

THE UNIVERSITY OF BRITISH COLUMBIA

Topics in AI (CPSC 532S): **Multimodal Learning with Vision, Language and Sound**

Lecture 9: RNNs (part 2)



Course Logistics

- Assignment 3 due date is Wednesday
- Assignment 1 solutions are out, being graded
- Assignment 2 solutions will be graded and out soon

- Course **Projects**

Start thinking of ideas and forming groups

Survey topic discussion

Student assignment survey will be up by the end of the week

Review: One Hot Encoding

Vocabulary

dog

cat

person

holding

tree

computer

using

*slide from V. Ordonex

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Review: One Hot Encoding

Vocabulary

- dog 1
- cat 2
- person 3
- holding 4
- tree 5
- computer 6
- using 7

*slide from V. Ordonex

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Review: One Hot Encoding

Vocabulary

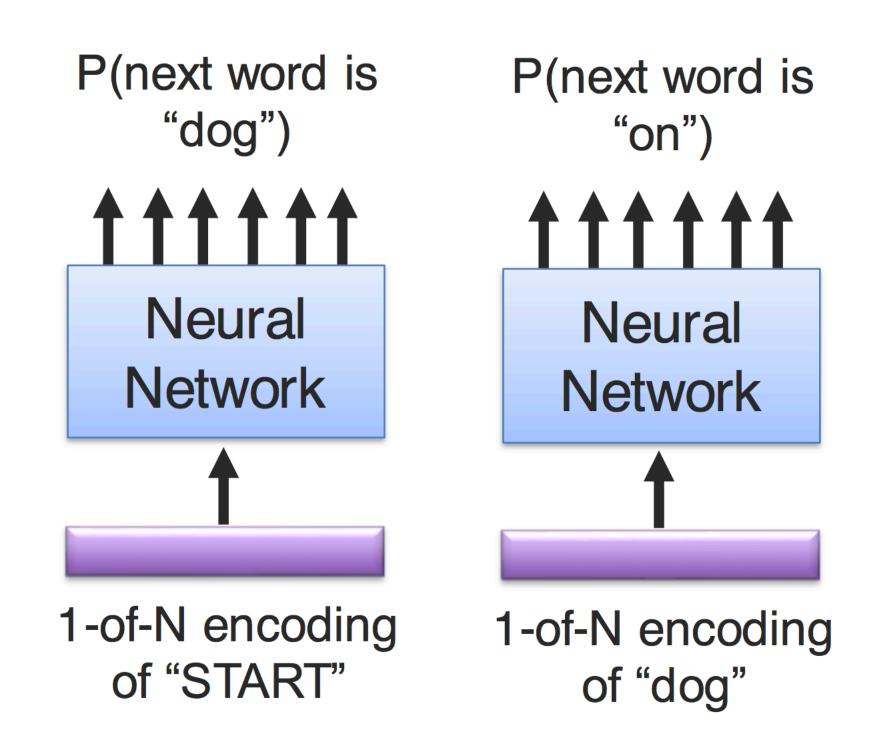
- dog 1
- cat 2
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- holding 4
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- computer 6
- using 7

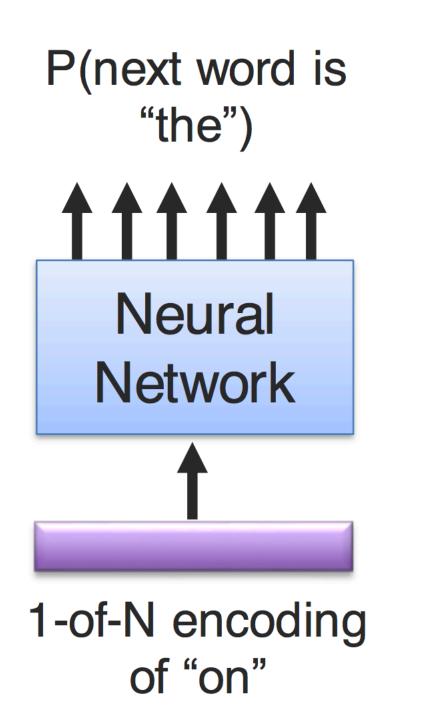
one-hot encodings

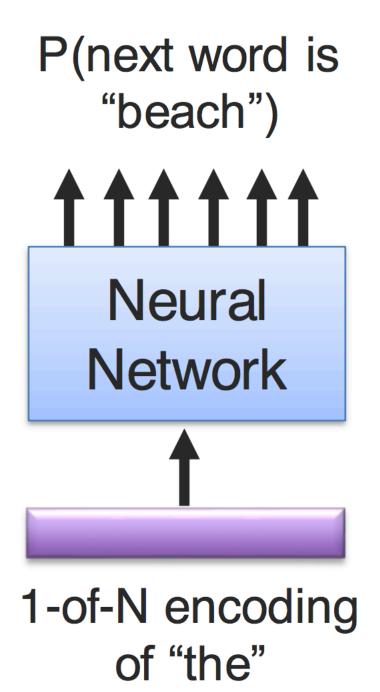
[1, 0, 0, 0, 0, 0, 0, 0, 0, 0] [0, 1, 0, 0, 0, 0, 0, 0, 0, 0][0, 0, 1, 0, 0, 0, 0, 0, 0, 0][0, 0, 0, 1, 0, 0, 0, 0, 0][0, 0, 0, 0, 1, 0, 0, 0, 0][0, 0, 0, 0, 0, 1, 0, 0, 0][0,0,0,0,0,0,1,0,0]

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Review: Neural-based Language Mode

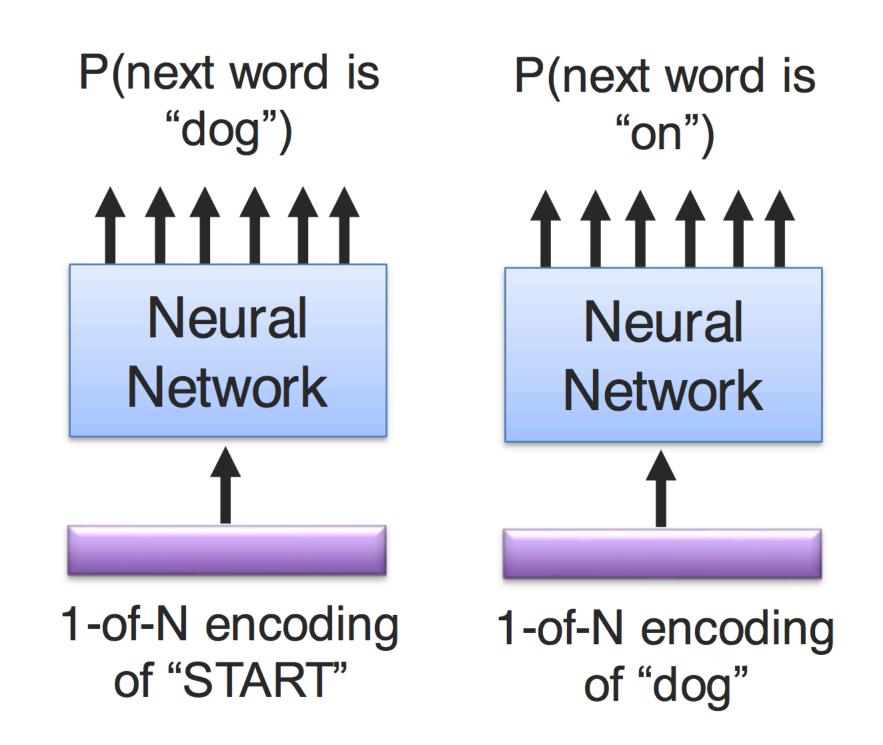


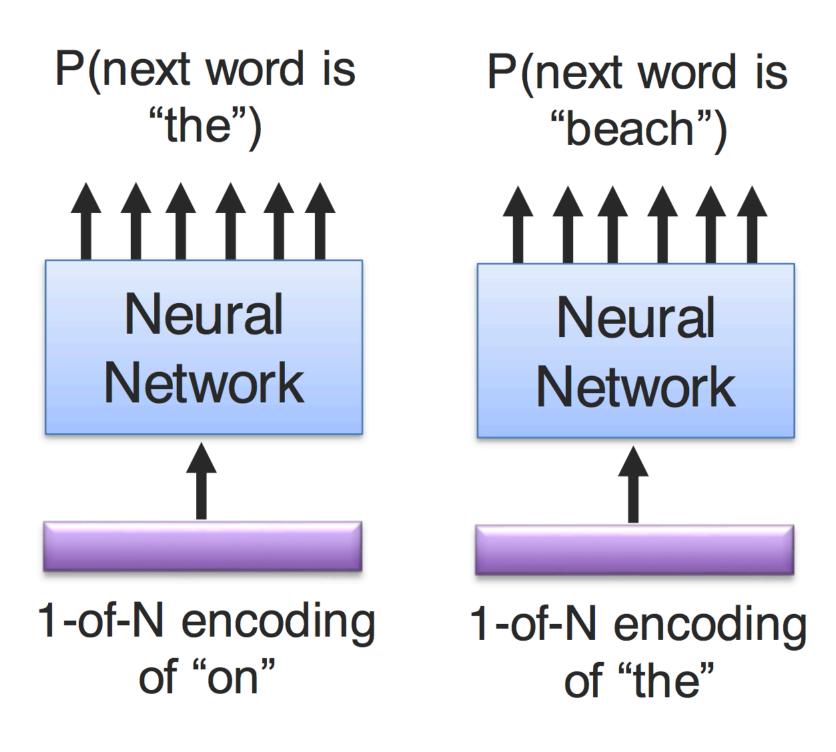




* Slides from Louis-Philippe Morency

Review: Neural-based Language Mode

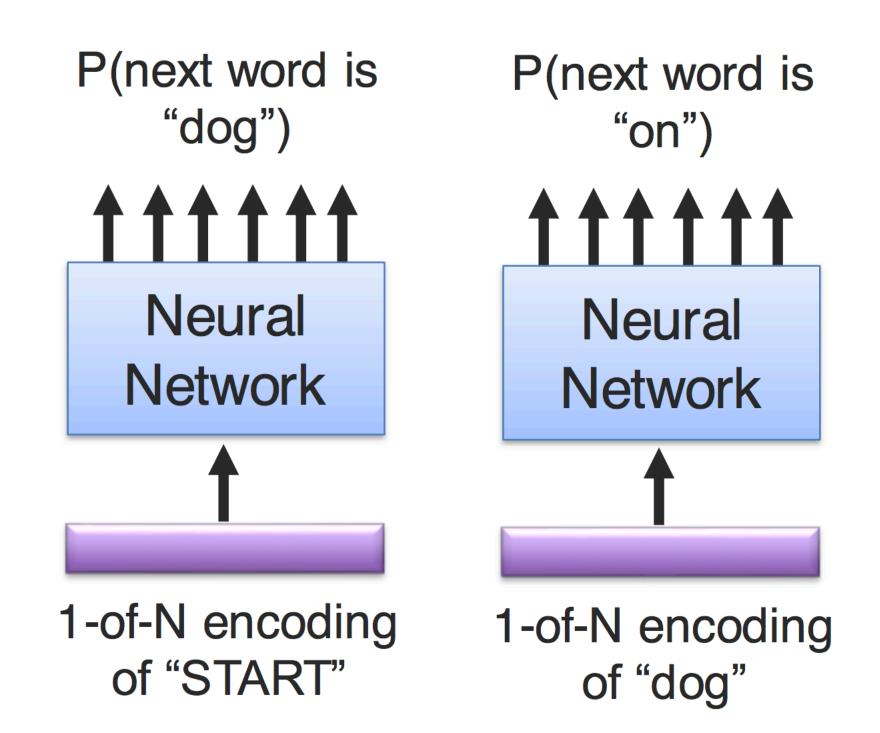




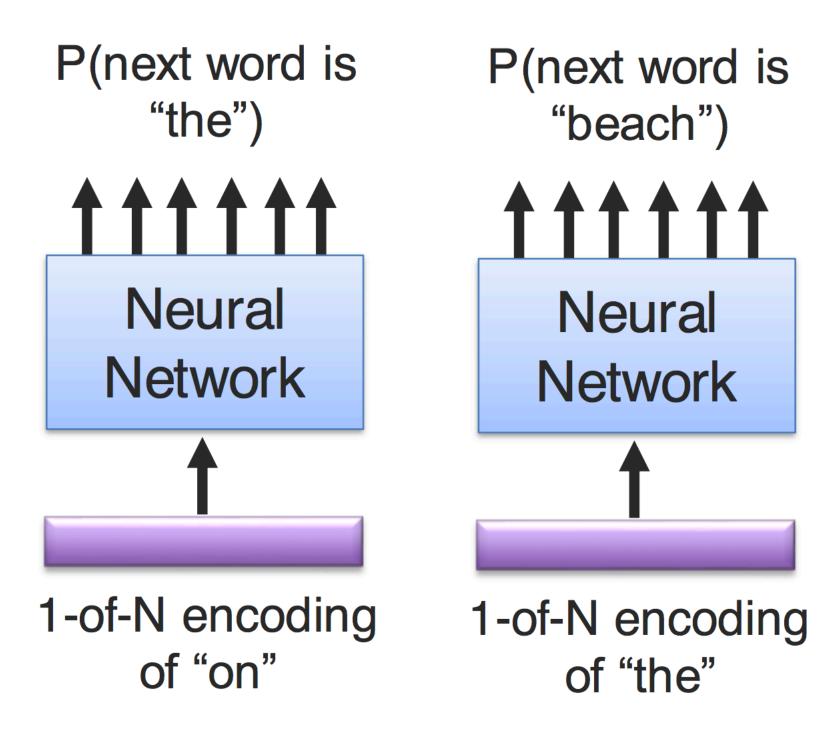
Problem: Does not model sequential information (too local)

* Slides from Louis-Philippe Morency

Review: Neural-based Language Mode



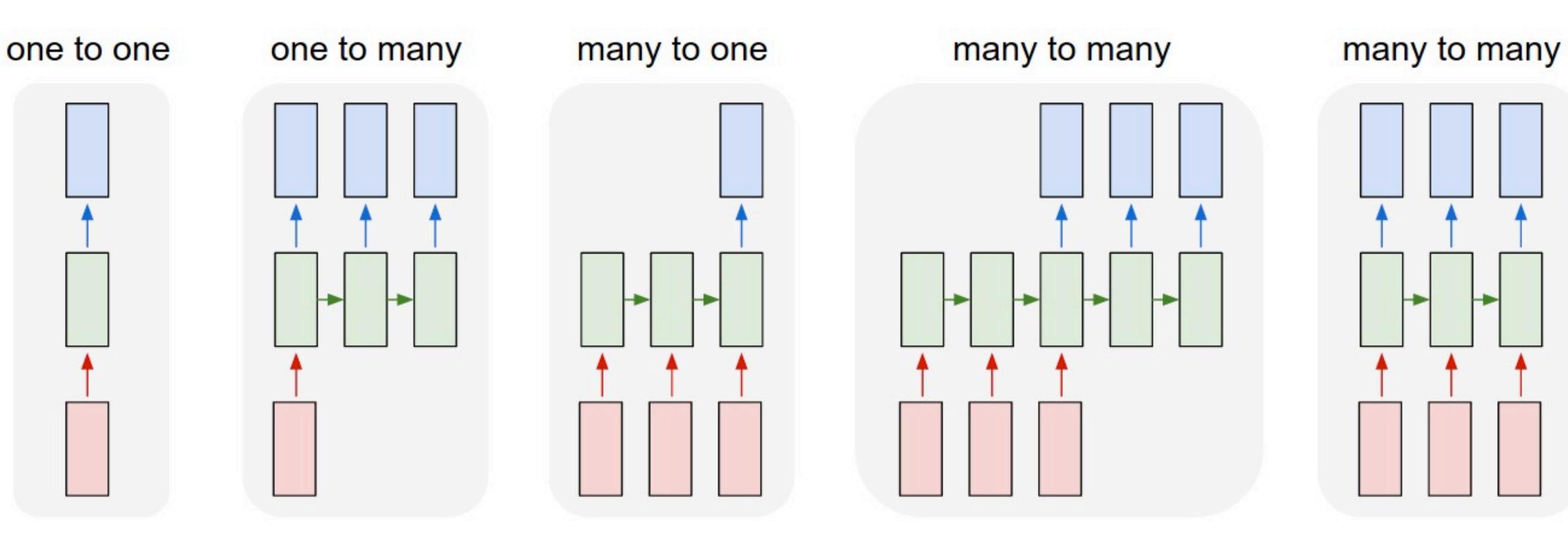
We need sequence modeling!



Problem: Does not model sequential information (too local)

* Slides from Louis-Philippe Morency

Review: Sequences Models



Input: No sequence Output: No seq.

Example:

"standard" classification / regression problems

Input: No sequence **Output:** Sequence **Example:** Im₂Caption

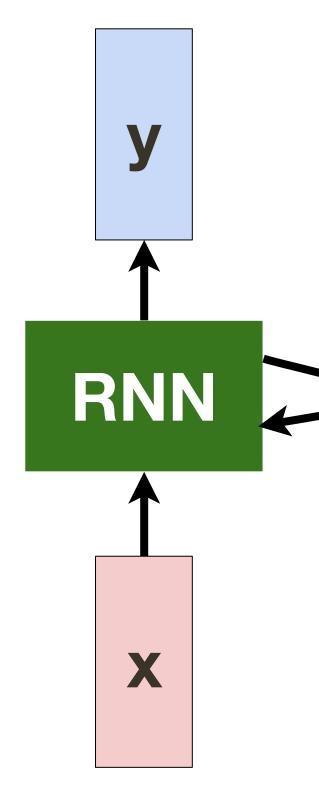
Input: Sequence Output: No seq. **Example:** sentence classification, multiple-choice question answering

Input: Sequence **Output:** Sequence

Example: machine translation, video captioning, open-ended question answering, video question answering



$h_t = f_W(h_{t-1}, x_t)$





$h_{t} = f_{W}(h_{t-1}, x_{t})$ $h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$

* slide from Fei-Dei Li, Justin Johnson, Serena Yeung, cs231n Stanford



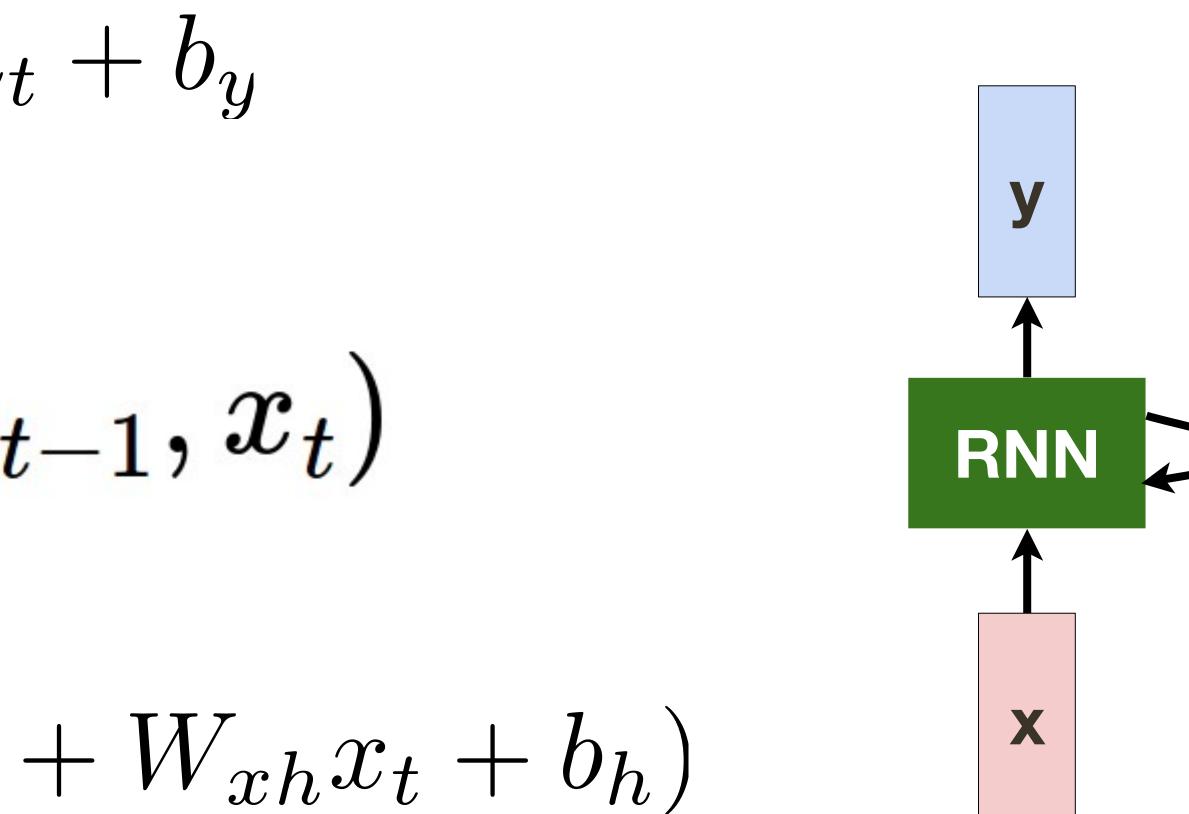
V

RNN

X

$y_t = W_{hy}h_t + b_y$

$h_{t} = f_{W}(h_{t-1}, x_{t})$ $h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$

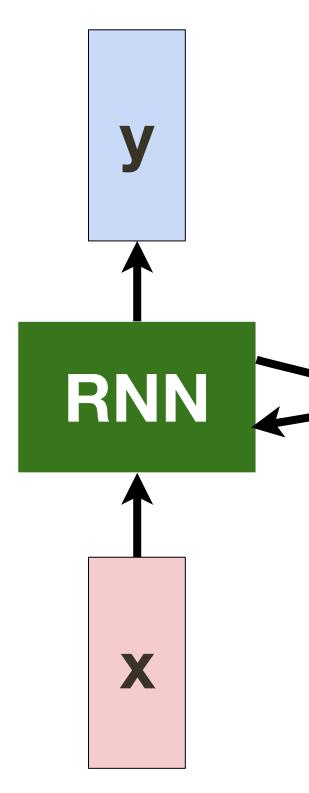




Intuition: RNN incorporates one element of sequence at a time (e.g. letter, word, video frame, etc.) building up a representation of the sequence "so far"

 $h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$



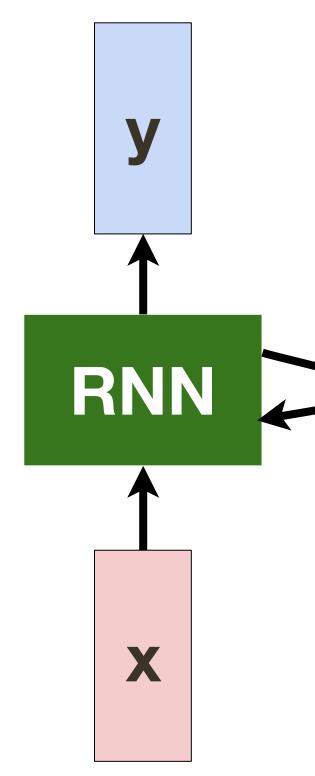


Intuition: RNN incorporates one element of sequence at a time (e.g. letter, word, video frame, etc.) building up a representation of the sequence "so far"

