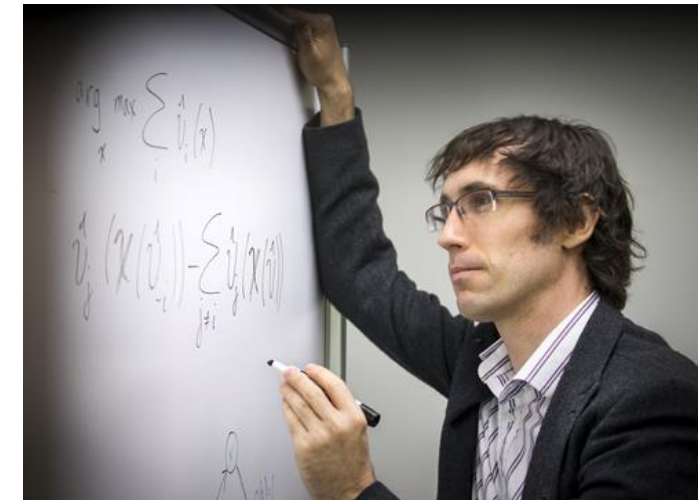
A mathematical concept

- *Used for trading, road design, ...*

Terminology

- **Dominant strategy:** one path that is stronger than all others
- **Fairness:** equal chances to win
- **Nash equilibrium:** each player's strategy is optimal when considering the decisions of other players

Interested?



Kevin Leyton-Brown

Important Considerations

- **Determinism vs. randomness**
- **Solvability**
 - *Has a best/dominant strategy*
 - Is this desirable?
 - *Can you solve a non-deterministic game?*
- **Intransitive games**
 - simultaneous choice between opponents, e.g. *Rock-Paper-Scissors*
- **Symmetric**
 - *same chances*
- **Game and meta game**



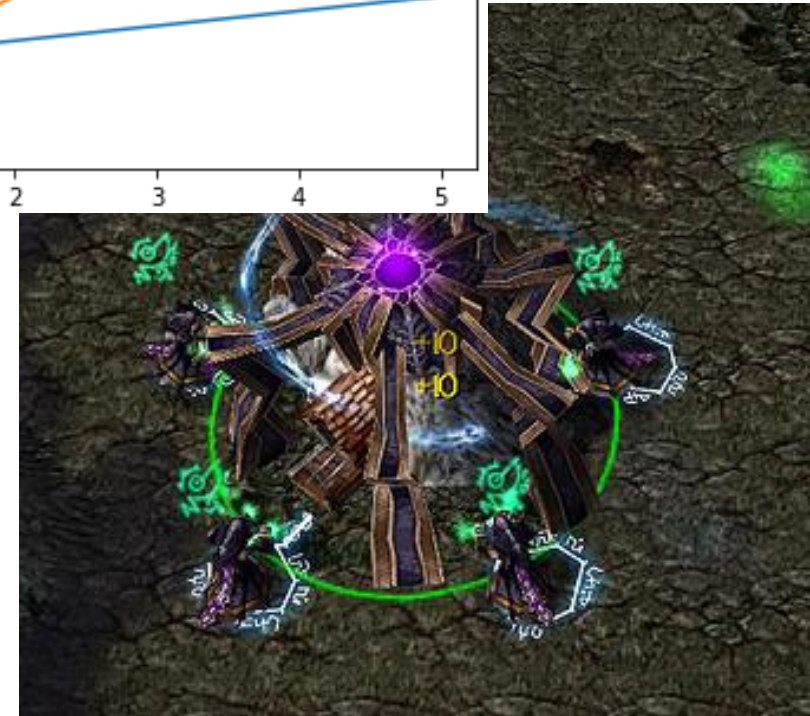
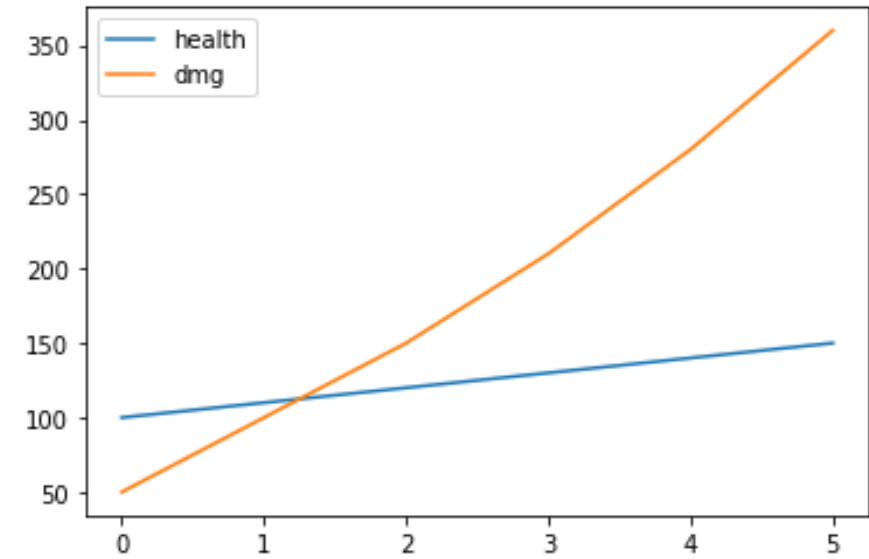
Numeric quantities

