Meta Learning

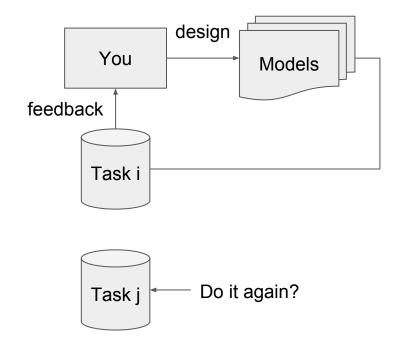
Introduction

Then no *wonder* I can catch up with you so fast after you've had four years of biology." They had wasted all their time memorizing stuff like that, when it could be looked up in fifteen minutes."

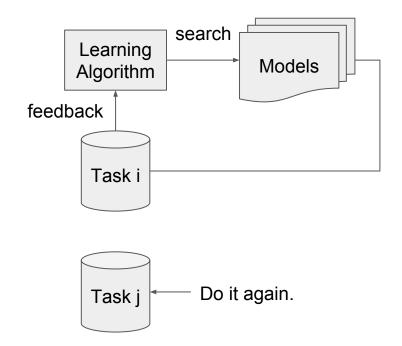
- Meta Learning: Learning to learn
- Big picture:
 - we want our learning algorithms to get better at learning with experience
- Towards AGI goal:
 - cannot just memorize task after task and start from scratch each time



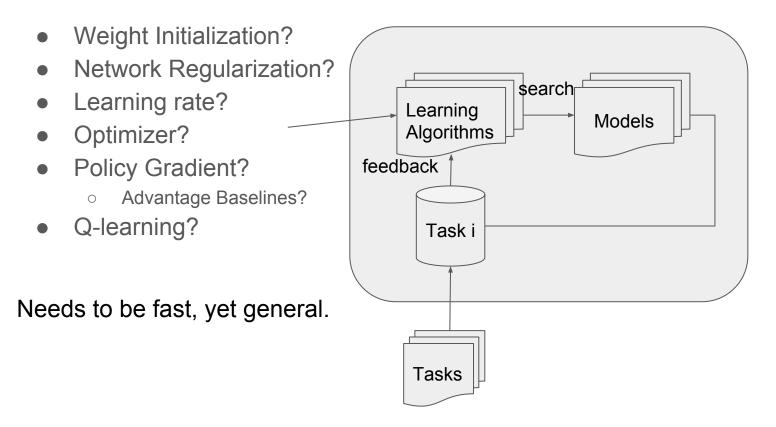
Designing a Task Solver



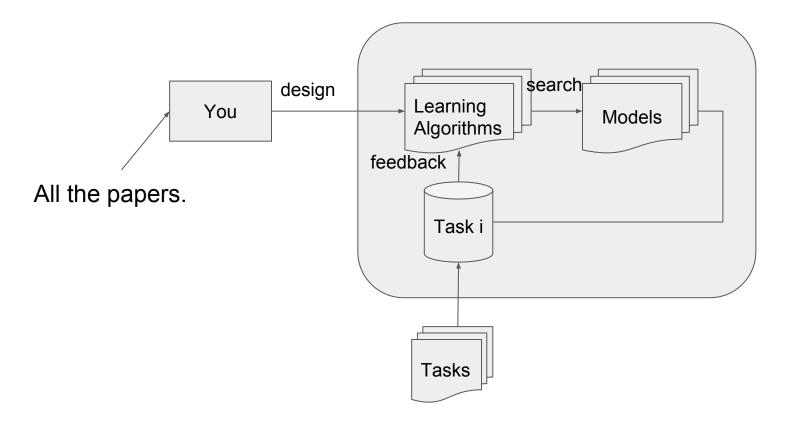
Problem Solved, right?



