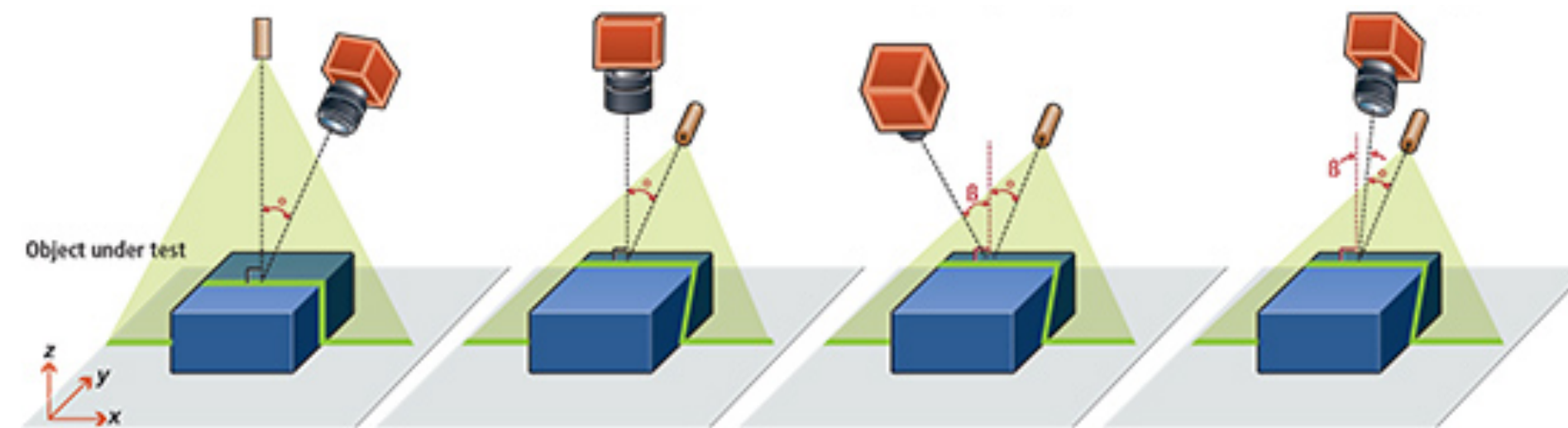


# CPSC 425: Computer Vision



## Lecture 3: Image Formation (continued)

( unless otherwise stated slides are taken or adopted from **Bob Woodham, Jim Little** and **Fred Tung** )

# Menu for Today (September 10, 2018)

## Topics:

- Image Formation
- Cameras and **Lenses**
- Projection
- **Human eye** (as camera)

## Readings:

- **Today's** Lecture: Forsyth & Ponce (2nd ed.) 1.1.1 — 1.1.3
- **Next** Lecture: Forsyth & Ponce (2nd ed.) 4.1, 4.5

## Reminders:

- Complete **Assignment 0** (ungraded) by Wednesday, **September 12**
- **Assignment 1** will be out, **September 12**



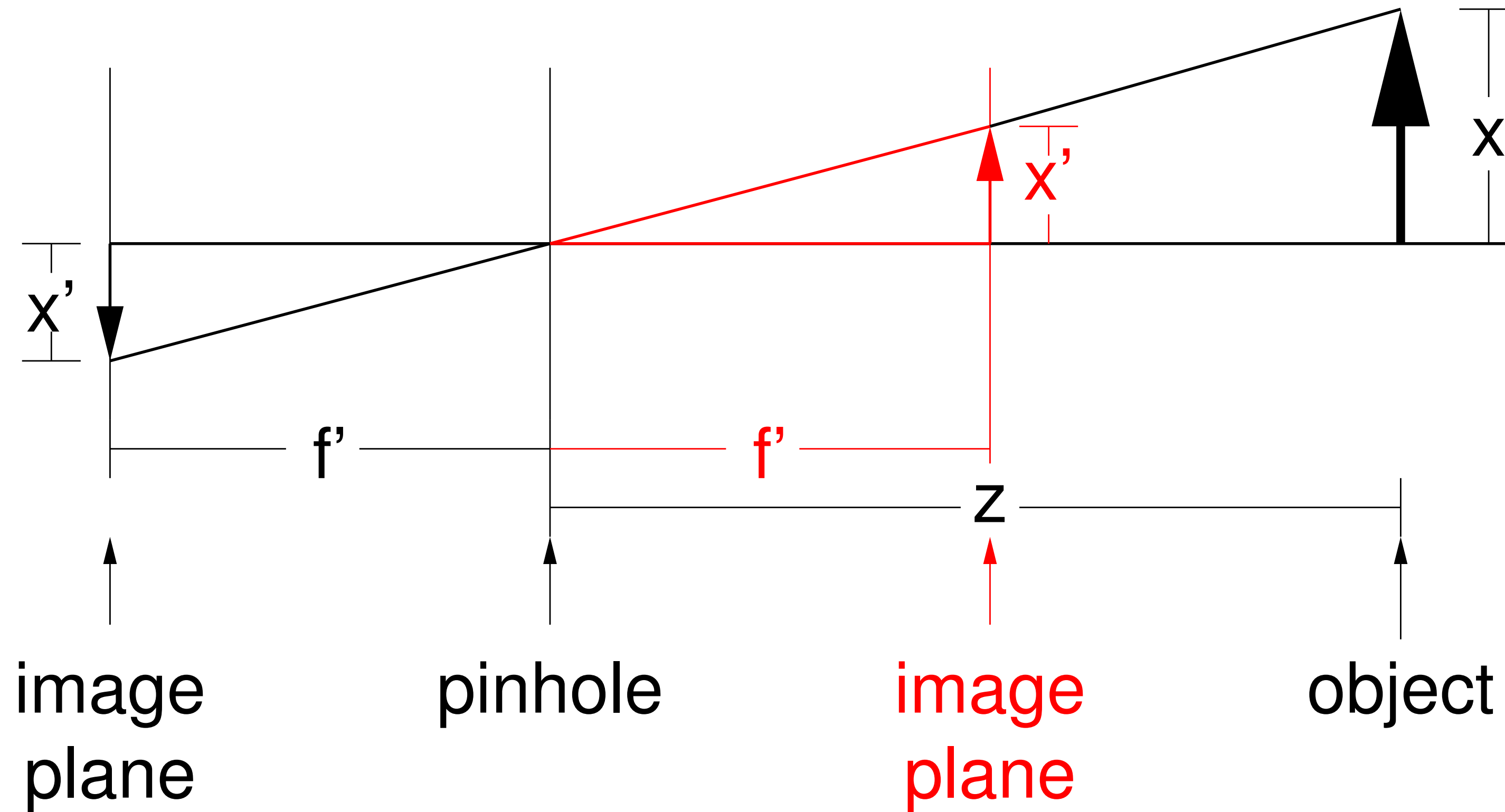
# Today's "fun" Example: **Automimicity**



**Image Credit:** [https://en.wikipedia.org/wiki/File:Peabluet\\_October\\_2007\\_Osaka\\_Japan.jpg](https://en.wikipedia.org/wiki/File:Peabluet_October_2007_Osaka_Japan.jpg)

# Lecture 2: Re-cap

## Pinhole Camera Abstraction



# Lecture 2: Re-cap

3D object point  $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$  projects to 2D image point  $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$  where

Perspective

$$\begin{aligned} x' &= f' \frac{x}{z} \\ y' &= f' \frac{y}{z} \end{aligned}$$

Weak Perspective

$$\begin{aligned} x' &= m x \\ y' &= m y \end{aligned} \quad m = \frac{f'}{z_0}$$

Orthographic

$$\begin{aligned} x' &= x \\ y' &= y \end{aligned}$$

# Projection Models: Pros and Cons

**Weak perspective** (including orthographic) has simpler mathematics

- accurate when object is small and/or distant
- useful for recognition

**Perspective** is more accurate for real scenes

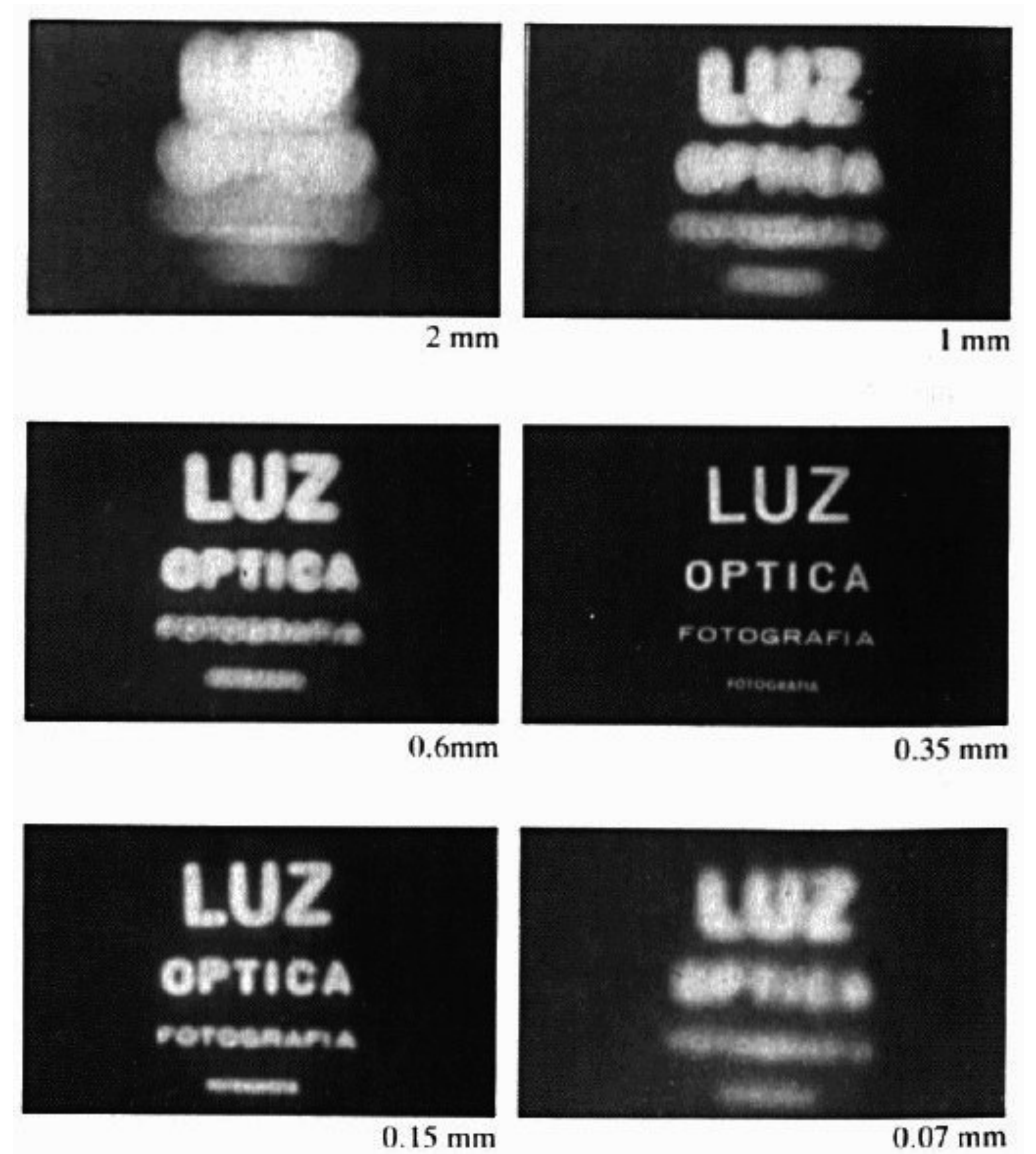
When **maximum accuracy** is required, it is necessary to model additional details of a particular camera