- *Values?*



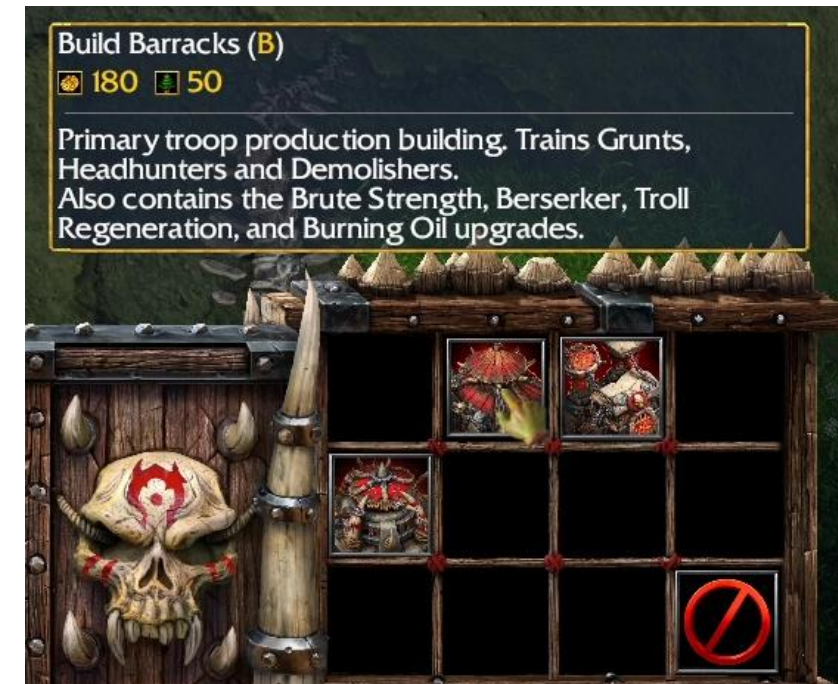
Relationships

- ***Linear relations***
- ***Exponential relations***
- ***Triangular relationship***
 - 1, 3, 6, 10, 15, 21, 28, ...
 - The difference increases linearly
- ***Periodic relations***



Interactions between relationships

- *2x item A + 1x item B = 5x item C*
- *attack speed * damage = damage / second*
- *Buff: 2x health or +100 health*
 - *what is better?*
- *Progression:*
 - *XP -> level up -> new skill -> ?*

