



Topics in AI (CPSC 532S): Multimodal Learning with Vision, Language and Sound

Lecture 8: Language Models and RNNs

Language Models

Model the **probability of a sentence**; ideally be able to sample plausible sentences

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Simple **Language Models**: N-Grams

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Bi-gram Approximation:

$$p(w_{1:n}) = \prod_{k=1}^n p(w_k|w_{k-1})$$

N-gram Approximation:

$$p(w_{1:n}) = \prod_{k=1}^n p(w_k|w_{k-N+1:k-1})$$

Estimating **Probabilities**

N-gram conditional probabilities can be estimated based on raw concurrence counts in the observed sequences

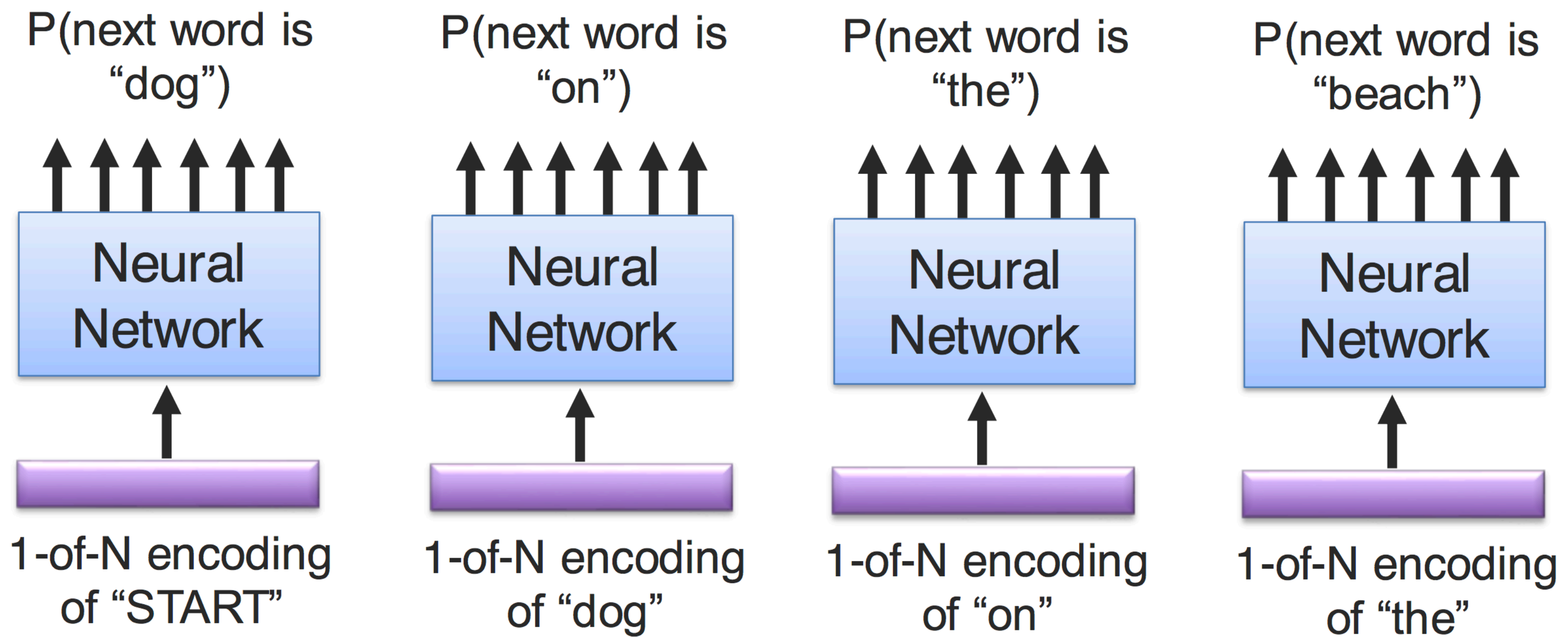
Bi-gram:

$$p(w_n | w_{n-1}) = \frac{C(w_{n-1}w_n)}{C(w_{n-1})}$$

N-gram:

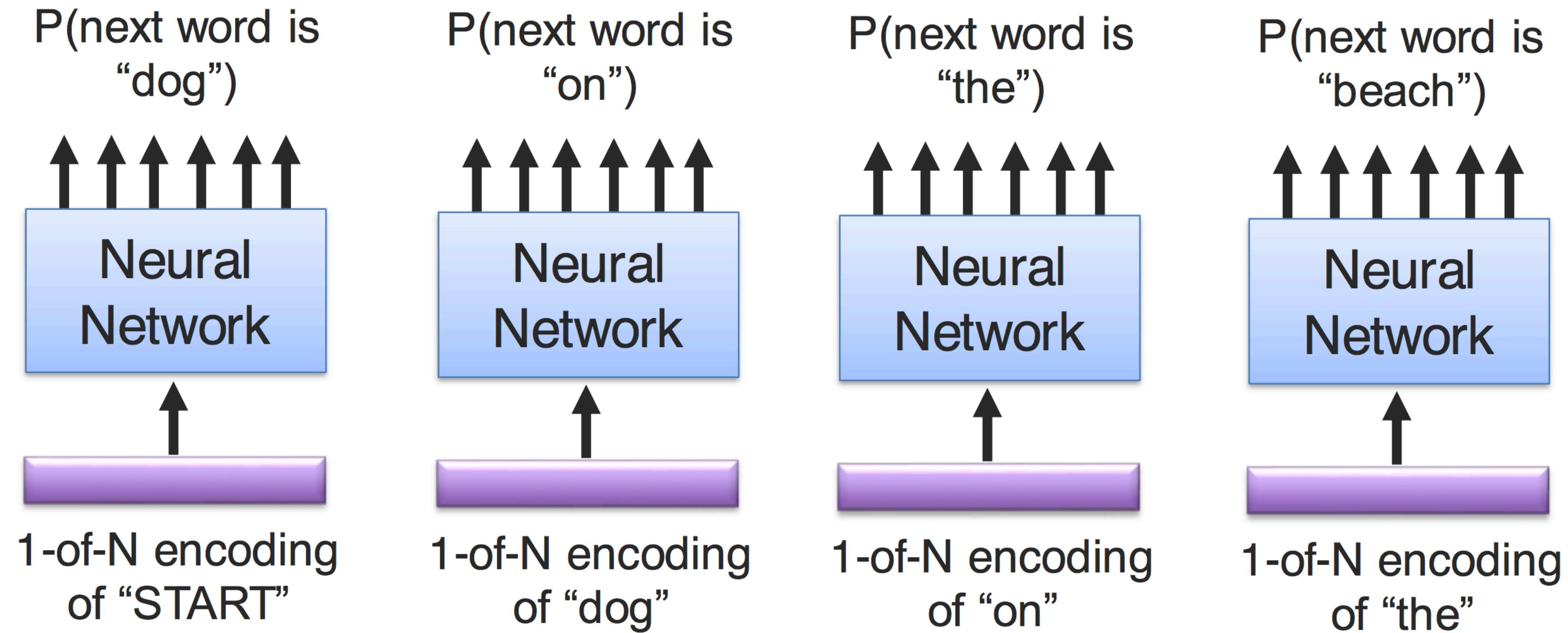
$$p(w_n | w_{n-N+1:n-1}) = \frac{C(w_{n-N+1:n-1}w_n)}{C(w_{n-N+1:n-1})}$$

Neural-based Unigram Language Mode



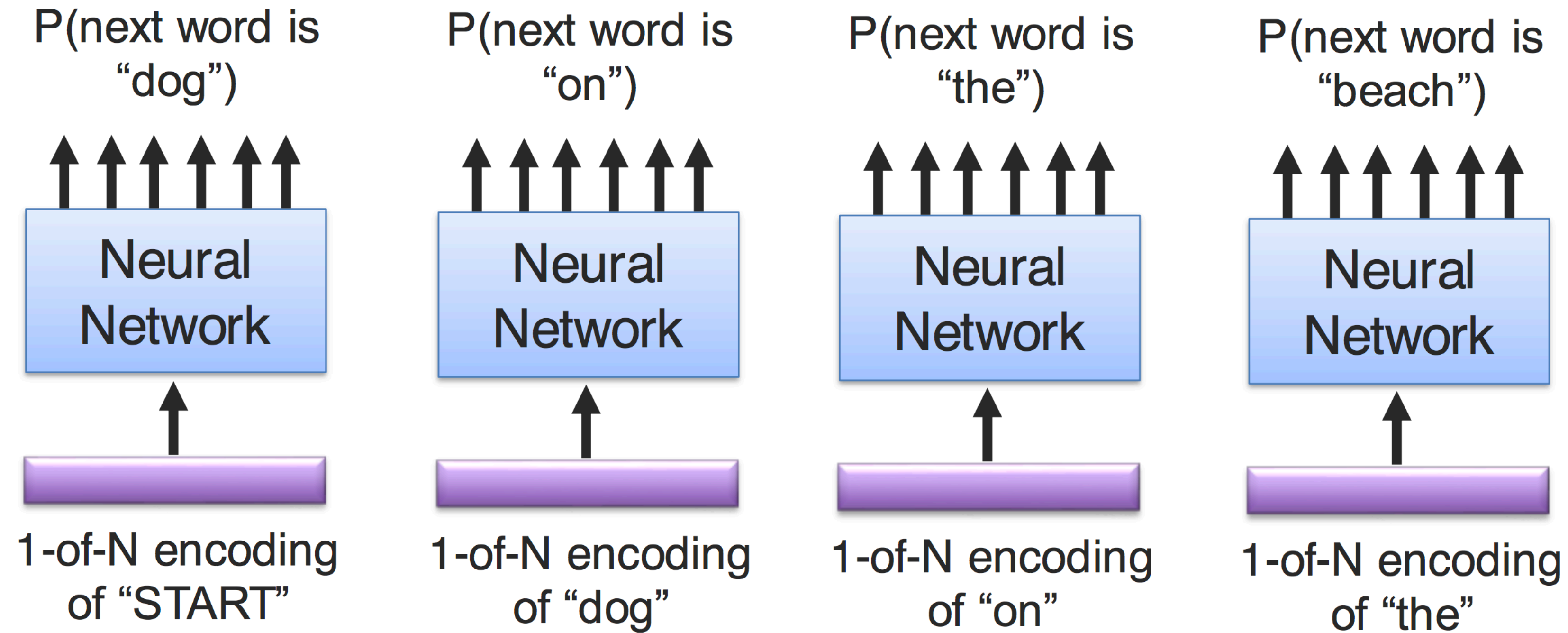
* Slides from Louis-Philippe Morency

Neural-based Unigram Language Mode



Problem: Does not model sequential information (too local)

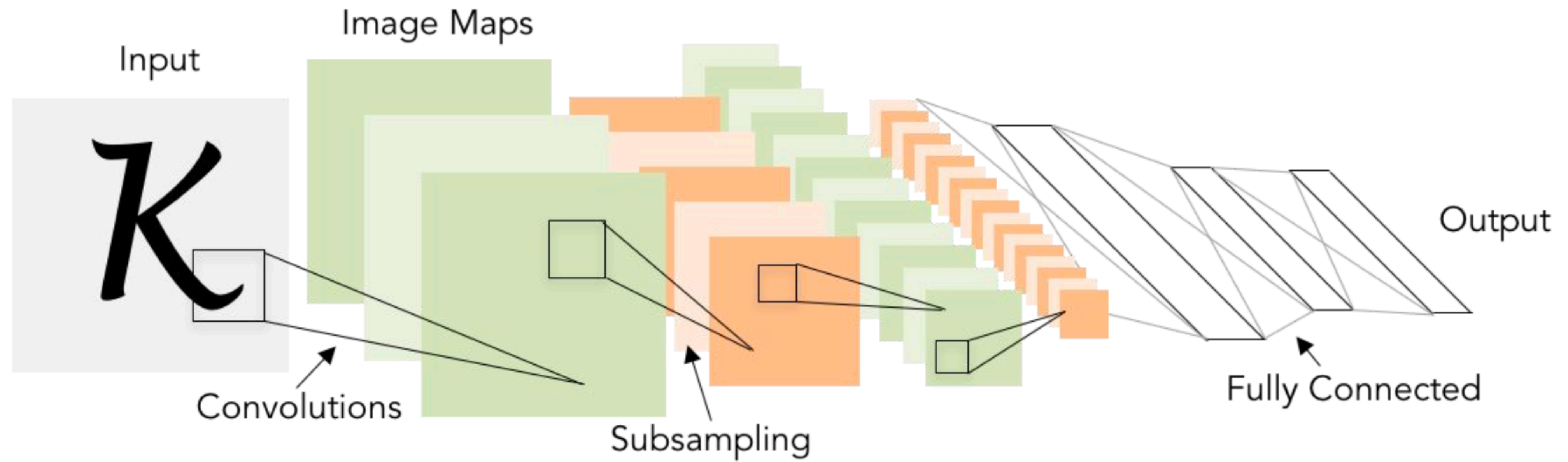
Neural-based Unigram Language Mode



Problem: Does not model sequential information (too local)

We need sequence modeling!

Sequence Modeling



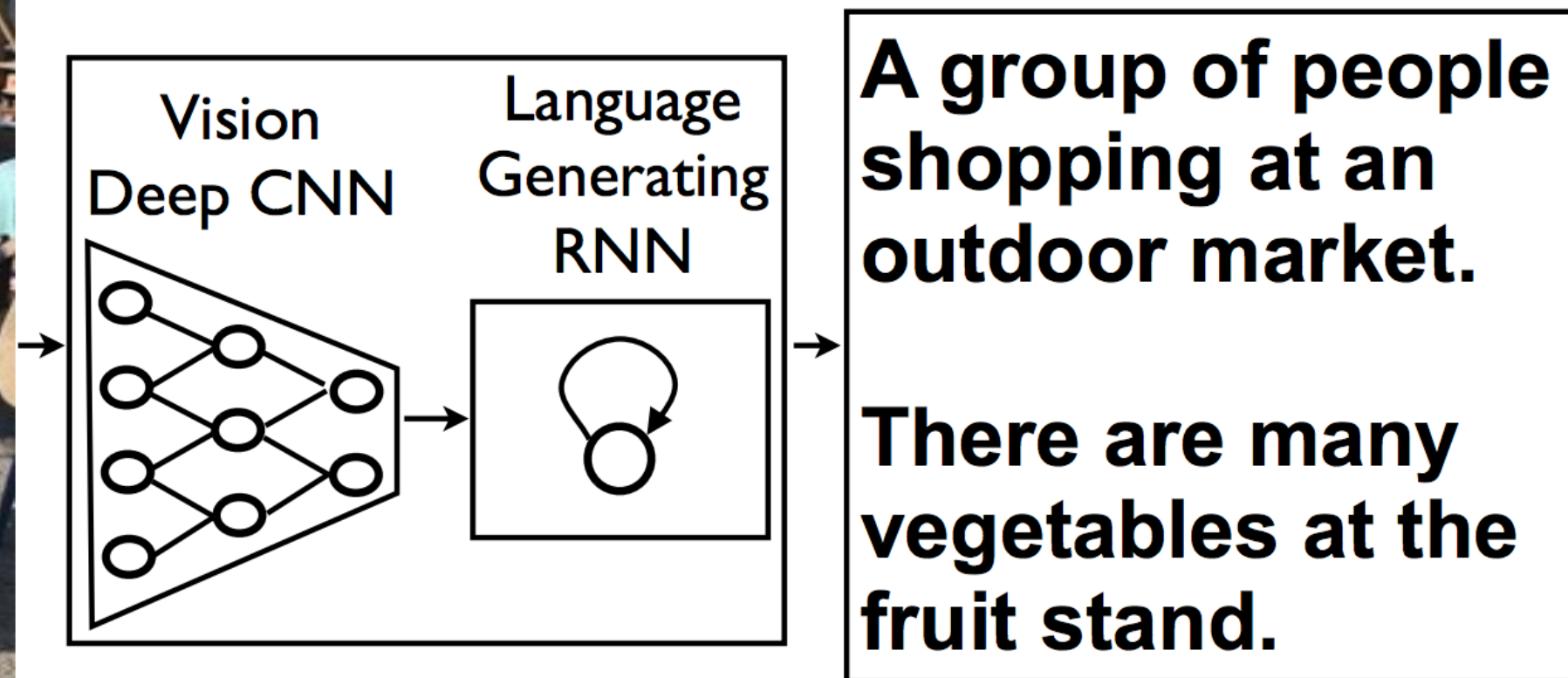
Why Model Sequences?