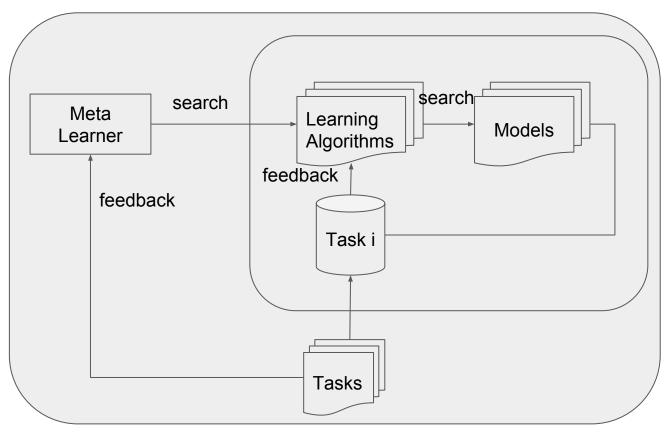
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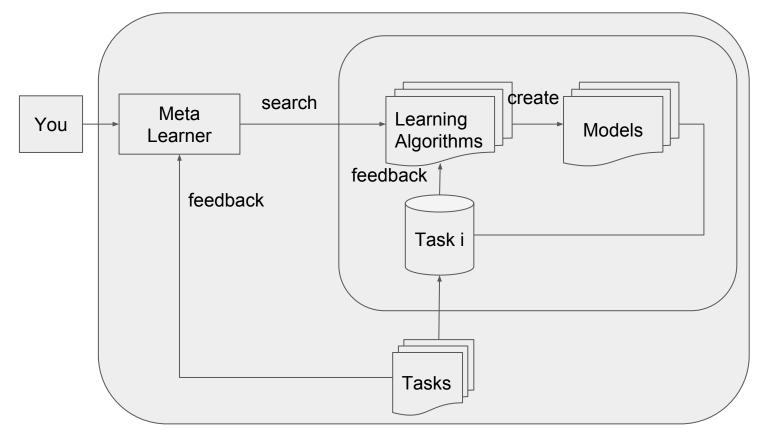
Designing a Tasks Learner



Learning a Tasks Learner

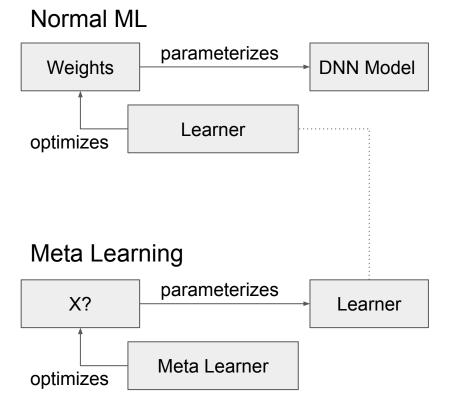


Designing a Tasks Learner Learner

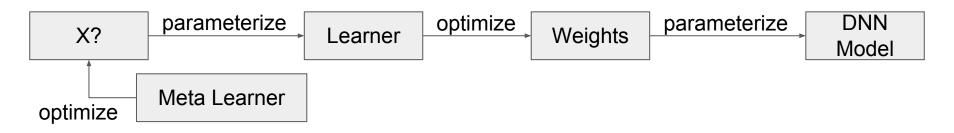


Approaches

- Parameterize the Learner Algorithm with some parameters X
- Meta Learner must optimize the learner with respect to X



Meta Learning Variants

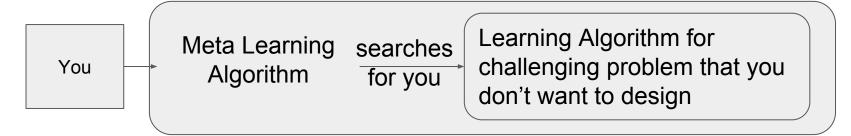


Method	Learner	X	Meta Learner
<u>MAML</u>	<u>SGD</u>	Initial Weights	<u>SGD</u>
L to L by GD by GD	LSTM Weight Updater	Weights of LSTM	SGD
L Transf. Architectures	SGD	Architecture	RNN Controller with RL

