

THE UNIVERSITY OF BRITISH COLUMBIA

CPSC 425: Computer Vision



Lecture 24: Clustering (cont)

Recall: Pareidolia





Photo credit: reddit user Liammm



Today's "fun" Example: Deep Dream — Algorithmic Pareidolia





Menu for Today (April 2nd, 2019)

Topics:

- Grouping
- Image Segmentation

Redings:

— **Today's** Lecture: Forsyth & Ponce (2nd ed.) 15.1, 15.2, 17.2 Introduction to Deep Learning - **Next** Lecture: Convolutional Neural Networks

Reminders:

- Assignment 5: Scene Recognition with Bag of Words due April 4th
- Some practice problems posted on Piazza, some more to come



Agglomerative Clustering with a Graph - Classification



Lecture 23: Re-cap

Detection scores in the **deformable part model** are based on both appearance and location

The **deformable part model** is trained iteratively by alternating the steps

- offset models
- 2. Assume appearance and offset models given; compute components and part locations

exhaustive sliding window search

1. Assume components and part locations given; compute appearance and

An **object proposal** algorithm generates a short list of regions with generic object-like properties that can be evaluated by an object detector in place of an

Lecture 23: Re-cap Agglomerative Clustering

Each data point starts as a separate cluster. Clusters are recursively merged.

Algorithm:

Make each point a separate cluster Until the clustering is satisfactory Merge the two clusters with the smallest inter-cluster distance end

The entire data set starts as a single cluster. Clusters are recursively split.

Algorithm:

Construct a single cluster containing all points Until the clustering is satisfactory Split the cluster that yields the two components with the largest inter-cluster distance end

- agglomerative and divisive clustering? Some common options:
- the distance between the closest members of C_1 and C_2
 - $\min d(a, b), a \in C_1, b \in C_2$
- single-link clustering
- the distance between the farthest members of C_1 and a member of C_2

 $\max d(a, b), a \in C_1, b \in C_2$

– complete-link clustering

How can we define the cluster distance between two clusters C_1 and C_2 in

How can we define the cluster distance between two clusters C_1 and C_2 in agglomerative and divisive clustering? Some common options:

an average of distances between members of C_1 and C_2

group average clustering

 $\frac{1}{|C_1||C_2|} \sum_{a \in C_1} \sum_{b \in C_2} d(a,b)$

The algorithms described generate a hierarchy of clusters, which can be visualized with a **dendrogram**.





Forsyth & Ponce (2nd ed.) Figure 9.15

A simple dataset is shown below. Draw the dendrogram obtained by



С

A simple dataset is shown below. Draw the dendrogram obtained by



С

agglomerative clustering with single-link (closest member) inter-cluster distance.

A B C D E

A simple dataset is shown below. Draw the dendrogram obtained by

A B

agglomerative clustering with single-link (closest member) inter-cluster distance.



Ε

С

A simple dataset is shown below. Draw the dendrogram obtained by

А R



C



A simple dataset is shown below. Draw the dendrogram obtained by

А





A simple dataset is shown below. Draw the dendrogram obtained by

А





K-Means Clustering

Assume we know how many clusters there are in the data - denote by K

Each cluster is represented by a cluster center, or mean

letting each data point be represented by some cluster center

Minimize



- Our objective is to minimize the representation error (or quantization error) in

$$\sum_{h \ cluster} ||x_j - \mu_i||^2 \bigg\}$$

K-Means Clustering

K-means clustering alternates between two steps:

- **1**. Assume the cluster centers are known (fixed). Assign each point to the closest cluster center.
- **2.** Assume the assignment of points to clusters is known (fixed). to the cluster.
- The algorithm is initialized by choosing K random cluster centers
- K-means converges to a local minimum of the objective function Results are initialization dependent

Compute the best center for each cluster, as the mean of the points assigned



True Clusters

Example 2: Mixed Vegetables

Original Image

K-means using colour alone, 11 segments

Segmentation Using Colour

Example 2: Mixed Vegetables

K-means using colour alone, 11 segments

Forsyth & Ponce (2nd ed.) Figure 9.18

25

Example 2: Mixed Vegetables

K-means using colour alone, 20 segments

Forsyth & Ponce (2nd ed.) Figure 9.19

26

An **Exercise**

Sketch an example of a 2D dataset for which agglomerative clustering performs well (finds the two true clusters) but K-means clustering fails.

Sketch an example of a 2D dataset for which agglomerative clustering performs well (finds the two true clusters) but K-means clustering fails.

Discussion of K-Means

Advantages:

- Algorithm always converges
- Easy to implement

Disadvantages:

- The number of classes, K, needs to be given as input
- Algorithm doesn't always converge to the (globally) optimal solution
- Limited to compact/spherical clusters

to be given as input to the (globally) optimal solution ters

Segmentation by Clustering

but segmentation typically makes use of a richer set of features.

- texture
- corners, lines, ...
- geometry (size, orientation, ...)

We just saw a simple example of segmentation based on colour and position,

- Suppose we represent an image as a weighted graph.
- Any pixels that are **neighbours** are connected by an edge.
- Each edge has a weight that measures the similarity between the pixels — can be based on colour, texture, etc.
- low weights \rightarrow similar, high weights \rightarrow different
- We will segment the image by performing an agglomerative clustering guided by this graph.

Recall that we need to define the inter-cluster distance for agglomerative clustering. Let

We also need to determine when to stop merging.

$d(C_1, C_2) = \min_{v_1 \in C_1, v_2 \in C_2, (v_1, v_2) \in \epsilon} w(v_1, v_2)$

Denote the 'internal difference' of a cluster as the largest weight in the minimum spanning tree of the cluster, M(C):

 $int(C) = \max_{e \in M(C)} w(e)$

Denote the 'internal difference' of a cluster as the largest weight in the minimum spanning tree of the cluster, M(C):

This is not going to work for small clusters: $int(C) + \tau(C)$

 $int(C) = \max_{e \in M(C)} w(e)$

Algorithm: (Felzenszwalb and Huttenlocher, 2004)

Make each point a separate cluster. For i = 1 to rIf both ends of e_i lie in the same cluster Do nothing Else

If $d(C_l, C_m) \leq MInt(C_l, C_m)$

Report the remaining set of clusters.

- Sort edges in order of non-decreasing weight so that $w(e_1) \ge w(e_2) \ge \cdots \ge w(e_r)$

- One end is in cluster C_l and the other is in cluster C_m
 - Merge C_l and C_m Report the remaining set of clusters.

Image credit: KITTI Vision Benchmark

Summary

To use standard clustering techniques we must define an inter-cluster distance measure

A **dendrogram** visualizes a hierarchical clustering process

K-means is a clustering technique that iterates between

1. Assume the cluster centers are known. Assign each point to the closest cluster center.

2. Assume the assignment of points to clusters is known. Compute the best cluster center for each cluster (as the mean).

K-means clustering is initialization dependent and converges to a local minimum