Foreign Minister. → FOREIGN MINISTER.

 → THE SOUND OF

$a_1=2$ $a_2=0$ $a_3=1$ $a_4=3$ $a_5=4$ $a_6=2$ $a_7=5$
 $x =$ bringen sie bitte das auto zurück .
 $y =$ please return the car .

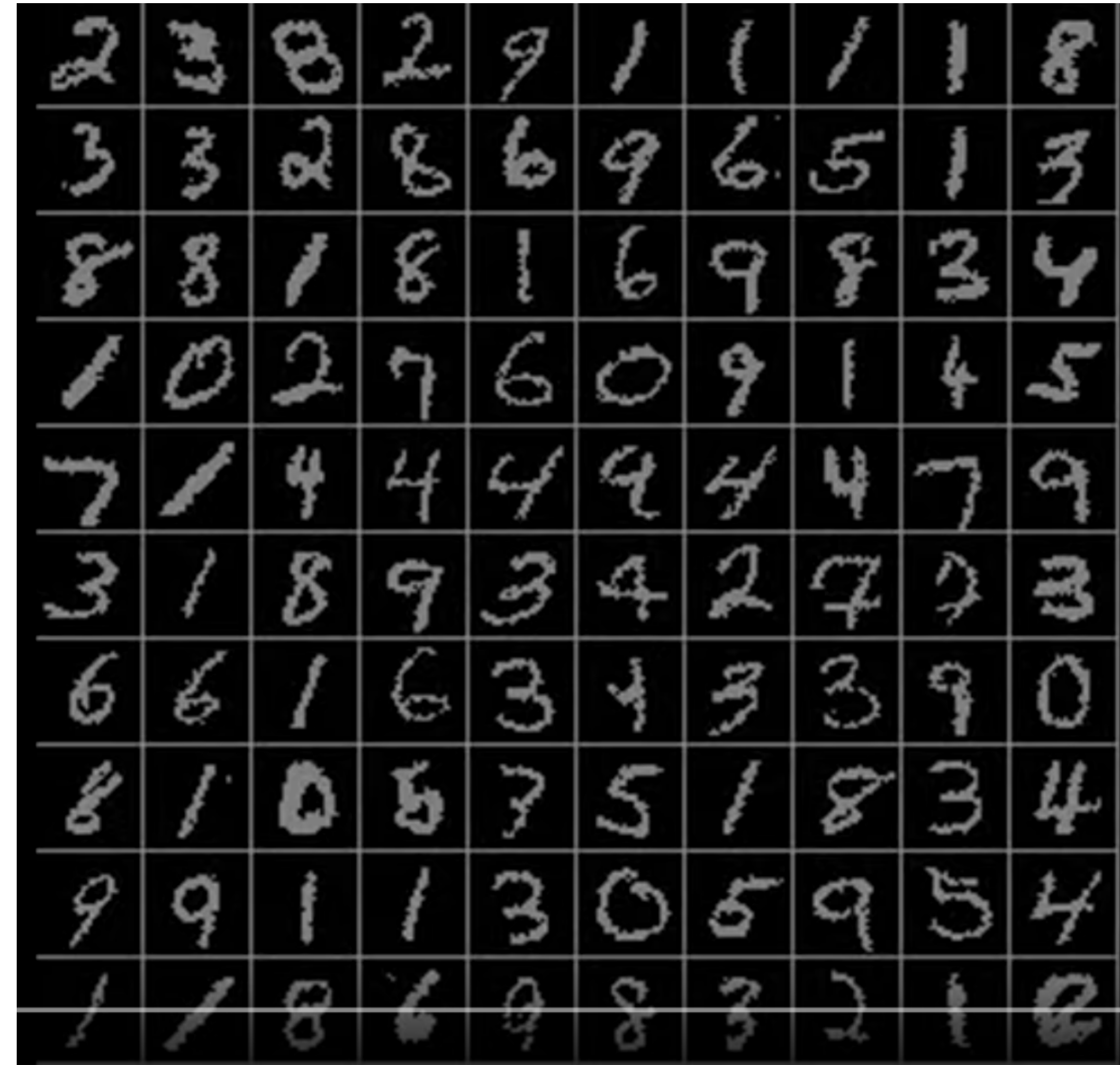
Multi-modal tasks



[Vinyals *et al.*, 2015]

Sequences where you don't expect them ...

Classify images by taking a series of “glimpses”

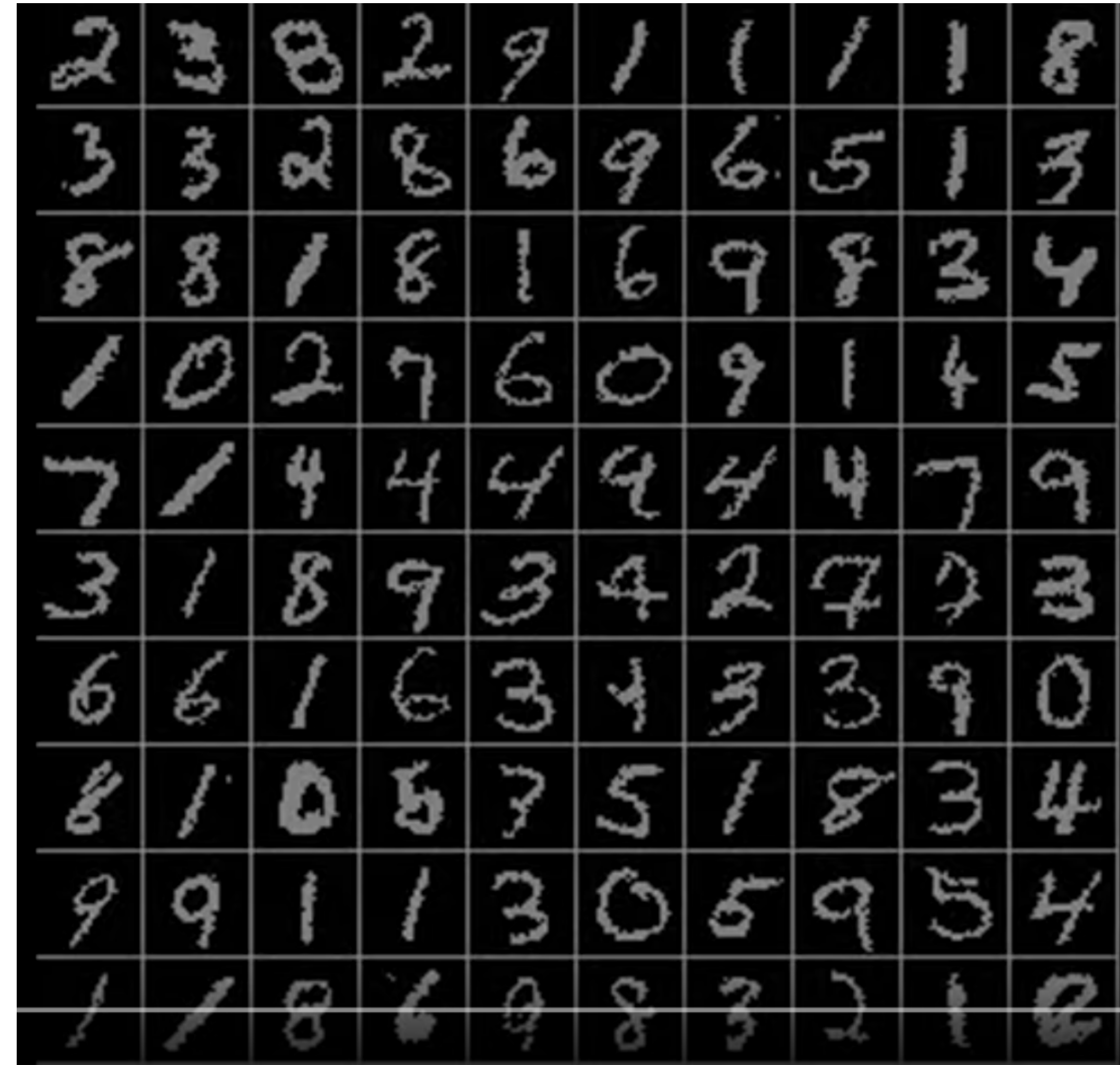


[Gregor et al., ICML 2015]

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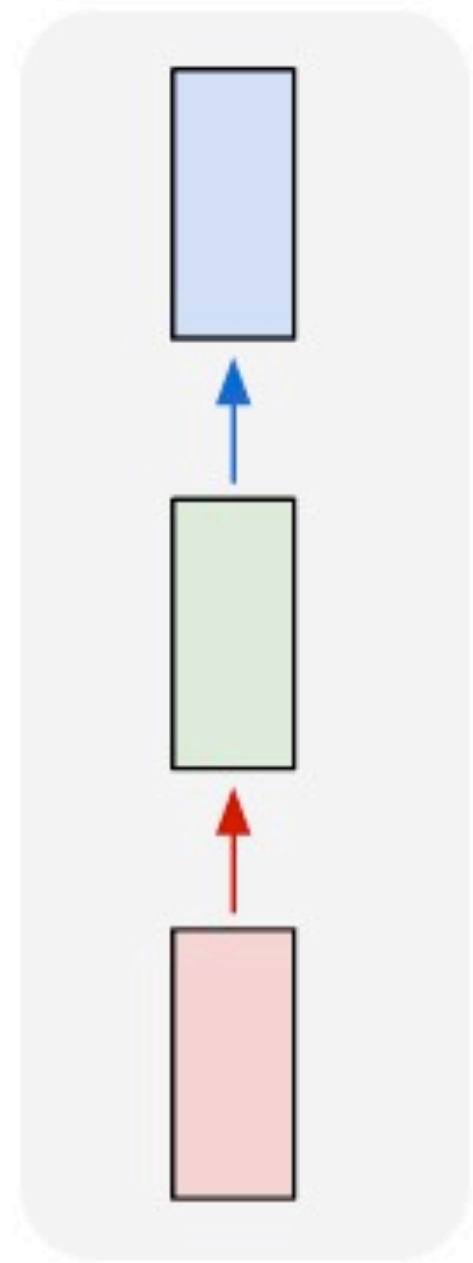


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Sequences in Inputs or Outputs?

one to one



Input: No sequence

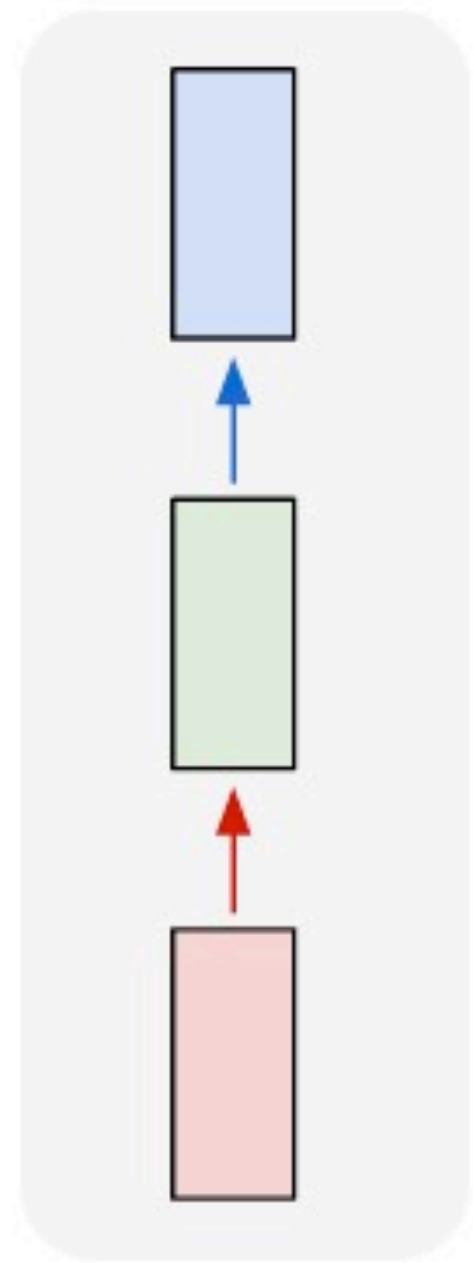
Output: No seq.

Example:

“standard”
classification /
regression problems

Sequences in Inputs or Outputs?