Applications

Learning to Learn X:

- Learning to do Fewshot Learning
- Learning Algorithms for Active Learning (Bachman et. al, 2017)
- Meta Learning Shared Hierarchies (Frans et. al, 2017)
- One-shot visual imitation learning via meta-learning (Finn et. al, 2017)
- Deep Online Learning Via Meta-Learning (Nagabandi et. al, 2019)



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$$\mathcal{T} = \{\mathcal{L}(\mathbf{x}_1, \mathbf{a}_1, \dots, \mathbf{x}_H, \mathbf{a}_H), q(\mathbf{x}_1), q(\mathbf{x}_{t+1} | \mathbf{x}_t, \mathbf{a}_t), H\}$$

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1

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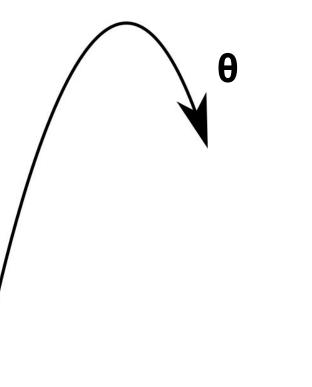
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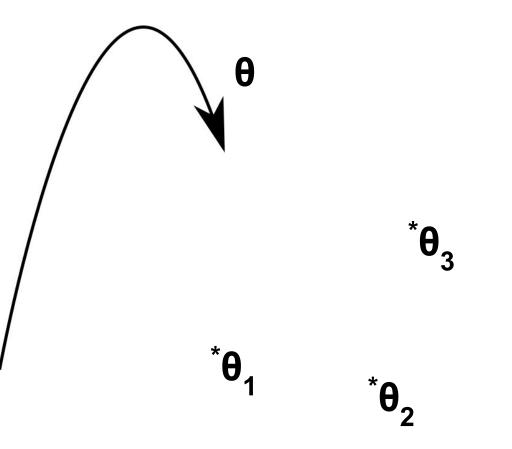
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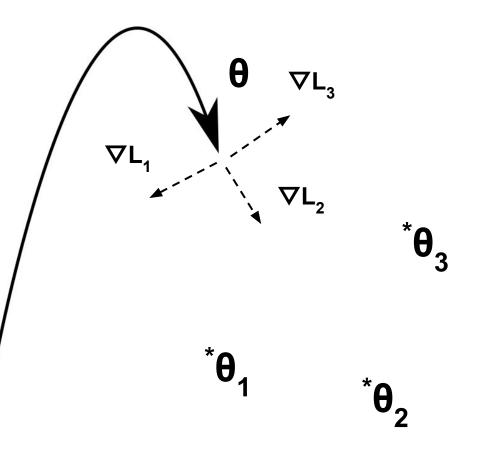
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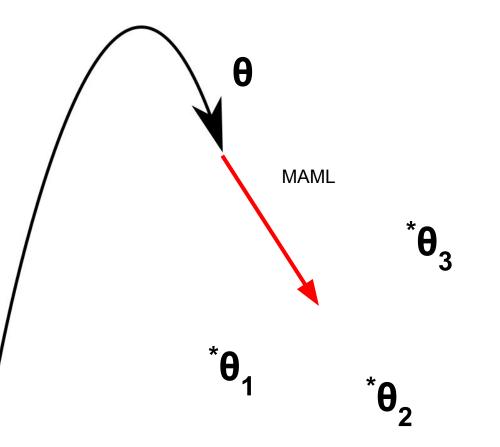
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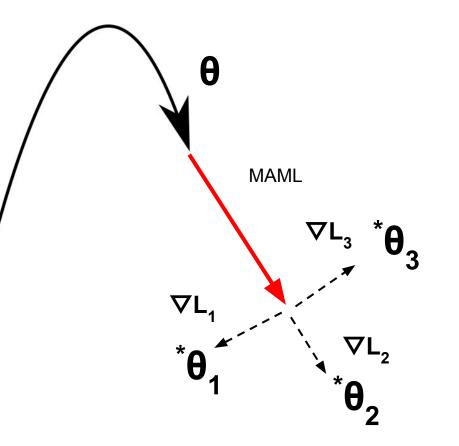
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- Meta-Test error: the test error on tasks that were held out during training











