

#### THE UNIVERSITY OF BRITISH COLUMBIA

# **CPSC 425: Computer Vision**



### Lecture 19: Visual Classification 1, Bag of Words

# Menu for Today

# **Topics:**

# — Visual Classification

## **Readings:**

- Today's Lecture: Szeliski 11.4, 12.3-12.4, 9.3, 5.1-5.2

## **Reminders:**

- Assignment 2 graded and posted
- Assignment 3 will be graded by the end of the week
- Assignment 4 is due today
- Assignment 5: Scene Recognition with Bag of Words is now available

## - **Bag of Words** Representations







# Today's "fun" Example:

# Audio-Visual Scene Analysis with Self-Supervised Multisensory Features

Andrew Owens Alexei A. Efros UC Berkeley



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# Audio-Visual Scene Analysis with Self-Supervised Multisensory Features

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# Object Recognition / Detection

## Template matching ...



\*







# Object Recognition / Detection

## Object recognition with SIFT features and RANSAC [Lowe 1999]





## What is present? Where? What orientation?







# Object Recognition / Detection

## PASCAL Visual Object Classes Challenges [2005-2012]







## What is present? Where? What orientation?

# Object Classification and Detection

## **Detection**: Label per region, e.g., PASCAL VOC



[Krizhevskv et al 2011][Ren et al 2016]

# Object Classification and Detection

## Classification: Label per image, e.g., ImageNet



## **Detection**: Label per region, e.g., PASCAL VOC

cockroach

starfish

tick

amphibian

drilling platform

fireboat



scooter	leopard	grille	mushroom
otor scooter	leopard	convertible	agaric
go-kart	jaguar	grille	mushroom
moped	cheetah	pickup	jelly fungus
bumper car	snow leopard	beach wagon	gill fungus
golfcart	Egyptian cat	fire engine	dead-man's-fingers

#### [Krizhevskv et al 2011][Ren et al 2016]

# Segmentation

## Segmentation: Label per pixel, e.g., MS COCO



#### [Hu et al 2017]

# Structured Image Understanding

"Girl feeding large elephant" "A man taking a picture behind girl"



#### visualgenome.org [Krishna et al 2017]

# Object Classification

## Classification: Label per image, e.g., ImageNet



oter	leopard	grille	mushroom		
cooter	leopard	convertible	agaric		
jo-kart	jaguar	grille	mushroom		
moped	cheetah	pickup	jelly fungus		
ber car	snow leopard	beach wagon	gill fungus		
olfcart	Egyptian cat	fire engine	dead-man's-fingers		

#### [Krizhevskv et al 2011][Ren et al 2016]

# Classification: Instance vs. Category



## Instance of Aeroplane (Wright Flyer)













### Category of Aeroplane

## [Caltech IOI]



# Classification: Instance vs. Category



#### Instance of a cat



### Category of domestic cats



# Taxonomy of Cats

- → Mammals (Class Mammalia)
  - → Therians (Subclass Theria)
    - → Placental Mammals (Infraclass Placentalia)
      - └→ Ungulates, Carnivorans, and Allies (Superorder Laurasiatheria)
        - → Carnivorans (Order Carnivora)
          - → Felines (Family Felidae)
            - → Small Cats (Subfamily Felinae)
              - → Genus *Felis* 
                - → Chinese Mountain Cat (Felis bieti)
                - → Domestic Cat (Felis catus)
                - → Jungle Cat (Felis chaus)
                - → African Wildcat (Felis lybica)
                - → Sand Cat (Felis margarita)
                - → Black-footed Cat (Felis nigripes)
                - └→ European Wildcat (Felis silvestris)





Ocelot [Jitze Couperus]



European Wildcat [the wasp factory]



[<u>inaturalist.org</u>]<sup>14</sup>

## **Problem**:

Assign new observations into one of a fixed set of categories (classes)

## Key Idea(s):

Build a model of data in a given category based on observations of instances in that category



(assume given set of discrete labels) {dog, cat, truck, plane, ...}

cat



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1	54	69	16	92	33	48	61	43	52	01	69	1.0	67	48

class label (probability over class labels)

# A classifier is a procedure that accepts as input a set of features and outputs a

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Classifiers can be **binary** (face vs. not-face) or **multi-class** (cat, dog, horse, ...).

**Binary**: [0]/[1]

Multi-class: [1, 0, 0, 0, ...] (one-hot)























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We build a classifier using a **training set** of labelled examples  $\{(\mathbf{x}_i, y_i)\}$ , where each  $\mathbf{x}_i$  is a feature vector and each  $y_i$  is a class label.