Alternative: RNN computes a representation of sequence element (e.g. letter, word, video frame, etc.) with context provided by all previous processed elements

$$h_t = \tanh(W_{hh}h_{t-1})$$

$$+W_{xh}x_t+b_h$$



Vocabulary

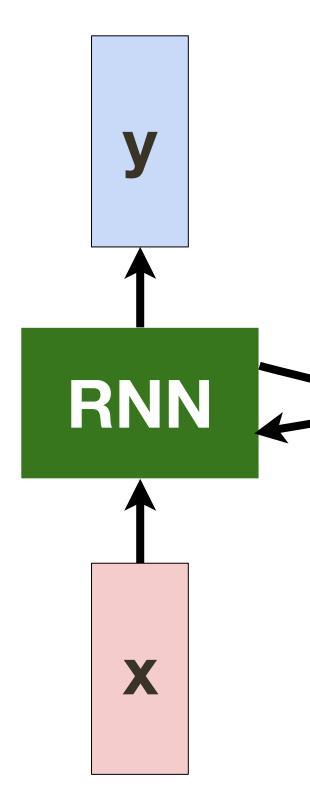
one-hot encodings

dog	1	[1 , 0, 0, 0, 0, 0, 0, 0, 0, 0]
cat	2	[0, 1 , 0, 0, 0, 0, 0, 0, 0, 0]
person	3	[0, 0, 1 , 0, 0, 0, 0, 0, 0, 0]
holding	4	[0,0,0, <mark>1</mark> ,0,0,0,0,0,0]
tree	5	[0,0,0,0, 1 ,0,0,0,0,0]
computer	6	[0,0,0,0,0, <mark>1</mark> ,0,0,0,0]
using	7	[0,0,0,0,0,0,1,0,0,0]

$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$



person holding dog



Vocabulary

one-hot encodings

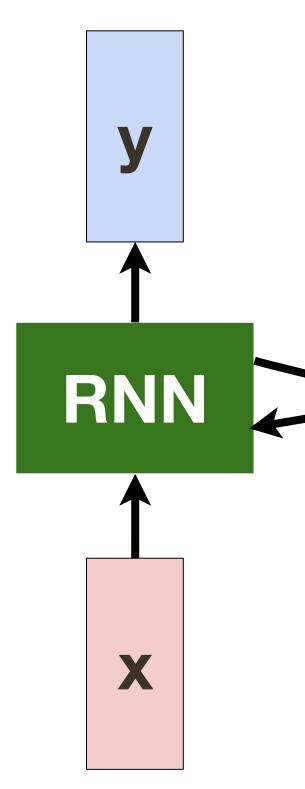
dog	1	[1 , 0, 0, 0, 0, 0, 0, 0, 0, 0]
cat	2	[0, 1 , 0, 0, 0, 0, 0, 0, 0, 0]
person	3	[0, 0, <mark>1</mark> , 0, 0, 0, 0, 0, 0, 0]
holding	4	[0,0,0, <mark>1</mark> ,0,0,0,0,0,0]
tree	5	[0,0,0,0, 1 ,0,0,0,0,0]
computer	6	[0,0,0,0,0, <mark>1</mark> ,0,0,0,0]
using	7	[0,0,0,0,0,0, <mark>1</mark> ,0,0,0]

Identity $h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t +$



person holding dog

Identity zero bh



Vocabulary

one-hot encodings

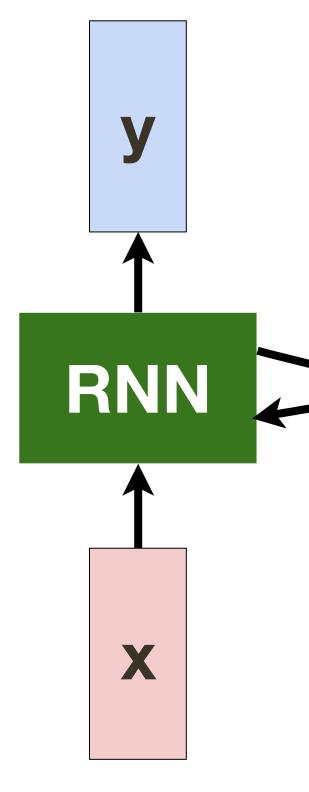
dog	1	[1 , 0, 0, 0, 0, 0, 0, 0, 0, 0]
cat	2	[0, 1 , 0, 0, 0, 0, 0, 0, 0, 0]
person	3	[0, 0, 1 , 0, 0, 0, 0, 0, 0, 0]
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tree	5	[0,0,0,0, 1 ,0,0,0,0,0]
computer	6	[0,0,0,0,0, 1 ,0,0,0,0]
using	7	[0,0,0,0,0,0, <mark>1</mark> ,0,0,0]

Identity $h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t +$

[0,0,0,0,0,0,0,0,0,0]

person holding dog

Identity zero



Vocabulary

one-hot	encodings
---------	-----------

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using	7	[0,0,0,0,0,0, <mark>1</mark> ,0,0,0]

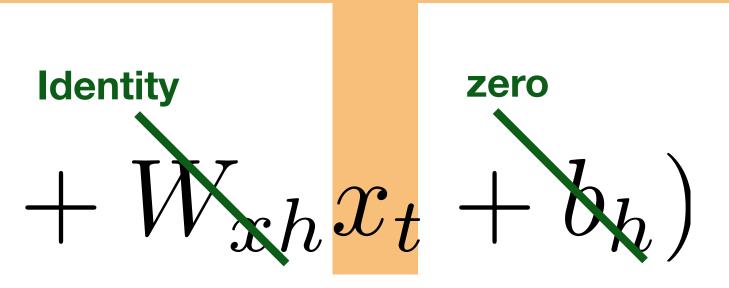
Identity $h_t = \tanh(W_{k,h}h_{t-1} + W_{k,h}x_t)$

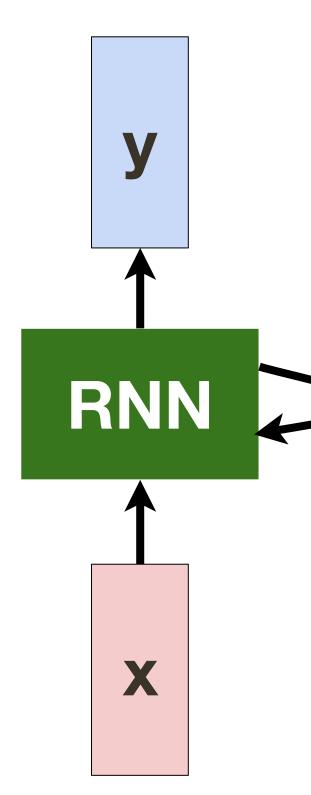
[0,0,0,0,0,0,0,0,0,0]



person holding dog

[0, 0, 1, 0, 0, 0, 0, 0, 0, 0]





Vocabulary

one-hot	encodings
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computer	6	[0,0,0,0,0, 1 ,0,0,0,0]
using	7	[0,0,0,0,0,0,1,0,0,0]

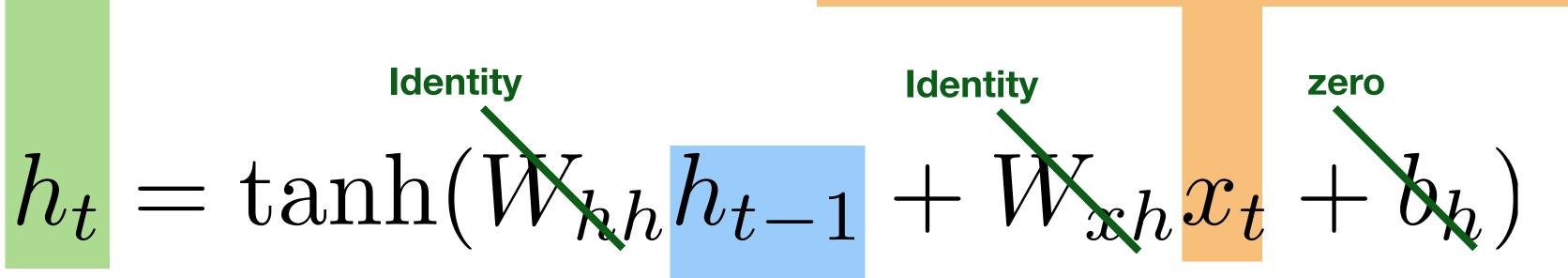
[0, 0, 0.76, 0, 0, 0, 0, 0, 0, 0]

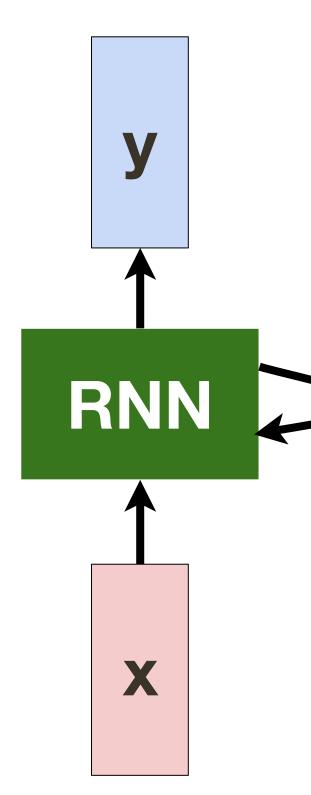
Identity



person holding dog

[0, 0, 1, 0, 0, 0, 0, 0, 0, 0]





[0,0,0,0,0,0,0,0,0,0]

Vocabulary

one-hot encodings

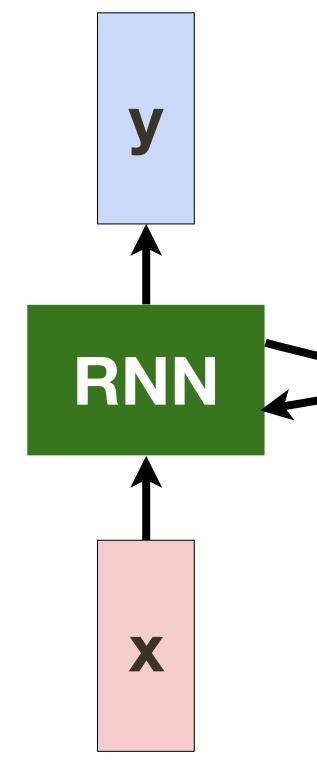
dog	1	[1 , 0, 0, 0, 0, 0, 0, 0, 0, 0]
cat	2	[0, 1 , 0, 0, 0, 0, 0, 0, 0, 0]
person	3	[0, 0, 1 , 0, 0, 0, 0, 0, 0, 0]
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Identity $h_t = \tanh(W_{kh}h_{t-1} + W_{xh}x_t +$



person holding dog

Identity zero





Vocabulary

one-hot	encodings
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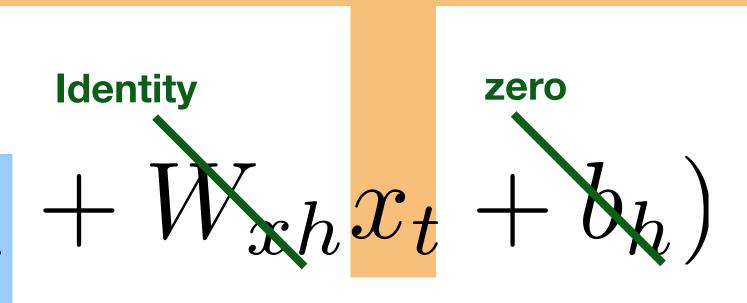
Identity $h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$

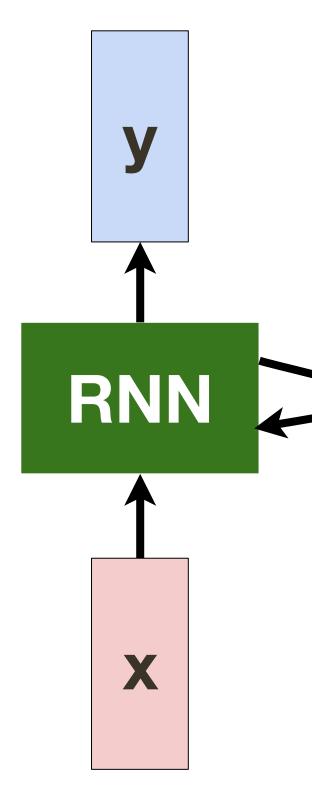
[0,0,0.76,0,0,0,0,0,0,0]



person holding dog

[0, 0, 0, 1, 0, 0, 0, 0, 0, 0]





Vocabulary

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cat	2	[0, 1, 0, 0, 0, 0, 0, 0, 0, 0]
person	3	[0,0, 1 ,0,0,0,0,0,0,0]
holding	4	[0,0,0, 1 ,0,0,0,0,0,0]
tree	5	[0,0,0,0, 1 ,0,0,0,0,0]
computer	6	[0,0,0,0,0, 1 ,0,0,0,0]
using	7	[0,0,0,0,0,0,1,0,0,0]

[0, 0, 0.64, 0.76, 0, 0, 0, 0, 0, 0]

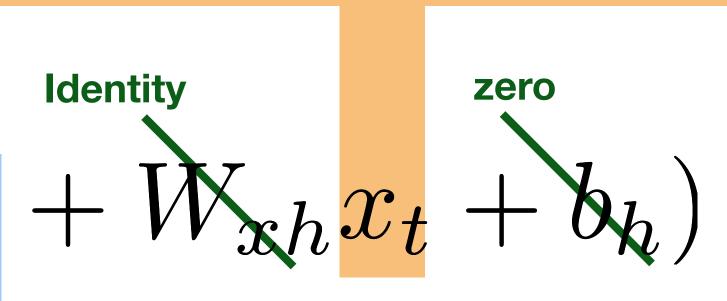
Identity $h_t = \tanh(W_{hh} h_{t-1} + W_{xh} x_t)$

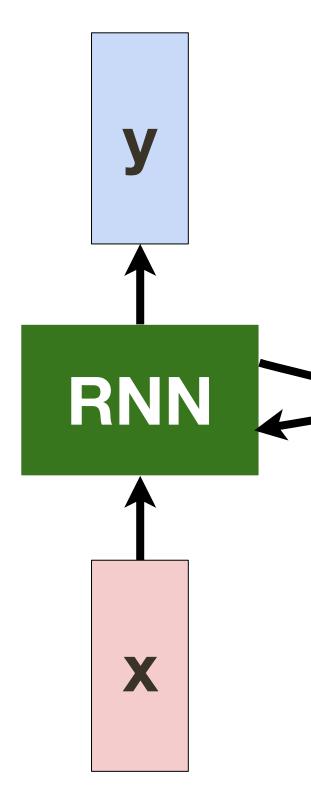
[0, 0, 0.76, 0, 0, 0, 0, 0, 0, 0]



person holding dog

[0, 0, 0, 1, 0, 0, 0, 0, 0, 0]





Vocabulary

one-hot encodings

dog	1	[1 , 0, 0, 0, 0, 0, 0, 0, 0, 0]
cat	2	[0, 1 , 0, 0, 0, 0, 0, 0, 0, 0]
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holding	4	[0,0,0, 1 ,0,0,0,0,0,0]
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computer	6	[0,0,0,0,0, 1 ,0,0,0,0]
using	7	[0,0,0,0,0,0,1,0,0,0]

[0, 0, 0.64, 0.76, 0, 0, 0, 0, 0, 0]

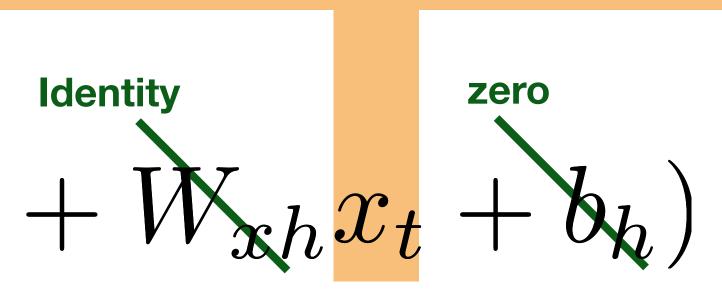
Identity $h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$

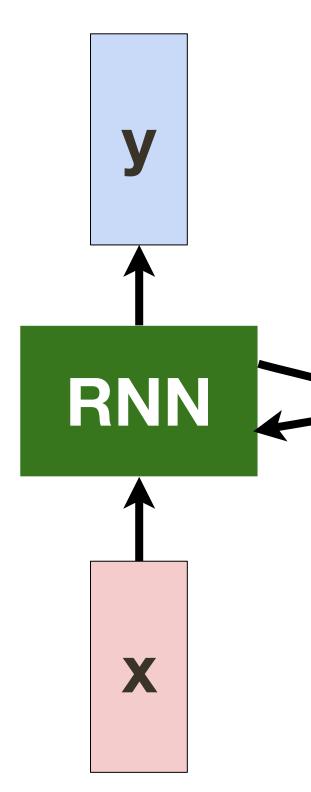
[0, 0, 0.76, 0, 0, 0, 0, 0, 0, 0]

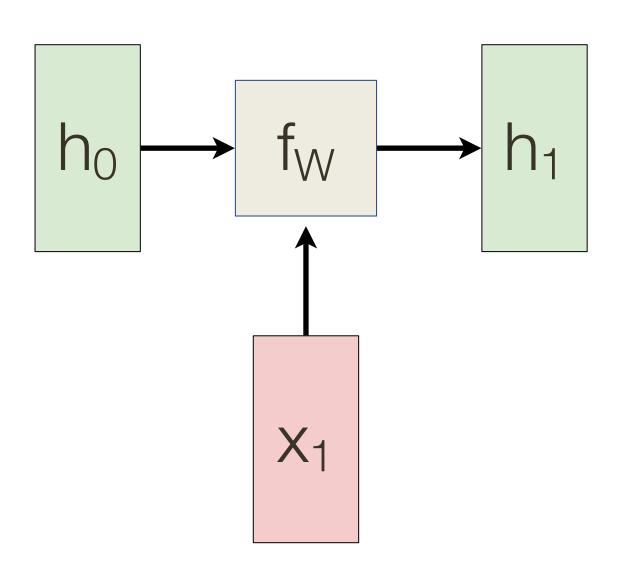


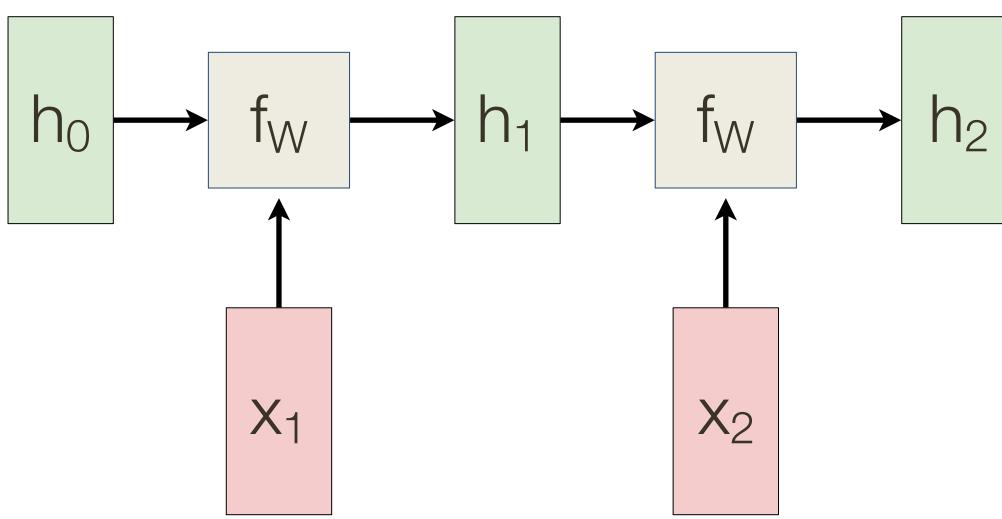
Like bag of words with some notion of recency

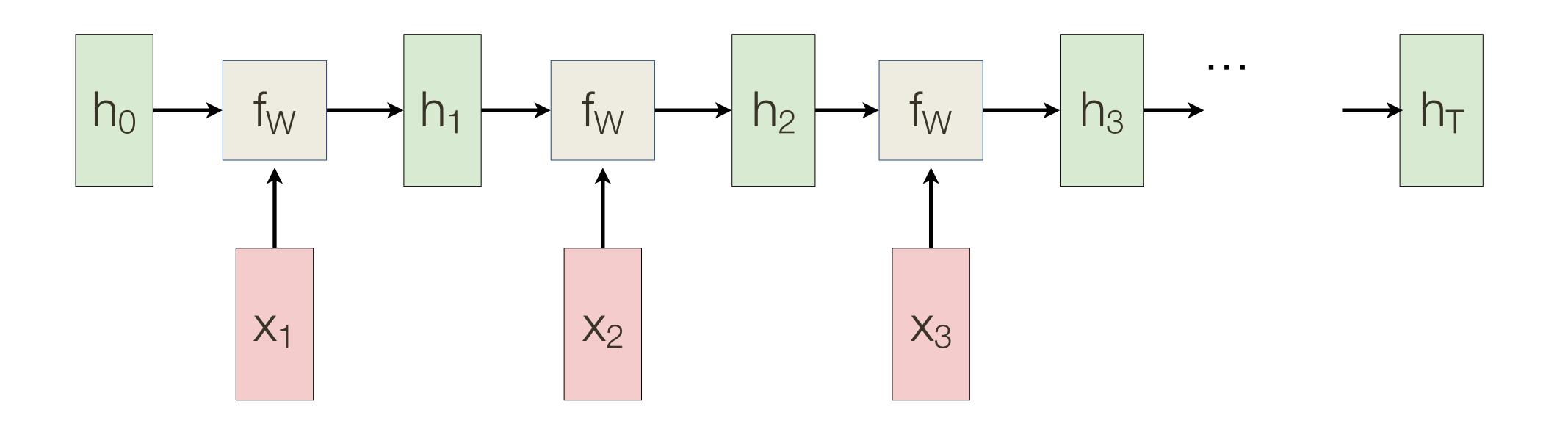
[0, 0, 0, 1, 0, 0, 0, 0, 0, 0]