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meta-objective

. . .

$$\min_{\theta} \sum_{\mathcal{T}_i \sim p(\mathcal{T})} \mathcal{L}_{\mathcal{T}_i}(f_{\theta'_i}) = \sum_{\mathcal{T}_i \sim p(\mathcal{T})} \mathcal{L}_{\mathcal{T}_i}(f_{\theta - \alpha \nabla_{\theta} \mathcal{L}_{\mathcal{T}_i}(f_{\theta})})$$

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- Draw **K** examples from **q**_i data points x^(j), y^(j)
- Loss function $L_{T_i}(f_{\theta})$ with respect to K examples:

$$\mathcal{L}_{\mathcal{T}_i}(f_{\phi}) = \sum_{\mathbf{x}^{(j)}, \mathbf{y}^{(j)} \sim \mathcal{T}_i} \|f_{\phi}(\mathbf{x}^{(j)}) - \mathbf{y}^{(j)}\|_2^2$$

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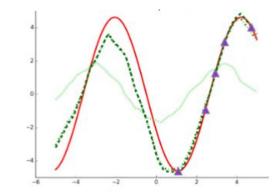
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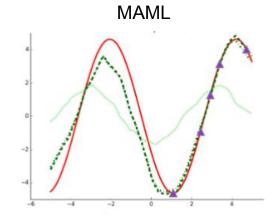
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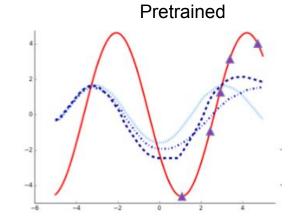
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 - Baseline (pretrained on all possible sine wave tasks)

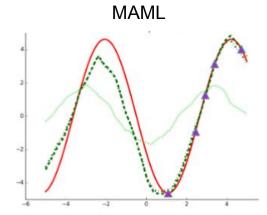
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 - Oracle

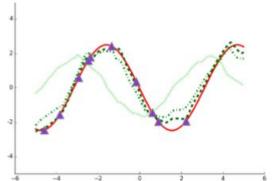
MAML

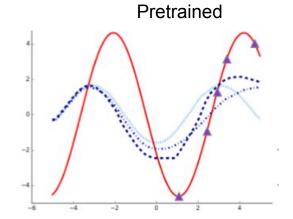




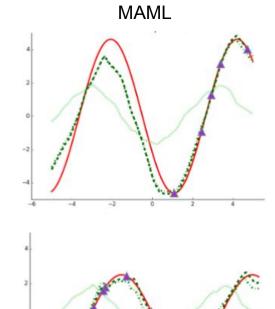


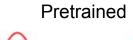


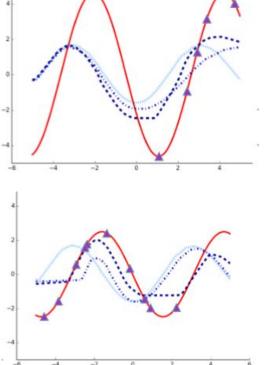




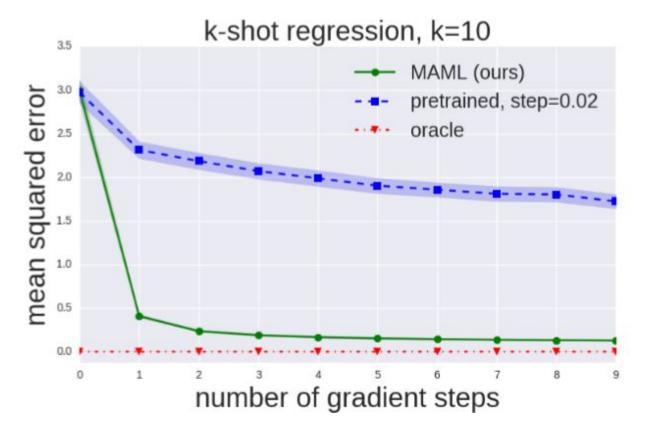








K=10



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 - Trained with only *K* examples from each of the *N* classes

