

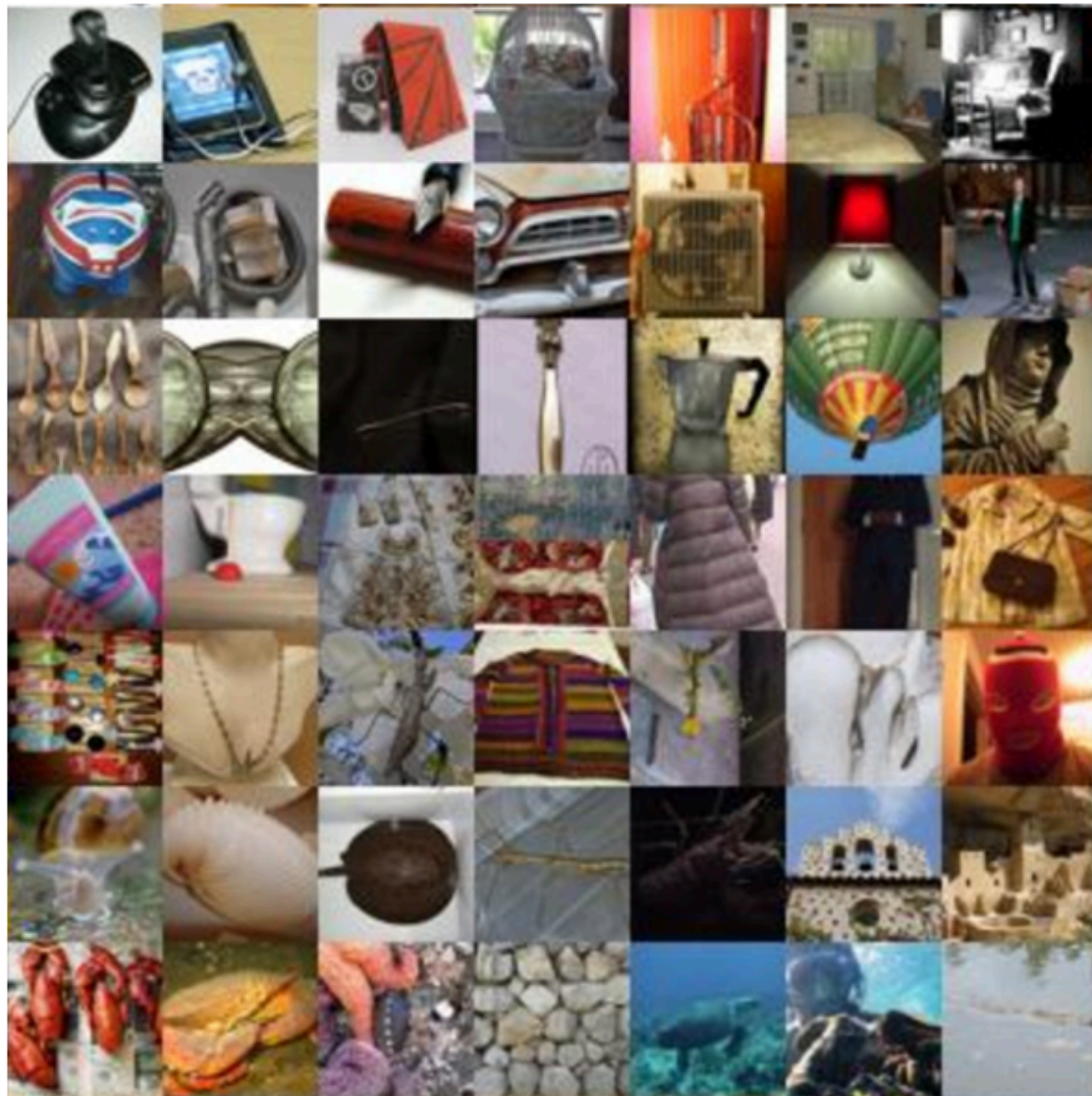


Topics in AI (CPSC 532S): Multimodal Learning with Vision, Language and Sound

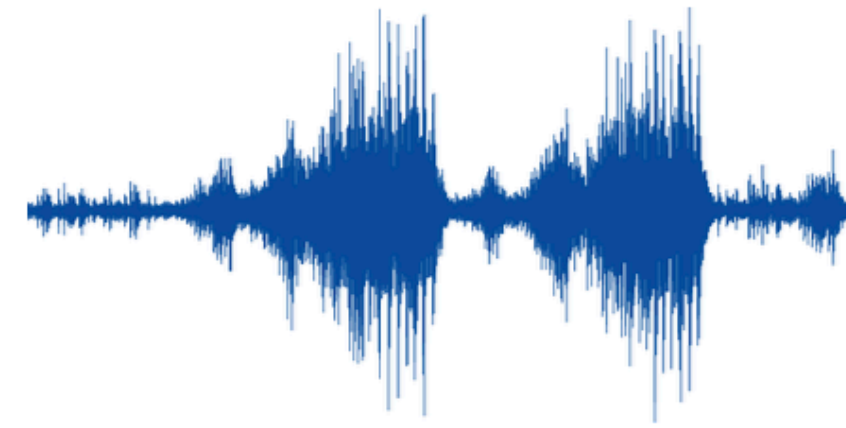
Lecture 19: Graph Neural Networks (cont)

Traditional Neural Networks

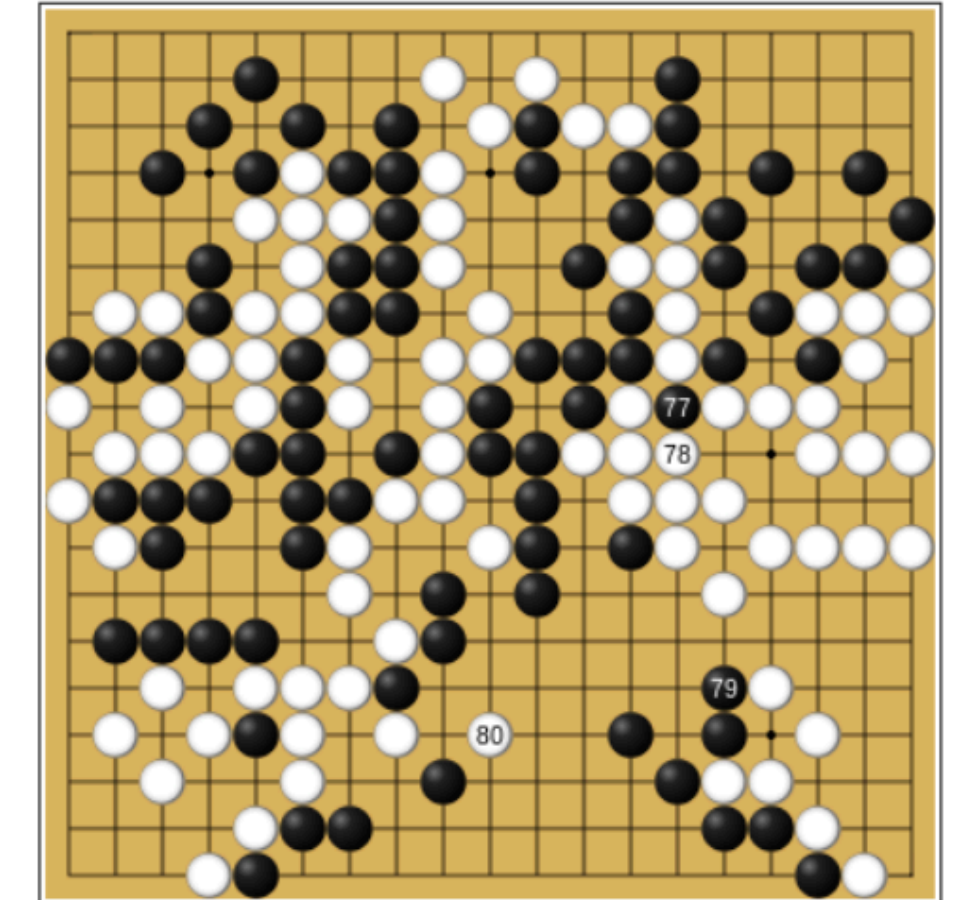
IMAGENET



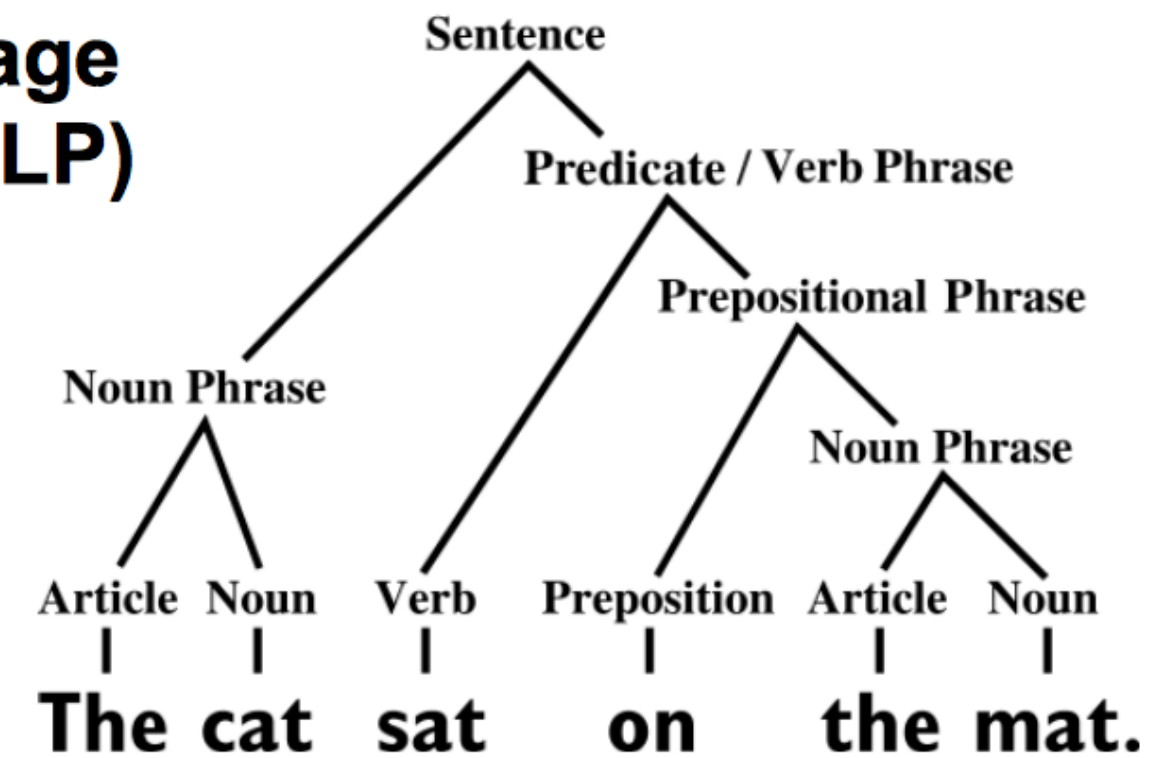
Speech data



Grid games

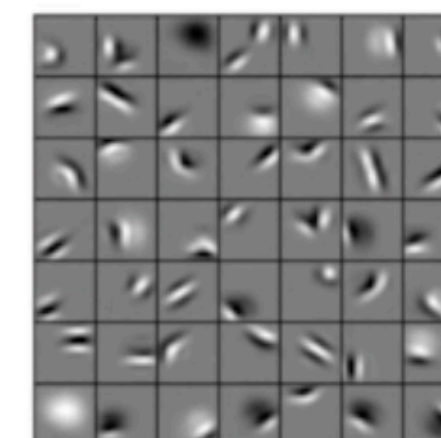


Natural language processing (NLP)

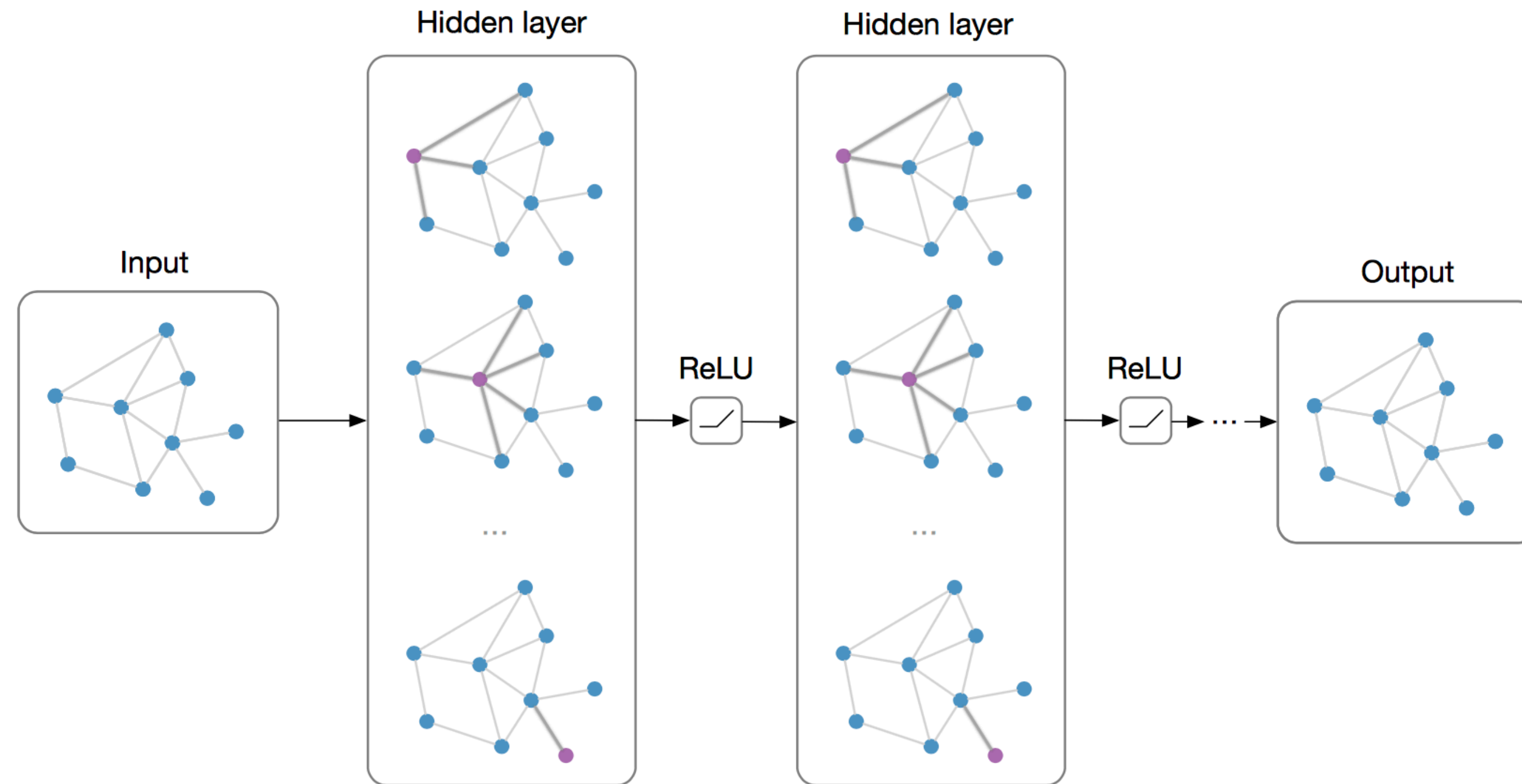


Deep neural nets that exploit:

- translation equivariance (weight sharing)
- hierarchical compositionality



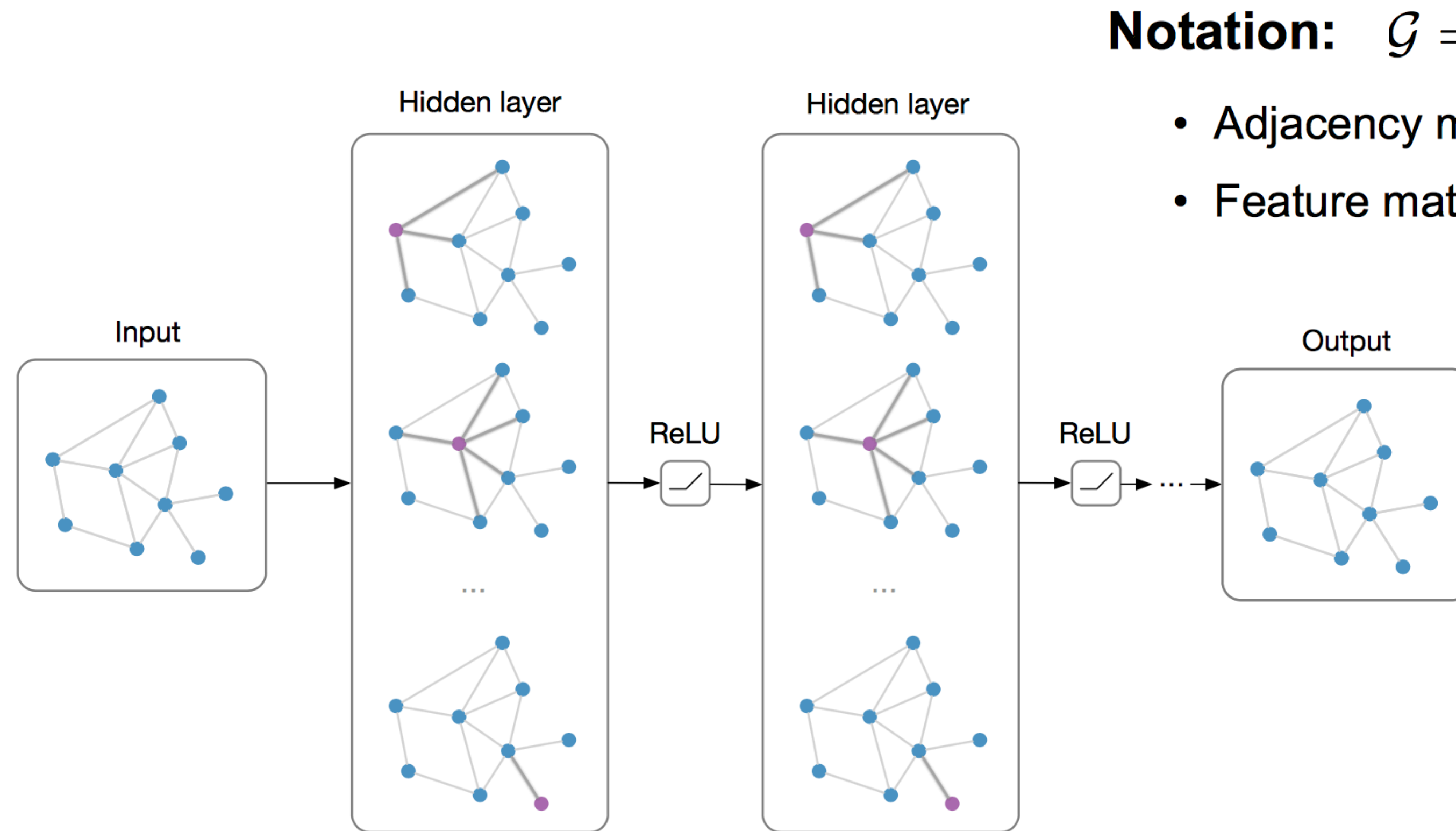
Graph Neural Networks (GNNs)



Main Idea: Pass messages between pairs of nodes and agglomerate

Alternative Interpretation: Pass messages between nodes to refine node (and possibly edge) representations

Graph Neural Networks (GNNs)



Notation: $\mathcal{G} = (\mathbf{A}, \mathbf{X})$

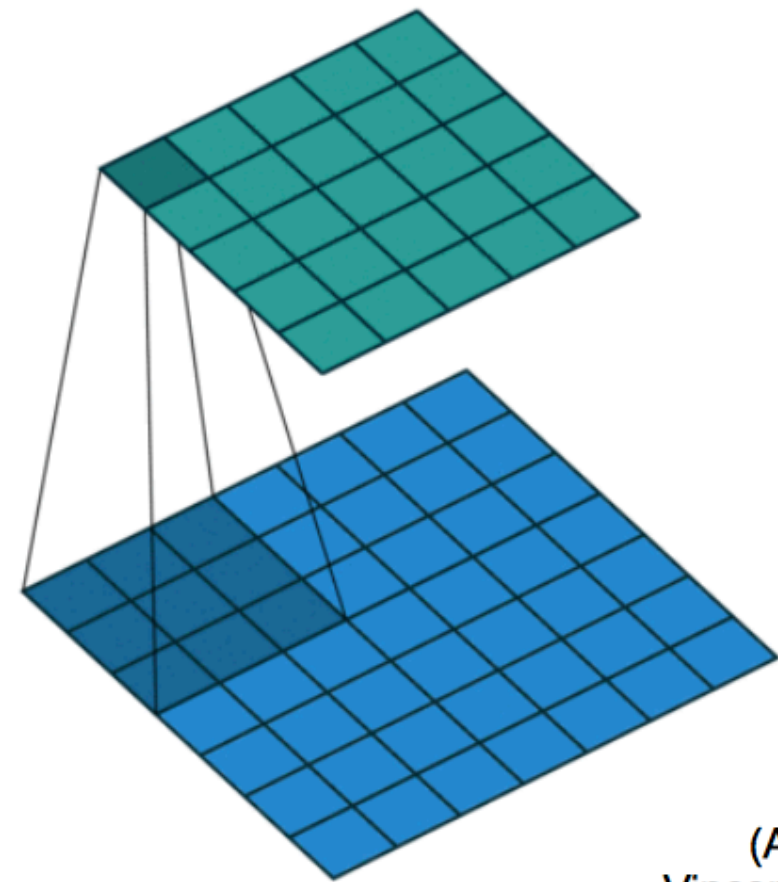
- Adjacency matrix $\mathbf{A} \in \mathbb{R}^{N \times N}$
- Feature matrix $\mathbf{X} \in \mathbb{R}^{N \times F}$

Main Idea: Pass messages between pairs of nodes and agglomerate

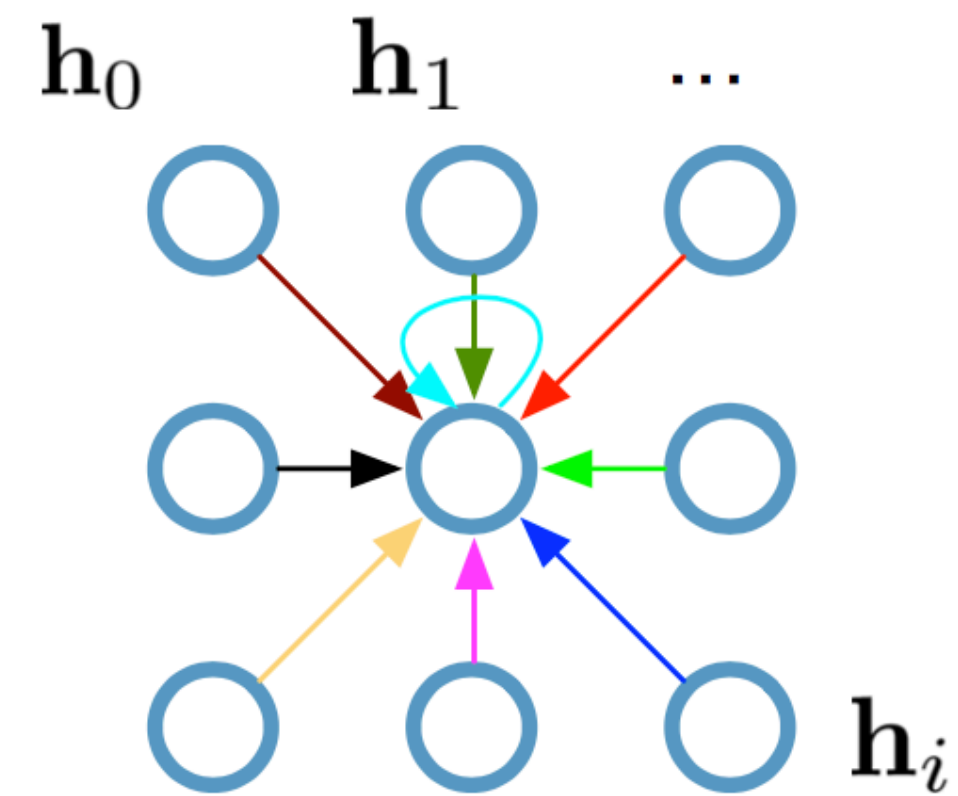
Alternative Interpretation: Pass messages between nodes to refine node (and possibly edge) representations

Recap: Convolutional Neural Networks (CNNs) on Grids

Single CNN layer with 3x3 filter:

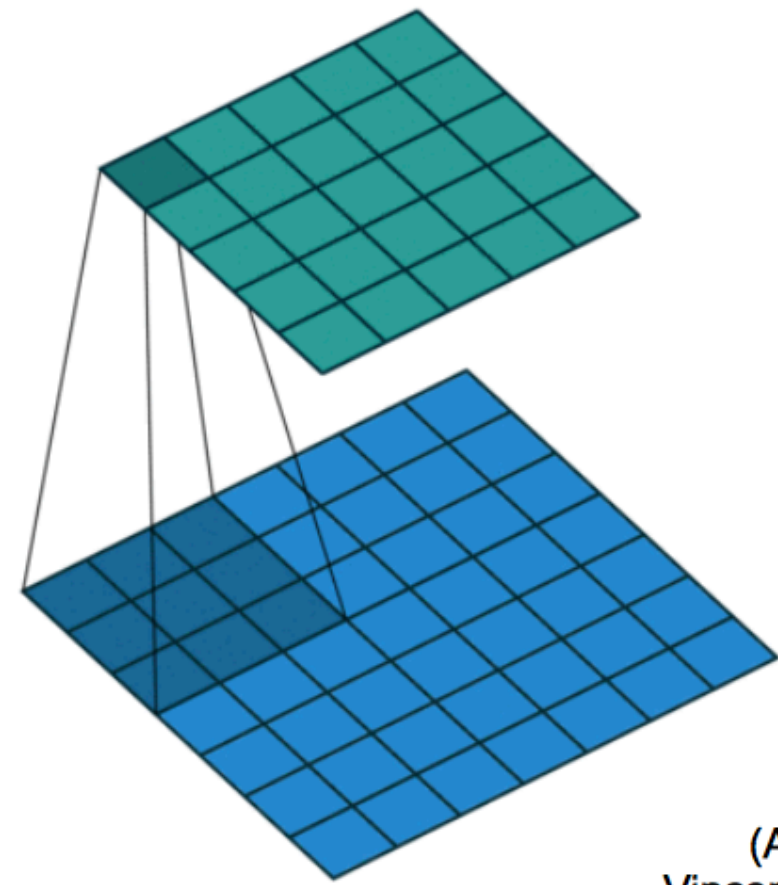


(Animation by Vincent Dumoulin)

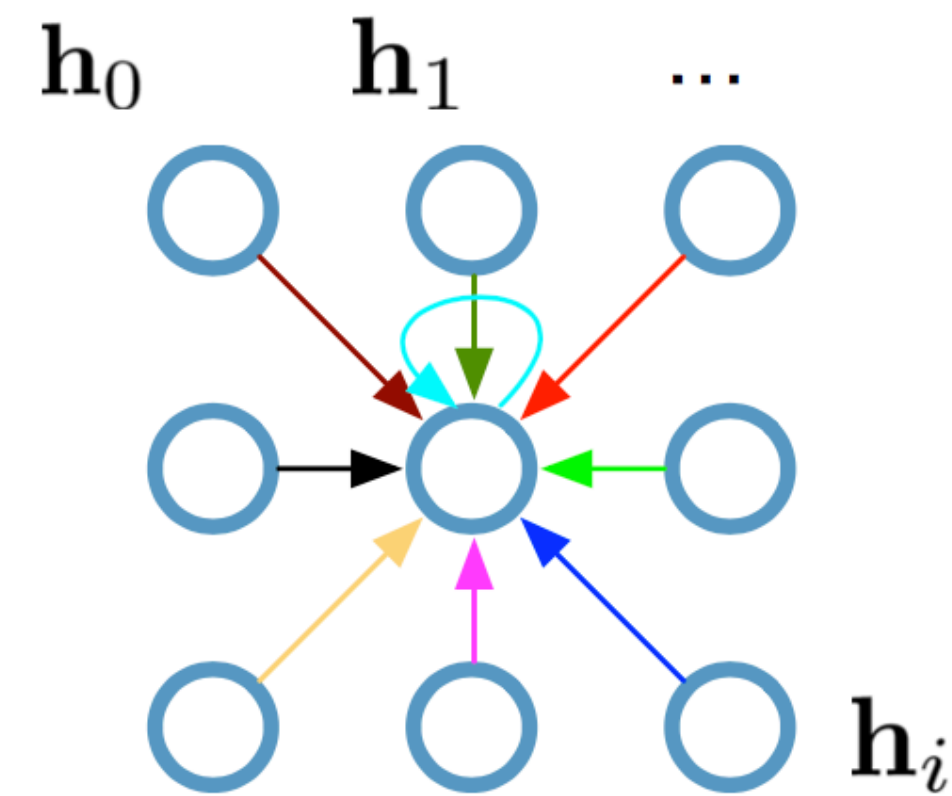


Recap: Convolutional Neural Networks (CNNs) on Grids

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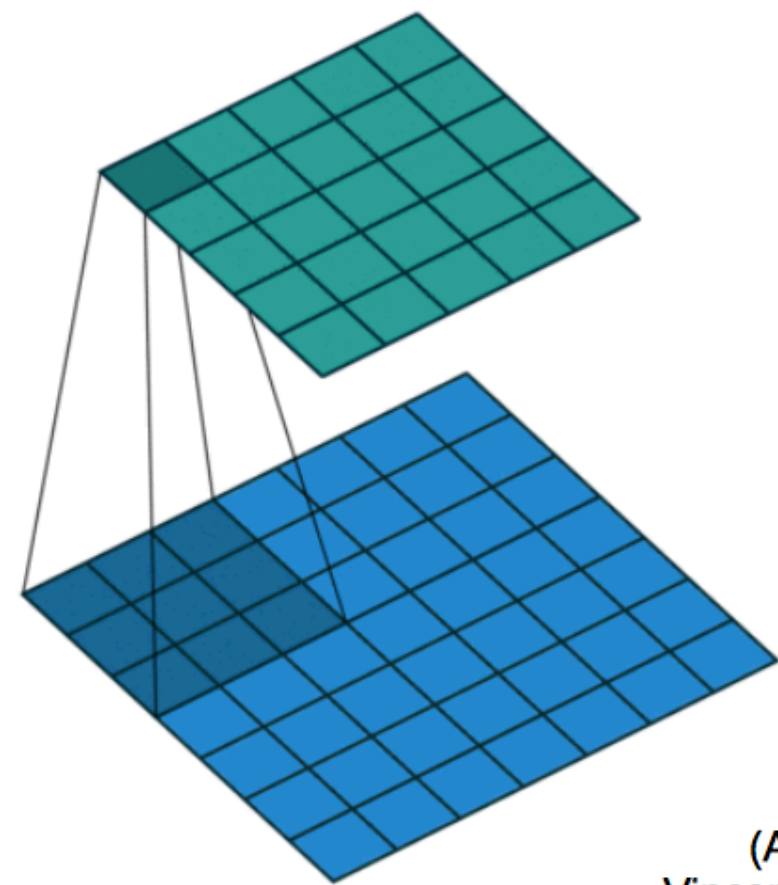
(Animation by Vincent Dumoulin)



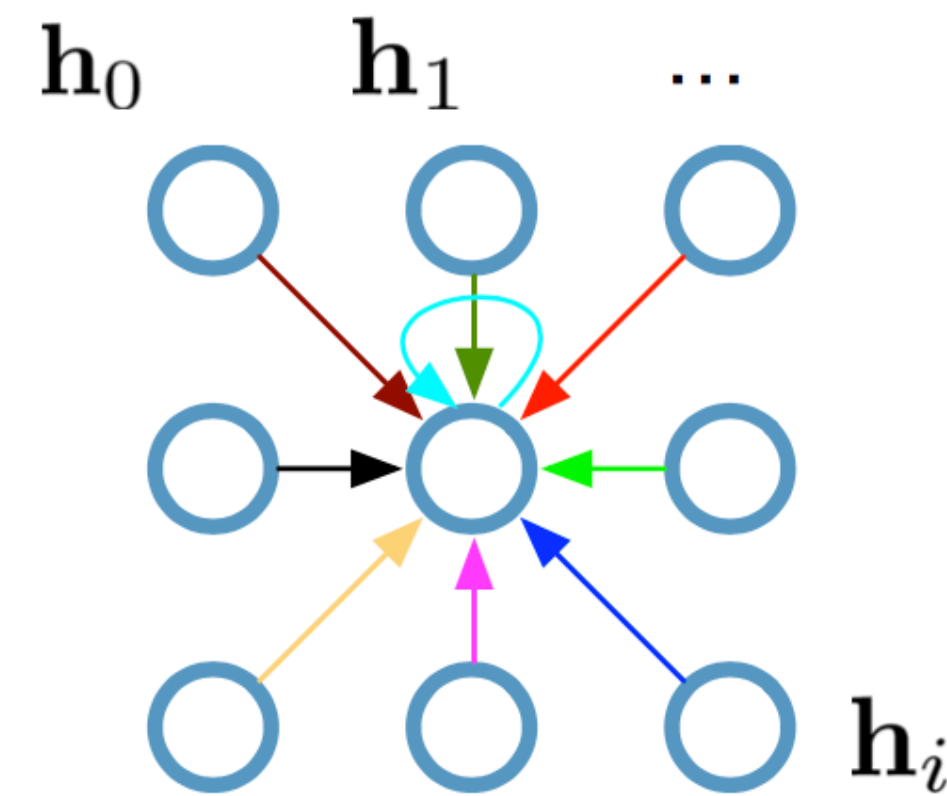
$h_i \in \mathbb{R}^F$ are (hidden layer) activations of a pixel/node

Recap: Convolutional Neural Networks (CNNs) on Grids

Single CNN layer with 3x3 filter:



(Animation by Vincent Dumoulin)



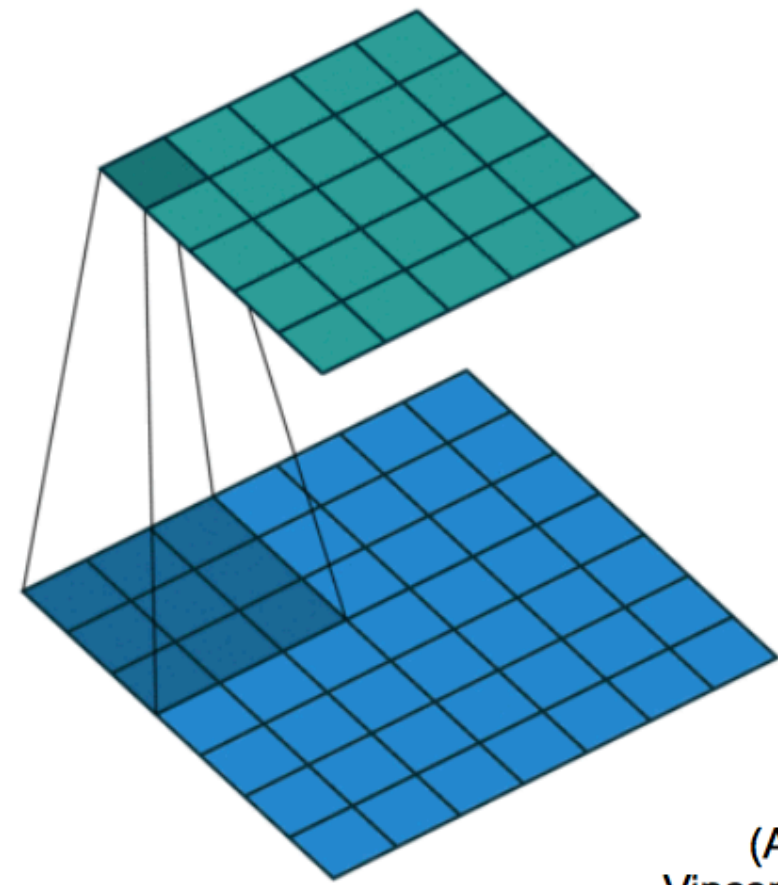
Update for a single pixel:

- Transform messages individually $\mathbf{W}_i \mathbf{h}_i$
- Add everything up $\sum_i \mathbf{W}_i \mathbf{h}_i$

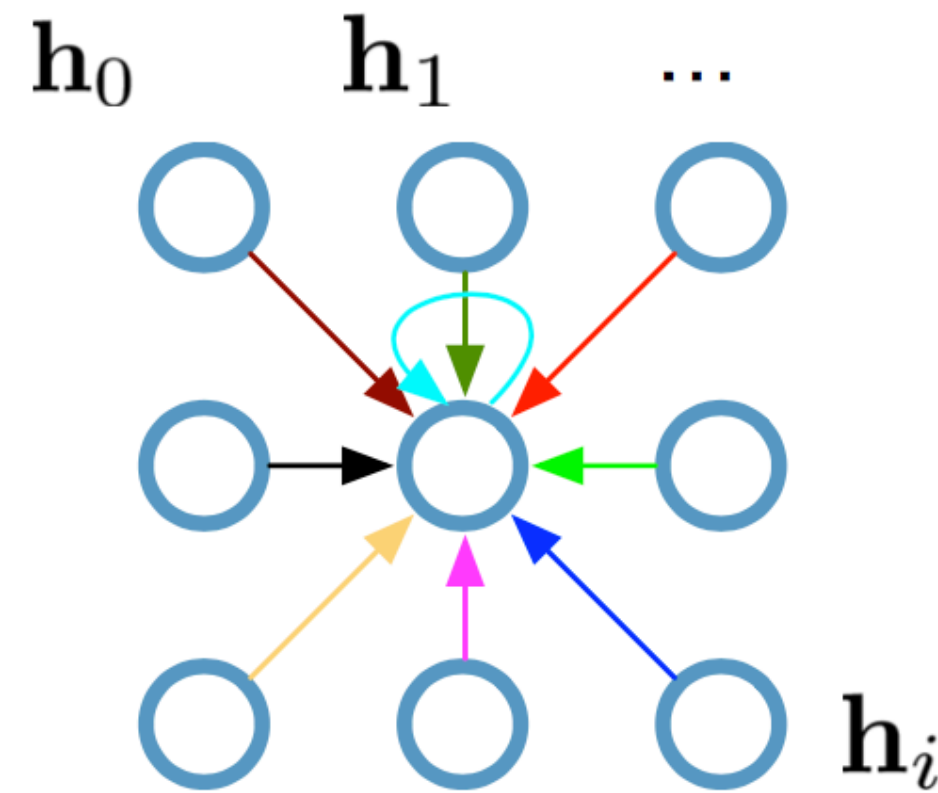
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Recap: Convolutional Neural Networks (CNNs) on Grids

Single CNN layer with 3x3 filter:



(Animation by Vincent Dumoulin)



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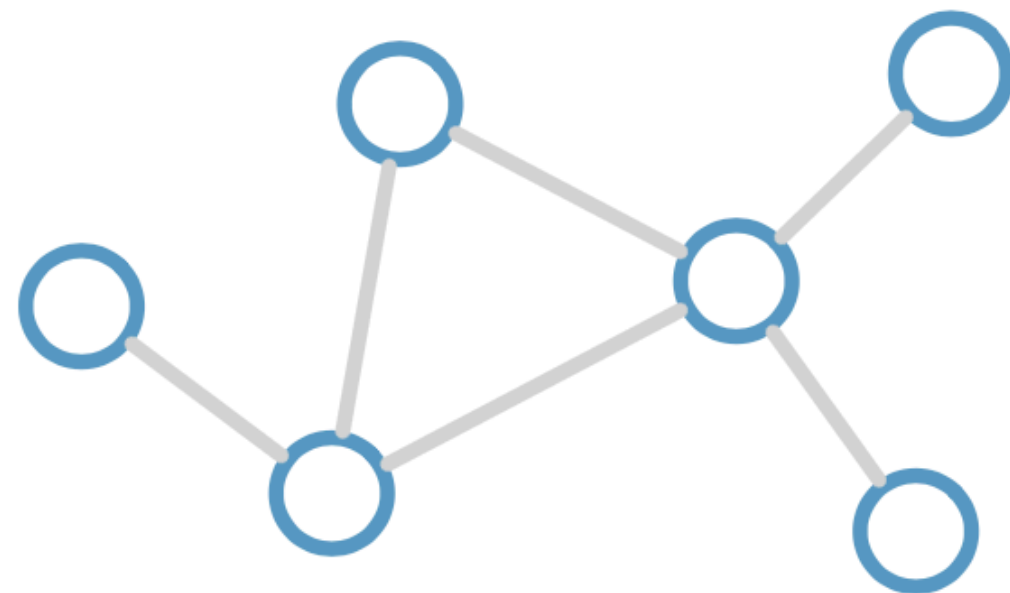
Full update:

$$\mathbf{h}_4^{(l+1)} = \sigma \left(\mathbf{W}_0^{(l)} \mathbf{h}_0^{(l)} + \mathbf{W}_1^{(l)} \mathbf{h}_1^{(l)} + \dots + \mathbf{W}_8^{(l)} \mathbf{h}_8^{(l)} \right)$$

Graph Convolutional Networks (GCNs)

Kipf & Welling (ICLR 2017), related previous works by Duvenaud et al. (NIPS 2015) and Li et al. (ICLR 2016)

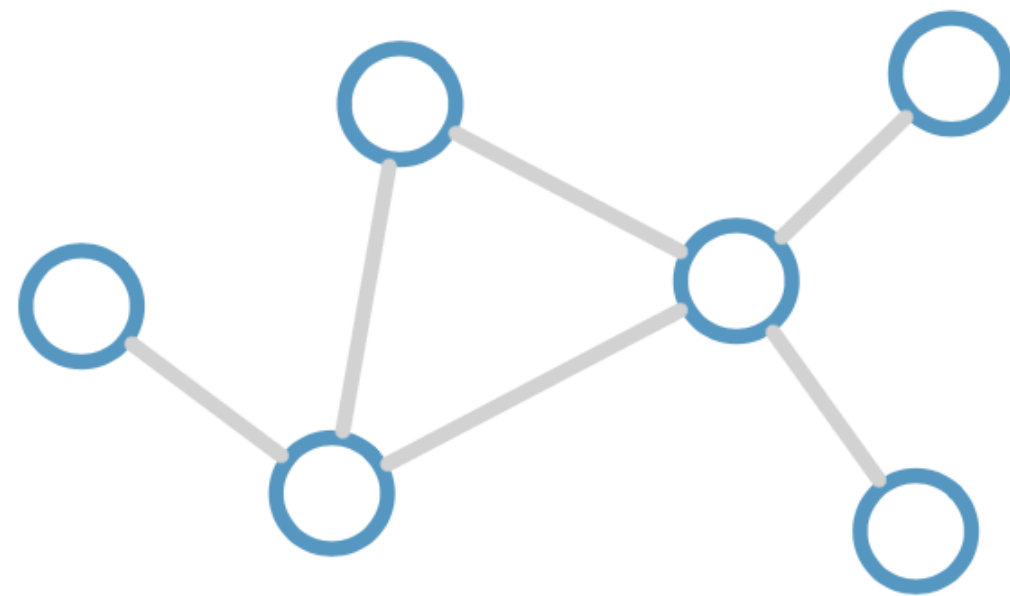
Consider this
undirected graph:



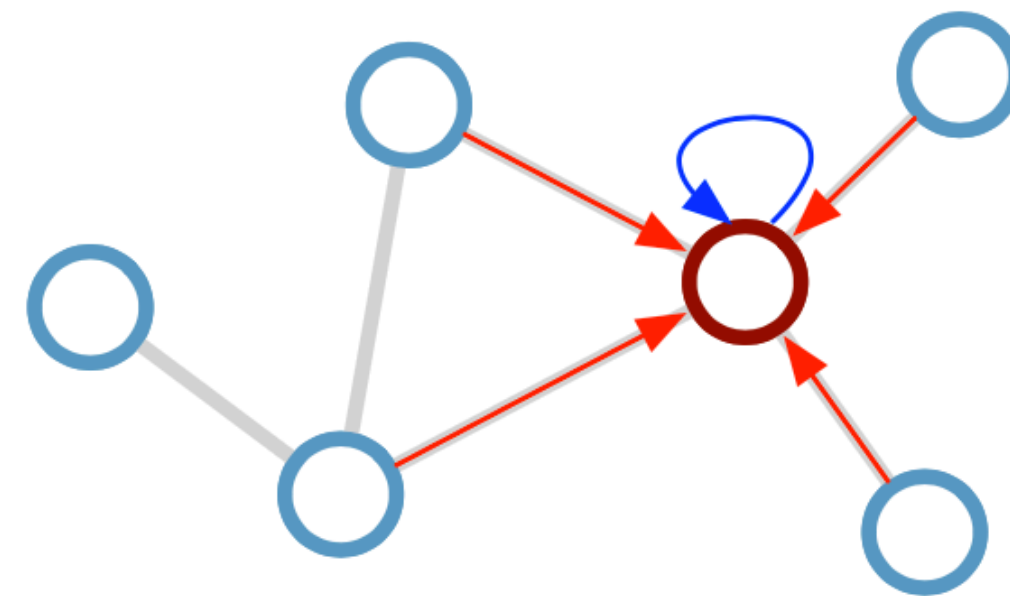
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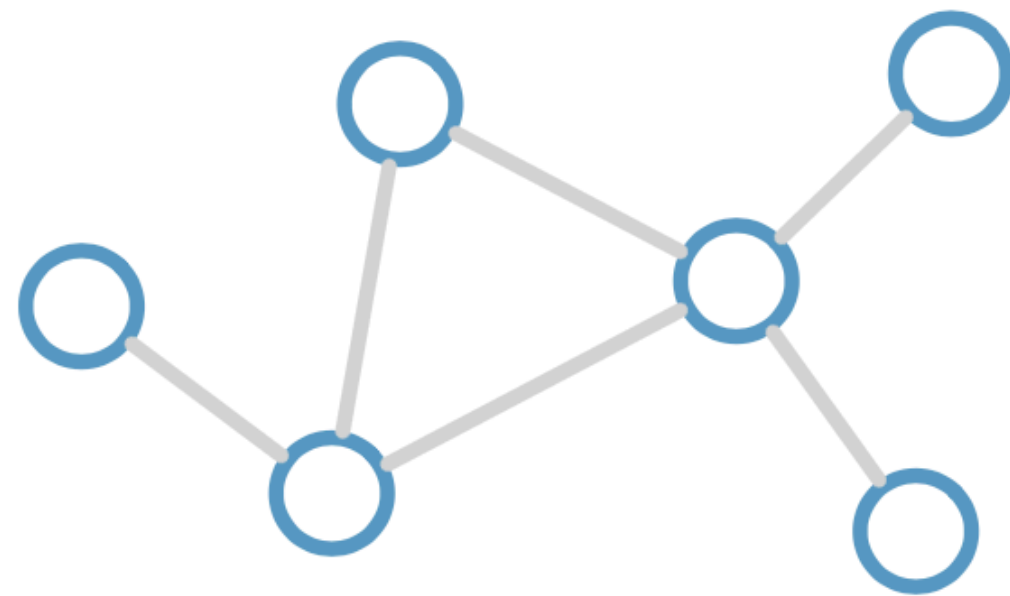
Calculate update for node in red:



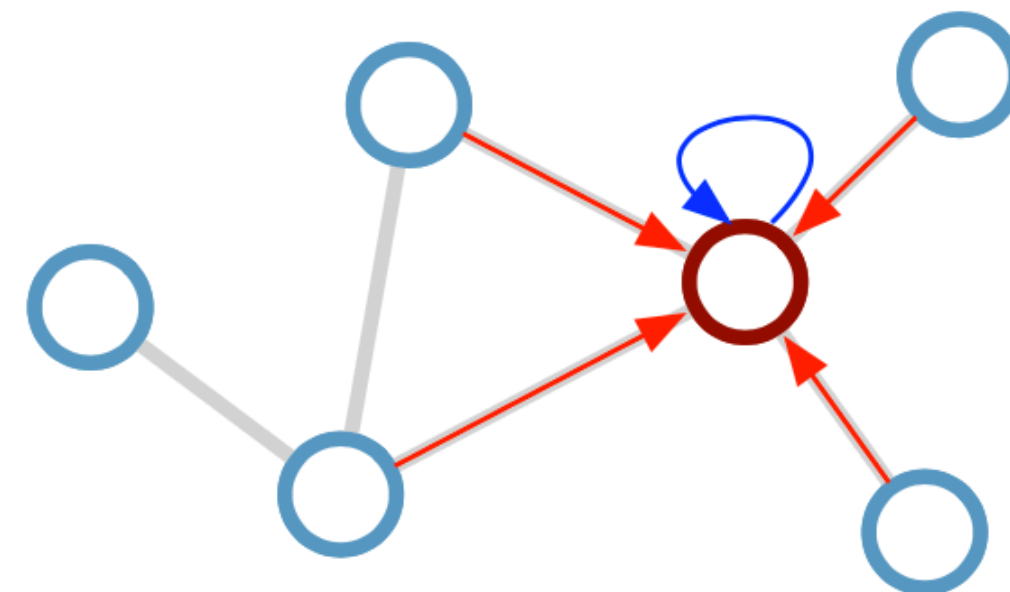
Graph Convolutional Networks (GCNs)

Kipf & Welling (ICLR 2017), related previous works by Duvenaud et al. (NIPS 2015) and Li et al. (ICLR 2016)

Consider this undirected graph:



Calculate update for node in red:



Update rule:

$$\mathbf{h}_i^{(l+1)} = \sigma \left(\mathbf{h}_i^{(l)} \mathbf{W}_0^{(l)} + \sum_{j \in \mathcal{N}_i} \frac{1}{c_{ij}} \mathbf{h}_j^{(l)} \mathbf{W}_1^{(l)} \right)$$

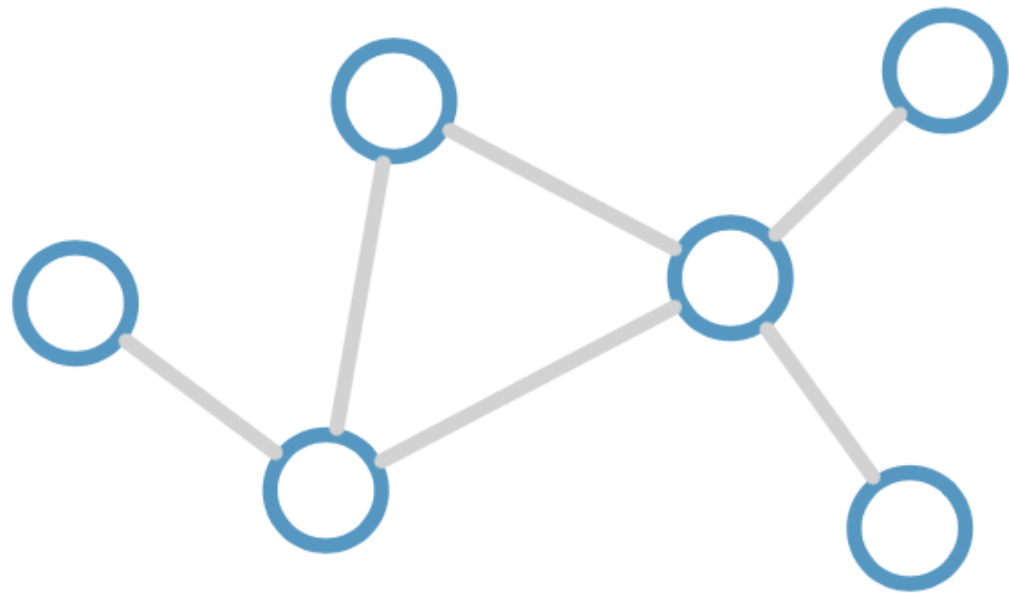
Scalability: subsample messages [Hamilton et al., NIPS 2017]

\mathcal{N}_i : neighbor indices c_{ij} : norm. constant
(fixed/trainable)

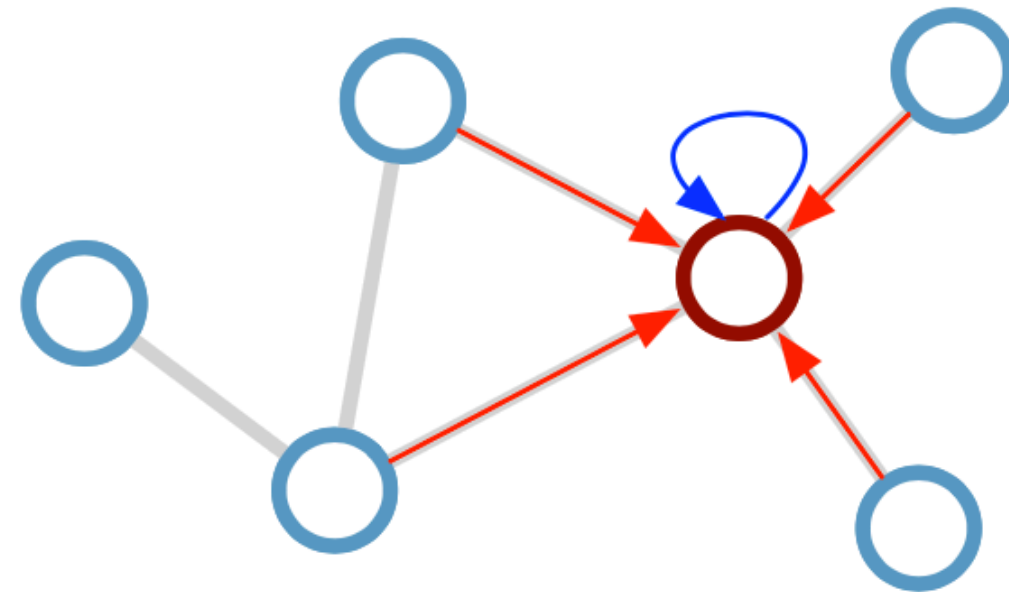
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Scalability: subsample messages [Hamilton et al., NIPS 2017]

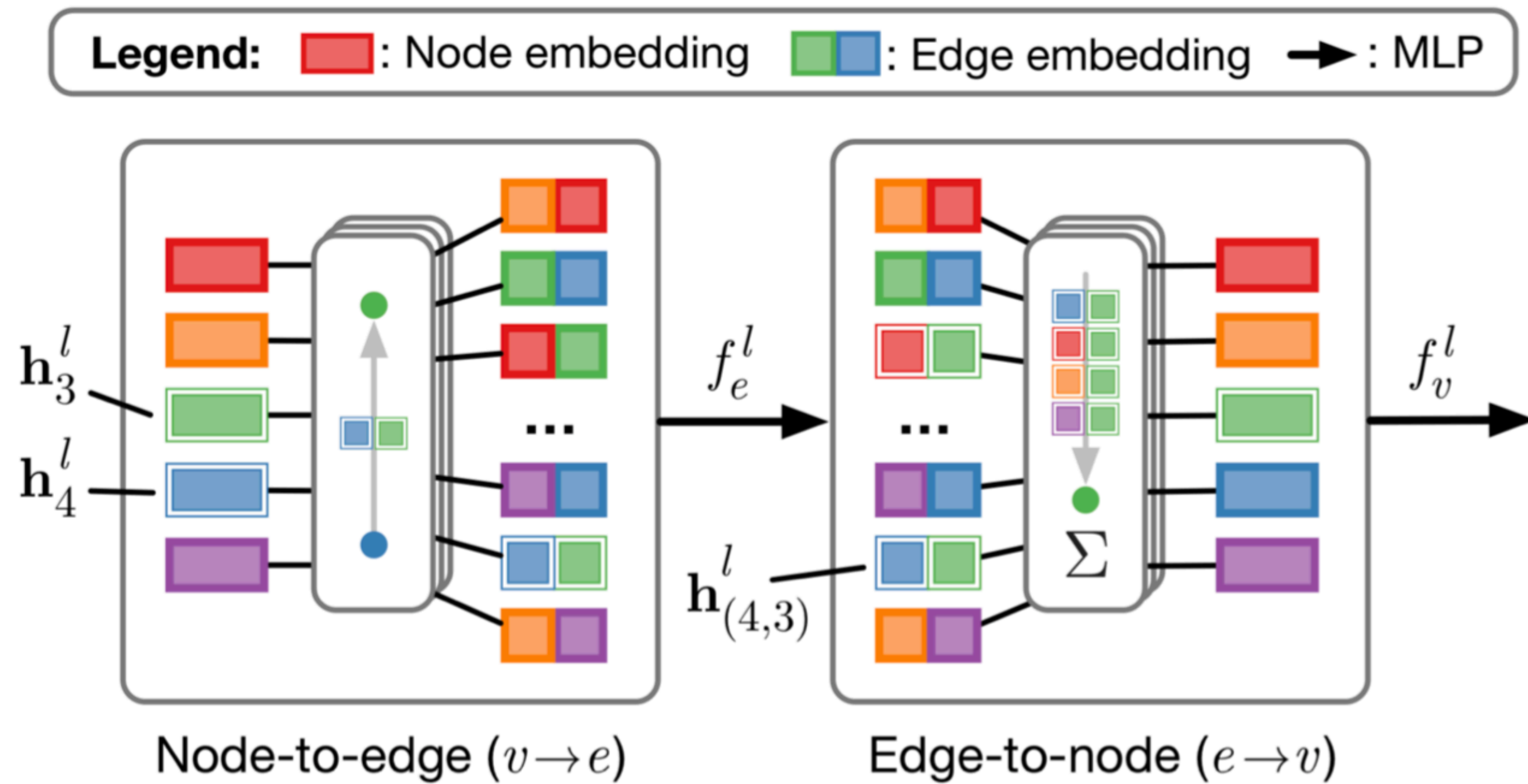
Desirable properties:

- Weight sharing over all locations
- Invariance to permutations
- Linear complexity $O(E)$
- Applicable both in transductive and inductive settings

\mathcal{N}_i : neighbor indices c_{ij} : norm. constant
(fixed/trainable)

GNNs with **Edge** Embeddings

Battaglia et al. (NIPS 2016), Gilmer et al. (ICML 2017), Kipf et al. (ICML 2018)

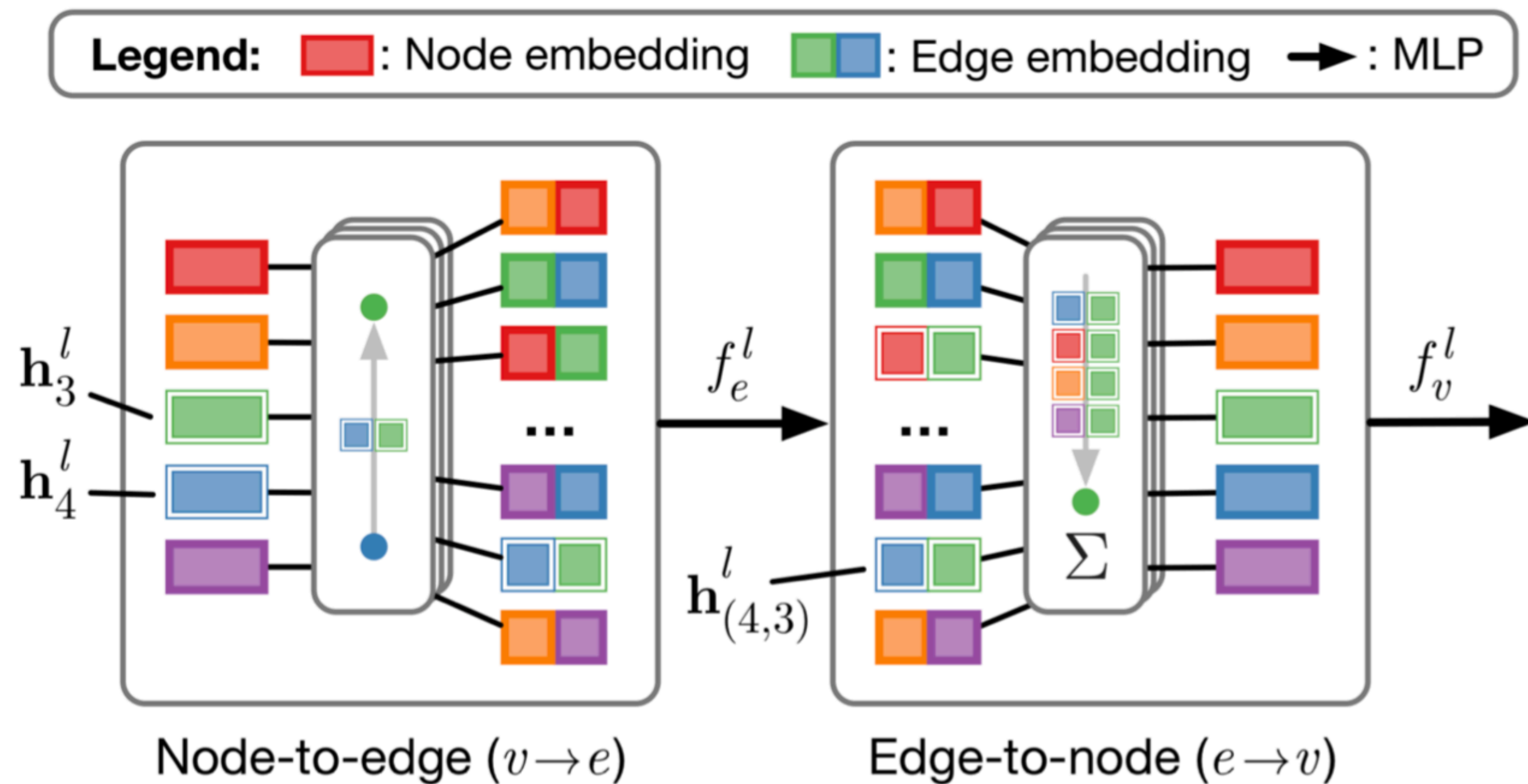


Formally:

$$v \rightarrow e : \mathbf{h}_{(i,j)}^l = f_e^l([\mathbf{h}_i^l, \mathbf{h}_j^l, \mathbf{x}_{(i,j)}])$$
$$e \rightarrow v : \mathbf{h}_j^{l+1} = f_v^l([\sum_{i \in \mathcal{N}_j} \mathbf{h}_{(i,j)}^l, \mathbf{x}_j])$$

GNNs with **Edge** Embeddings

Battaglia et al. (NIPS 2016), Gilmer et al. (ICML 2017), Kipf et al. (ICML 2018)



Pros:

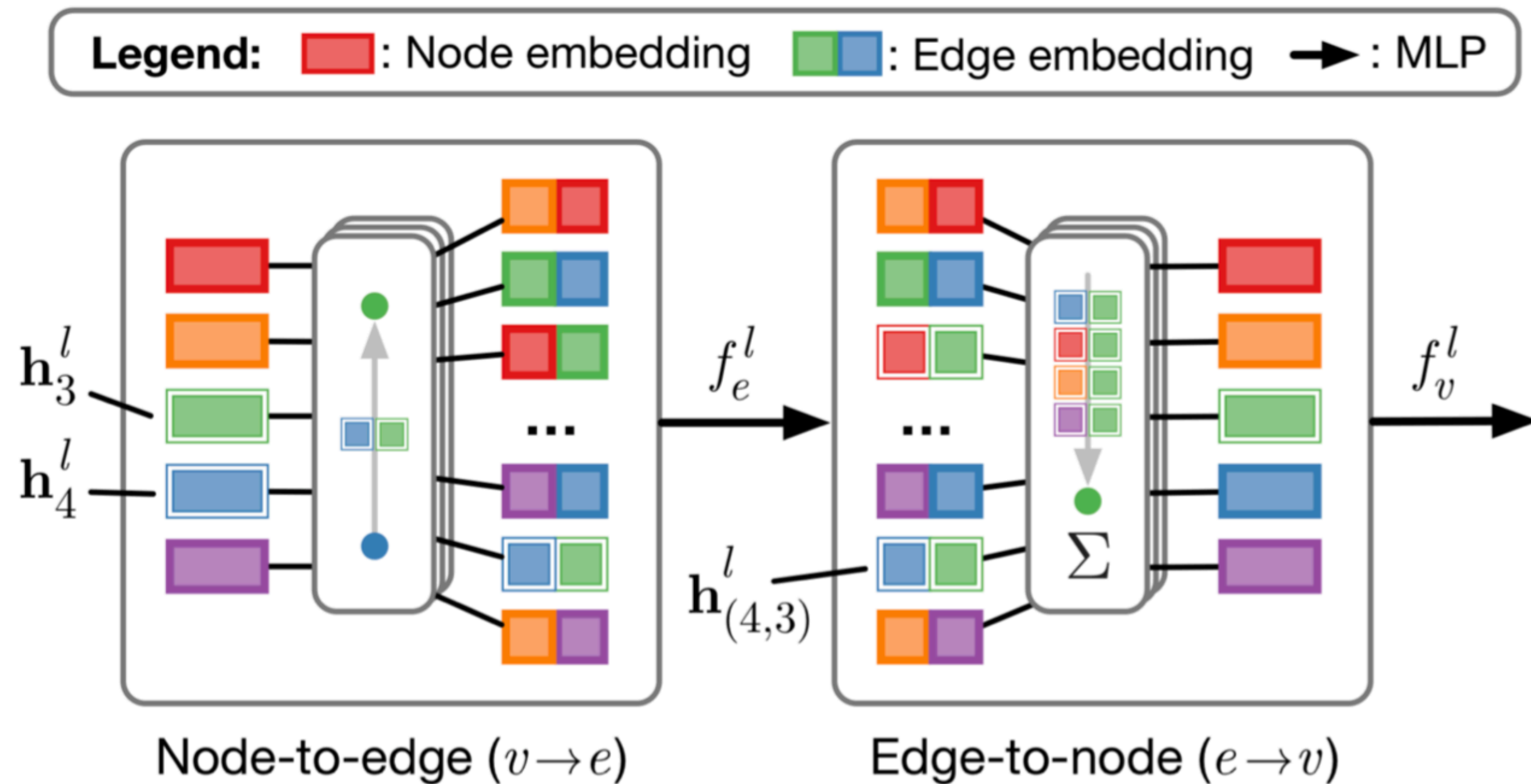
- Supports edge features
- More expressive than GCN
- As general as it gets (?)
- Supports sparse matrix ops

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GNNs with **Edge** Embeddings

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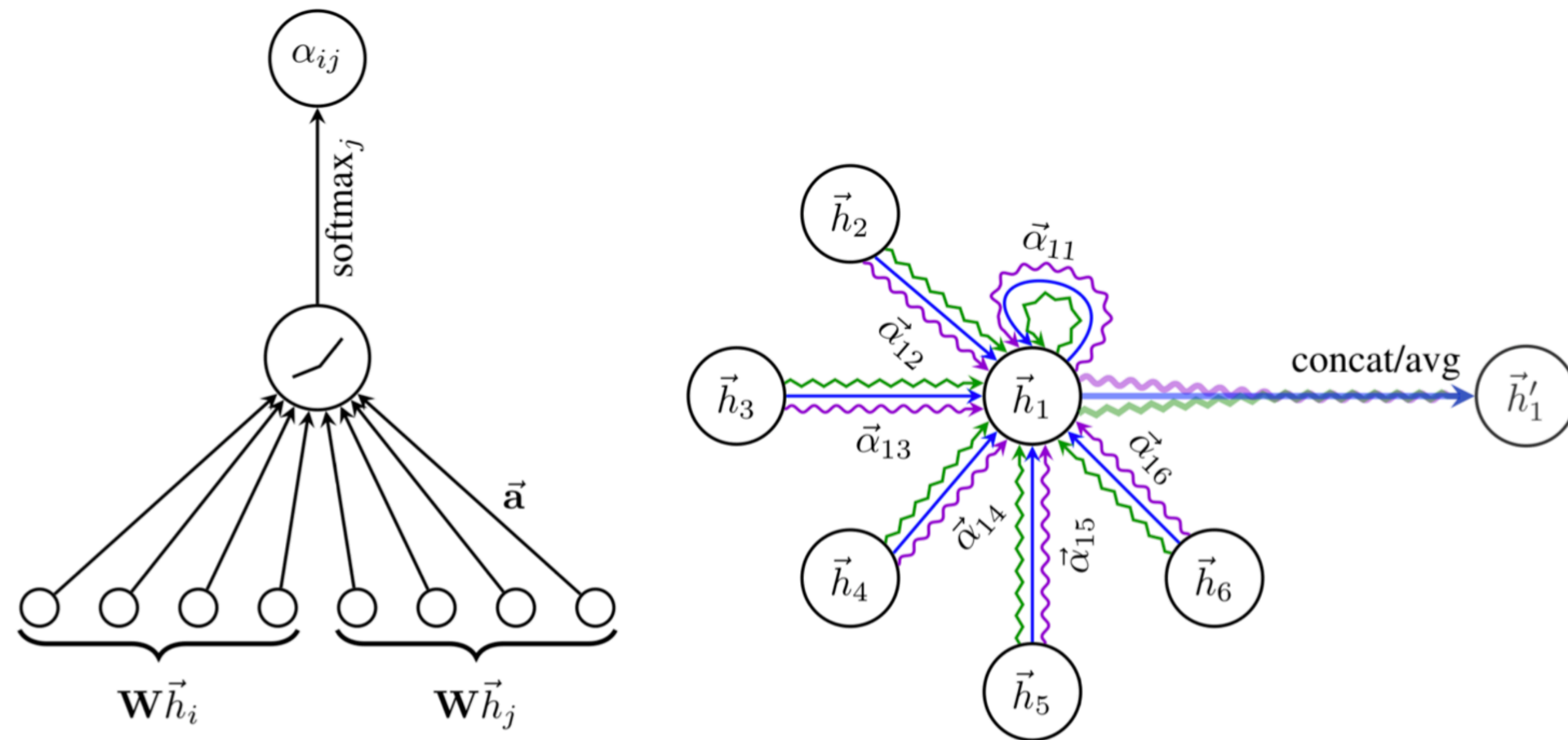
- Supports edge features
- More expressive than GCN
- As general as it gets (?)
- Supports sparse matrix ops

Cons:

- Need to store intermediate edge-based activations
- Difficult to implement with subsampling
- ➔ In practice limited to small graphs

Graph Neural Networks (GNNs) with **Attention**

Monti et al. (CVPR 2017), Hoshen (NIPS 2017), Veličković et al. (ICLR 2018)