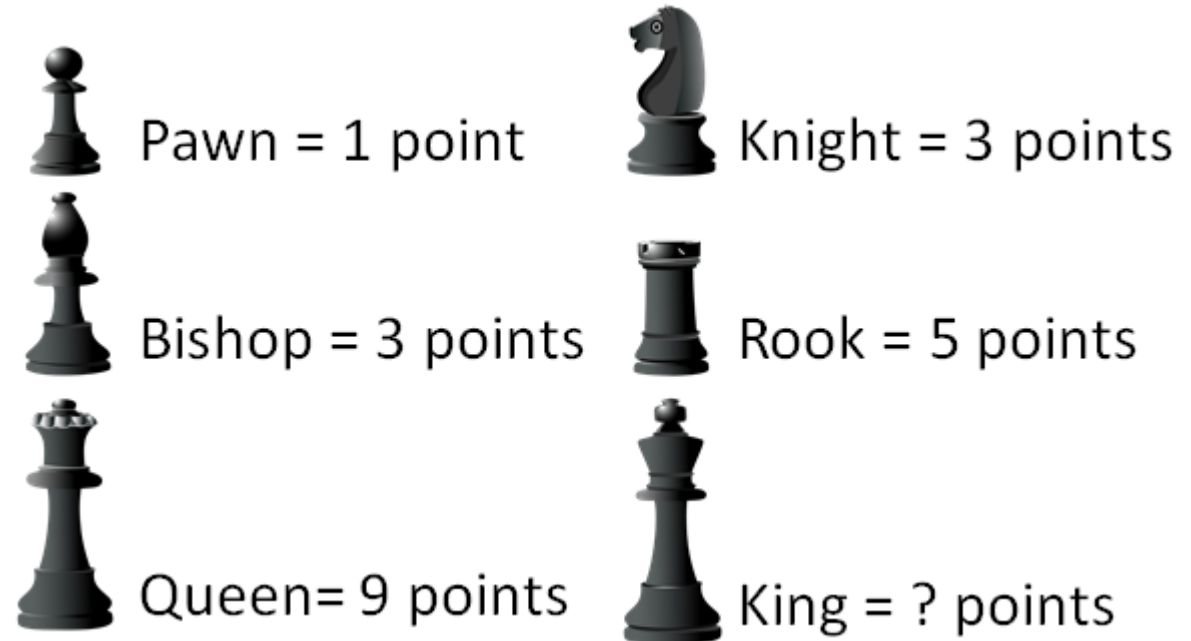


Indirect relationships

Value of a piece

- *It is not possible to get a knight for 3 pawns*
- *But one can 'trade' pieces*
- *A currency*

How to determine?



Breakout

- ***List all relevant quantities in your game***
- ***List their relations:***
 - Type: e.g., linear
 - Quantitatively: e.g., +5 gold per round,
1 gold = 100 silver
- ***Investigate interactions between relations***
- ***What is your game's currency?***
 - *Gold, life, ...?*



6 min
select representative to report

How to quantify difficulty?

- ***Player vs. enemy strength***

- ***Likelihood of winning***

-> Estimate player strength in relation skill level: beginner, intermediate, pro?
-> requires user studies!

- ***Required skill***

- *Knowledge of the game*
- *Reaction*
- *Precision*
- *Tactics*



Randomness

- *How to compute with probabilities?*
- *Distributions instead of single values*
- *Expectation instead of a certain value*

- *How to quantify uncertainty?*
 - *Probability over discrete events, e.g., Bernoulli distribution*
 - *Variance for continuous variables*



Self study: *Gambler's Fallacy*
Hot-Hand fallacy

Do you have randomness in your game

- ***Where?***
 - *Level, damage, AI, ???*
- What kind?
 - *Independent, correlated, uniform, normal distribution?*
- Random or pseudo-random?
 - *Save a player from being unlucky!*

Balancing example

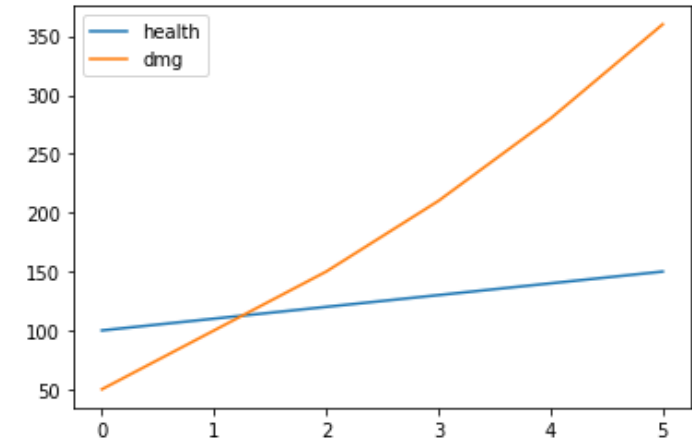
- *10 enemies per level*
- *One tower does 1 damage / sec*
- *One tower costs 2 gold*
- *It takes enemies 10 seconds to pass*