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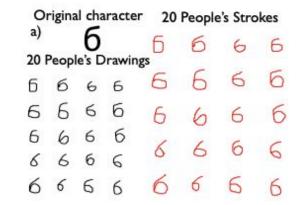
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- Datasets
 - Omniglot
 - MinilmageNet

• Omniglot: 1623 characters with 20 instances each



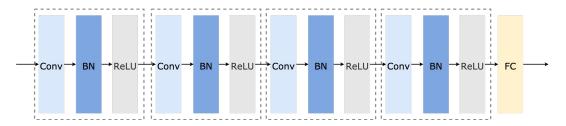
- Omniglot: 1623 characters with 20 instances each
- Randomly sample 1200 characters for training MAML, and use the rest for evaluation

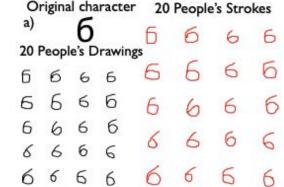
		rigina	al cha	aracter	20	People	e's Stro	kes
. ,	a) 20 I	Peop	6	Prawing	6	б	6	6
	б	б	6	6	6	6	6	б
	6	6	б	б	6	6	6	б
	6	6	6	б	6	6	6	6
	6	6	6	6		-		2
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	6	6	б	6	0	0	v	0
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- N = 5, 20
- K = 1, 5
- A CNN-based classifier





	5-way A	ccuracy	20-way Accuracy			
Omniglot (Lake et al., 2011)	1-shot	5-shot	1-shot	5-shot		
MANN, no conv (Santoro et al., 2016)	82.8%	94.9%	-	-		
MAML, no conv (ours)	$89.7 \pm \mathbf{1.1\%}$	$97.5 \pm \mathbf{0.6\%}$	-	-		
Siamese nets (Koch, 2015)	97.3%	98.4%	88.2%	97.0%		
matching nets (Vinyals et al., 2016)	98.1%	98.9%	93.8%	98.5%		
neural statistician (Edwards & Storkey, 2017)	98.1%	99.5%	93.2%	98.1%		
memory mod. (Kaiser et al., 2017)	98.4%	99.6%	95.0%	98.6%		
MAML (ours)	$98.7\pm\mathbf{0.4\%}$	$99.9 \pm \mathbf{0.1\%}$	$95.8 \pm \mathbf{0.3\%}$	$98.9 \pm \mathbf{0.2\%}$		

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 - 64 training classes
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	5-way Accuracy					
MiniImagenet (Ravi & Larochelle, 2017)	1-shot	5-shot				
fine-tuning baseline	$28.86 \pm 0.54\%$	$49.79 \pm 0.79\%$				
nearest neighbor baseline	$41.08 \pm 0.70\%$	$51.04 \pm 0.65\%$				
matching nets (Vinyals et al., 2016)	$43.56 \pm 0.84\%$	$55.31 \pm 0.73\%$				
meta-learner LSTM (Ravi & Larochelle, 2017)	$43.44 \pm 0.77\%$	$60.60 \pm 0.71\%$				
MAML, first order approx. (ours)	$48.07 \pm \mathbf{1.75\%}$	$63.15 \pm \mathbf{0.91\%}$				
MAML (ours)	$48.70 \pm \mathbf{1.84\%}$	$63.11 \pm \mathbf{0.92\%}$				