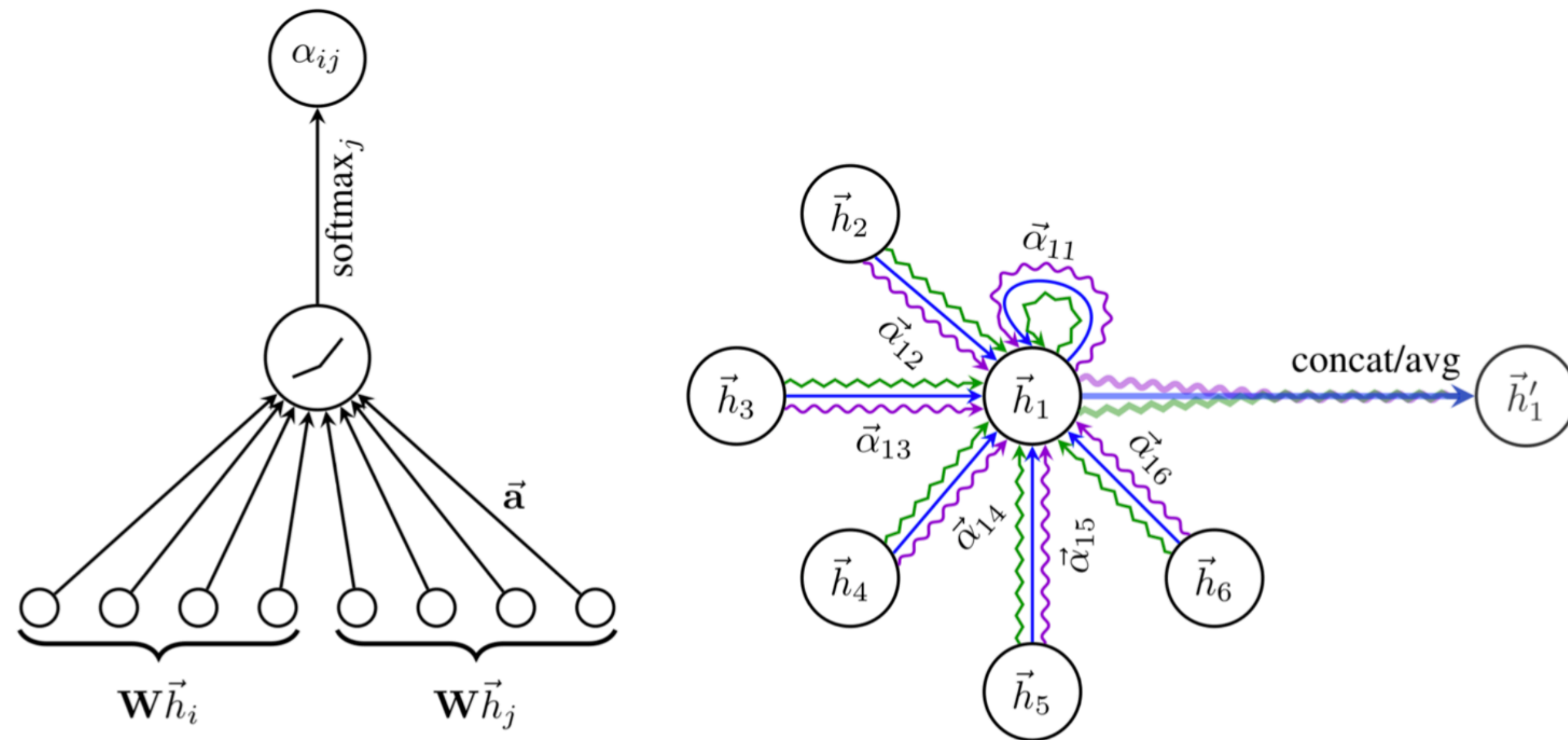


[Figure from Veličković et al. (ICLR 2018)]

$$\vec{h}'_i = \sigma \left(\frac{1}{K} \sum_{k=1}^K \sum_{j \in \mathcal{N}_i} \alpha_{ij}^k \mathbf{W}^k \vec{h}_j \right)$$

Graph Neural Networks (GNNs) with **Attention**

Monti et al. (CVPR 2017), Hoshen (NIPS 2017), Veličković et al. (ICLR 2018)

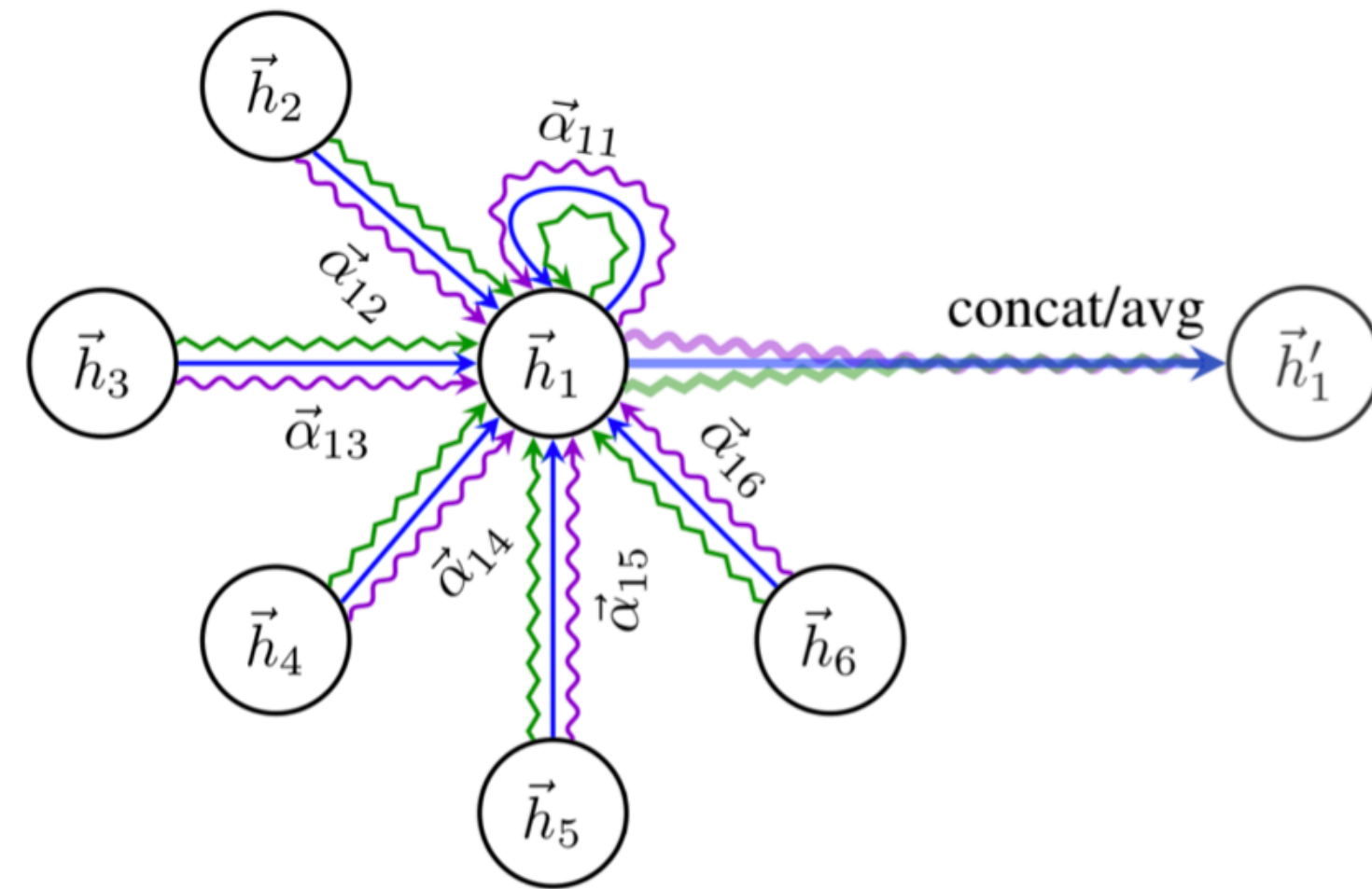
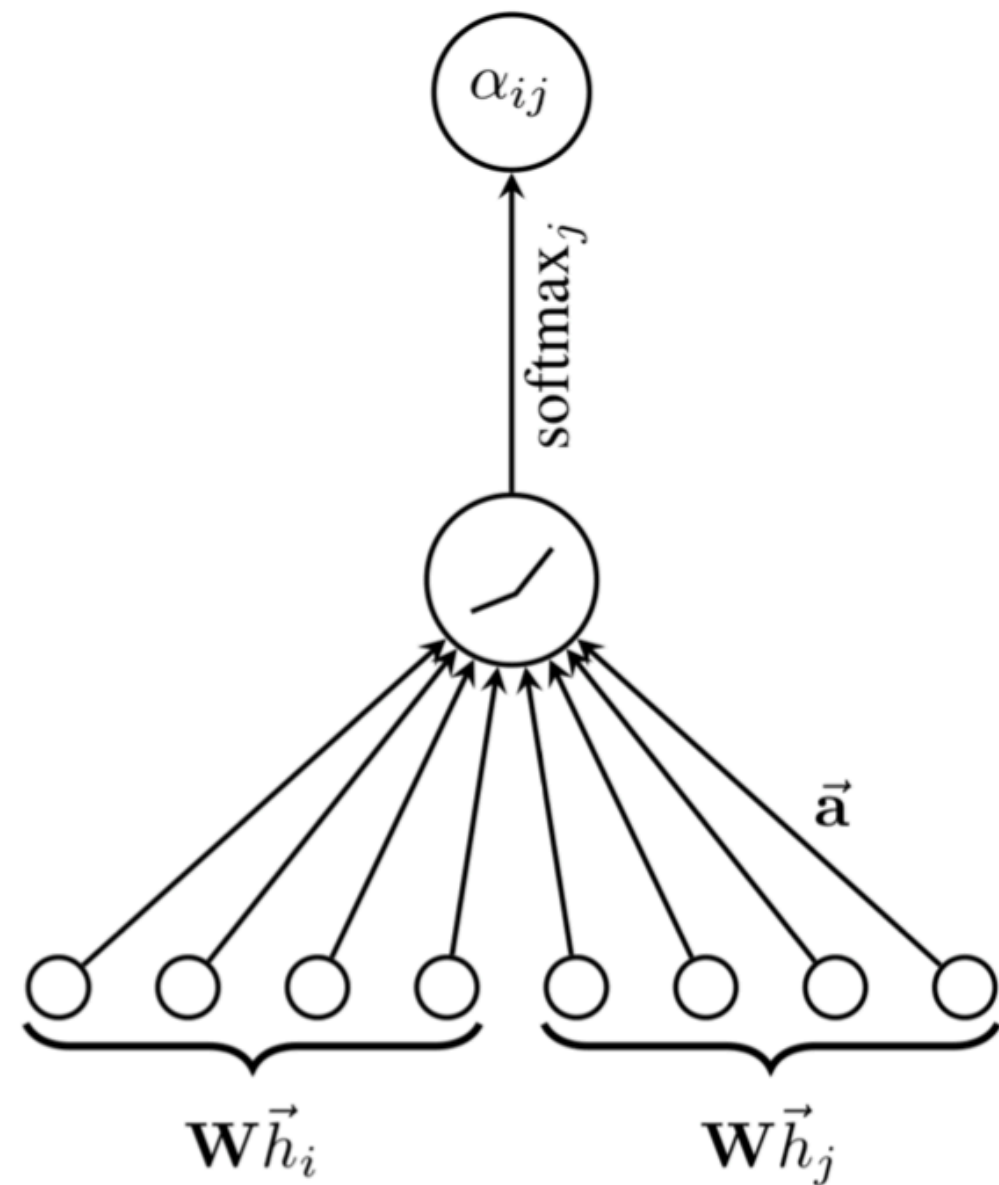


[Figure from Veličković et al. (ICLR 2018)]

$$\vec{h}'_i = \sigma \left(\frac{1}{K} \sum_{k=1}^K \sum_{j \in \mathcal{N}_i} \alpha_{ij}^k \mathbf{W}^k \vec{h}_j \right) \quad \alpha_{ij} = \frac{\exp \left(\text{LeakyReLU} \left(\vec{\mathbf{a}}^T [\mathbf{W}\vec{h}_i \parallel \mathbf{W}\vec{h}_j] \right) \right)}{\sum_{k \in \mathcal{N}_i} \exp \left(\text{LeakyReLU} \left(\vec{\mathbf{a}}^T [\mathbf{W}\vec{h}_i \parallel \mathbf{W}\vec{h}_k] \right) \right)}$$

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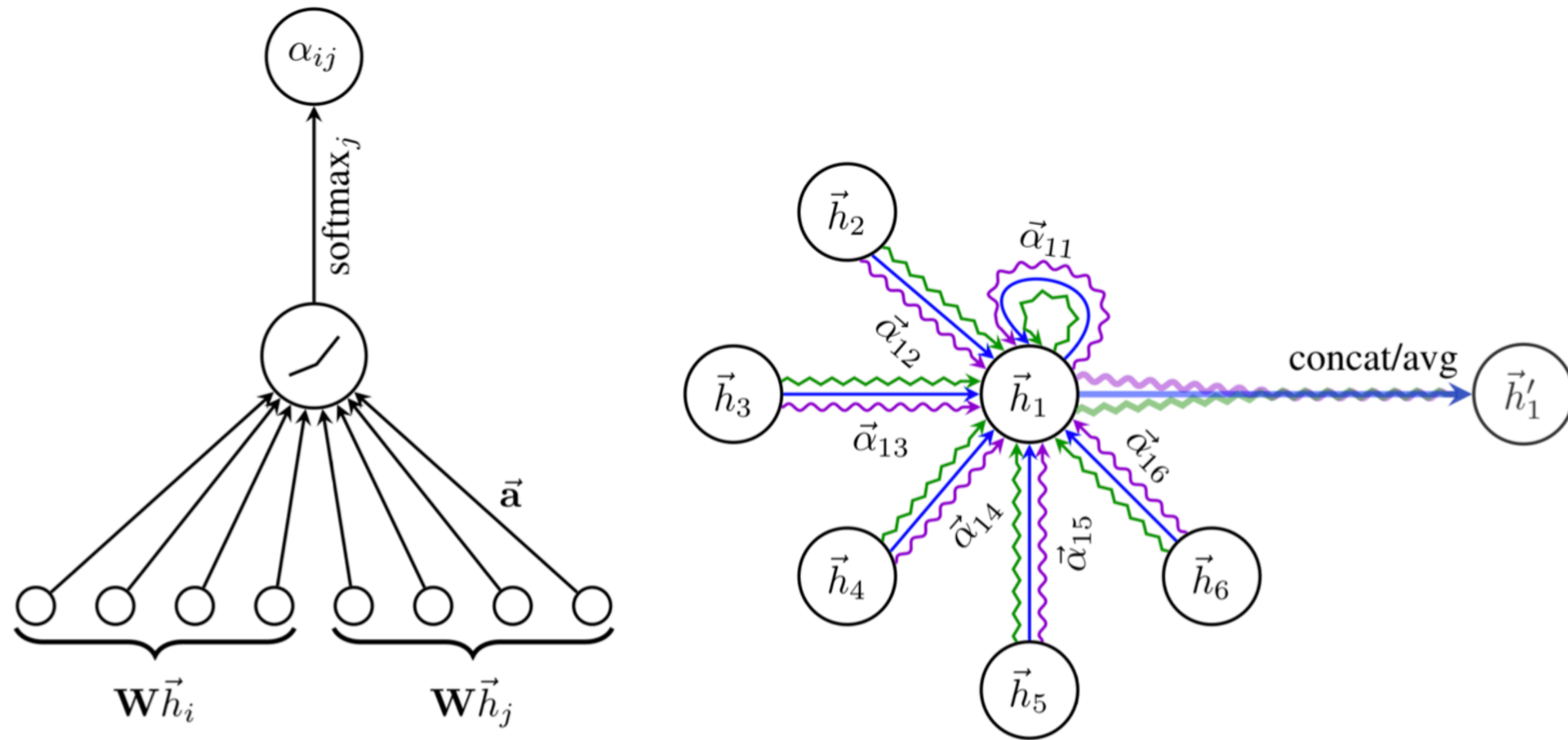
Pros:

- No need to store intermediate edge-based activation vectors (when using dot-product attn.)
- Slower than GCNs but faster than GNNs with edge embeddings

$$\vec{h}'_i = \sigma \left(\frac{1}{K} \sum_{k=1}^K \sum_{j \in \mathcal{N}_i} \alpha_{ij}^k \mathbf{W}^k \vec{h}_j \right) \quad \alpha_{ij} = \frac{\exp \left(\text{LeakyReLU} \left(\vec{a}^T [\mathbf{W} \vec{h}_i \| \mathbf{W} \vec{h}_j] \right) \right)}{\sum_{k \in \mathcal{N}_i} \exp \left(\text{LeakyReLU} \left(\vec{a}^T [\mathbf{W} \vec{h}_i \| \mathbf{W} \vec{h}_k] \right) \right)}$$

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Pros:

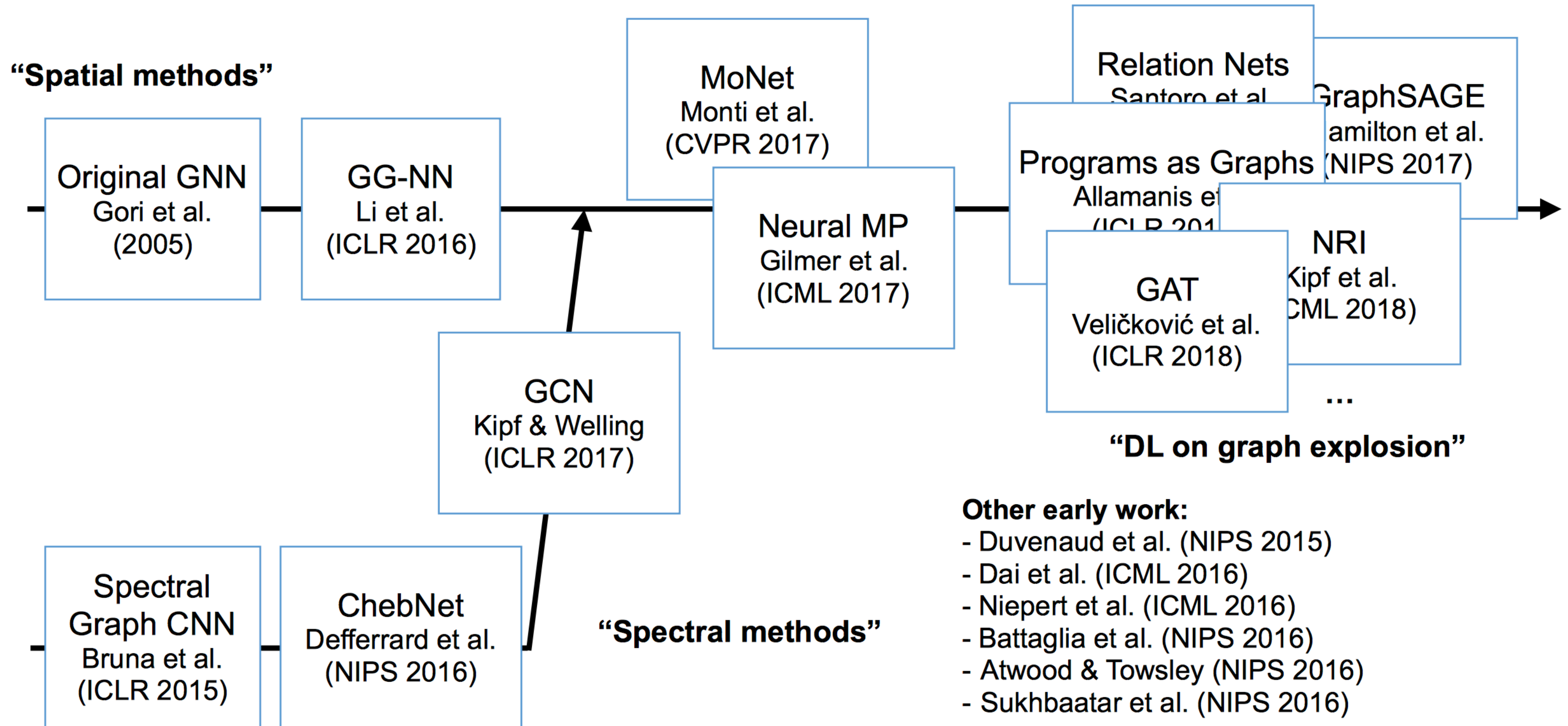
- No need to store intermediate edge-based activation vectors (when using dot-product attn.)
- Slower than GCNs but faster than GNNs with edge embeddings

Cons:

- (Most likely) less expressive than GNNs with edge embeddings
- Can be more difficult to optimize

$$\vec{h}'_i = \sigma \left(\frac{1}{K} \sum_{k=1}^K \sum_{j \in \mathcal{N}_i} \alpha_{ij}^k \mathbf{W}^k \vec{h}_j \right) \quad \alpha_{ij} = \frac{\exp \left(\text{LeakyReLU} \left(\vec{\mathbf{a}}^T [\mathbf{W} \vec{h}_i \| \mathbf{W} \vec{h}_j] \right) \right)}{\sum_{k \in \mathcal{N}_i} \exp \left(\text{LeakyReLU} \left(\vec{\mathbf{a}}^T [\mathbf{W} \vec{h}_i \| \mathbf{W} \vec{h}_k] \right) \right)}$$

A Brief History of Graph Neural Nets

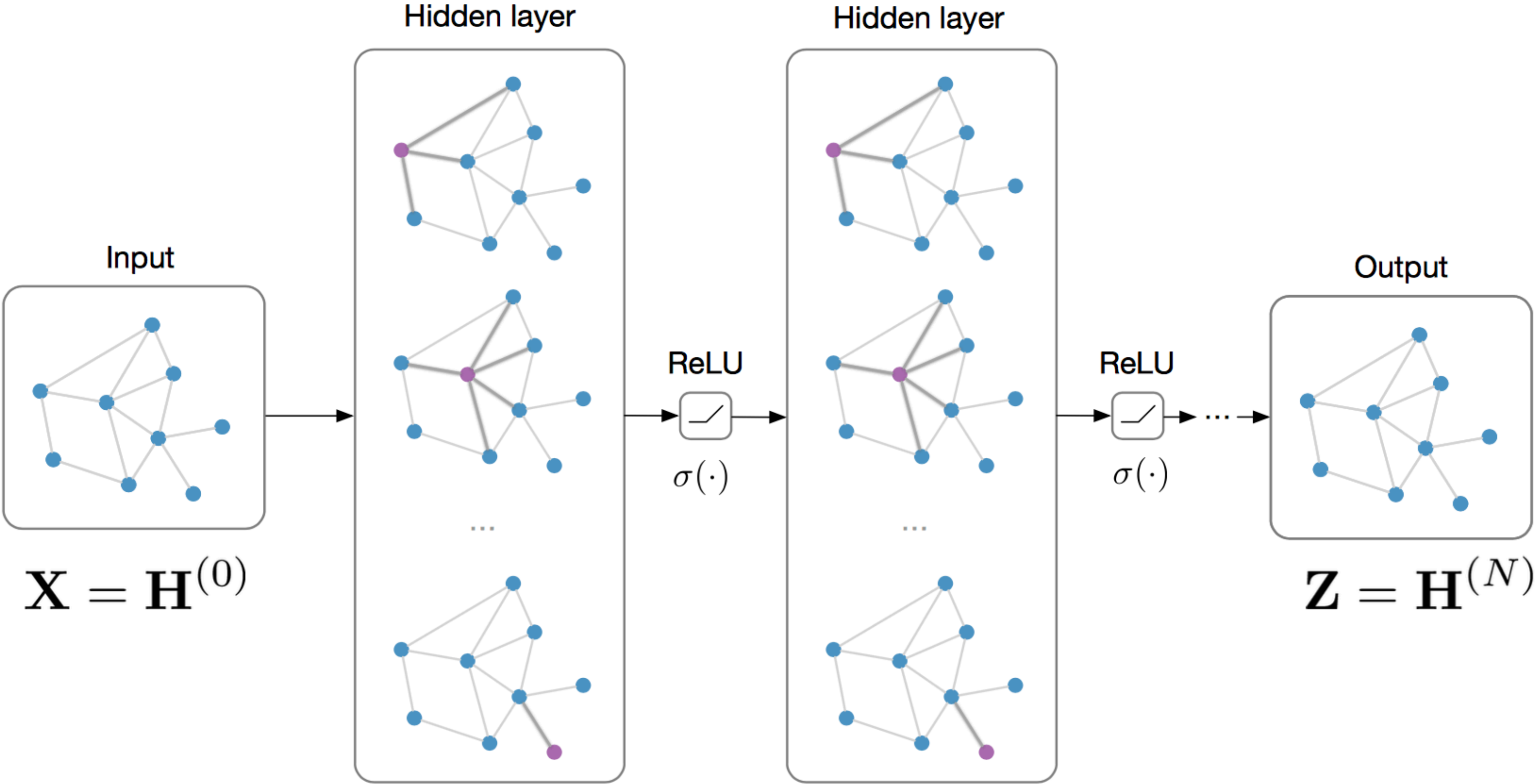


(slide inspired by Alexander Gaunt’s talk on GNNs)

How do we use GNN / GCN for real problems?

Classification and Link Prediction with GNNs / GCNs

Input: Feature matrix $\mathbf{X} \in \mathbb{R}^{N \times E}$, preprocessed adjacency matrix $\hat{\mathbf{A}}$

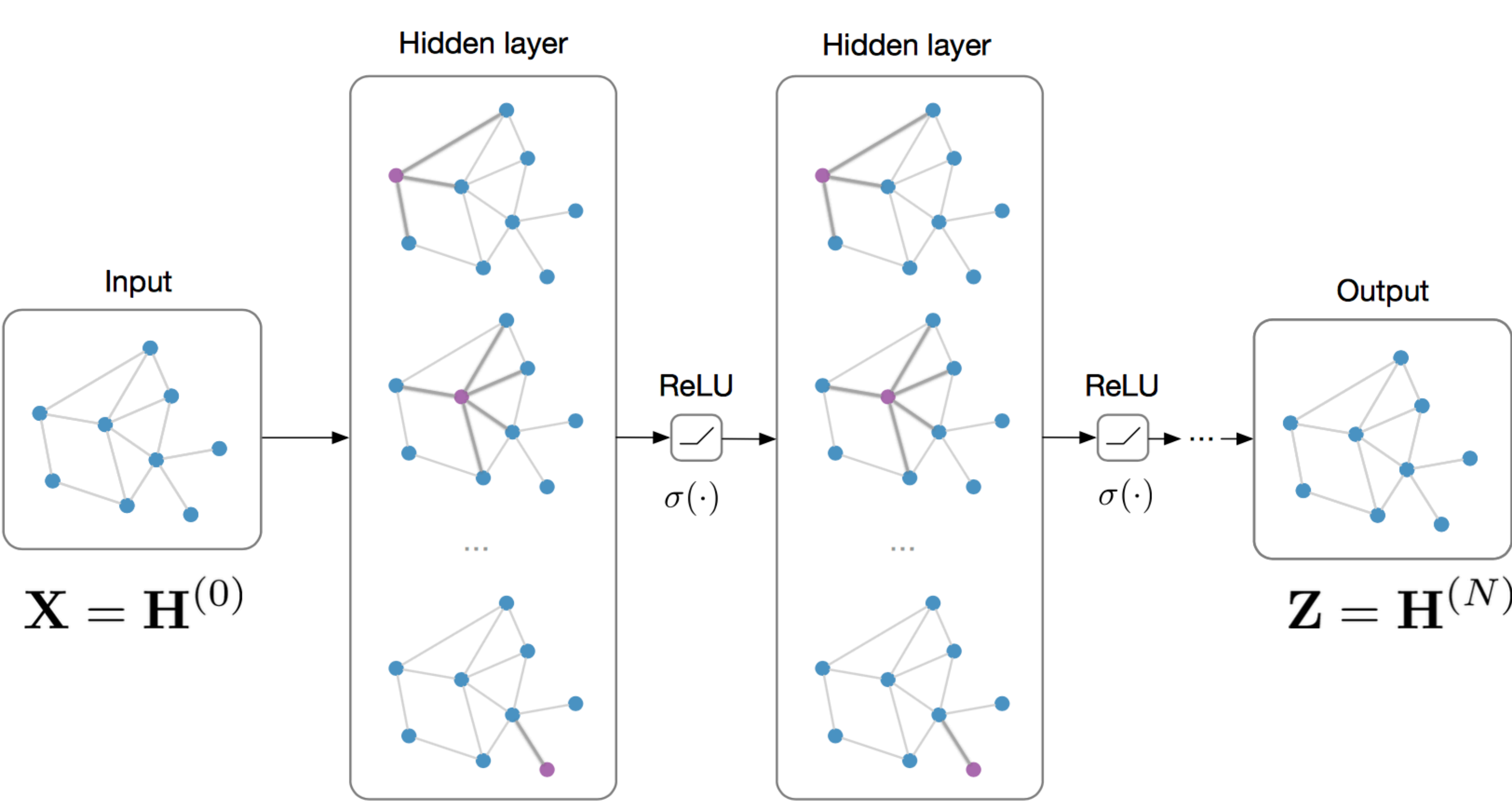


$$\mathbf{H}^{(l+1)} = \sigma \left(\hat{\mathbf{A}} \mathbf{H}^{(l)} \mathbf{W}^{(l)} \right)$$

* slide from Thomas Kipf, **University of Amsterdam**

Classification and Link Prediction with GNNs / GCNs

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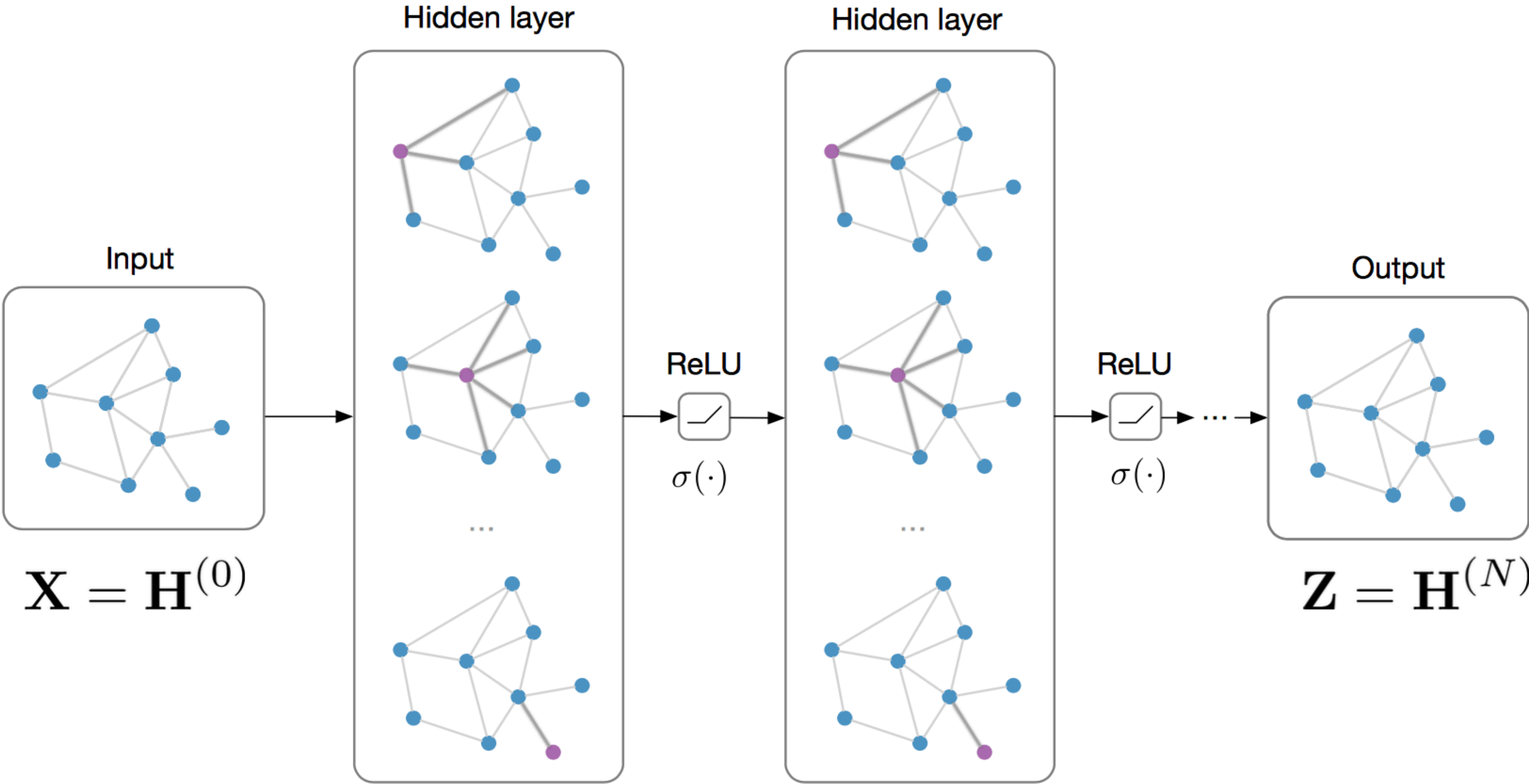
Node classification:
 $\text{softmax}(\mathbf{z}_n)$
e.g. Kipf & Welling (ICLR 2017)

$$\mathbf{H}^{(l+1)} = \sigma \left(\hat{\mathbf{A}} \mathbf{H}^{(l)} \mathbf{W}^{(l)} \right)$$

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Classification and Link Prediction with GNNs / GCNs

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$$\text{softmax}(\mathbf{z}_n)$$

e.g. Kipf & Welling (ICLR 2017)

Graph classification:

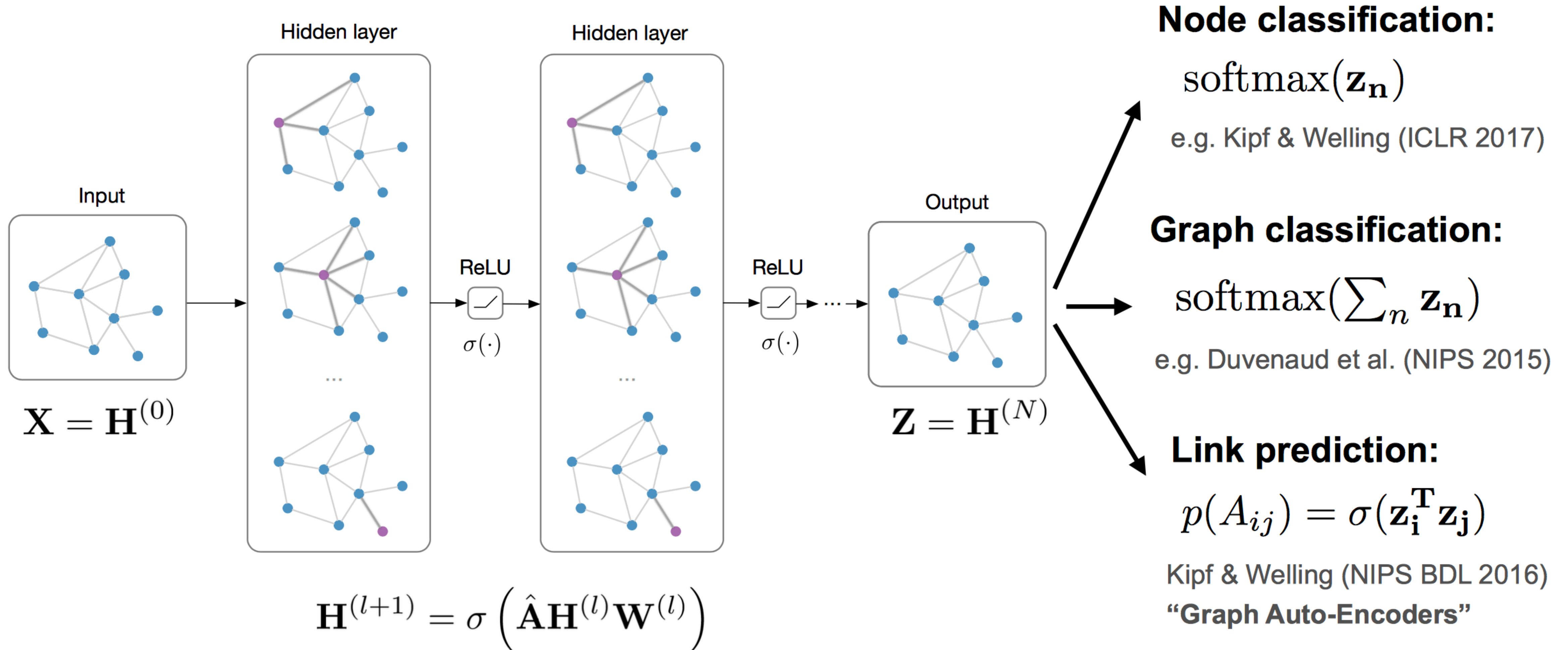
$$\text{softmax}(\sum_n \mathbf{z}_n)$$

e.g. Duvenaud et al. (NIPS 2015)

* slide from Thomas Kipf, University of Amsterdam

Classification and Link Prediction with GNNs / GCNs

Input: Feature matrix $\mathbf{X} \in \mathbb{R}^{N \times E}$, preprocessed adjacency matrix $\hat{\mathbf{A}}$



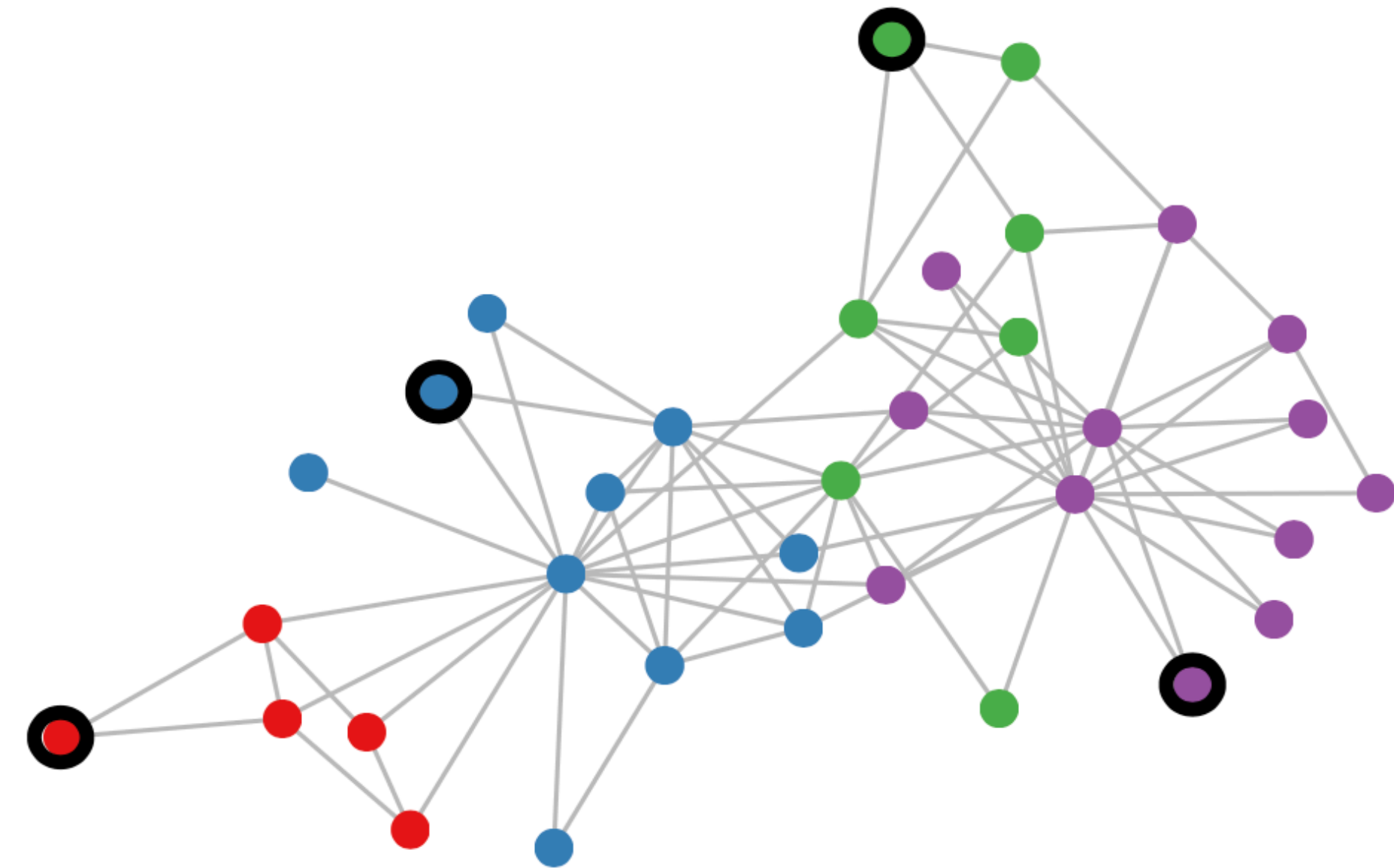
Semi-supervised Classification on Graphs

Setting:

Some nodes are labeled (black circle)
All other nodes are unlabeled

Task:

Predict node label of unlabeled nodes



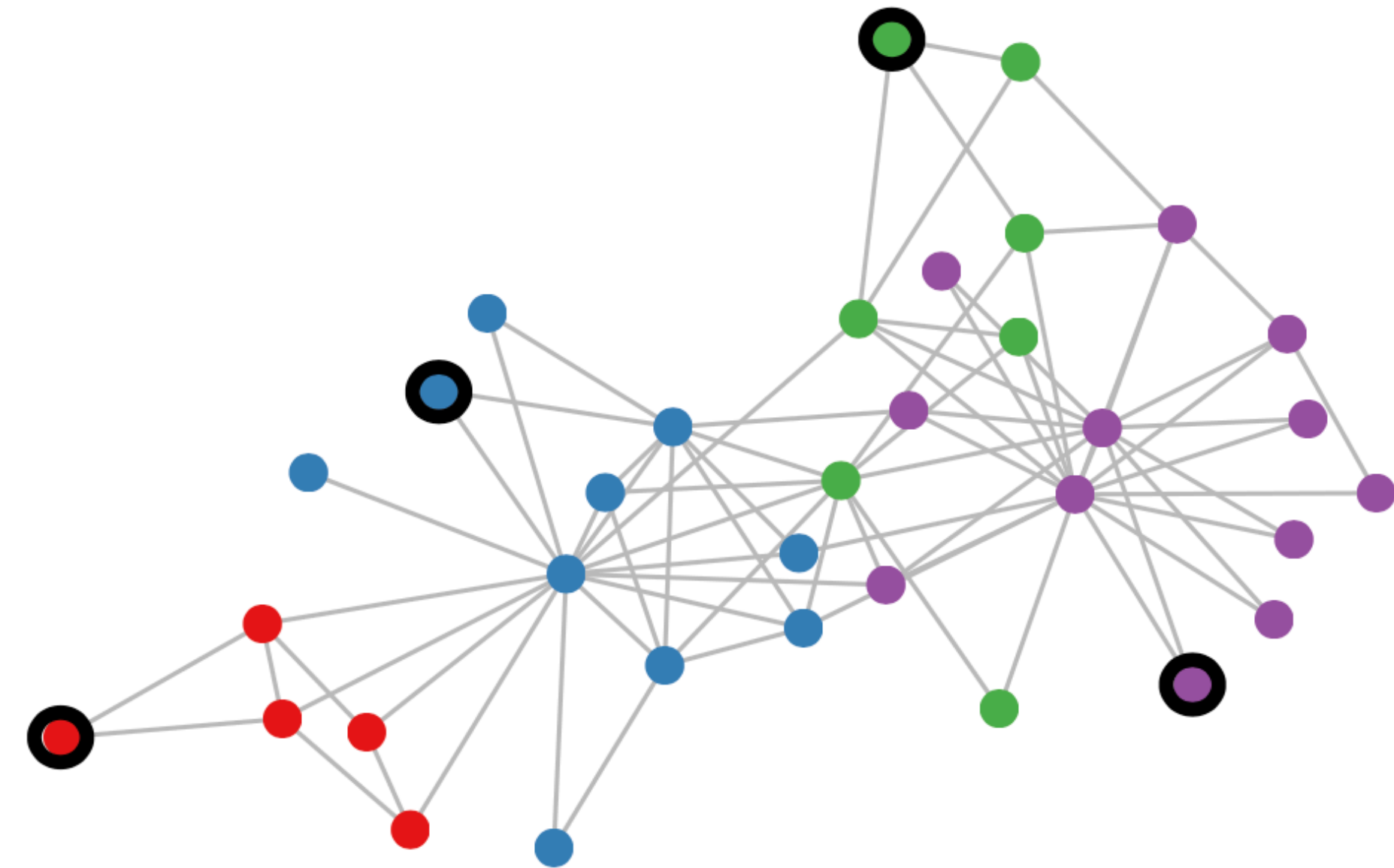
Semi-supervised Classification on Graphs

Setting:

Some nodes are labeled (black circle)
All other nodes are unlabeled

Task:

Predict node label of unlabeled nodes



Evaluate loss on labeled nodes only:

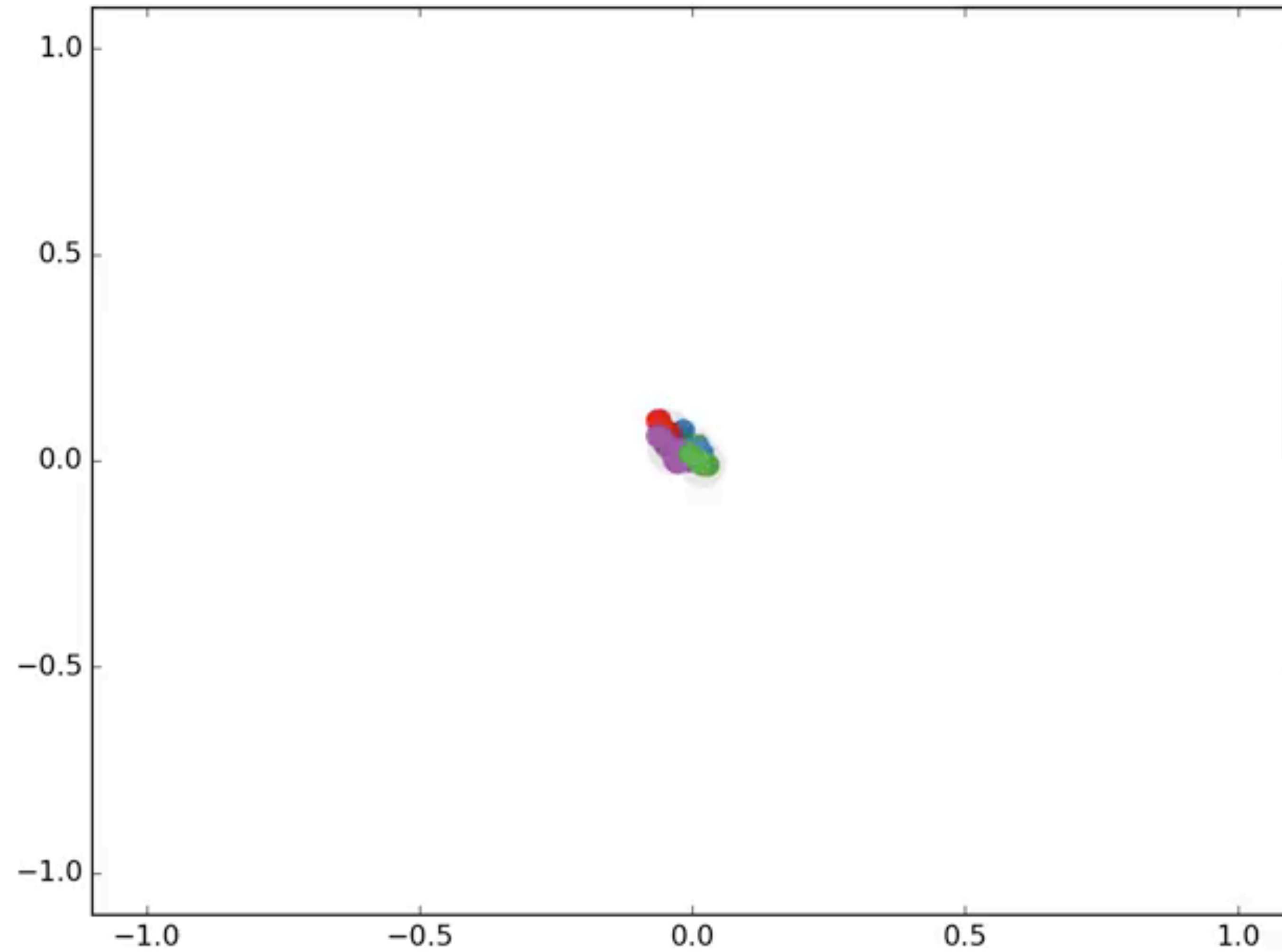
$$\mathcal{L} = - \sum_{l \in \mathcal{Y}_L} \sum_{f=1}^F Y_{lf} \ln Z_{lf}$$

\mathcal{Y}_L set of labeled node indices

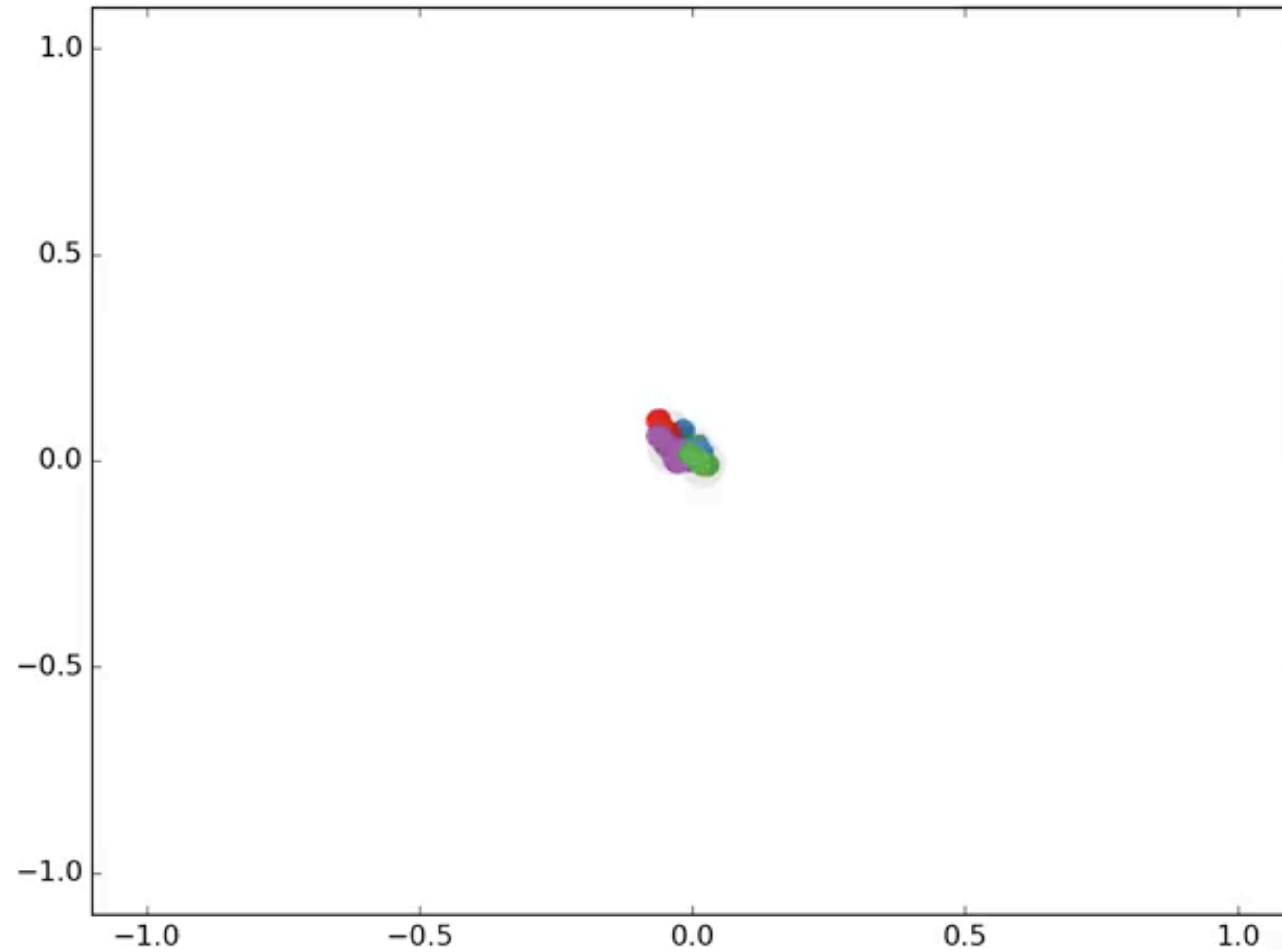
\mathbf{Y} label matrix

\mathbf{Z} GCN output (after softmax)

Semi-supervised Classification on Graphs



Semi-supervised Classification on Graphs



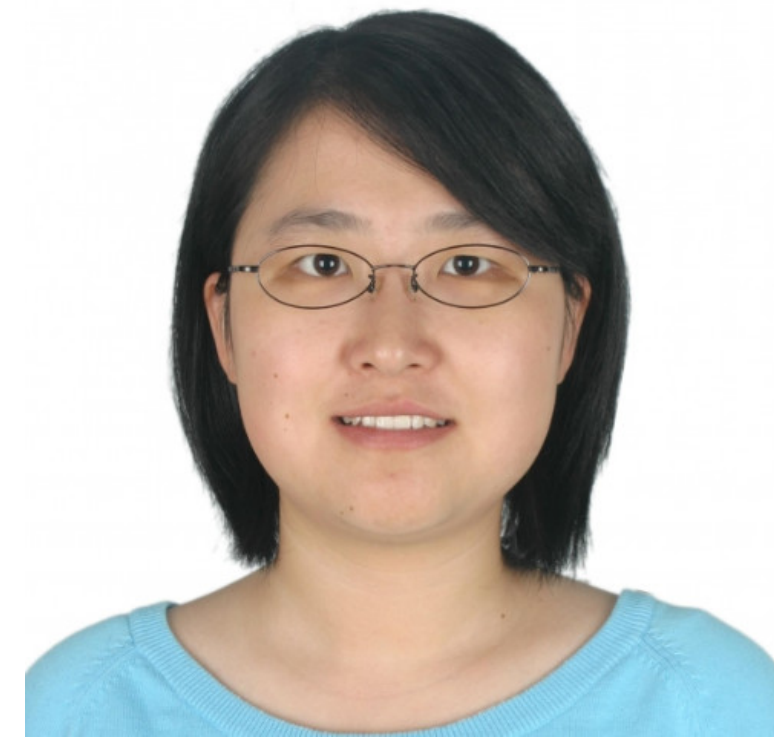
Graph Neural Nets (GNNs) are strict Generalizations of Traditional Neural Nets

(CNNs / RNNs can be implemented using GNNs / GCNs, but this is inefficient)

G³raphGround: Graph-based Language Grounding



Mohit Bajaj



Lanjun Wang



Leonid Sigal



Image Grounding: Beyond Object Detection

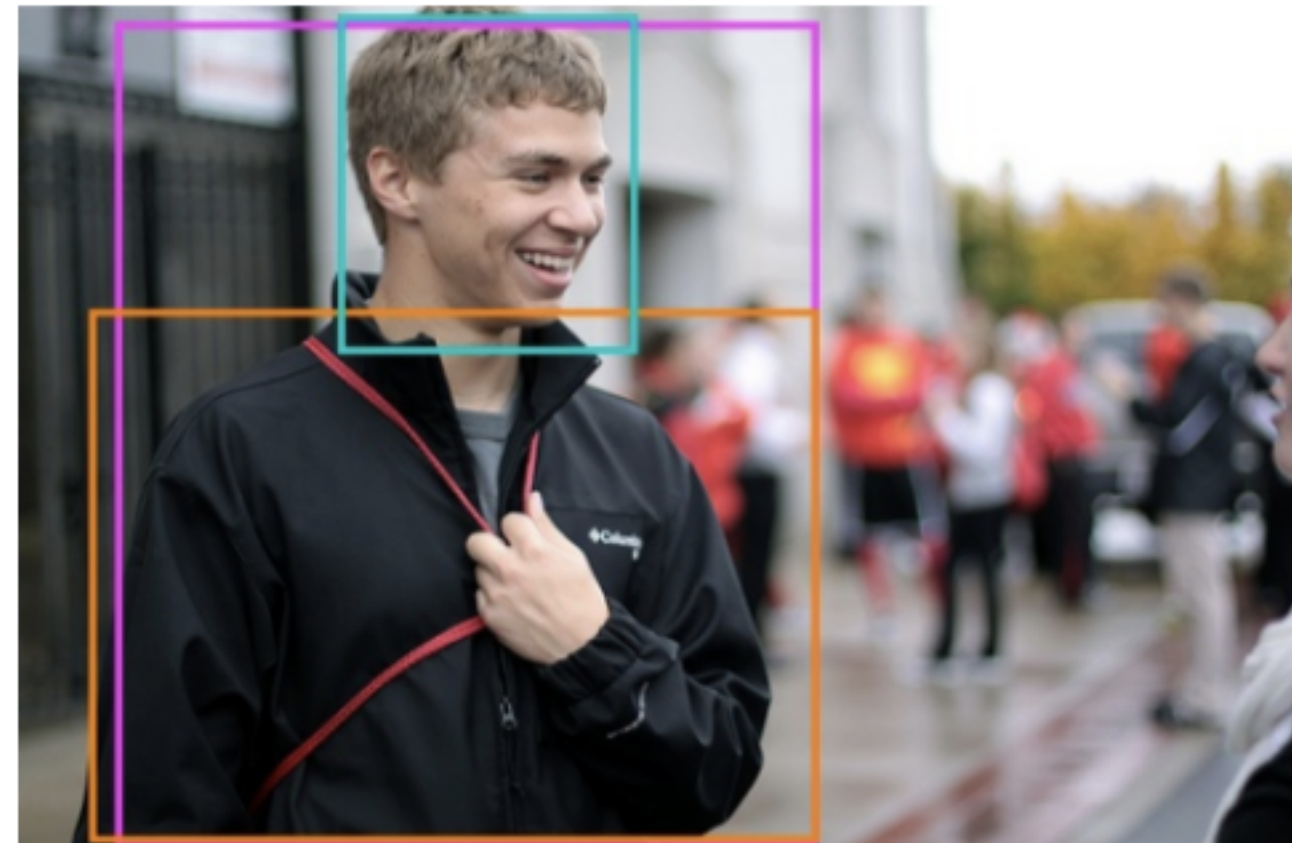
Given the **image** and one or more **natural language phrases**, locate regions that correspond to those phrases.



A man wearing a black-jacket has a smile on his face.

Image Grounding: Beyond Object Detection

Given the **image** and one or more **natural language phrases**, locate regions that correspond to those phrases.



A man wearing a black-jacket has a smile on his face.

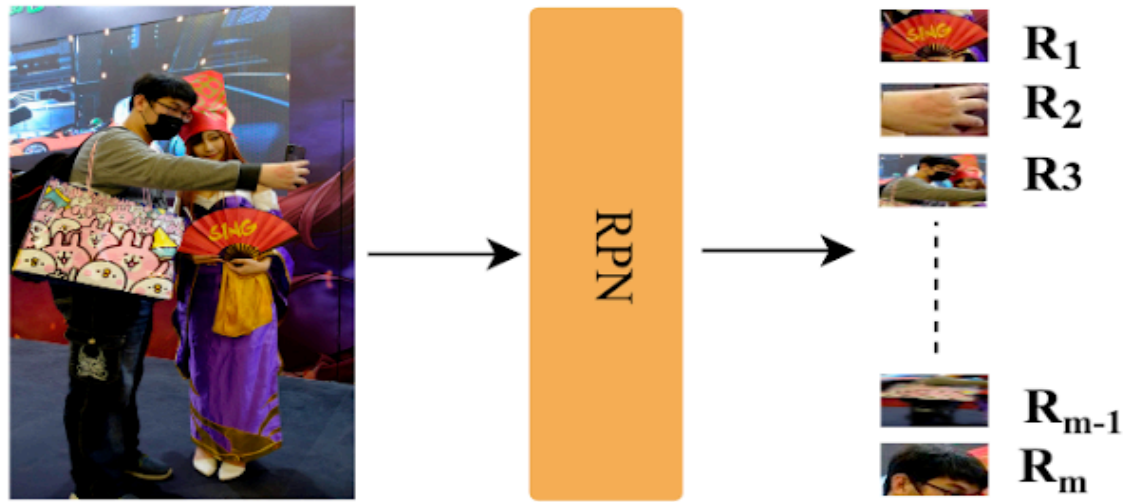
Fundamental task for **image / video understanding**

— Helps improve performance on other tasks (e.g., image captioning, VQA)

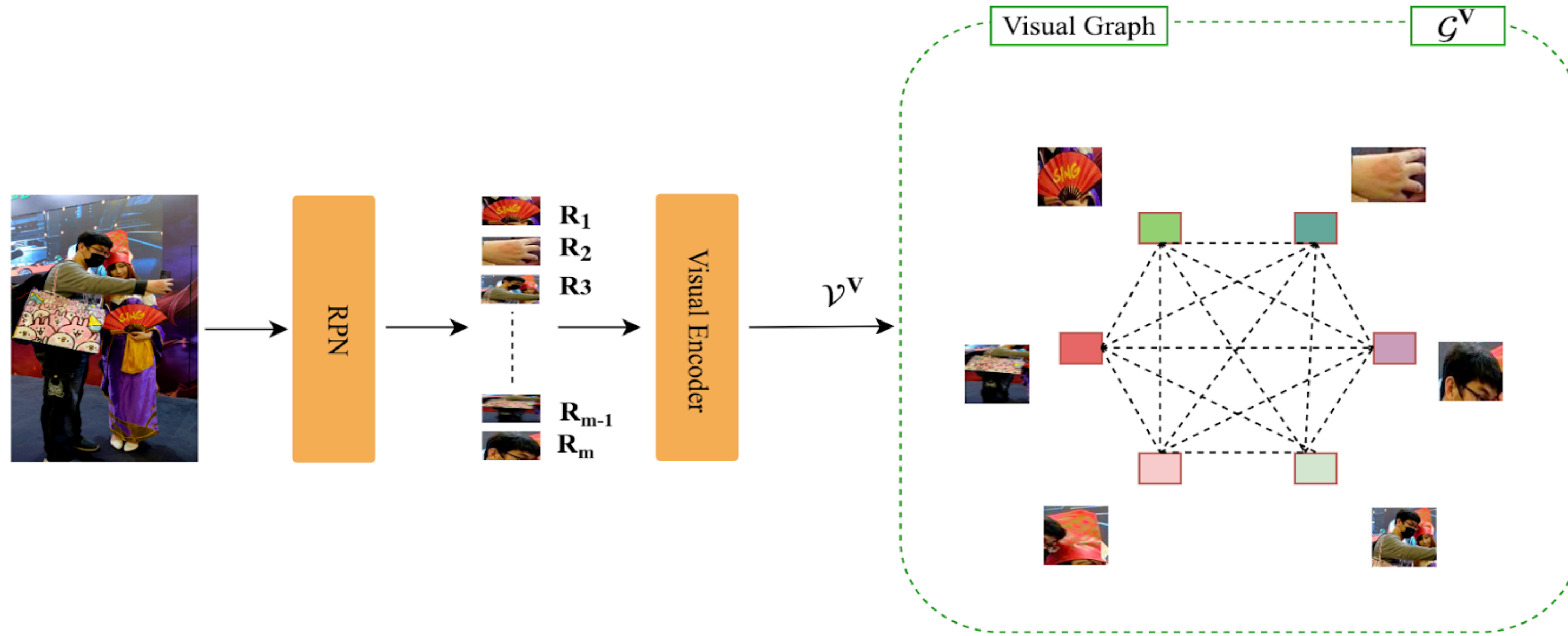
Proposed **Architecture**



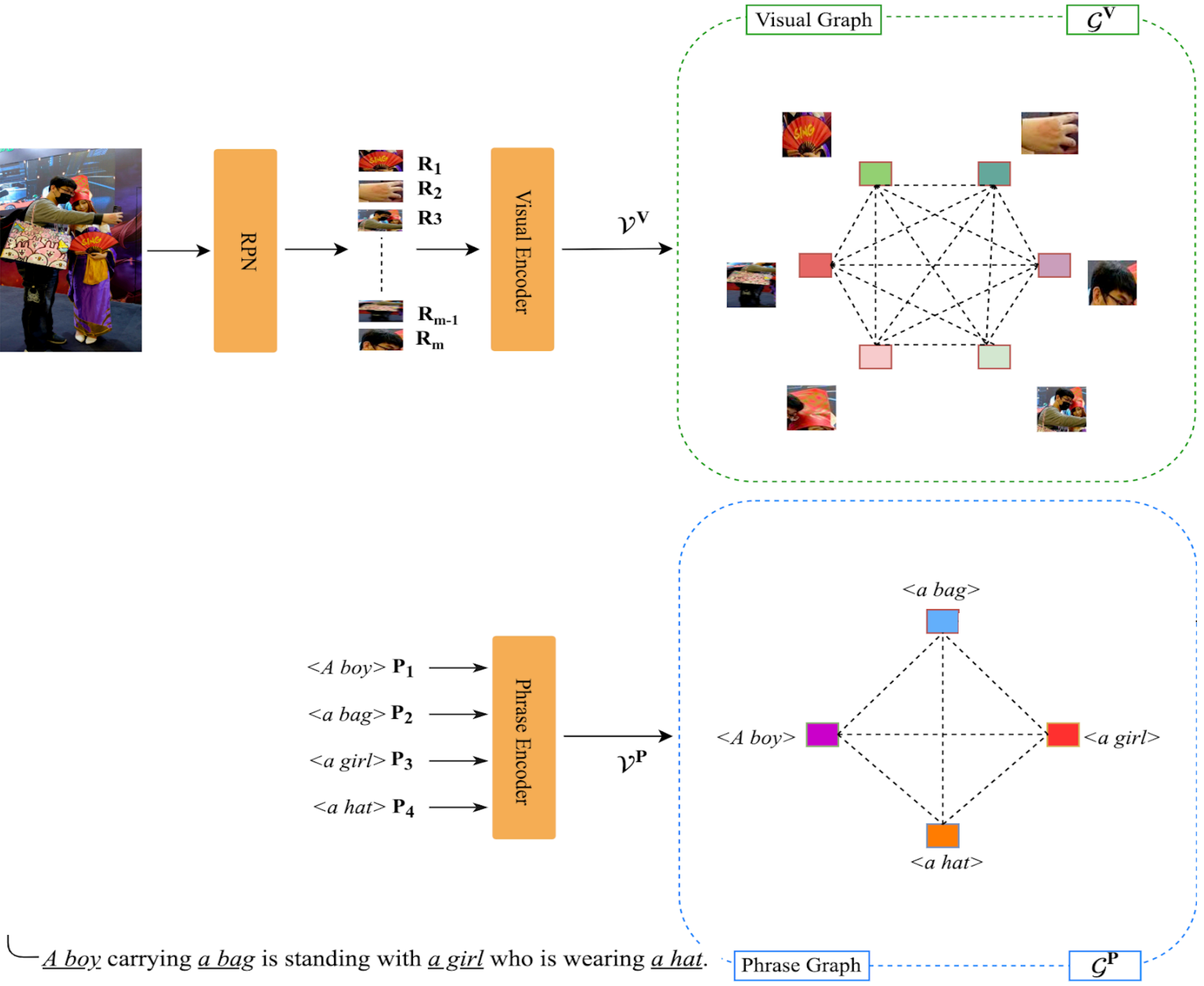
Proposed **Architecture**



Proposed Architecture

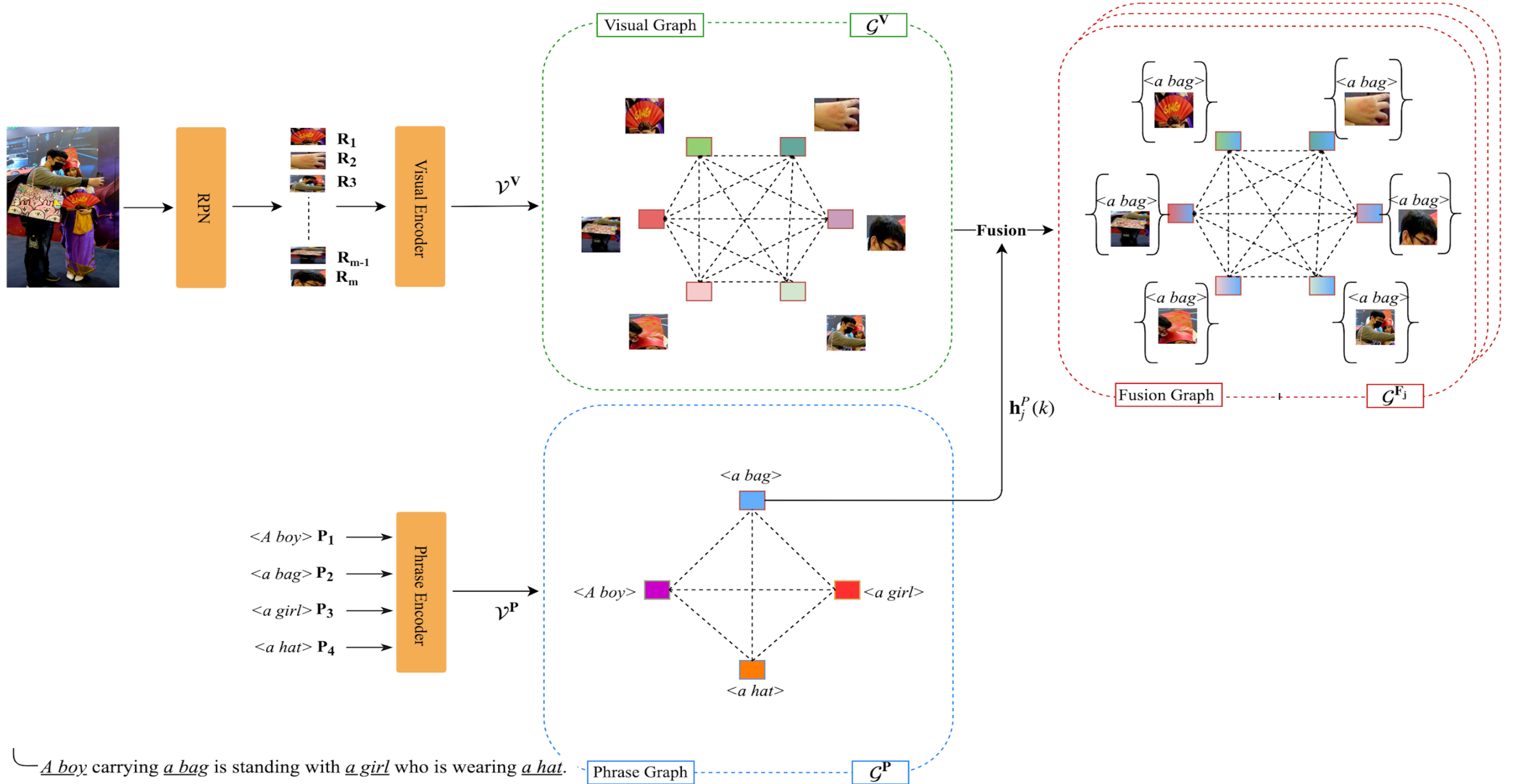


Proposed Architecture



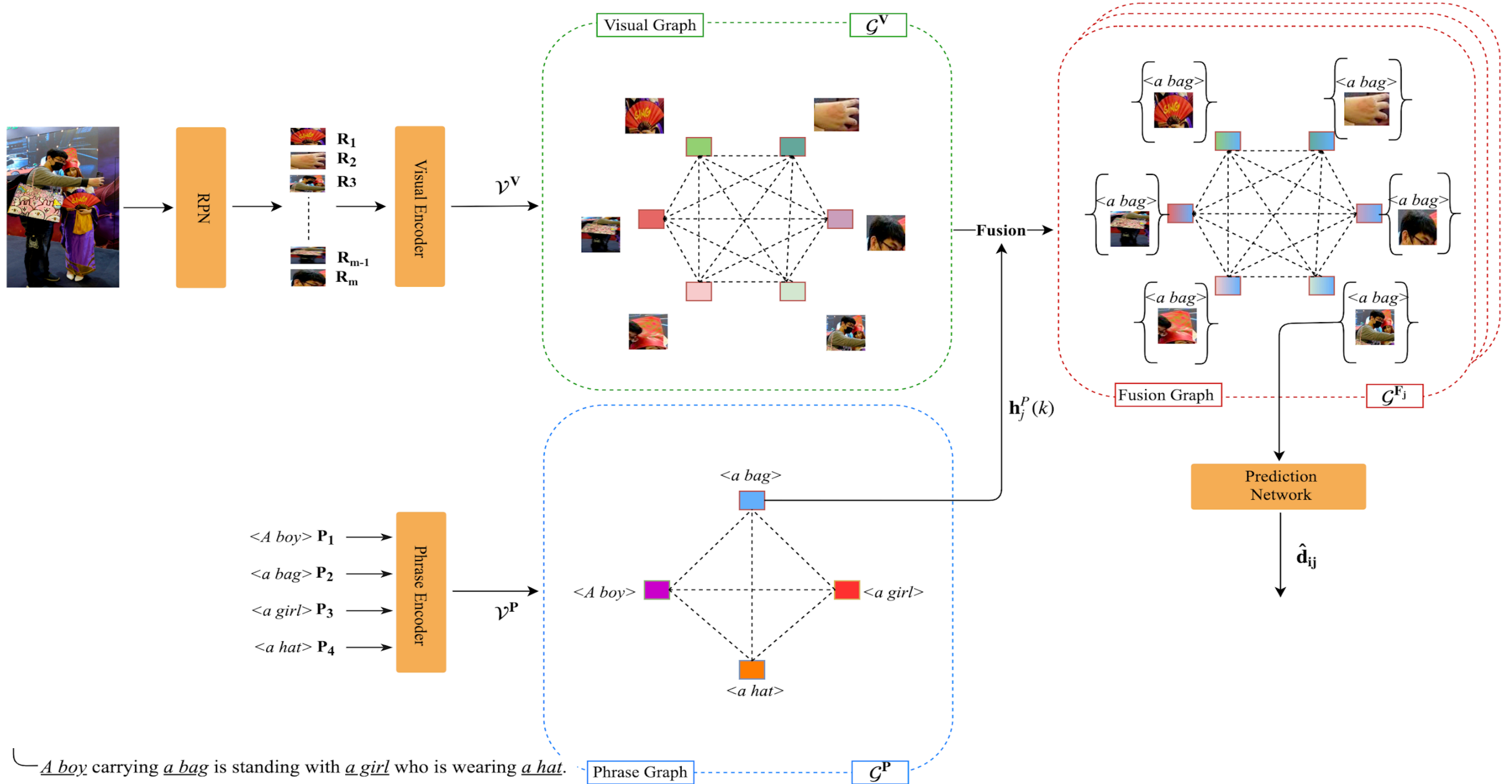
<A boy> carrying <a bag> is standing with <a girl> who is wearing <a hat>.

