Question 1 [10 marks]

Consider the following knowledge base, $KB$. (Assume predicates have been defined dynamic so there are no undefined procedure errors.)

\[
\begin{align*}
p &: m, c. \\
p &: r, s. \\
m &: n. \\
c. \\
r &: t. \\
r &: w. \\
t &: v. \\
w. \\
s &: a. \\
a. \\
\end{align*}
\]

(a) [4 marks] $m$ is not a logical consequence of $KB$. Give a model of $KB$ in which $m$ is false.

(b) [6 marks] $p$ is a logical consequence of $KB$. Complete the following successful top-down derivation for the query $?- p$. (Hint: work out which choices lead to a proof; do not include the failing branches)

<table>
<thead>
<tr>
<th>Answer clause</th>
<th>Clause resolved</th>
</tr>
</thead>
<tbody>
<tr>
<td>yes :- p</td>
<td>-</td>
</tr>
<tr>
<td>yes :- r, s</td>
<td>p :- r, s</td>
</tr>
</tbody>
</table>

Question 2 [12 marks]

Here is the KB from the previous page

\[
\begin{align*}
p &: m, c. \\
p &: r, s. \\
m &: n. \\
c. \\
s &: a. \\
r &: t. \\
r &: w. \\
t &: v. \\
w. \\
\end{align*}
\]
(a) [6 marks] Draw the box model for \( p \). You need to include the ports, but not the port names. You need to include the names for the atoms that the boxes represent.

(b) [6 marks] Here is a (edited) trace of the query \(?- p\). Fill in the missing (underlined) lines:

```
  Call: p
  __________________________________________
  Call: n
  __________________________________________
  Fail: m
  Redo: p
  __________________________________________
  Call: t
  Call: v
  Fail: v
  __________________________________________
  Redo: r
  Call: w
  Exit: w
  Exit: r
  __________________________________________
  Call: a
  Exit: a
  __________________________________________
  Exit: p
true.
```

**Question 3 [10 marks]**

The following code is from Assignment 4.

\% name(P,F,L) means person P’s first name is F and last name is L
name(davidp, "David", "Poole").
name(ainaz, "Ainaz", "Hajimoradlou").
name(liran, "Liran", "Li").
nname(rui, "Rui", "Ge").

\% office_hour(P, D, S, F) means office hours for person P are on day D from S to F.
office_hour(davidp, wednesday, 15, 16).
office_hour(ainaz, thursday, 16, 17).
office_hour(liran, monday, 11, 12).
office_hour(liran, wednesday, 17, 18).
office_hour(rui, thursday, 10, 11).

(a) [4 marks] David wrote the following program

\% twoofficehours(D) is true if there are office hours
% on day D starting at different times
twoofficehours(D) :-
    office_hour(_,D,H1,_),
    office_hour(_,D,H2,_),
    H1 < H2.

Why did he write \( H_1 < H_2 \)?

(b) [6 marks] Define the following predicate that is true if \( F_1 \) and \( F_2 \) are the first names of two people that have office hours on the same day. This must work even if two or more of the people have the same first name. It should work whether the names are provided in a query or not. You may use any of: dif, append, length, <

\[
\text{office_hours_on_same_day}(F_1,F_2) :-
\]

**Question 4 [10 marks]**

(a) [6 marks] Write a program \( \text{delall}(E, L, R) \) which is true when \( R \) is a list with the same elements as list \( L \) (in the same order) but with all instances of \( E \) deleted. The only predefined predicate you may use is \( \text{dif}(X, Y) \) that is true when \( X \) and \( Y \) are different. For example, it should have the following behaviour (where these are all the answers and different answers are separated by ";"): 

\[
?- \text{delall}(a, [a, v, a, t, a, r], R).
R = [v, t, r]
\]

\[
?- \text{delall}(a, [f, U, n], R).
U = a,
R = [f, n] ;
R = [f, U, n],
dif(U, a)
\]

(b) [4 marks] What are all of the answers to the query

\[
?- \text{delall}(X, [a, b, c, a], R).
\]

(Note that you should be able to do this, even if you cannot do part (a).)