- use perspective projection with additional parameters (e.g., lens distortion)

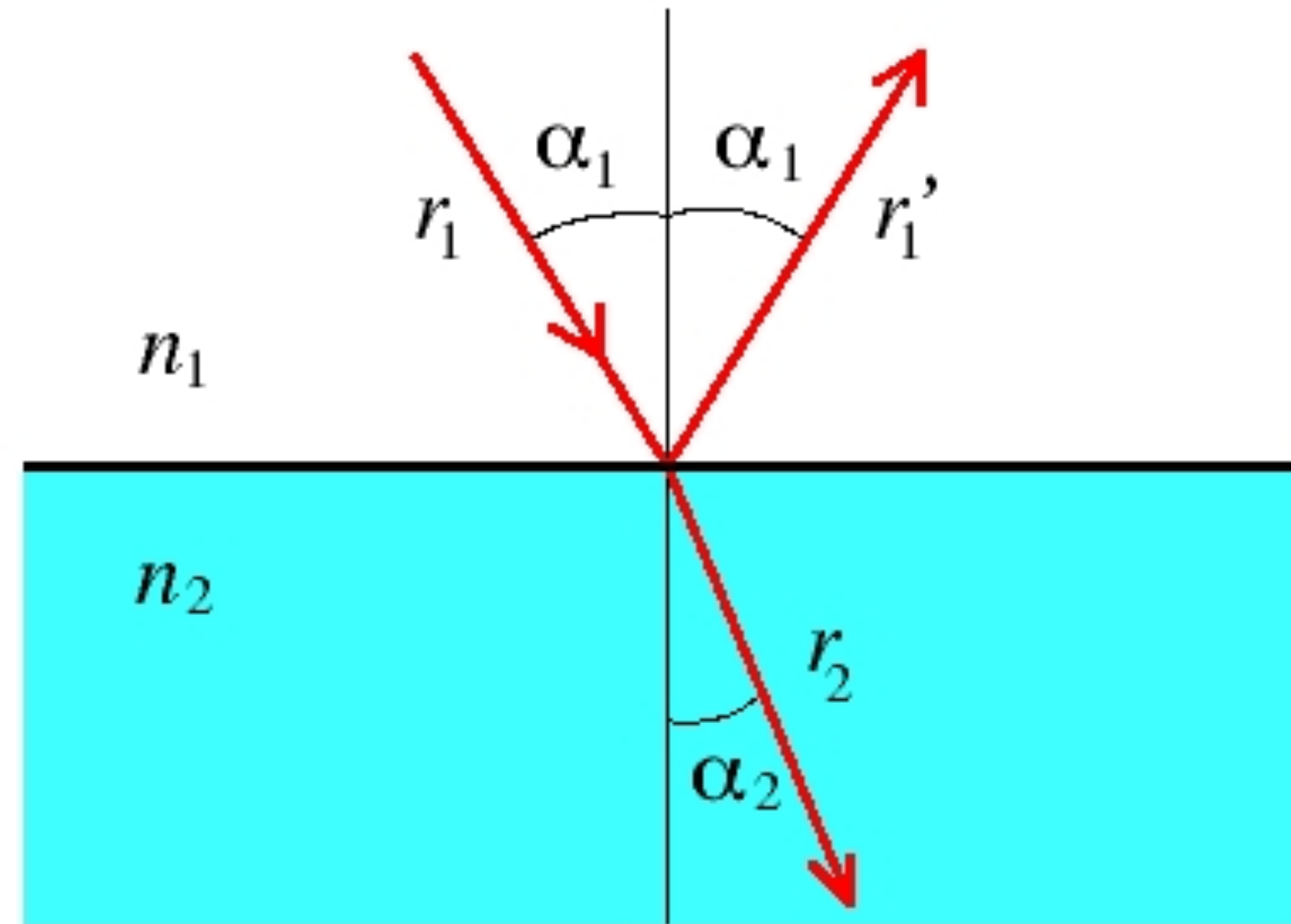


# Why **Not** a Pinhole Camera?

- If pinhole is **too big** then many directions are averaged, blurring the image
- If pinhole is **too small** then diffraction becomes a factor, also blurring the image
- Generally, pinhole cameras are **dark**, because only a very small set of rays from a particular scene point hits the image plane
- Pinhole cameras are **slow**, because only a very small amount of light from a particular scene point hits the image plane per unit time