Proposed Architecture

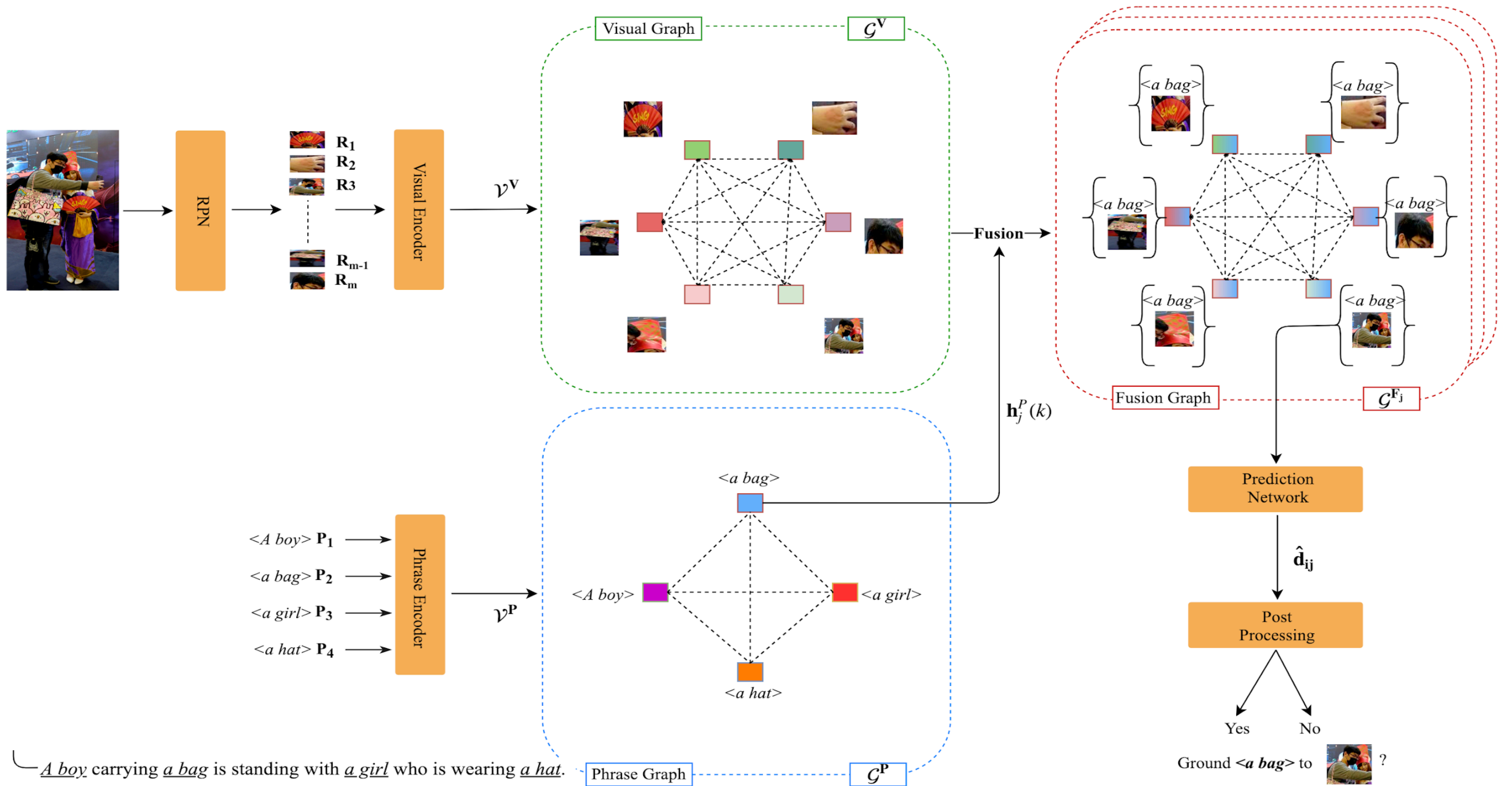


A boy carrying a bag is standing with a girl who is wearing a hat.

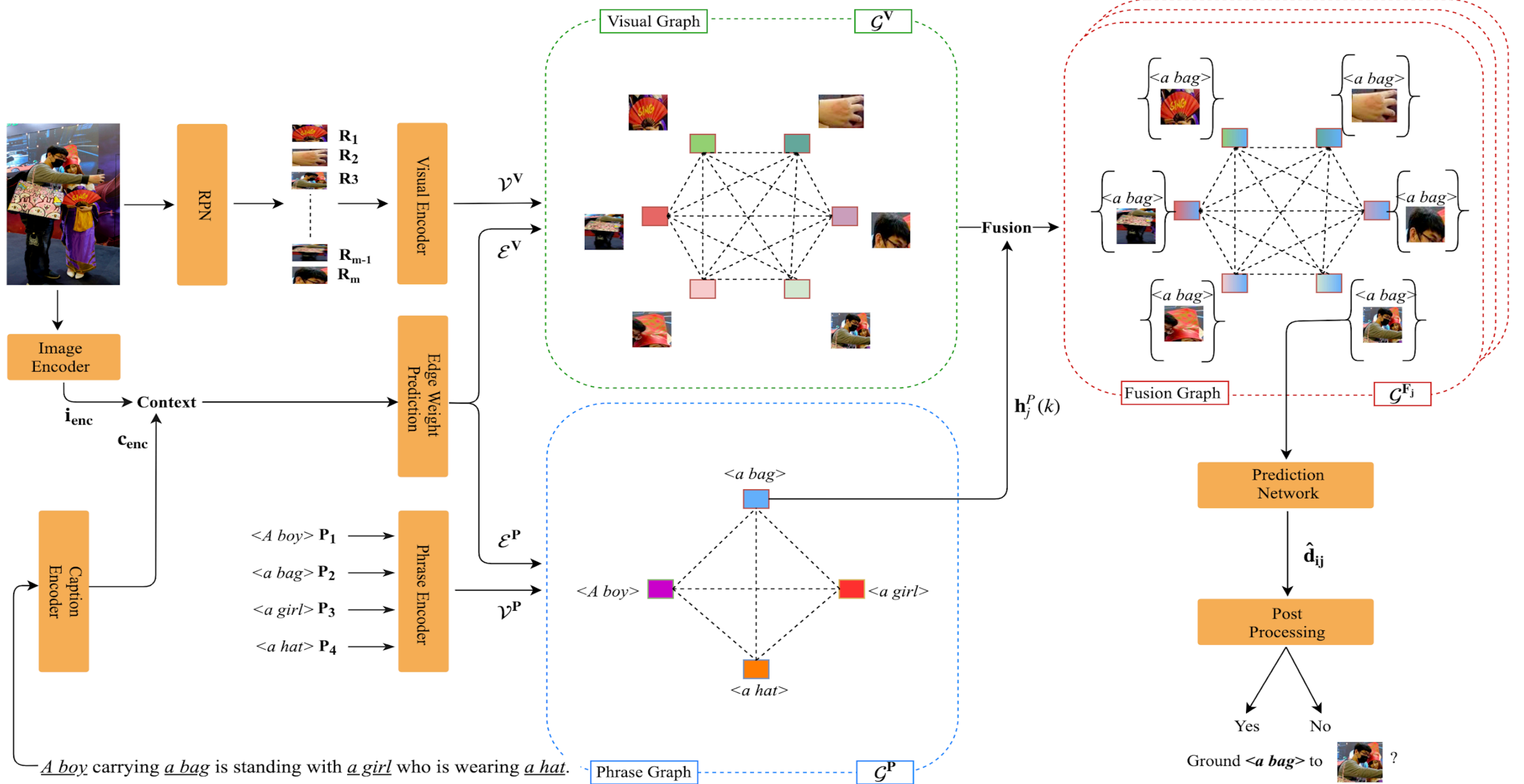
Proposed Architecture



Proposed Architecture



Proposed Architecture



Experiments

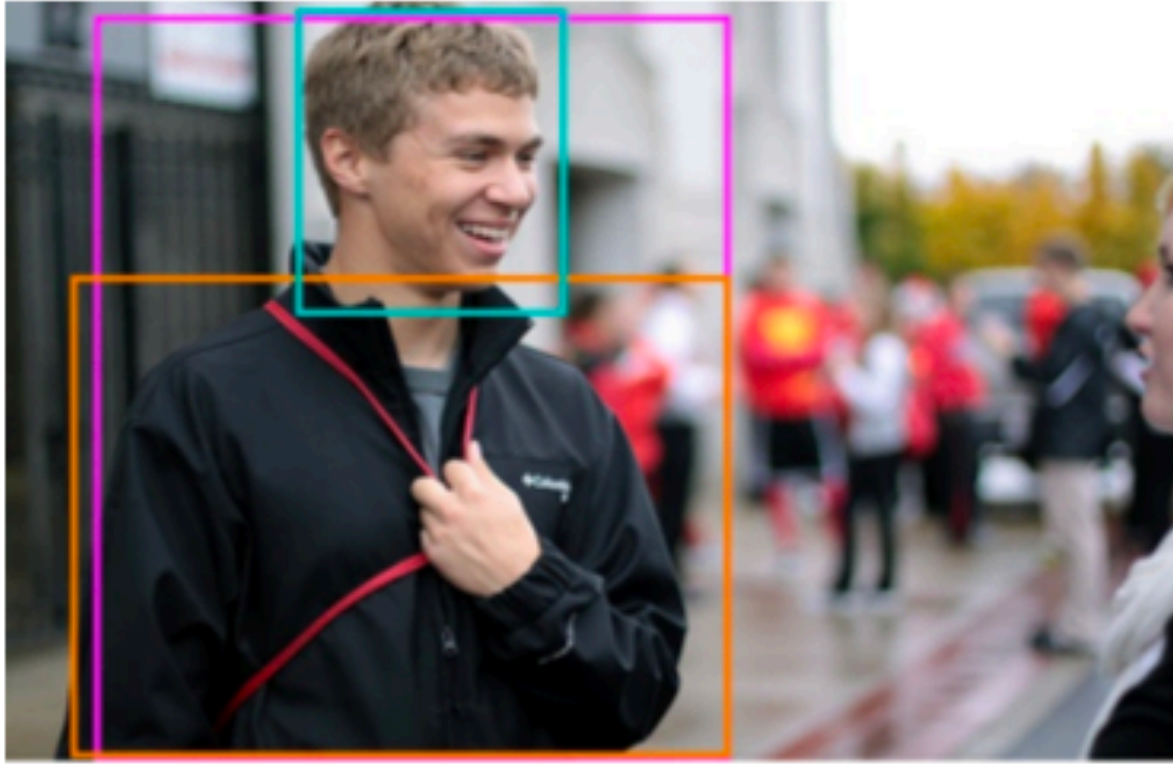
Datasets

- **Flickr30K Entities:** (mostly noun) Phrases parsed from image captions
- **ReferIt Game:** Unambiguous single phrases

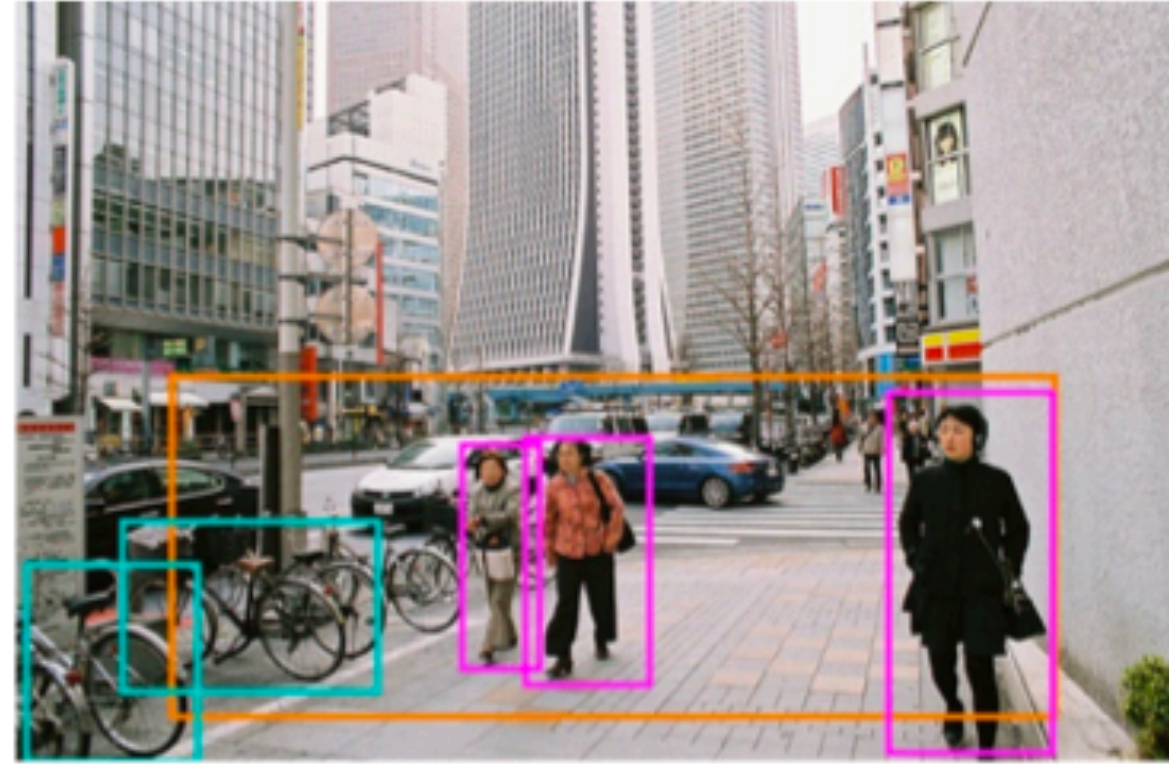
Evaluation

- Ratio of correctly grounded phrases to the total phrases

Qualitative Results: Flickr30K



(a) A man wearing a black-jacket has a smile on his face.



(b) People are walking on the street, with bikes parked up to the left of the picture.



(c) A woman in a yellow shirt is walking down the sidewalk.



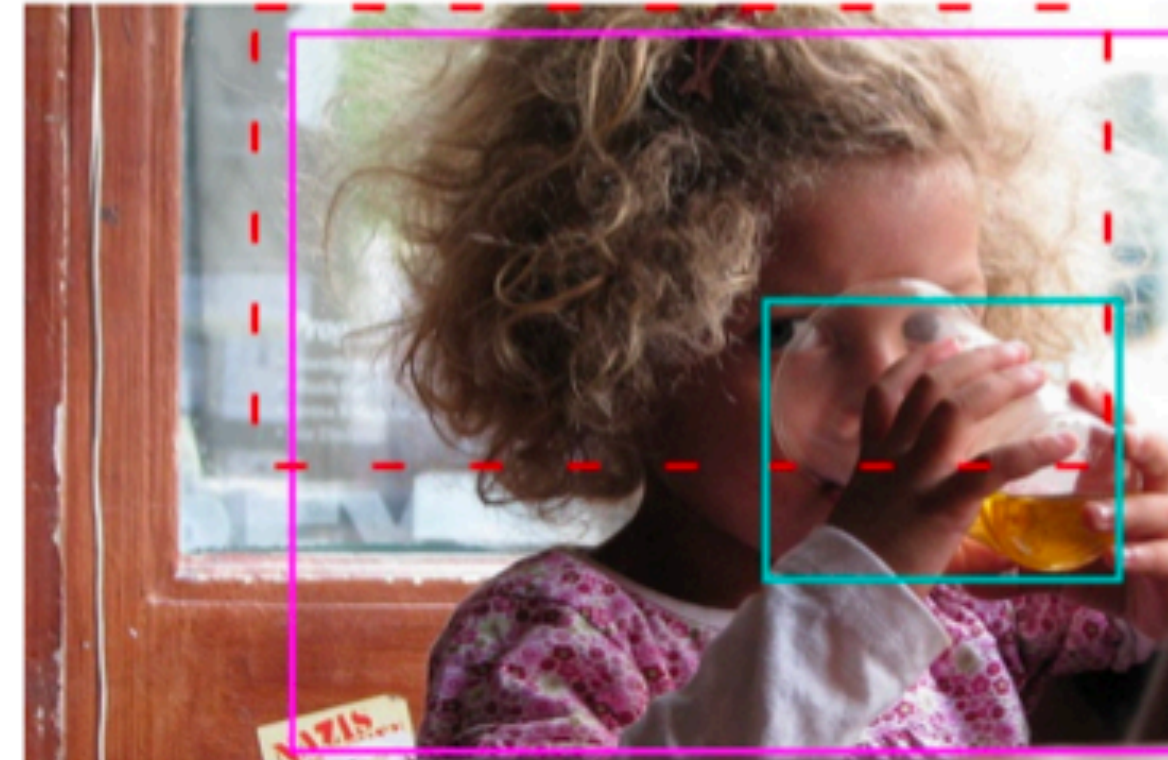
(d) A young boy is walking on wooden path in the middle of trees.



(e) Two women in colorful clothing are dancing inside a circle of other women.



(f) Lady wearing white shirt with blue umbrella in the rain.



(g) Young girl with curly hair is drinking out of a plastic cup.



(h) The bearded man keeps his blue Bic pen in hand while he plays the guitar.

Quantitative Results

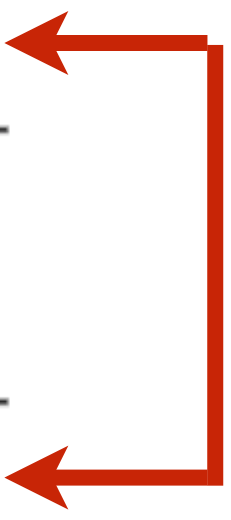
Flickr30k Entities:

Method	Accuracy
SMPL [27]	42.08
NonlinearSP [26]	43.89
GroundeR [23]	47.81
MCB [7]	48.69
RtP [21]	50.89
Similarity Network [25]	51.05
IGOP [34]	53.97
SPC+PPC [20]	55.49
SS+QRN (VGGdet) [4]	55.99
CITE [19]	59.27
SeqGROUND	61.60
CITE [19] (finetuned)	61.89
QRC Net [4] (finetuned)	65.14
G³RAPHGROUND++	66.67

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G³RAPHGROUND++	66.67

ReferIt Game:


Method	Accuracy
SCRC [9]	17.93
MCB + Reg + Spatial [3]	26.54
GroundeR + Spatial [23]	26.93
Similarity Network + Spatial [25]	31.26
CGRE [17]	31.85
MNN + Reg + Spatial [3]	32.21
EB+QRN (VGGcls-SPAT) [4]	32.21
CITE [19]	34.13
IGOP [34]	34.70
QRC Net [4] (finetuned)	44.07
G³RAPHGROUND++	44.91

Ablation

Method	Flickr30k	ReferIt
GG - VisualG - FusionG	56.32	32.89
GG - VisualG	62.23	38.82
GG - FusionG	59.13	36.54
GG - PhraseG	60.82	38.12
GGFusionBase	60.41	38.65
GG - ImageContext	62.32	40.92
GG - PhraseContext	62.73	<i>n.a.</i>
G ³ RAPHGROUND (GG)	63.65	41.79
G³RAPHGROUND++	66.67	44.91

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G³RAPHGROUND++	66.67	44.91



Visualizing Graph Attention



(a) A young boy is looking at a man painted in all gold.



(b) A man is checking his blue sneakers next to two men having a conversation.



(c) A brown dog jumps high on a field of grass.



(d) A woman stands in a field near a car and looks through binoculars.



Energy-Based Learning for Scene Graph Generation



Mohammed Suhail

+ + +

Scene Graphs:

A **graph** based data structure for semantically representing image content

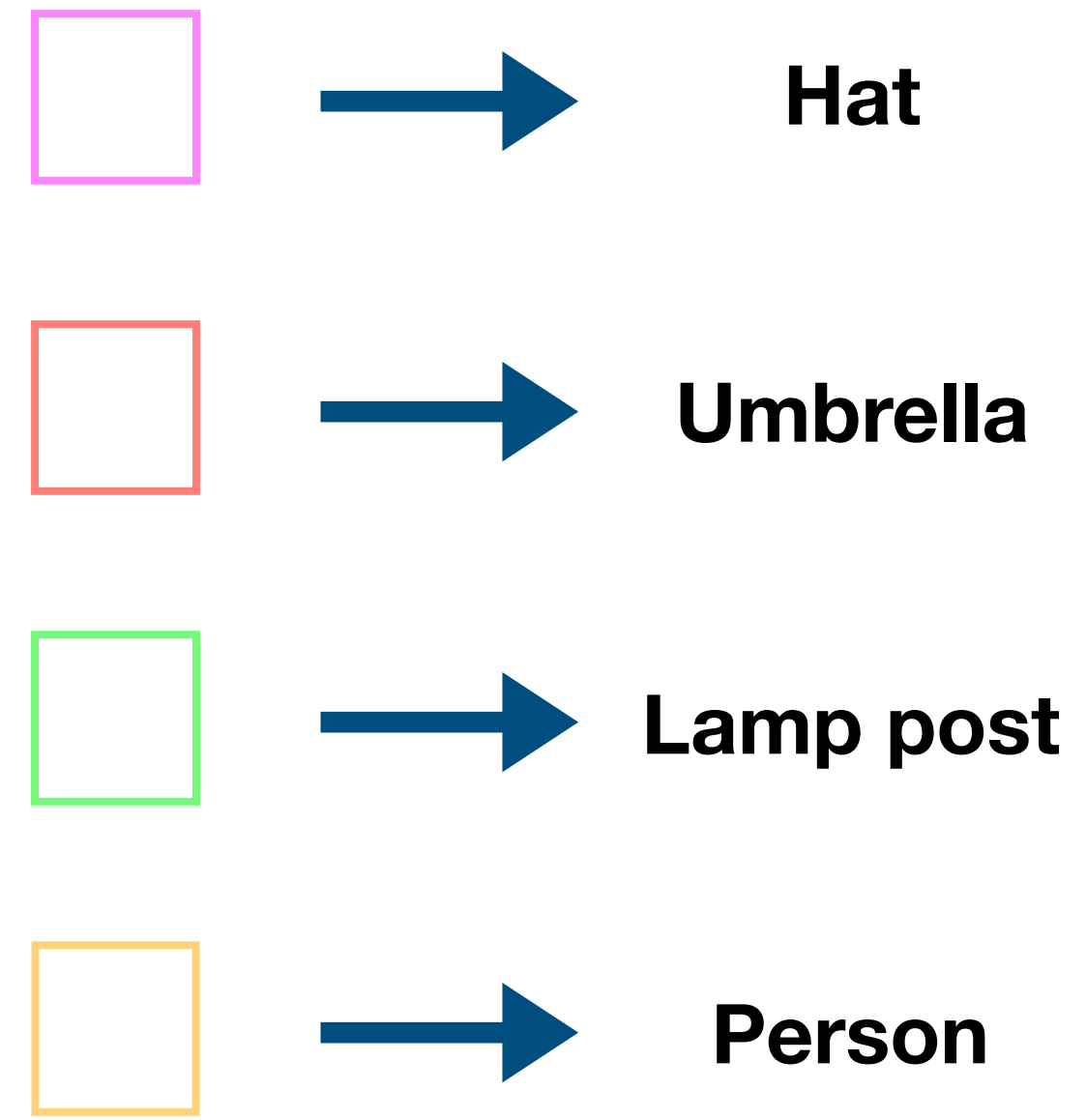
Scene Graphs



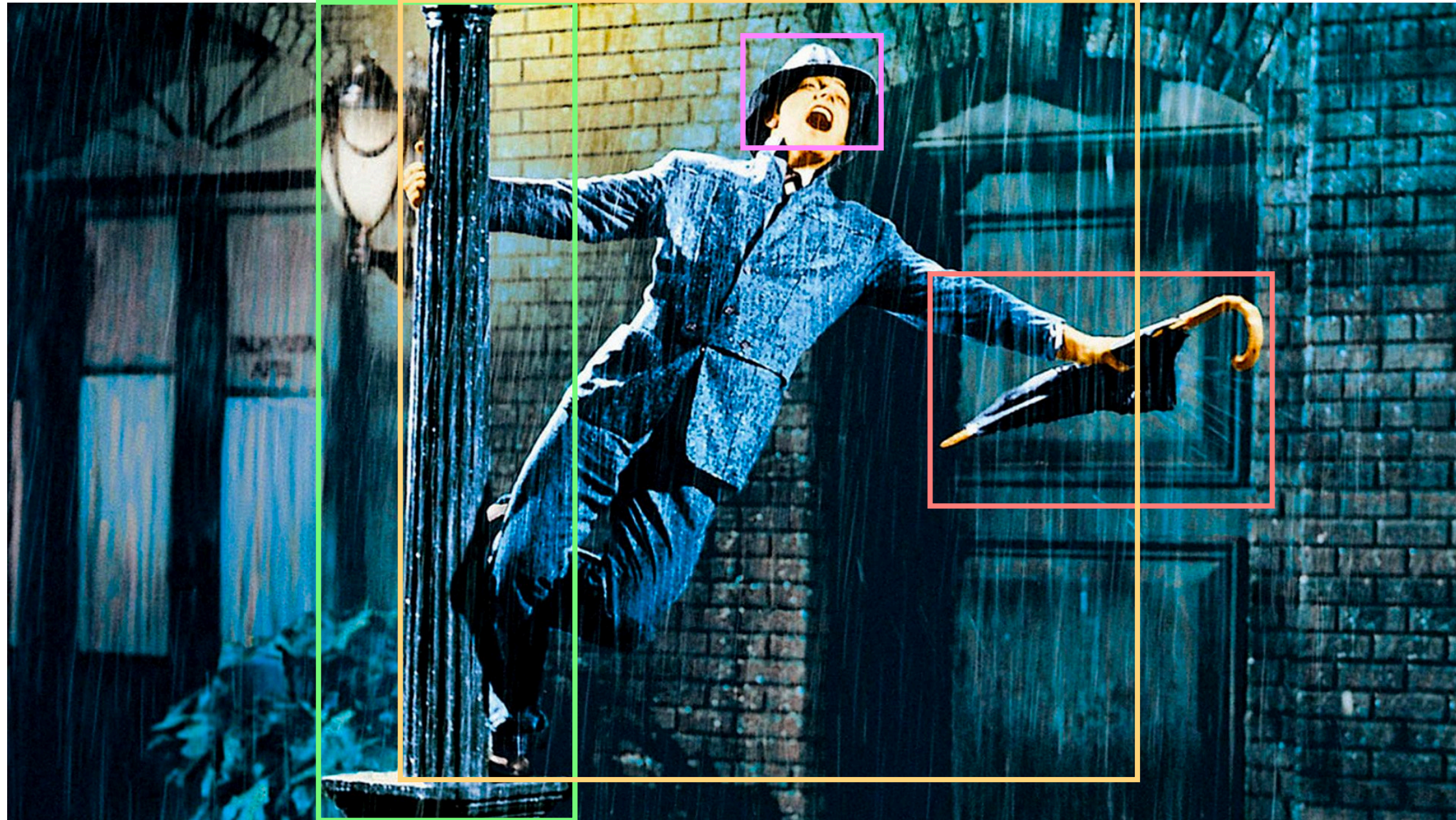
Scene Graphs



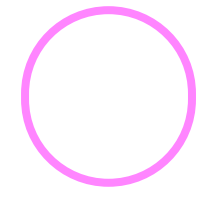
Scene Graphs



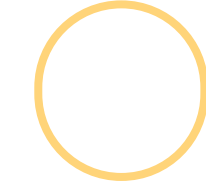
Scene Graphs



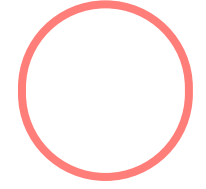
Hat



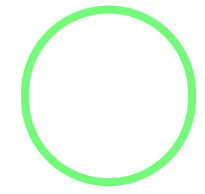
Person



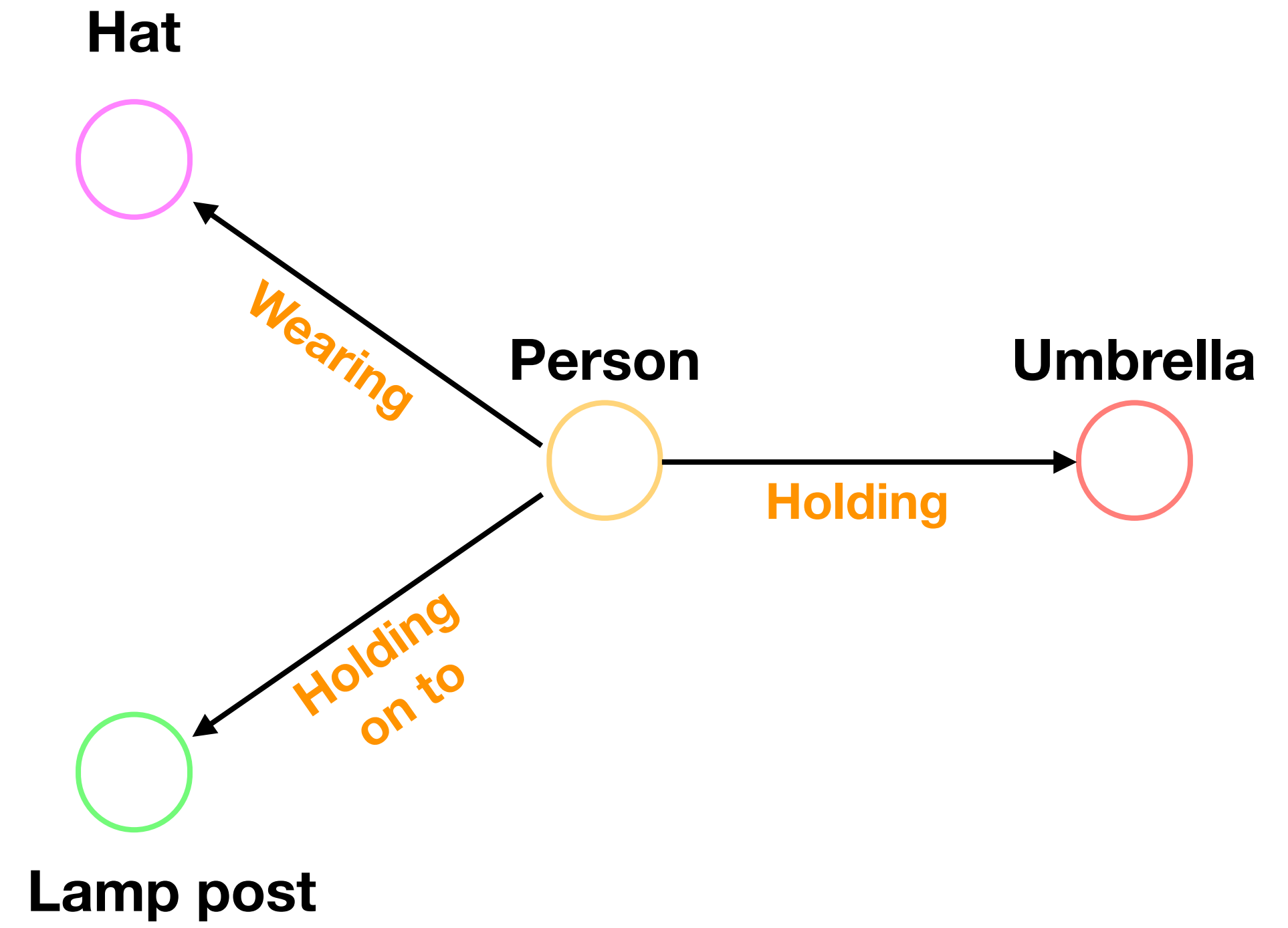
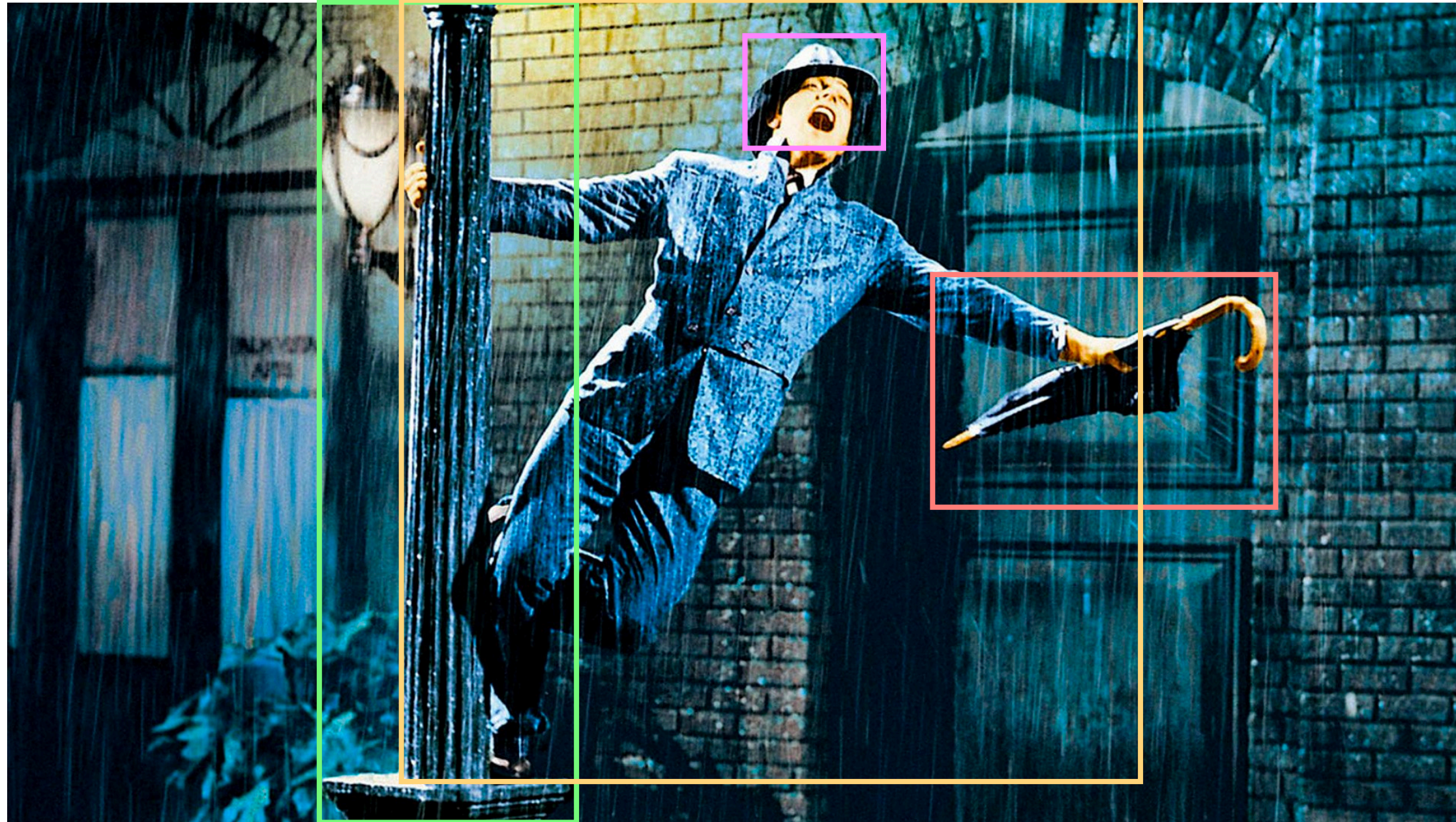
Umbrella