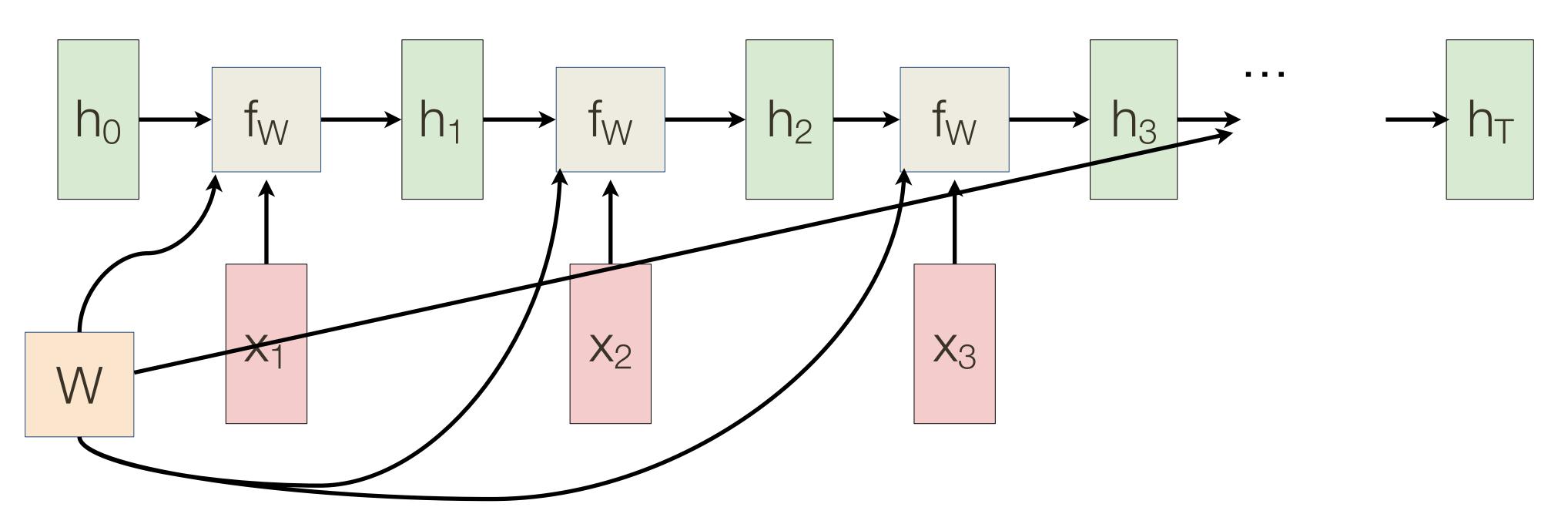




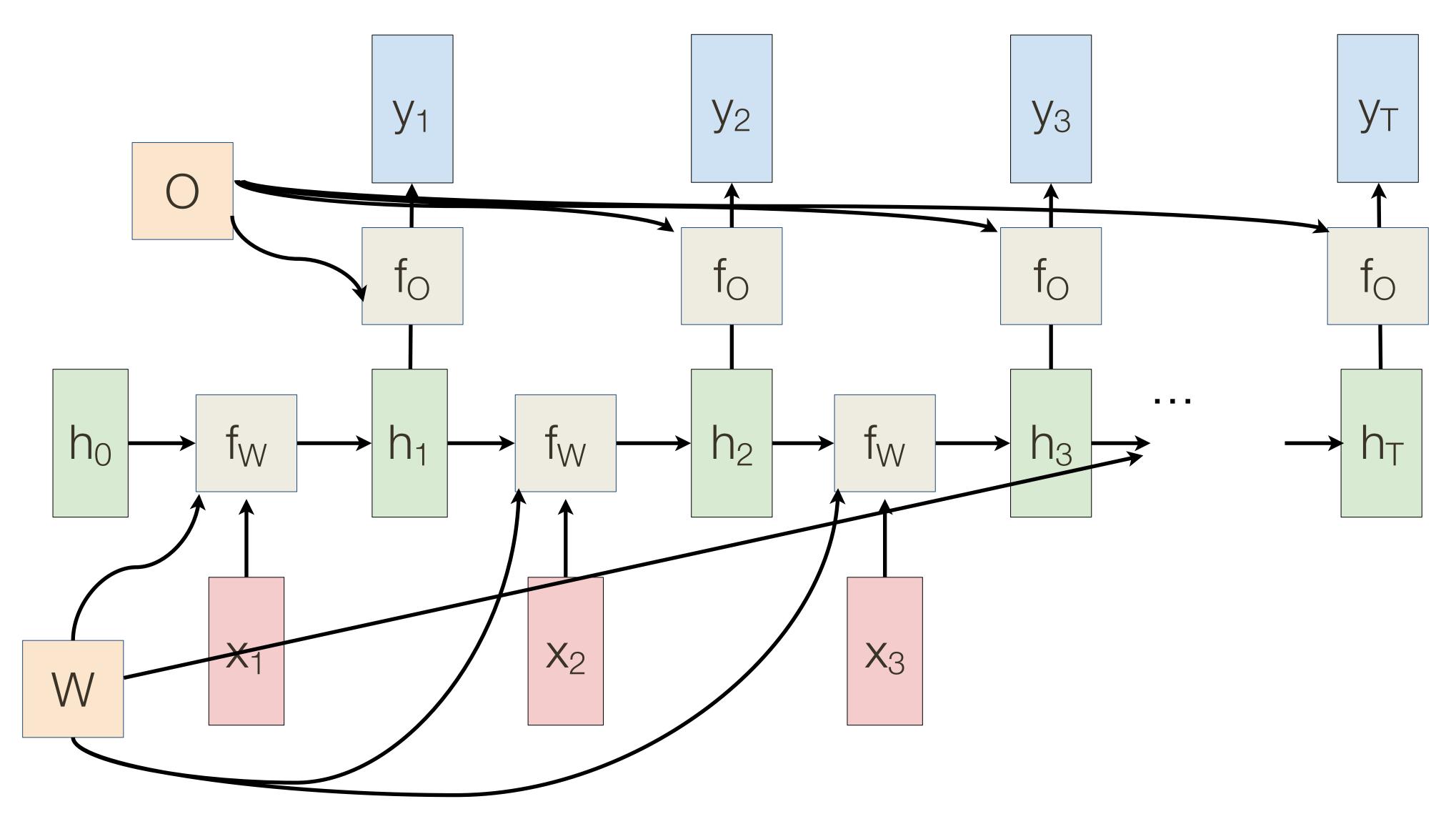




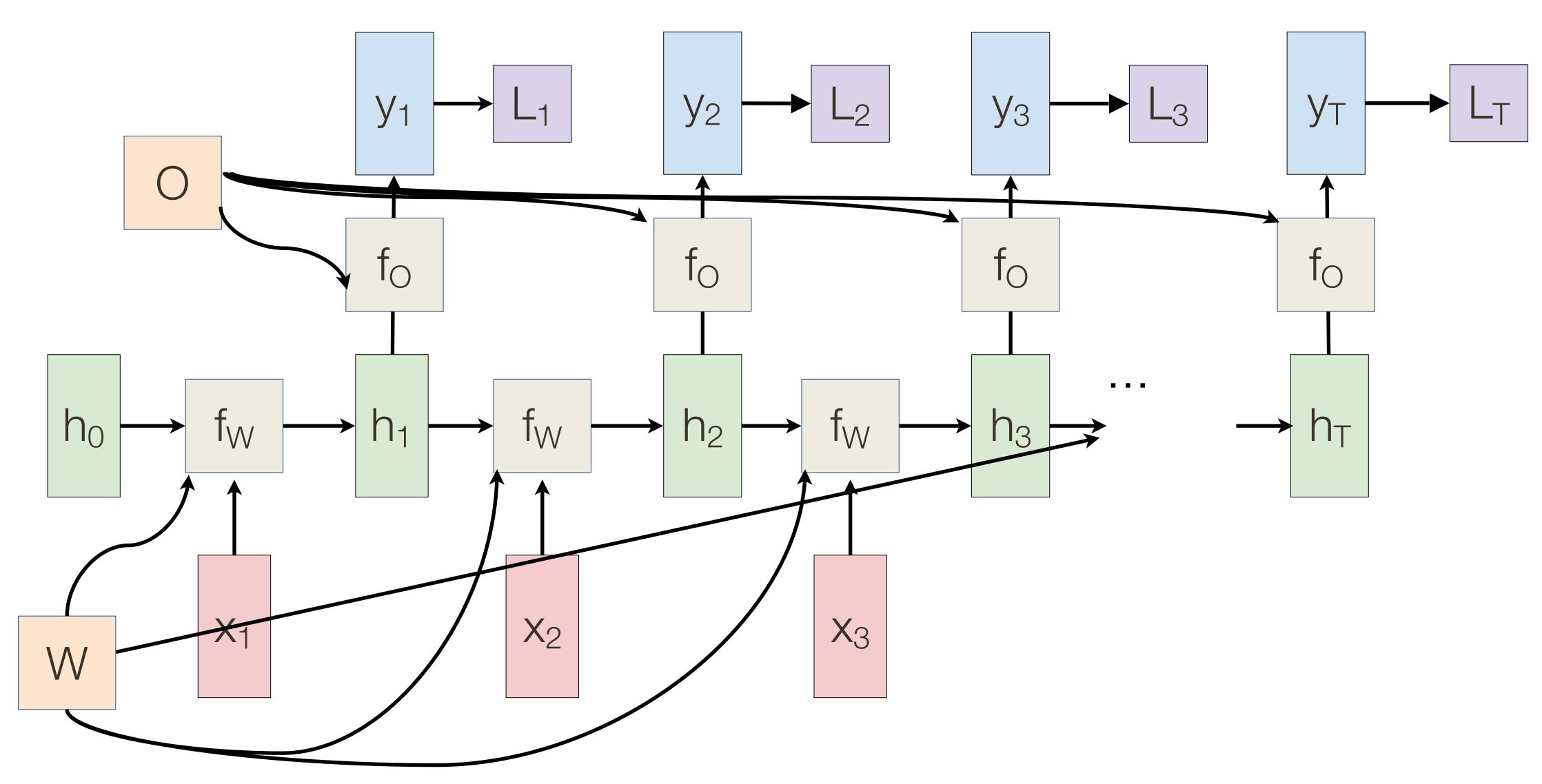
Re-use the same weight matrix at every time-step



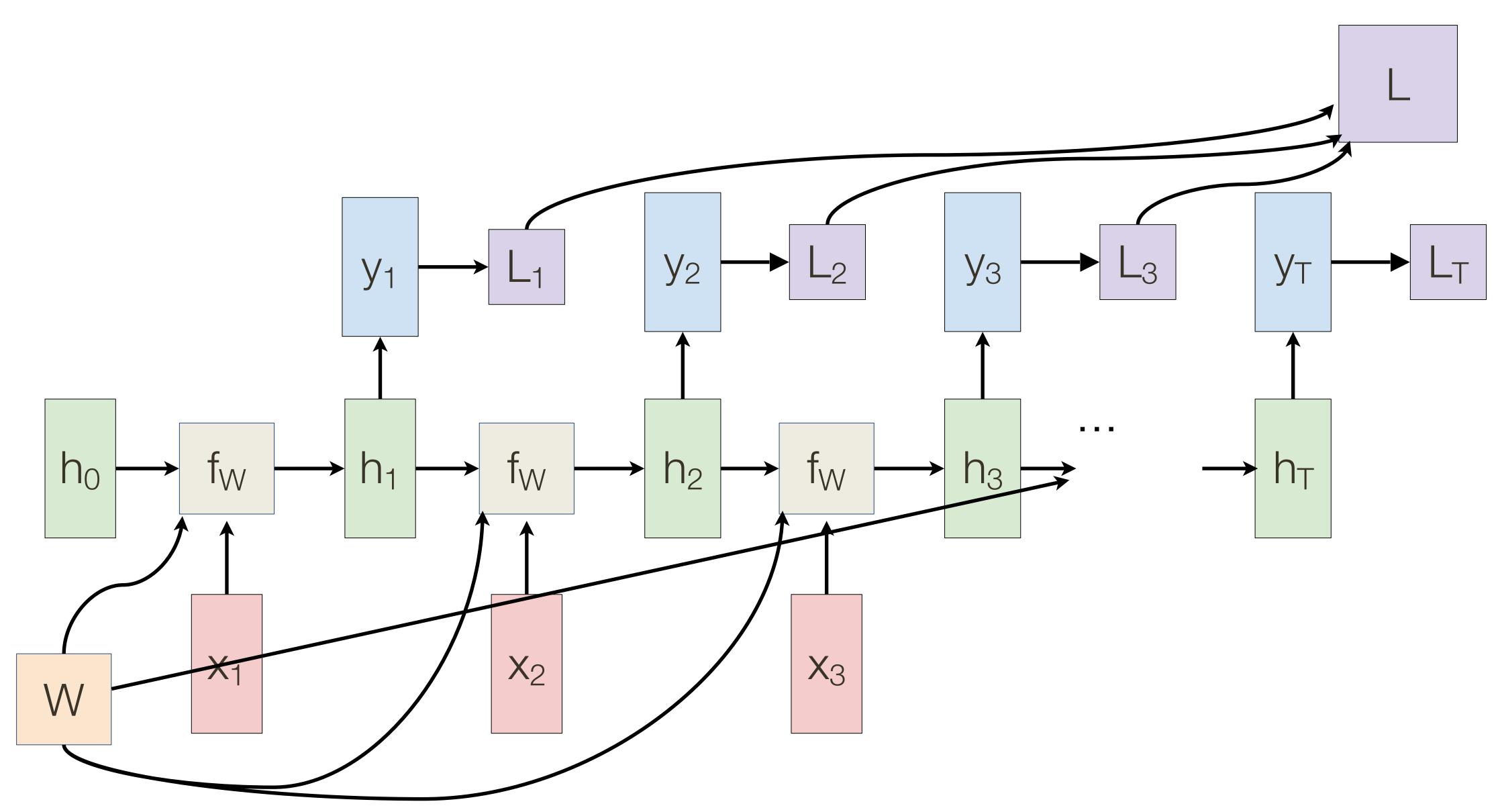
RNN Computational Graph: Many to Many



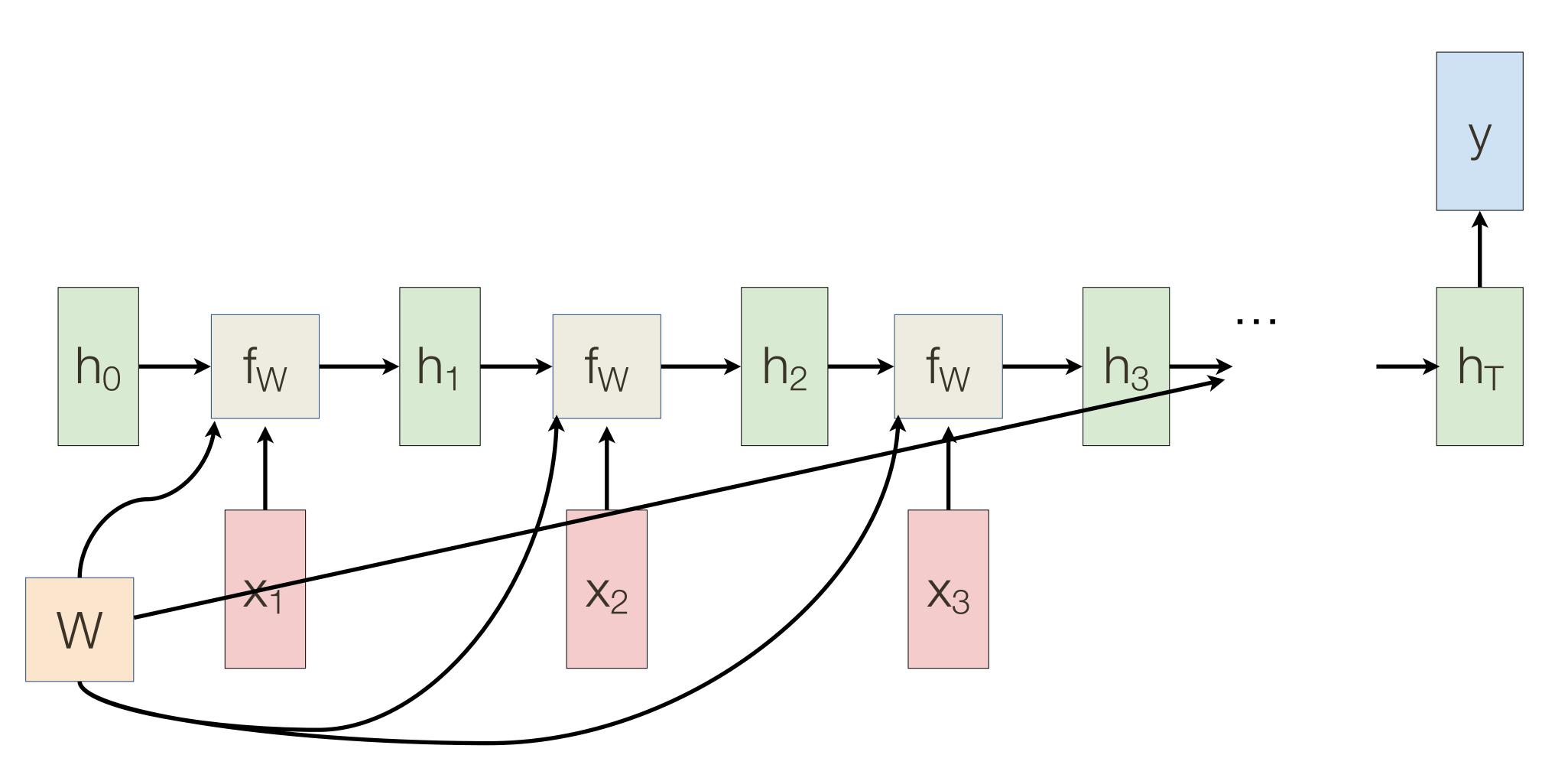
RNN Computational Graph: Many to Many



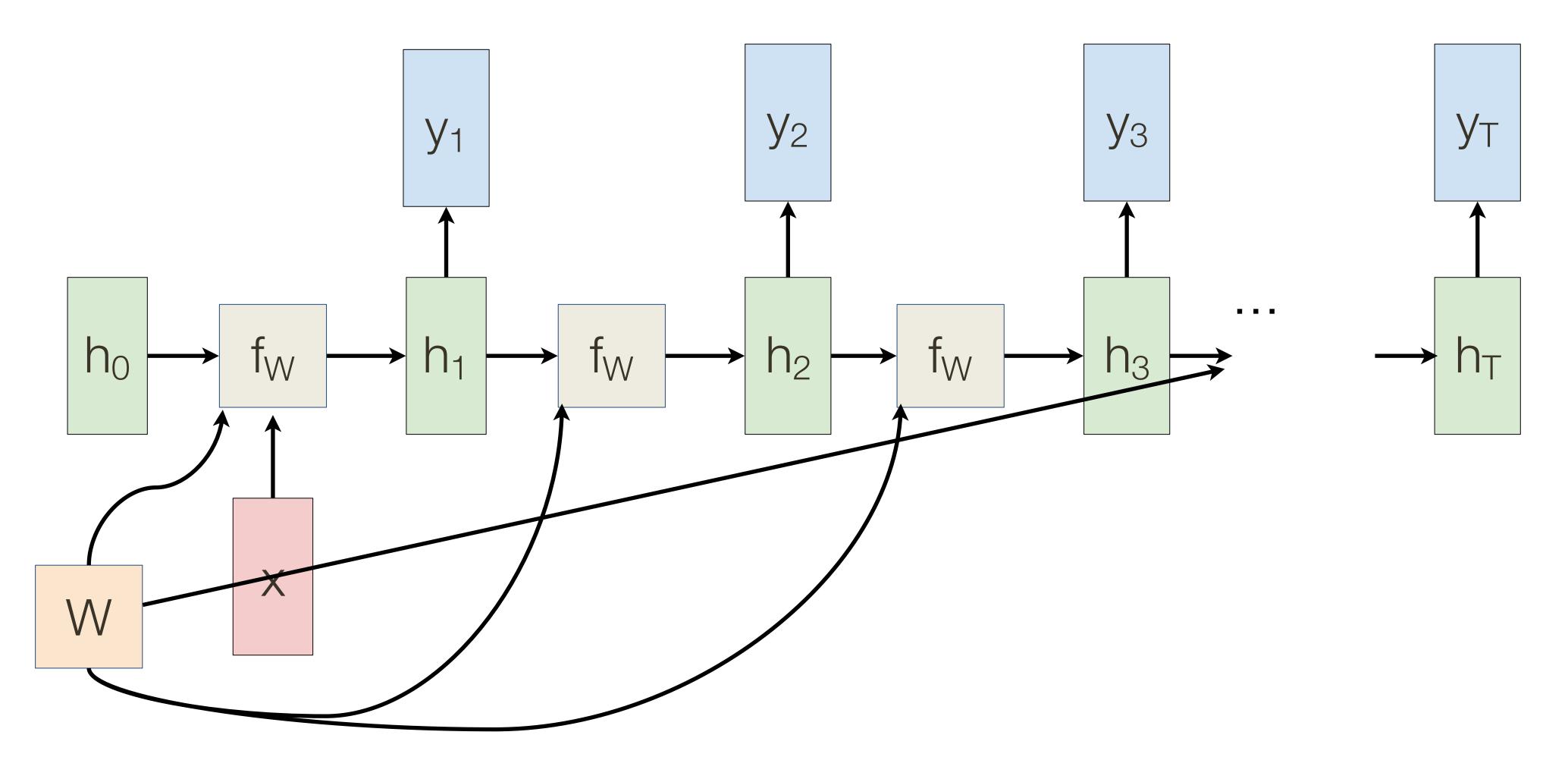
RNN Computational Graph: Many to Many



RNN Computational Graph: Many to One

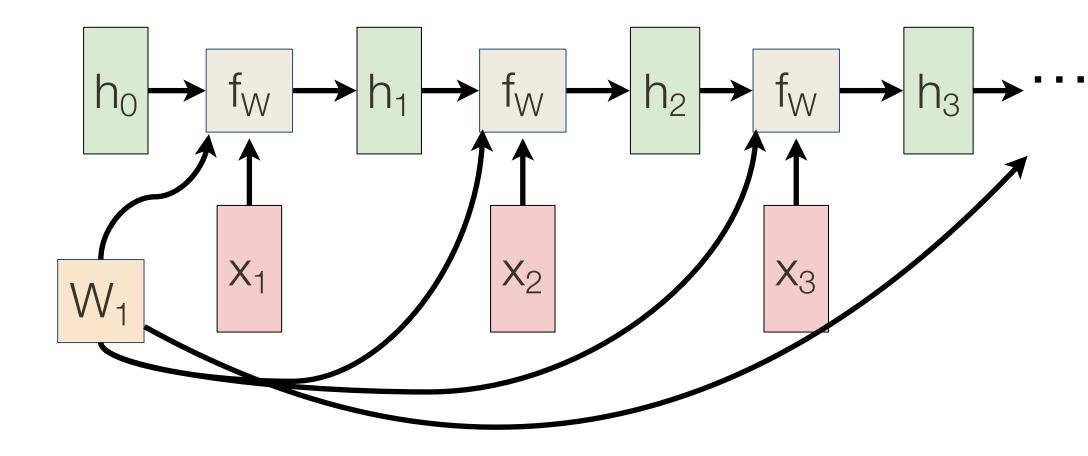


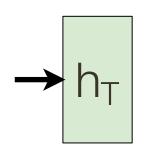
RNN Computational Graph: One to Many



Sequence to Sequence: Many to One + One to Many

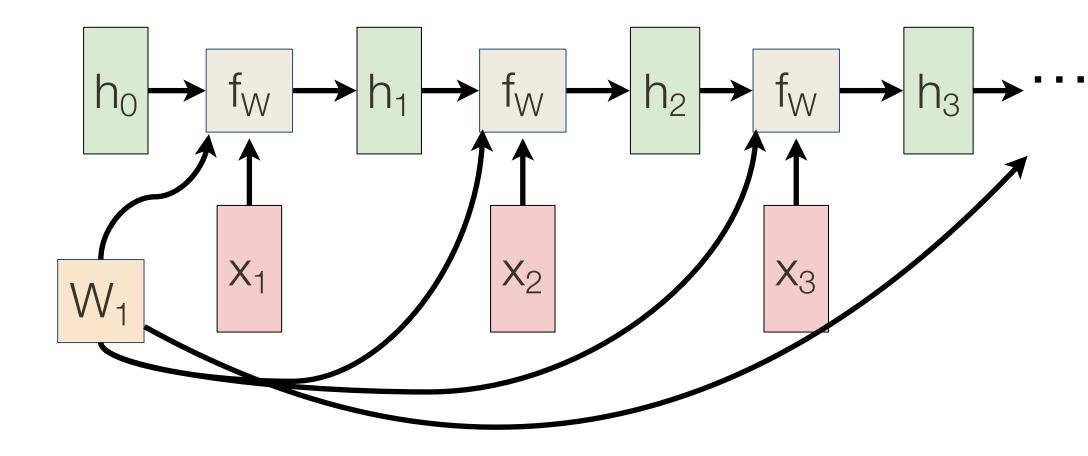
Many to one: Encode input sequence in a single vector