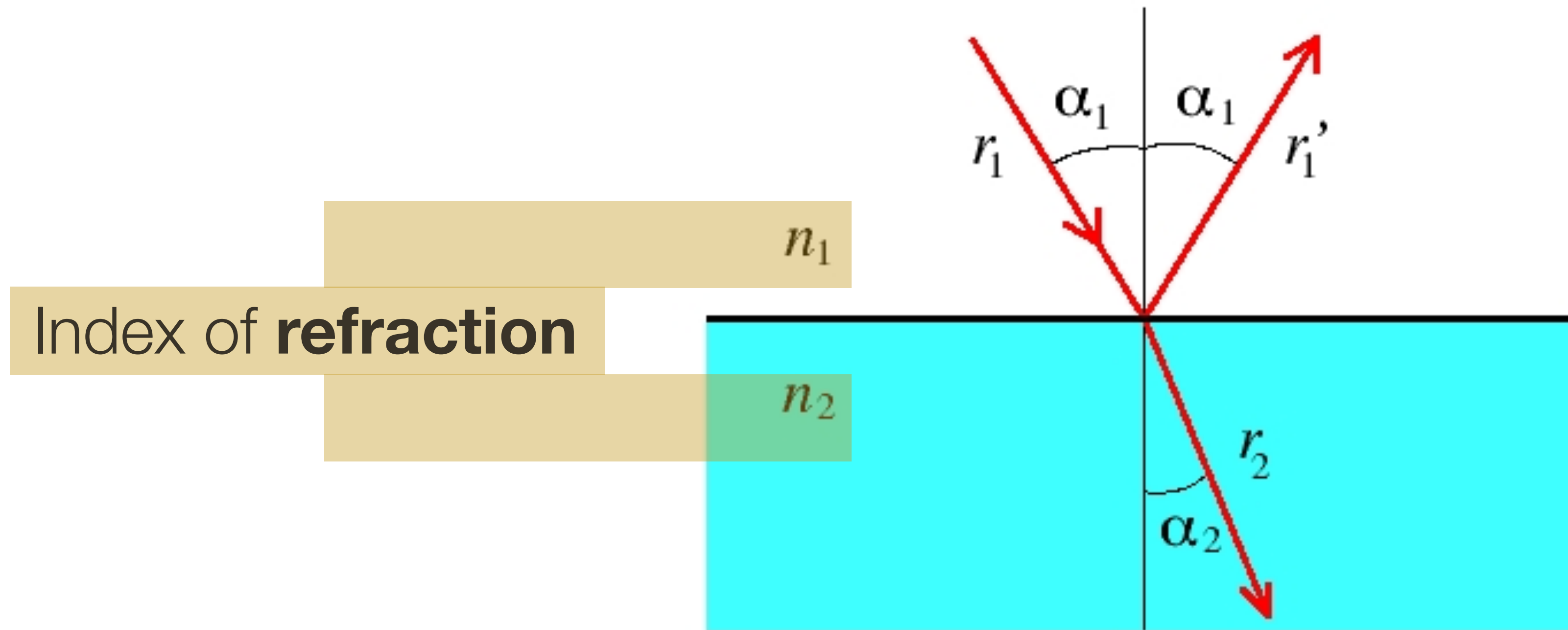
# Snell's Law



$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$



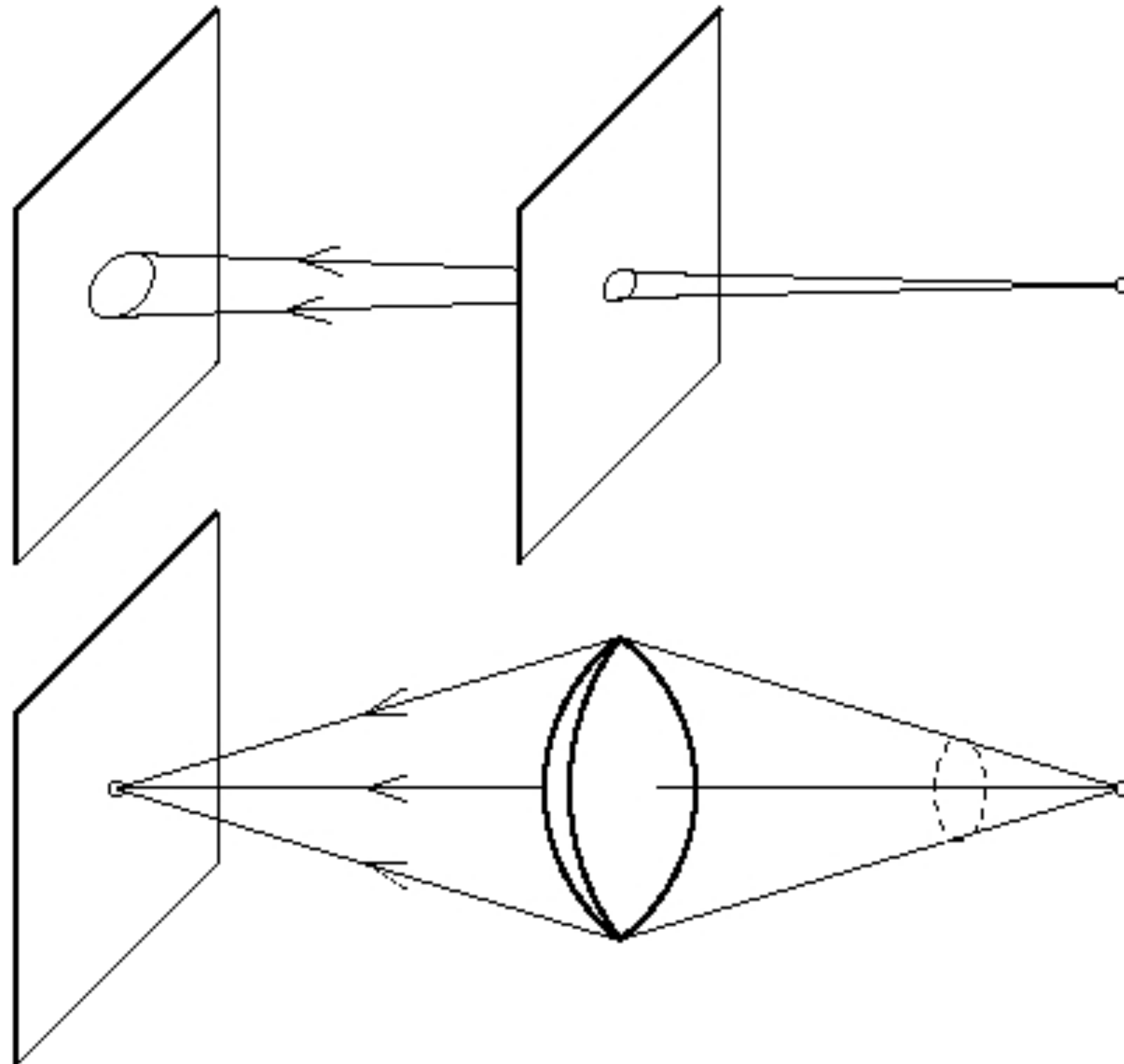
# Snell's Law



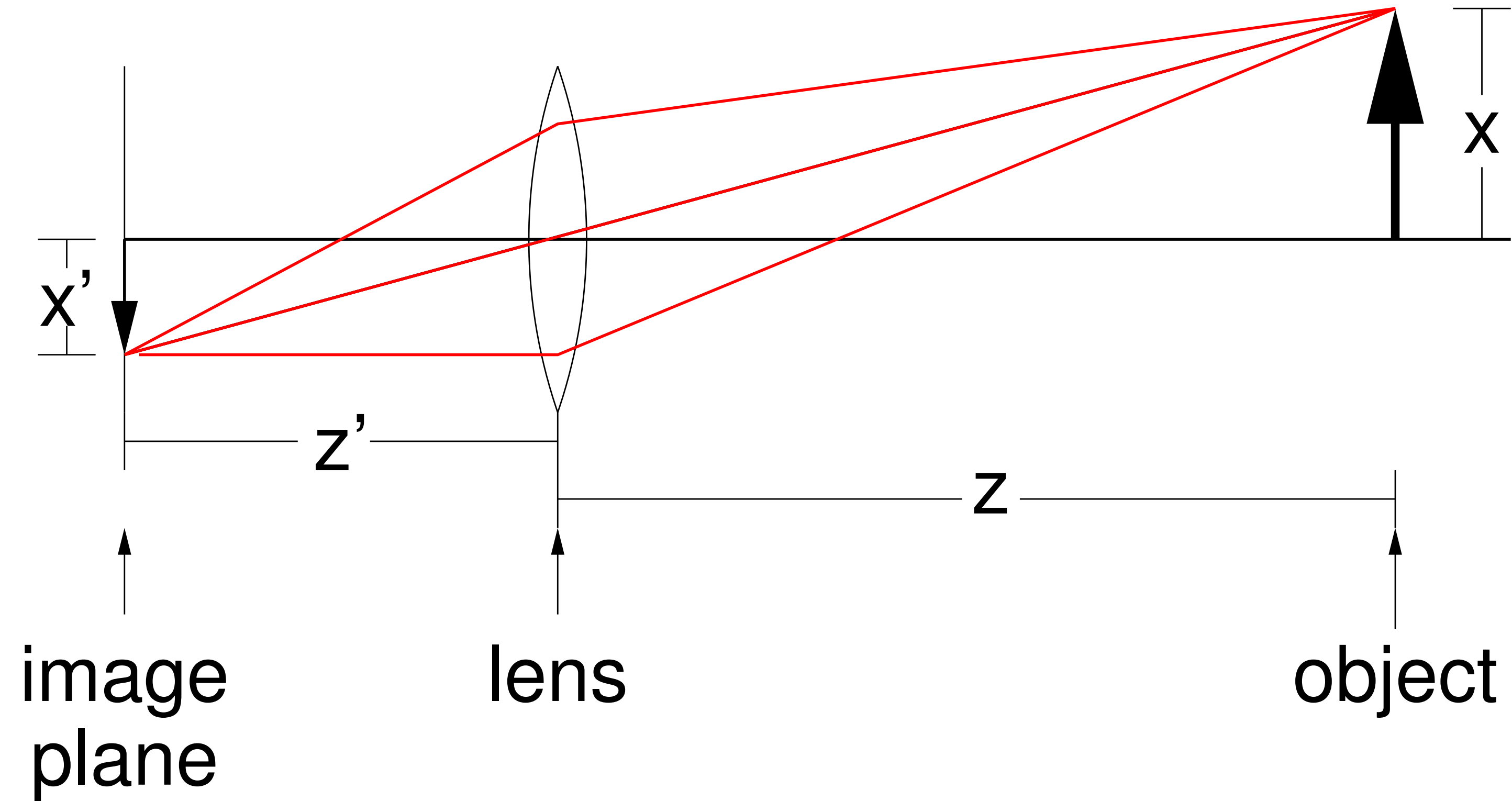
$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

# Reason for **Lenses**

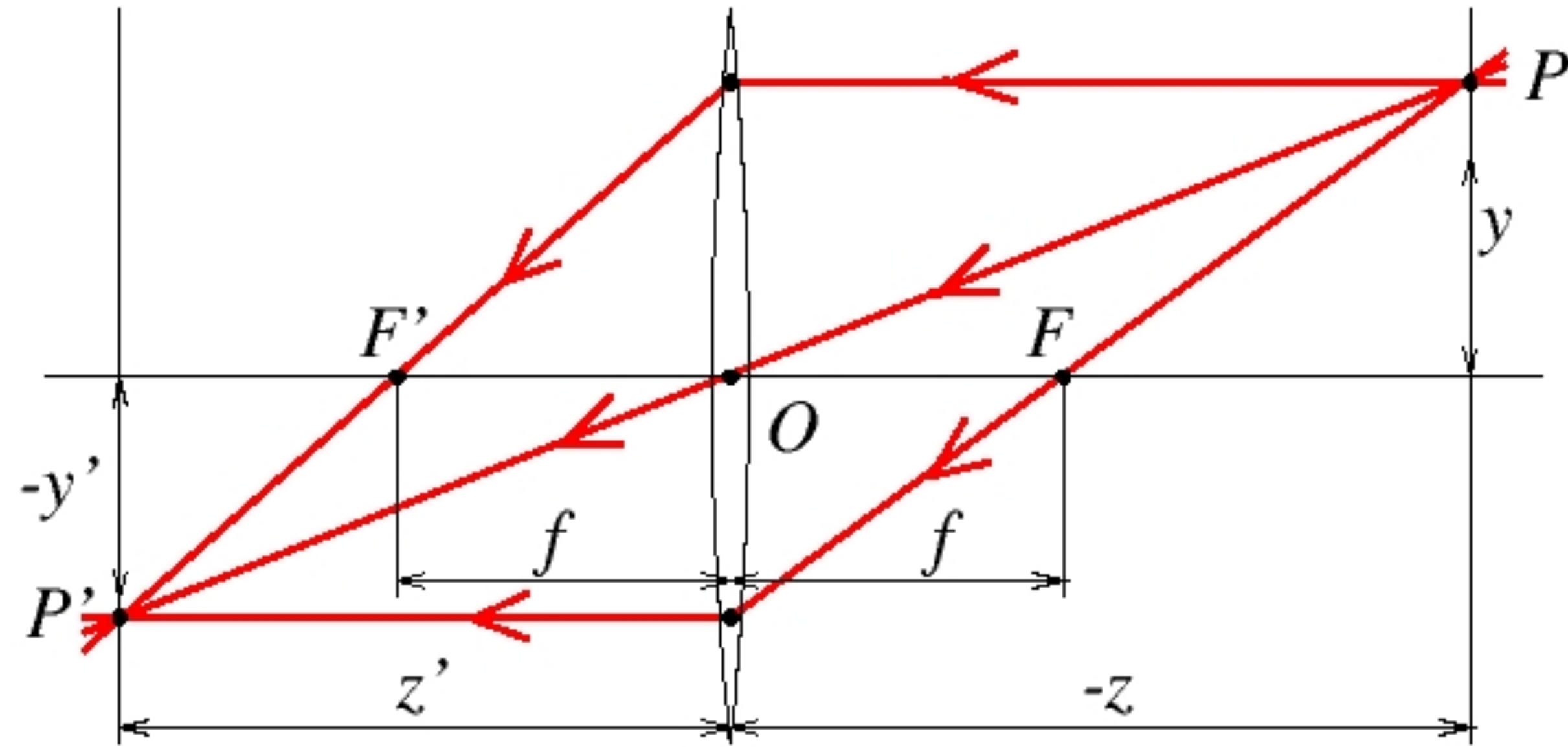
The role of a lens is to **capture more light** while preserving, as much as possible, the abstraction of an ideal pinhole camera.