Lamp post



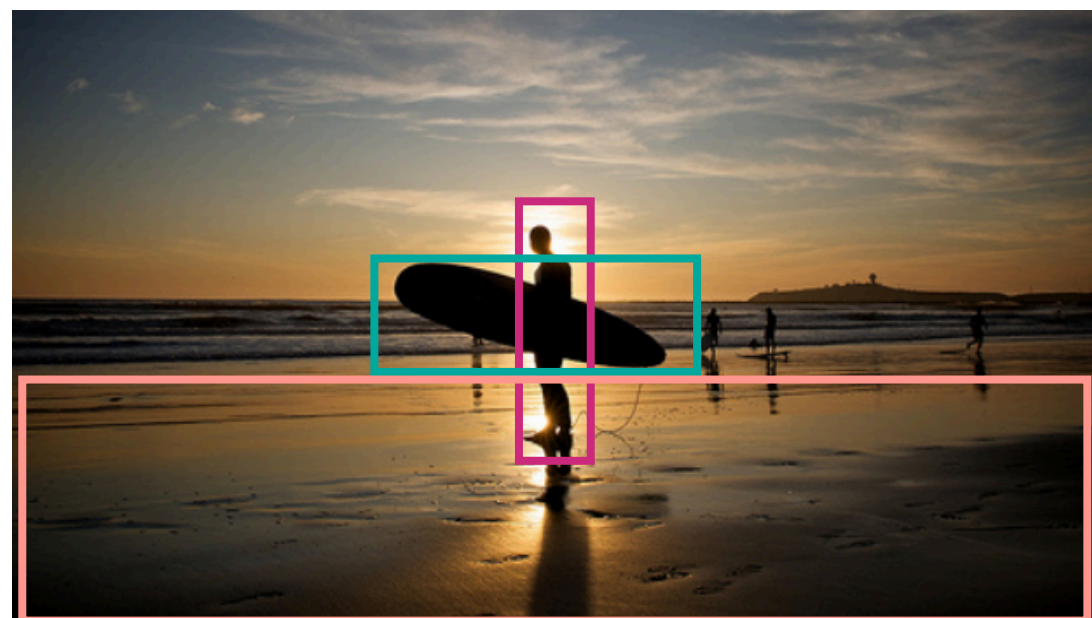
Scene Graphs



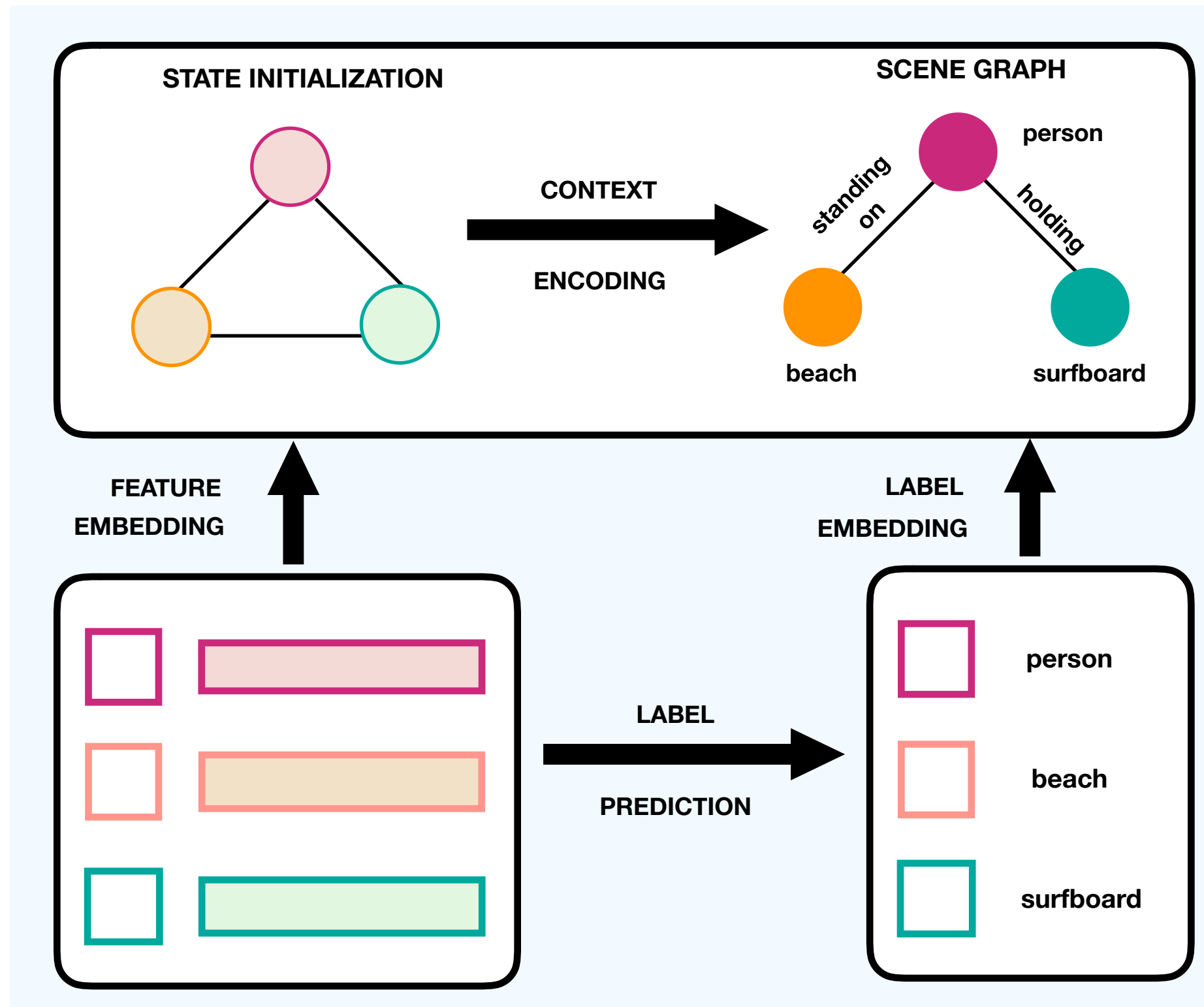
Scene Graph Generation Pipeline



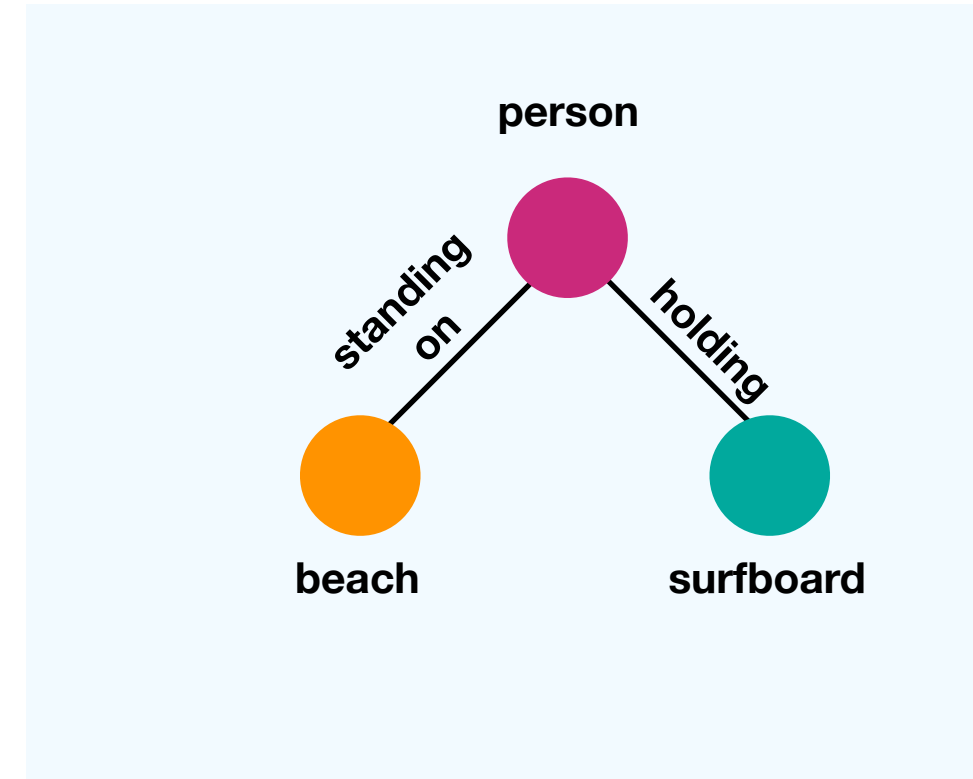
OBJECT DETECTOR



FEATURE
EXTRACTION

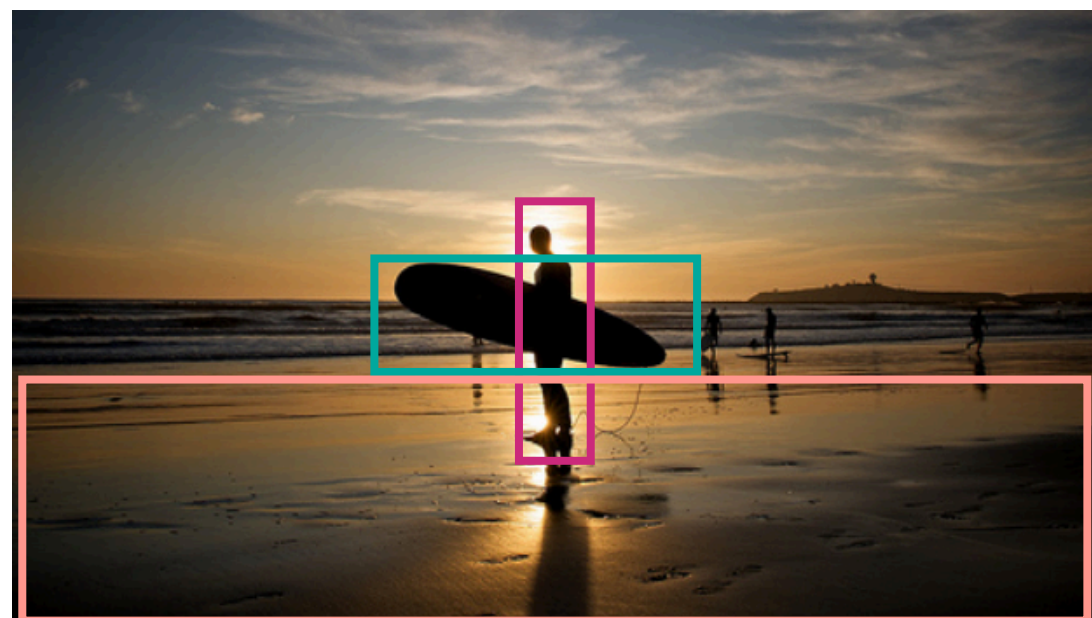


LOSS
COMPUTATION

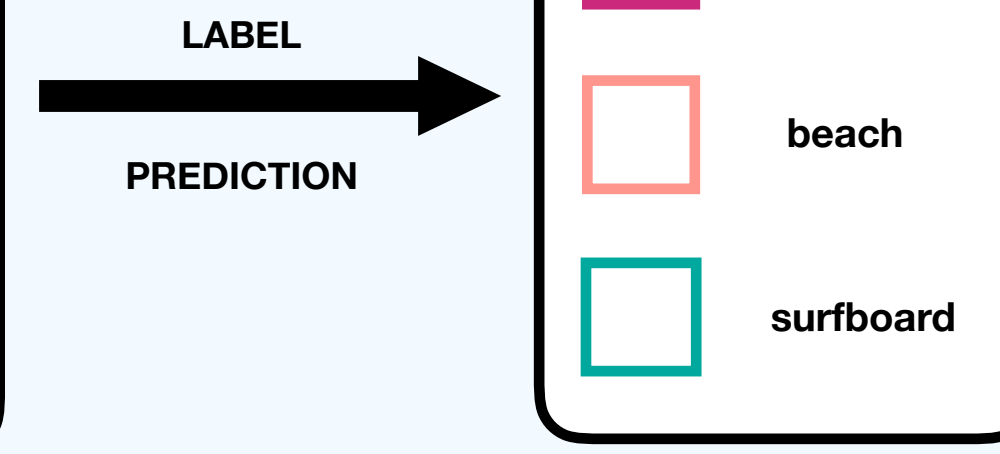
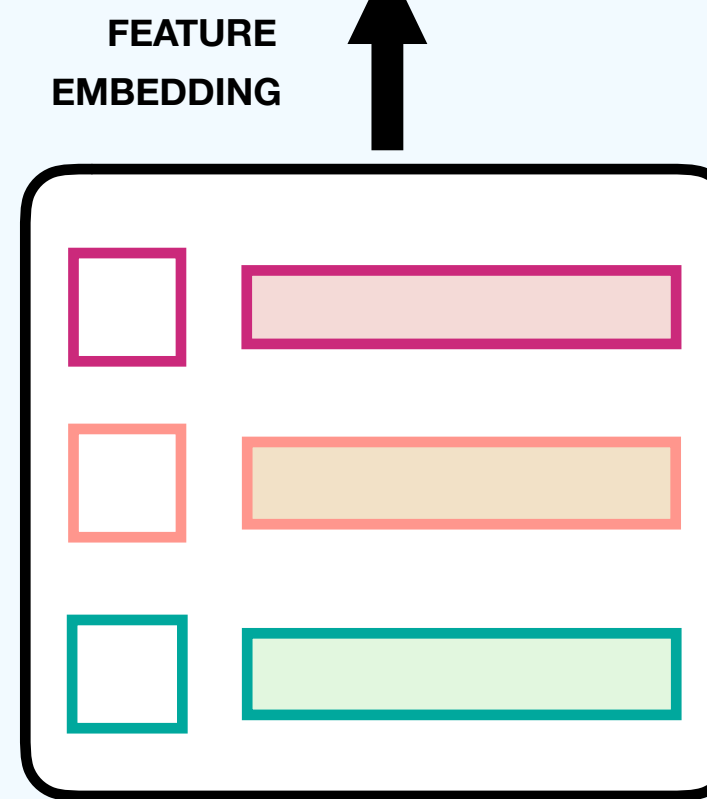
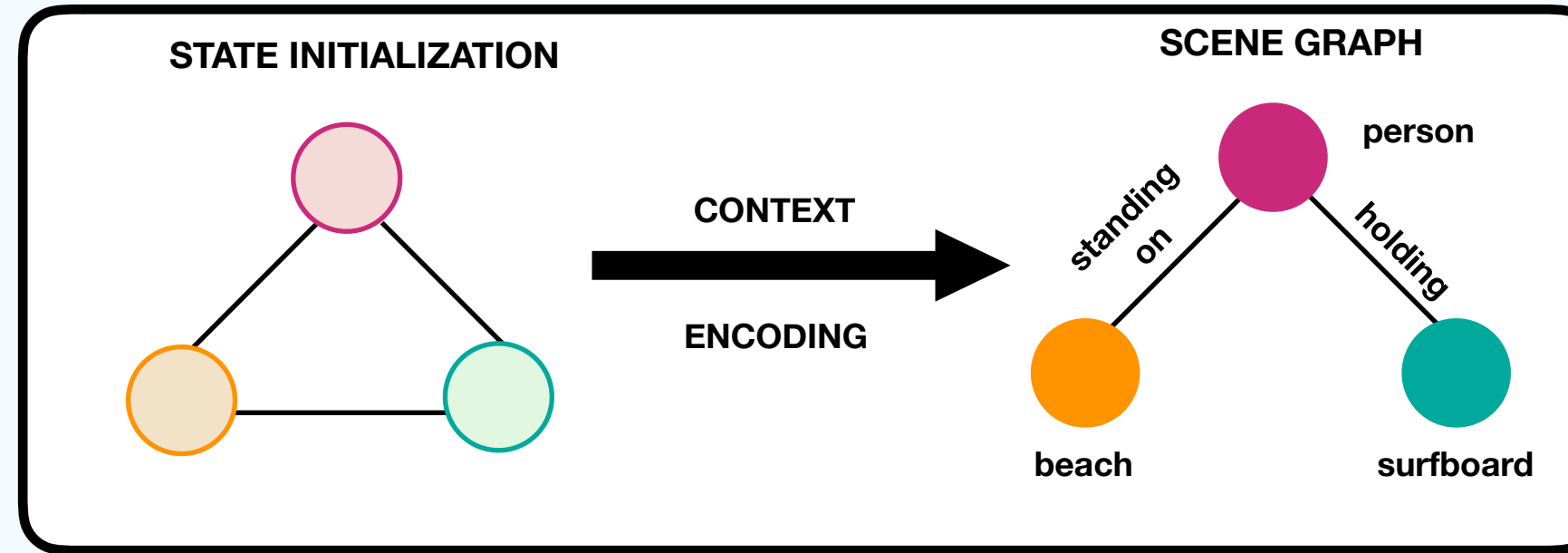




OBJECT DETECTOR



FEATURE
EXTRACTION

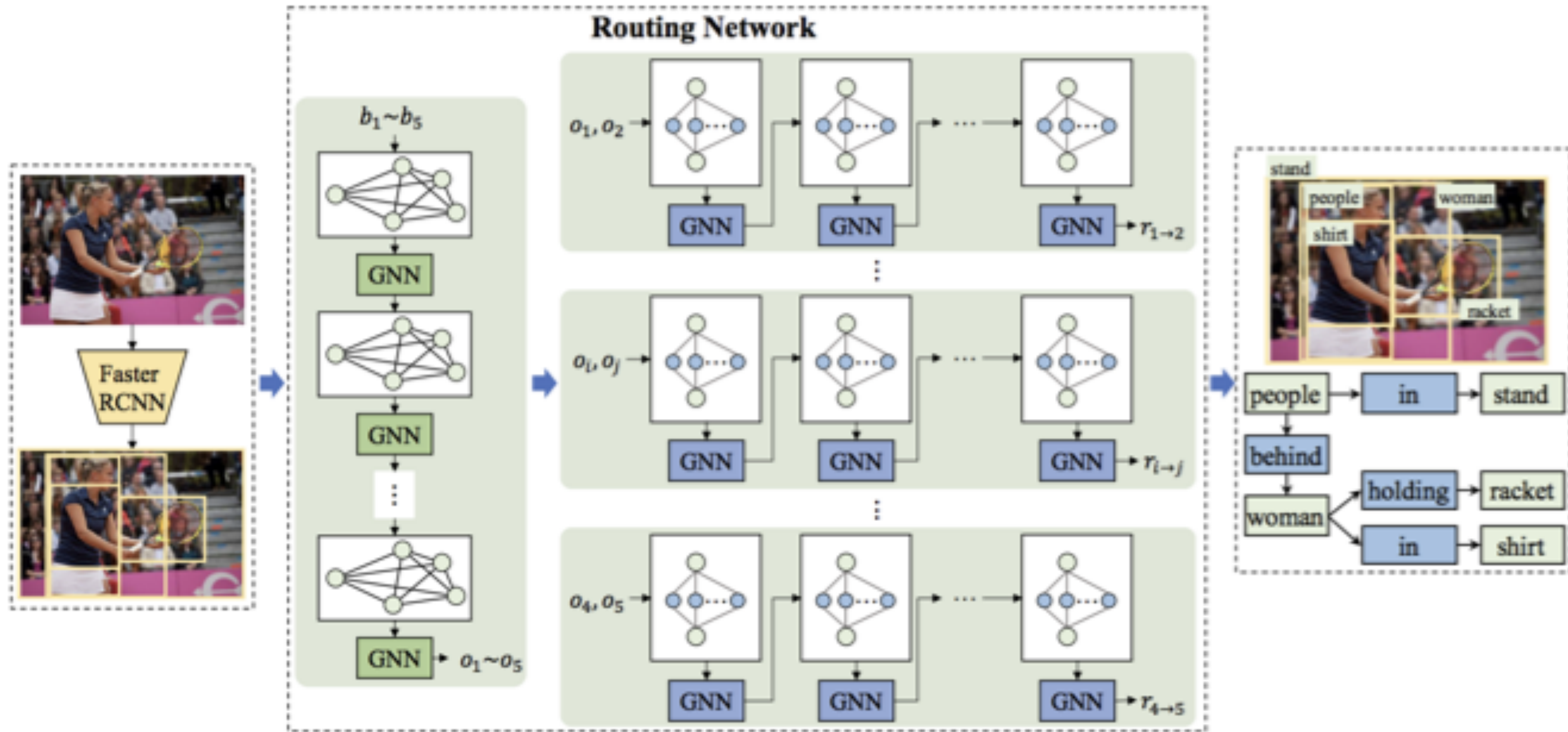


LOSS
COMPUTATION

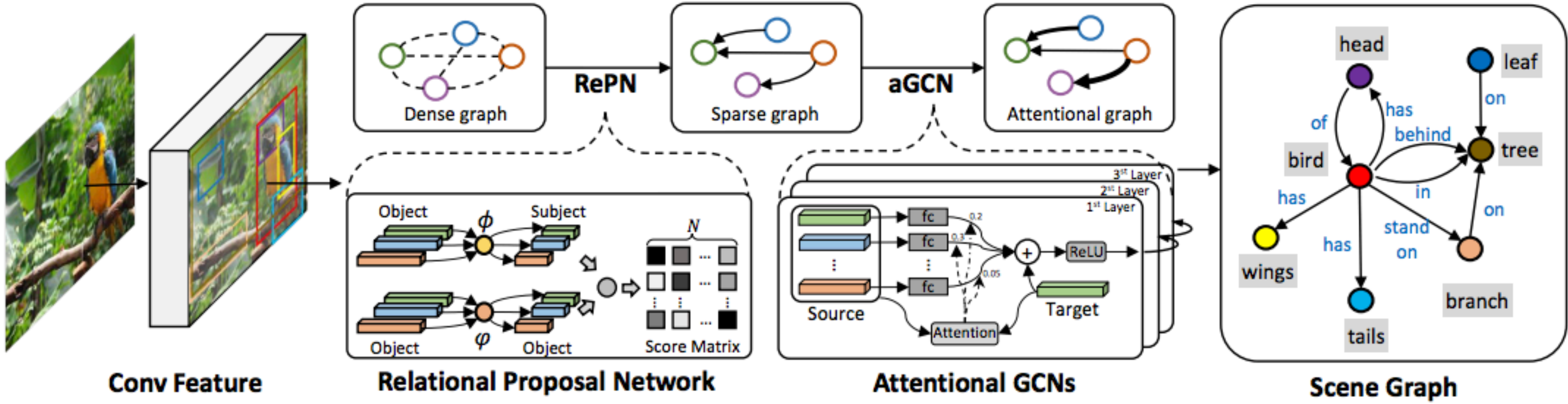
person
beach
surfboard
standing
on
holding