Multi-class: [1, 0, 0, 0, ...] (one-hot)























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Given a previously unseen observation, we use the classifier to predict its class label.

**Binary**: [0]/[1]

Multi-class: [1, 0, 0, 0, ...] (one-hot)























Collect a database of images with labels

- Use ML to train an image classifier
- Evaluate the classifier on test images



#### Example training set

# **Example 1**: A Toy Classification Problem

Categorize images of fish - "Atlantic salmon" vs "Pacific salmon"

Use **features** such as length, width, lightness, fin shape & number, mouth position, etc.

Given a previously unobserved image of a salmon, use the learned classifier to guess whether it is an Atlantic or Pacific salmon



#### Figure credit: Duda & Hart

# **Example 2**: Real Classification Problem

## **SUN Dataset**

- 131K images
- 908 scene categories

indoor	shopping and dining	auto showroom
outdoor natural	workplace (office building, factory, lab, etc.)	bakery kitchen
outdoor man-made	home or hotel	bakery shop
	transportation (vehicle interiors, stations, etc.)	bank indoor
	sports and leisure	bank vault
	cultural (art, education, religion, millitary, law, politics, etc.)	banquet hall
		bar
		IV = - with

# **Example 3**: Real Classification Problem



An object occurring naturally; not made by man

• Numbers in brackets: (the number of synsets in the subtree ). Treemap Visualization Images of the Synset Downloads M ) ImageNet 2011 Fall Release ) Natural object ImageNet 2011 Fall Release (32326) plant, flora, plant life (4486) Plant Covering P 2 -1 1 0 DE 5 geological formation, formation (1) aquifer (0) beach (1) cave (3) 45 0 cliff, drop, drop-off (2) delta (0) diapir (0) 50 folium (0) Extraterre Body Sample foreshore (0) ice mass (10) lakefront (0) 14.6 massif (0) monocline (0) 3 <u>Asterism</u> Celestia Mechanism mouth (0) natural depression, depression natural elevation, elevation (41) . oceanfront (0) 16 12 range, mountain range, range of Radiator Body relict (0) 24 ridge, ridgeline (2) T ridge (0) Rock 10 A 10 shore (7) 27 slope, incline, side (17) Tangle 2. spring, fountain, outflow, outpo 27 talus, scree (0) vein, mineral vein (1) \*\* 🎲 👫 🎥 🍣 🏹 volcanic crater, crater (2)

# 

## ImageNet Dataset

- 14 Million images
- 21K object categories

#### Natural object





wall (0)

water table, water level, ground

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# **Closed-world** problem

**Issue:** Classification assumes that incoming image belongs to one of k classes. However, in practice it is impossible to enumerate all relevant classes in the world, nor would doing so be useful. So how do we deal with images which don't belong?

**Solution**: Create an "unknown" or "irrelevant" class.

# Image Classification

- **Classification** Algorithms
- Bayes' Classifier
- Nearest Neighbor Classifier
- SVM Classifier

- Representation of Images
- Image pixels directly
- Bag of Words



Let c be the **class label** and let x be the **measurement** (i.e., evidence)

#### posterior probability



 $P(c|x) = \frac{P(x|c)p(c)}{P(x)}$ 

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

class-conditional probability (a.k.a. likelihood)



#### posterior probability

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

## Simple case:

- binary classification; i.e.,  $c \in \{1, 2\}$
- features are 1D; i.e.,  $x \in \mathbb{R}$

 $P(c|x) = \frac{P(x|c)p(c)}{P(x)}$ 



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Classify **x** as

1 if  $p(1|\mathbf{x}) > p(2|\mathbf{x})$ 



2 if  $p(1|\mathbf{x}) < p(2|\mathbf{x})$ 

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## **General** case:

- multi-class; i.e.,  $c \in \{1, ..., 1000\}$
- features are high-dimensional; i.e.,  $x \in \mathbb{R}^{2,000+}$



# **Example**: Discrete Bayes Classifier

Assume we have two classes:  $c_1 = male$ We have a person who's gender we don't know, who's name is *drew* 

### $c_2 = \mathbf{female}$

#### **Example from:** Eamonn Keogh

# **Example**: Discrete Bayes Classifier

# Assume we have two classes: $c_1 = \text{male}$ $c_2 = \text{female}$ We have a person who's gender we don't know, who's name is *drew*