# Pinhole Model (Simplified) **with Lens**



# Thin Lens Equation



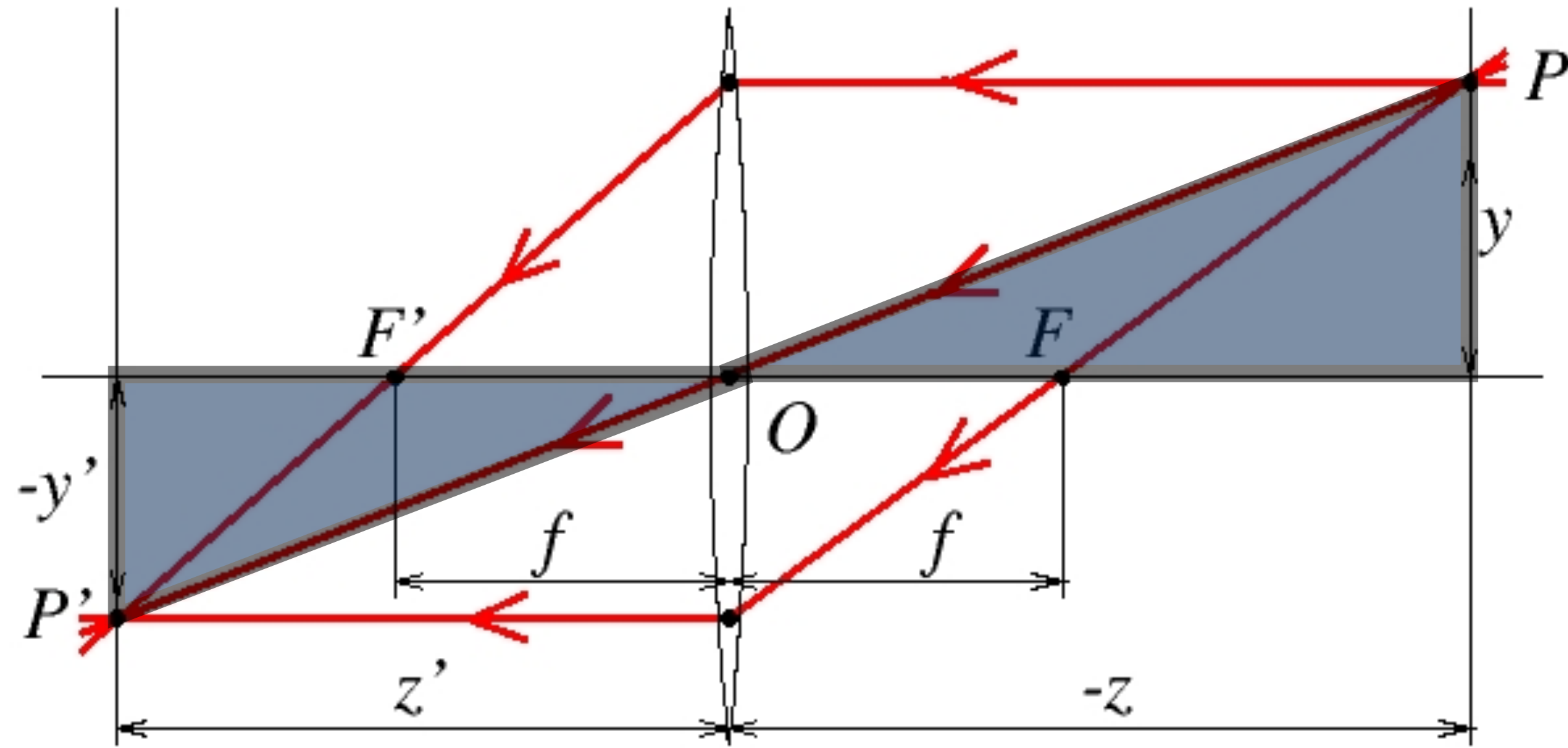
Forsyth & Ponce (1st ed.) Figure 1.9

$$\frac{1}{z'} - \frac{1}{z} = \frac{1}{f}$$



# Thin Lens Equation: Derivation

$$\frac{y}{-z} = \frac{-y'}{z'}$$
$$\frac{y}{y'} = \frac{z}{z'}$$



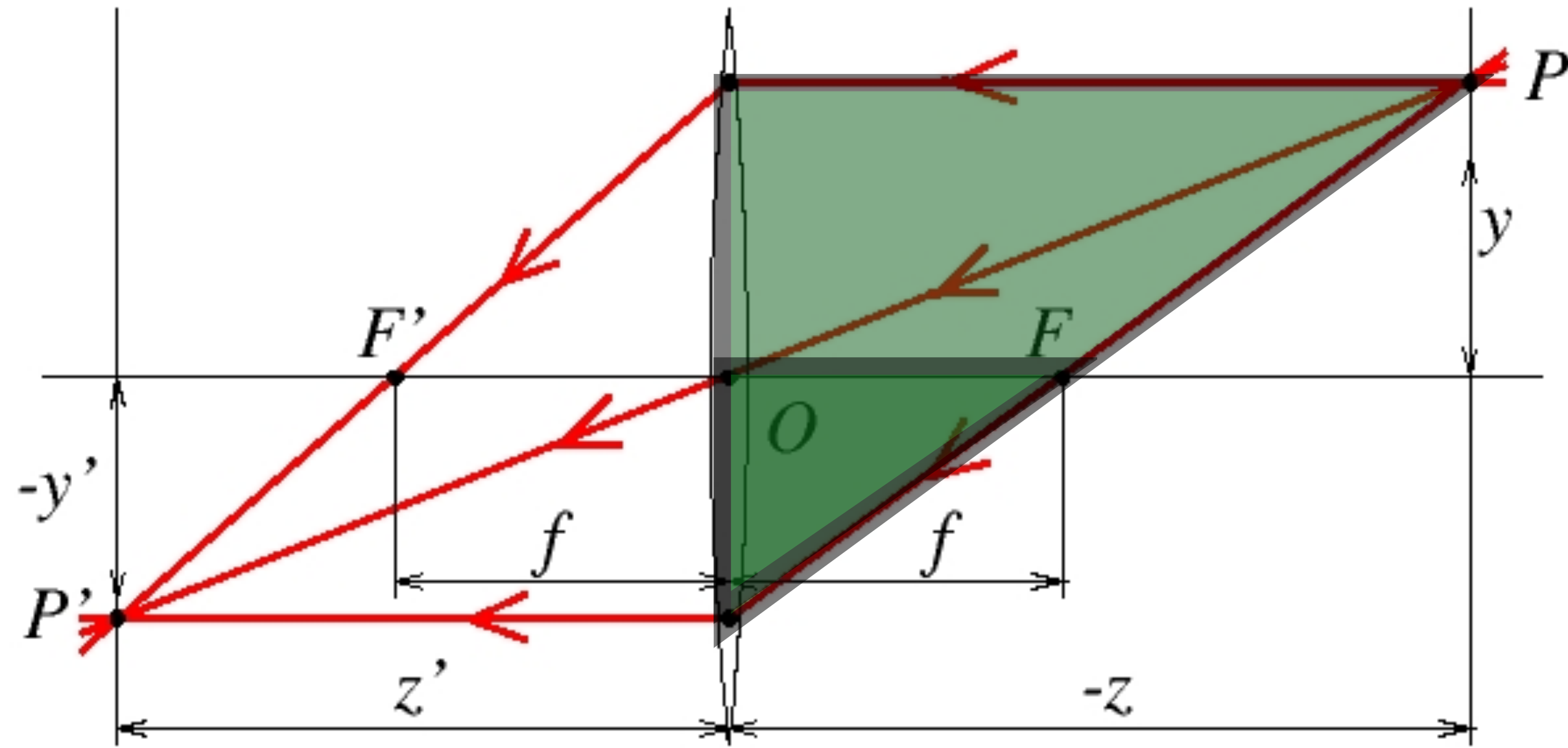
Forsyth & Ponce (1st ed.) Figure 1.9

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Forsyth & Ponce (1st ed.) Figure 1.9