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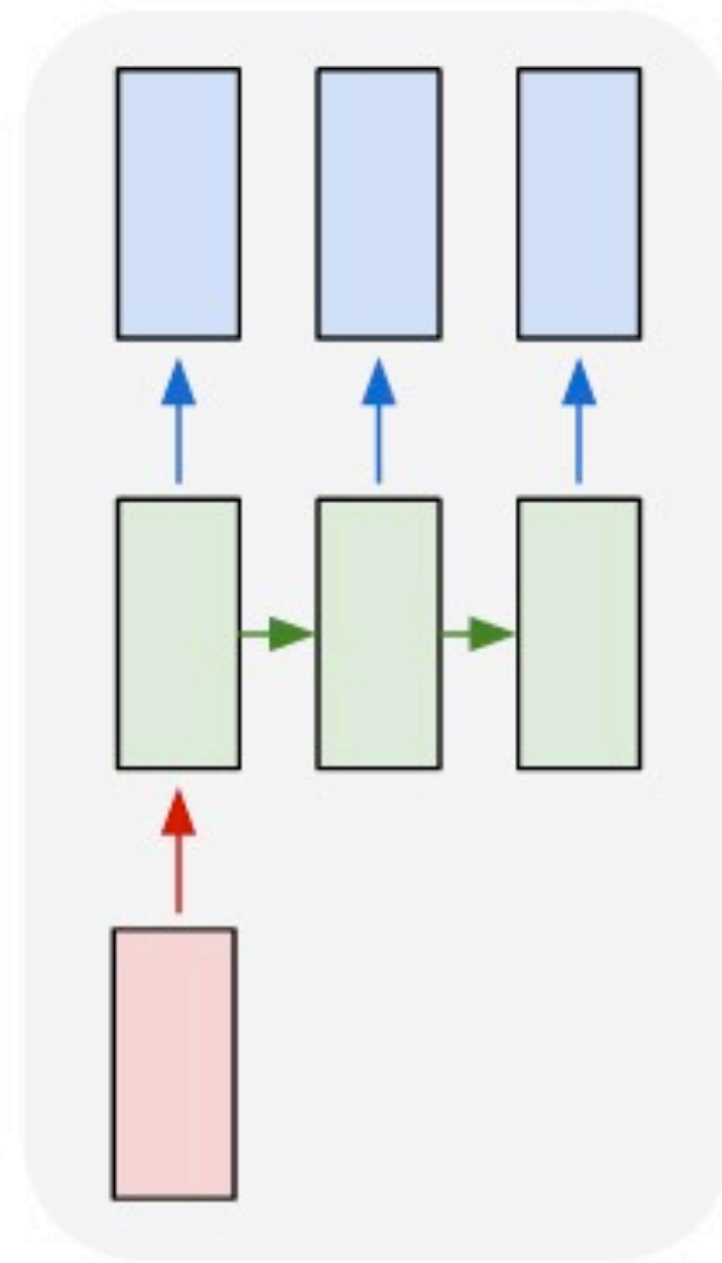
Input: No sequence

Output: No seq.

Example:

“standard”
classification /
regression problems

one to many



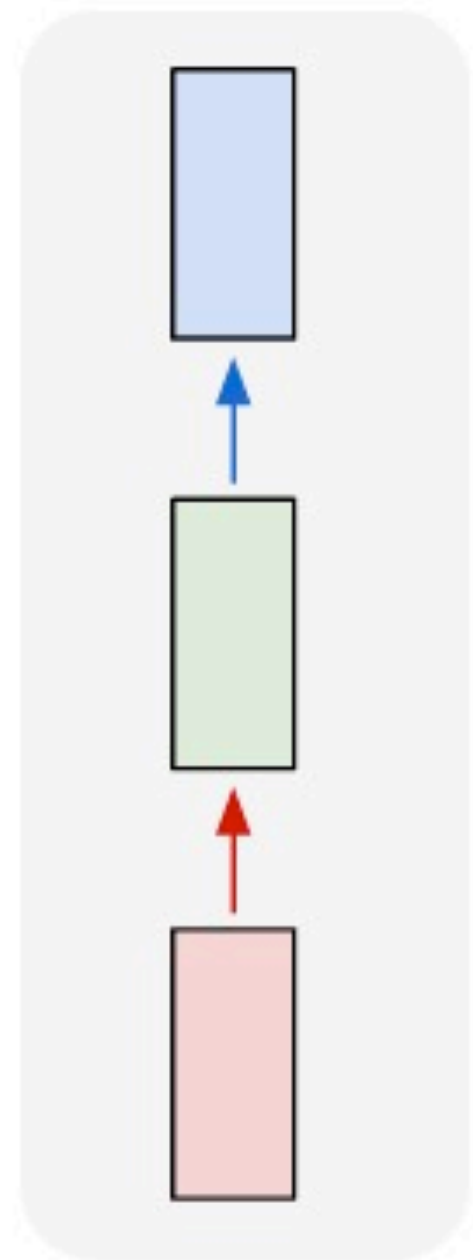
Input: No
sequence

Output:
Sequence

Example:
Im2Caption

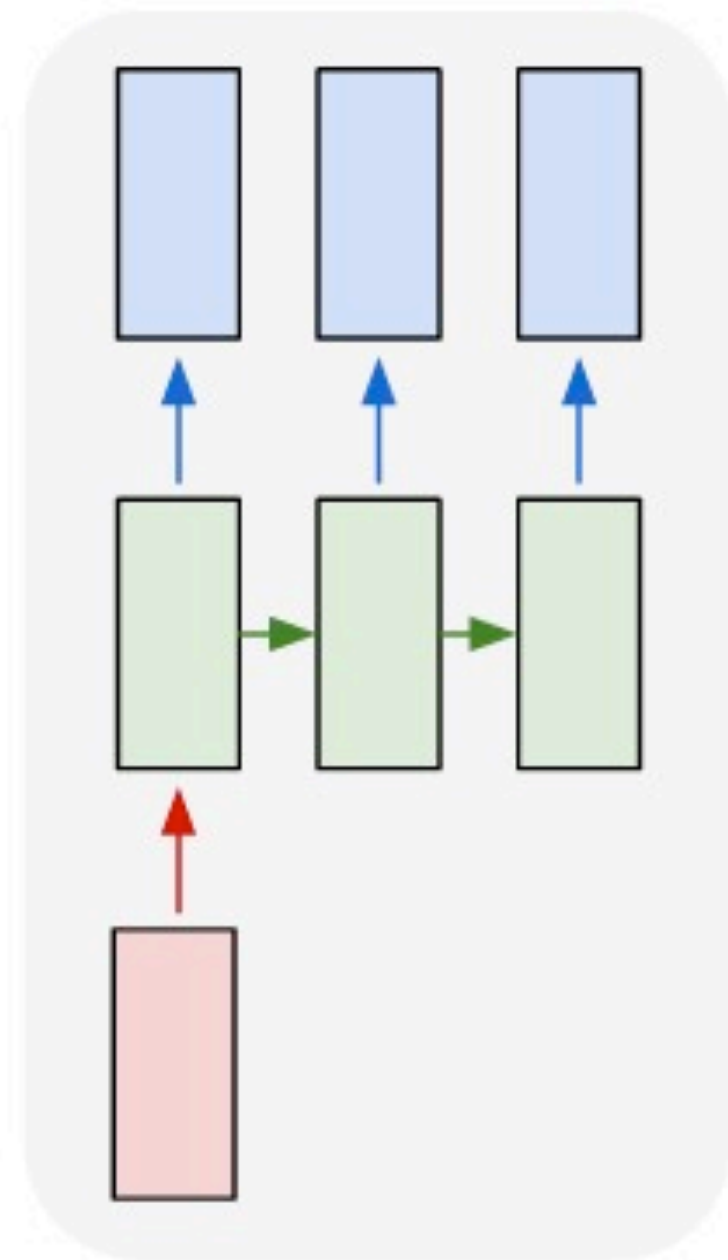
Sequences in Inputs or Outputs?

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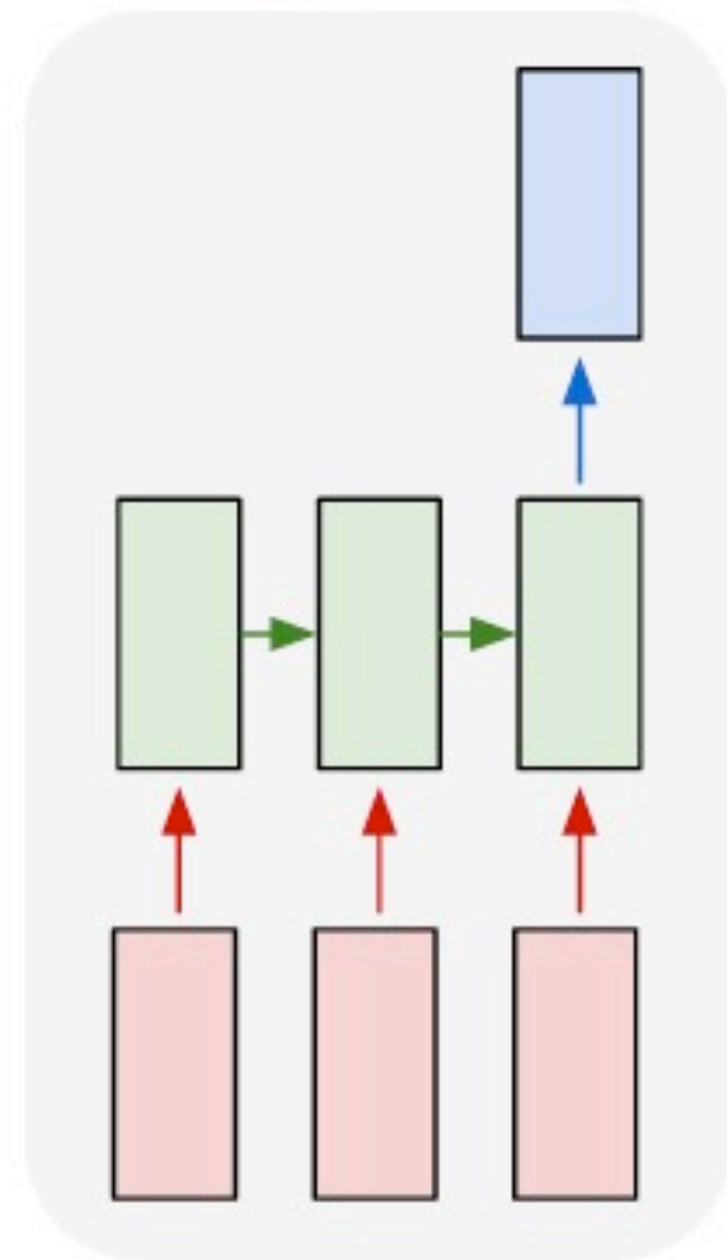
Input: No sequence
Output: No seq.
Example:
“standard”
classification /
regression problems

one to many



Input: No
sequence
Output:
Sequence
Example:
Im2Caption

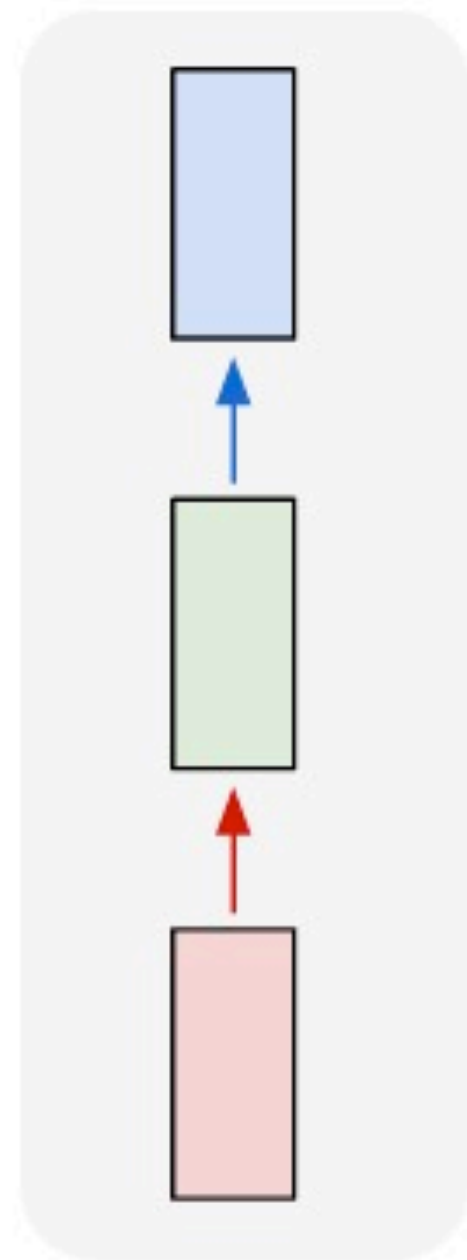
many to one



Input: Sequence
Output: No seq.
Example: sentence
classification,
multiple-choice
question answering

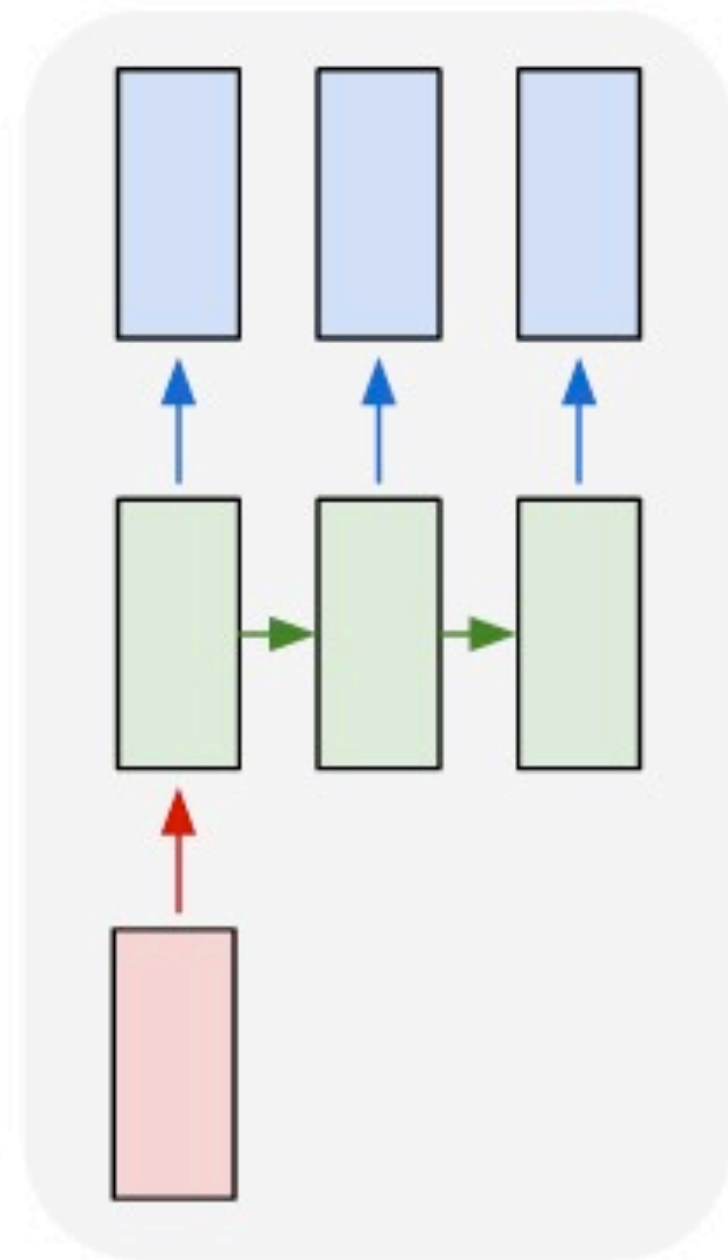
Sequences in Inputs or Outputs?