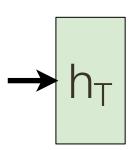
Sequence to Sequence: Many to One + One to Many

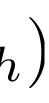
Many to one: Encode input sequence in a single vector



$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$

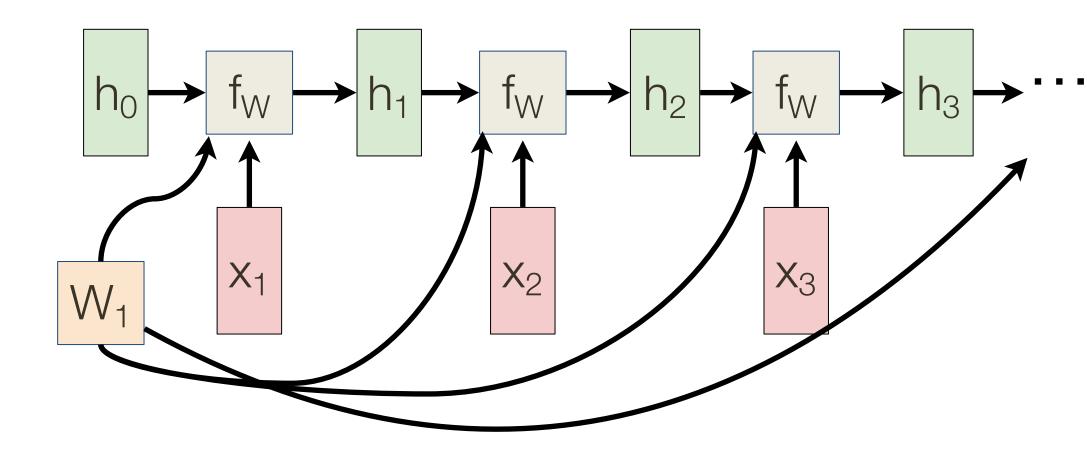
Basically a fully connected layer (with shared params)





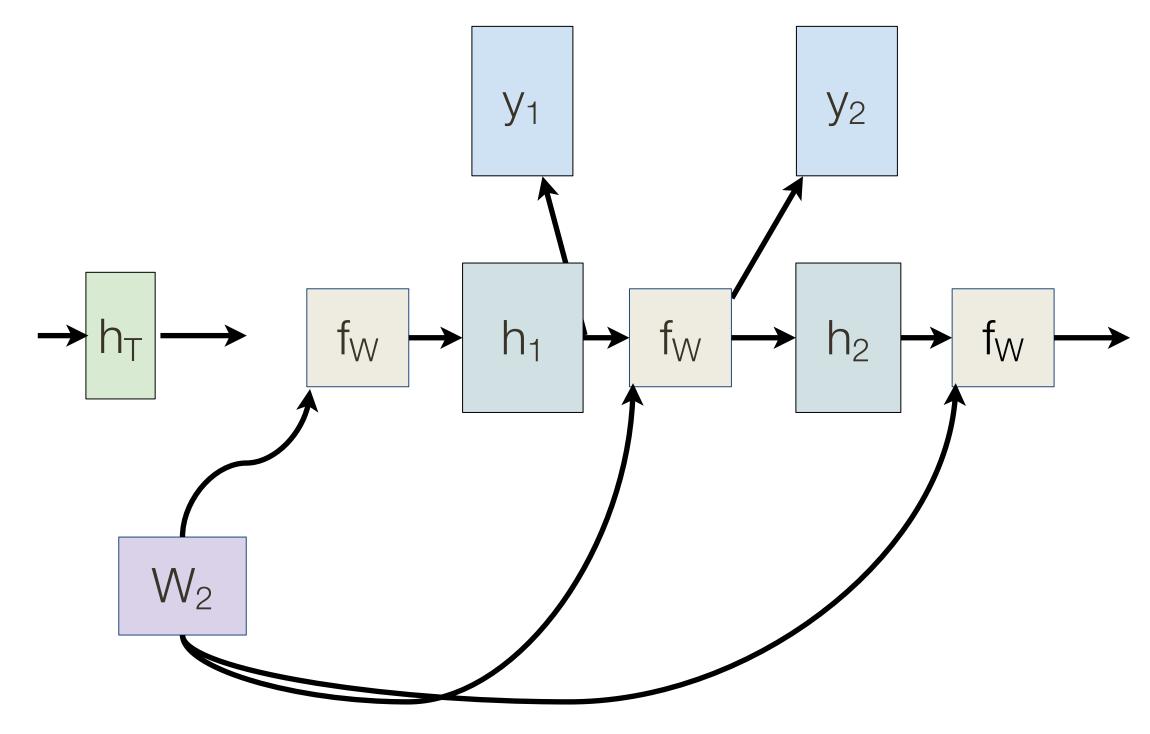
Sequence to Sequence: Many to One + One to Many

Many to one: Encode input sequence in a single vector



Assignment 3: Part 1

One to many: Produce output sequence from single input vector





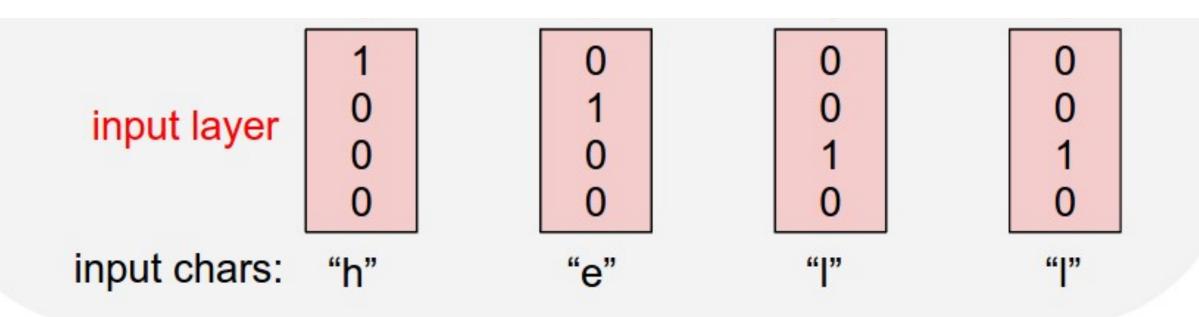
Example: Character-level Language Model (Training)

Assignment 3: Decoder of Part 1

(encoder is similar, but with no outputs, so easier)

Vocabulary: ['h', 'e', 'l', 'o']

Example training sequence: "hello"

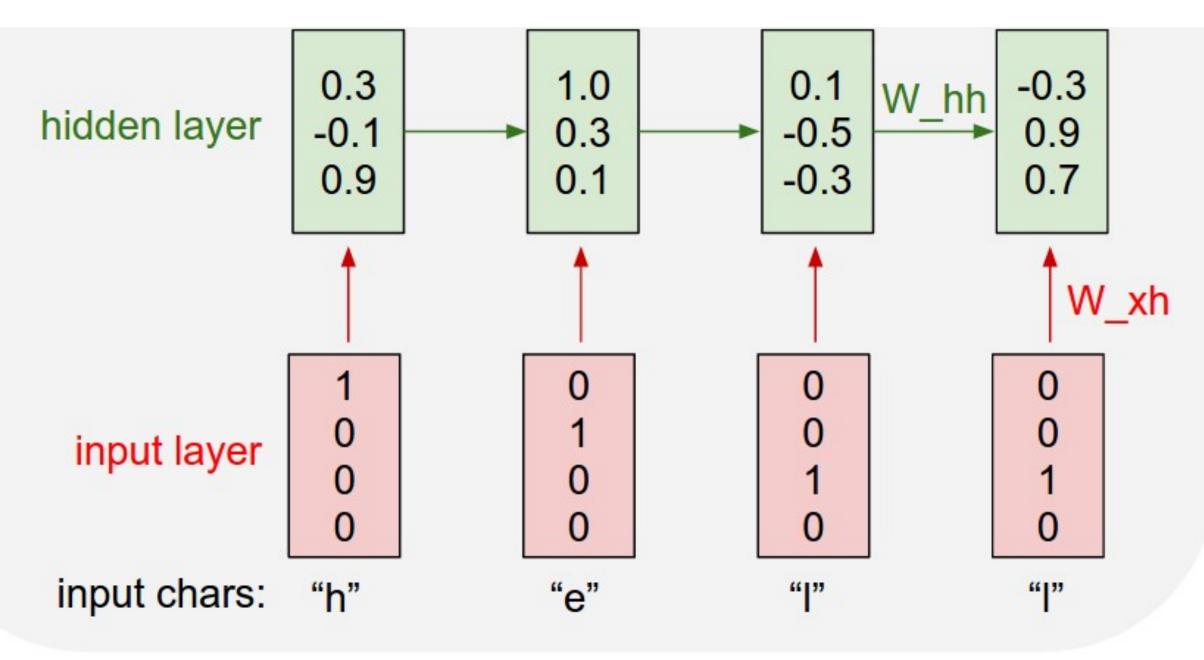




Vocabulary: ['h', 'e', 'l', 'o']

Example training sequence: "hello"

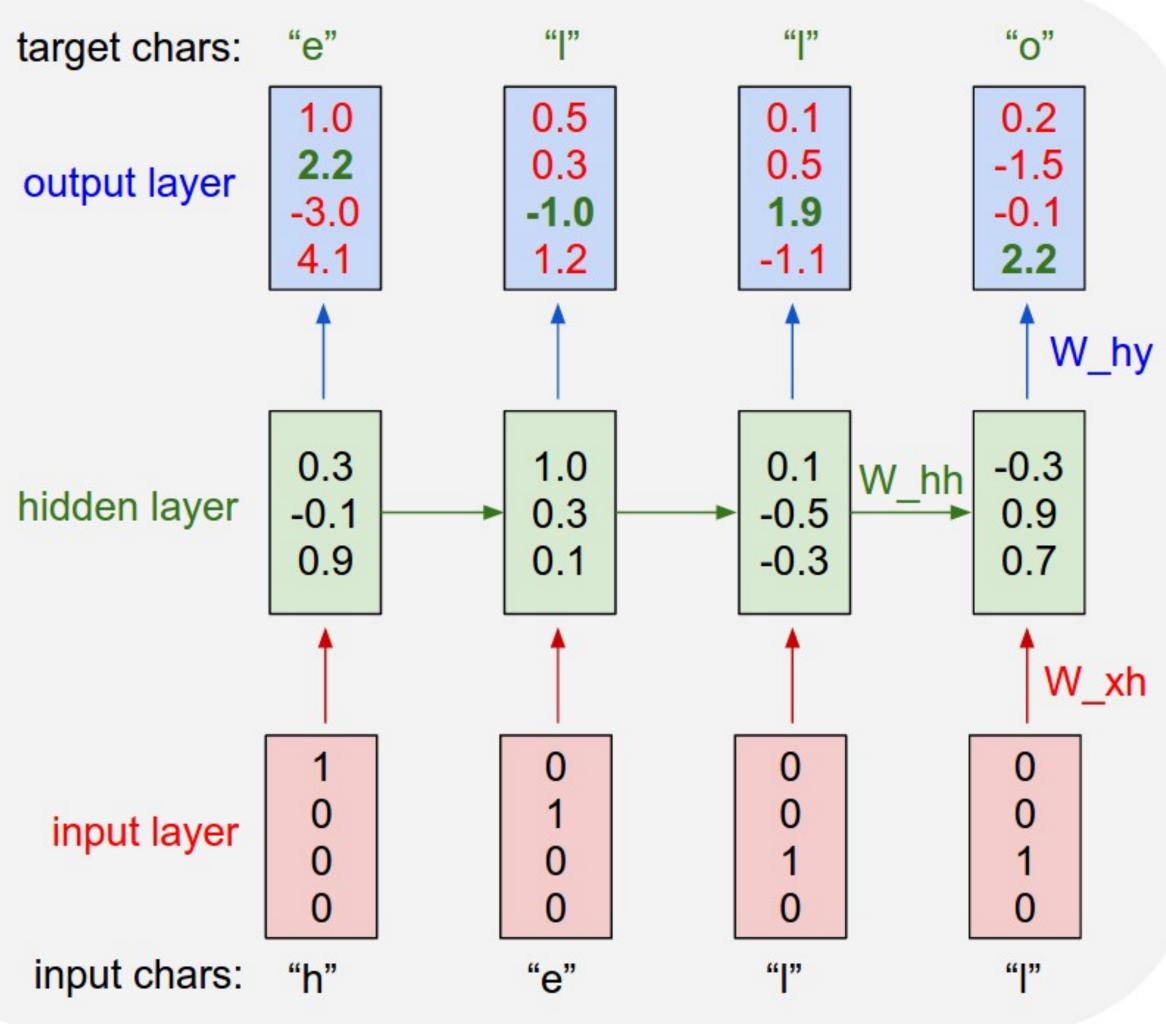
$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$





Vocabulary: ['h', 'e', 'l', 'o']

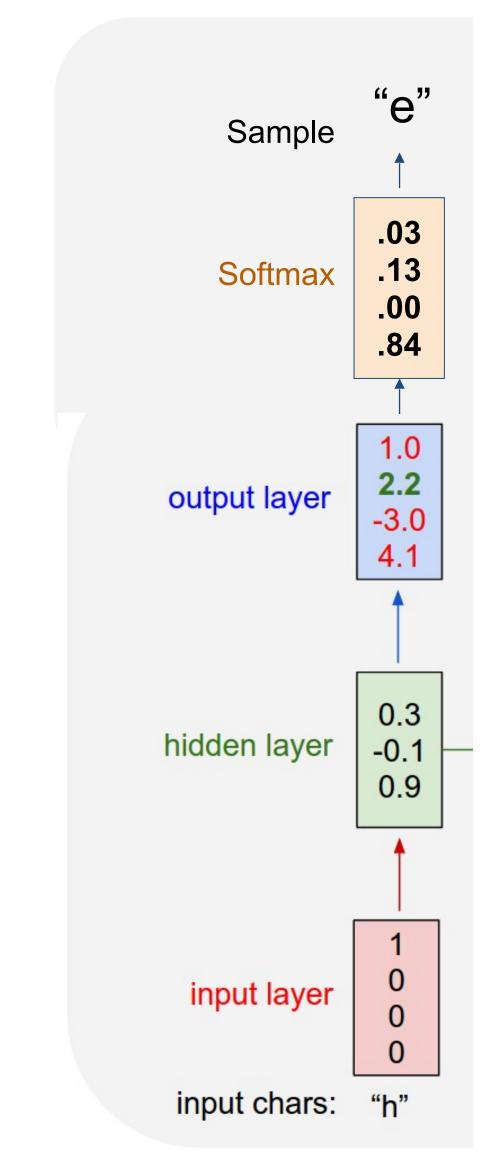
Example training sequence: "hello"





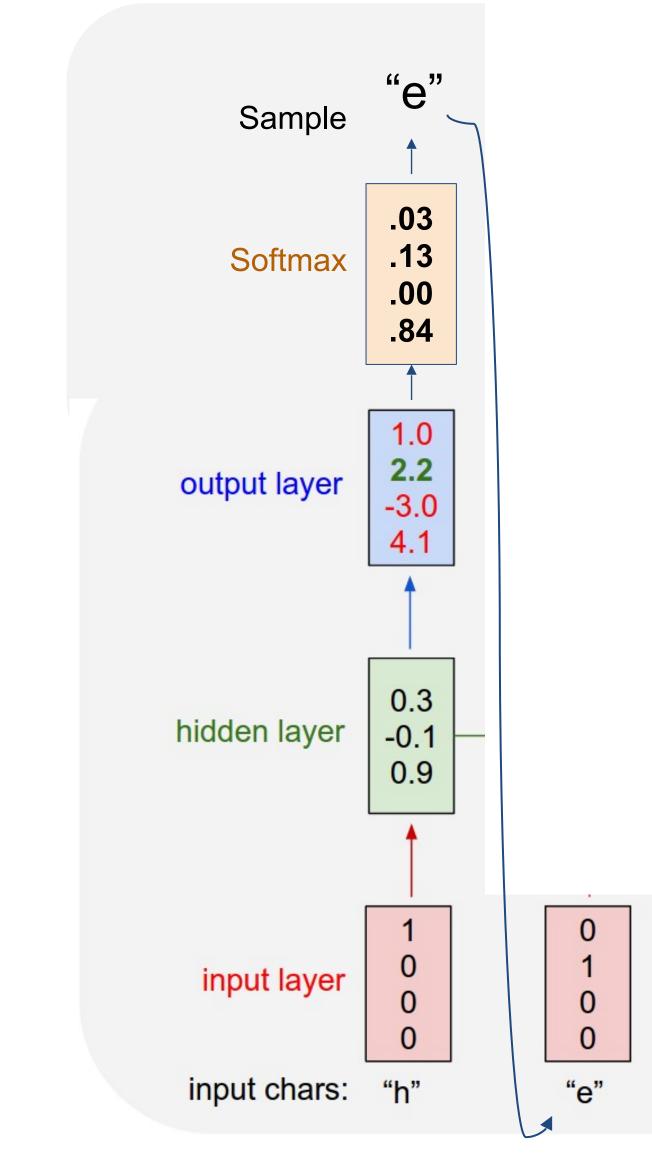
Vocabulary: ['h', 'e', 'l', 'o']

At test time sample one character at a time and feed back to the model



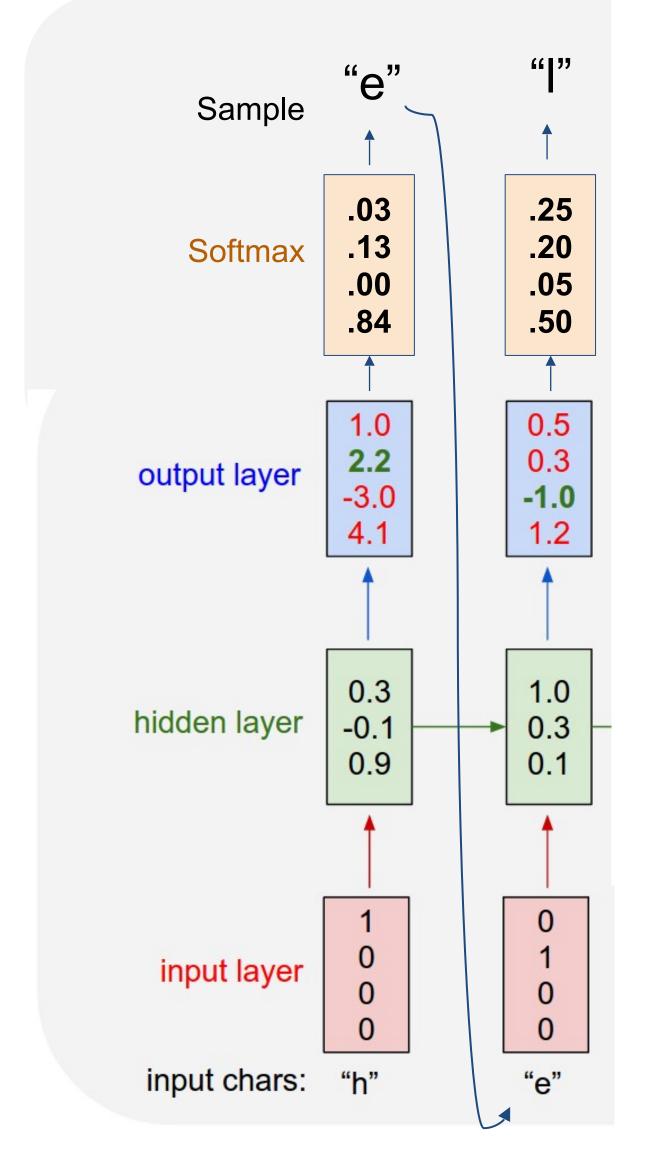
Vocabulary: ['h', 'e', 'l', 'o']

At test time sample one character at a time and feed back to the model



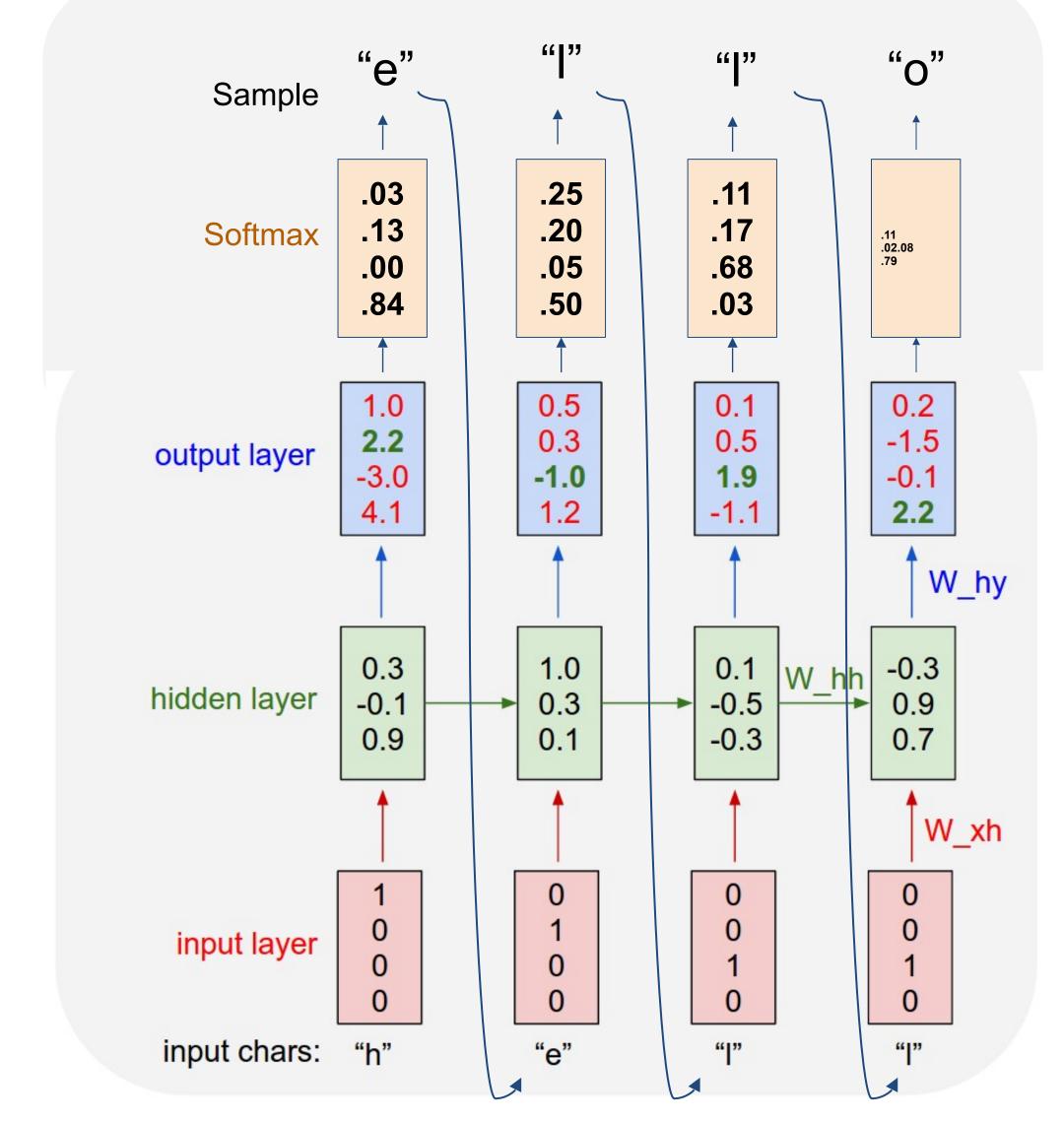
Vocabulary: ['h', 'e', 'l', 'o']