$$\frac{-y'}{f} = \frac{y - y'}{-z}$$

$$\frac{1}{f} = \frac{y - y'}{zy'}$$

$$= \frac{y}{zy'} - \frac{y'}{zy'}$$

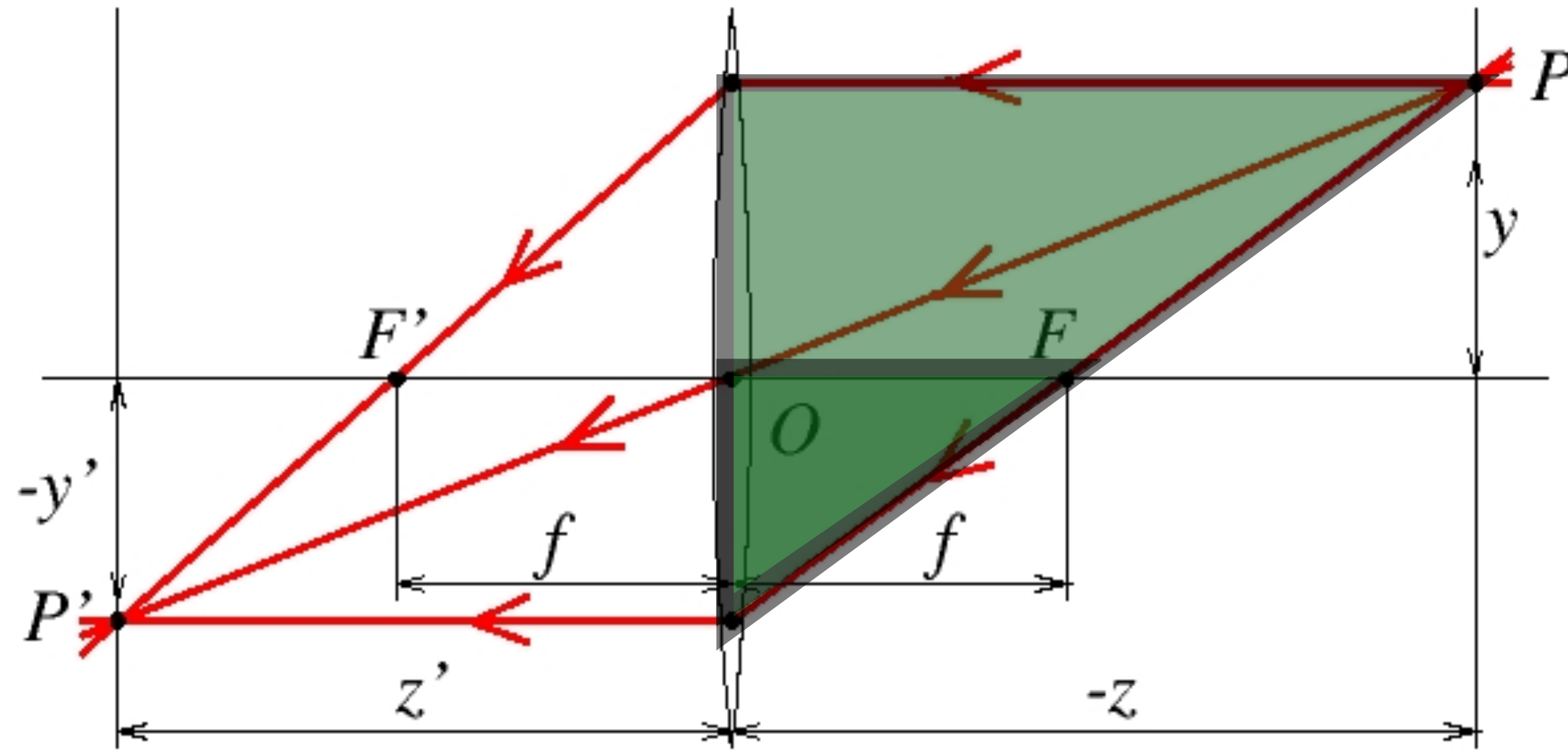
$$= \frac{y}{zy'} - \frac{1}{z}$$

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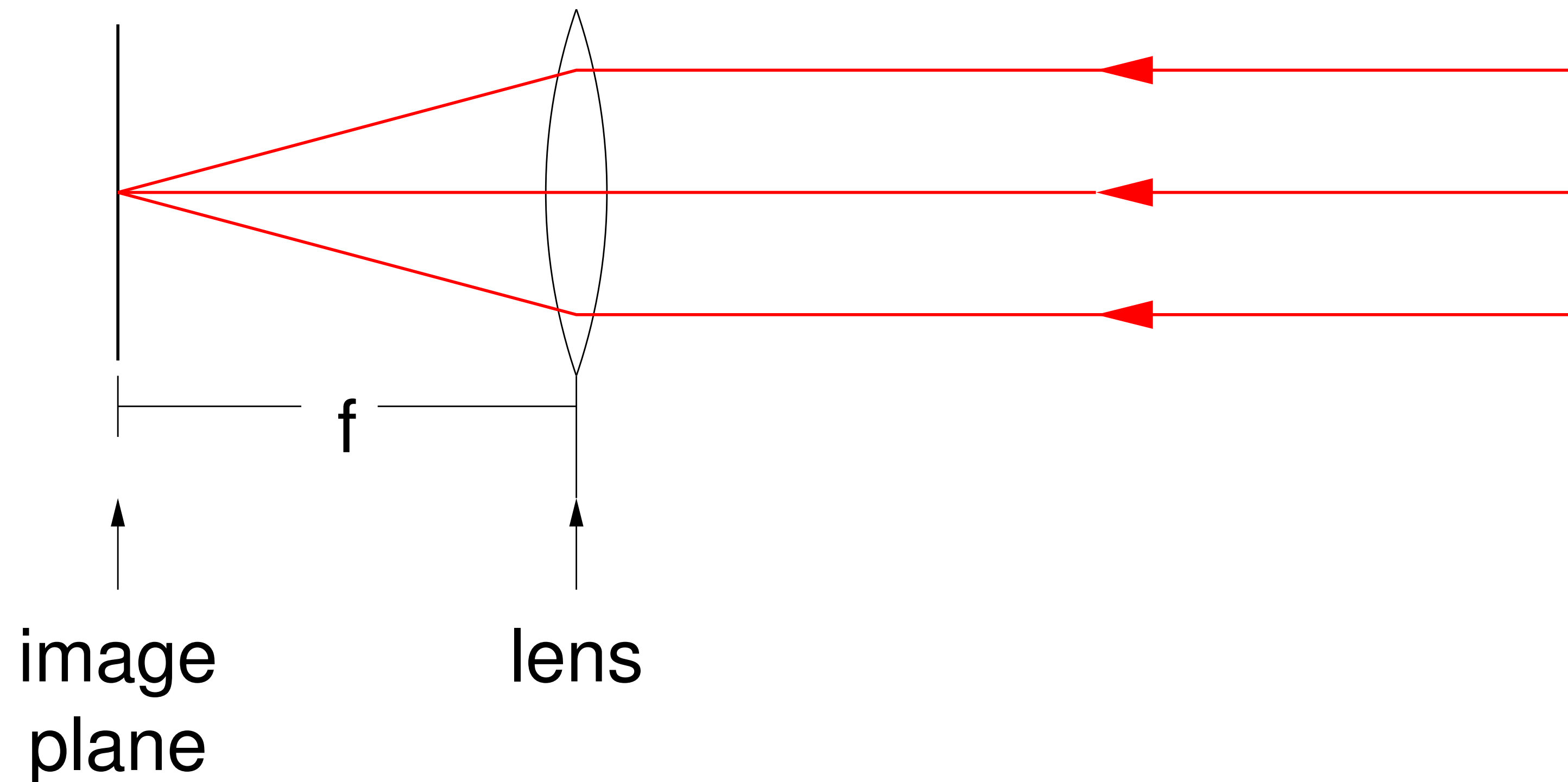
$$= \frac{y}{zy'} - \frac{1}{z}$$

$$\frac{1}{z'} - \frac{1}{z} = \frac{1}{f}$$

Substitute:  $\frac{1}{f} = \frac{1}{z} - \frac{1}{z'}$

# Focal Length

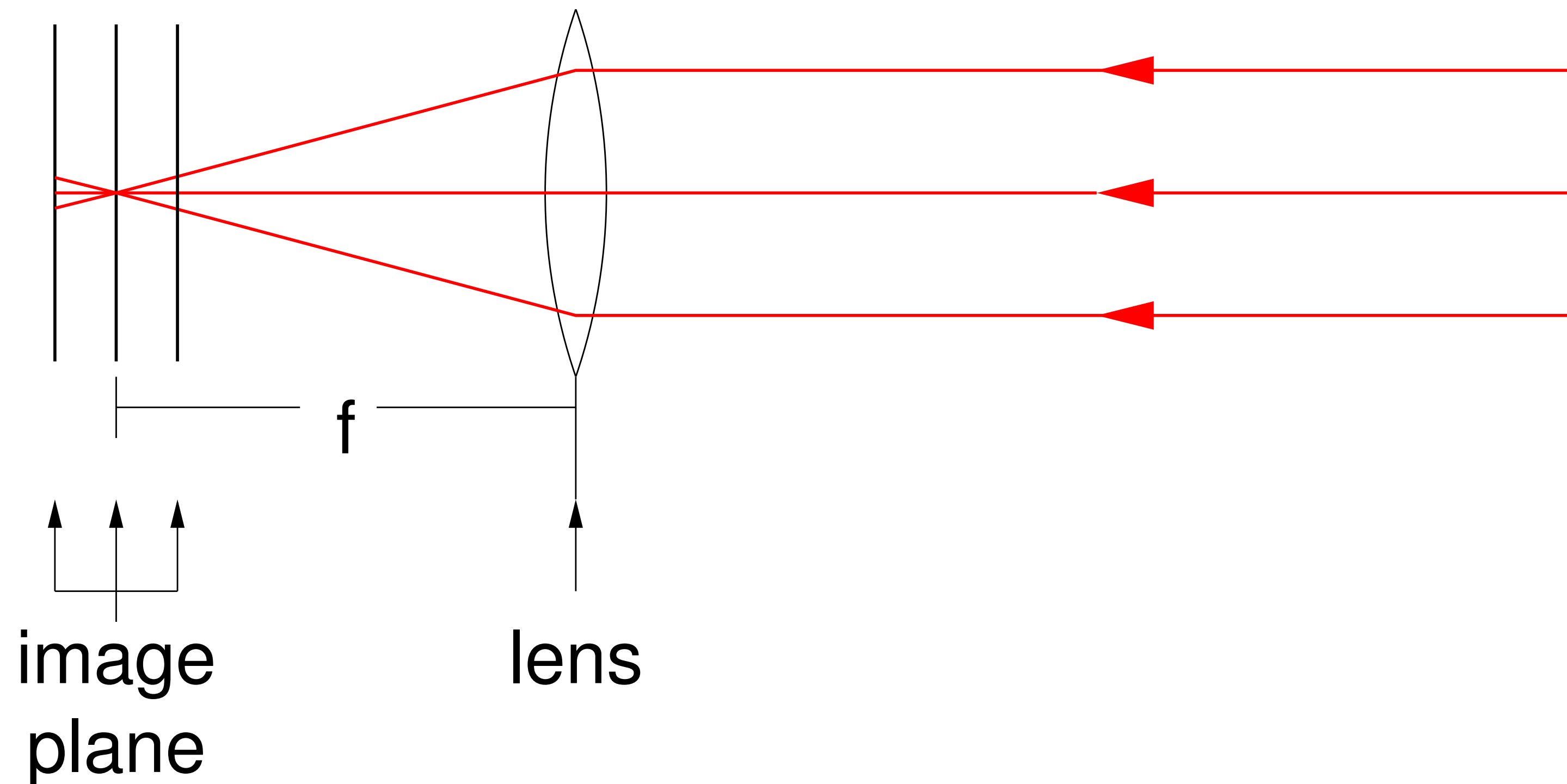
Another way of looking at the **focal length** of a lens. The incoming rays, parallel to the optical axis, **converge to a single point a distance  $f$  behind the lens**. This is where we want to place the image plane.



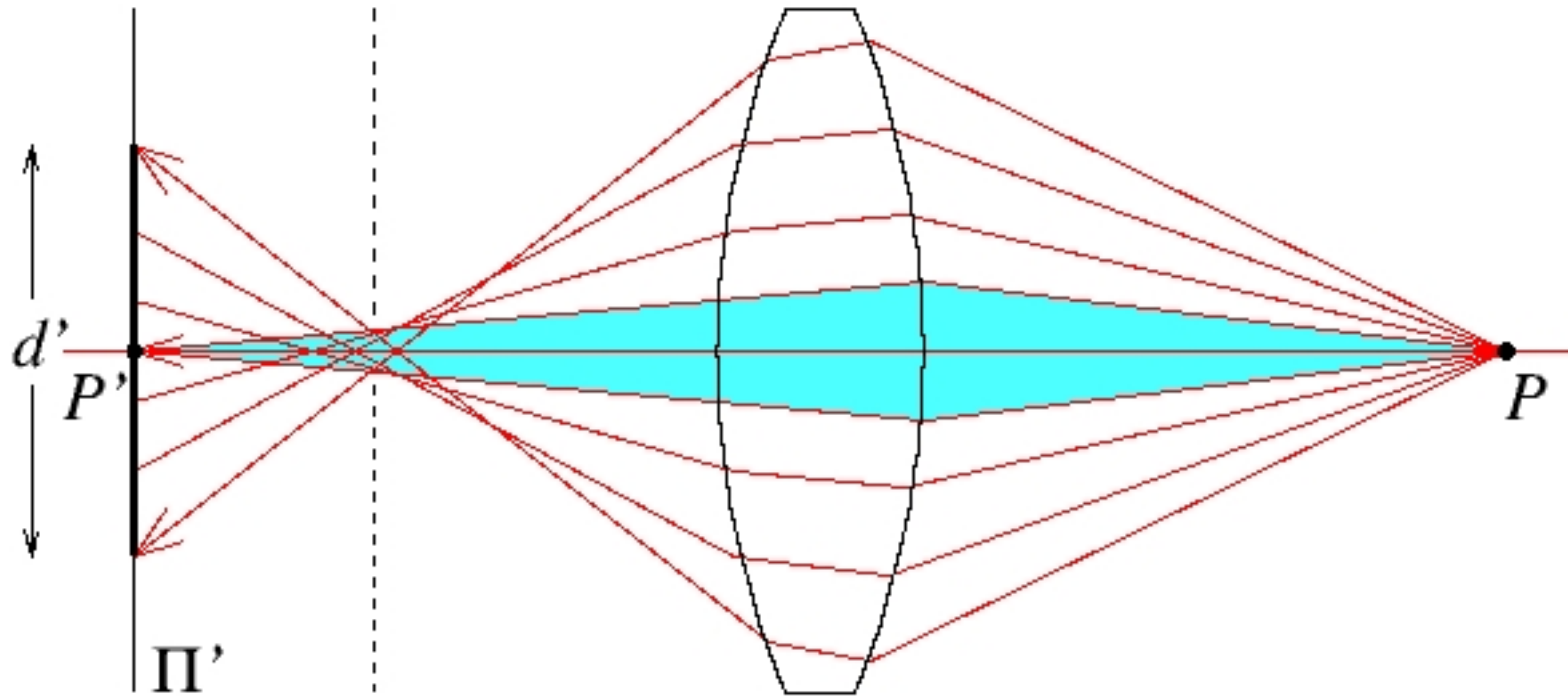


# Out-of-Focus

The image plane is in the wrong place, either slightly closer than the required focal length,  $f$ , or slightly further than the required focal length,  $f$ .