one to one



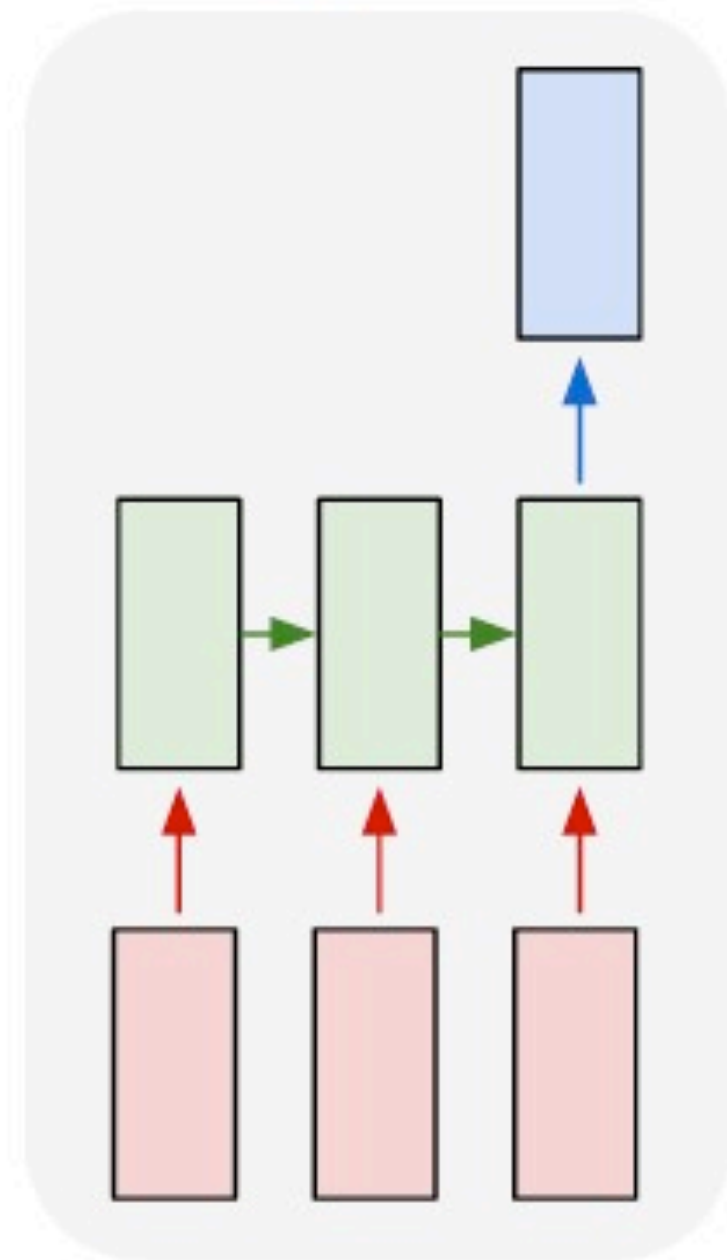
Input: No sequence
Output: No seq.
Example: “standard” classification / regression problems

one to many



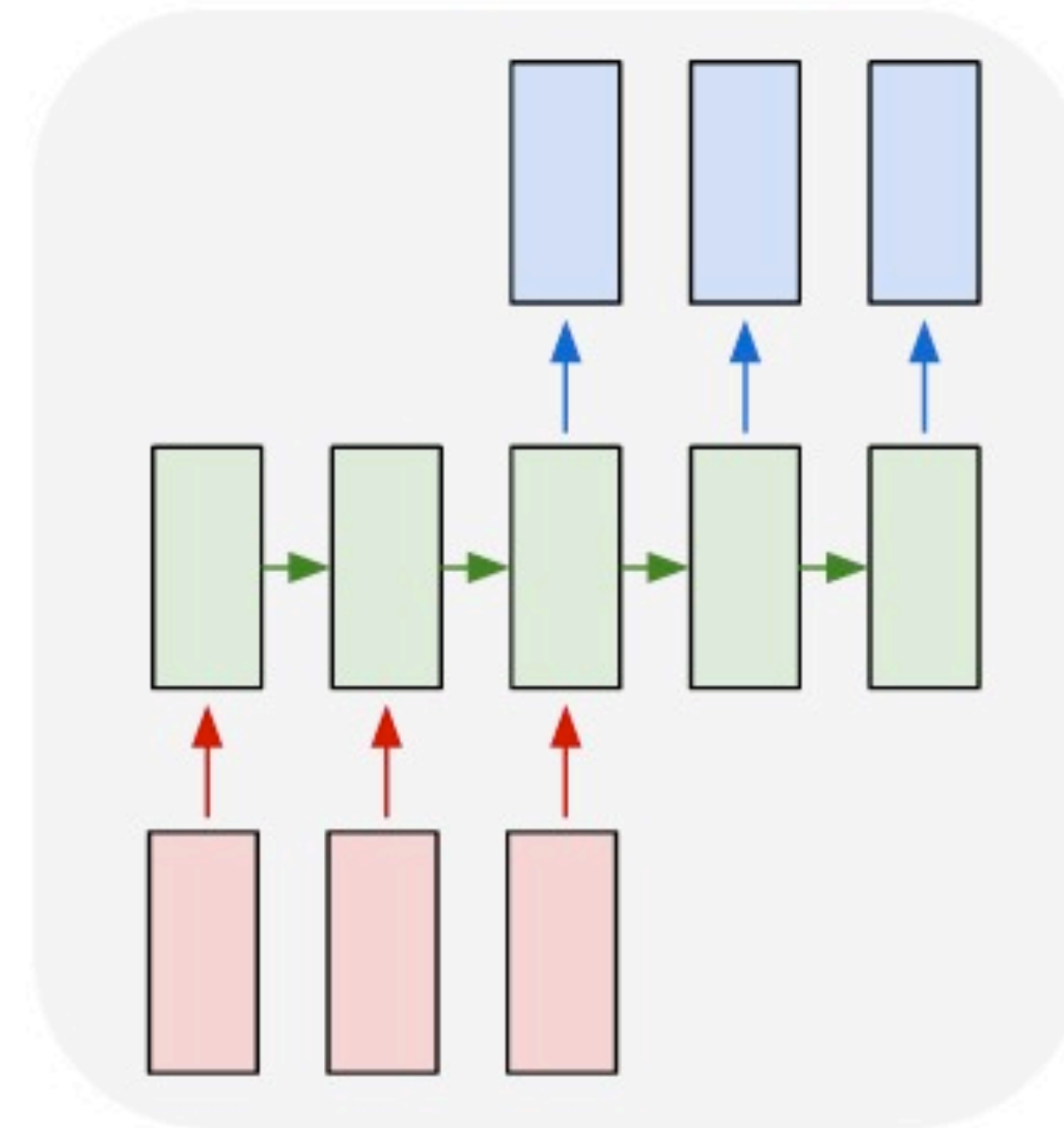
Input: No sequence
Output: Sequence
Example: Im2Caption

many to one



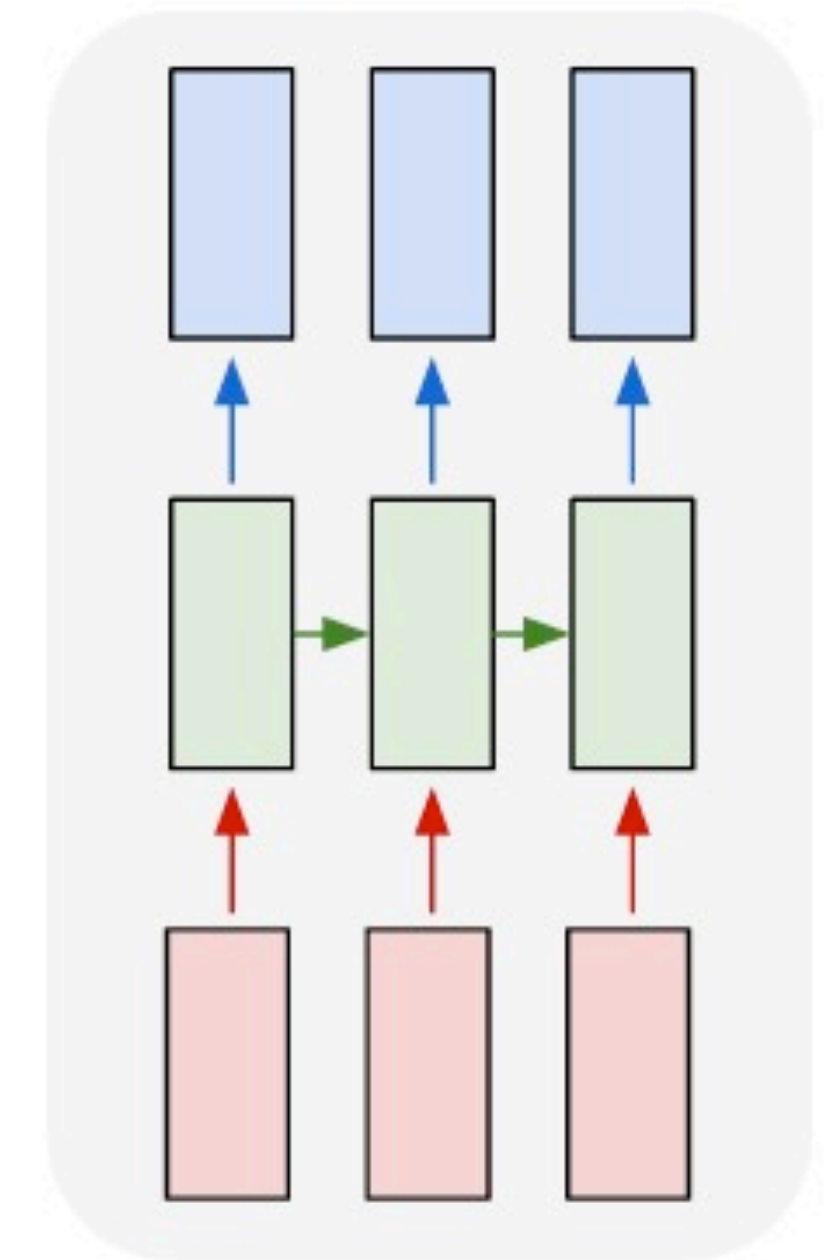
Input: Sequence
Output: No seq.
Example: sentence classification, multiple-choice question answering

many to many



Input: Sequence
Output: Sequence
Example: machine translation, video captioning, open-ended question answering, video question answering

many to many



Key Conceptual Ideas

Parameter Sharing

- in computational graphs = adding gradients

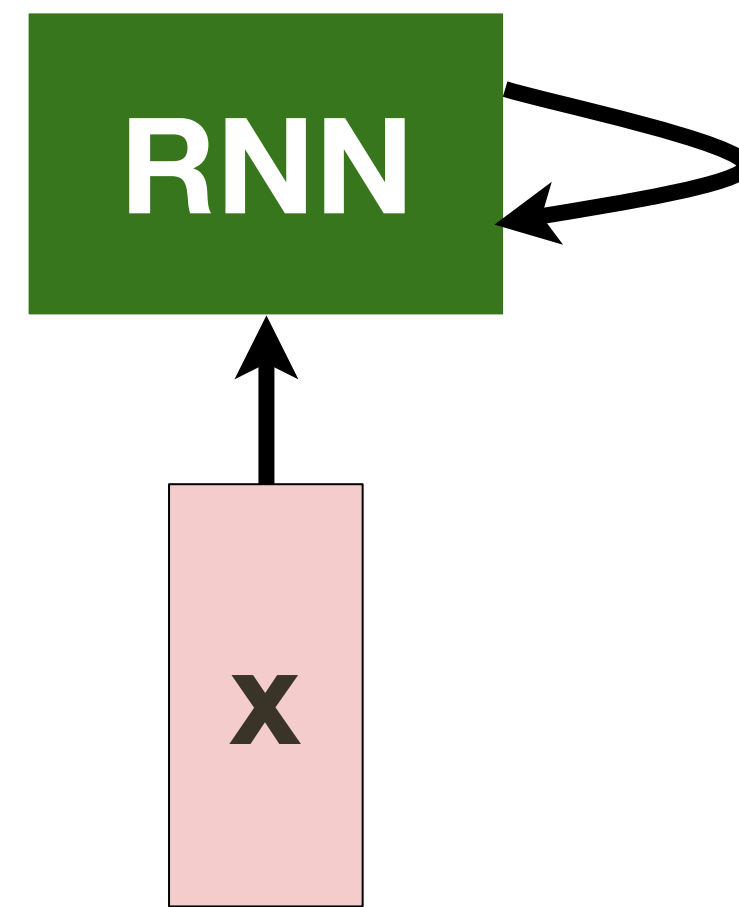
“Unrolling”

- in computational graphs with parameter sharing

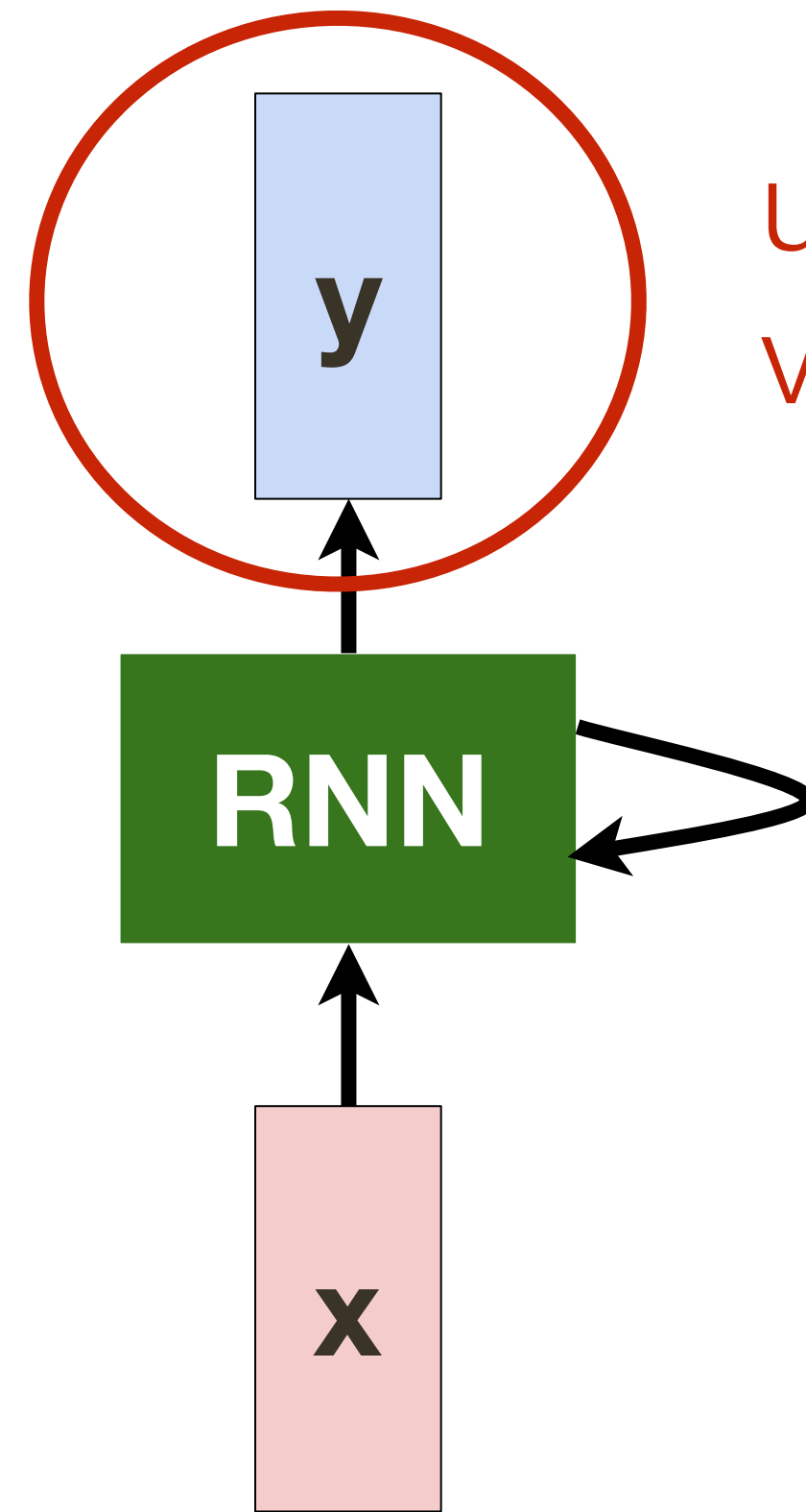
Parameter Sharing + “Unrolling”

