

Announcements

■ Assignment 1

- programming (**due Friday**)
- submission directories are fixed use (submit -N A1b **cscd18f08** a1_solution.tgz)
- theory will be returned (**Wednesday**)

■ Midterm

- Will cover **all of the materials so far including today's lecture**
 - Lecture notes, lecture slides, readings, assignment are all fair game
- Practice midterms are on-line (no solutions will be given)

■ Tutorial this week

- Life of the polygon
- A1 theory questions

■ Office Hours

- I will have office hours **today 1-2 pm**
- Alex will have office hours later in the week
- I will also have office hours on **Tuesday 4-5pm**

Last week's review ...

■ Cameras (theory)

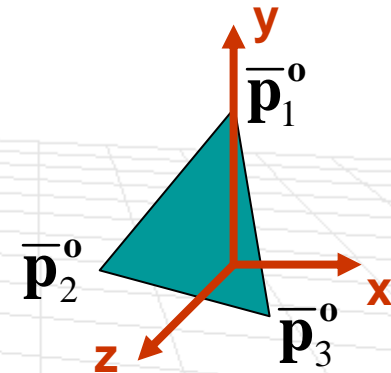
- ❑ Pinhole Camera
- ❑ Thin Lens model
- ❑ Virtual pinhole camera
- ❑ Perspective and orthographic projections

■ Cameras (practice)

- ❑ Location of camera in space
- ❑ Transformation of geometry from camera to world coordinate frame and (**vice versa**)
- ❑ **Homogeneous Perspective Projection** (how do we represent perspective using a single 4x4 matrix)
- ❑ Homogeneous Prospective Projection with **Pseudodepth**

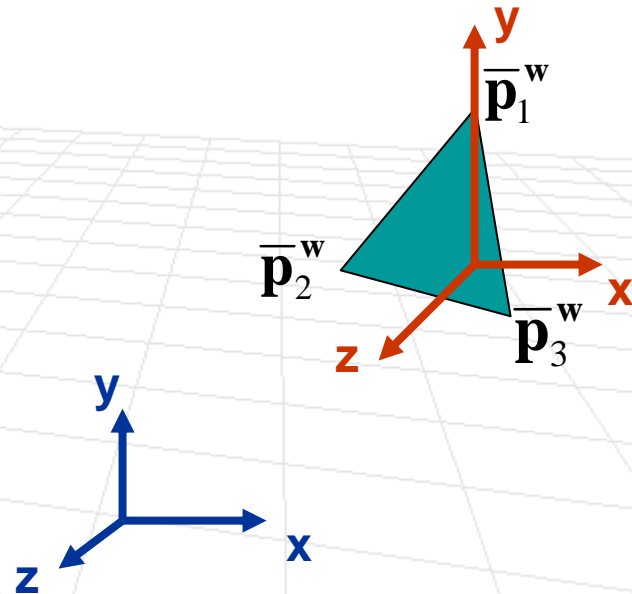
Projecting Triangle

- Lets review steps in the rendering hierarchy
 - Triangle is given in the object-based coordinate frame as three vertices



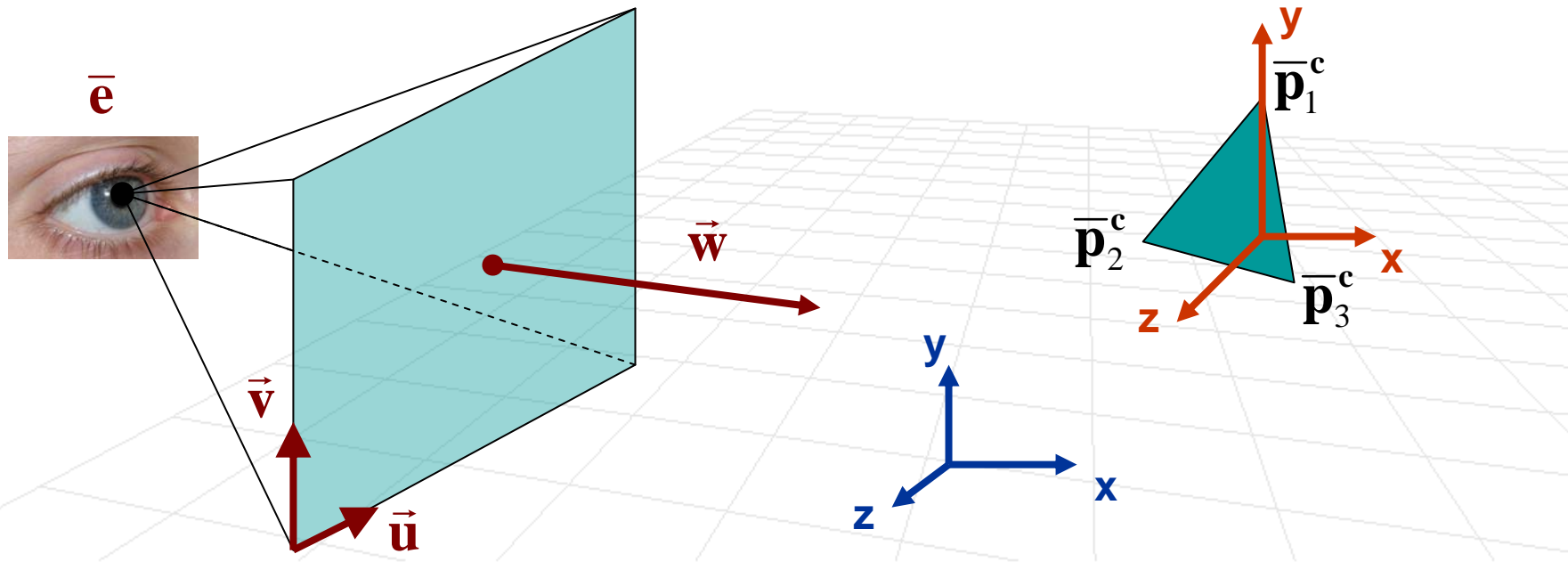
Projecting Triangle

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 - Triangle is given in the object-based coordinate frame as three vertices
 - Transform to world coordinated $\bar{\mathbf{p}}_i^w = \mathbf{M}_{ow} \bar{\mathbf{p}}_i^o$



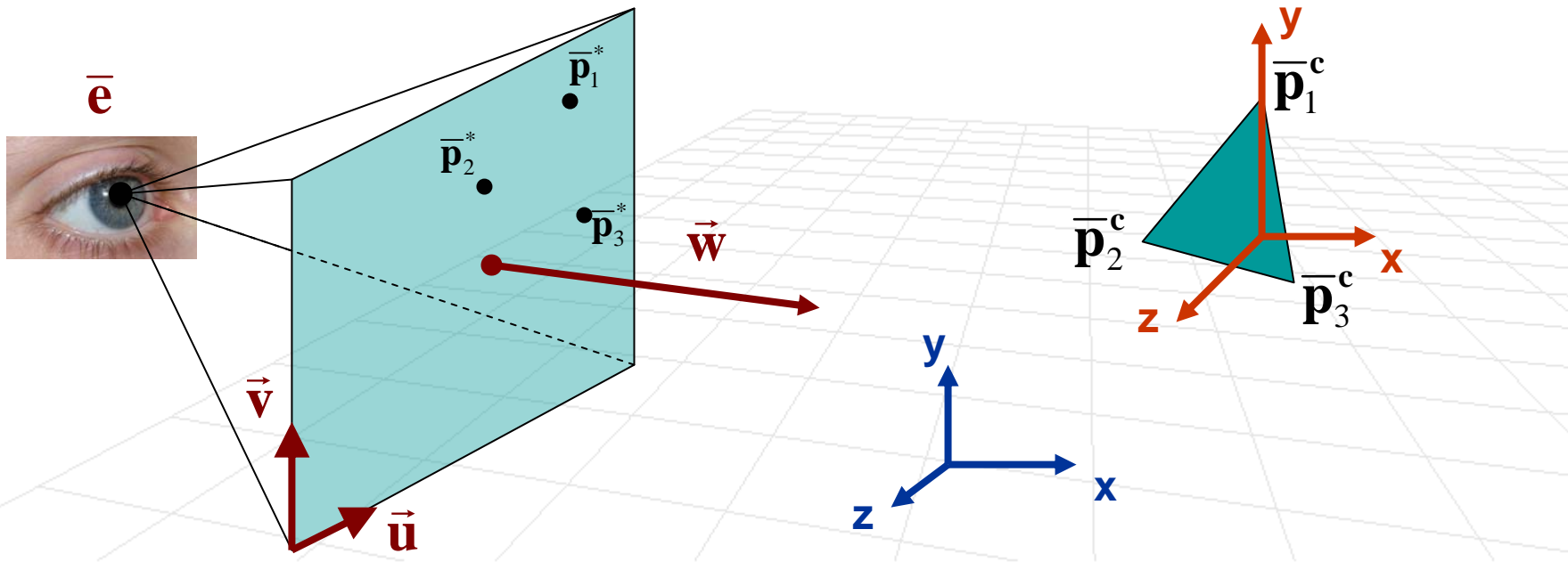
Projecting Triangle

- Lets review steps in the rendering hierarchy
 - Triangle is given in the object-based coordinate frame as three vertices
 - Transform to world coordinated $\bar{\mathbf{p}}_i^w = \mathbf{M}_{ow} \bar{\mathbf{p}}_i^o$
 - Transform from world to camera coordinates $\bar{\mathbf{p}}_i^c = \mathbf{M}_{wc} \bar{\mathbf{p}}_i^w$



