

“A language that doesn't affect the way you think about programming, is not worth knowing.”

— Alan J. Perlis, Epigrams on Programming, 1982

Last class

- Examples of simple Haskell programs.
- Infix and prefix functions
- How Haskell works

Today

- Basic types and classes

- comments are either
 - comment to end of line or {- comment -}
- variables either:
 - ▶ prefix: made up of letters, digits, ' or _ and start with a lower-case letter
 - ▶ infix: made up of sequences of other characters
- indentation is significant
- parentheses are used for precedence and tuples
- Function application binds most strongly
 - factorial 3*5 means
 - (factorial 3)*5
- Binary prefix functions can be made infix using back-quotes, e.g. 'div'
Infix operators can be made prefix using parentheses, e.g. (*)

Definition of a function

- Function Definition:

name $x_1 x_2 \dots x_k = e$

$x_1 x_2 \dots x_k$ are formal parameters

e is an expression

- Multiple equations can define a function; the first one to succeed is used.

Evaluation of Haskell program

- Haskell evaluates expressions.
- Haskell knows how to implement some expressions (such as $3+4*7$)
- Given the definition of name:

`name x1 x2 ... xk = e`

The expression

`name v1 v2 ... vk`

when all k arguments are provided, evaluates to value of e but with each x_i replaced with v_i

`foo x y = 1000*x+y`

`foo 9 3`

`bar = foo 7`

`bar 3`

Type Declarations

For the definition of name:

`name x1 x2 ... xk = e`

- Type declaration:

`name :: t1 -> t2 -> ... -> tk -> t`

t_i is type of x_i , and t is the type of e .

- Each function takes only one argument:

`name v1` is a function of type `t2 -> ... -> tk -> t`

`name v1 v2 ... vk` is a value of type t

It's value is the value of e with each x_i replaced by v_i

- Haskell Types:

Bool (&&, ||, not)

Num (+, -, *, abs)

Integral (div, mod)

Int

Integer

Fractional (/)

Floating (log, sin, exp, ...)

Double

Eq (==, /=)

Ord (>, >=, <=, <)

Char

String

Type: Bool

- Bool is a type with two values True and False.
- operations:

<code>&&</code>	and
<code> </code>	or
<code>not</code>	not

- How can we define exclusive-or (`xor`)?
- How can we define if-then-else?
- What would happen if we tried to do this in Java?
(Answer: because Java evaluates a method's arguments before calling the method, a method implementation of if-then-else would not halt for recursive methods.)

Integral types

- **Integral** types represent integers.
- They implement `+` `*` `^` `-` `div` `mod` `abs` `negate`
- Two implementations:
 - ▶ **Int** - fixed-precision integers
 - ▶ **Integer** - arbitrary precision integers
- Integral is a **class**.
Int and Integer are **types** in class Integral.
Only types have implementations.
(Haskell classes are like Java interfaces)
- `div :: Integral a => a -> a -> a`
div takes two arguments of the same type, and returns a value of that type.
That type must be in the Integral class.

Fractional types

- **Fractional** types represent real numbers.
- They implement + * ^ - / abs negate
- **Floating** types also implement log sin exp ...
- Multiple implementations:
 - ▶ **Double** - double precision floating-point numbers (64 bit)
 - ▶ **Float** - single precision floating-point numbers (32 bit)
— don't use
 - ▶ **Rational** - exact rational numbers
- There are no types that are both Integral and Fractional.
- Num types implement + * ^ - abs negate
Num is a class (elements are types).
Integral and Fractional are subclasses of Num

Eq and Ord classes

- **Eq** types implement `== /=`
- **Ord** types implement `> >= <= < max min`
- `Int`, `Integer`, `Double` implement `Eq` and `Ord`
- Can you think of a `Num` type that isn't an `Ord` type?
How about `Complex`?
- What is the type of `3`?
- What is the type of `div 100 3`?
What is the type of `3.7`?
What is the type of `(div 100 3) + 3.7`?
- `fromIntegral` converts an integer to a `Num`.

- Guards are used for if-then-else structure in definition of functions.
- Example

```
mymax x y  
  | x>y = x  
  | otherwise = y
```

It evaluates the guards; the first one succeeding, the corresponding expression is returned

- General case:

```
name x1 x2 ... xk
  | g1 = e2
  | g2 = e2
  ...
  | gn = en
```

- evaluate g_1, g_2 in turn until the first one g_i evaluates to true, then return value of e_i .
- An Exception is raised if none of the guards are True
- Typical to have last condition to be otherwise which is a variable with value True.
- How can we implement max3?
- Haskell also has “if ... then ... else ...” structure