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- Each task is an MDP with horizon H
 - \circ q_i(x₁): initial state distribution
 - \circ q(x_{t+1} | x_t, a_t): transition probabilities
 - Task-specific loss corresponds to the negative reward function

$$\mathcal{L}_{\mathcal{T}_i}(f_{\phi}) = -\mathbb{E}_{\mathbf{x}_t, \mathbf{a}_t \sim f_{\phi}, q_{\mathcal{T}_i}} \left[\sum_{t=1}^H R_i(\mathbf{x}_t, \mathbf{a}_t)
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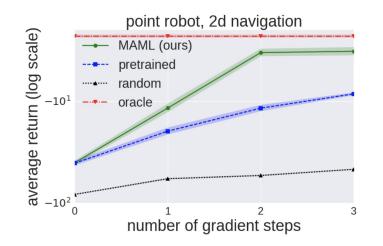
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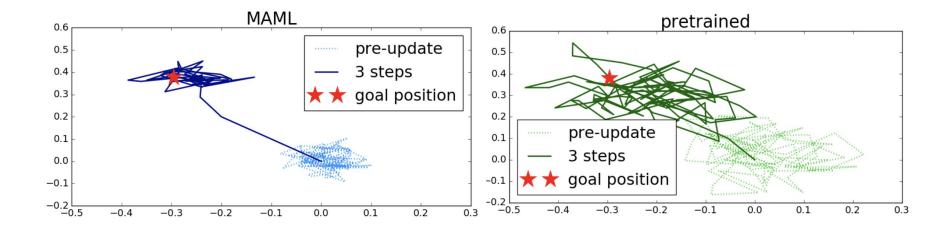
• *K*-shot: sample *K* rollouts from the current policy for each task

- Policy: MLP with 2 hidden layers of size 100 with ReLU non-linearities
- Update: REINFORCE
- Meta-update: TRPO

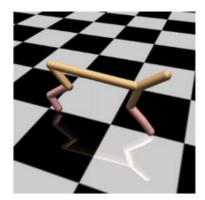
- Policy: MLP with 2 hidden layers of size 100 with ReLU non-linearities
- Update: REINFORCE
- Meta-update: TRPO
- Baselines models for comparisons
 - pretrained: pretrained on all tasks, fine-tuned on the specific task
 - random: training a policy from randomly initialized weights
 - oracle: an oracle policy which receives the parameters of the task as input

- 2D navigation
 - Observation: current 2D coordinates
 - Goal: navigate to a target location
 - Reward: negative squared distance to the target location





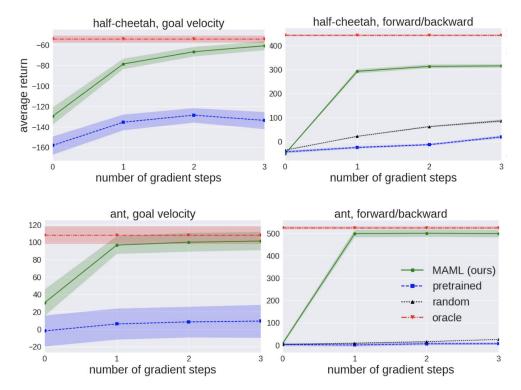
- Continuous control tasks in MuJoCo
 - Agent: ant, half cheetah
 - Observation: torques
 - Goal: run in a particular direction or at a particular velocity
 - Reward:
 - The magnitude of the velocity
 - The negative absolute value between the current velocity of the agent and a goal



Half Cheetah







Video results can be found at https://sites.google.com/view/maml

PAML - Proactive and Adaptive meta-learning.

- L.-Y. Gui et al modified the MAML algorithm in their paper: Few-Shot Human Motion Prediction via Meta-learning
- The paper combined the MAML algorithm with a model regression network (MRN) to predict outcomes of human motion in with only a few examples.
- PAML was developed out of the need to develop a more flexible meta-learning algorithm to learn a more complicated tasks quickly.