- Allows modeling **arbitrary length sequences!**
- Keeps number of parameters in check

Recurrent Neural Network



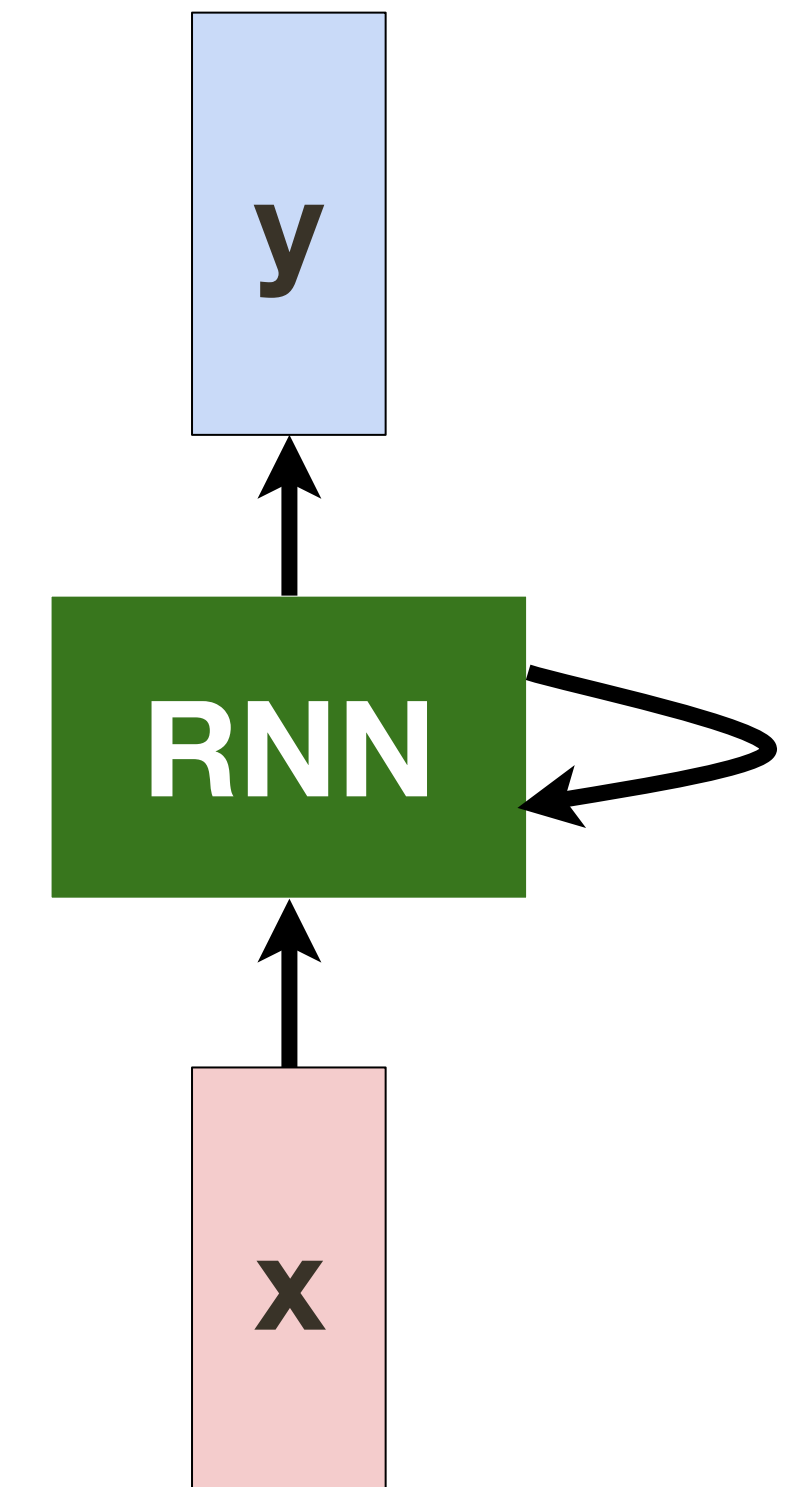
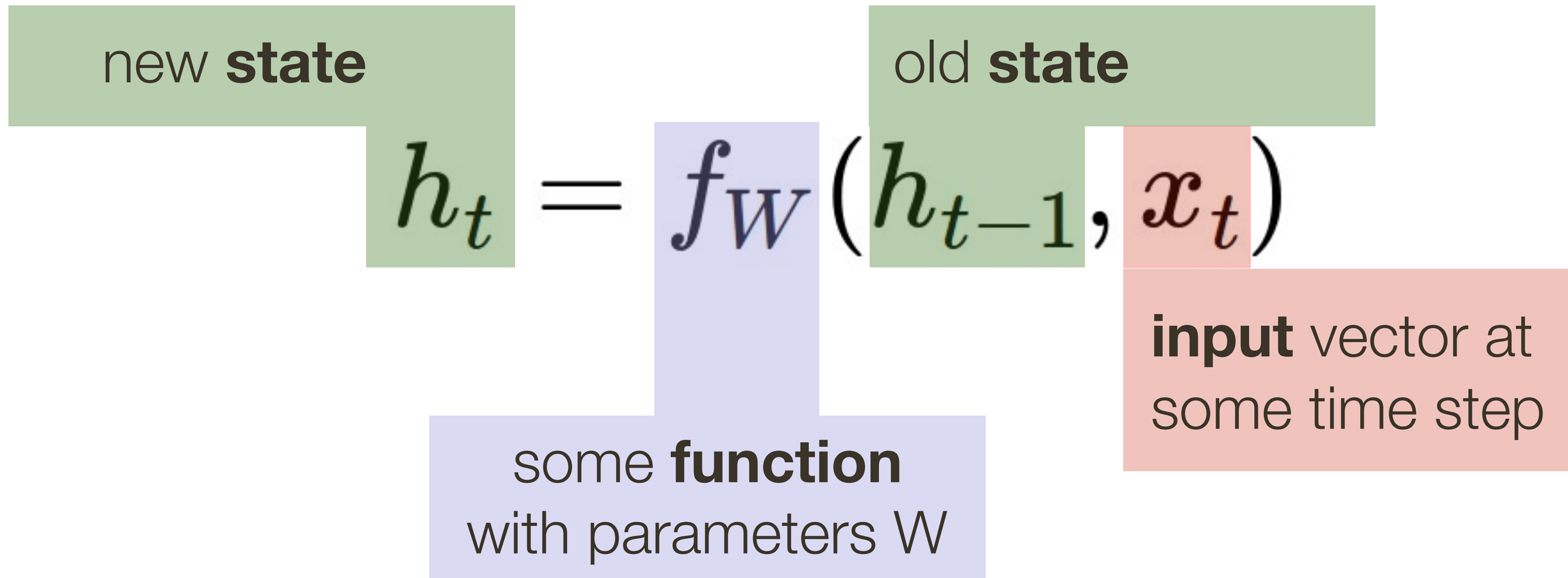
Recurrent Neural Network



usually want to predict a vector at some time steps

Recurrent Neural Network

We can process a sequence of vectors \mathbf{x} by applying a **recurrence formula** at every time step:

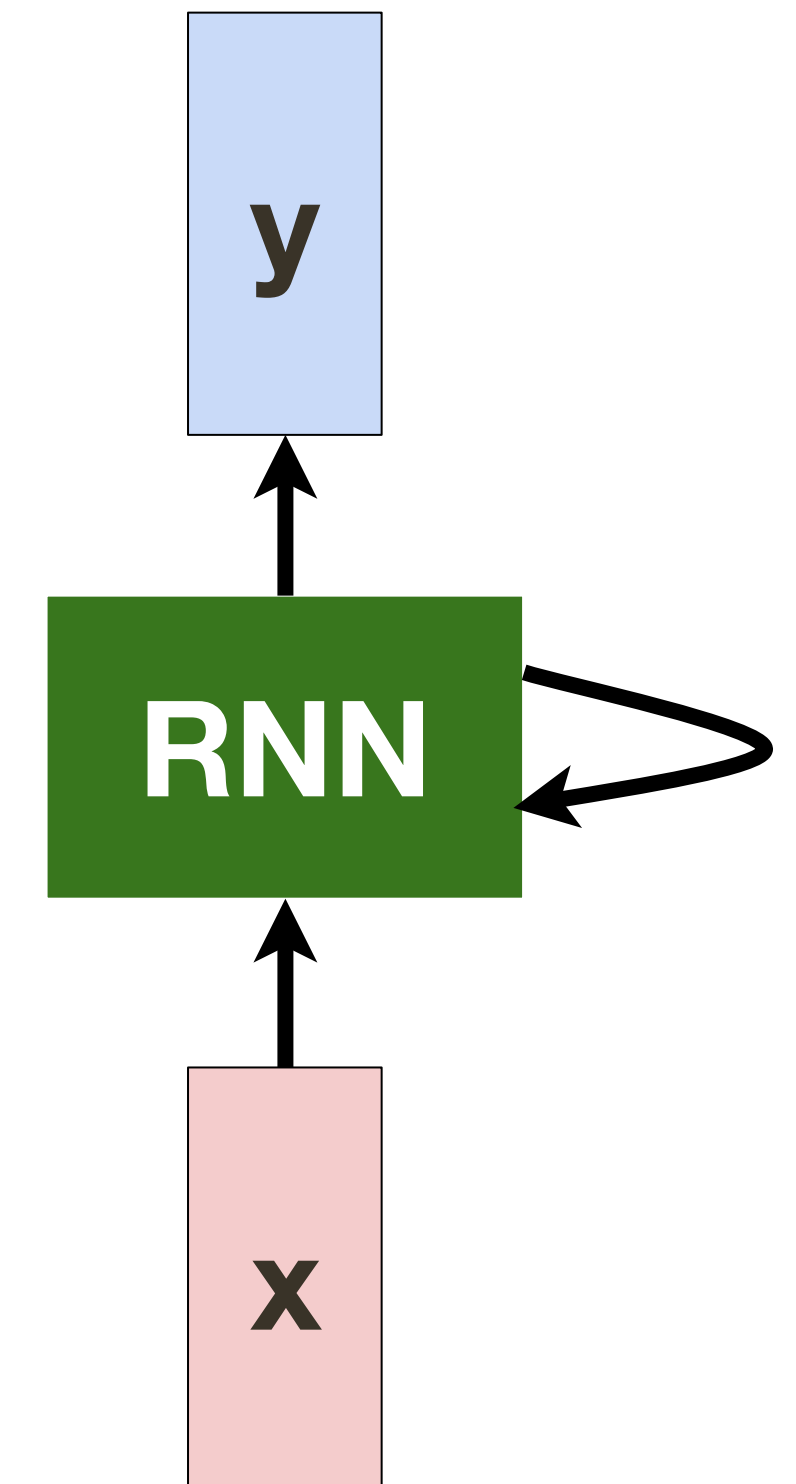


Recurrent Neural Network

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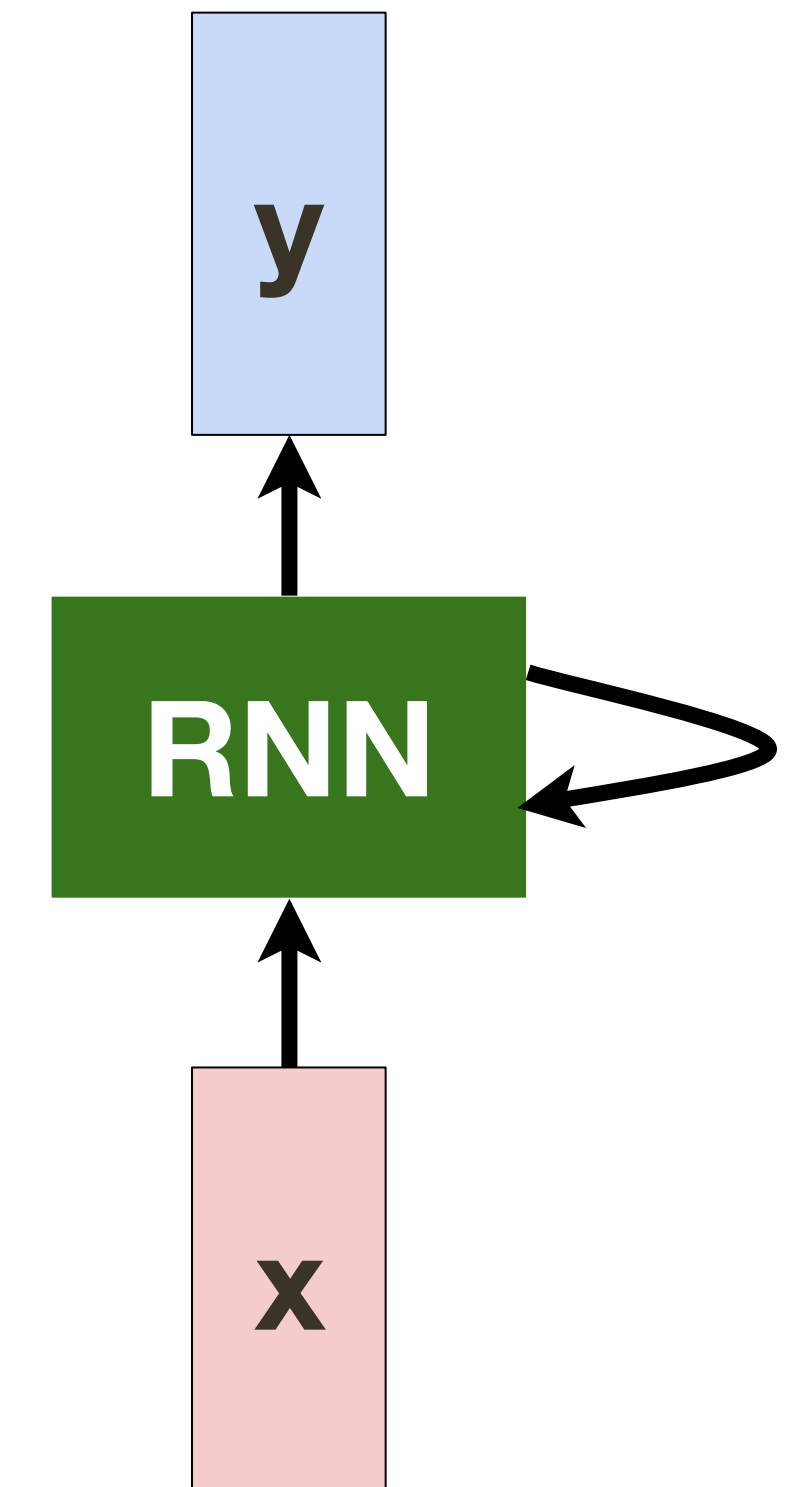
$$h_t = f_W(h_{t-1}, x_t)$$