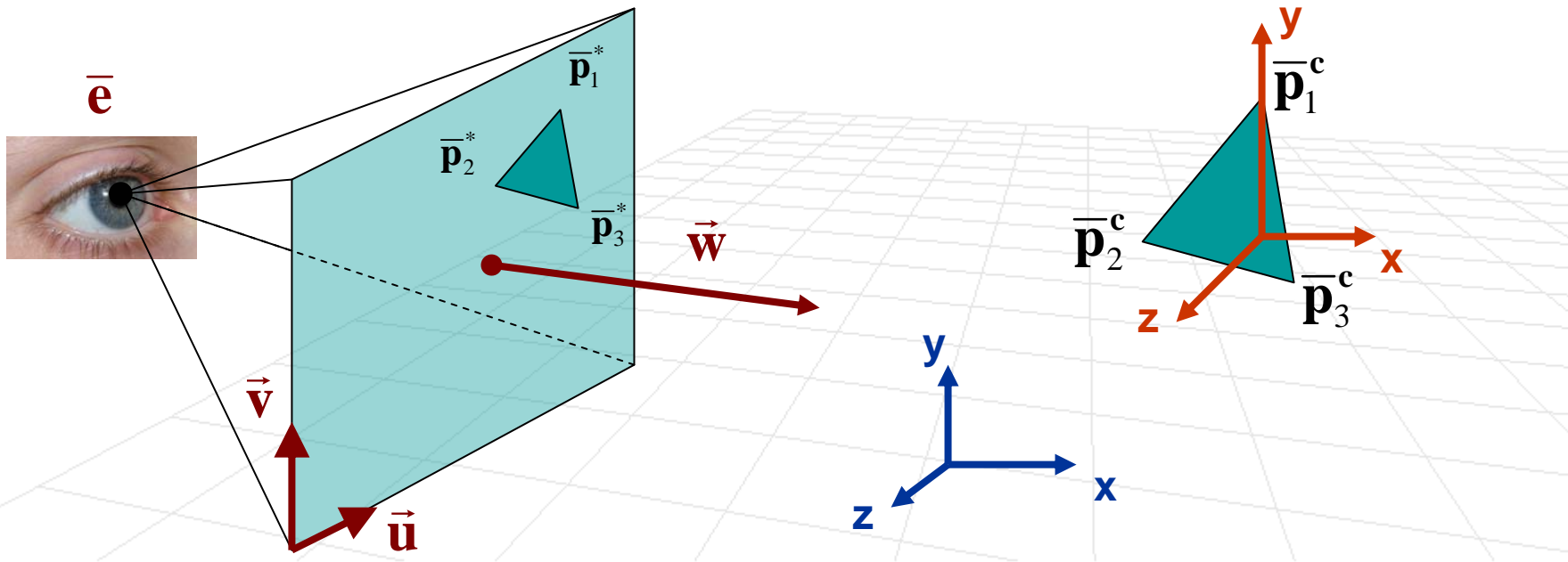
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 - Apply homogeneous perspective $\bar{\mathbf{p}}_i^* = \mathbf{M}_p \bar{\mathbf{p}}_i^c$
 - Divide by last component



Projecting Triangle

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Visibility

Computer Graphics, CSCD18

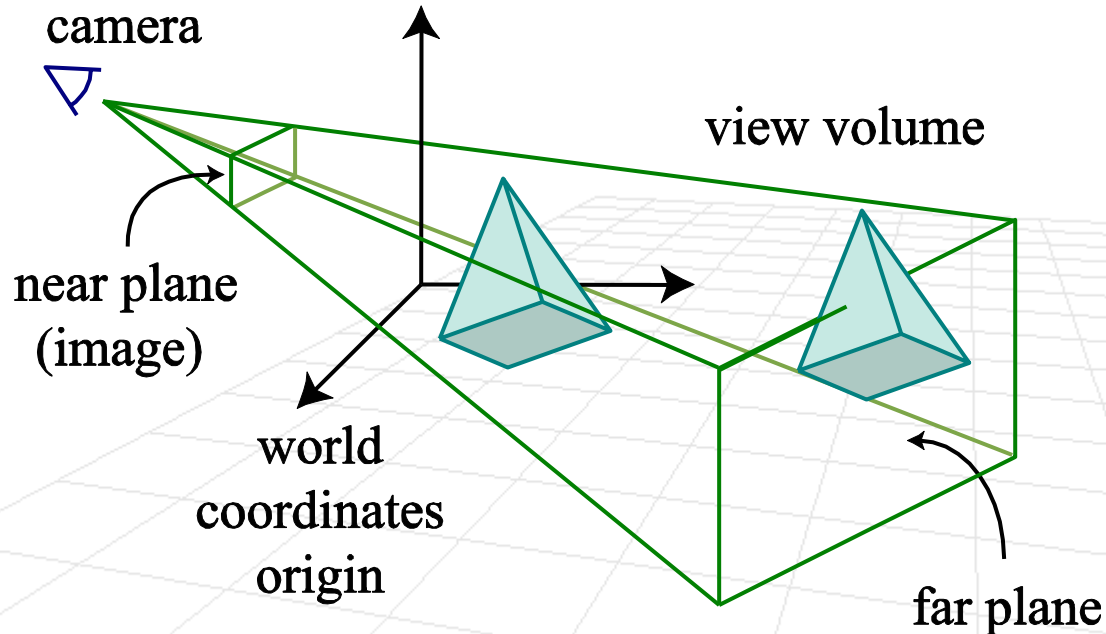
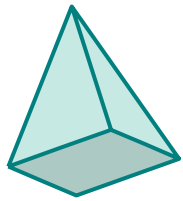
Fall 2008

Instructor: Leonid Sigal



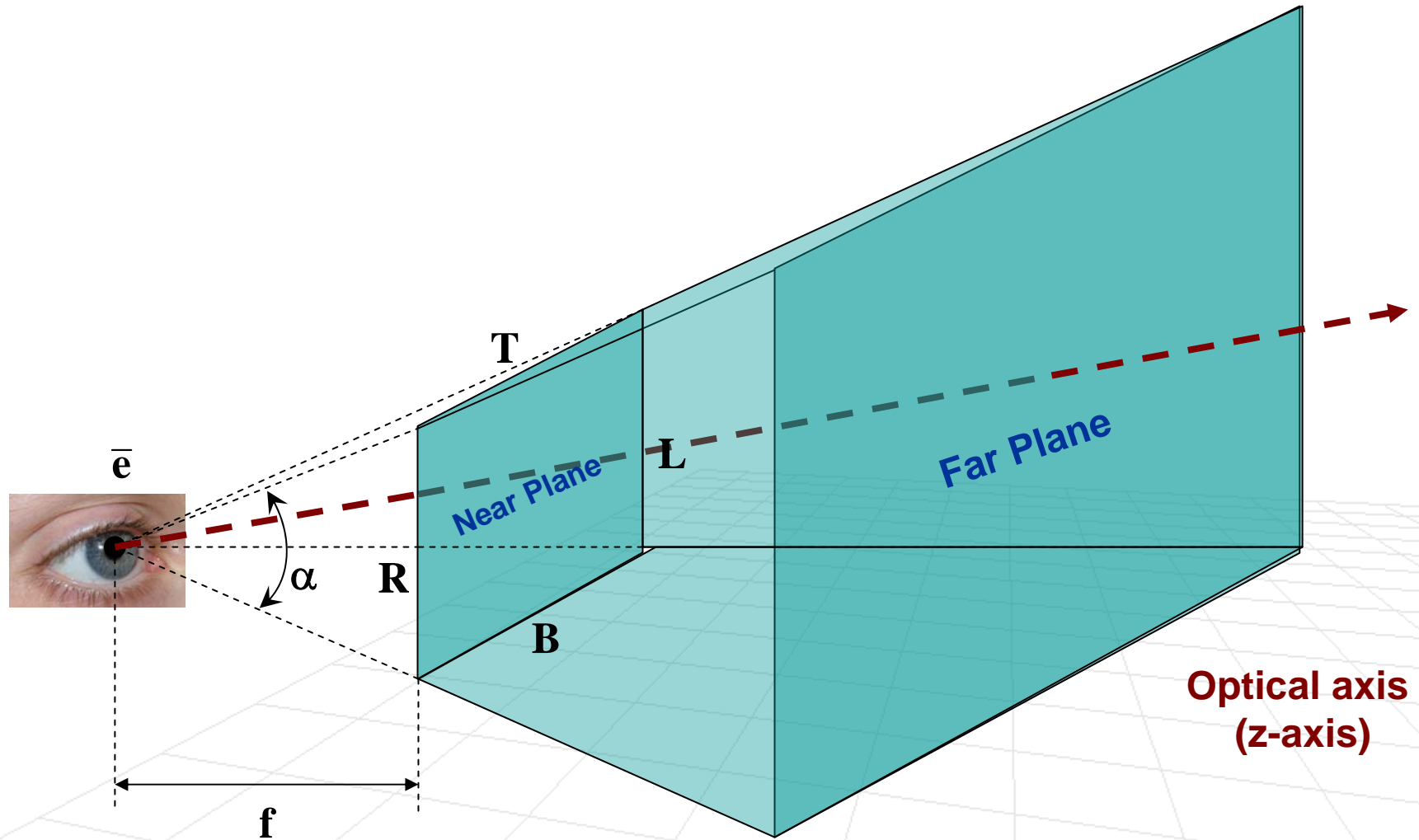
Clipping

- **Idea:** Remove points and parts of objects outside view volume
- Sounds simple, but consider if we have an object on a boundary