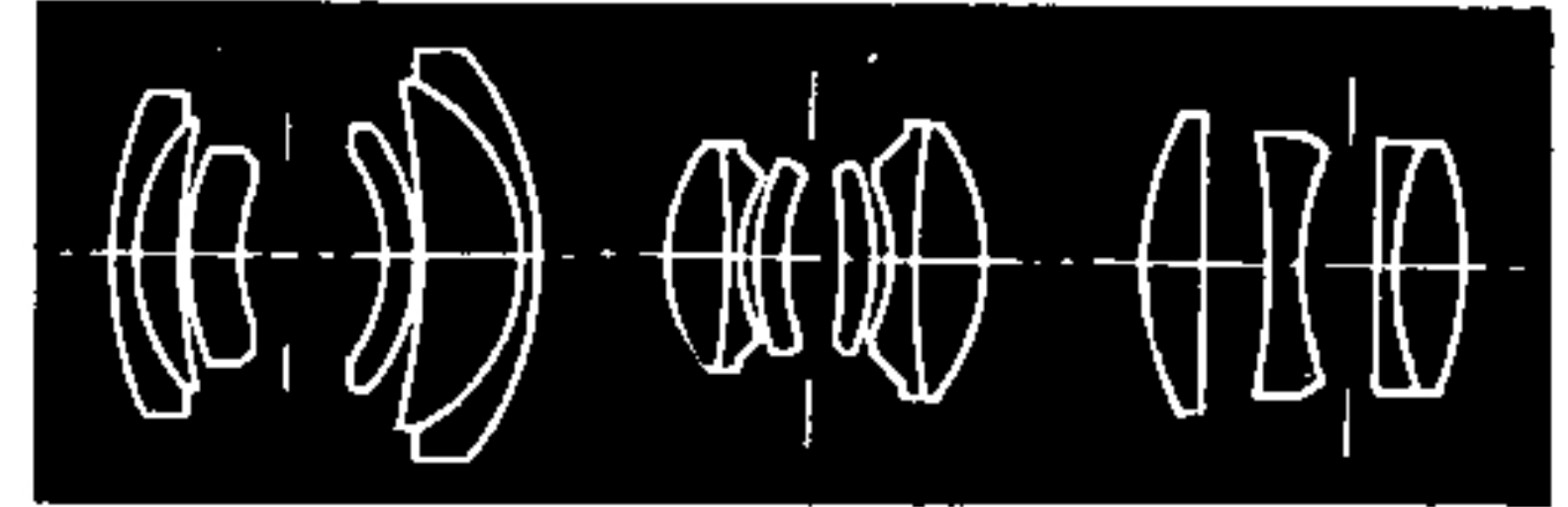
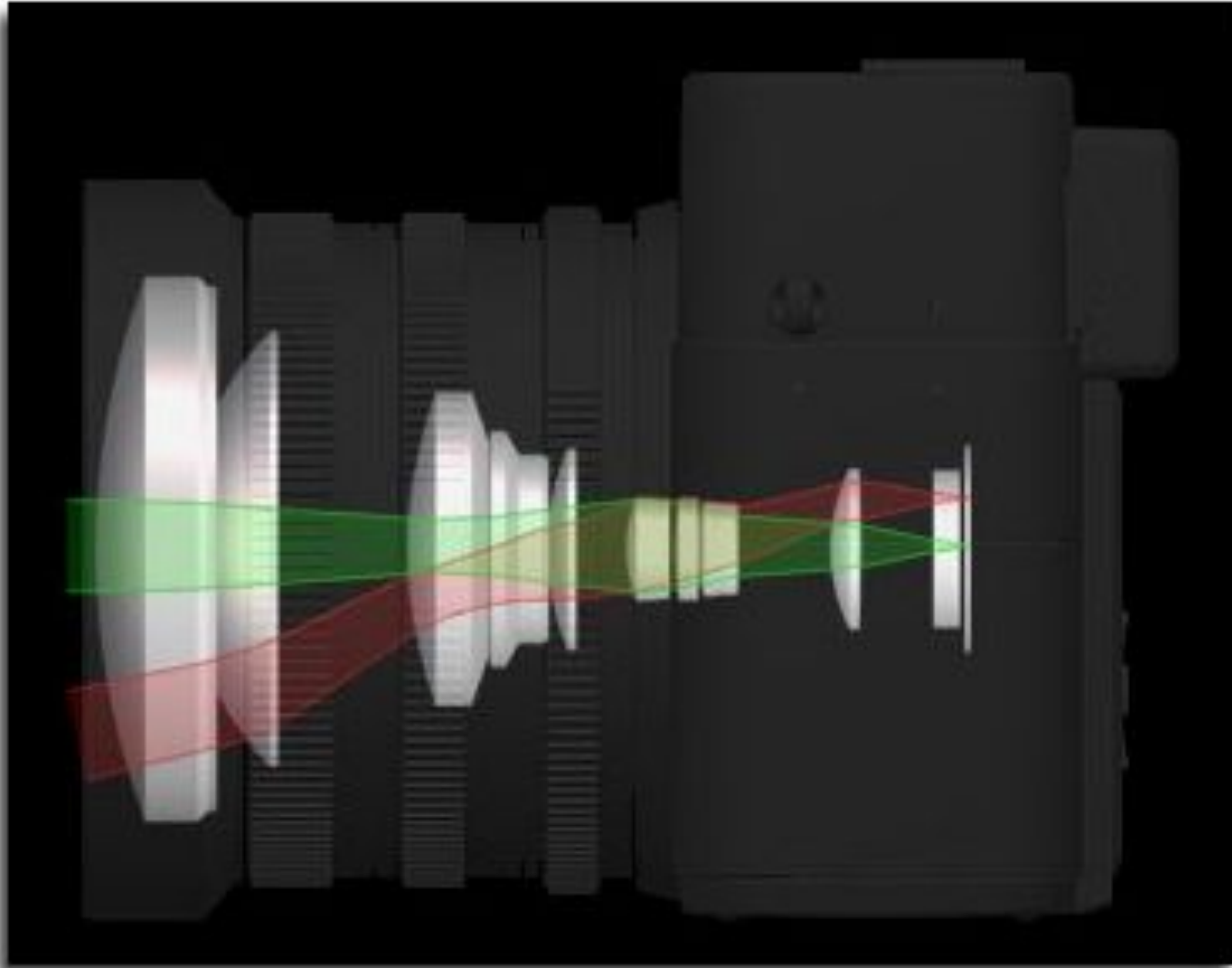


# Spherical Aberration



Forsyth & Ponce (1st ed.) Figure 1.12a

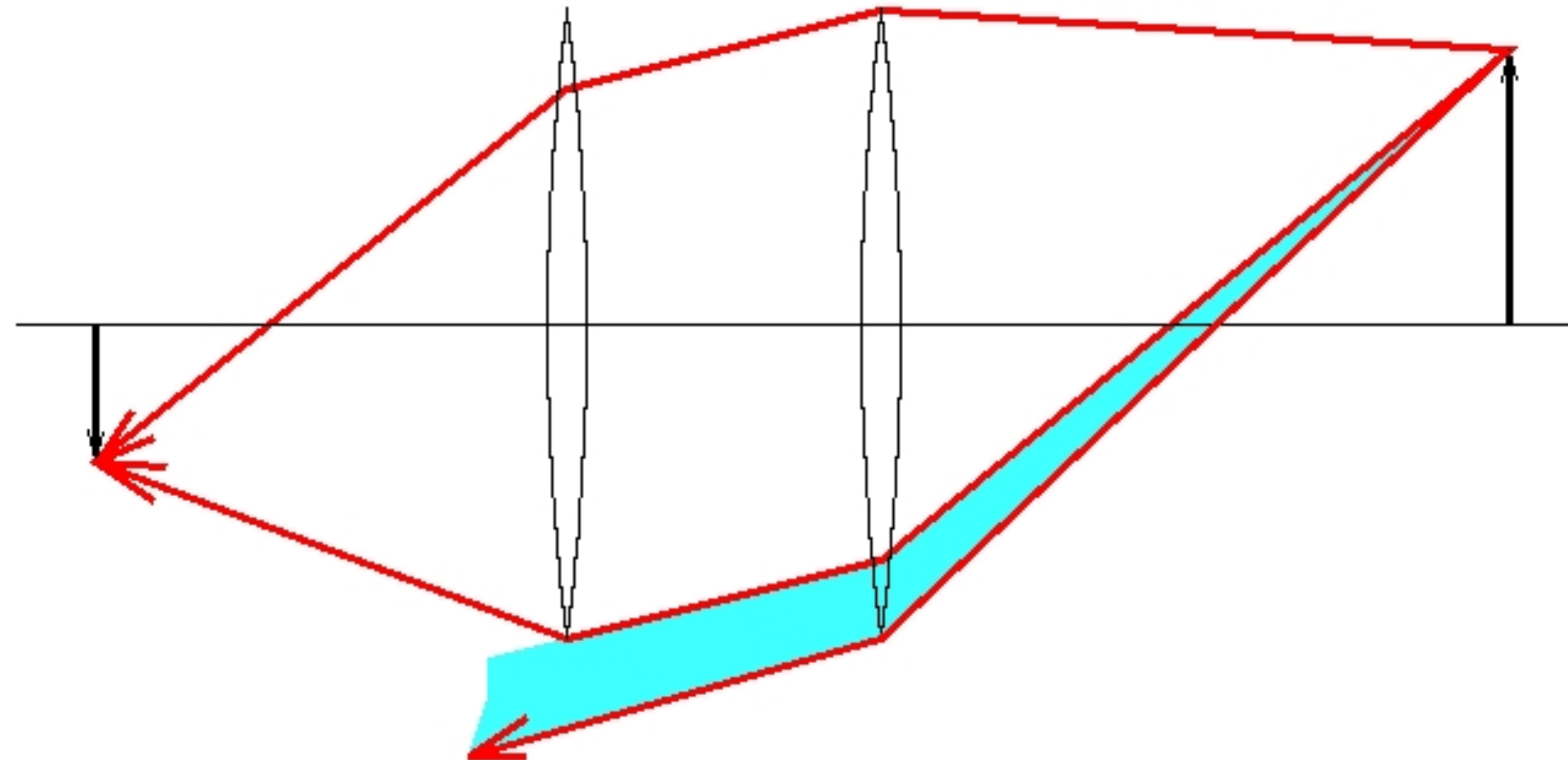
# Compound **Lens Systems**



A modern camera lens may contain multiple components, including aspherical elements