Note: the same function and the same set of parameters are used at every time step



(Vanilla) **Recurrent** Neural Network

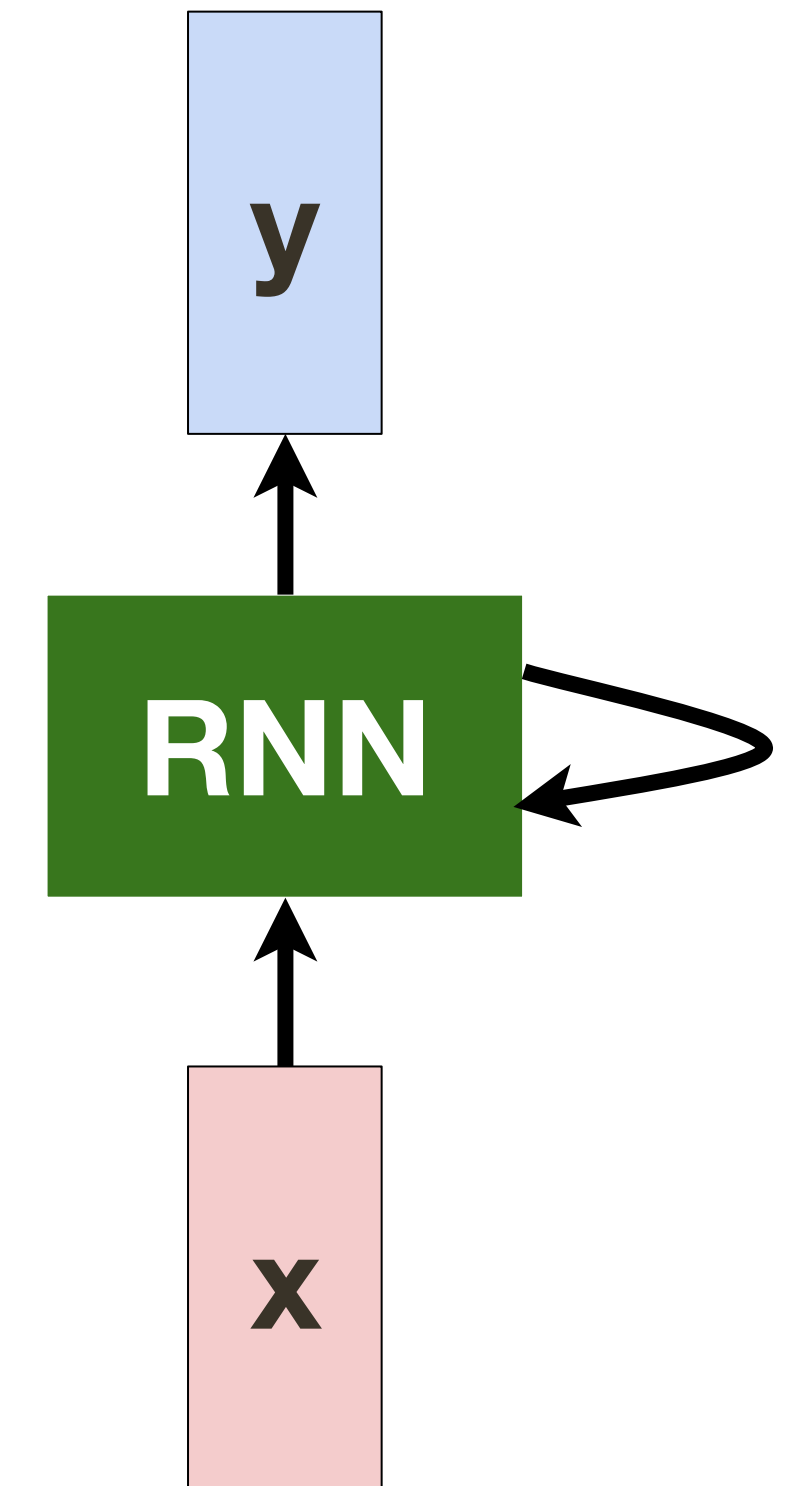
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(Vanilla) **Recurrent** Neural Network

$$h_t = f_W(h_{t-1}, x_t)$$

$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$$

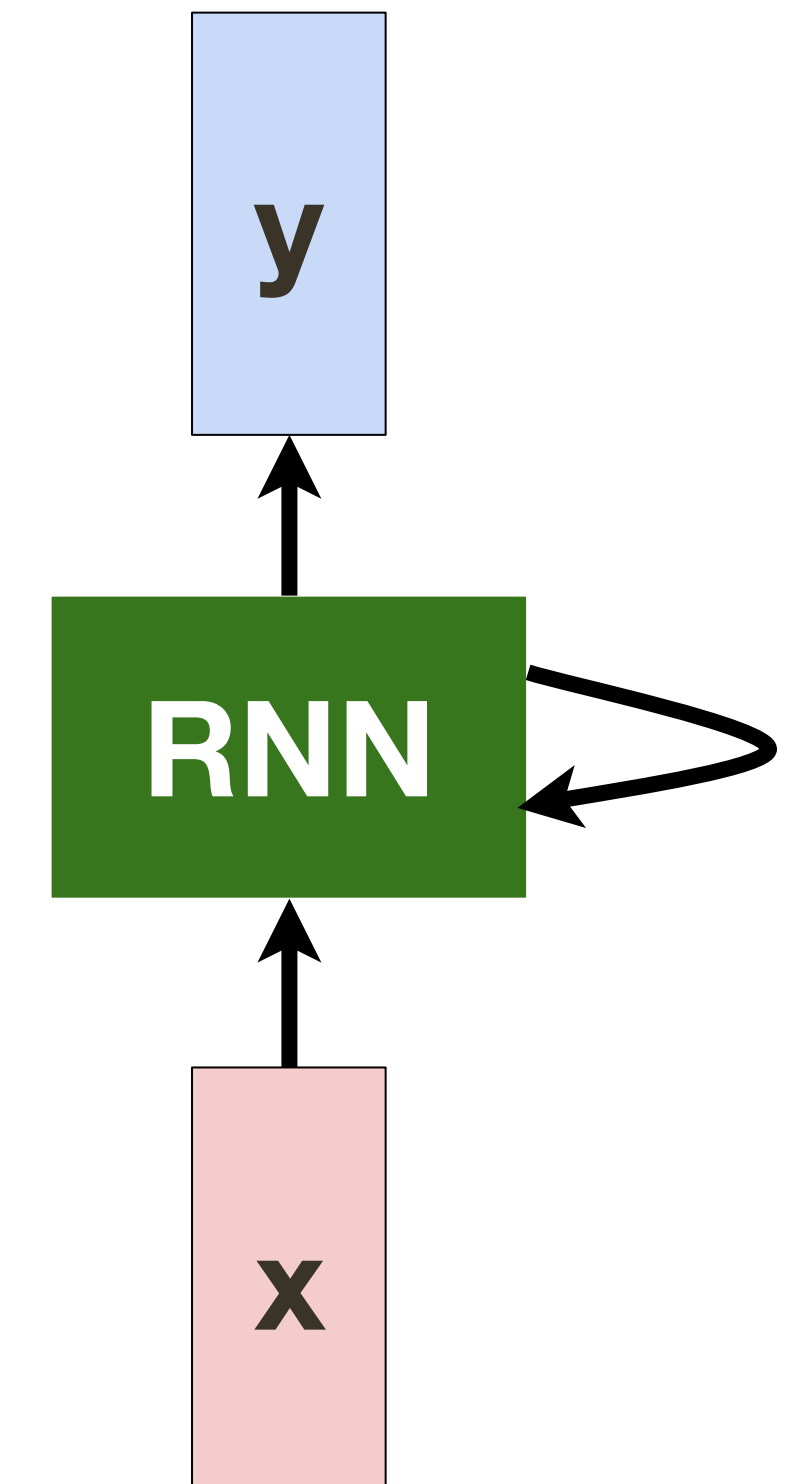


(Vanilla) **Recurrent** Neural Network

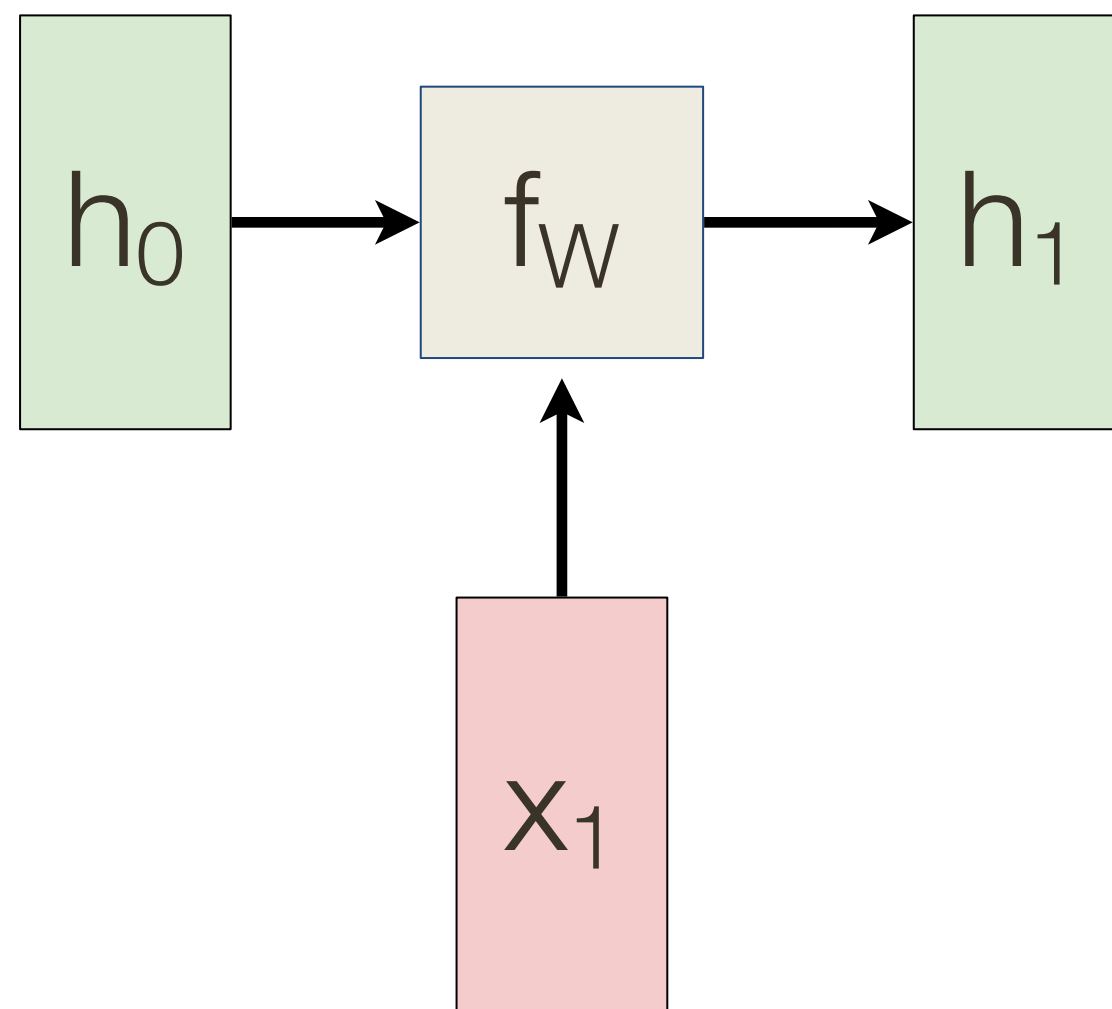
$$y_t = W_{hy}h_t + b_y$$

$$h_t = f_W(h_{t-1}, x_t)$$

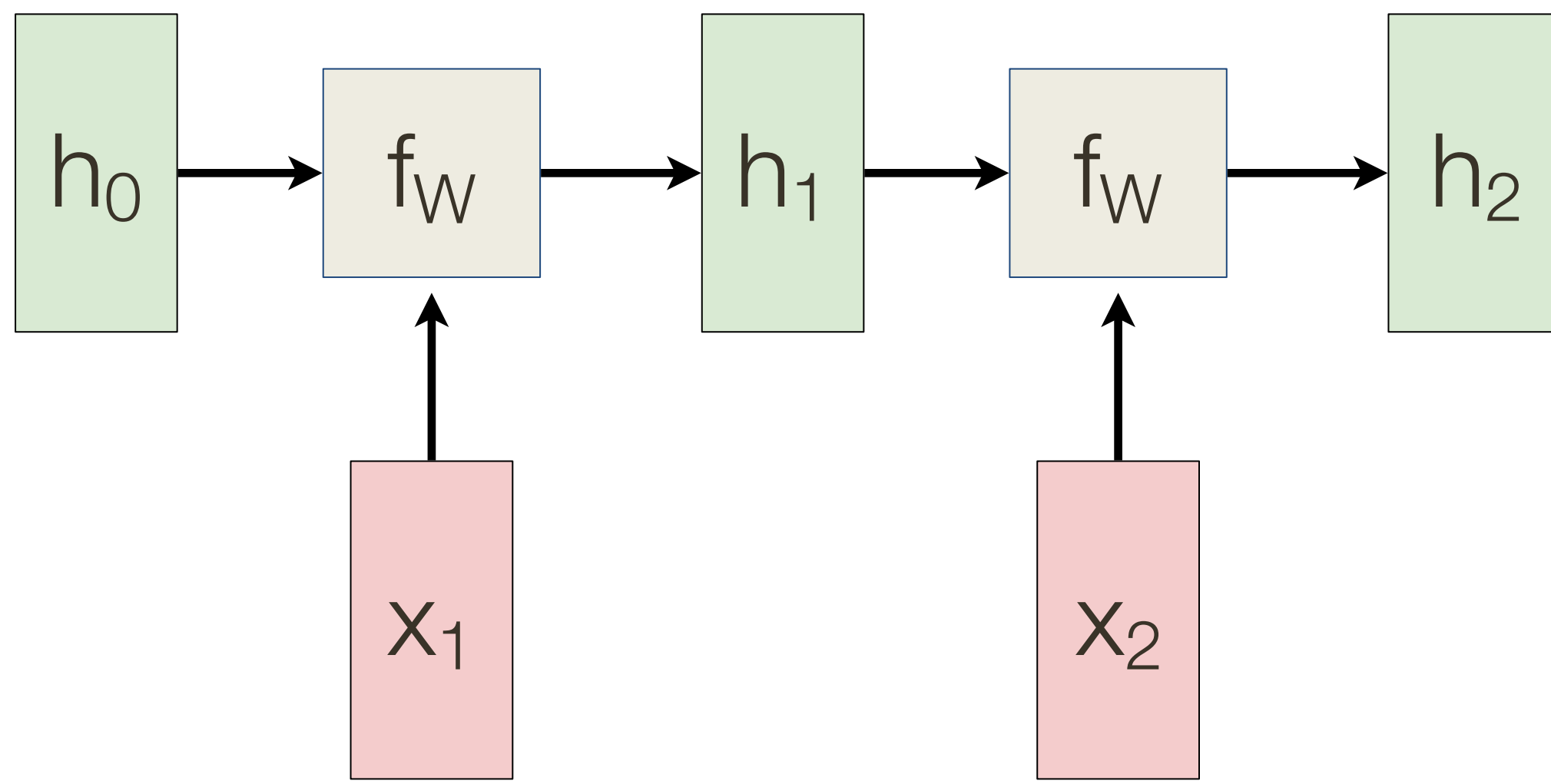
$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t + b_h)$$