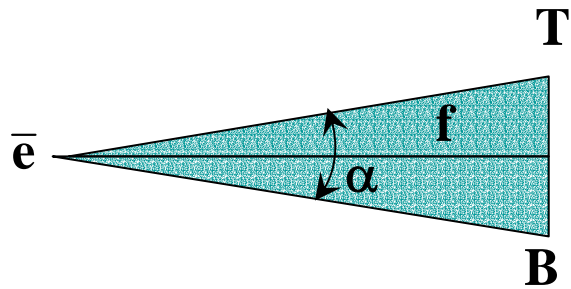


View Volume

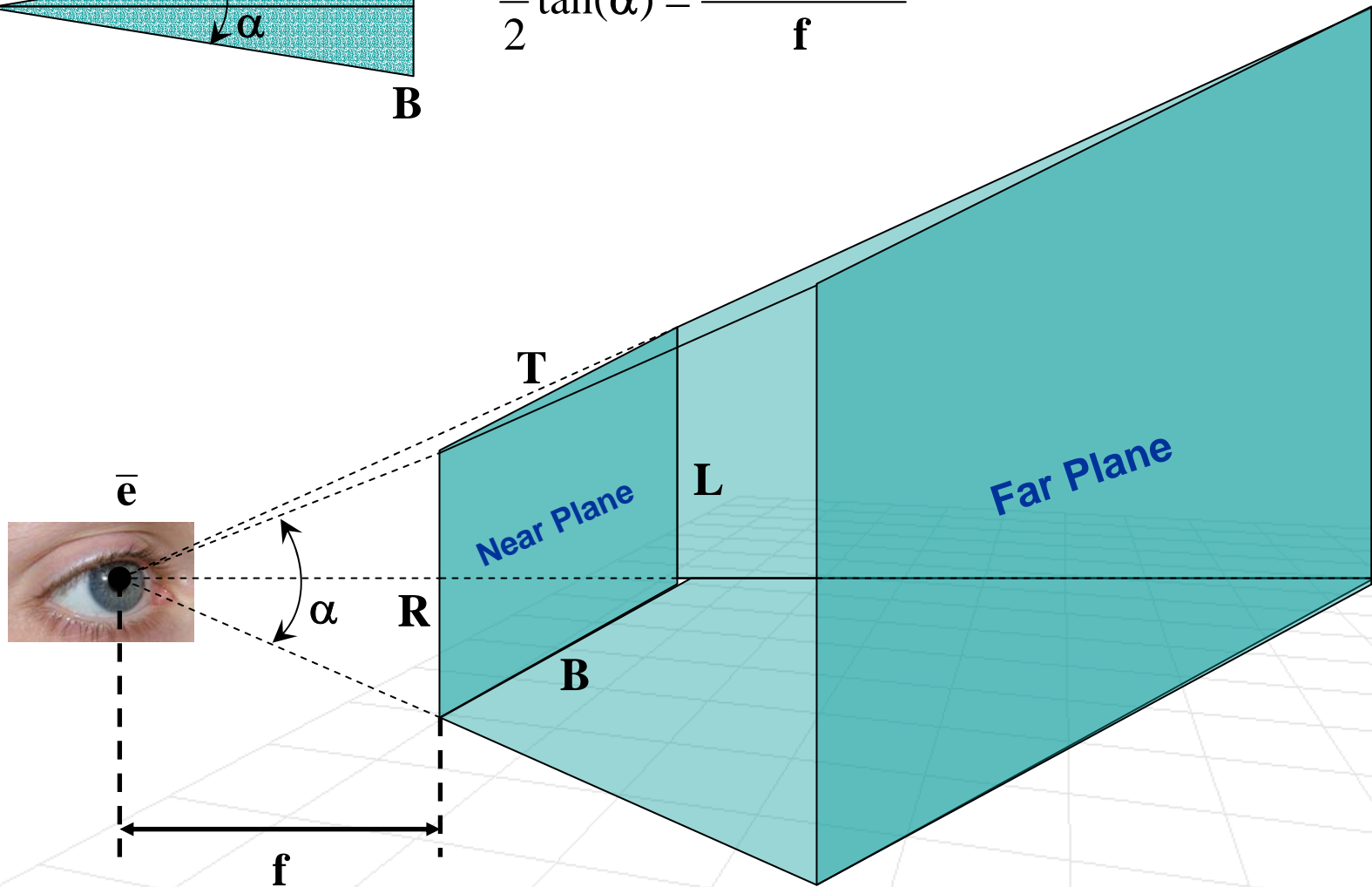
- Consider what we can actually see



Side note: Field of View



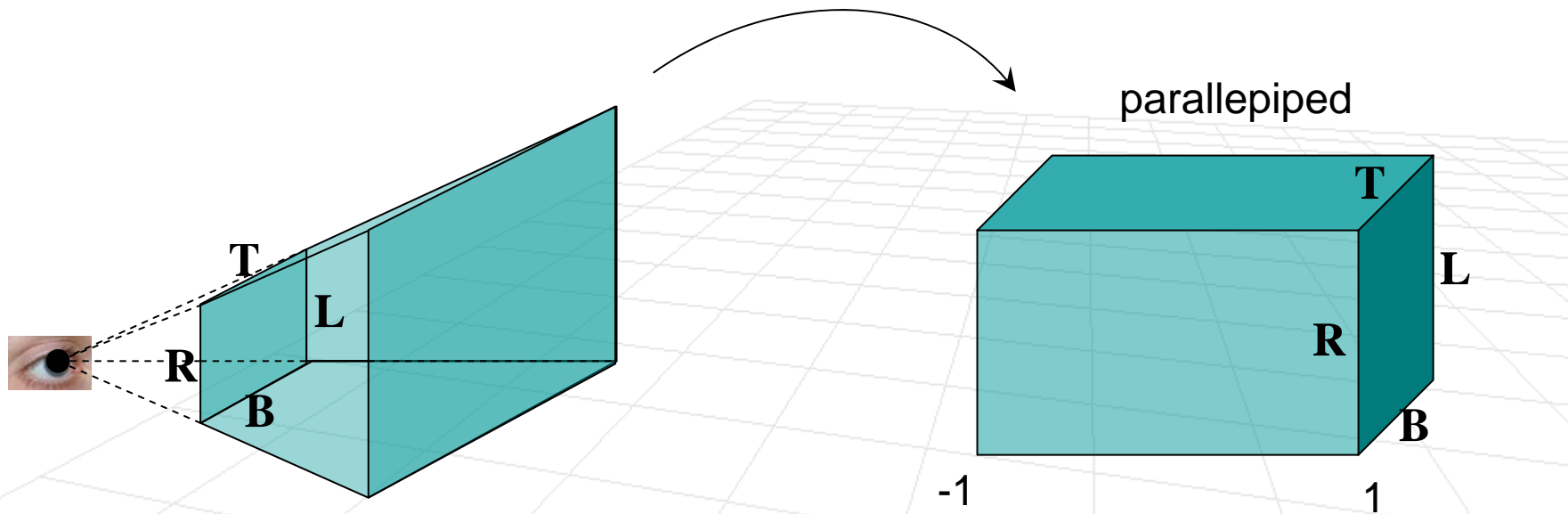
$$\frac{1}{2} \tan(\alpha) = \frac{1/2(\mathbf{T}-\mathbf{B})}{\mathbf{f}}$$



View Volume

- What does homogeneous perspective projection do to our view volume?

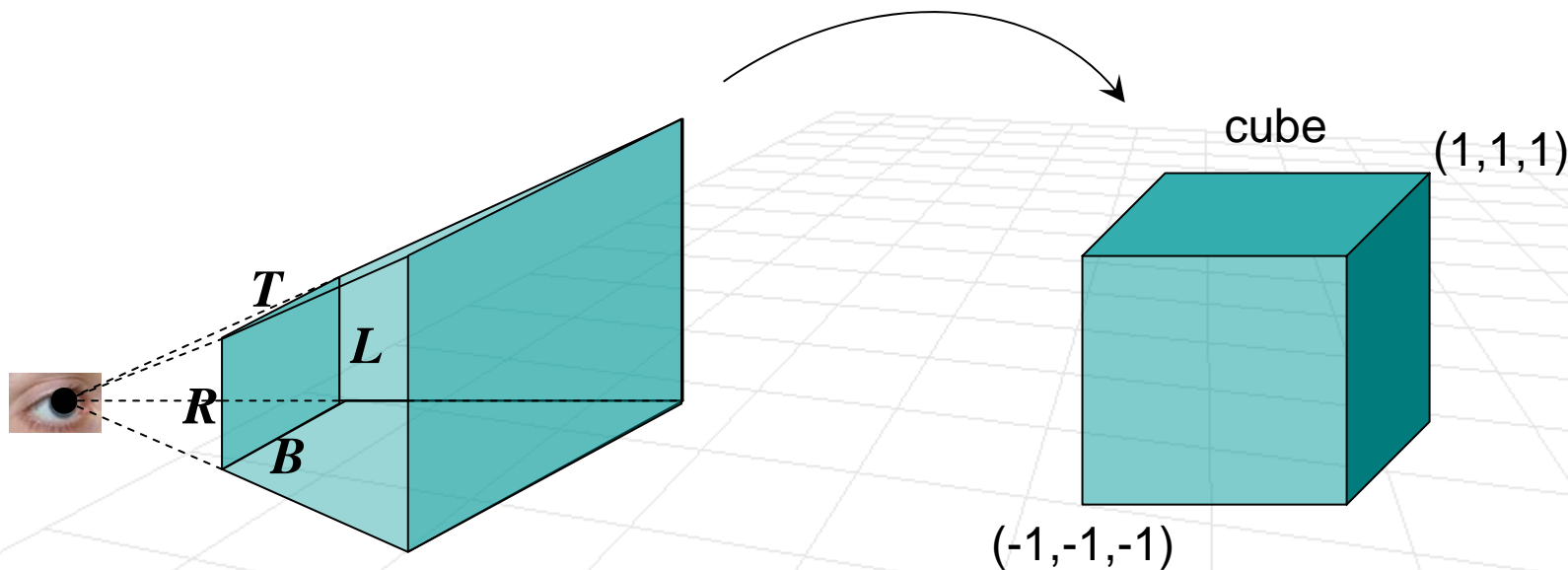
$$\mathbf{M}_p = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \frac{2F}{\mathbf{f} - \mathbf{F}} & -\frac{1}{\mathbf{f}} \left(\frac{\mathbf{f} + \mathbf{F}}{\mathbf{f} - \mathbf{F}} \right) \\ 0 & 0 & 1/\mathbf{f} & 0 \end{bmatrix}$$



Canonical View Volume

- Can we alter homogeneous perspective projection to help us clip?

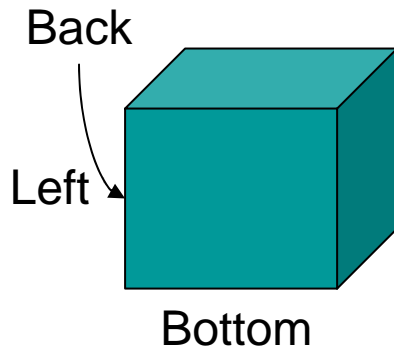
$$\mathbf{M}_p = \begin{bmatrix} \frac{2}{\mathbf{R}-\mathbf{L}} & 0 & \frac{\mathbf{R}+\mathbf{L}}{\mathbf{R}-\mathbf{L}} & 0 \\ 0 & \frac{2}{\mathbf{T}-\mathbf{B}} & \frac{\mathbf{T}+\mathbf{B}}{\mathbf{T}-\mathbf{B}} & 0 \\ 0 & 0 & \frac{2\mathbf{F}}{\mathbf{f}-\mathbf{F}} & -\frac{1}{\mathbf{f}}\left(\frac{\mathbf{f}+\mathbf{F}}{\mathbf{f}-\mathbf{F}}\right) \\ 0 & 0 & 1/\mathbf{f} & 0 \end{bmatrix}$$