At test time sample one character at a time and feed back to the model



Vocabulary: ['h', 'e', 'l', 'o']

At test time sample one character at a time and feed back to the model

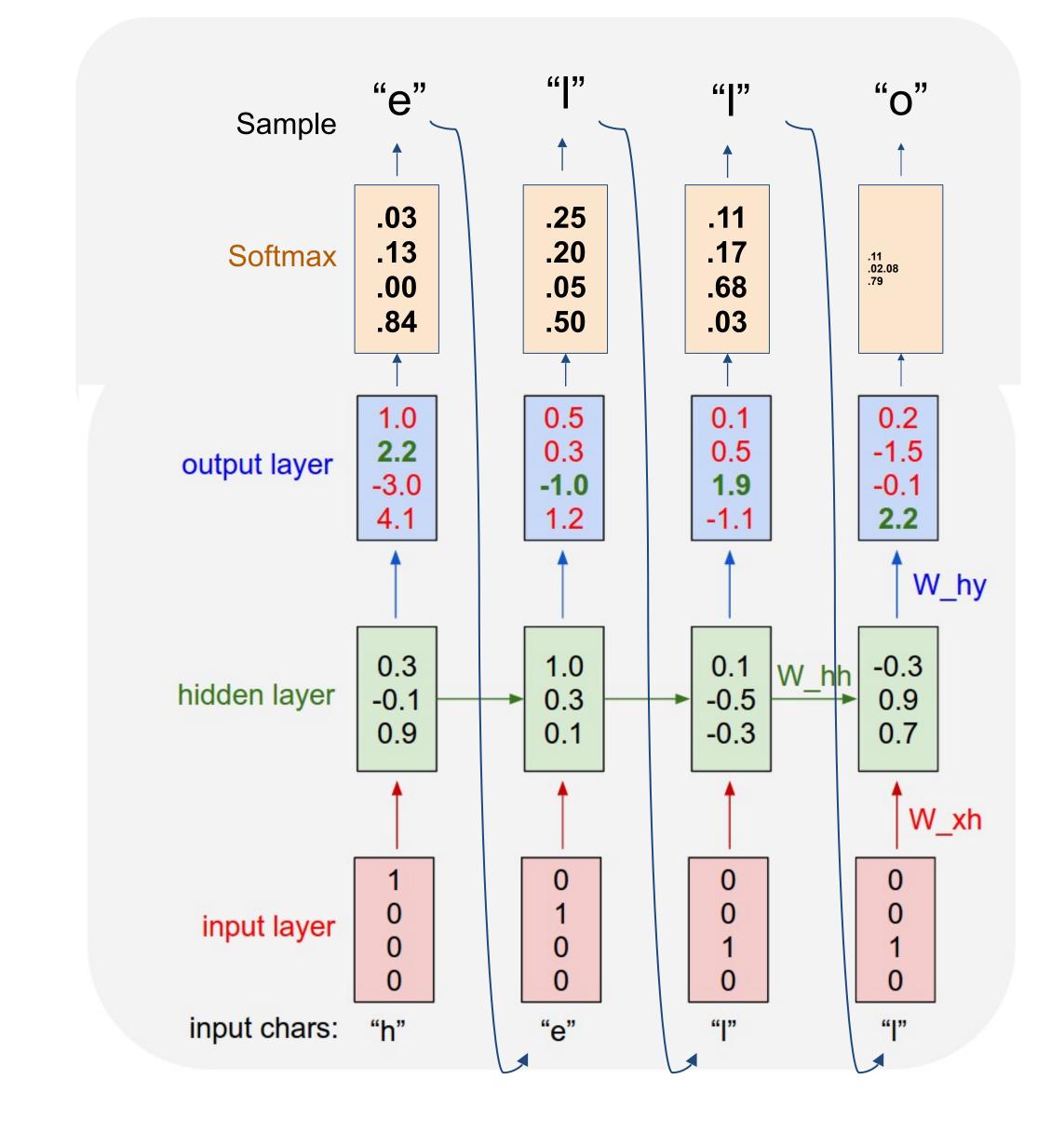


Sampling vs. ArgMax vs. Beam Search

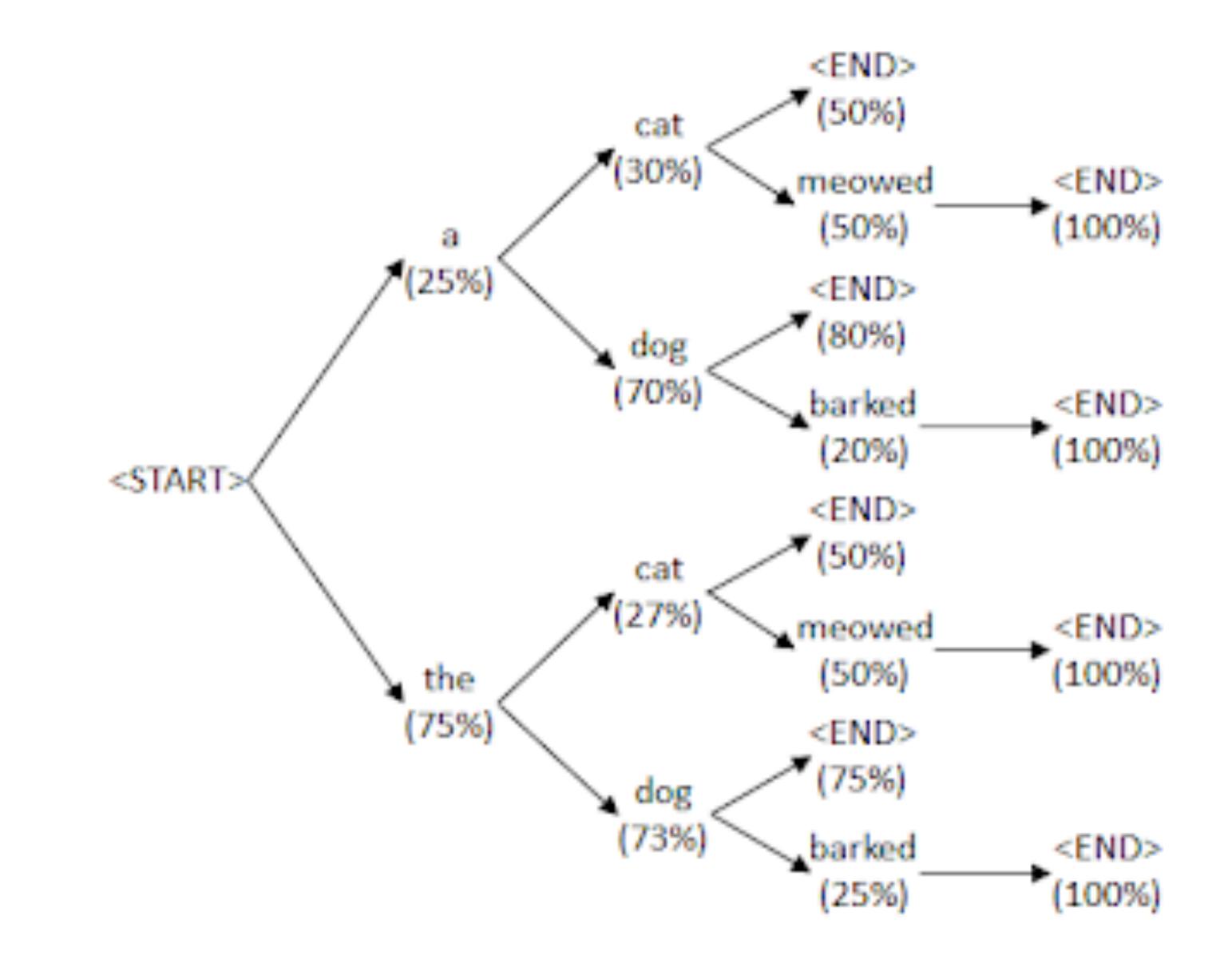
Sampling: allows to generate diverse outputs

ArgMax: could be more stable in practice

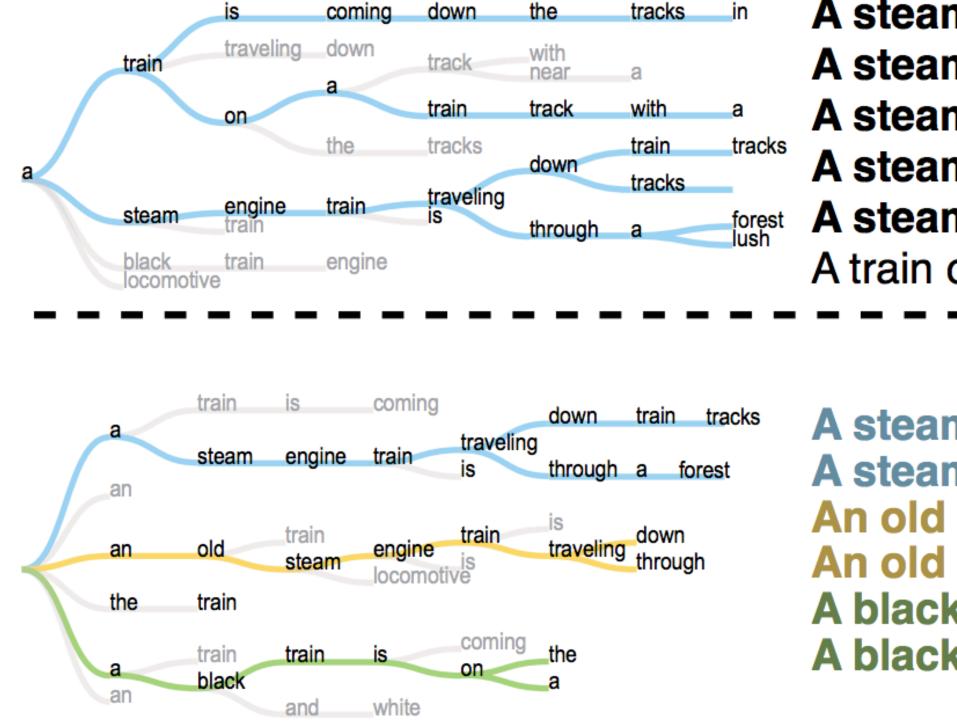
Beam Search: typically gets the best results



Beam Search



Beam Search



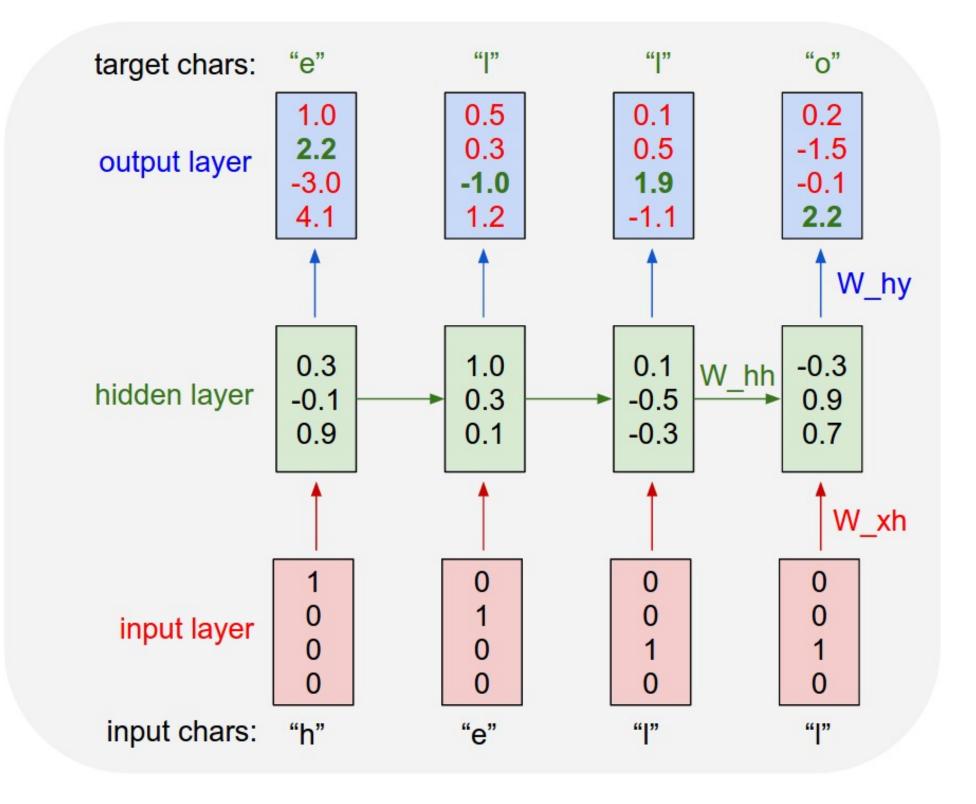
Beam Search

A steam engine train travelling down train tracks.
A steam engine train travelling down tracks.
A steam engine train travelling through a forest.
A steam engine train travelling through a lush green forest.
A steam engine train travelling through a lush green countryside A train on a train track with a sky background.

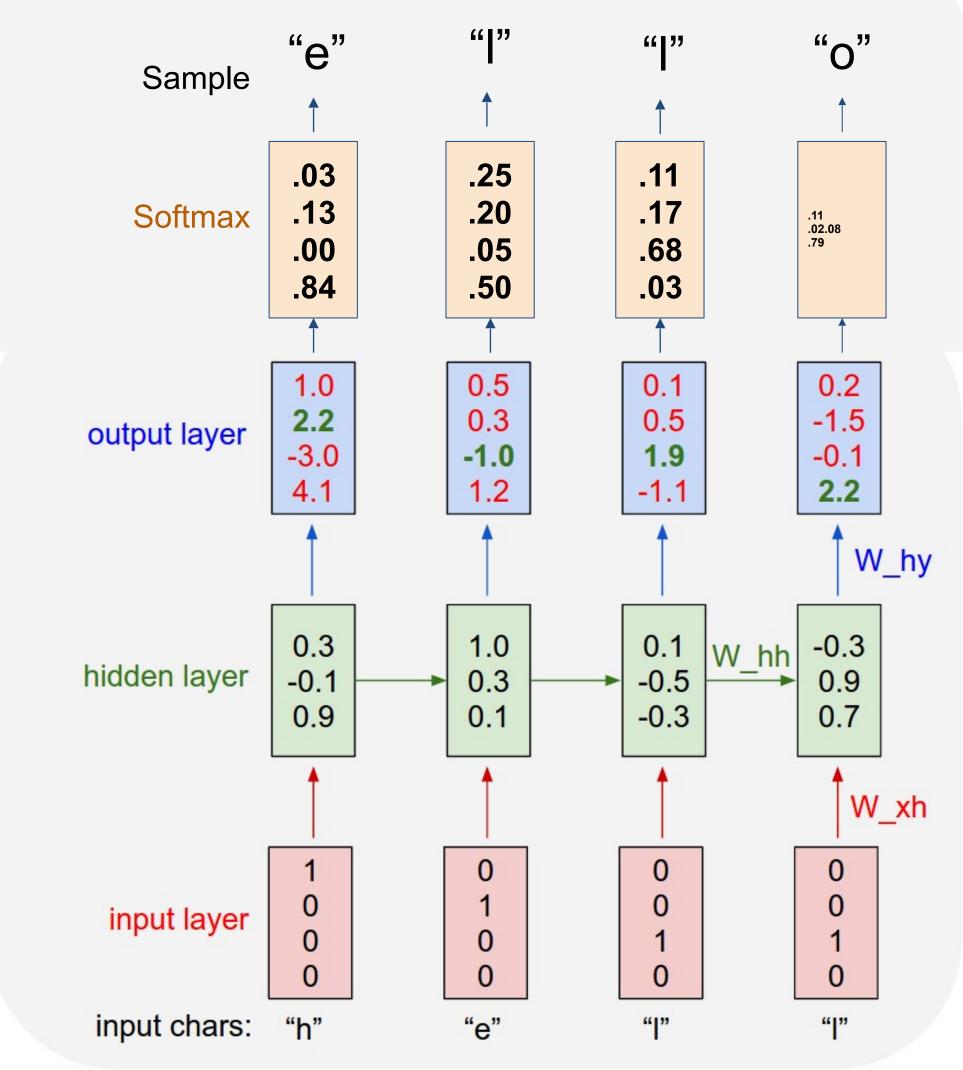
Diverse Beam Search

A steam engine travelling down train tracks. A steam engine train travelling through a forest. An old steam engine train travelling down train tracks. An old steam engine train travelling through a forest. A black train is on the tracks in a wooded area. A black train is on the tracks in a rural area.

Training Objective: Predict the next word (cross entropy loss)

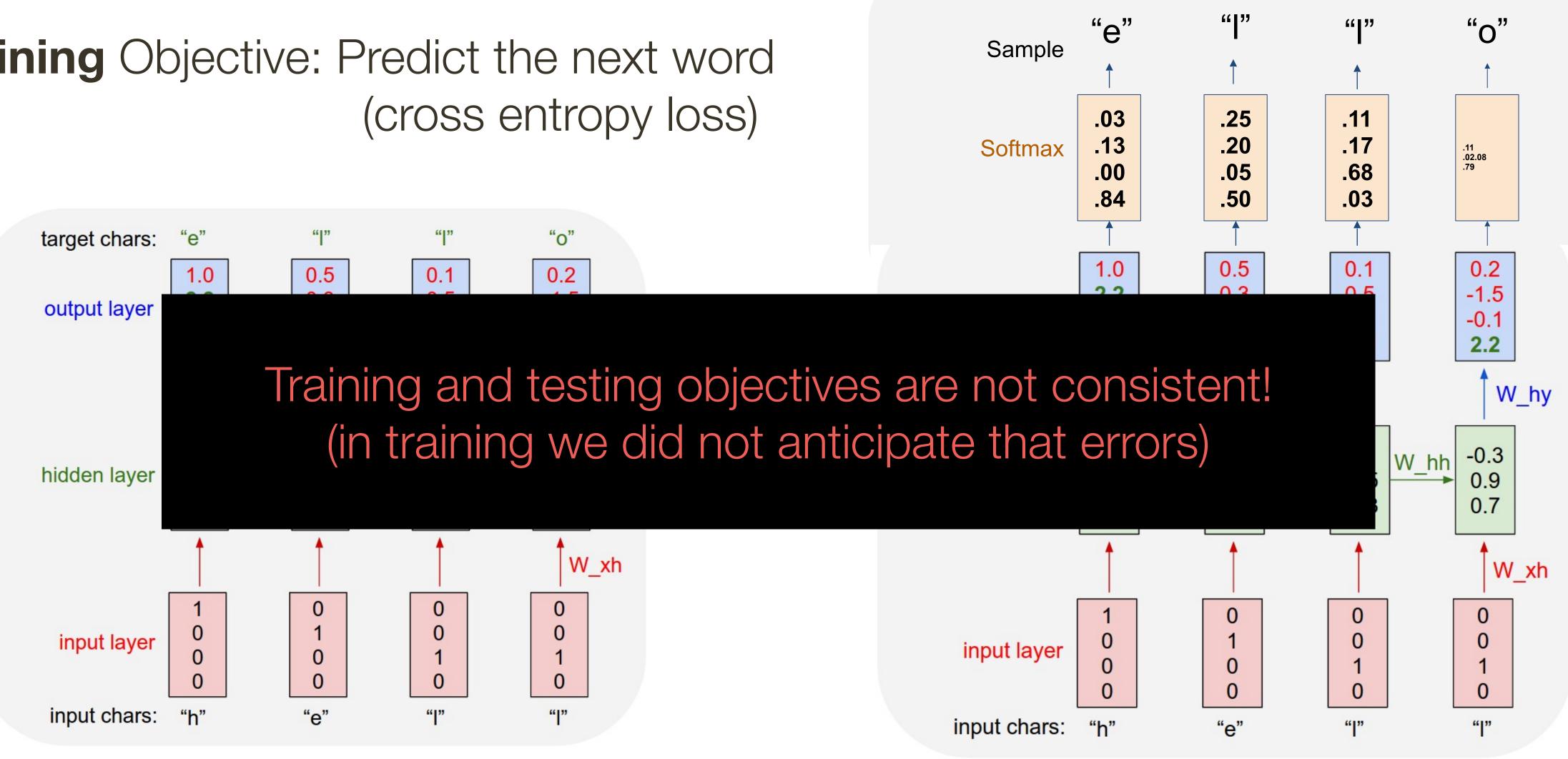


Testing: Sample the full sequence



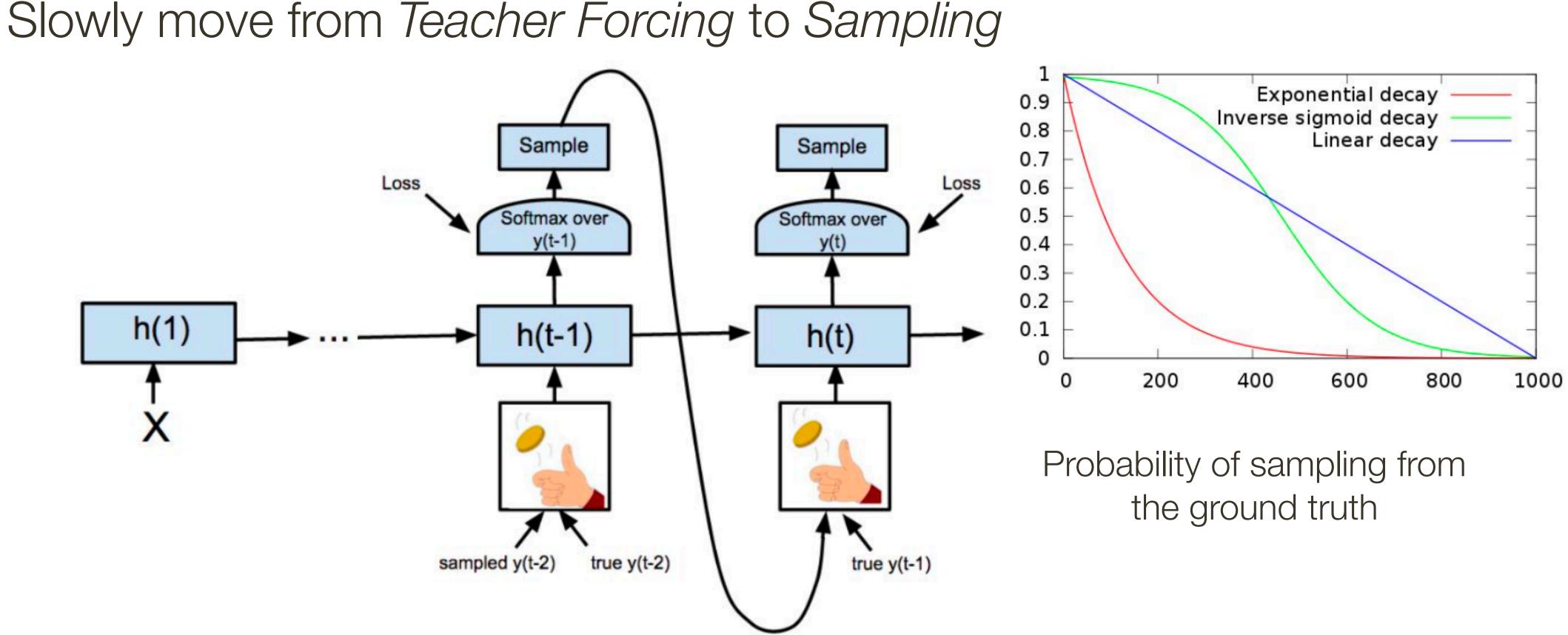


Training Objective: Predict the next word



Testing: Sample the full sequence





Note: for the Assignment 3 its OK to sample once per sequence (not per step as is illustrated here)