# Vignetting

Vignetting in a two-lens system



Forsyth & Ponce (2nd ed.) Figure 1.12

The shaded part of the beam **never reaches** the second lens



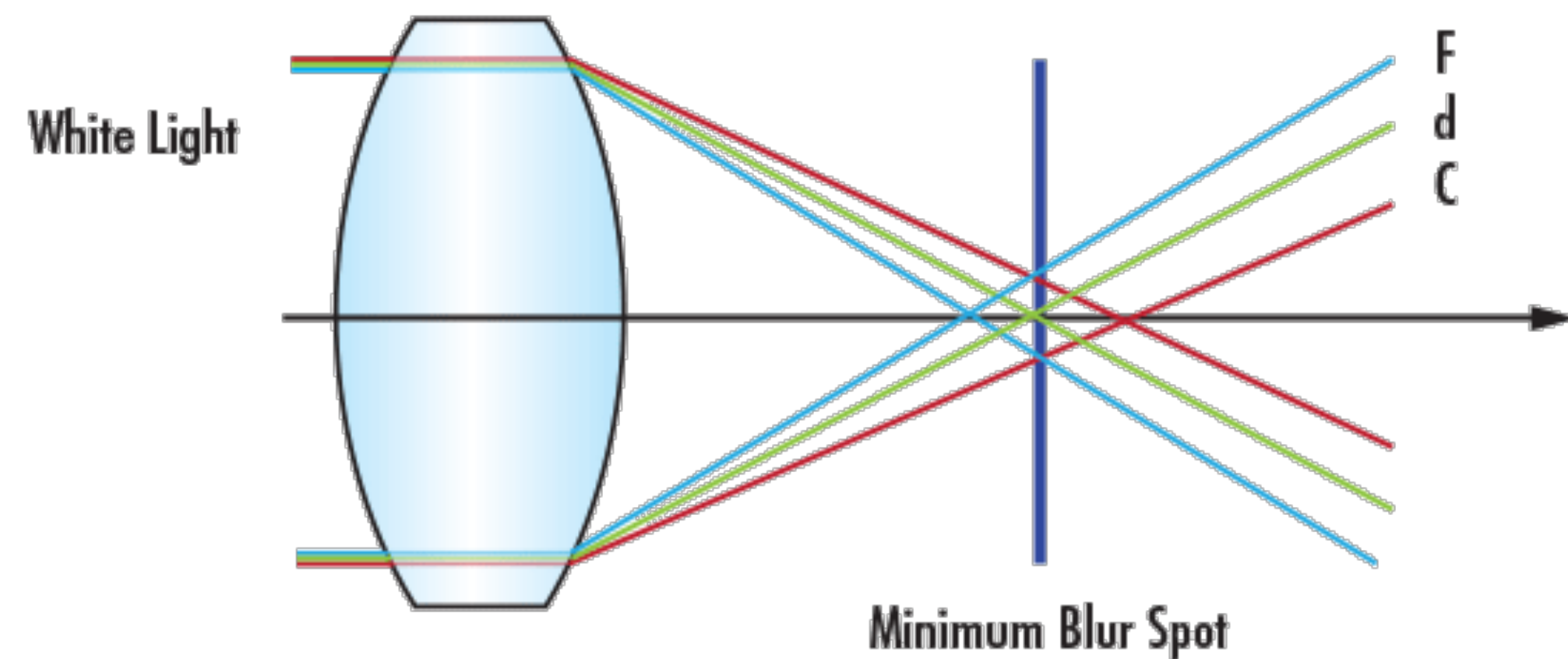
# Vignetting





# Chromatic **Aberration**

- Index of **refraction depends on wavelength**,  $\lambda$ , of light
- Light of different colours follows different paths
- Therefore, not all colours can be in equal focus



**Image Credit:** Trevor Darrell

# Other (Possibly Significant) **Lens Effects**

## Chromatic **aberration**

- Index of refraction depends on wavelength,  $\lambda$ , of light
- Light of different colours follows different paths
- Therefore, not all colours can be in equal focus

## **Scattering** at the lens surface

- Some light is reflected at each lens surface

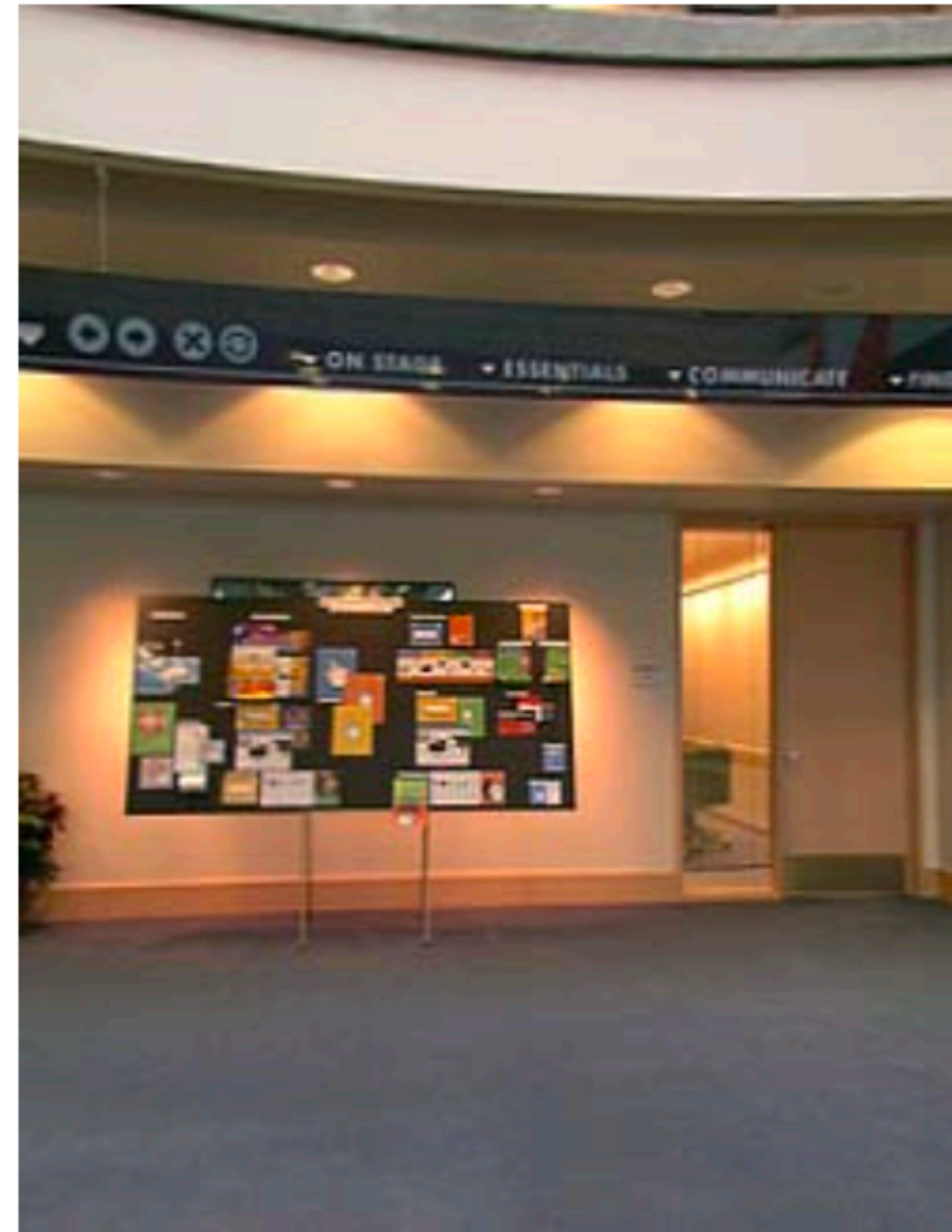
## There are other **geometric phenomena/distortions**

- pincushion distortion
- barrel distortion
- etc



# Lens Distortion

Fish-eye Lens



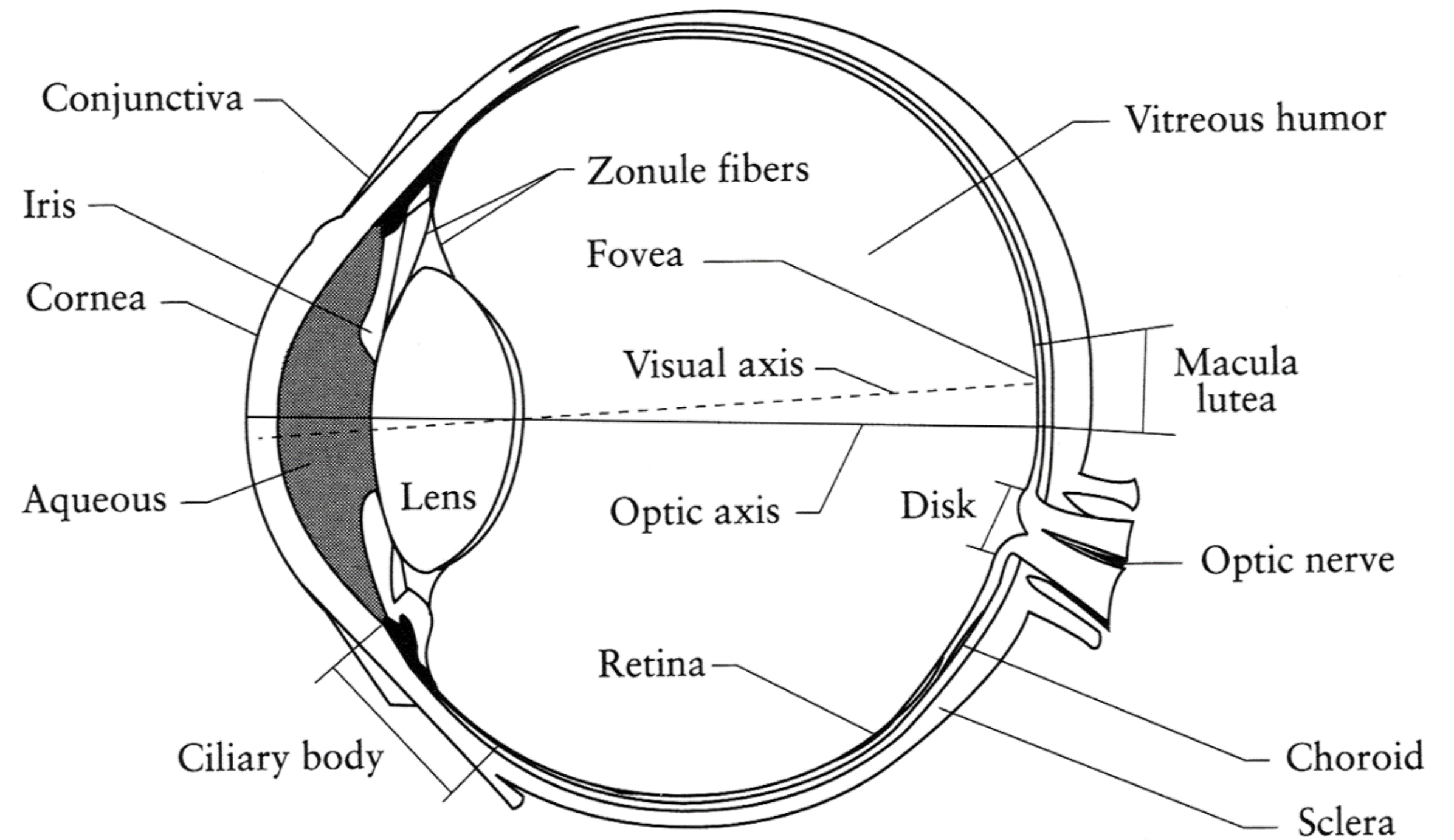
Szeliski (1st ed.) Figure 2.13

Lines in the world are no longer lines on the image, they are curves!