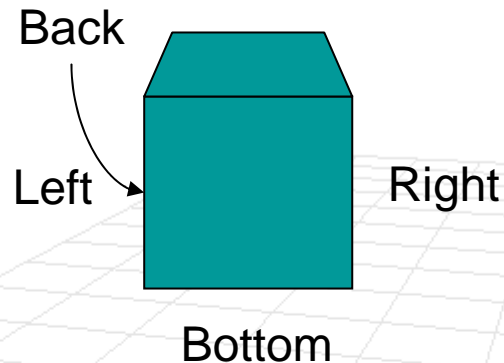
Back-face Removal

- **Idea:** Remove surface patches that point away from the camera (like backside of the object as it viewed from the front)
- Consider a cube

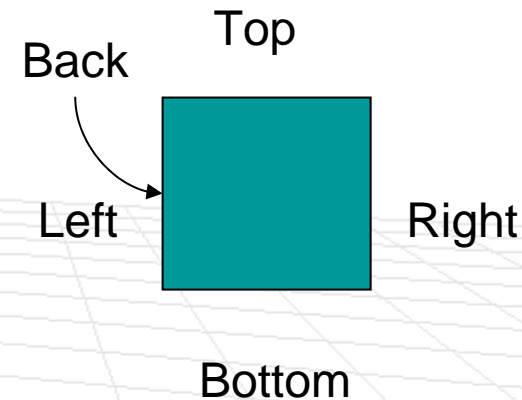
3 Back Faces



4 Back Faces



5 Back Faces

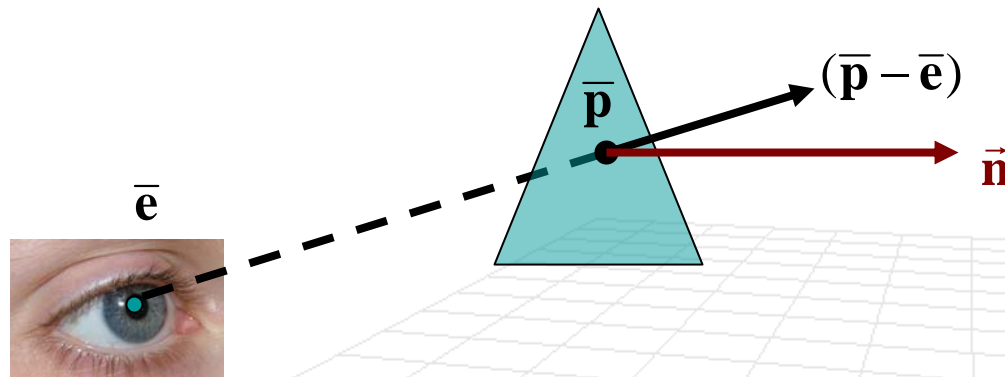


We only need to render at most half of the sides depending on the view

Back-face Removal

- How do we know if the patch (triangle) points away from the camera?

Consider a normal of the patch (triangle)

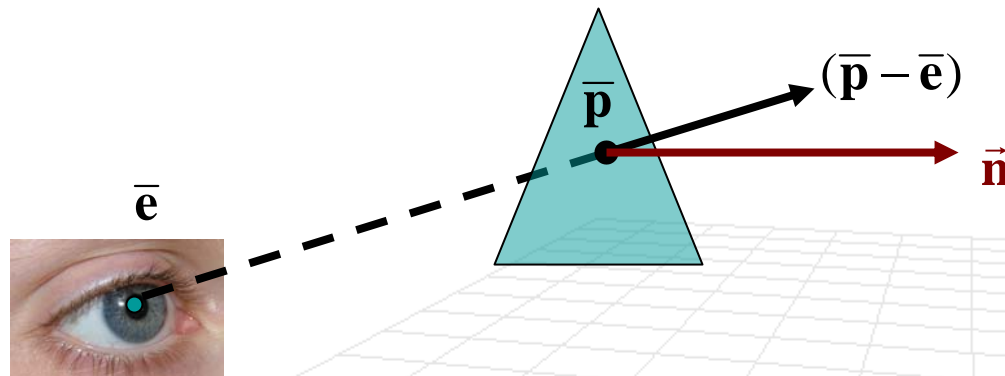


- If $(\bar{\mathbf{p}} - \bar{\mathbf{e}}) \cdot \vec{\mathbf{n}} > 0$ then triangle is part of the back-face and needs to be removed
- If $(\bar{\mathbf{p}} - \bar{\mathbf{e}}) \cdot \vec{\mathbf{n}} < 0$ then triangle **may** be visible

Back-face Removal

- Does it matter which point we consider on the patch?
 - Not if this is a **planar** patch

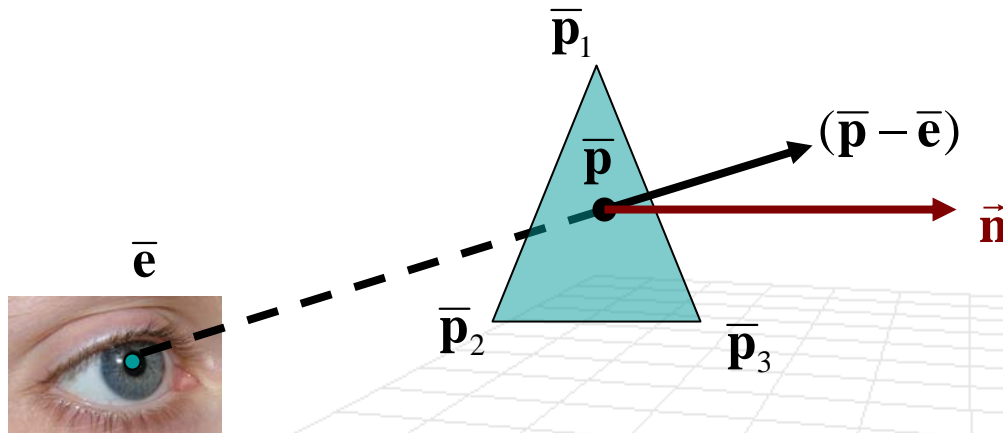
Consider a normal of the patch (triangle)



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Back-face Removal

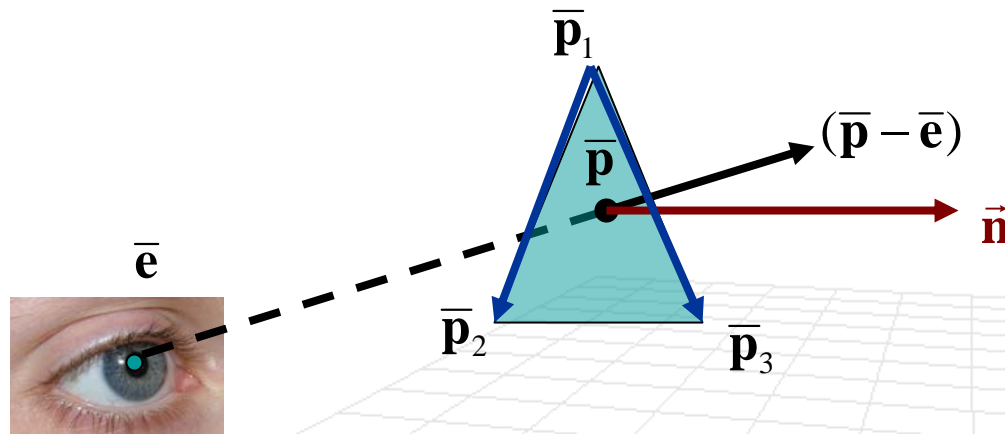
- Does it matter which point we consider on the patch?
 - Not if this is a **planar** patch
- How do we compute \vec{n}
 - If $\bar{p}_1, \bar{p}_2, \bar{p}_3$ are patch vertices in CCW order



- If $(\bar{p} - \bar{e}) \cdot \vec{n} > 0$ then triangle is part of the back-face and needs to be removed
- If $(\bar{p} - \bar{e}) \cdot \vec{n} < 0$ then triangle **may** be visible

Back-face Removal

- Does it matter which point we consider on the patch?
 - Not if this is a **planar** patch
- How do we compute $\vec{n} = \frac{(\bar{\mathbf{p}}_2 - \bar{\mathbf{p}}_1) \times (\bar{\mathbf{p}}_3 - \bar{\mathbf{p}}_1)}{\|(\bar{\mathbf{p}}_2 - \bar{\mathbf{p}}_1) \times (\bar{\mathbf{p}}_3 - \bar{\mathbf{p}}_1)\|}$



- If $(\bar{\mathbf{p}} - \bar{\mathbf{e}}) \cdot \vec{n} > 0$ then triangle is part of the back-face and needs to be removed
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Z-Buffer (a.k.a Depth Buffer)

- We have a **frame-buffer** (this is where an image that we see on the screen is stored)
- We also have a **z-buffer** that keeps track of the z^* coordinate for every pixel in the frame-buffer
- To draw point in the world with color c that projects to (x^*, y^*, z^*) we can execute the following algorithm

```
if  $z^* < z\text{-buffer}(x^*, y^*)$  then  
    frame-buffer( $x^*, y^*$ ) =  $c$   
    z-buffer( $x^*, y^*$ ) =  $z^*$   
end
```

Z-Buffer (a.k.a Depth Buffer)

- We need to initialize the z-buffer with some value. What is the good value to initialize with?
 - If we are using canonical view volume then 1 would work
- To draw point in the world with color \mathbf{c} that projects to $(\mathbf{x}^*, \mathbf{y}^*, \mathbf{z}^*)$ we can execute the following algorithm

```
if  $\mathbf{z}^* < \text{z-buffer}(\mathbf{x}^*, \mathbf{y}^*)$  then  
    frame-buffer( $\mathbf{x}^*, \mathbf{y}^*$ ) =  $\mathbf{c}$   
    z-buffer( $\mathbf{x}^*, \mathbf{y}^*$ ) =  $\mathbf{z}^*$   
end
```