[Bengio et al., 2015]

* slide from Marco Pedersoli and Thomas Lucas





Approach vs Metric

Baseline **Baseline with Dropout Always Sampling** Scheduled Sampling **Uniform Scheduled Sampling** Baseline ensemble of 10 Scheduled Sampling ensemble of

Baseline: Google NIC captioning model

Baseline with Dropout: Regularized RNN version

Always sampling: Use sampling from the beginning of training

Scheduled sampling: Sampling with inverse Sigmoid decay

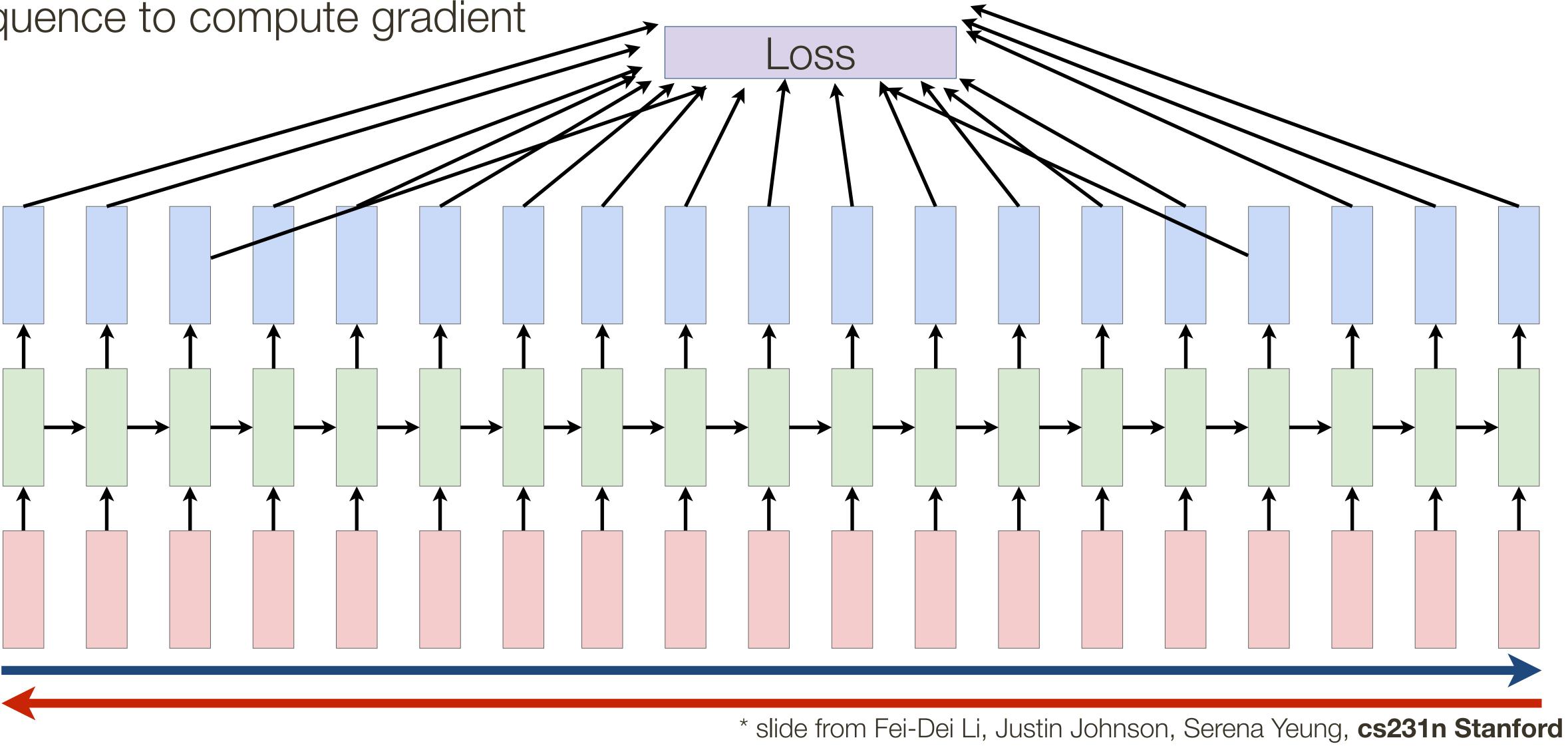
Uniformed scheduled sampling: Scheduled sampling but uniformly

Microsoft COCO developement set			
	BLEU-4	METEOR	CIDER
	28.8	24.2	89.5
	28.1	23.9	87.0
	11.2	15.7	49.7
	30.6	24.3	92.1
3	29.2	24.2	90.9
	30.7	25.1	95.7
of 5	32.3	25.4	98.7

* slide from Marco Pedersoli and Thomas Lucas

BackProp Through Time

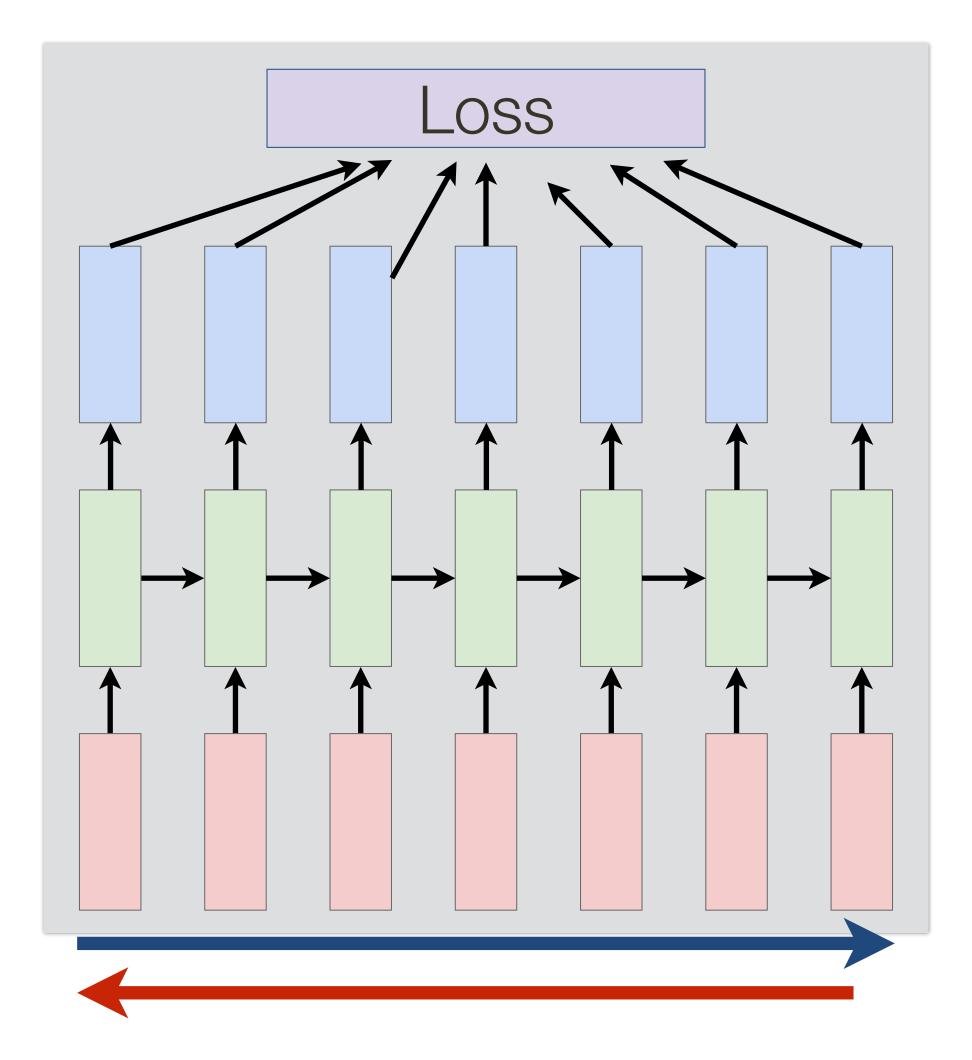
sequence to compute gradient



Forward through entire sequence to compute loss, then backward through entire

Truncated BackProp Through Time

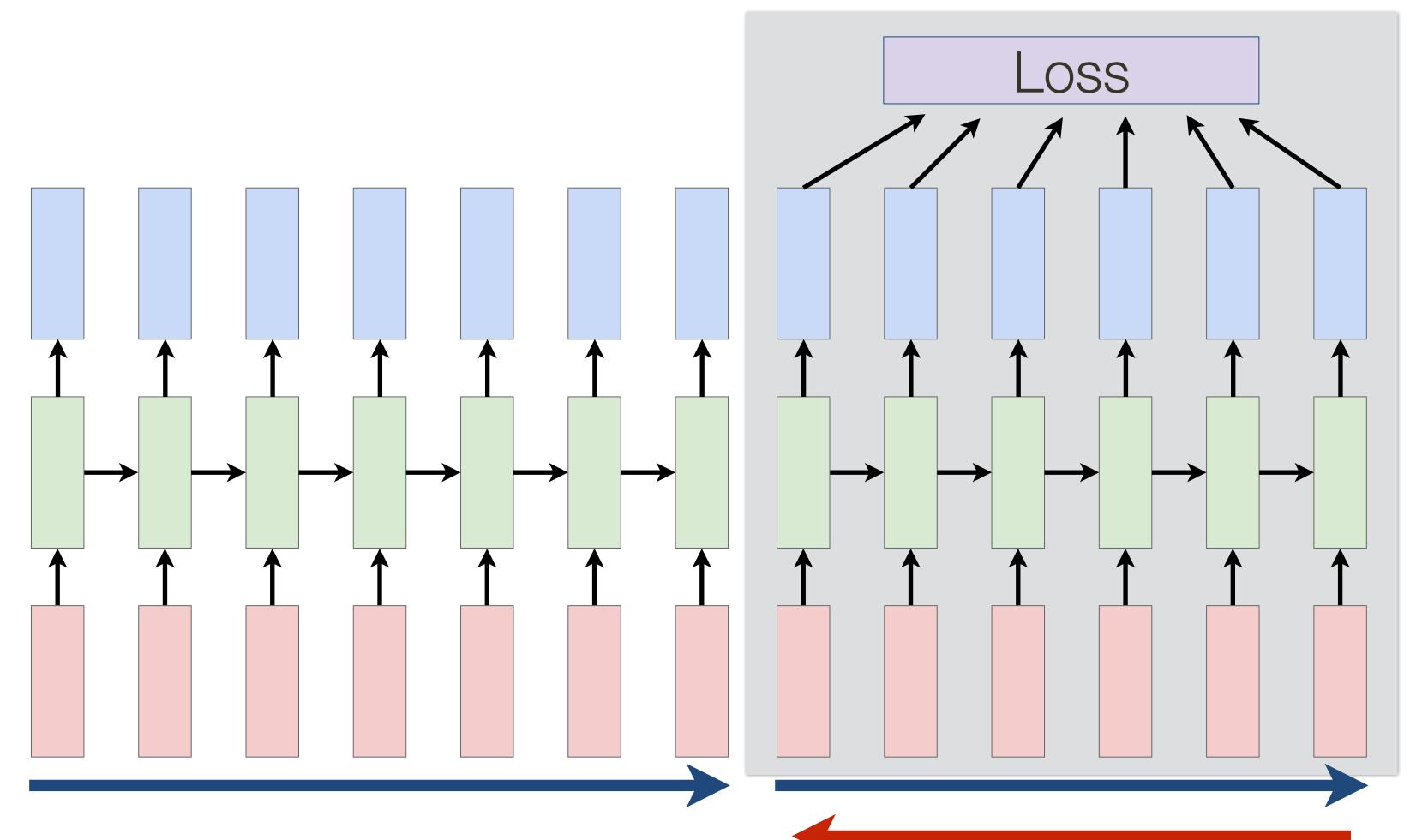
instead of the whole sequence



Run backwards and forwards through (fixed length) chunks of the sequence,

Truncated BackProp Through Time

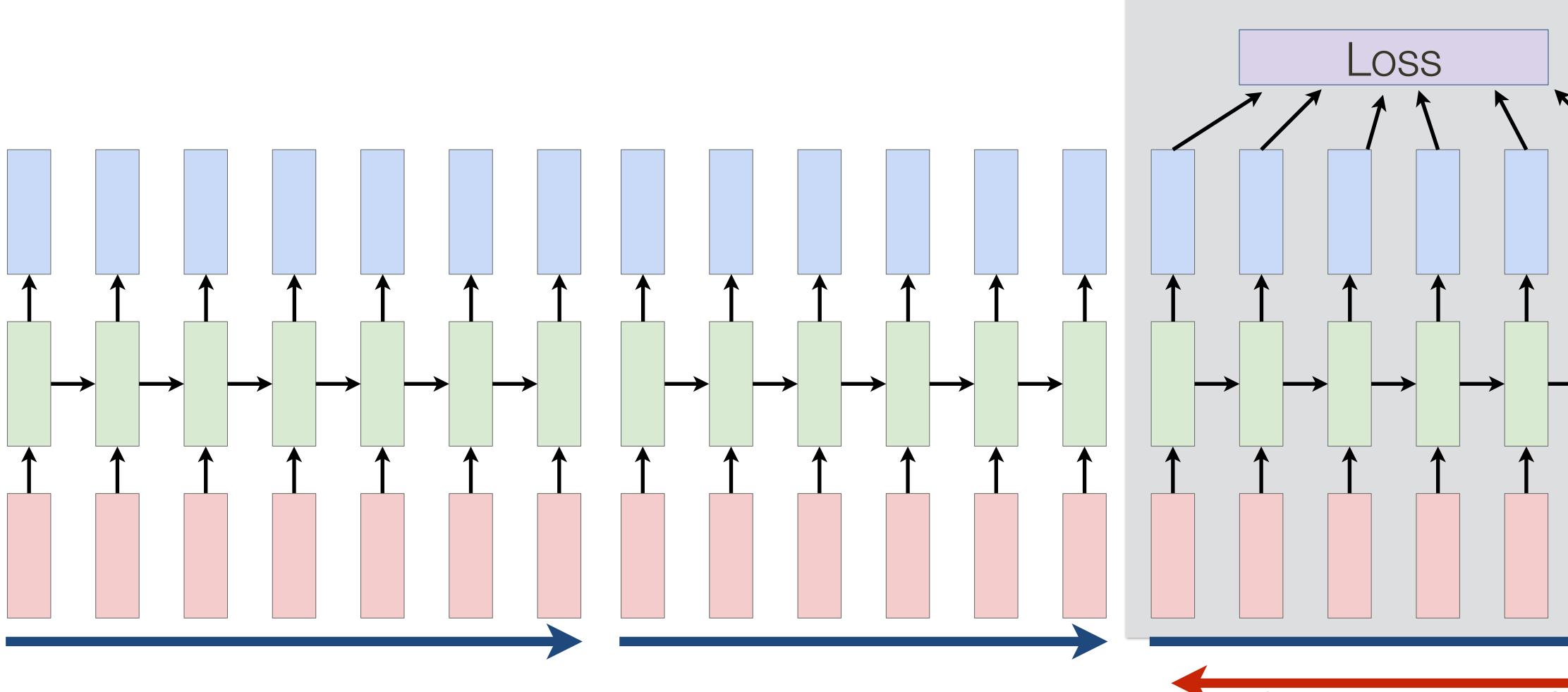
Run backwards and forwards through (fixed length) chunks of the sequence, instead of the whole sequence



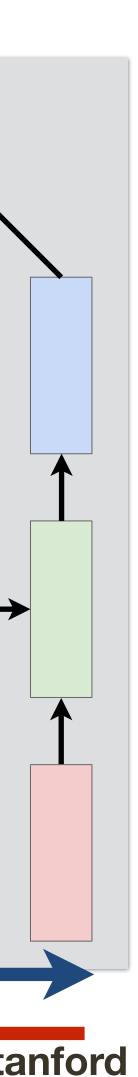
Carry hidden states forward, but only BackProp through some smaller number of steps

Truncated BackProp Through Time

instead of the whole sequence



Run backwards and forwards through (fixed length) chunks of the sequence,



Learning to Write Like Shakespeare — Training **Decoder**

THE SONNETS

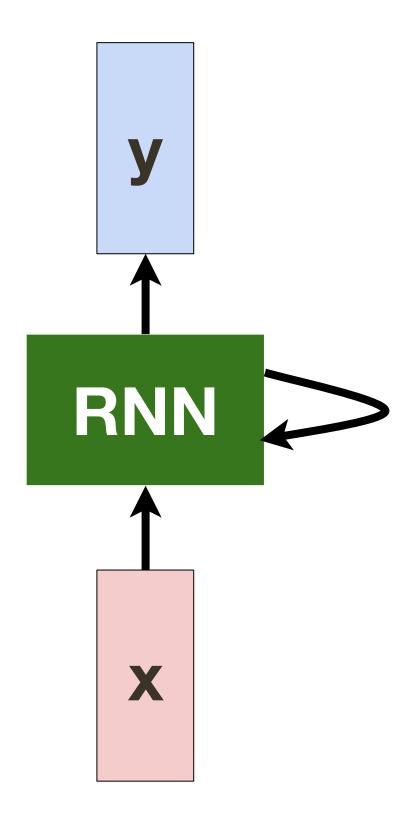
by William Shakespeare

From fairest creatures we desire increase, That thereby beauty's rose might never die, But as the riper should by time decease, His tender heir might bear his memory: But thou, contracted to thine own bright eyes, Feed'st thy light's flame with self-substantial fuel, Making a famine where abundance lies, Thyself thy foe, to thy sweet self too cruel: Thou that art now the world's fresh ornament, And only herald to the gaudy spring, Within thine own bud buriest thy content, And tender churl mak'st waste in niggarding:

Pity the world, or else this glutton be, To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow, And dig deep trenches in thy beauty's field, Thy youth's proud livery so gazed on now, Will be a tatter'd weed of small worth held: Then being asked, where all thy beauty lies, Where all the treasure of thy lusty days; To say, within thine own deep sunken eyes, Were an all-eating shame, and thriftless praise. How much more praise deserv'd thy beauty's use, If thou couldst answer 'This fair child of mine Shall sum my count, and make my old excuse,' Proving his beauty by succession thine!

This were to be new made when thou art old, And see thy blood warm when thou feel'st it cold.





Learning to Write Like Shakespeare ... after training a bit

at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e
plia tklrgd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

"Tmont thithey" fomesscerliund Keushey. Thom here sheulke, anmerenith ol sivh I lalterthend Bleipile shuwy fil on aseterlome coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

Aftair fall unsuch that the hall for Prince Velzonski's that me of her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort how, and Gogition is so overelical and ofter.

"Why do what that day," replied Natasha, and wishing to himself the fact the princess, Princess Mary was easier, fed in had oftened him. Pierre aking his soul came to the packs and drove up his father-in-law women.

train more

train more

train more

* slide from Fei-Dei Li, Justin Johnson, Serena Yeung, cs231n Stanford

nford

Learning to Write Like Shakespeare ... after training

PANDARUS:

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death, I should not sleep.

Second Senator:

They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish The earth and thoughts of many states.

DUKE VINCENTIO: Well, your wit is in the care of side and that.

```
Second Lord:
They would be ruled after this chamber, and
my fair nues begun out of the fact, to be conveyed,
Whose noble souls I'll have the heart of the wars.
```

Clown: Come, sir, I will make did behold your worship.

VIOLA: I'll drink it.

VIOLA:

Why, Salisbury must find his flesh and thought That which I am not aps, not a man and in fire, To show the reining of the raven and the wars To grace my hand reproach within, and not a fair are hand, That Caesar and my goodly father's world; When I was heaven of presence and our fleets, We spare with hours, but cut thy council I am great, Murdered and by thy master's ready there My power to give thee but so much as hell: Some service in the noble bondman here, Would show him to her wine.

KING LEAR:

O, if you were a feeble sight, the courtesy of your law, Your sight and several breath, will wear the gods With his heads, and my hands are wonder'd at the deeds, So drop upon your lordship's head, and your opinion Shall be against your honour.

