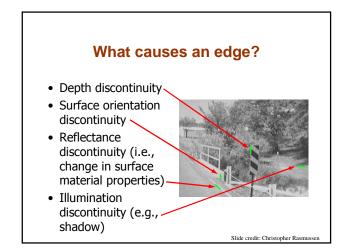
Edge and Corner Detection Reading: Chapter 8 (skip 8.1)

- Goal: Identify sudden changes (discontinuities) in an image
- This is where most shape information is encoded
- **Example:** artist's line drawing (but artist is also using object-level knowledge)

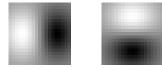


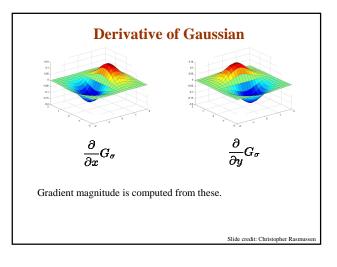


Smoothing and Differentiation

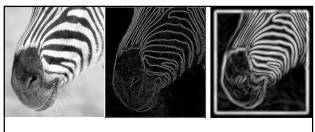
- Edge: a location with high gradient (derivative)
- · Need smoothing to reduce noise prior to taking derivative
- Need two derivatives, in x and y direction.
- We can use derivative of Gaussian filters
 - because differentiation is convolution, and convolution is associative:

D * (G * I) = (D * G) * I





Gradient magnitude Let I(X, Y) be a (digital) image Let $I_x(X, Y)$ and $I_y(X, Y)$ be estimates of the partial derivatives in the x and y directions, respectively. Call these estimates I_x and I_y (for short) The vector $[I_x, I_y]$ is the gradient The scalar $\sqrt{I_x^2 + I_y^2}$ is the gradient magnitude



Scale

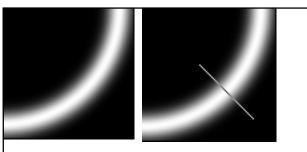
Increased smoothing:

- Eliminates noise edges.
- Makes edges smoother and thicker.
- Removes fine detail.

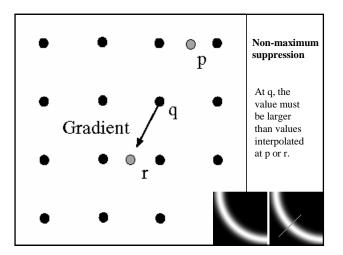
Canny Edge Detection

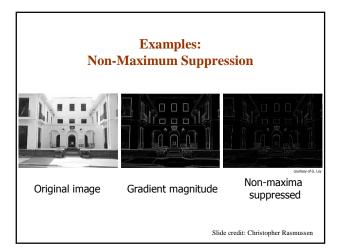
Steps:

- 1. Apply derivative of Gaussian
- 2. Non-maximum suppression
 - Thin multi-pixel wide "ridges" down to single pixel width
- 3. Linking and thresholding
 - Low, high edge-strength thresholds
 - Accept all edges over low threshold that are connected to edge over high threshold
- Matlab: edge(I, `canny')

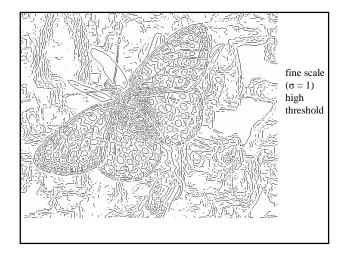


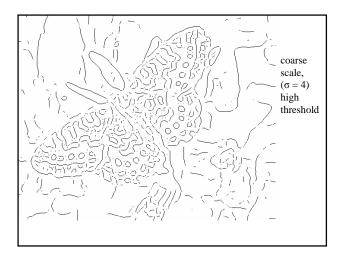
- Non-maximum suppression:
 - Select the single maximum point across the width of an edge.