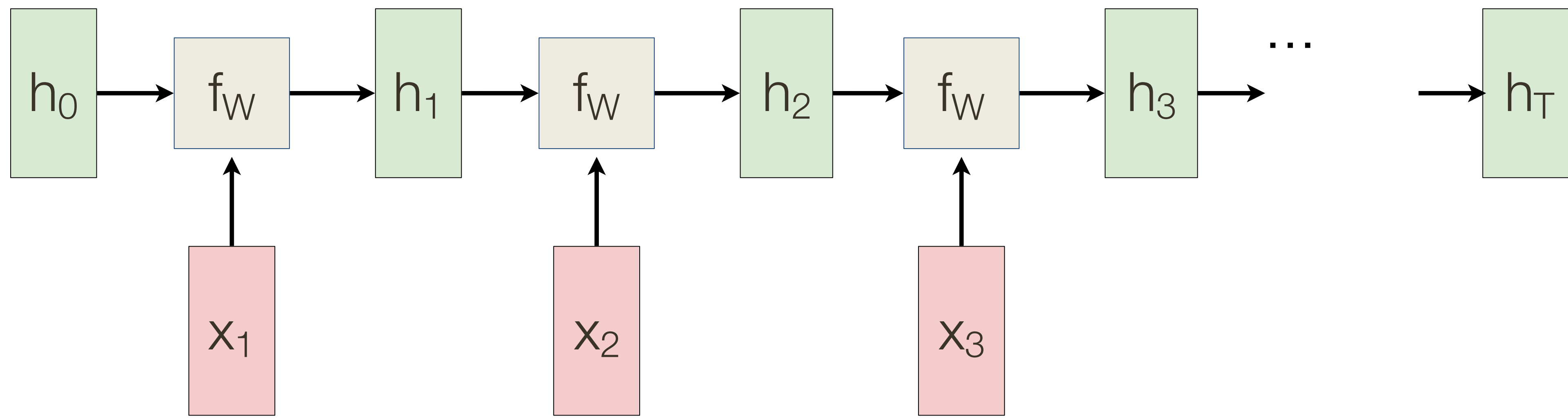
RNN Computational Graph



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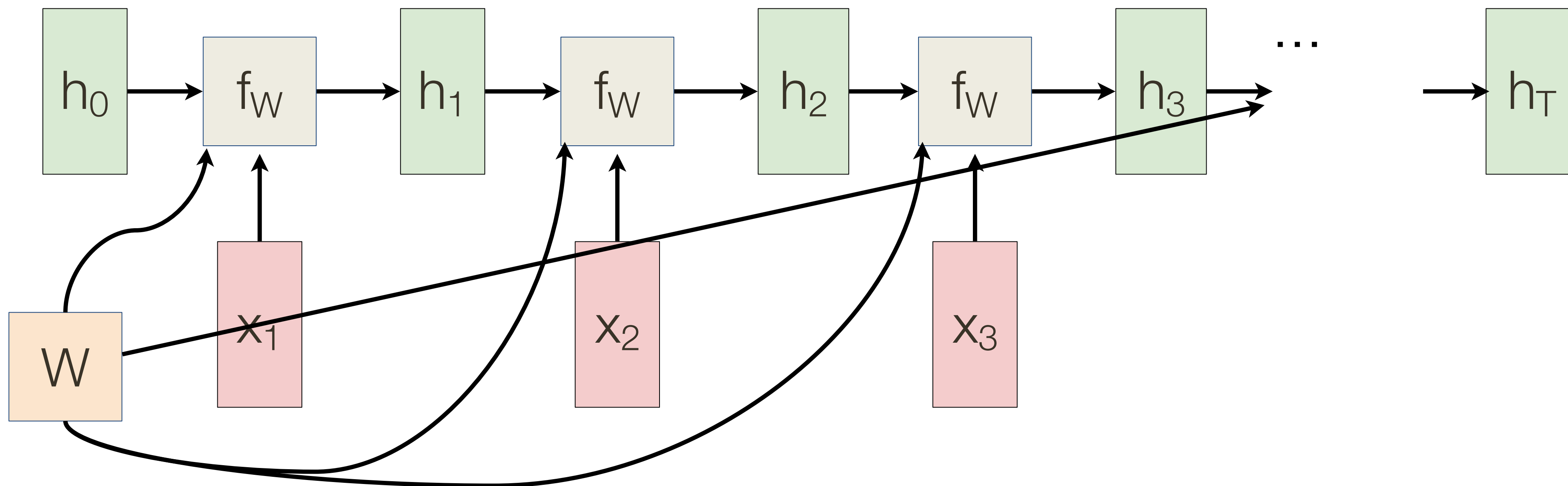


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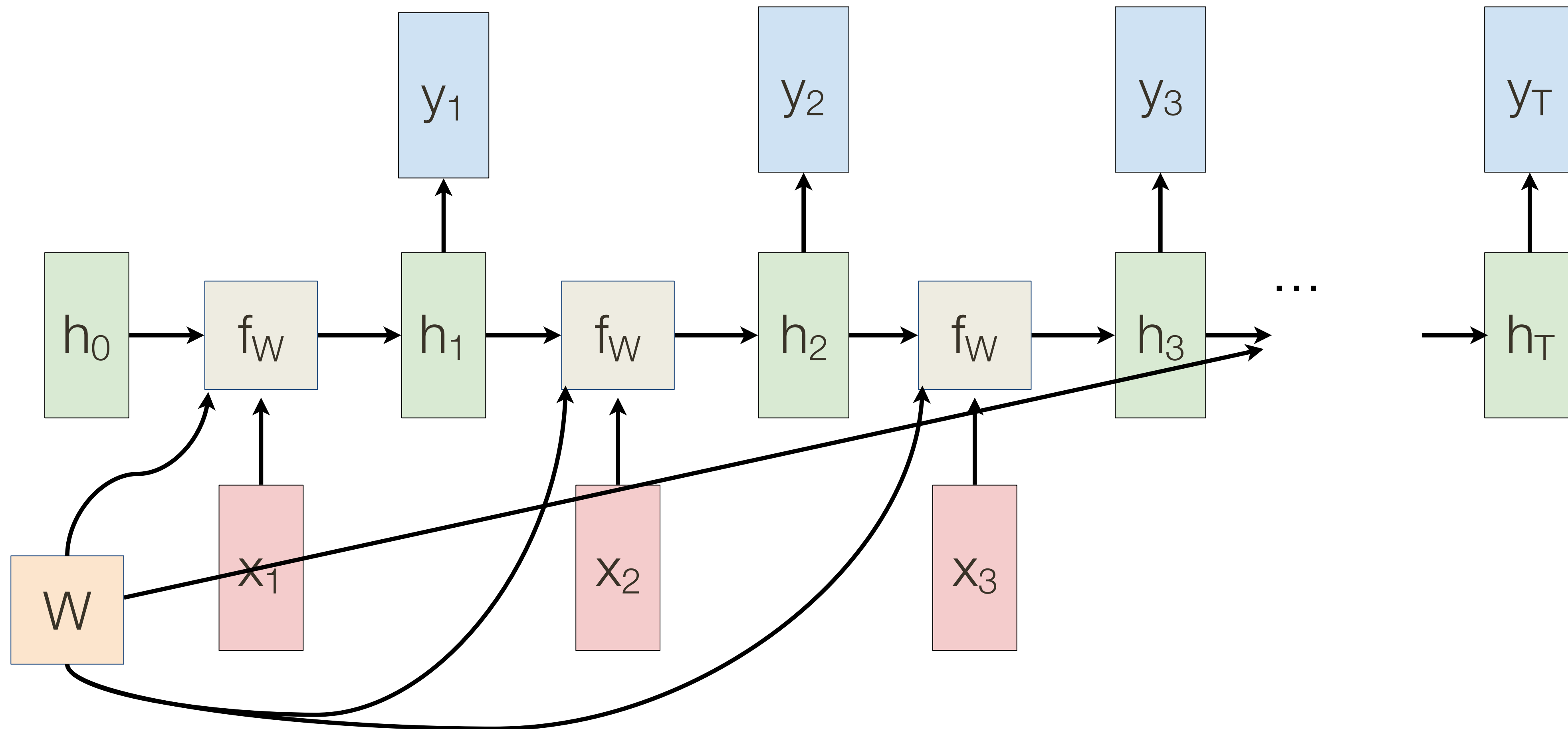


RNN Computational Graph

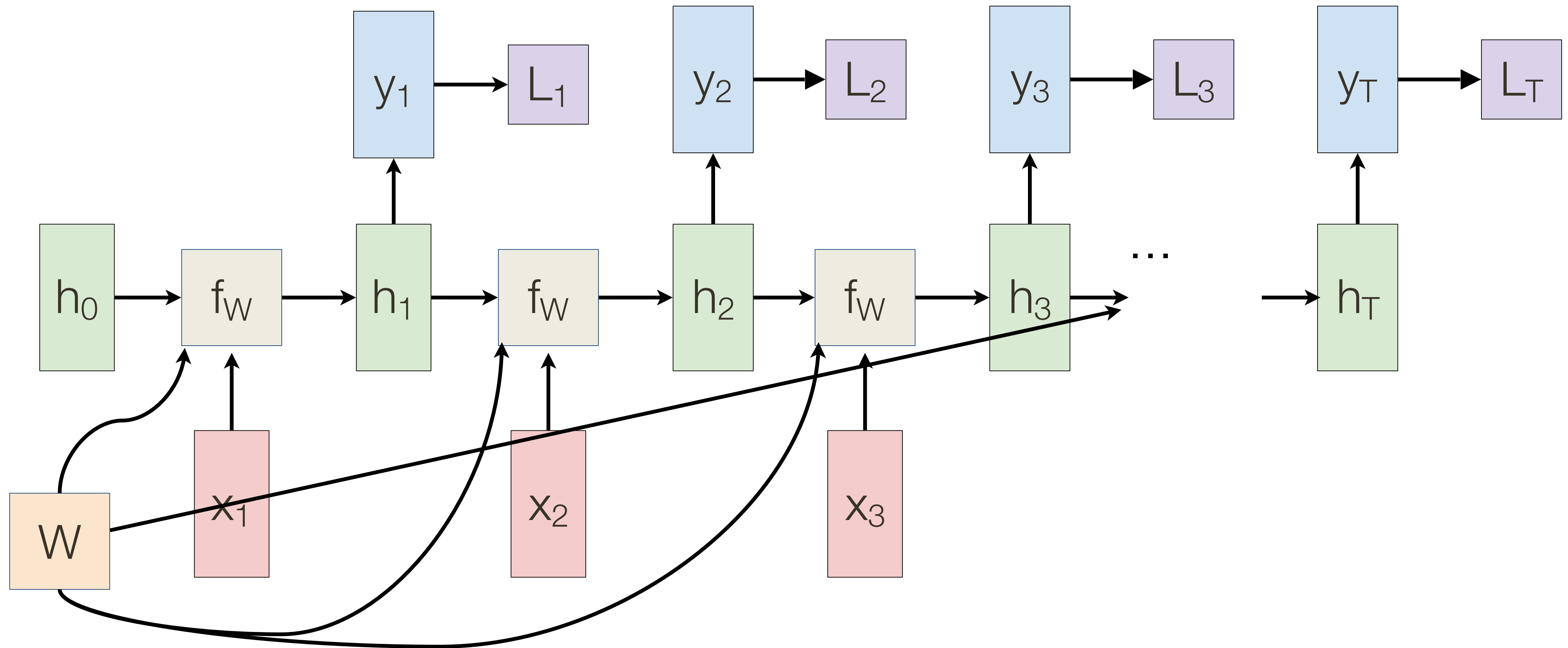
Re-use the same weight matrix at every time-step