Learning Code

```
static void do_command(struct seq_file *m, void *v)
  int column = 32 << (cmd[2] & 0x80);</pre>
  if (state)
    cmd = (int)(int_state ^ (in_8(&ch->ch_flags) & Cmd) ? 2 : 1);
  else
    seq = 1;
  for (i = 0; i < 16; i++) {</pre>
    if (k & (1 << 1))
      pipe = (in_use & UMXTHREAD_UNCCA) +
        ((count & 0x0000000fffffff8) & 0x000000f) << 8;
    if (count == 0)
      sub(pid, ppc_md.kexec_handle, 0x2000000);
    pipe_set_bytes(i, 0);
  /* Free our user pages pointer to place camera if all dash */
  subsystem_info = &of_changes[PAGE_SIZE];
  rek_controls(offset, idx, &soffset);
  /* Now we want to deliberately put it to device */
  control_check_polarity(&context, val, 0);
  for (i = 0; i < COUNTER; i++)
    seq_puts(s, "policy ");
}
```

Trained on entire source code of Linux kernel



DopeLearning: Computational Approach to Rap Lyrics

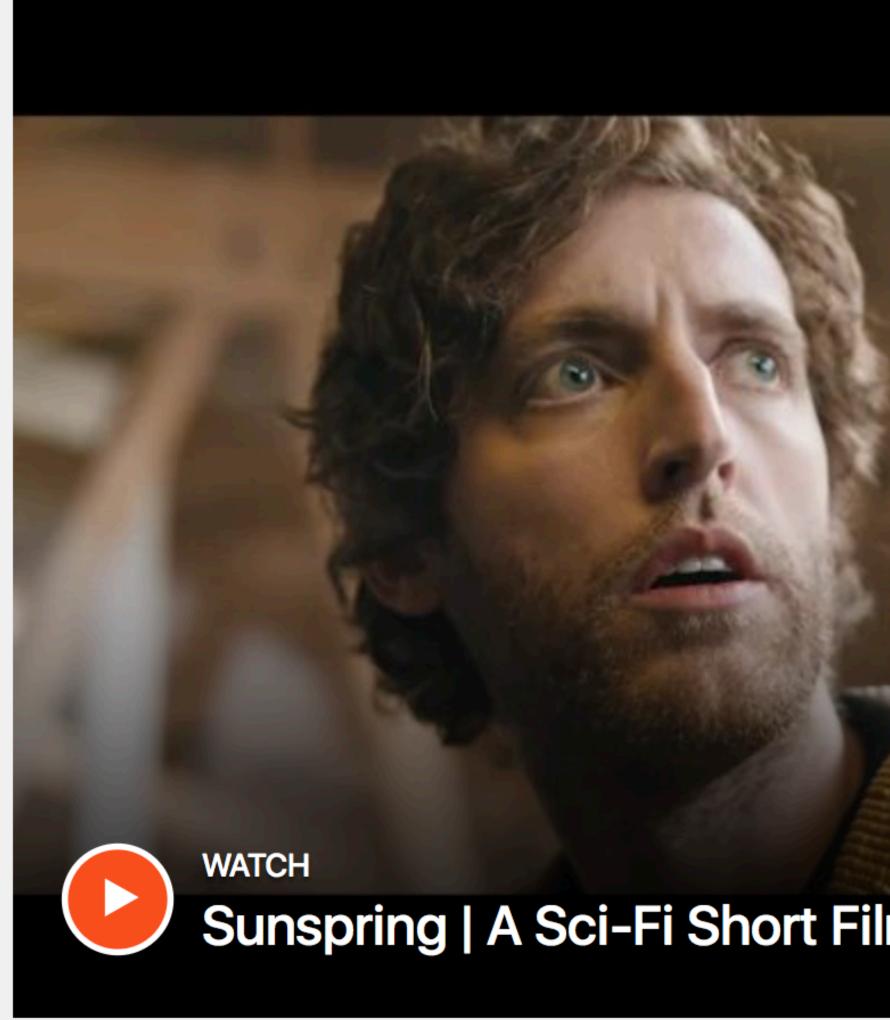
Everybody got one And all the pretty mommies want some And what i told you all was But you need to stay such do not touch They really do not want you to vote what do you condone Music make you lose control What you need is right here ahh oh This is for you and me I had to dedicate this song to you Mami Now I see how you can be I see u smiling i kno u hattig Best I Eva Had x4 That I had to pay for Do I have the right to take yours Trying to stay warm

- (2 Chainz Extremely Blessed)
- (Mos Def Undeniable)
- (Lil Wayne Welcome Back)
- (Common Heidi Hoe)
- (KRS One The Mind)
- (Cam'ron Bubble Music)
- (Missy Elliot Lose Control)
- (Wiz Khalifa Right Here)
- (Missy Elliot Hit Em Wit Da Hee)
- (Fat Joe Bendicion Mami)
- (Lil Wayne How To Hate)
- (Wiz Khalifa Damn Thing)
- (Nicki Minaj Best I Ever Had)
- (Ice Cube X Bitches)
- (Common Retrospect For Life)
- (Everlast 2 Pieces Of Drama)

[Malmi et al., KDD 2016]



Sunspring: First movie generated by Al

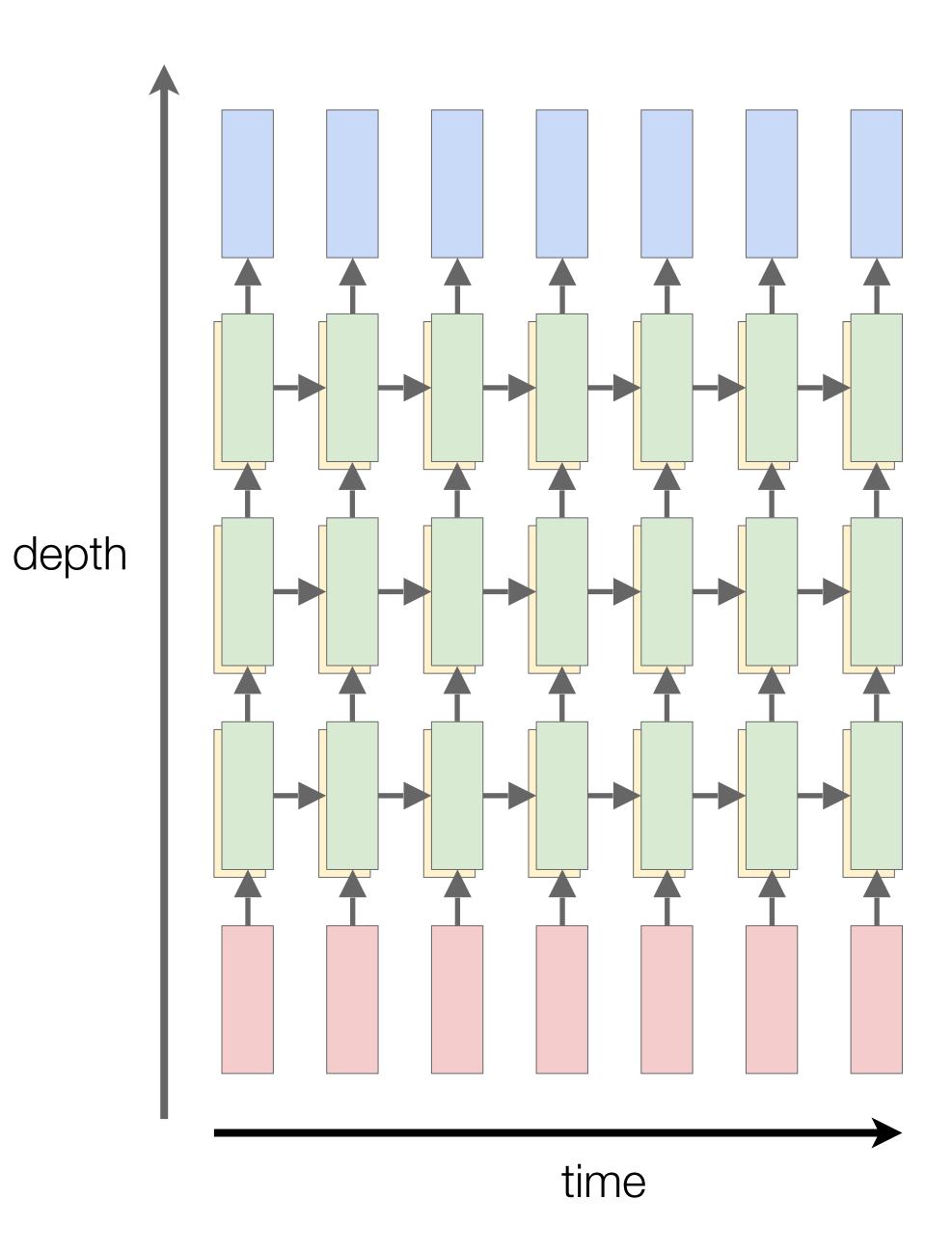


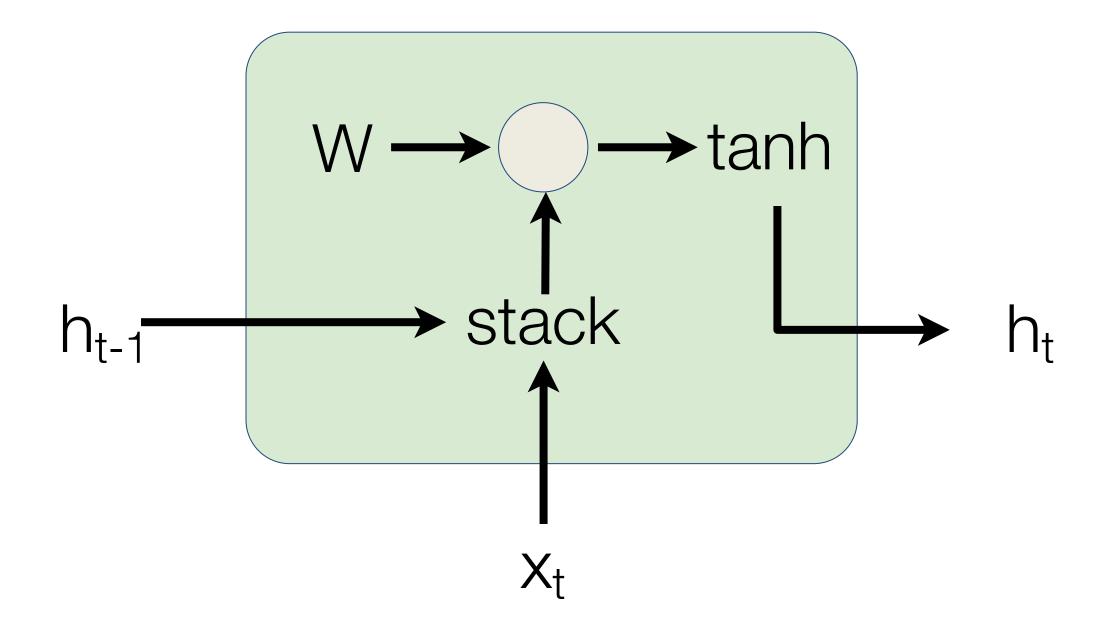
Sunspring, a short science fiction movie written entirely by AI, debuts exclusively on Ars today.

Sunspring | A Sci-Fi Short Film Starring Thomas Middleditch

Multilayer RNNs

$$\begin{aligned} h_t^l &= \tanh W^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix} \\ h \in \mathbb{R}^n, \qquad W^l \ [n \times 2n] \end{aligned}$$

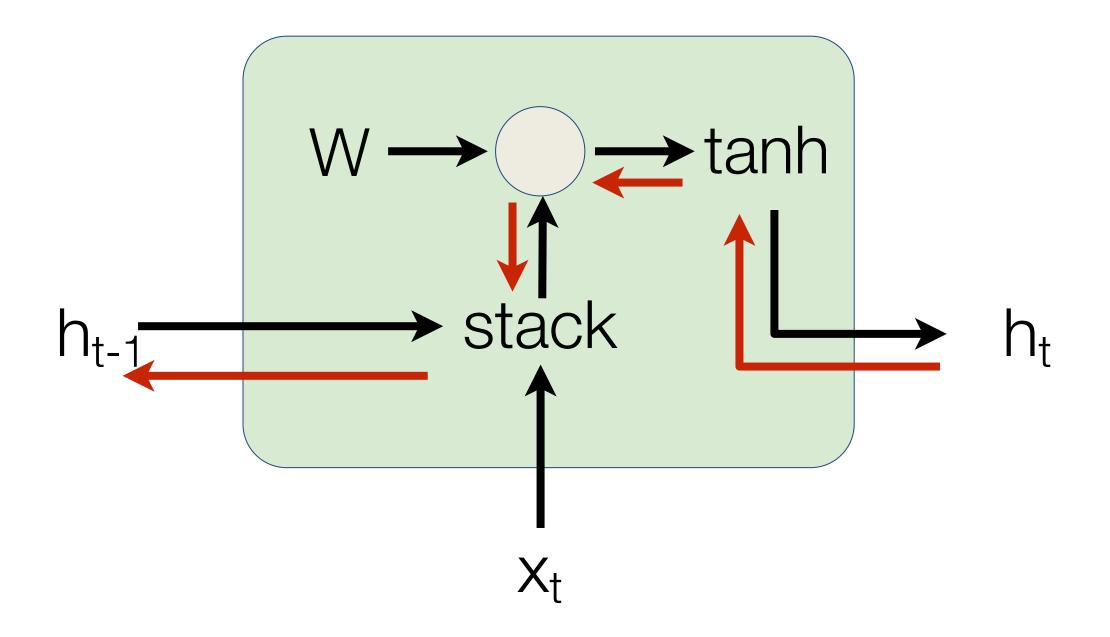




[Bengio et al., 1994] [Pascanu et al., ICML 2013]

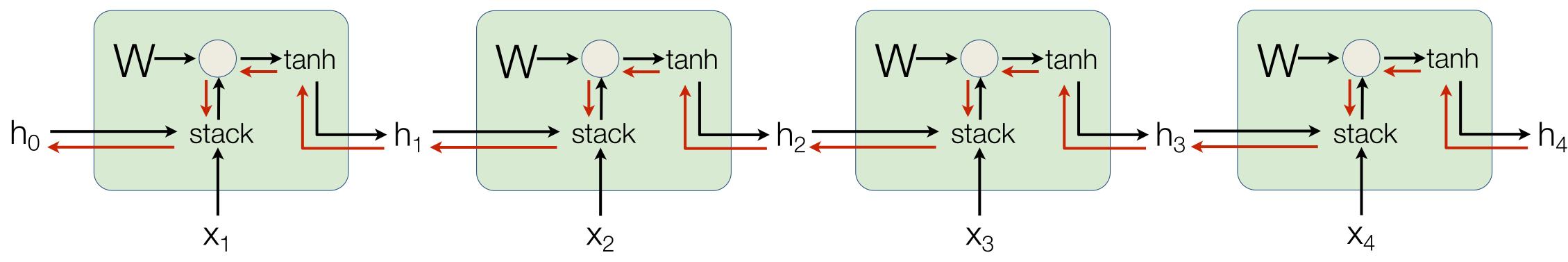
$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

Backpropagation from ht to ht-1 multiplies by W (actually W_{hh}^{T})



[Bengio et al., 1994] [Pascanu et al., ICML 2013]

$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

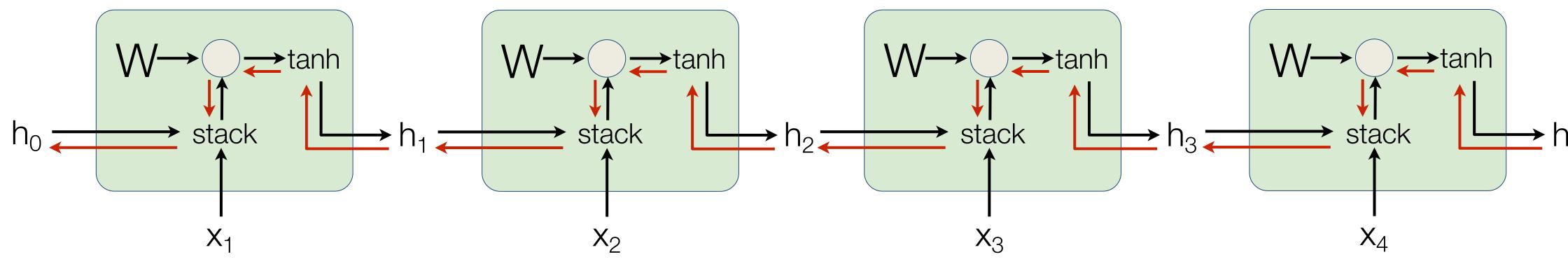


Computing gradient of h₀ involves many factors of W (and repeated tanh)

[Bengio et al., 1994] [Pascanu et al., ICML 2013]

* slide from Fei-Dei Li, Justin Johnson, Serena Yeung, cs231n Stanford

4



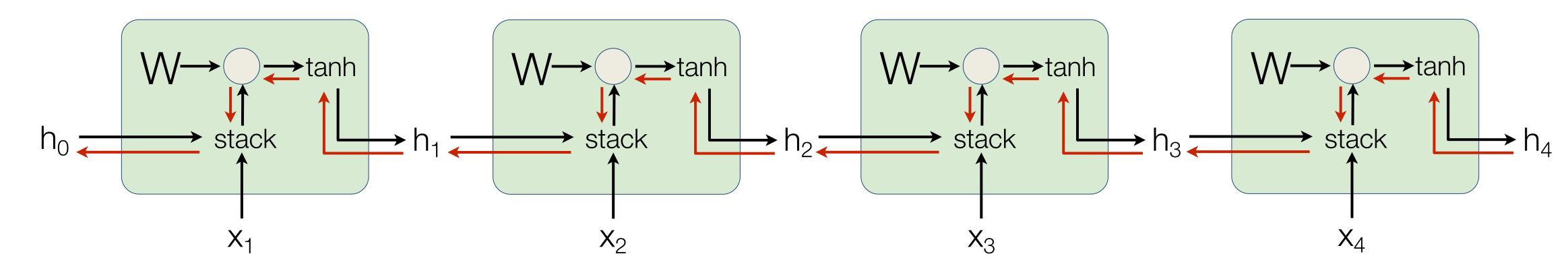
Computing gradient of h₀ involves many factors of W (and repeated tanh)

Largest singular value > 1: **Exploding gradients**

Vanishing gradients

[Bengio et al., 1994] [Pascanu et al., ICML 2013]

Largest singular value < 1:



Computing gradient of h₀ involves many factors of W (and repeated tanh)

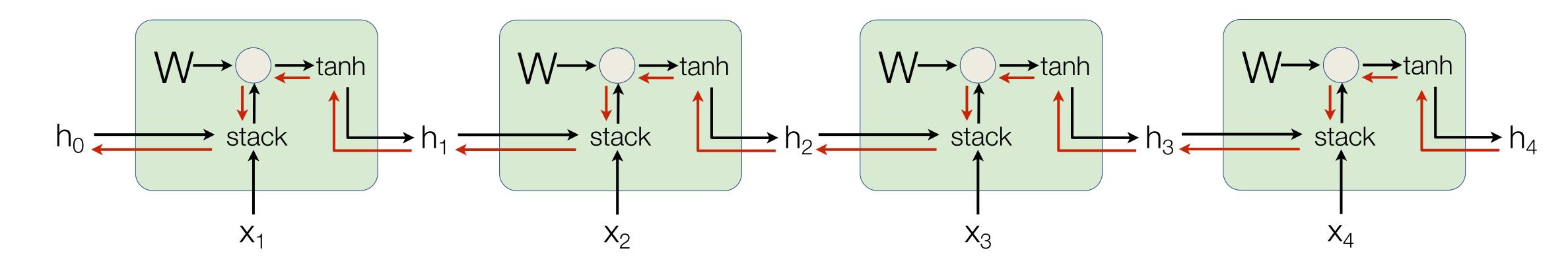
Largest singular value > 1: **Exploding gradients**

Largest singular value < 1: Vanishing gradients

[Bengio et al., 1994] [Pascanu et al., ICML 2013]

Gradient clipping: Scale gradient if its norm is too big

> grad_norm = np.sum(grad * grad) if grad_norm > threshold: grad *= (threshold / grad_norm)



Computing gradient of h₀ involves many factors of W (and repeated tanh)

Exploding gradients

Vanishing gradients

[Bengio et al., 1994] [Pascanu et al., ICML 2013]

Largest singular value > 1:

Largest singular value < 1: Change RNN architecture

Long-Short Term Memory (LSTM)

Vanilla RNN

$$h_t = \tanh\left(W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}\right)$$



LSTM

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$



[Hochreiter and Schmidhuber, NC **1977**]





Long-Short Term Memory (LSTM)

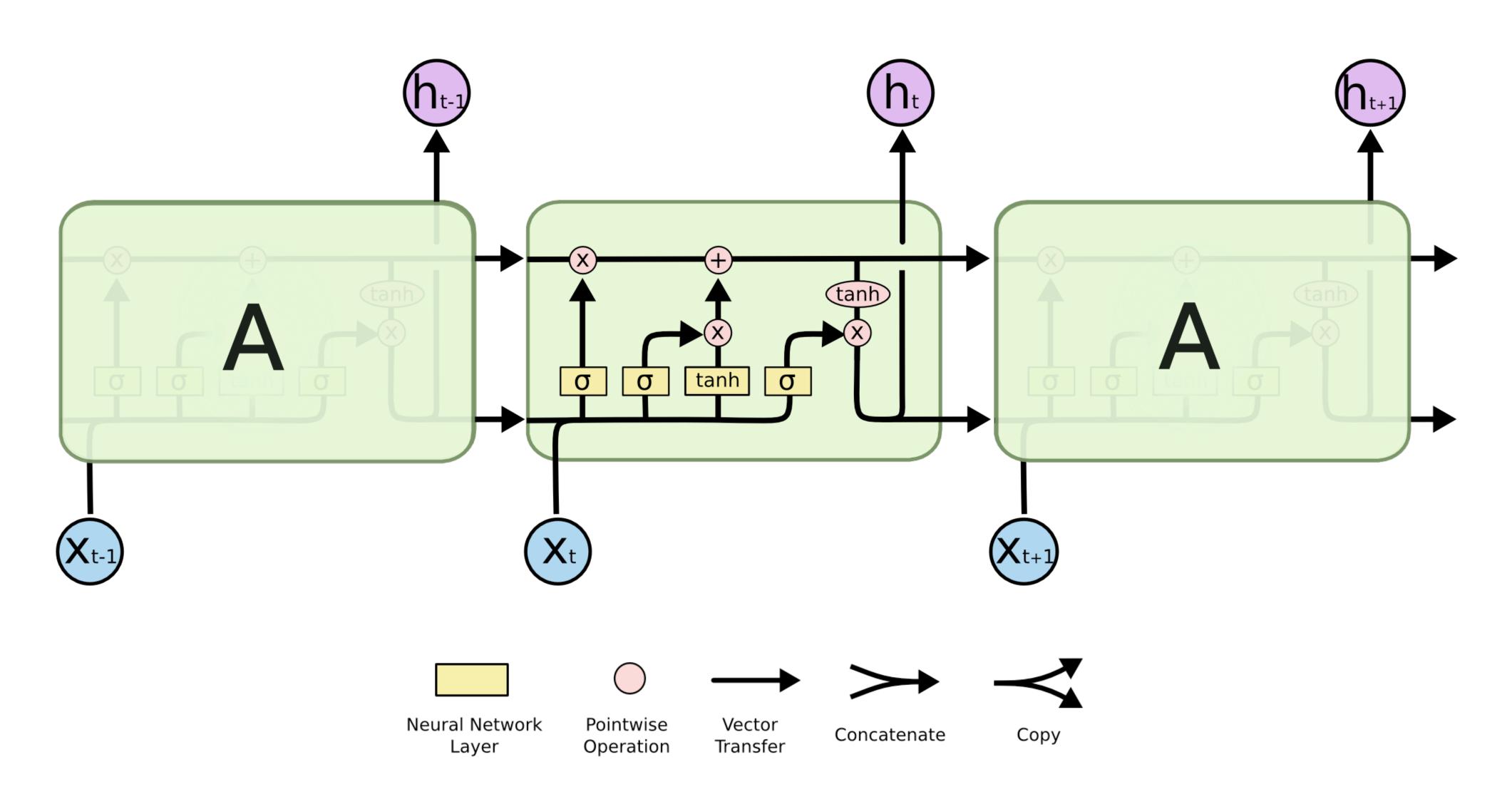


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)



Long-Short Term Memory (LSTM)

Cell state / **memory**

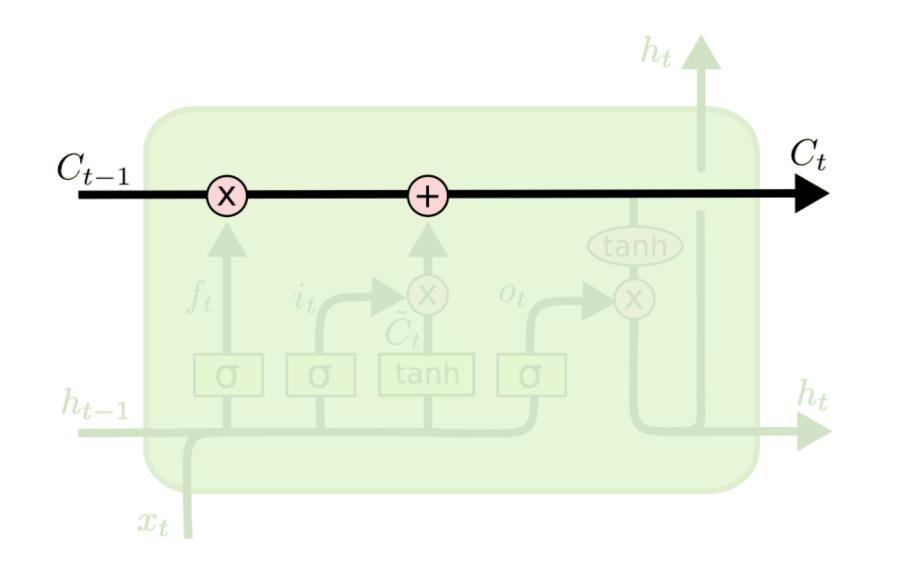


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

LSTM Intuition: Forget Gate

Should we continue to **remember** this "bit" of information or not?