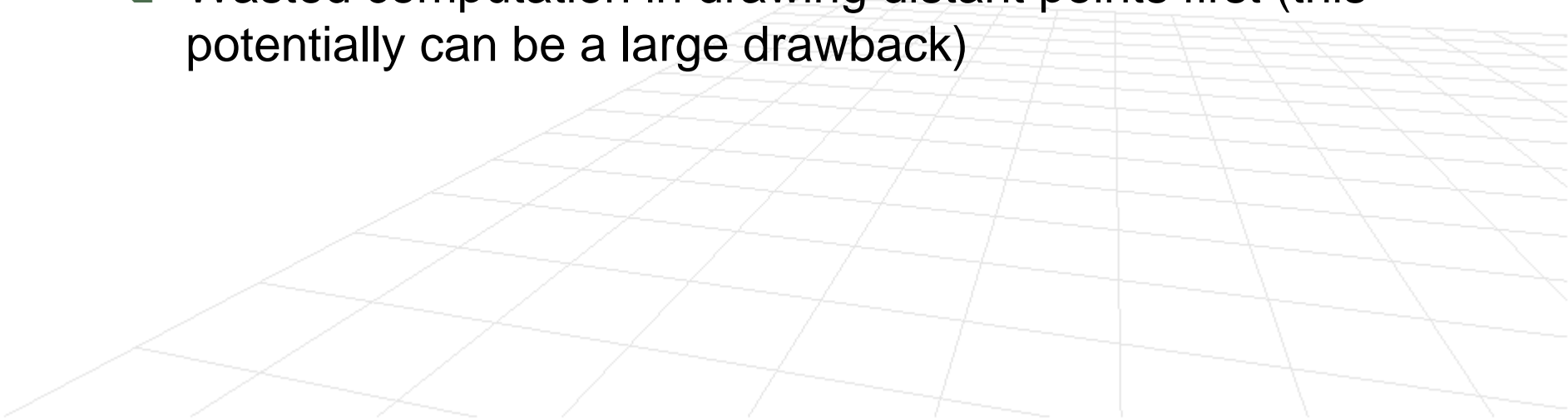
Z-Buffer (a.k.a Depth Buffer)

■ Advantages of Z-buffering

- Simple and accurate
- Independent of the order the polygons are drawn

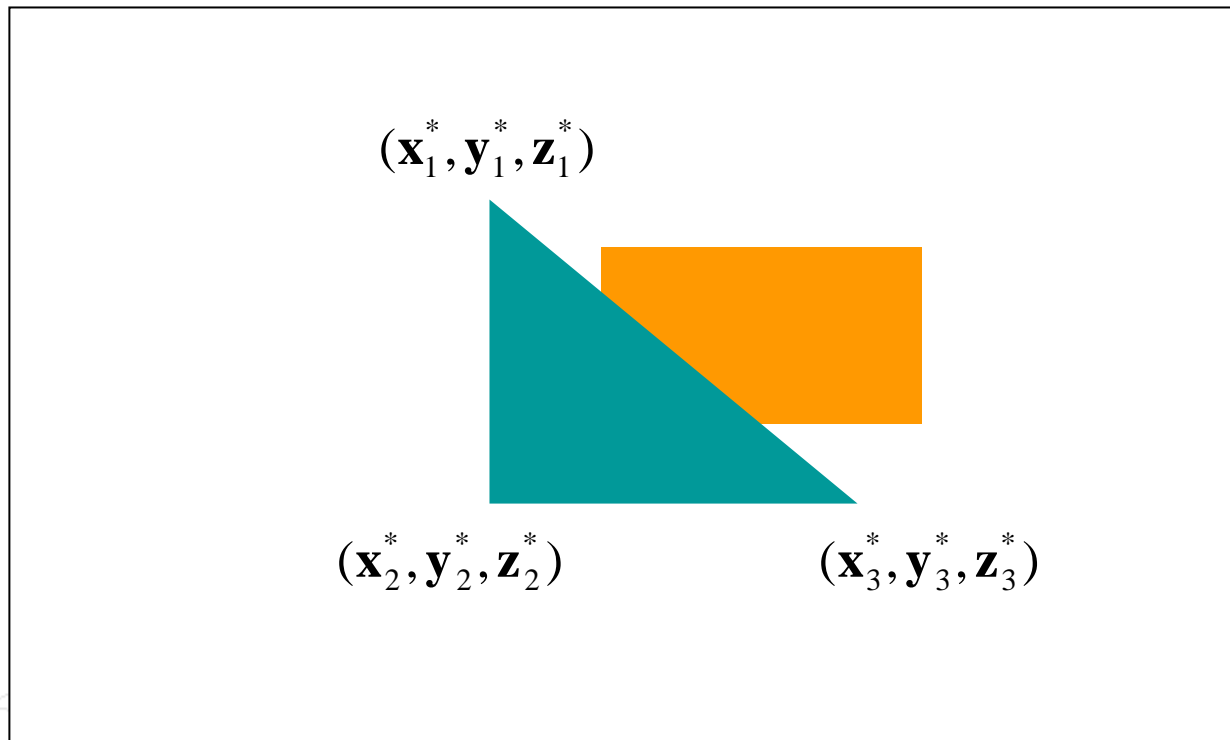
■ Disadvantages of Z-buffering

- Memory for a Z-buffer (small consideration)
- Wasted computation in drawing distant points first (this potentially can be a large drawback)



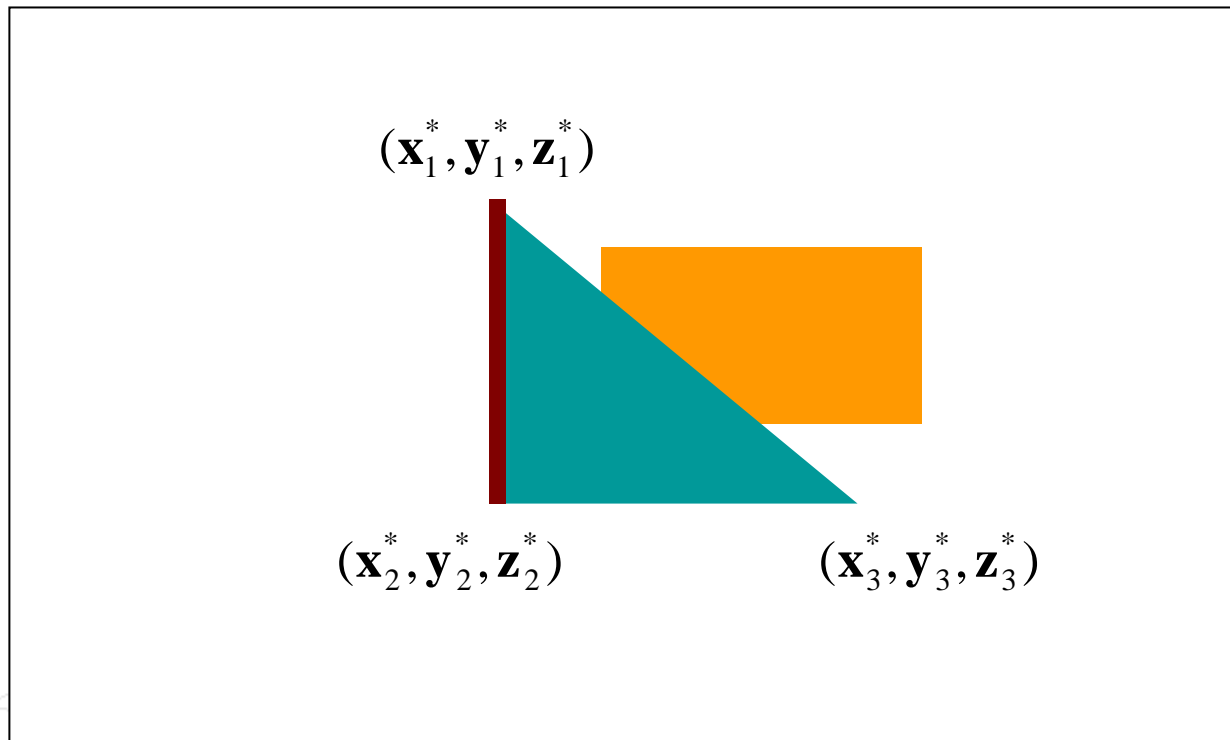
Z-Buffer (a.k.a Depth Buffer)

- We represent a patch using vertices
- How do we get a pseudodepth and proper rendering everywhere else?



Z-Buffer (a.k.a Depth Buffer)

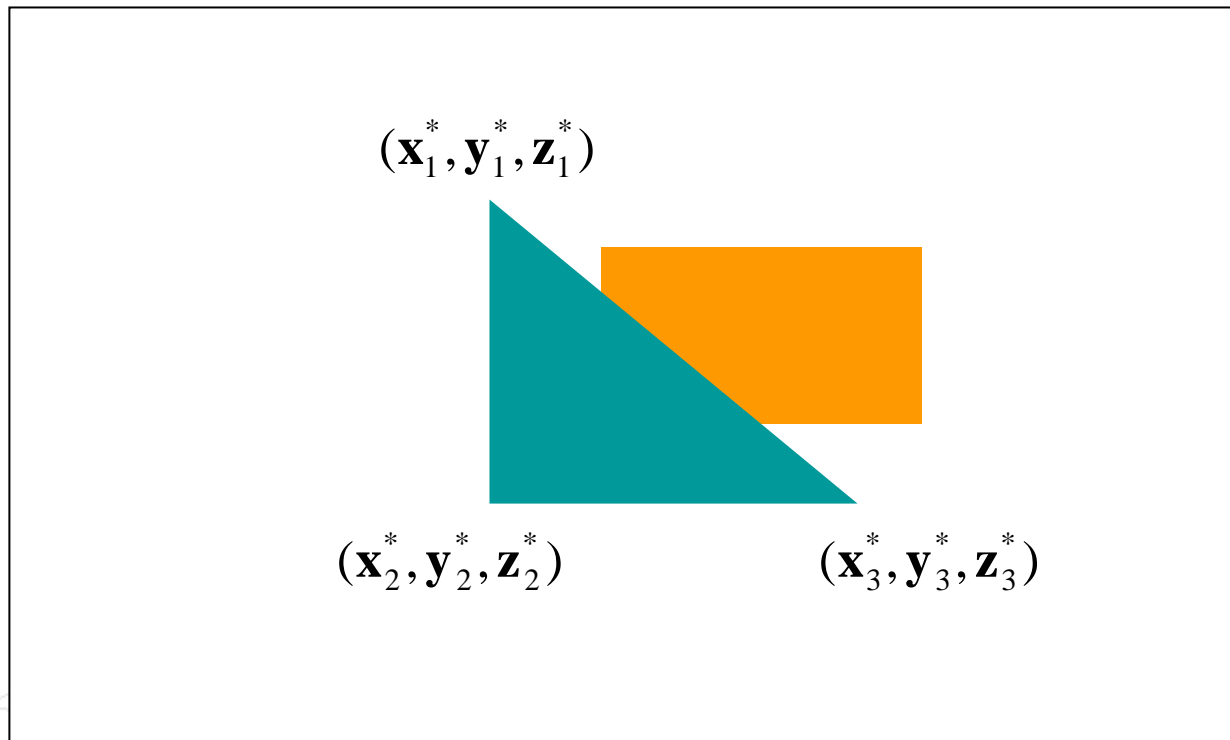
- We represent a patch using vertices
- How do we get a pseudodepth and proper rendering everywhere else?