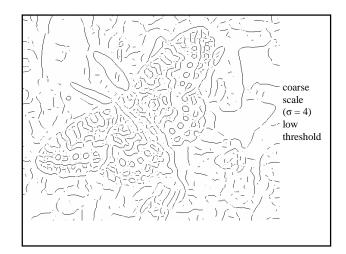


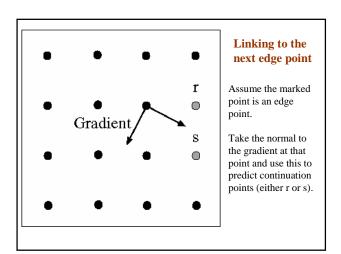










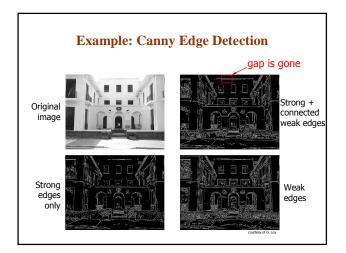


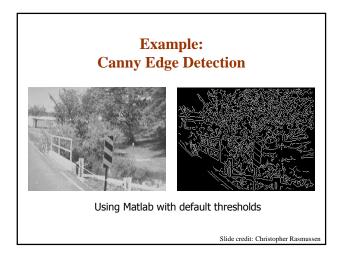


- Hysteresis: A lag or momentum factor
- + Idea: Maintain two thresholds k_{high} and k_{low} – Use k_{high} to find strong edges to start edge chain

 - Use $\boldsymbol{k}_{\text{low}}$ to find weak edges which continue edge chain
- Typical ratio of thresholds is roughly

 $k_{high} / k_{low} = 2$





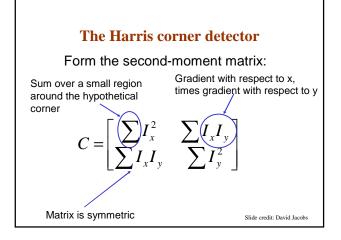
Finding Corners

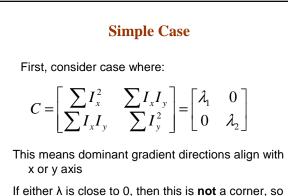
Edge detectors perform poorly at corners.

Corners provide repeatable points for matching, so are worth detecting.

Idea:

- Exactly at a corner, gradient is ill defined.
- However, in the region around a corner, gradient has two or more different values.





look for locations where both are large.

Slide credit: David Jacobs

General Case

It can be shown that since C is symmetric:

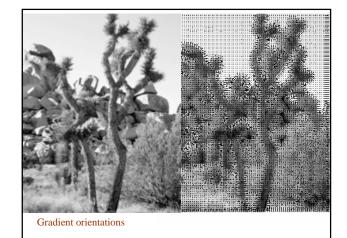
$$C = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$$

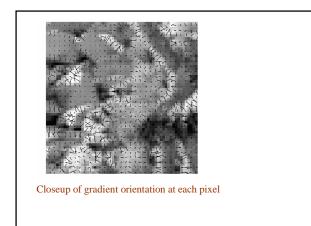
So every case is like a rotated version of the one on last slide.

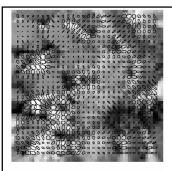
Slide credit: David Jacobs

So, to detect corners

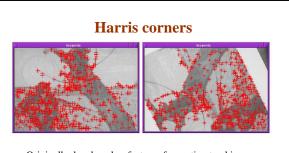
- · Filter image with Gaussian to reduce noise
- Compute magnitude of the x and y gradients at each pixel
- Construct C in a window around each pixel (Harris uses a Gaussian window just blur)
- Solve for product of λs (determinant of C)
- If λs are both big (product reaches local maximum and is above threshold), we have a corner (Harris also checks that ratio of λs is not too high)







Corners are detected where the product of the ellipse axis lengths reaches a local maximum.



- Originally developed as features for motion tracking
- Greatly reduces amount of computation compared to tracking every pixel
- Translation and rotation invariant (but not scale invariant)