- ***How much gold should the player start with?***
- ***Enemy health increases: 11,12,14,17,21,...***
- ***How much gold should the player get in round 2?***
- ***How much gold should each eliminated enemy give?***

Asymptotic analysis?

- *Linear * linear?*
- *Linear + linear?*
- *Linear + exponential?*
- *Linear * exponential?*



Formally, given functions $f(x)$ and $g(x)$, we define a binary relation

$$f(x) \sim g(x) \quad (\text{as } x \rightarrow \infty)$$

if and only if (de Bruijn 1981, §1.4)

$$\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = 1.$$



Demo

Numerical Methods - Optimization

- ***Iterative optimizers***
 - Single variable?
 - Multiple variables?
 - Gradient descent?

Difficulties:

- ***Placement of towers changes the time damage is dealt***
- ***Path of enemies can be hindered to increase time***
- ***Measure during playtest***
 - *cross-play*
- ***Some enemies are resistant to fire/magic/...?***
 - *kind of a periodic feature*



M4 updated requirement

~~User study~~

***Carefully balance one aspect of your game
(e.g., movement-speed, health points, strength, bonus,...).***

- ***Report on the theoretical analysis***
- ***Change log with testing***

Breakout II

- ***Sketch progression***
 - *Quantities over time*
 - *Interactions between quantities*
- ***Use pen & paper, plotting tool, or python***
- ***Start balancing your game***

Counter Measures

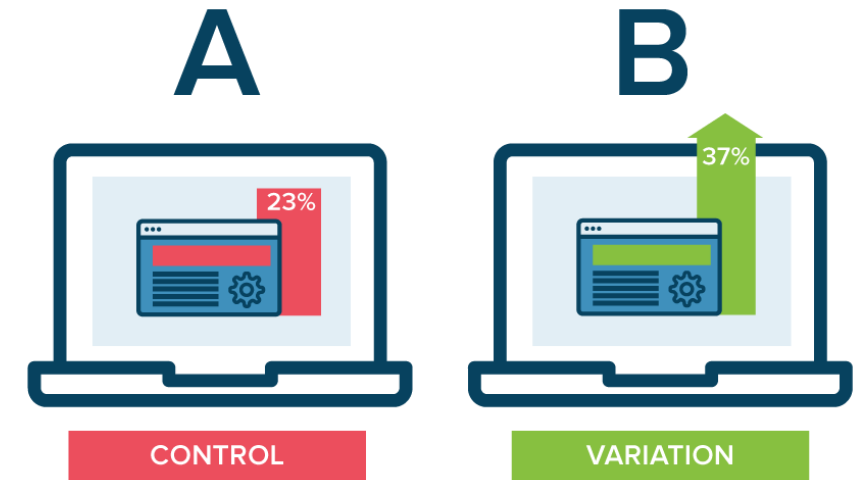
- **Transitive Mechanics**
 - *Repair costs*
 - *Consumables (food, potions, ...)*
 - *Tax*



A/B Testing

Testing two variants of your game (with and w/o a feature)

- *randomized participants (same pool)*
- *with respect to a measurable objective (e.g., clicks on website)*



Related to

- two-sample hypothesis testing
- Clinical tests, e.g., testing of a COVID-19 vaccine
- Placebo effect

Next week:

Tuesday:

Guest lecture

- *By Skybox*
- *On multithreading and optimization*

Thursday:

Team presentation

- *30 min*

Cross-play

- *50 min* *be there!*

Next next week ():

Tuesday:

Guest lecture

- *By Dinos (Charm Games)*
- *Virtual Reality*

Thursday:

• ***Lecture***

- *Articulated motion and inverse kinematics*