Cross
Entropy
Loss

KERN Architecture

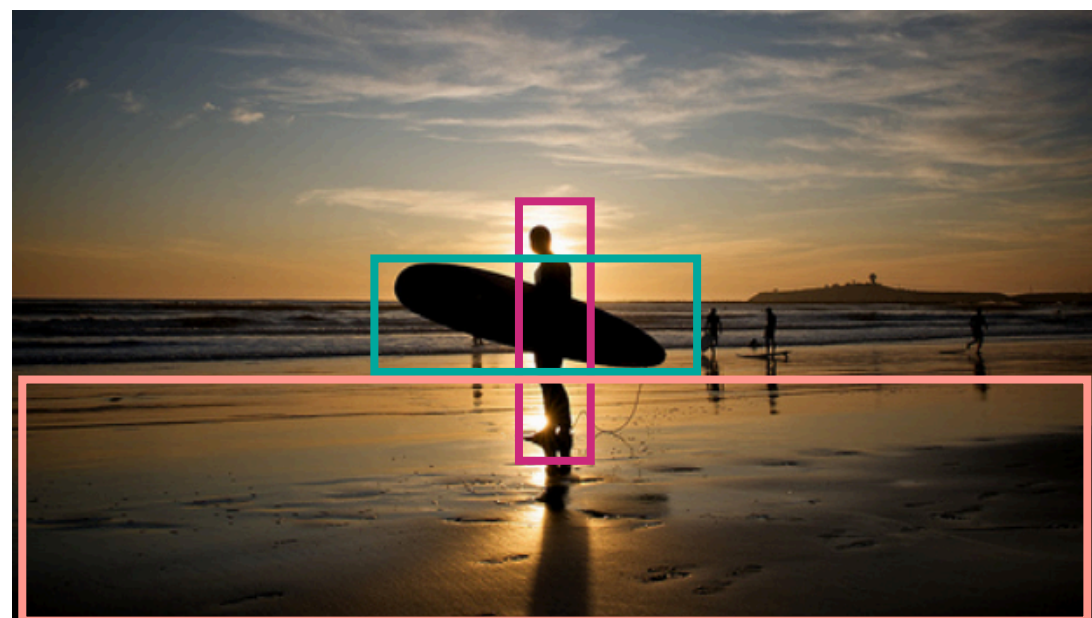


Graph RCNN

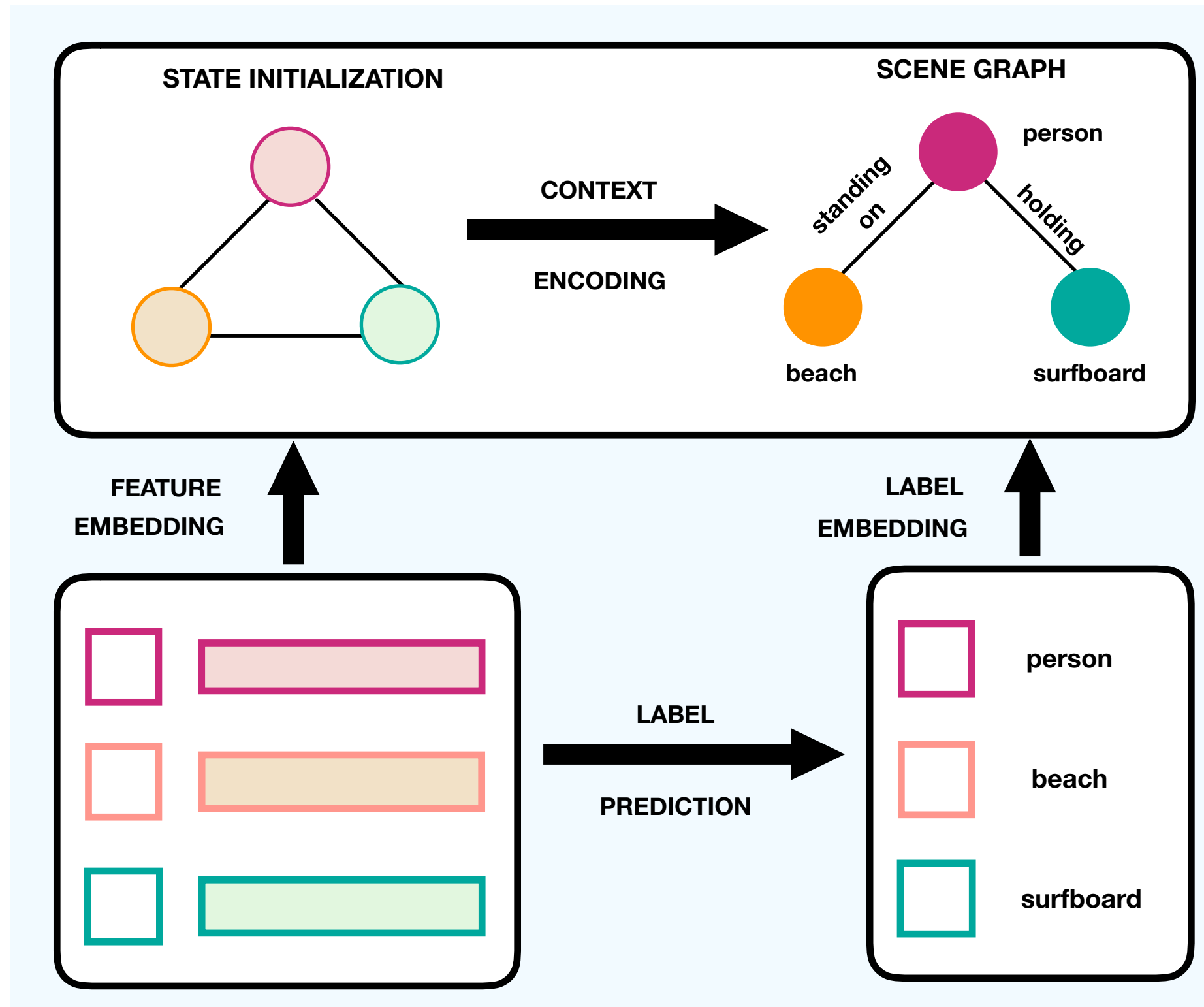




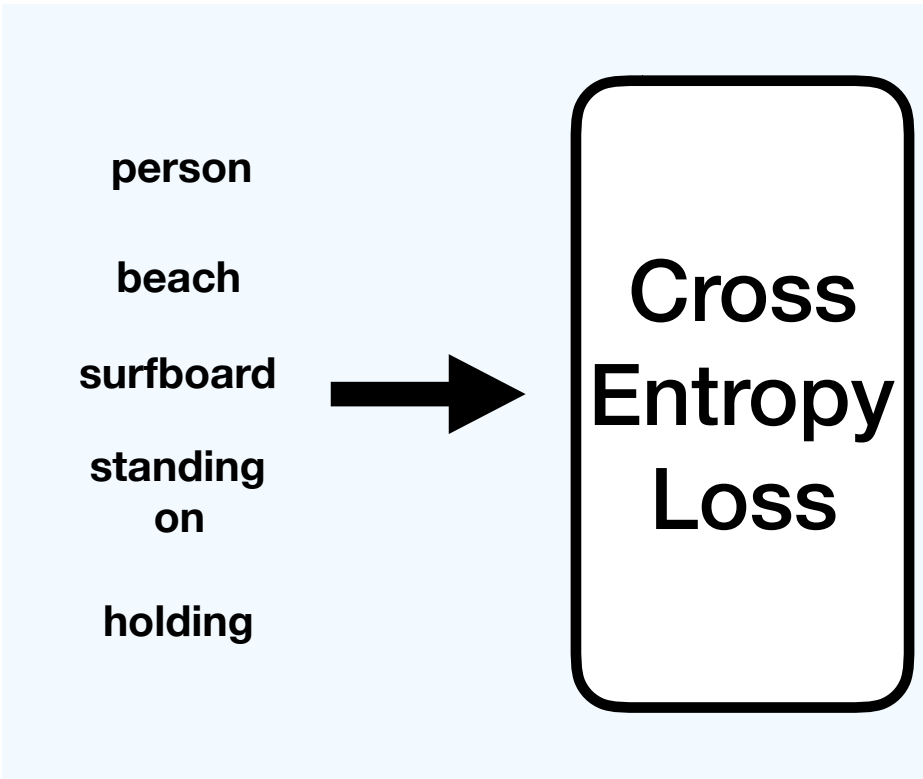
OBJECT DETECTOR



FEATURE
EXTRACTION



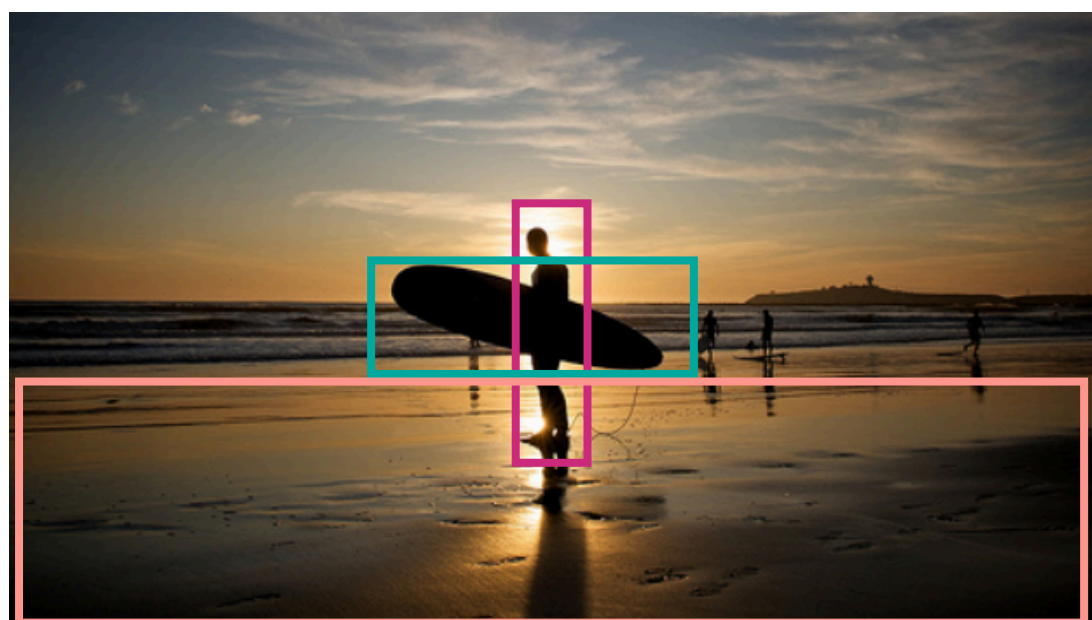
LOSS
COMPUTATION



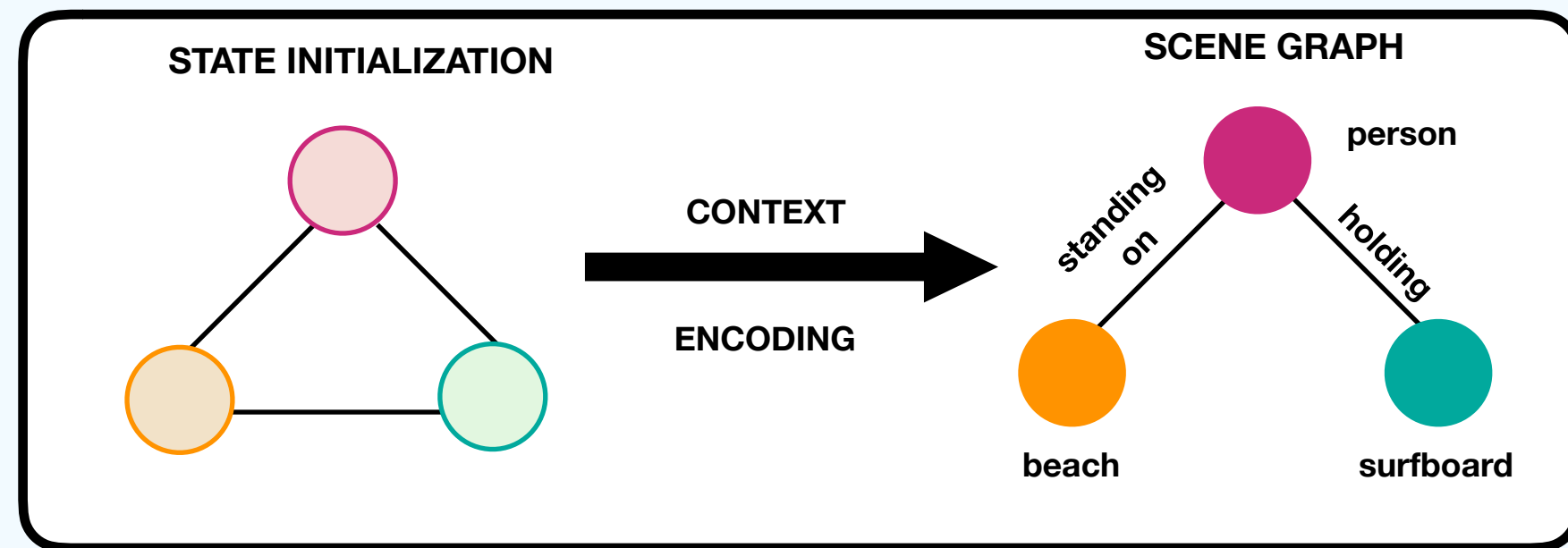
Structure information
is lost



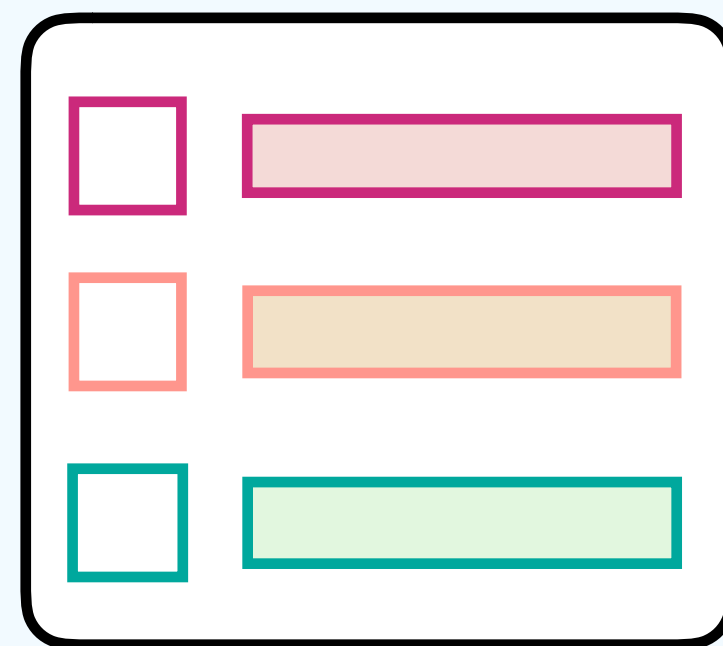
OBJECT DETECTOR



FEATURE
EXTRACTION

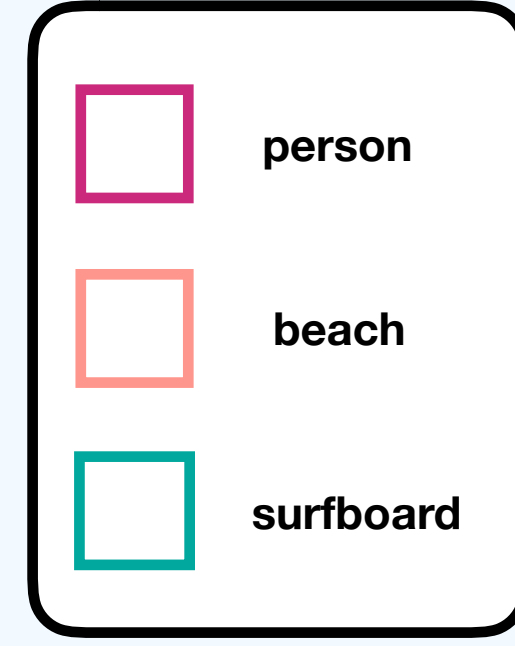


FEATURE
EMBEDDING



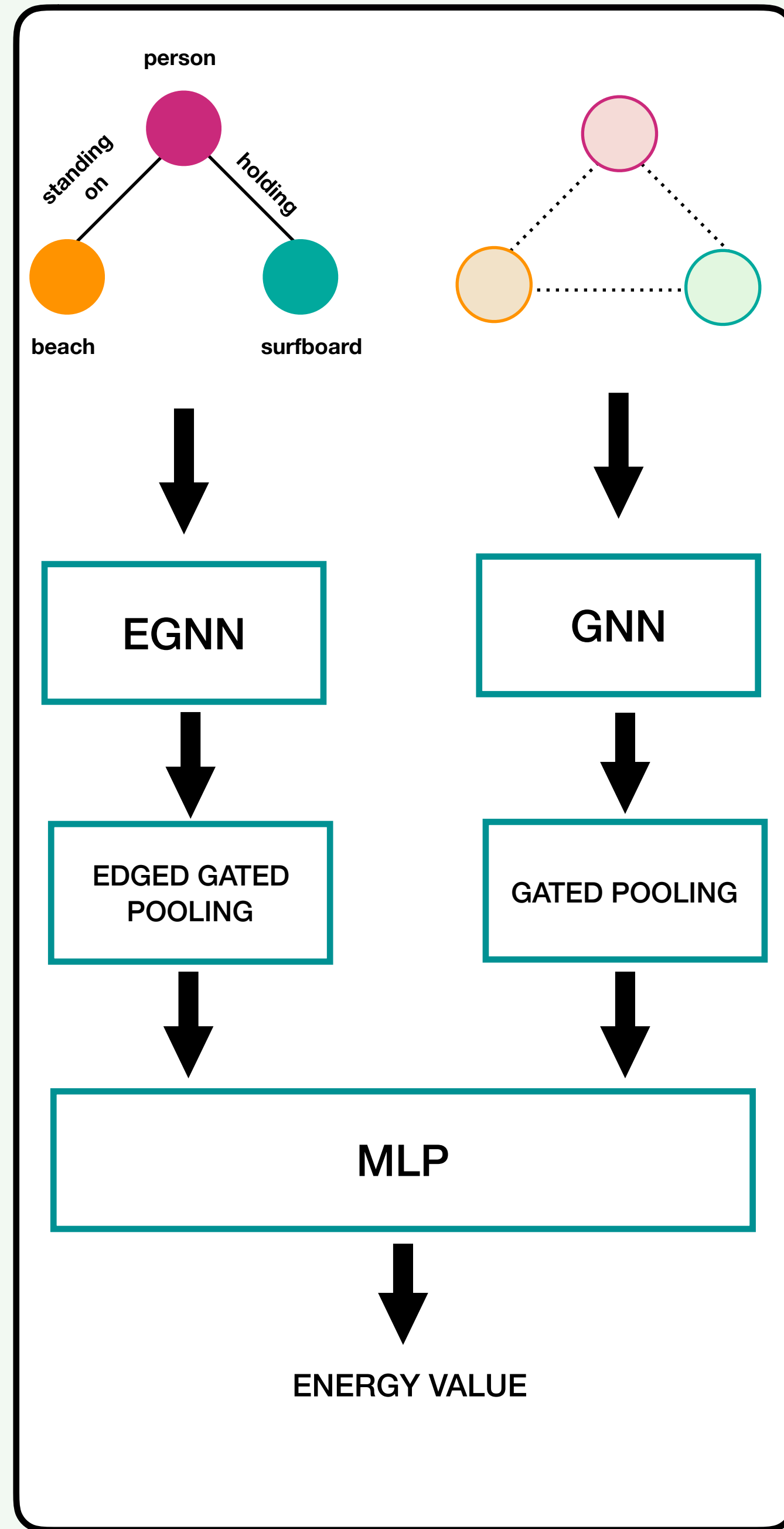
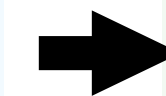
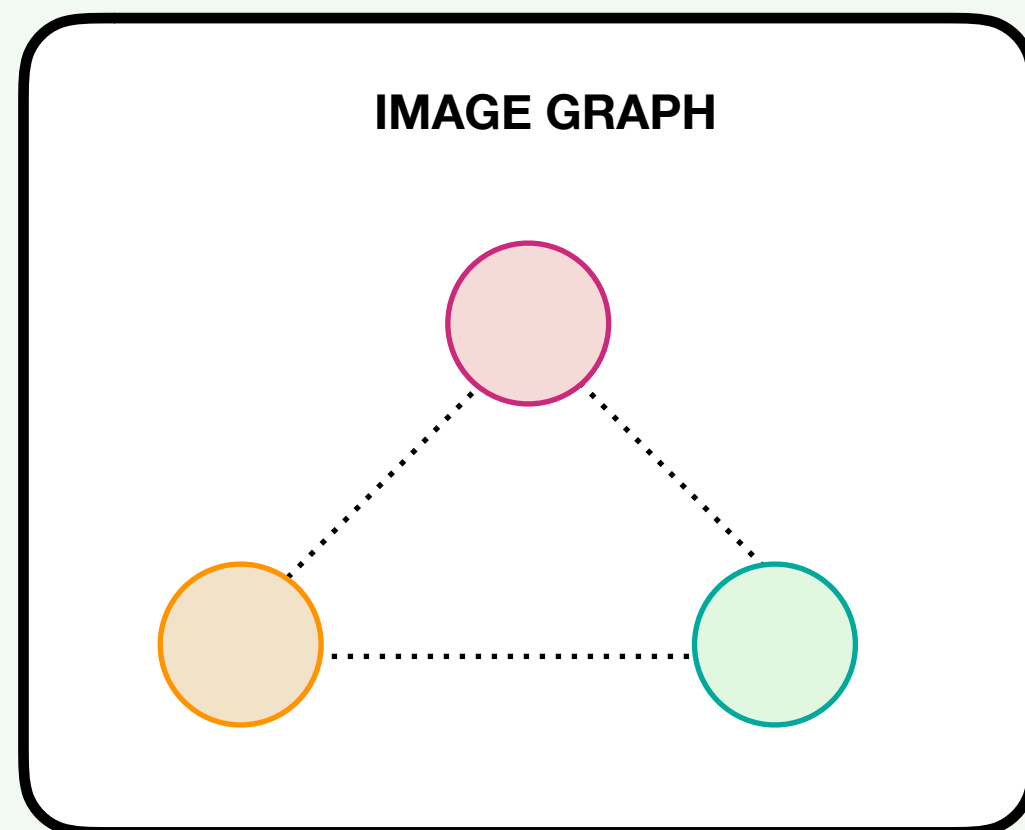
LABEL
PREDICTION

LABEL
EMBEDDING

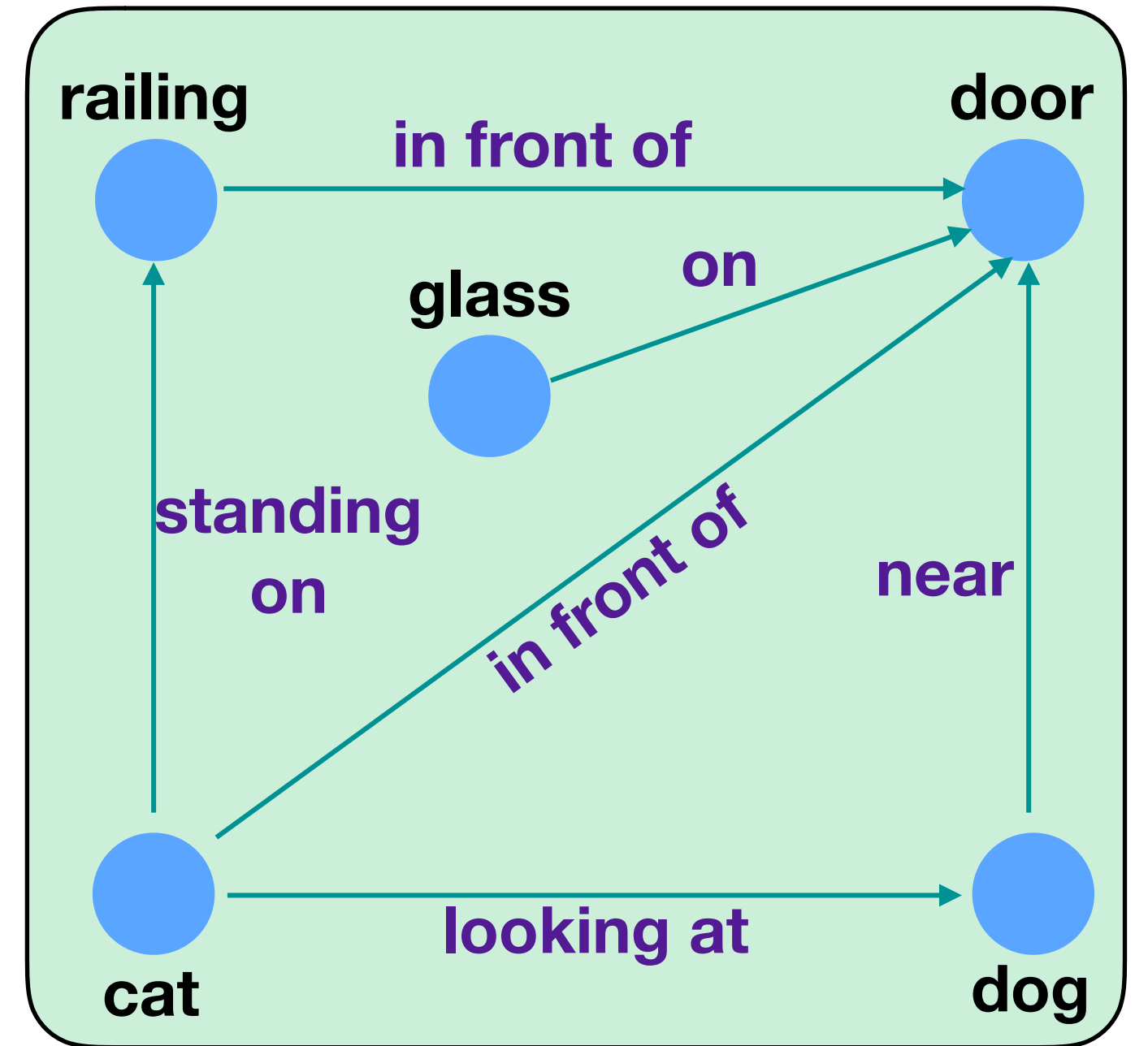
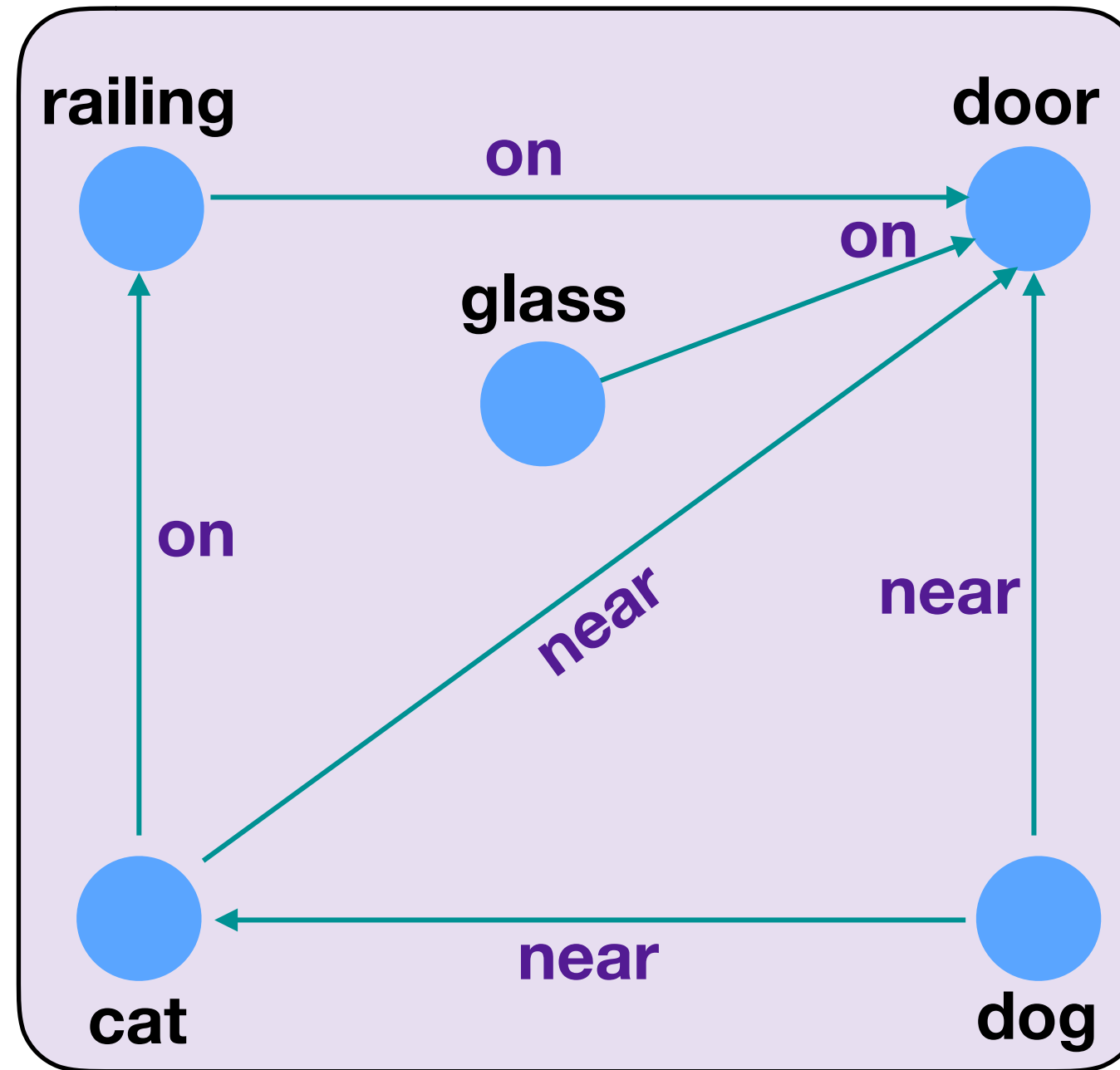
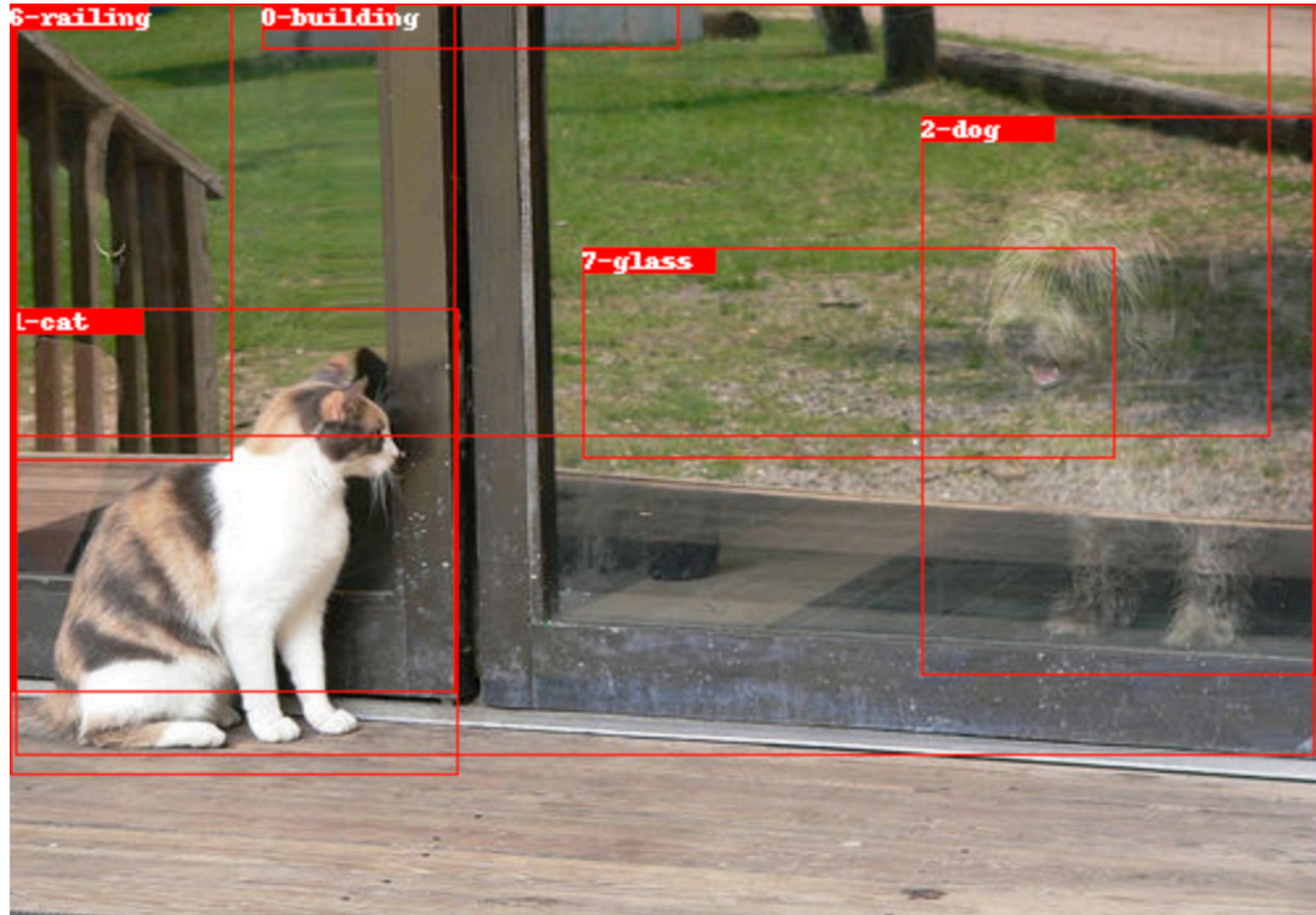


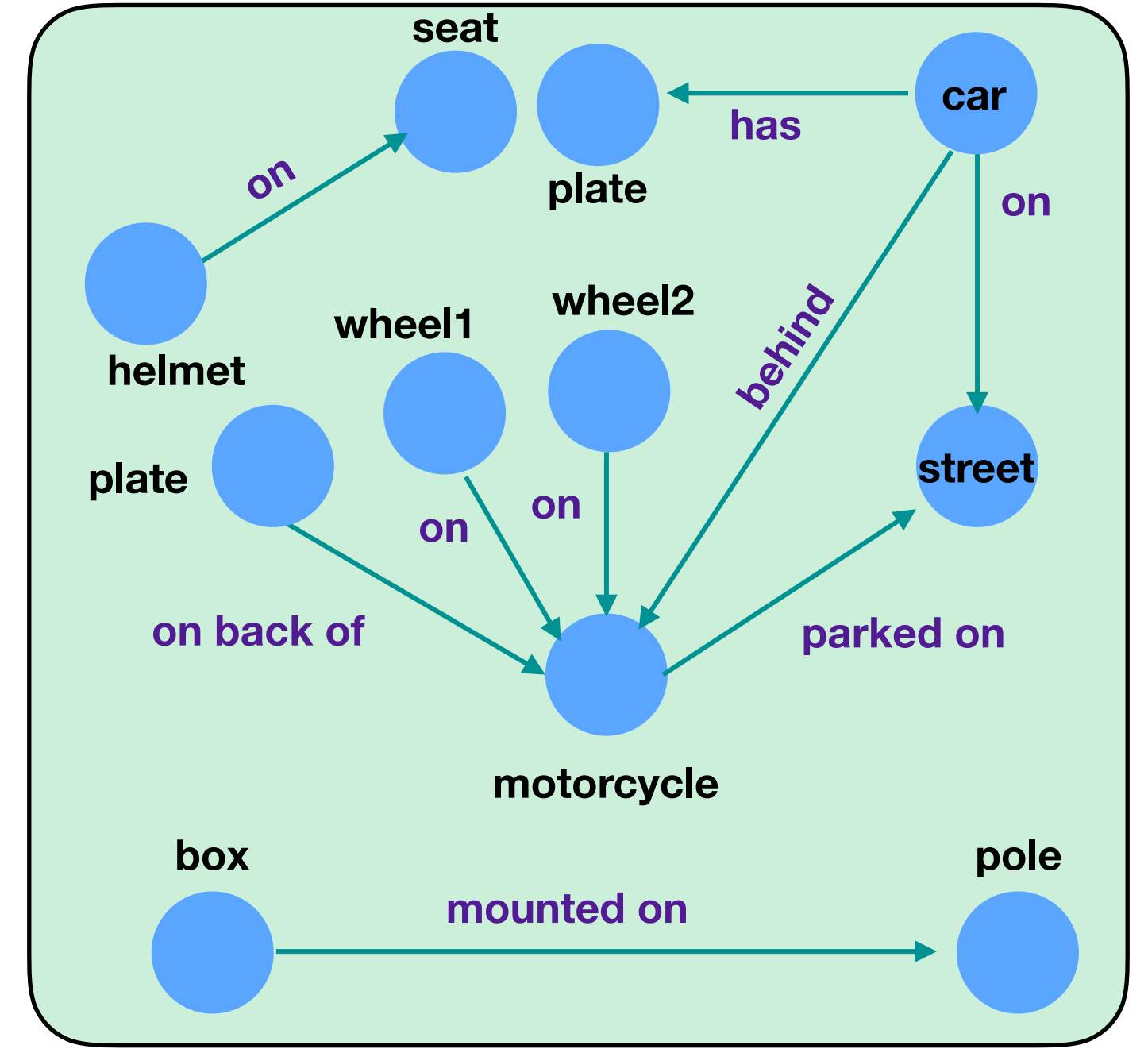
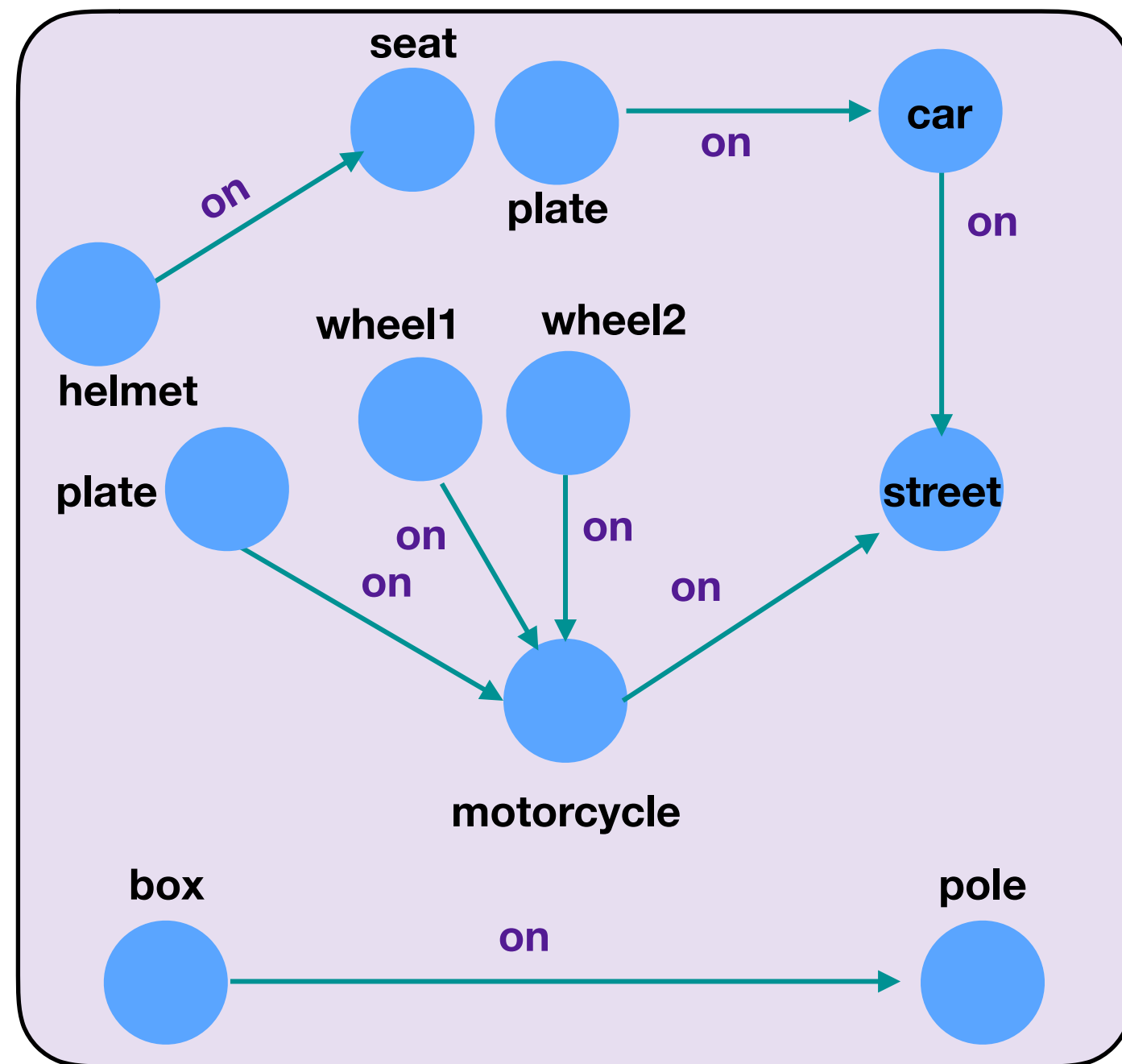
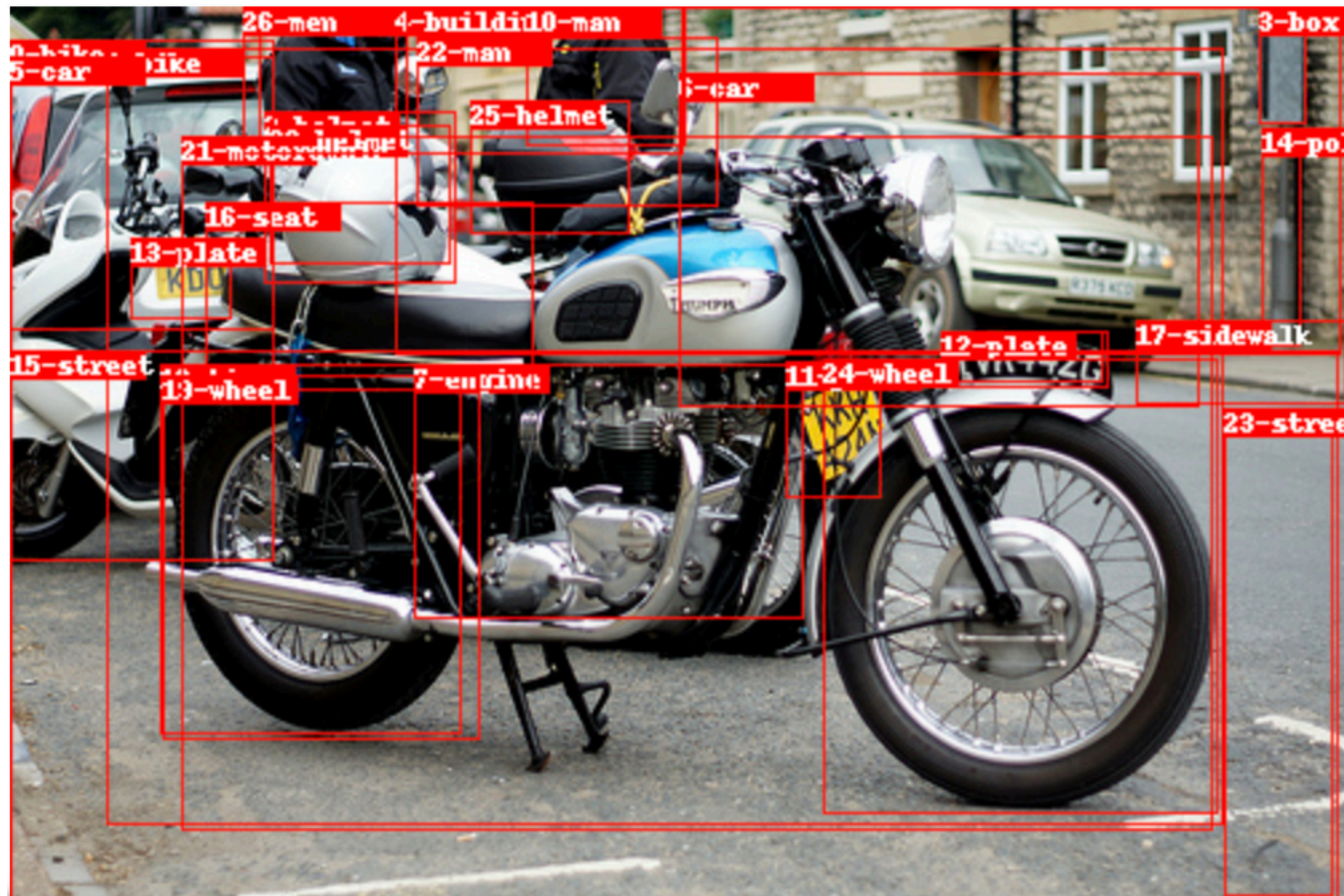
FEATURE
EMBEDDING