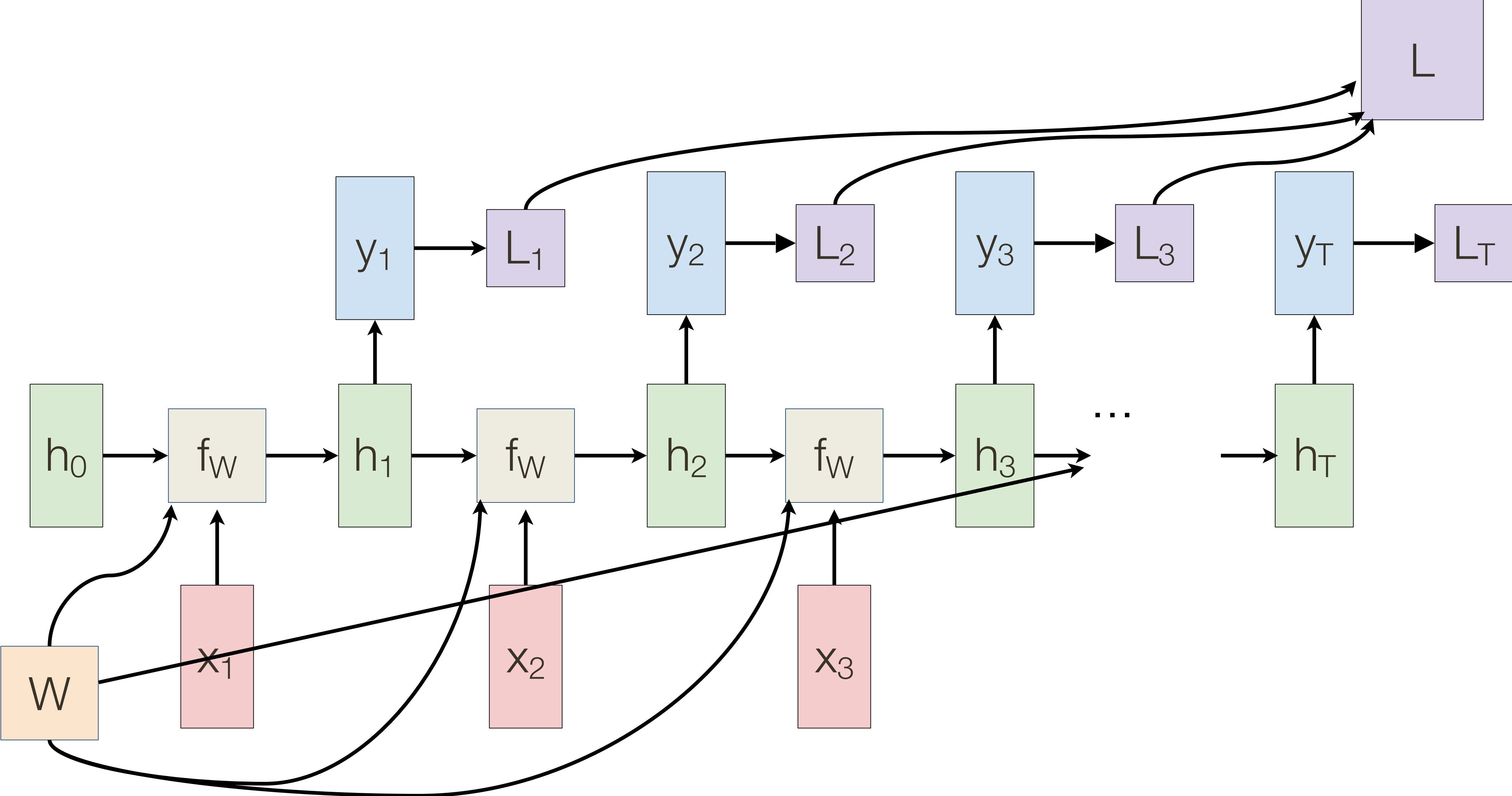
RNN Computational Graph: Many to Many



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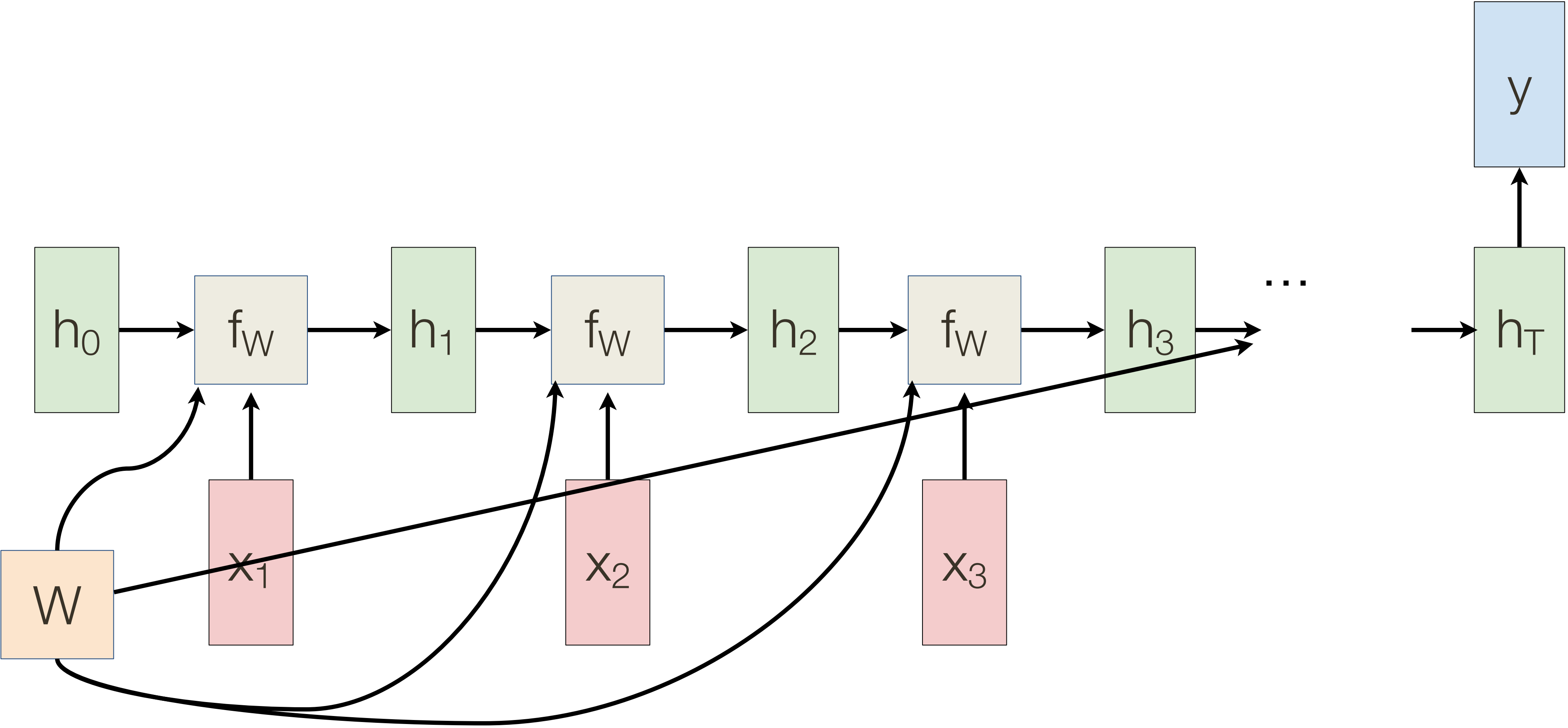


RNN Computational Graph: Many to Many



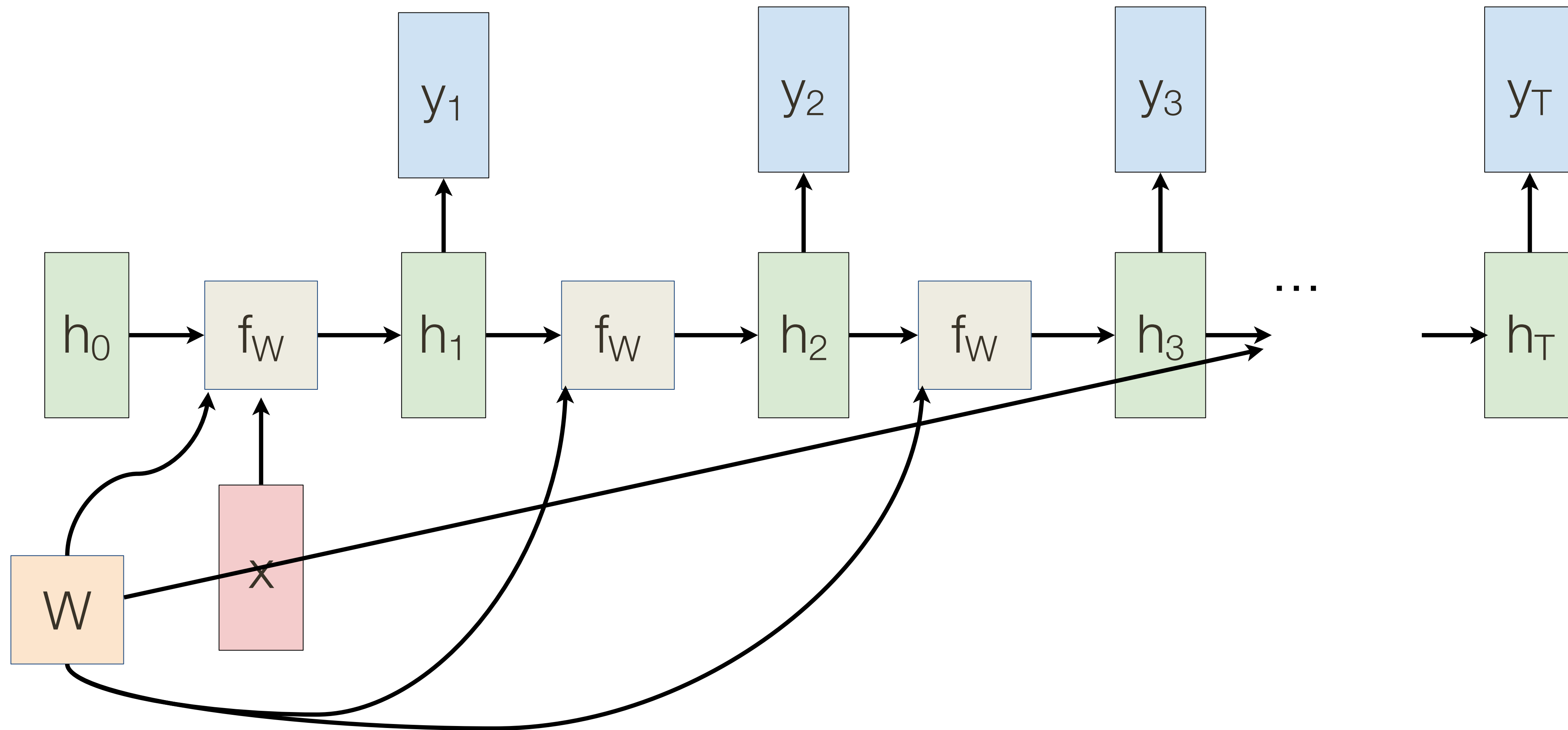
* slide from Fei-Dei Li, Justin Johnson, Serena Yeung, **cs231n Stanford**

RNN Computational Graph: Many to One



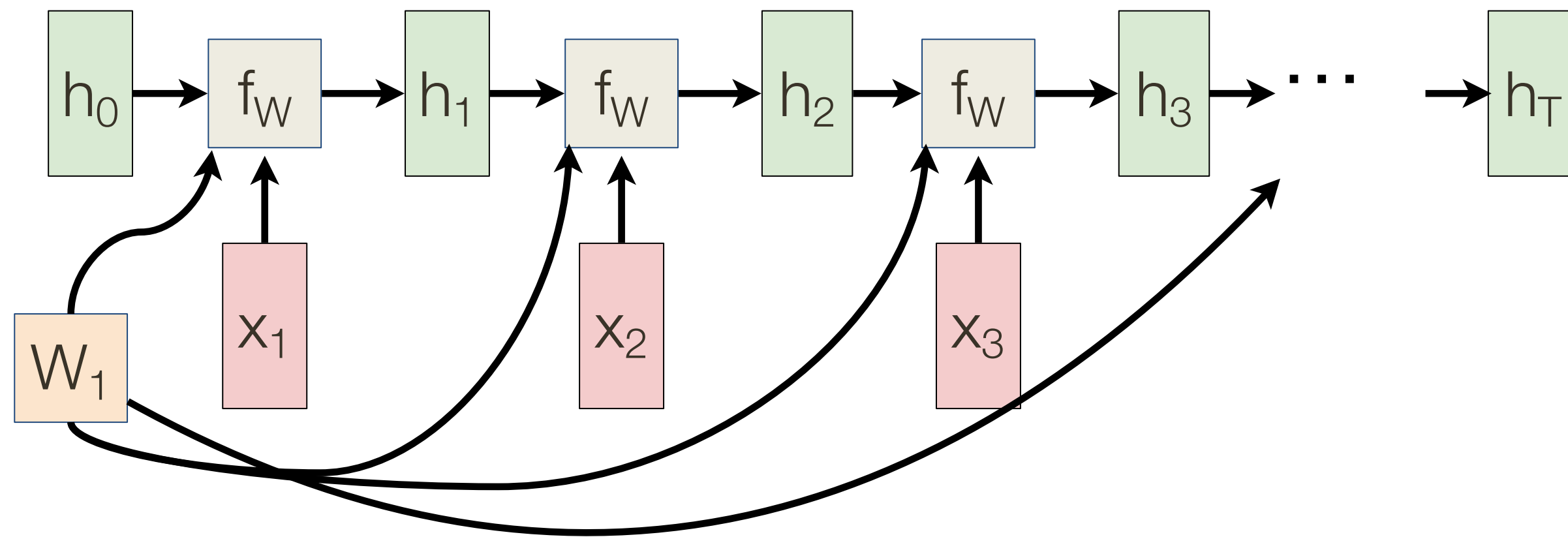
* slide from Fei-Dei Li, Justin Johnson, Serena Yeung, **cs231n Stanford**

RNN Computational Graph: One to Many



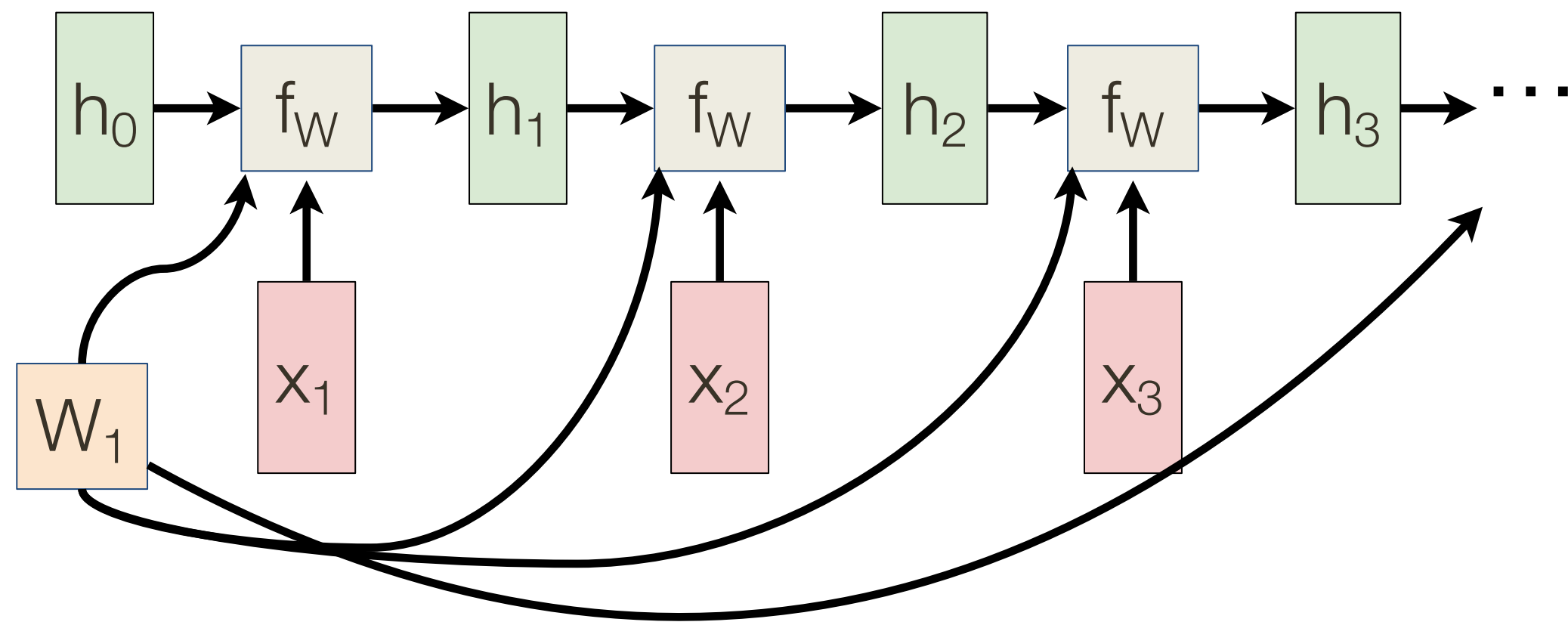
Sequence to Sequence: Many to One + One to Many

Many to one: Encode input sequence in a single vector



Sequence to Sequence: Many to One + One to Many

Many to one: Encode input sequence in a single vector



One to many: Produce output sequence from single input vector