Linearly interpolate \mathbf{z}^* along a scan line

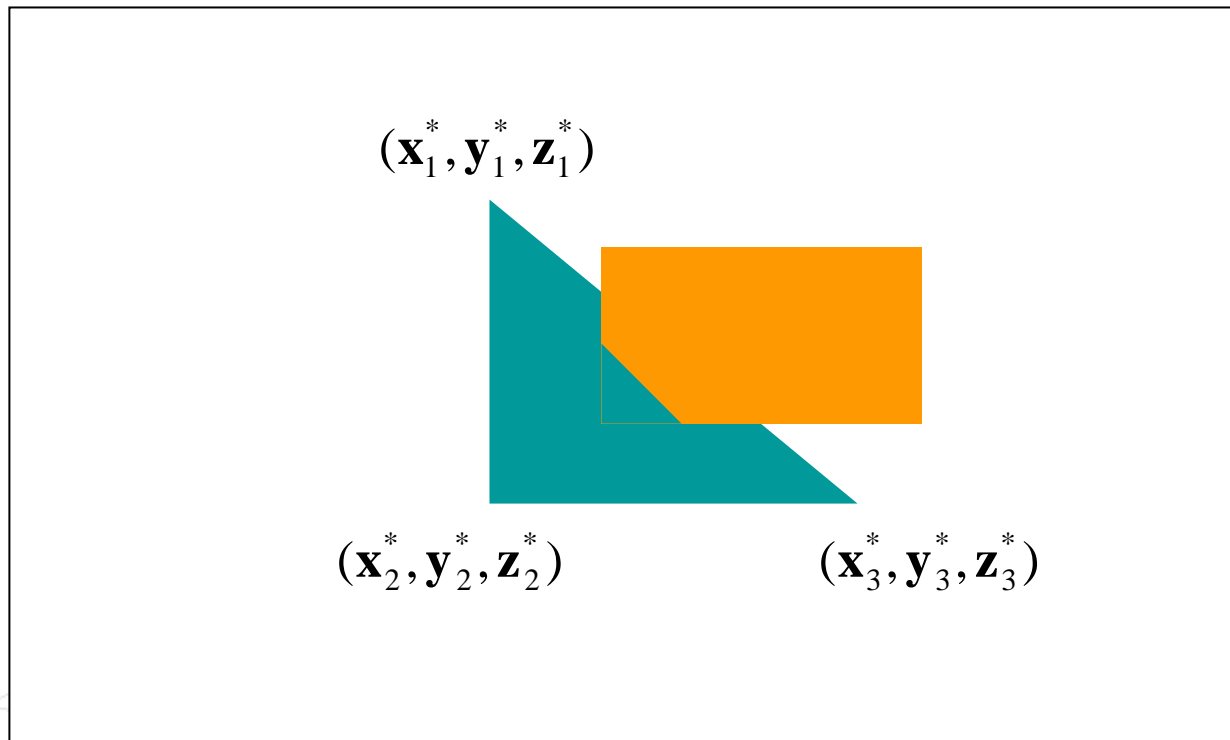
Painter's Algorithm

- **Idea:** Order the patches and draw them in the order of depth (with most distant patches first)
 - This is an alternative to Z-buffering



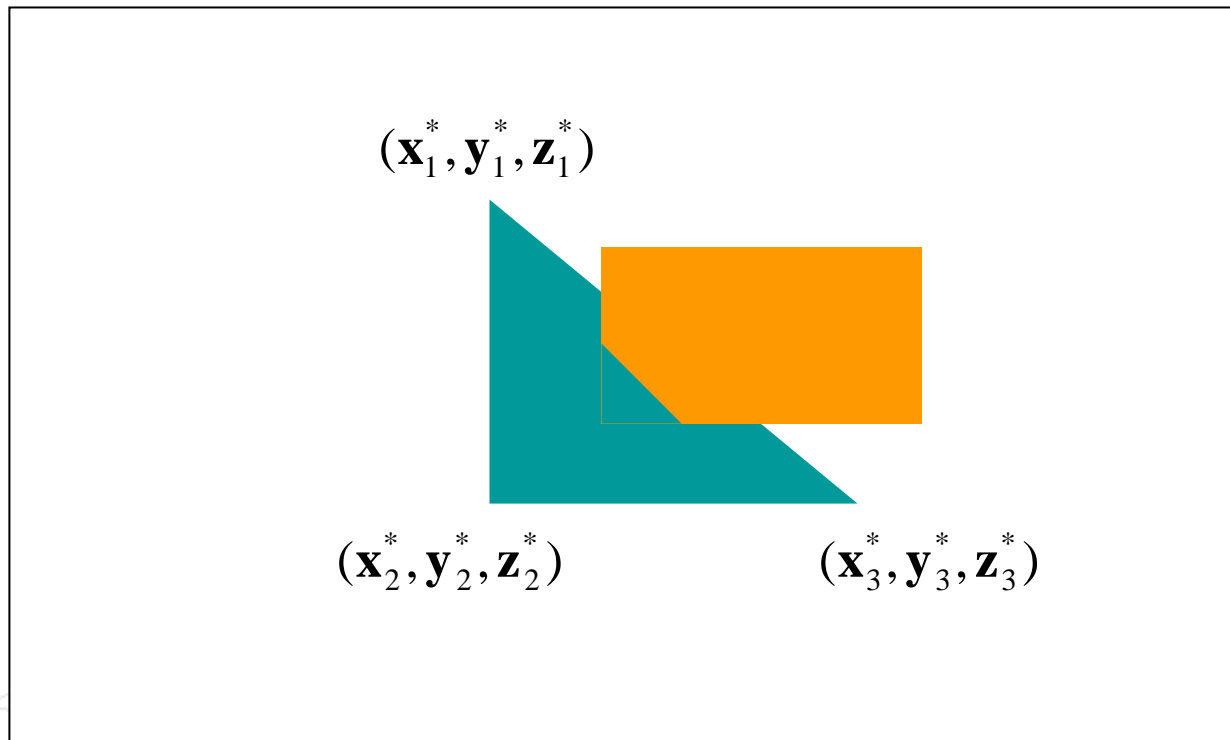
Painter's Algorithm

- How do we deal with intersecting patches?
 - Break patches into smaller patches



BSP Trees

- **Binary space partition tree** (BSP tree) is an algorithm for making back-to-front ordering of polygons efficient and to break polygons to avoid intersections



BSP Tree

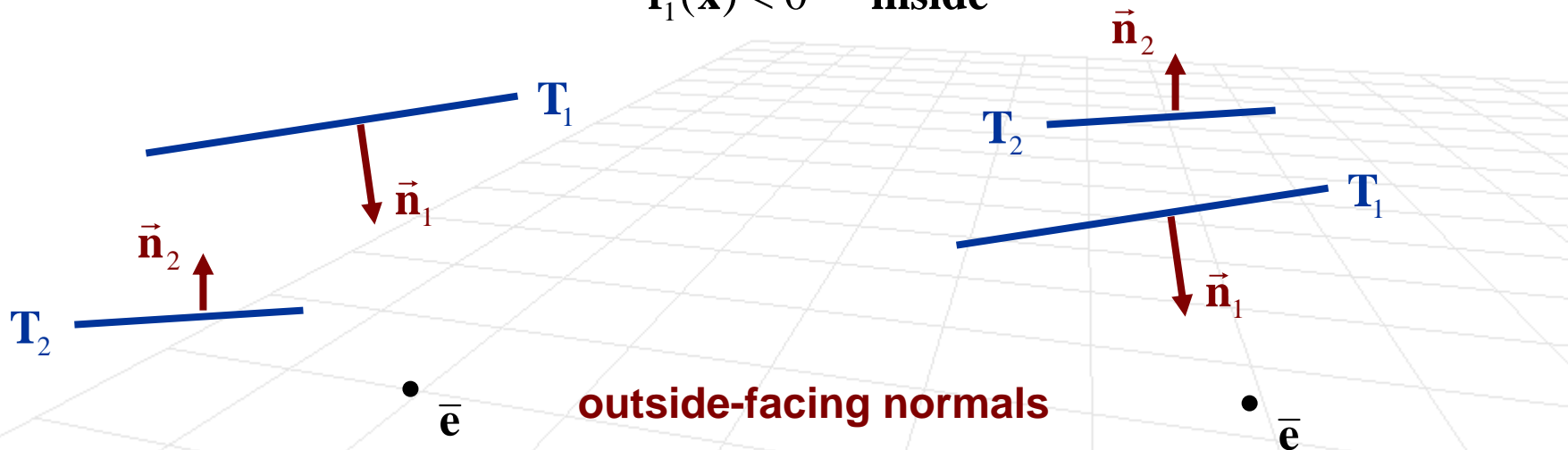
- If \bar{e} and T_2 on the same side of T_1 (left) then draw T_1 first then T_2
- If \bar{e} and T_2 are on different sides of T_1 (right) then draw T_2 first then T_1
- How do we know if points are on the same side?