Drew Carey



Drew Barrymore

#### Example from: Eamonn Keogh

eoah
Assume we have two classes:  $c_1$ 

We have a person who's gender we don't know, who's name is drew

Classifying drew as being male or female is equivalent to asking is it more probable that *drew* is male or female, i.e. which is greater  $p(\mathbf{male}|drew)$  $p(\mathbf{female}|drew)$ 



Drew Carey

#### $c_1 =$ male $c_2 =$ female



Drew Barrymore

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Assume we have two classes:

We have a person who's gender we don't know, who's name is *drew* 

Classifying drew as being male or female is equivalent to asking is it more probable that *drew* is male or female, i.e. which is greater p(male|drew) $p(\mathbf{female}|drew)$ 

#### $c_1 = \mathbf{male}$ $c_2 = \mathbf{female}$

 $p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$ 

Name	Gend	
Drew	Male	
Claudia	Female	
Drew	Female	
Drew	Female	
Alberto	Male	
Karin	Female	
Nina	Female	
Sergio	Male	

 $p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$ 



 $p(\mathbf{male}) =$ 

 $p(drew|\mathbf{male}) =$ 

p(drew) =

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 $p(\mathbf{male}|drew) = \frac{p(drew|\mathbf{male})p(\mathbf{male})}{p(drew)}$ 



 $p(\text{male}) = \frac{3}{8}$  $p(drew|\mathbf{male}) =$ 

p(drew) =

Name	Gend	
Drew	Male	
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$$e^{3} = \frac{5}{8}$$

$$e^{3} = \frac{2}{5}$$

Name	Gend	
Drew	Male	
Claudia	Female	
Drew	Female	
Drew	Female	
Alberto	Male	
Karin	Female	
Nina	Female	
Sergio	Male	

 $p(\mathbf{female}|drew) = \frac{p(drew|\mathbf{female})p(\mathbf{female})}{p(\mathbf{female})}$ = 0.25



### **Example**: 2D Bayes Classifier

- 17 samples of grass
- 15 samples of sky





Image Credit: Ioannis (Yannis) Gkioulekas (CMU)





# **Example**: 2D Bayes Classifier **Green** color channel value • 17 samples of grass 15 samples of sky 0 Given a (g,b) pixel value from a new patch is it more likely to be be grass or sky? These could be (g,b) pixel value of an image patch with sky



These could be (g,b) pixel value of an image patch with grass







### **Example**: 2D Bayes Classifier

• 17 samples of grass • 15 samples of sky

$$p(blue) = \frac{17}{17 + 15}$$

$$p(green) = \frac{15}{17 + 15}$$





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### **Example**: 2D Bayes Classifier

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# **Example**: 2D Bayes Classifier $p(green| \Delta)$

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#### **Bayes** Rule (Review and Definitions)

Let c be the **class label** and let x be the **measurement** (i.e., evidence)

#### Simple case:

- binary classification; i.e.,  $c \in \{1, 2\}$
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#### **General** case:

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## Bayes' Risk

# Some errors may be inevitable: the minimum risk (shaded area) is called the **Bayes' risk**



Forsyth & Ponce (2nd ed.) Figure 15.1



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Forsyth & Ponce (2nd ed.) Figure 15.1

### Loss Functions and Classifiers

#### Loss

- Some errors may be more expensive than others
   **Example**: A fatal disease that is easily cured by a cheap medicine with no side-effects. Here, false positives in diagnosis are better than false negatives
- We discuss two class classification:  $L(1 \rightarrow 2)$  is the loss caused by calling 1 a 2
- Total risk of using classifier s is

$$R(s) = Pr\{1 \rightarrow 2 \mid using s\} L(1)$$

Probability of Miss-classification

Loss (i.e. cost of miss-classification)

#### $\rightarrow$ 2) + Pr{2 $\rightarrow$ 1 | using **s**} L(2 $\rightarrow$ 1)

Probability of Miss-classification

Loss (i.e. cost of miss-classification)

## Bayes' Risk

# Some errors may be inevitable: the minimum risk (shaded area) is called the **Bayes' risk**



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### Taxonomy of Cats

- → Mammals (Class Mammalia)
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Ocelot [Jitze Couperus]



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[<u>inaturalist.org</u>]<sup>55</sup>

**Training error** is the error a classifier makes on the training set

unseen testing set

error

called **overfitting** 

- We want to minimize the **testing error** the error the classifier makes on an

Classifiers that have small training error may not necessarily have small testing

The phenomenon that causes testing error to be worse than training error is

# **Underfitting**: model is too simple to represent all the relevant class characteristics



**Underfitting**: model is too simple to represent all the relevant class characteristics

**Overfitting**: model is too complex and fits irrelevant characteristics (noise) in the data



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the classifier on the rest of the data and evaluate on the validation set

Try out what hyperparameters work best on test set.