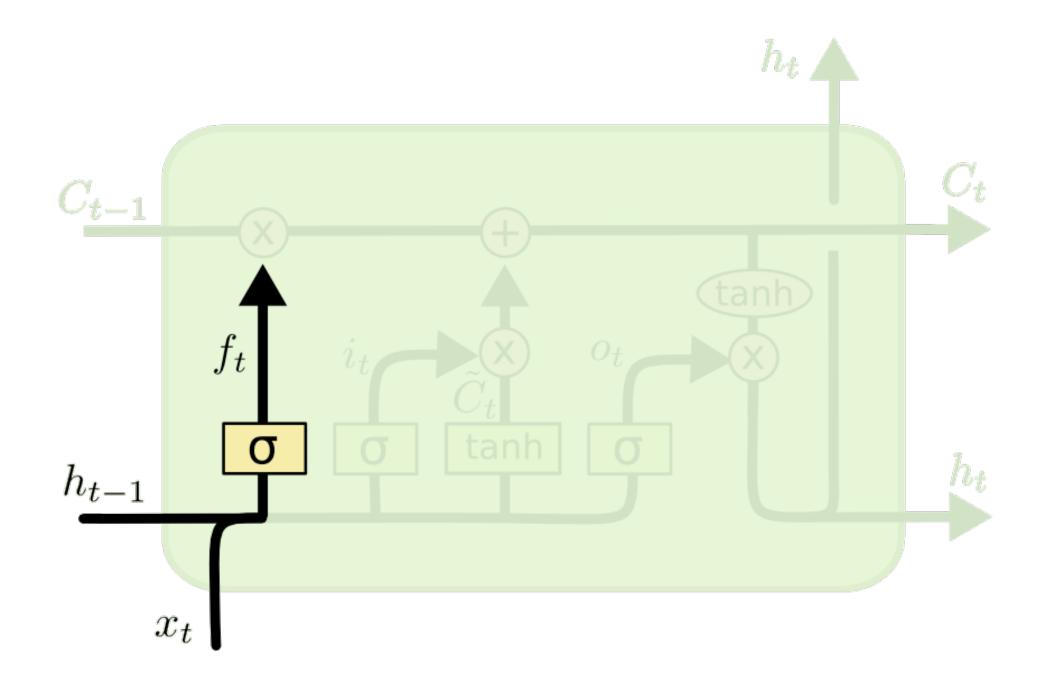
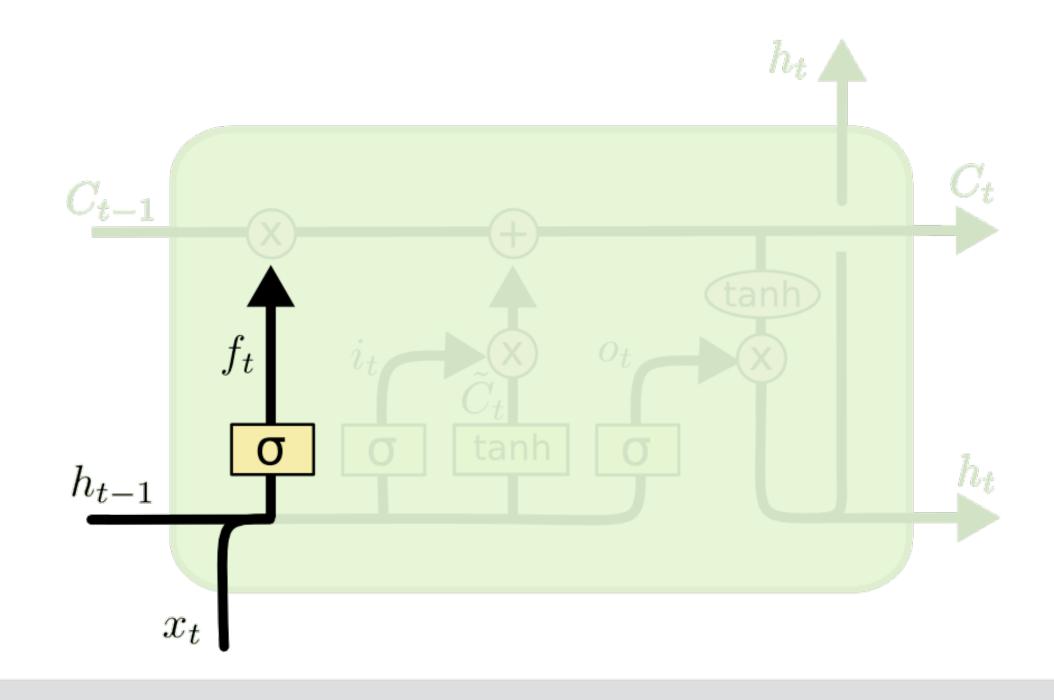


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

$f_t = \sigma \left(W_f \cdot [h_{t-1}, x_t] + b_f \right)$

LSTM Intuition: Forget Gate

Should we continue to **remember** this "bit" of information or not?



Intuition: memory and forget gate output multiply, output of forget gate can be though of as binary (0 or 1) anything x 1 = anything (remember) anything x 0 = 0 (forget)

Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

$f_t = \sigma \left(W_f \cdot [h_{t-1}, x_t] + b_f \right)$

LSTM Intuition: Input Gate

Should we **update** this "bit" of information or not? If yes, then what should we **remember**?

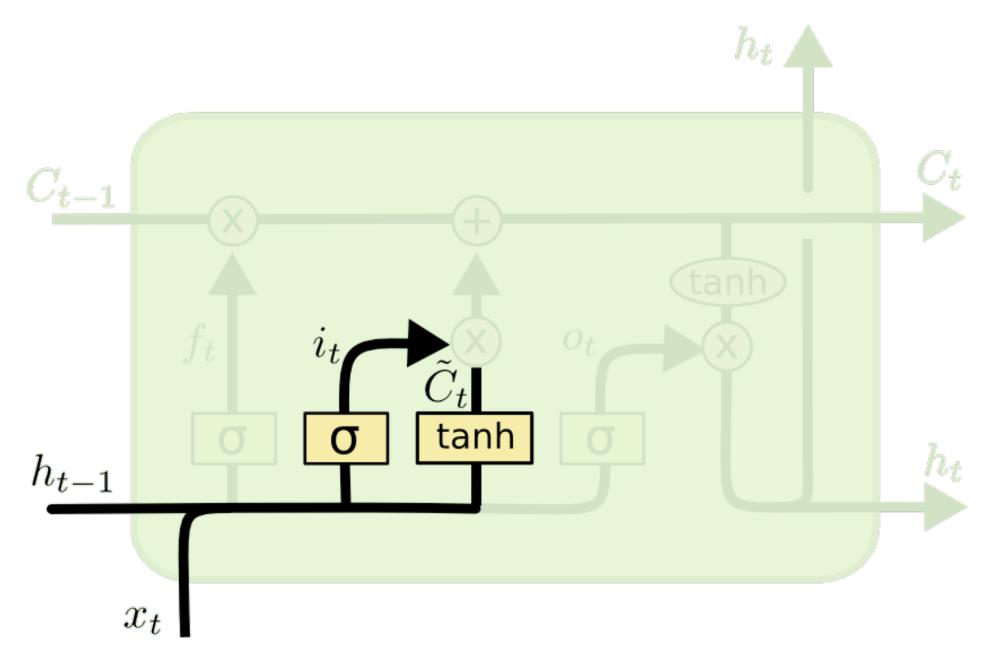


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] + b_i \right)$$
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

* slide from Dhruv Batra

/ Batra

LSTM Intuition: Memory Update

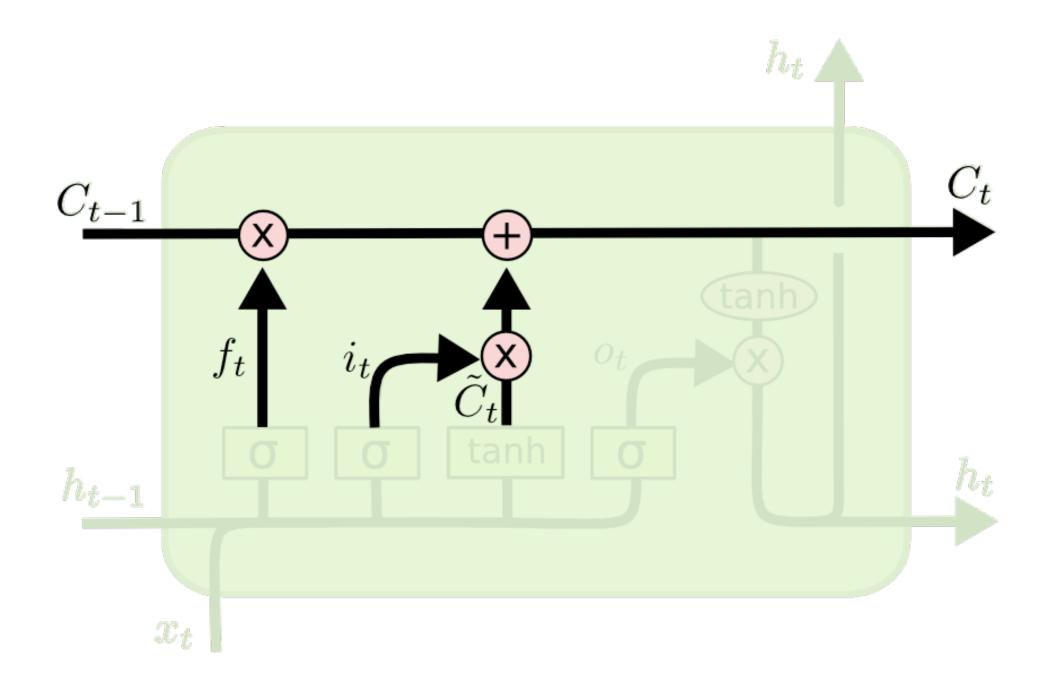


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

Forget what needs to be forgotten + memorize what needs to be remembered

$C_t = f_t * C_{t-1} + i_t * C_t$





LSTM Intuition: Output Gate

Should we output this bit of information (e.g., to "deeper" LSTM layers)?

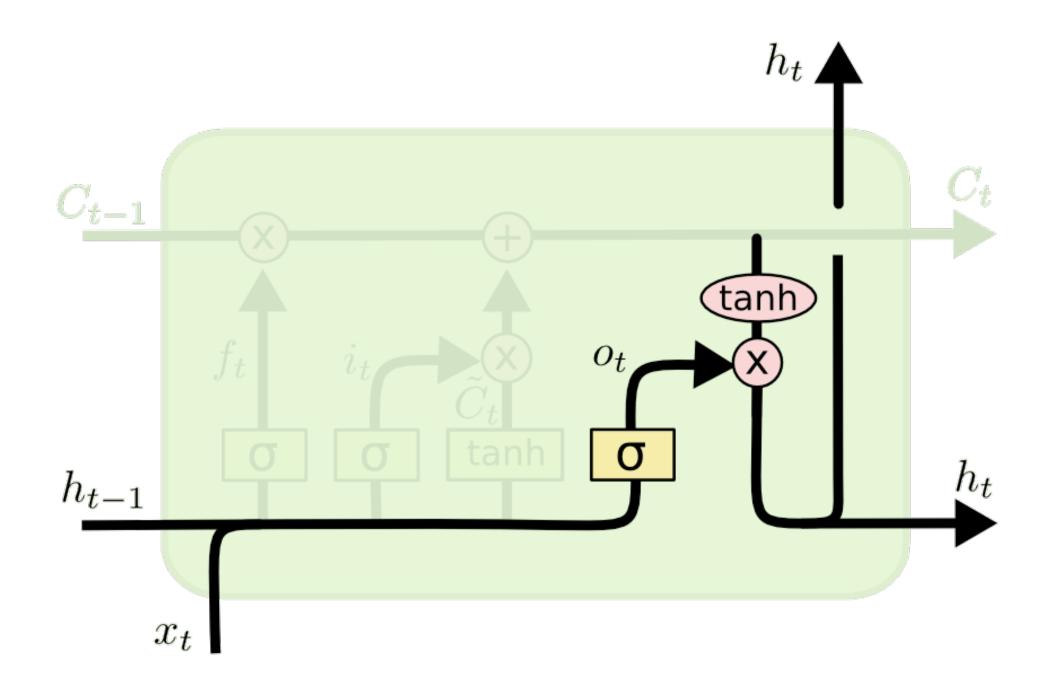


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

$o_t = \sigma \left(W_o \left[h_{t-1}, x_t \right] + b_o \right)$ $h_t = o_t * \tanh \left(C_t \right)$

* slide from Dhruv Batra

/ Batra

LSTM Intuition: Additive Updates

Backpropagation from c_t to c_{t-1} only elementwise multiplication by f, no matrix multiply by W

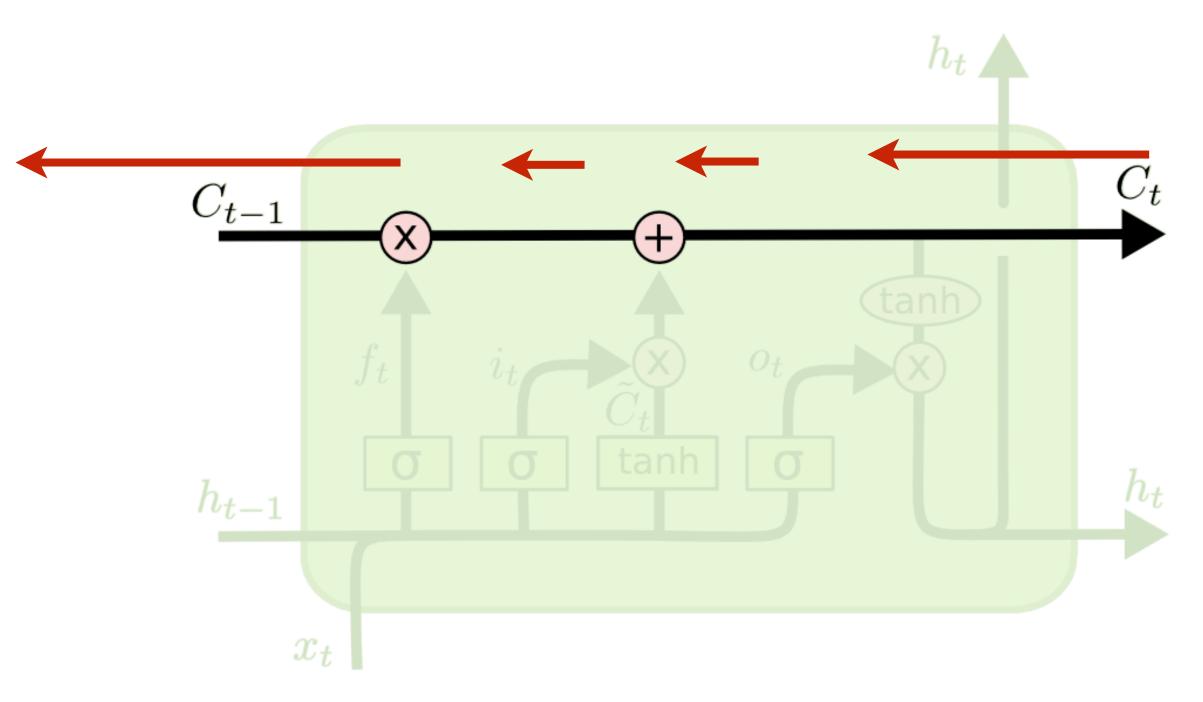


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

* slide from Dhruv Batra

/ Batra

LSTM Intuition: Additive Updates

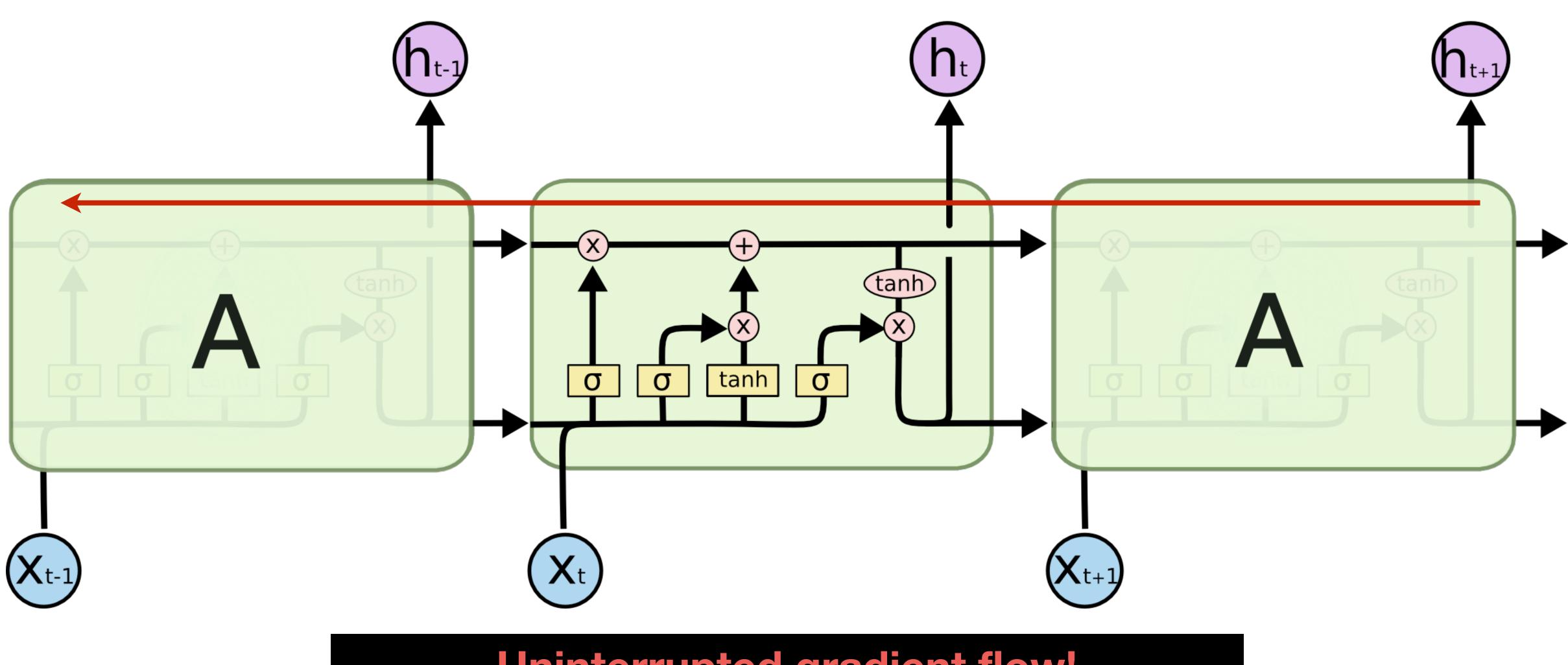


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

Uninterrupted gradient flow!

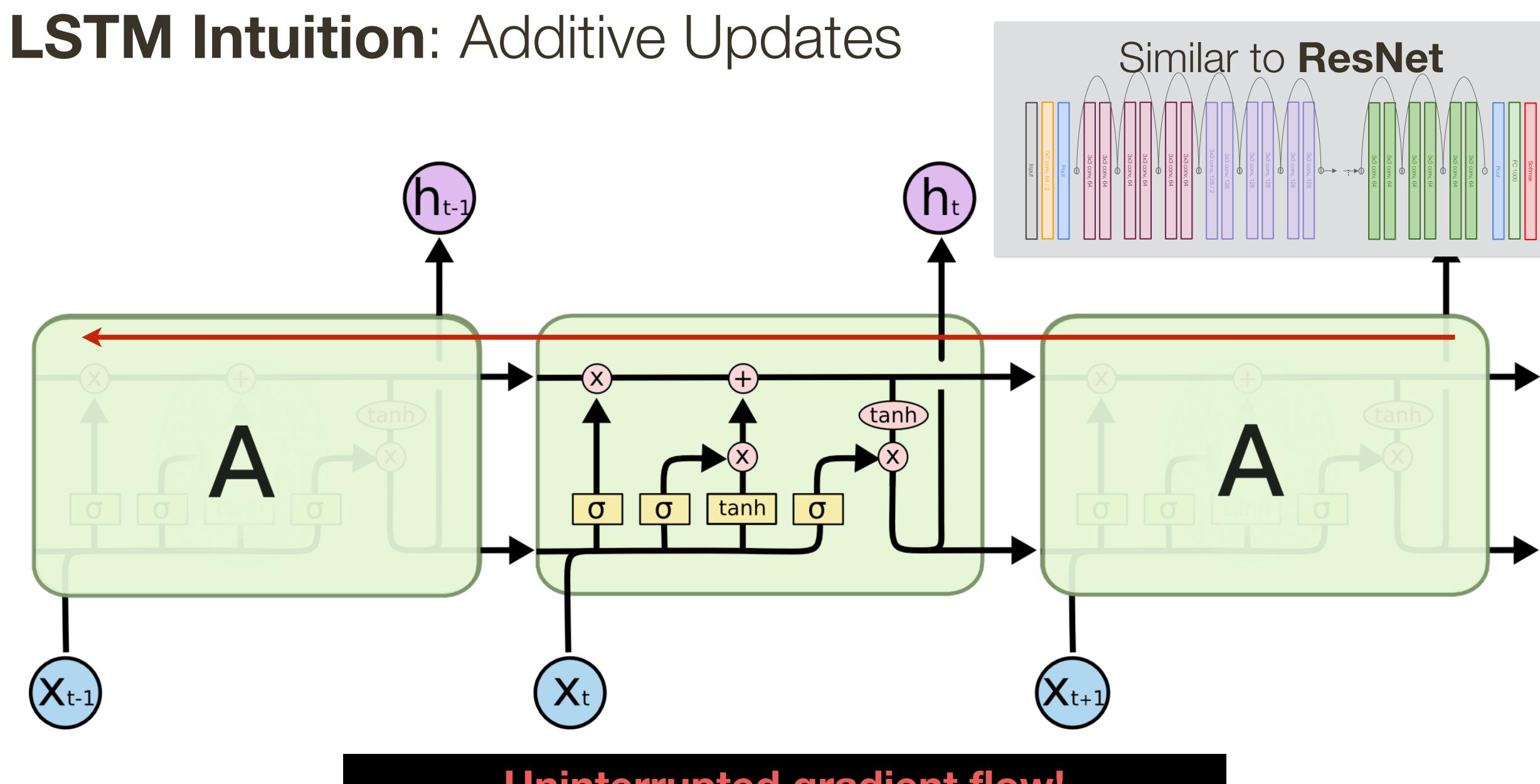


Image Credit: Christopher Olah (http://colah.github.io/posts/2015-08-Understanding-LSTMs/)

Uninterrupted gradient flow!