$$f_1(\bar{x}) = (\bar{x} - \bar{p}_1) \cdot \vec{n}_1$$

$$f_1(\bar{x}) = 0 \quad \text{on the plane}$$

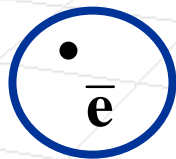
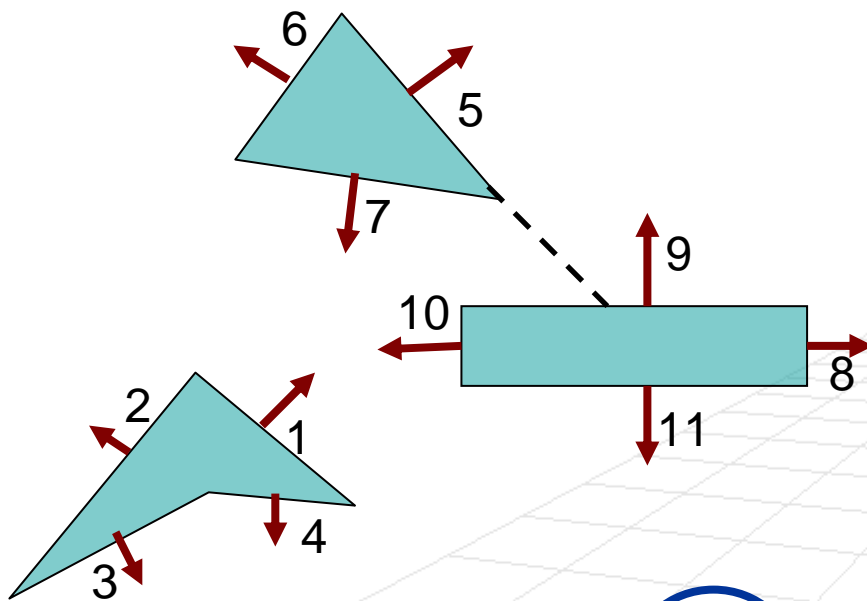
$$f_1(\bar{x}) > 0 \quad \text{"outside"}$$

$$f_1(\bar{x}) < 0 \quad \text{"inside"}$$



BSP Tree Example

- Let's try building a BSP tree for this scene



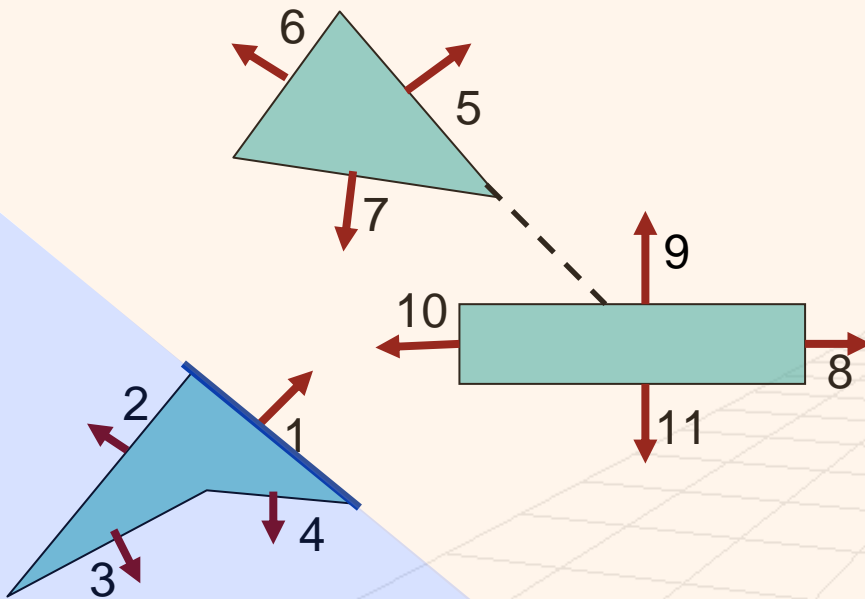
The tree will be the same regardless of the camera placement

BSP Tree Example

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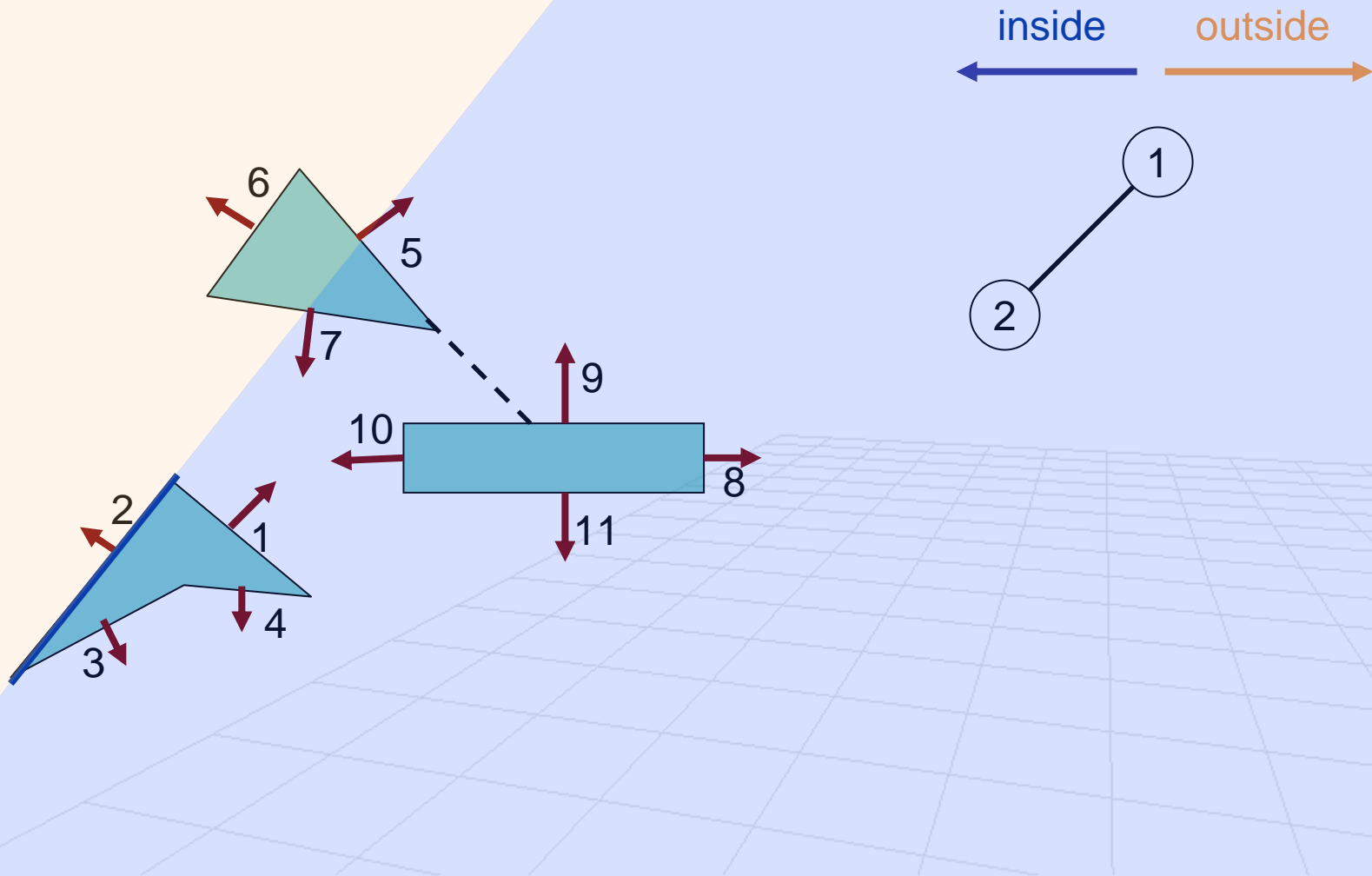