#### We cannot reliably estimate the error rate of the classifier using the training set

# An alternative is to split some training data to form a validation set, then train

the classifier on the rest of the data and evaluate on the validation set

Trying out what hyperparameters work best on test set: Very bad idea. The test set is a proxy for the generalization performance! Use only VERY SPARINGLY, at the end.

#### We cannot reliably estimate the error rate of the classifier using the training set

# An alternative is to split some training data to form a validation set, then train

train data test data

the classifier on the rest of the data and evaluate on the validation set

		train da
fold 1	fold 2	fold 3

#### We cannot reliably estimate the error rate of the classifier using the training set

# An alternative is to split some training data to form a validation set, then train



# **Cross-validation** involves performing multiple splits and averaging the error over all splits



### **Confusion** Matrix

When evaluating a multi-class classifier, it may be useful to know how often certain classes are often misclassified as others.

#### A confusion matrix is a table whose (i,j)th entry is the frequency (or proportion) an item of true class i was labelled as j by the classifier.



Forsyth & Ponce (2nd ed.) Figure 15.3. Original credit: H. Zhang et al., 2006.

### **Classifier** Strategies

parametric.

#### Classification strategies fall under two broad types: parametric and non-

### **Classifier** Strategies

Classification strategies fall under two broad types: parametric and nonparametric.

- Parametric classifiers are **model driven**. The parameters of the model are model.
- fast, compact
- flexibility and accuracy depend on model assumptions

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### **Classifier** Strategies

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Non-parametric classifiers are **data driven**. New data points are classified by comparing to the training examples directly. "The data is the model". - slow

highly flexible decision boundaries

## **Nearest Neighbor** Classifier

space.

Ο O  $\mathbf{O}$ 0 0 OC 0 0 0

#### Given a new data point, assign the label of nearest training example in feature



Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

## **Nearest Neighbor** Classifier

space.

#### Given a new data point, assign the label of nearest training example in feature



Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

## k-Nearest Neighbor (kNN) Classifier

by majority vote.

various dimensions

minimizing probability of error

- We can gain some robustness to noise by voting over **multiple** neighbours.
- Given a **new** data point, find the k nearest training examples. Assign the label

Simple method that works well if the **distance measure** correctly weights the

For **large data sets**, as k increases kNN approaches optimality in terms of

## k-Nearest Neighbor (kNN) Classifier

1-Nearest Neighbor Classifier



15-Nearest Neighbor Classifier

kNN decision boundaries respond to local clusters where one class dominates

Figure credit: Hastie, Tibshirani & Friedman (2nd ed.)
### **Classifier** Strategies

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- fast, compact
- flexibility and accuracy depend on model assumptions

Non-parametric classifiers are **data driven**. New data points are classified by comparing to the training examples directly. "The data is the model". - slow

highly flexible decision boundaries

- **Idea:** Try to obtain the decision boundary directly
- The decision boundary is parameterized as a **separating hyperplane** in feature space.
- e.g. a separating line in 2D
- We choose the hyperplane that is as far as possible from each class that maximizes the distance to the closest point from either class.



### Linear Classifier

Defines a score function:



### Linear Classifier

### Example with an image with 4 pixels, and 3 classes (cat/dog/ship)

stretch pixels into single column

0.2	-0.5	0.1	2.	
1.5	1.3	2.1	0.0	
0	0.25	0.2	-0.	

W



input image







What's the best w?

O O 



What's the best w?





What's the best w?



What's the best w?



What's the best w?







What's the best w?





from all interior points

What's the best w?





Want a hyperplane that is far away from 'inner points'

Find hyperplane w such that ...



### Image Classification

- **Classification** Algorithms
- Bayes' Classifier
- Nearest Neighbor Classifier
- SVM Classifier

- Representation of Images
- Image pixels directly
- Bag of Words



### Visual Words

# Many algorithms for image classification accumulate evidence on the basis of **visual words**.

To classify a text document (e.g. as an article on sports, entertainment, business, politics) we might find patterns in the occurrences of certain words.