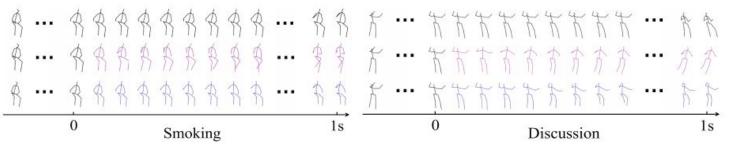
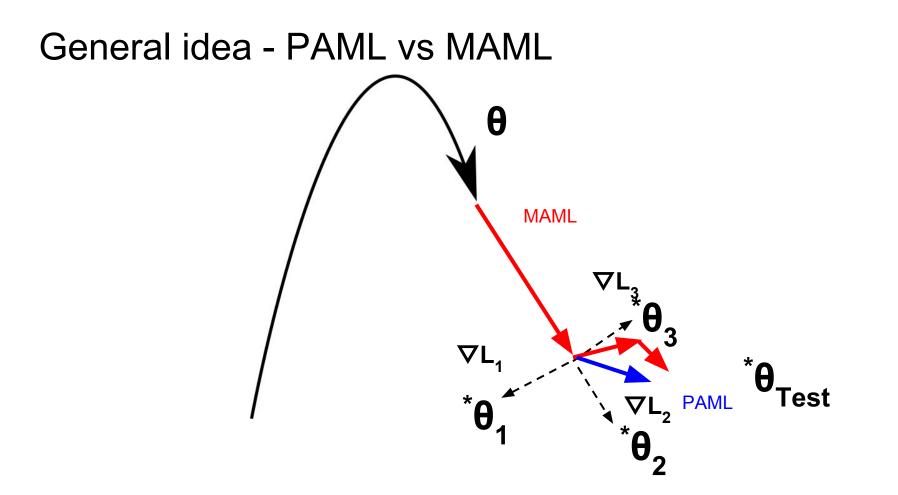
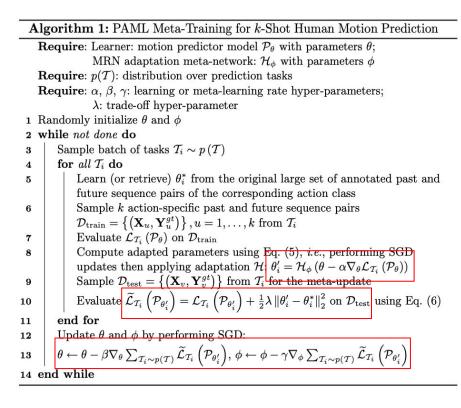


Figure from L.-Y. Gui et al. where the top is the ground truth of motion, the pink are the baseline predictions and the bottom is the prediction form PAML.



PAML - Algorithm changes



- The main difference is using a feed forward network to perform the parameter update for the k shot learning.
- We also must solve for parameters from many shot learning before hand and use it in the regularization term.
- We then update two sets of parameters: the learners parameters, and the meta learners parameters.
- The idea is the meta-network will learn how to adjust parameters to allow it to generalize well.

$$\min_{\theta,\phi} \sum_{\mathcal{T}_{i} \sim p(\mathcal{T})} \widetilde{\mathcal{L}}_{\mathcal{T}_{i}}\left(\mathcal{P}_{\theta_{i}'}\right) = \min_{\theta,\phi} \sum_{\mathcal{T}_{i} \sim p(\mathcal{T})} \mathcal{L}_{\mathcal{T}_{i}}\left(\mathcal{P}_{\theta_{i}'}\right) + \frac{1}{2}\lambda \left\|\theta_{i}' - \theta_{i}^{*}\right\|_{2}^{2},$$

r

Experimental results - sanity check.

Method	5-way accuracy							
Method	1-shot	5-shot						
Matching networks [61]	$43.56\% \pm 0.84\%$	$55.31\%\pm 0.73\%$						
MAML [14]	$48.70\% \pm 1.84\%$	$63.11\% \pm 0.92\%$						
Meta-learner LSTM [43]	$43.44\% \pm 0.77\%$	$60.60\%\pm 0.71\%$						
Prototypical networks [51]	$46.61\% \pm 0.78\%$	$65.77\% \pm 0.70\%$						
Meta networks [34]	$49.21\% \pm 0.96\%$							
PAML (Ours)	${\bf 53.26\% \pm 0.52\%}$	${\bf 68.19\% \pm 0.61\%}$						

Table from L.-Y. Gui et al.