①



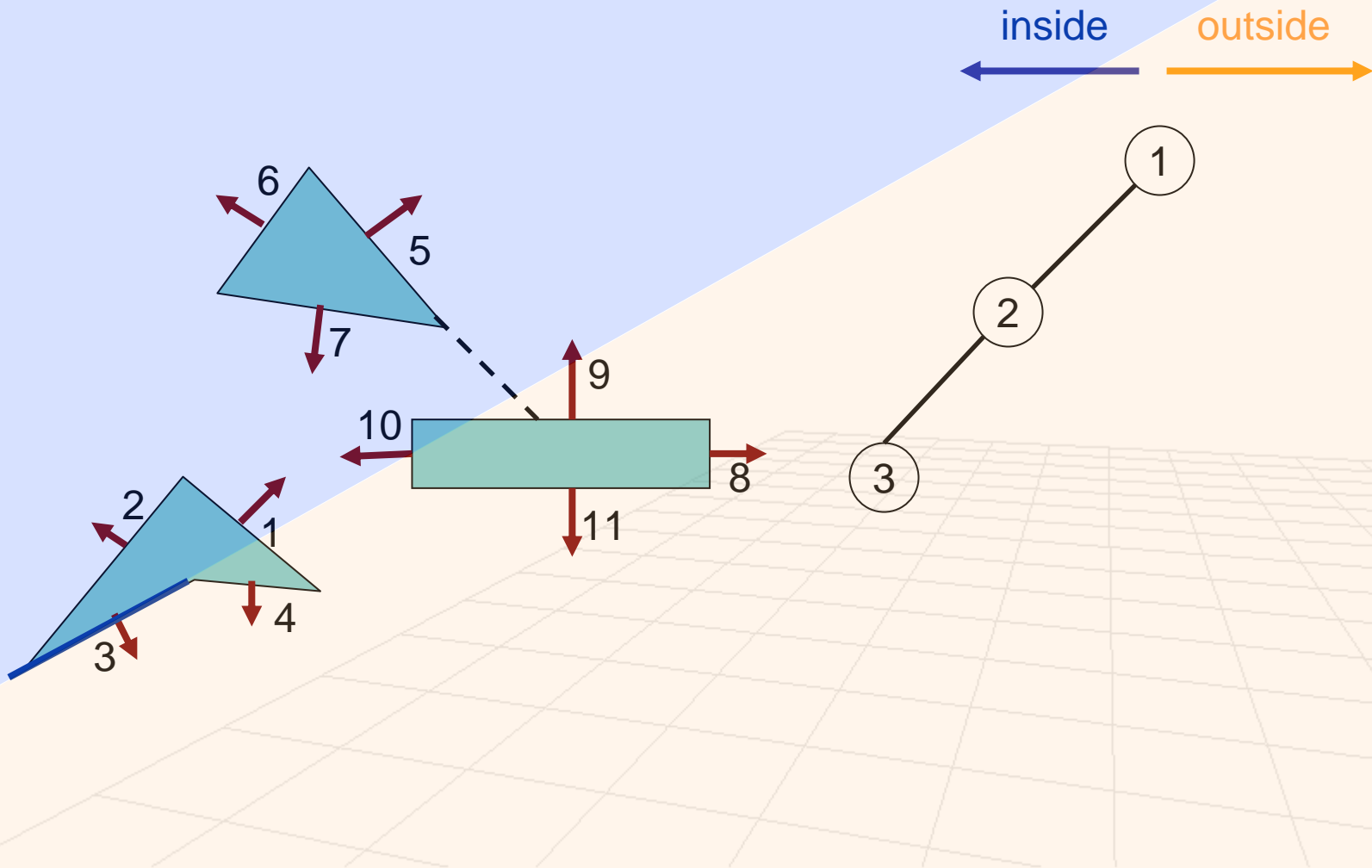
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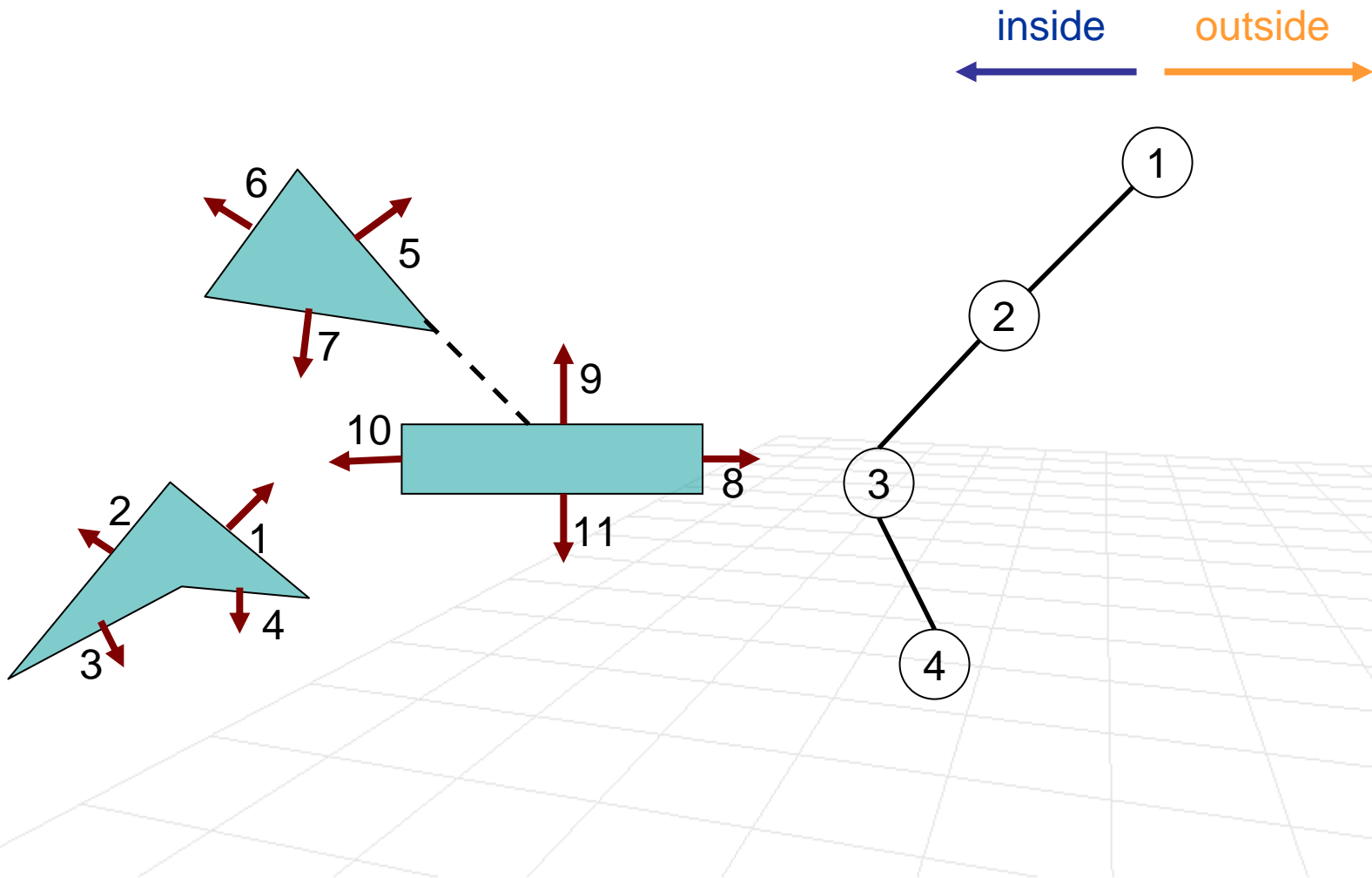
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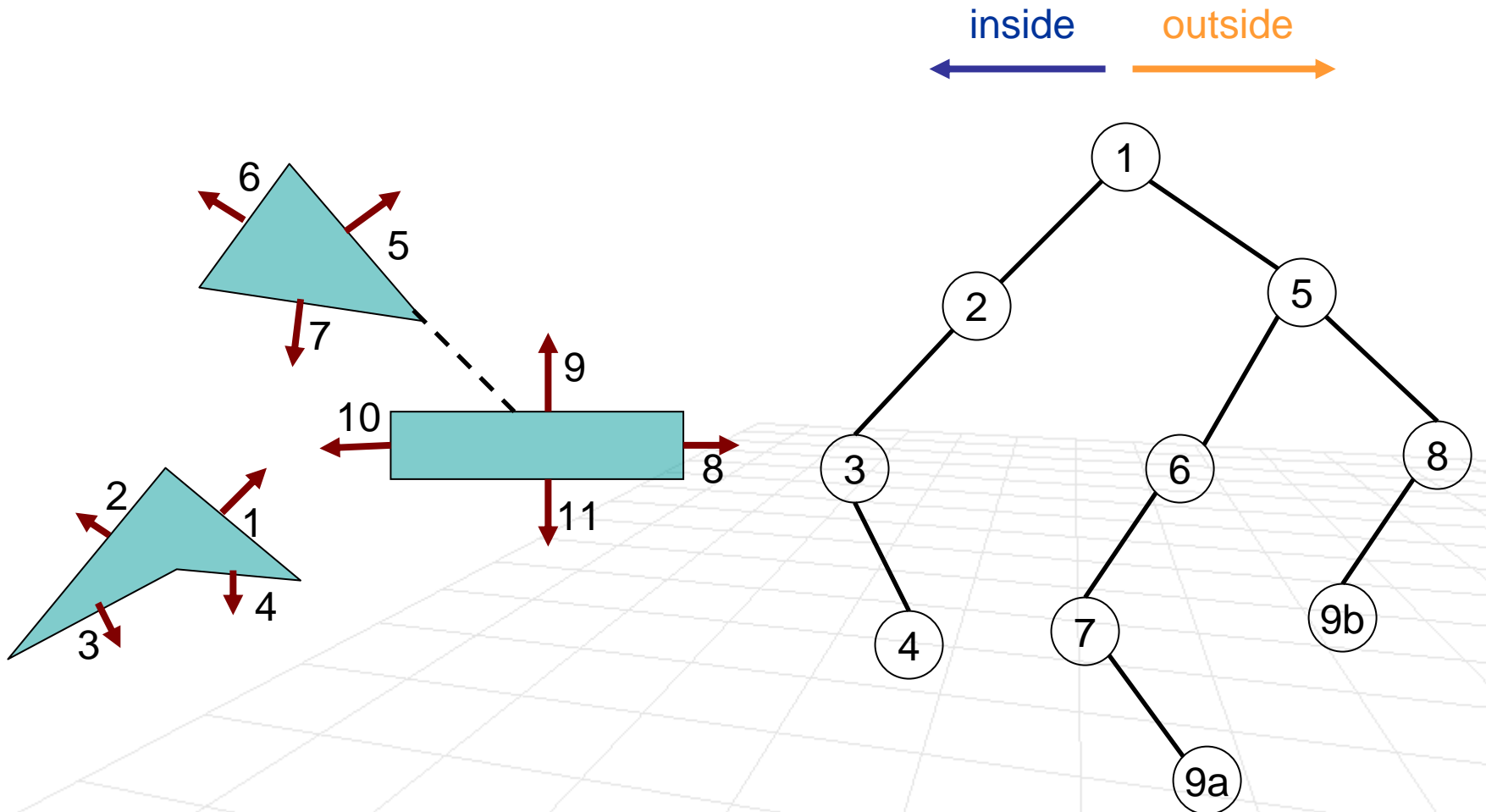
BSP Tree Example

- Let's try building a BSP tree for this scene



BSP Tree Example

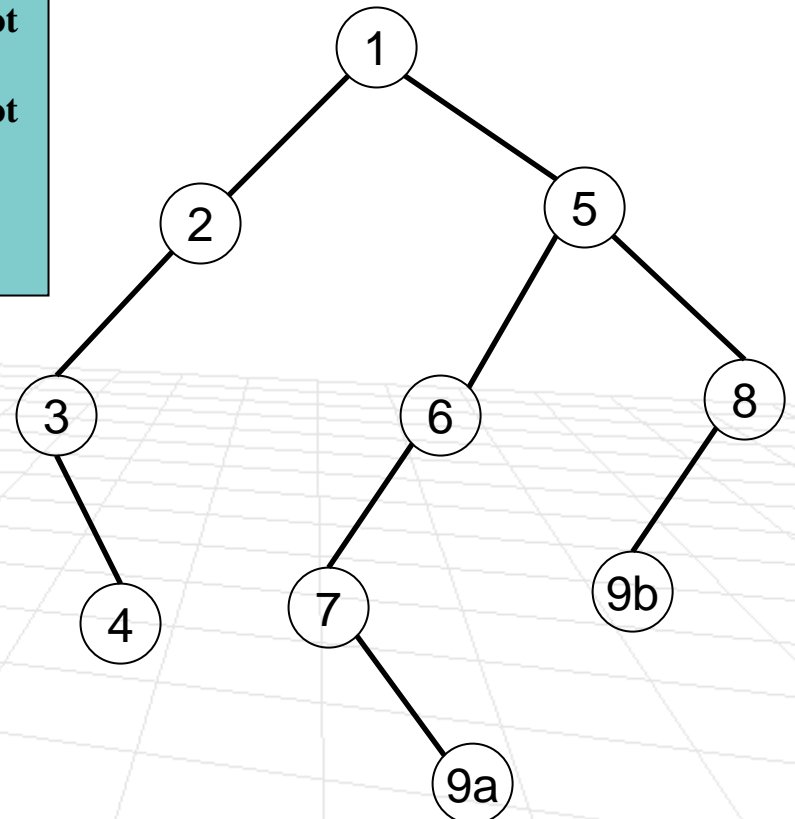
- Let's try building a BSP tree for this scene



BSP Tree Traversal

- Tree traversal algorithm

if eye in the outside half-space of the root
 Draw faces on inside sub-tree of the root
 Draw the root
else
 Draw faces is the outside of sub-tree of the root
 Draw the root
 Draw faces on inside sub-tree of the root
end



- Easy to modify to do back-face removal

BSP Tree

■ Advantages

- Can easily discard portions of the scene behind the camera
- Artifacts of z-buffer quantization are not seen
- Tree construction fixed for the static scenes

■ Disadvantages

- How can we handle dynamic scenes?

This is what is typically done in games, because it's fast