### Vector Space Model

### G. Salton. 'Mathematics and Information Retrieval' Journal of Documentation, 1979





University of Southern the ankle. California, MIT and

Mellon University. Park, software, made it possible in li working with collaborators for the robotic device to its at Harvard University, the achieve natural motions in beh CON

Tartan

http://www.fodey.com/generators/newspaper/snippet.asp



1	6	2	1	0	0	0	1
Tartan	robot	CHIMP	CMU	bio	soft	ankle	sensor



### Vector Space Model

### A document (datapoint) is a vector of counts over each word (feature)

 $n(\cdot)$  counts the number of occurrences just a histogram over words

### What is the similarity between two documents?

 $\boldsymbol{v}_d = [n(w_{1,d}) \ n(w_{2,d}) \ \cdots \ n(w_{T,d})]$ 





### Vector Space Model

### A document (datapoint) is a vector of counts over each word (feature)

 $n(\cdot)$  counts the number of occurrences

### What is the similarity between two documents?

Use any distance you want but the cosine distance is fast and well designed for high-dimensional vector spaces:

$$egin{aligned} d(oldsymbol{v}_i,oldsymbol{v}_j) &= \cos heta \ &= rac{oldsymbol{v}_i \cdot oldsymbol{v}_i}{\|oldsymbol{v}_i\|} \end{aligned}$$

 $oldsymbol{v}_d = [n(w_{1,d}) \quad n(w_{2,d}) \quad \cdots \quad n(w_{T,d})]$ 

just a histogram over words









### Visual Words

patch is described using a descriptor such as SIFT.

We construct a vocabulary or codebook of local descriptors, containing representative local descriptors.

# In images, the equivalent of a **word** is a **local image patch**. The local image

## What **Objects** do These Parts Belong To?









0.40























### Some local feature are very informative

### An object as





- deals well with occlusion
- scale invariant
- rotation invariant

### (not so) Crazy Assumption



### spatial information of local features can be ignored for object recognition (i.e., verification)

### **Recall:** Texture Representation













### Standard **Bag-of-Words** Pipeline (for image classification)

**Dictionary Learning**: Learn Visual Words using clustering

**Encode**: build Bags-of-Words (BOW) vectors for each image

**Classify**: Train and test data using BOWs

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## 1. Dictionary Learning: Learn Visual Words using Clustering

1. Extract features (e.g., SIFT) from images









## 1. Dictionary Learning: Learn Visual Words using Clustering

2. Learn visual dictionary (e.g., K-means clustering)





## What **Features** Should We Extract?

- Regular grid Vogel & Schiele, 2003 Fei-Fei & Perona, 2005
- Interest point detector Csurka et al. 2004 Fei-Fei & Perona, 2005 Sivic et al. 2005
- Other methods Random sampling (Vidal-Naquet & Ullman, 2002) Segmentation-based patches (Barnard et al. 2003)



## Extracting SIFT Patches



### **Compute SIFT** descriptor

[Lowe'99]

Normalize patch



### **Detect patches**

[Mikojaczyk and Schmid '02] [Mata, Chum, Urban & Pajdla, '02] [Sivic & Zisserman, '03]

### Extracting SIFT Patches







## Creating **Dictionary**



## Creating **Dictionary**





## Creating **Dictionary**





## K-means clustering

### **K-Means** Clustering

Assume we **know** how many clusters there are in the data - denote by K

Each **cluster** is represented by a **cluster center**, or mean

in letting each data point be represented by some cluster center

Minimize



# Our objective is to minimize the representation error (or quantization error)

$$\sum_{h \ cluster} ||x_j - \mu_i||^2 \bigg\}$$

## **K-Means** Clustering

**K-means** clustering alternates between two steps:

- **1**. Assume the cluster centers are known (fixed). Assign each point to the closest cluster center.
- **2.** Assume the assignment of points to clusters is known (fixed). to the cluster.
- The algorithm is initialized by choosing K random cluster centers
- K-means converges to a local minimum of the objective function Results are initialization dependent

Compute the best center for each cluster, as the mean of the points assigned


**True Clusters** 



















## Example Visual Dictionary







Source: B. Leibe

## Example Visual Dictionary





Source: B. Leibe

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## 2. Encode: build Bag-of-Words (BOW) vectors for each image



### 1. Quantization: image features gets associated to a visual word (nearest cluster center)













## 2. Encode: build Bag-of-Words (BOW) vectors for each image

### 2. Histogram: count the number of visual word occurrences







## 2. Encode: build Bag-of-Words (BOW) vectors for each image







frequency

codewords





## Standard **Bag-of-Words** Pipeline (for image classification)

**Classify**: Train and test data using BOWs

**Dictionary Learning:** Learn Visual Words using clustering

Encode: build Bags-of-Words (BOW) vectors for each image

## **3. Classify:** Train and text classifier using BOWs



### K nearest neighbors