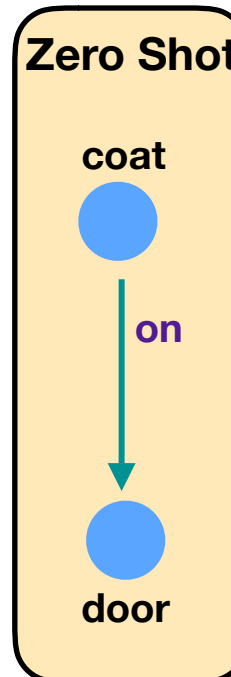
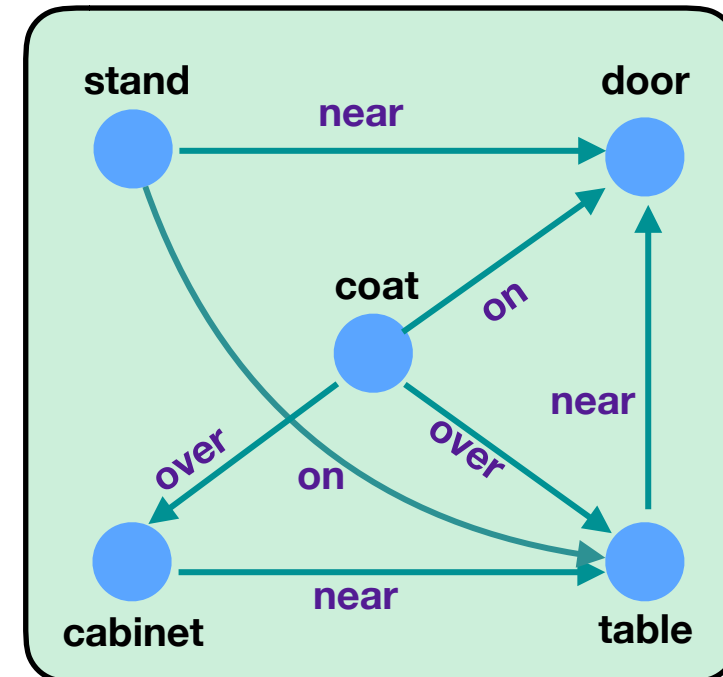
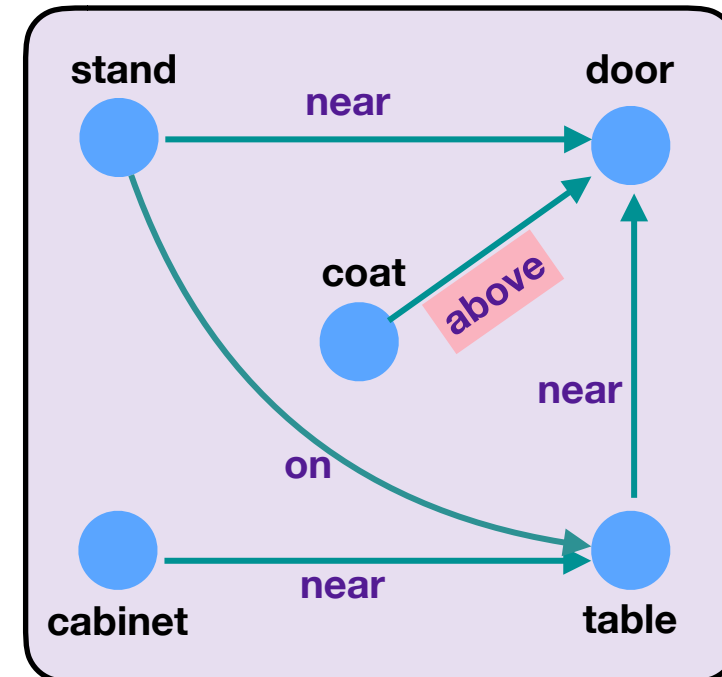
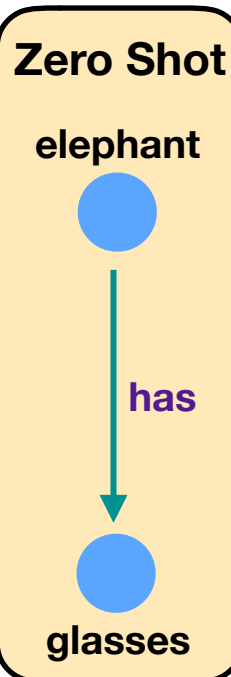
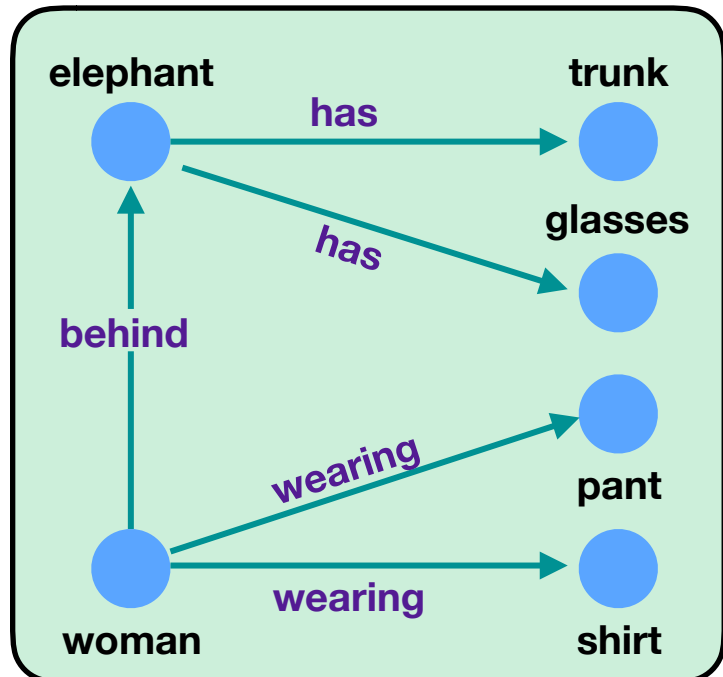
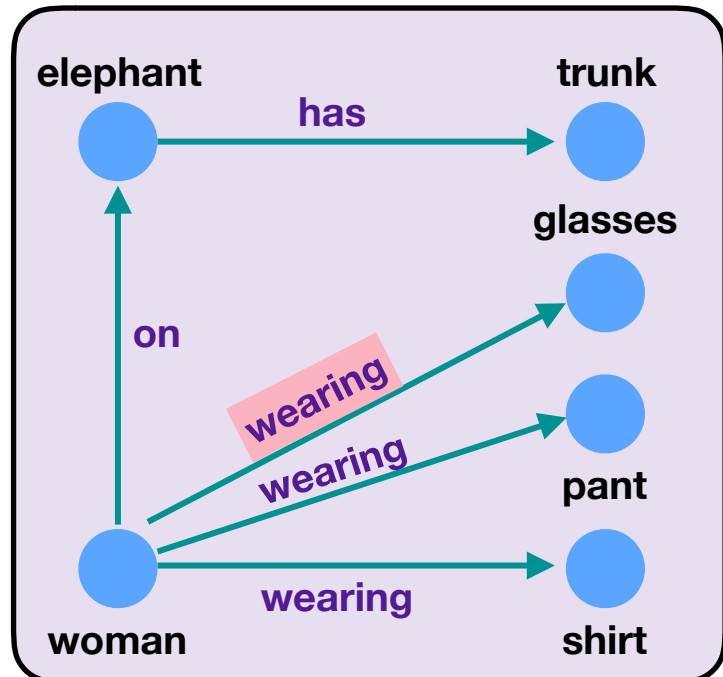
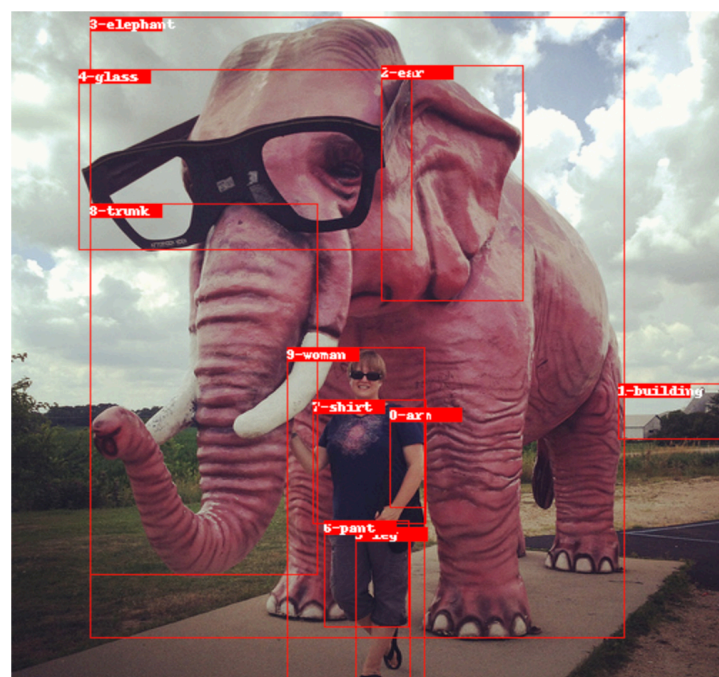
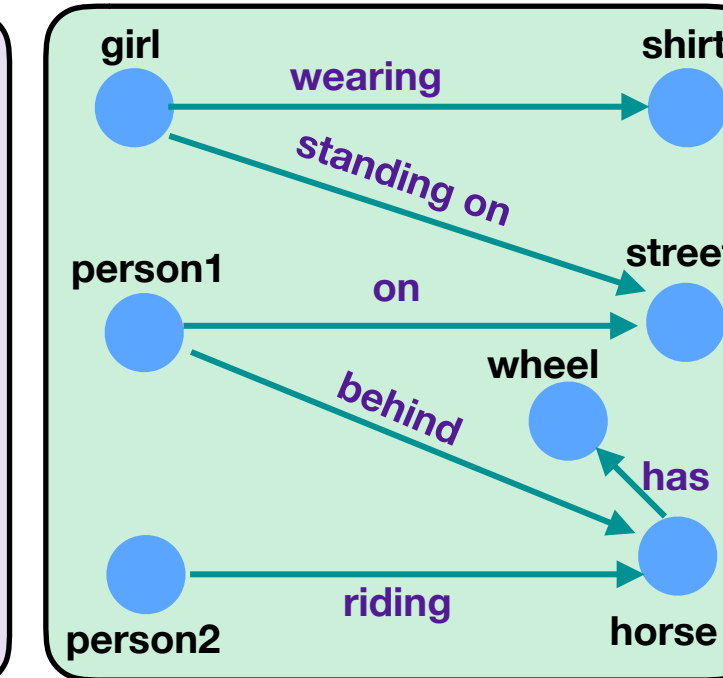
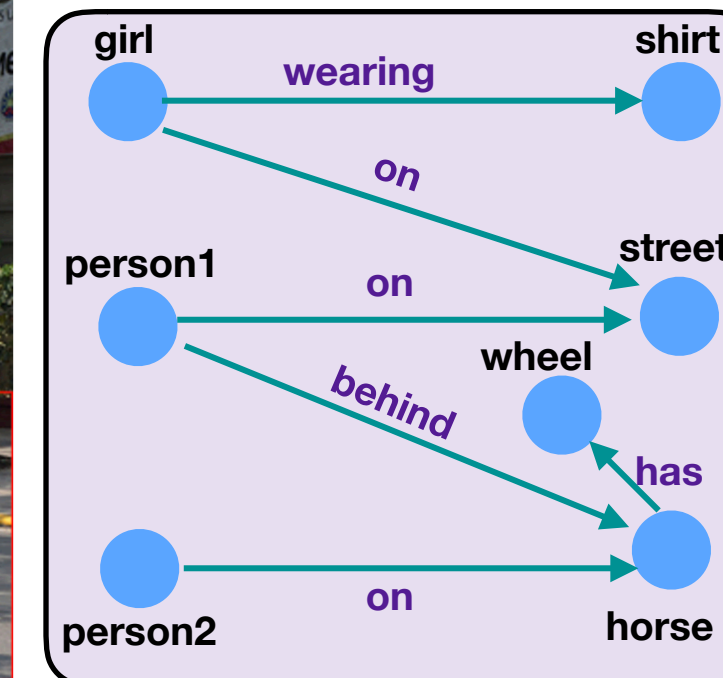
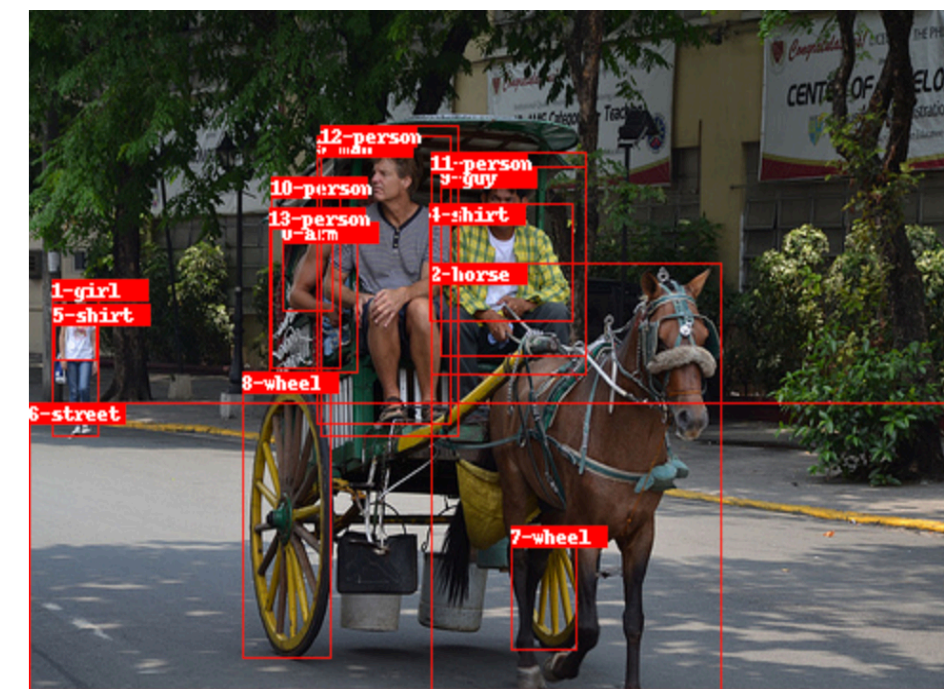
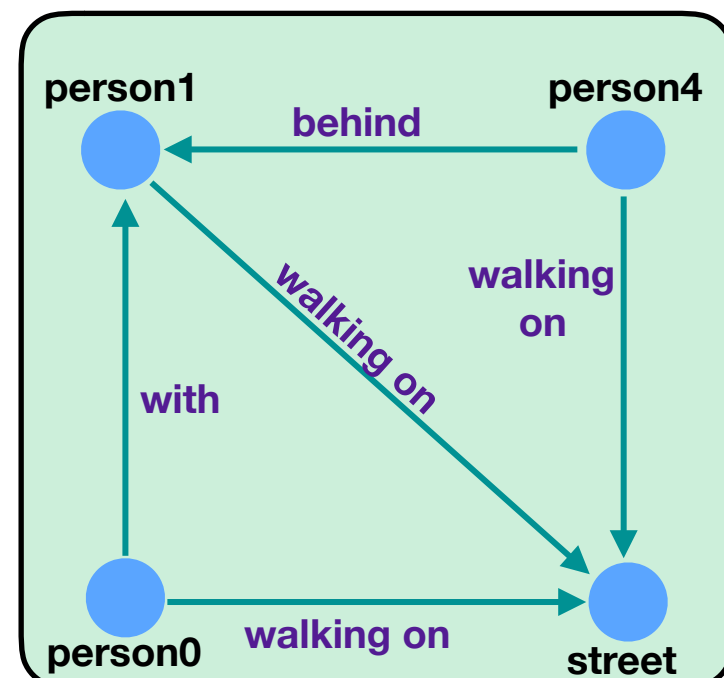
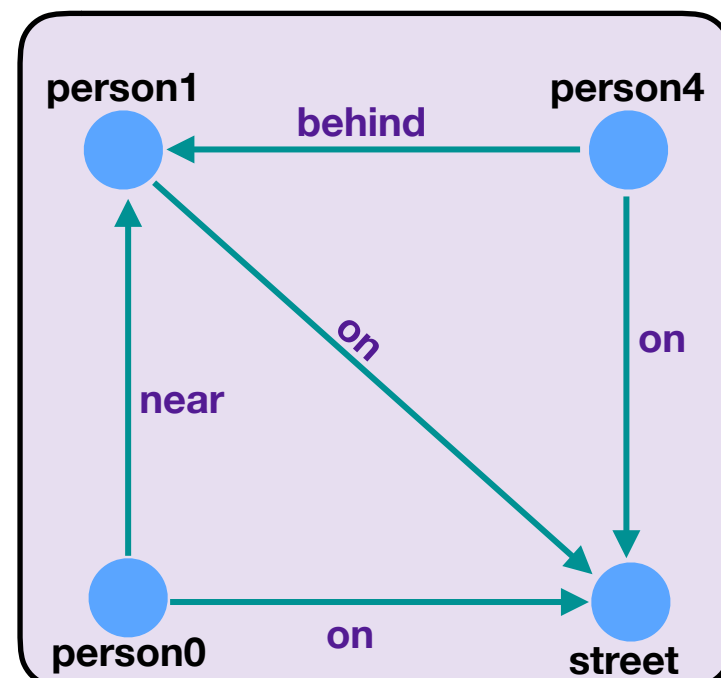
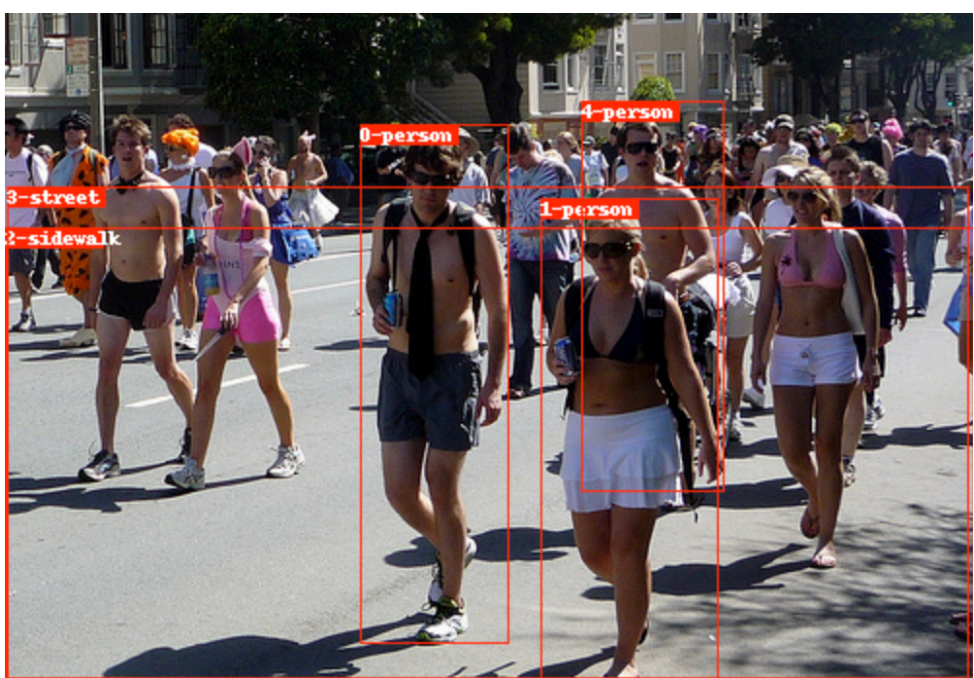
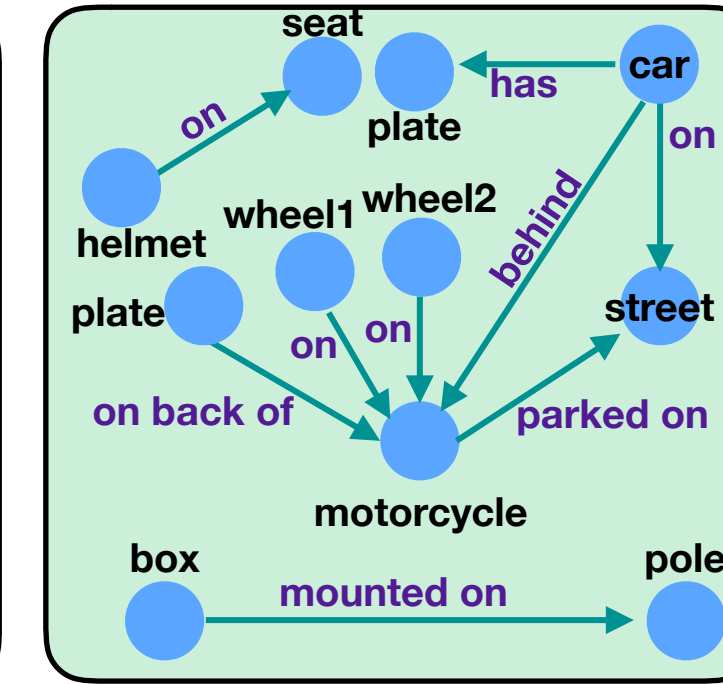
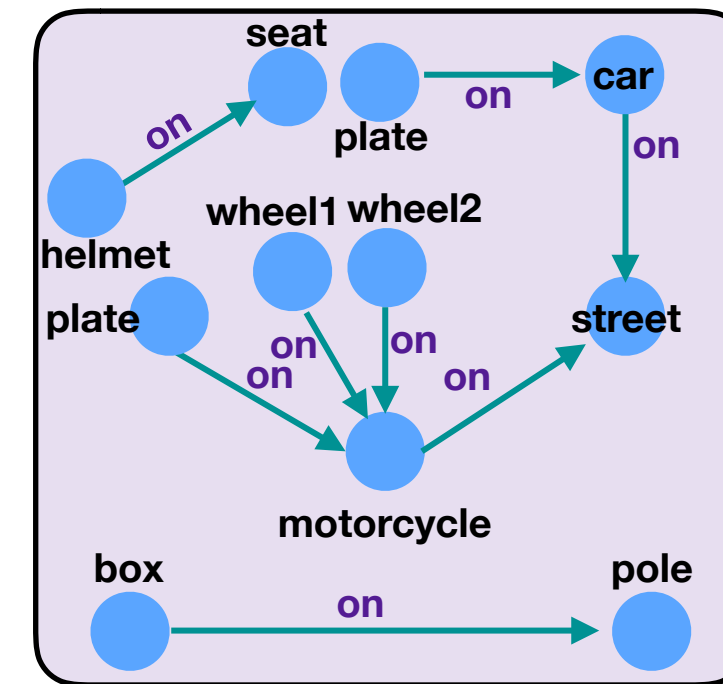
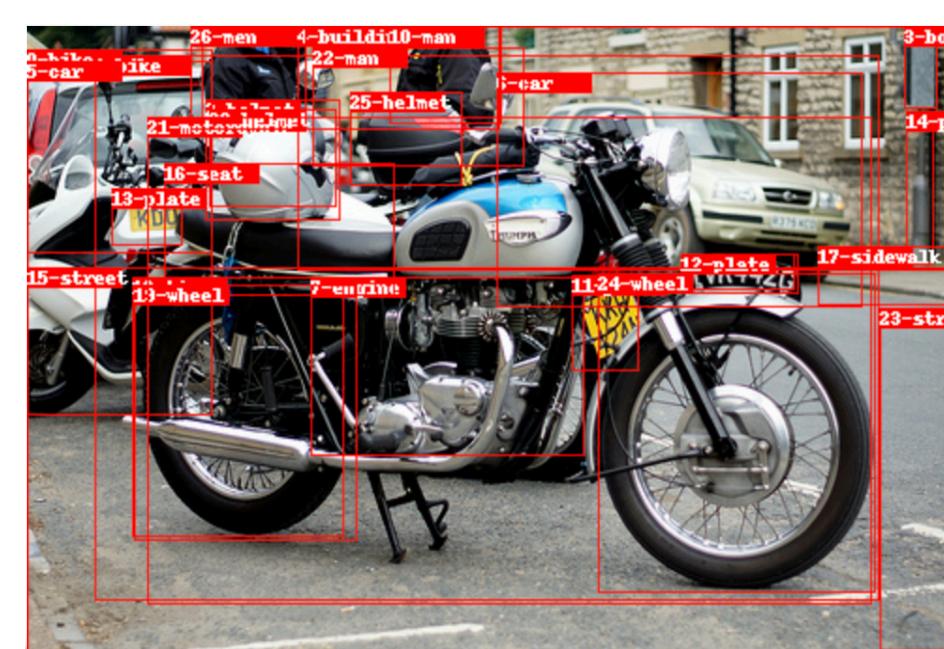
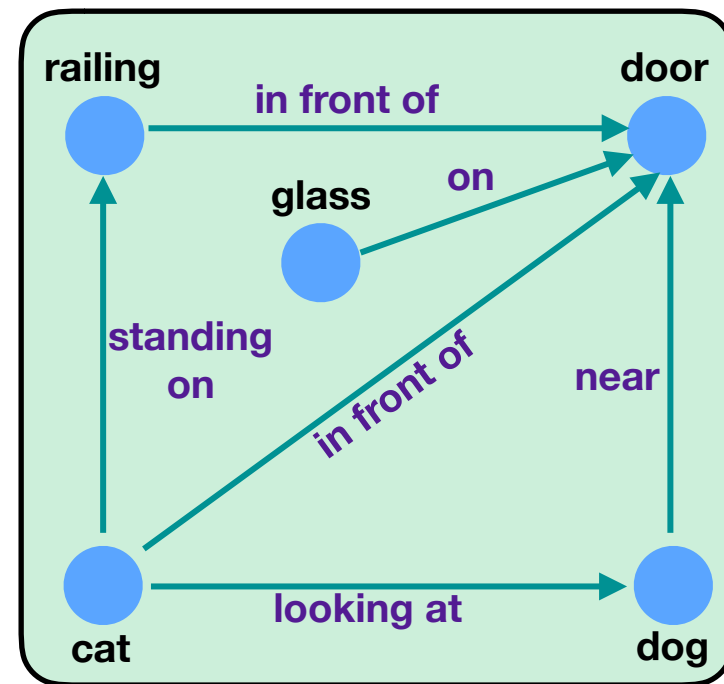
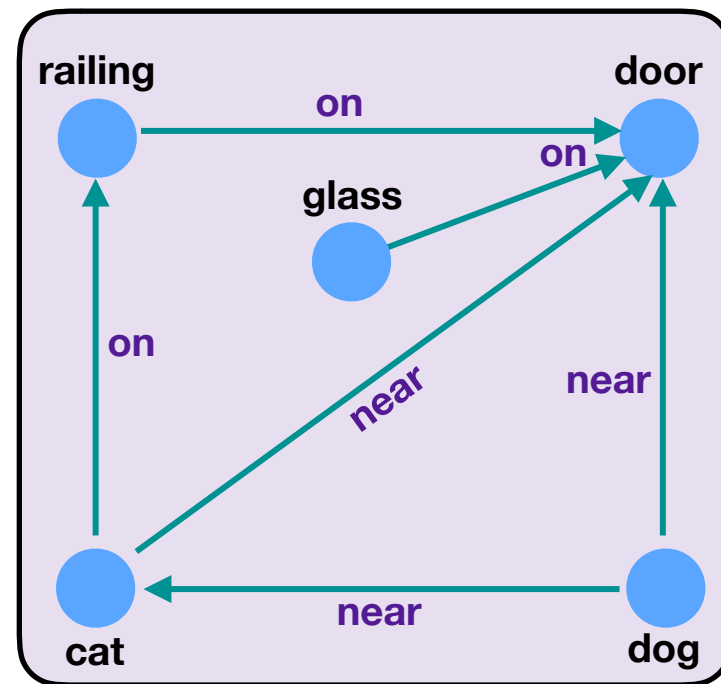
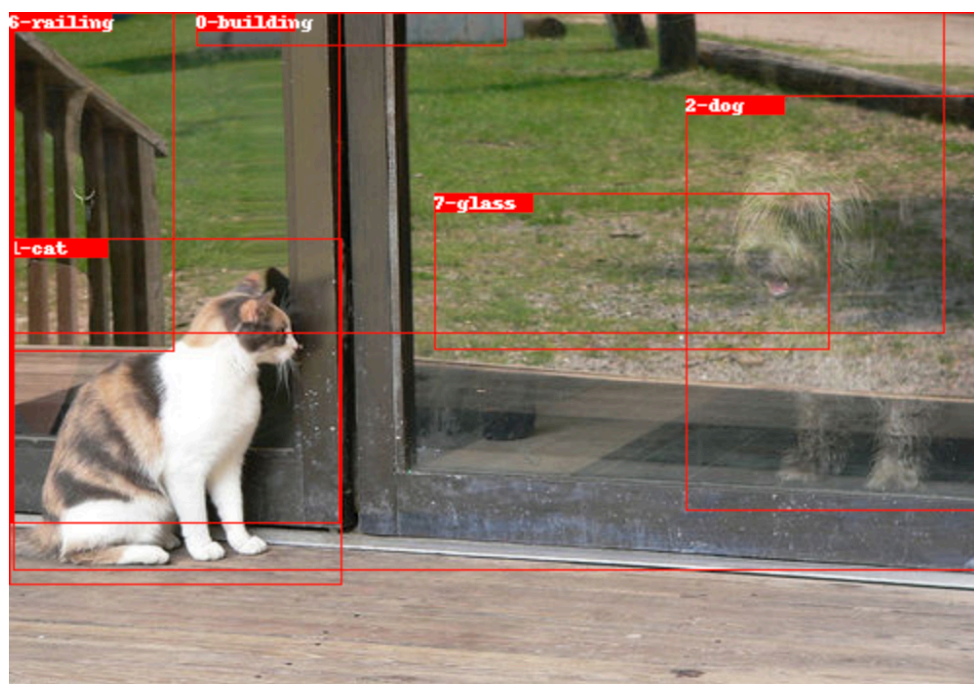
IMAGE GRAPH



Visualizations







Conclusions

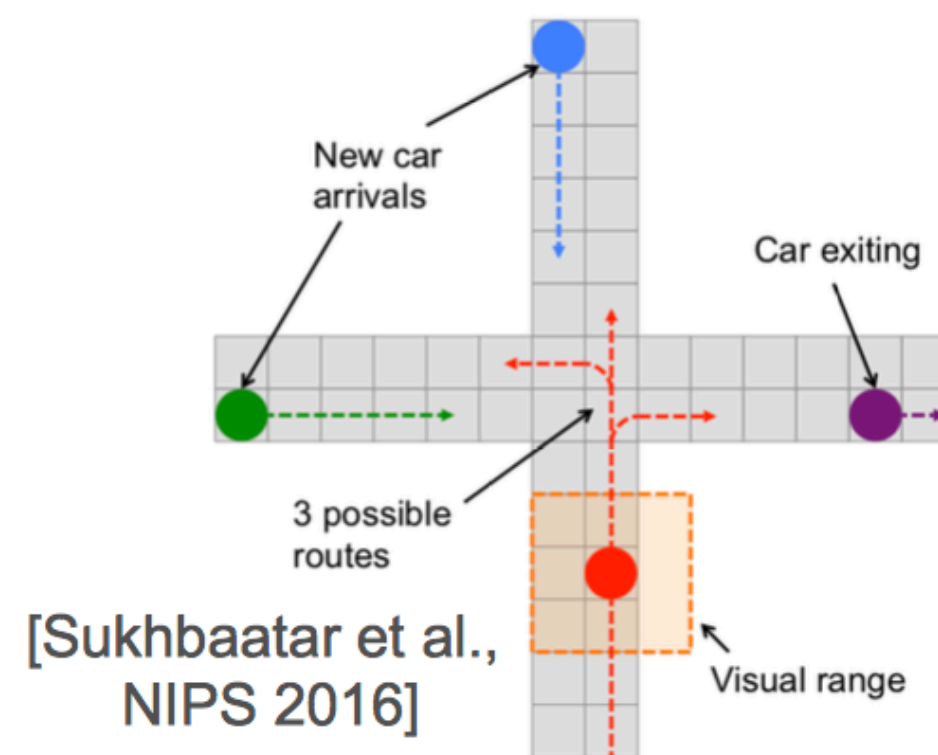
- **Deep learning on graphs works and is very effective!**
- Exciting area: lots of new applications and extensions (hard to keep up)

Relational reasoning



[Santoro et al., NIPS 2017]

Multi-Agent RL



[Sukhbaatar et al., NIPS 2016]

GCN for recommendation on 16 billion edge graph!



Source pin

[Leskovec lab, Stanford]



SUCCESSFUL
RECOMMENDATION



BAD RECOMMENDATION

Open problems:

- Theory
- Scalable, stable generative models
- Learning on large, evolving data
- Multi-modal and cross-model learning (e.g., sequence2graph)

* slide from Thomas Kipf, **University of Amsterdam**