- L.-Y Gui et al performed a sanity check using 1-shot and 5-shot learning on classification tasks on mini-ImageNet.
- Results showed their accuracy to be the best.
- I don't think this should be surprising. It's more flexible method and there is no shortage of data.

Experimental results - Human motion prediction

		Walking				Eating							
milliseconds			160	320	400	560	1000	80	160	320	400	560	1000
	$Scratch_{spec}$	1.90	1.95	2.16	2.18	1.99	2.00	2.33	2.31	2.30	2.30	2.31	2.34
residual sup. [32] w/	Scratch _{agn}	1.78	1.89	2.20	2.23	2.02	2.05	2.27	2.16	2.18	2.27	2.25	2.31
(Baselines)	Transfer _{ots}	0.60	0.75	0.88	0.93	1.03	1.26	0.57	0.70	0.91	1.04	1.19	1.58
	Multi-task	0.57	0.71	0.79	0.85	0.96	1.12	0.59	0.68	0.83	0.93	1.12	1.33
	Transfer _{ft}	0.44	0.55	0.85	0.95	0.74	1.03	0.61	0.65	0.74	0.78	0.86	1.19
Meta-learning (Ours) PAML		0.35	0.47	0.70	0.82	0.80	0.83	0.36	0.52	0.65	0.70	0.71	0.79
		Smoking				Discussion							
millisecond	s	80	160	320	400	560	1000	80	160	320	400	560	1000
	Scratch _{spec}	2.88	2.86	2.85	2.83	2.80	2.99	3.01	3.13	3.12	2.95	2.62	2.99
residual sup. $[32] w/$	Scratch _{agn}	2.53	2.61	2.67	2.65	2.71	2.73	2.77	2.79	2.82	2.73	2.82	2.76
(Baselines)	Transfer _{ots}	0.70	0.84	1.18	1.23	1.38	2.02	0.58	0.86	1.12	1.18	1.54	2.02
	Multi-task	0.71	0.79	1.09	1.20	1.25	1.23	0.53	0.82	1.02	1.17	1.33	1.97
	Transfer _{ft}	0.87	1.02	1.25	1.30	1.45	2.06	0.57	0.82	1.11	1.11	1.37	2.08

Figures from L.-Y. Gui et al.

- Dataset is human 3.6M, which is benchmarked often.
- Used 5 shot learning.
- Training was done on 11 action classes: directions, greeting, phoning, posing, purchases, sitting, sitting down, taking photo, waiting, walking dog, and walking together
- Testing was done on the four shown here.
- The numbers correspond to mean angle error, so lower is better.

Discussion - MAML

Positives

- MAML is a simple way to get a good network initialization.
- It is also Model agnostic, so it is easy to implement.
- It is great for building pretrained models for others to use without having to spend weeks of training time.

Negatives

• My not be flexible enough for other certain applications, but is a great start.

Discussion - PAML

Positives

- Adds more flexibility to the MAML architecture.
- Trained model can learn more complex tasks in a few shots.
- Needed when an agent needs to learn from few examples.
- L.-Y. Gui et al. found would be useful for robots to learn interactions with humans quickly.

Negatives

- We need to train a second network which adds time and complexity.
- Does appear to outperform MAML, but we need to train more hyper parameters with also adds more time for cross validation.
- A lot of hyper parameters mean we have to be careful to not overfit the validation set.

Conclusion

- Meta Learning is learning how to learn.
- Main goal: we want our learning algorithms to get better at learning with experience
- We presented two major meta learning frameworks.
- Maml to find a good parameter initialization
- PAML which adds more flexibility to learn in less examples, with the trade off of more training time and more hyper parameter tuning.
- Thank you for listening, Questions?