# Human Eye

- The eye has an iris (like a camera)
- Focusing is done by changing shape of lens
- When the eye is properly focused, light from an object outside the eye is imaged on the retina
- The retina contains light receptors called rods and cones



**pupil** = pinhole / aperture

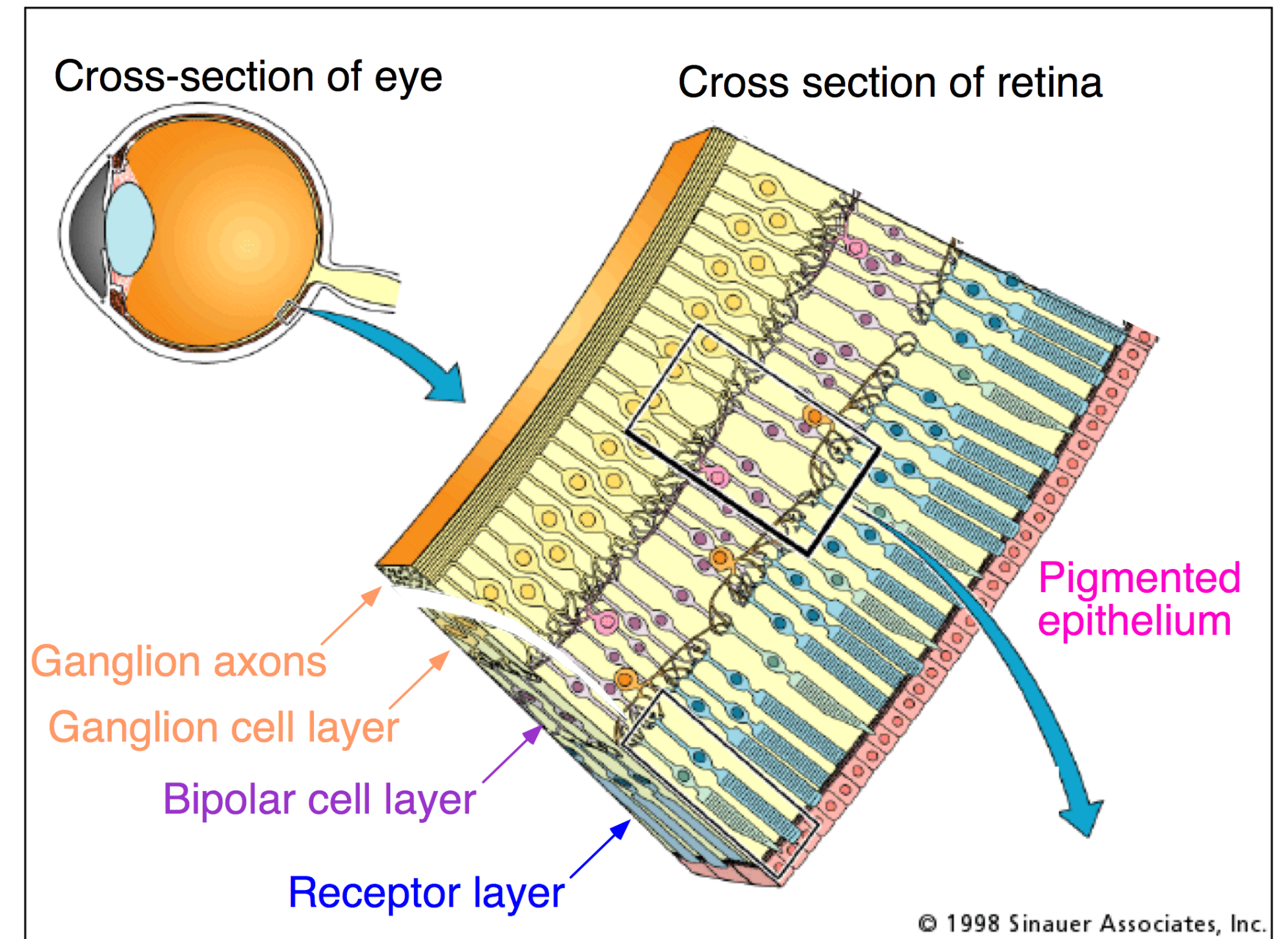
**retina** = film / digital sensor

Slide adopted from: Steve Seitz



# Human Eye

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**pupil** = pinhole / aperture

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Slide adopted from: Steve Seitz

# Two-types of **Light Sensitive Receptors**

## **Rods**

75-150 million rod-shaped receptors

**not** involved in color vision, gray-scale vision only

operate at night

highly sensitive, can responding to a single photon

yield relatively poor spatial detail

## **Cones**

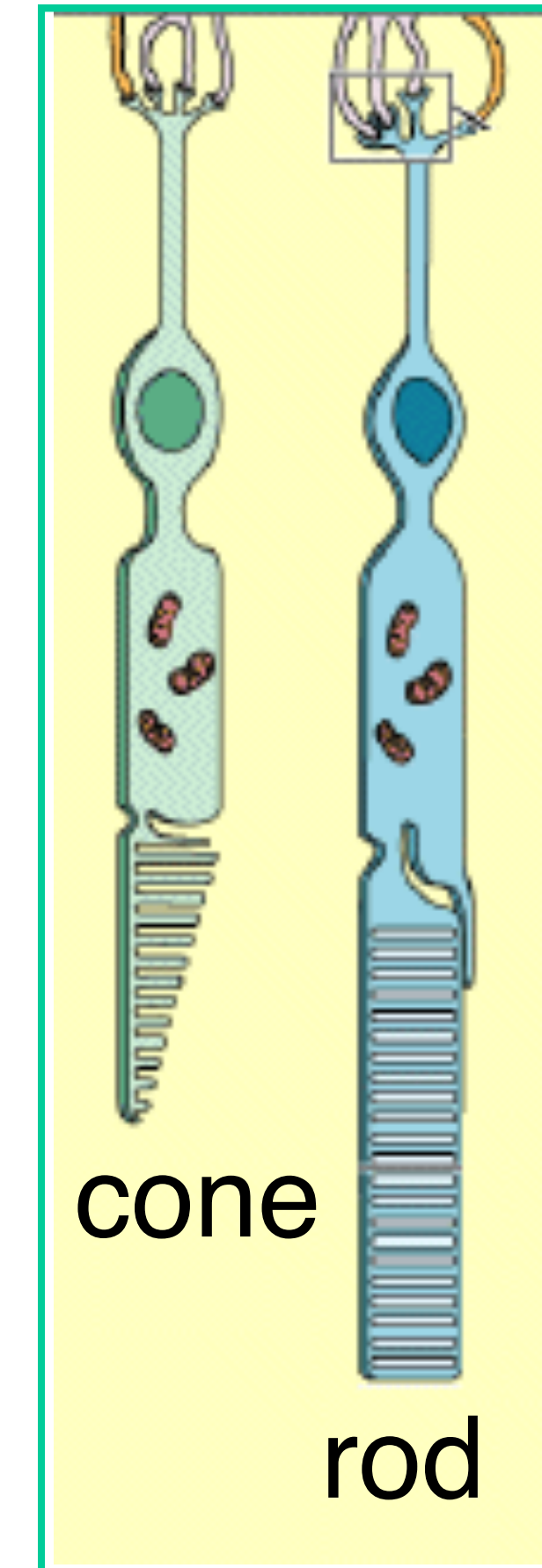
6-7 million cone-shaped receptors

color vision

operate in high light

less sensitive

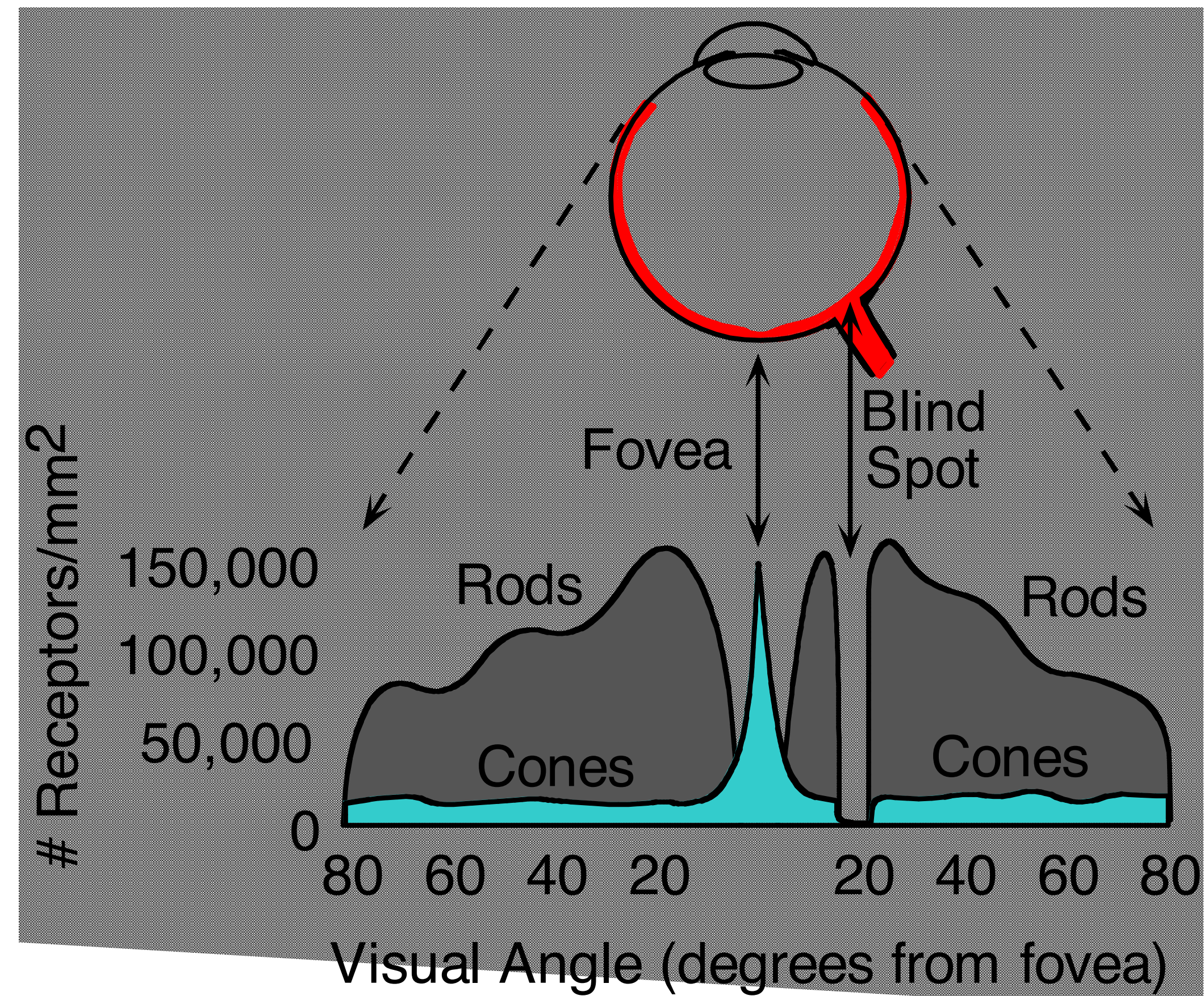
yield higher resolution



Slide adopted from: James Hays

# Human Eye

## Density of rods and cones





# Lecture **Summary**

- We discussed a “physics-based” approach to image formation. Basic abstraction is the **pinhole camera**.
- **Lenses overcome limitations** of the pinhole model while trying to preserve it as a useful abstraction
- Projection equations: **perspective**, weak perspective, orthographic
- Thin lens equation
- Some “aberrations and **distortions**” persist (e.g. spherical aberration, vignetting)
- The **human eye** functions much like a camera