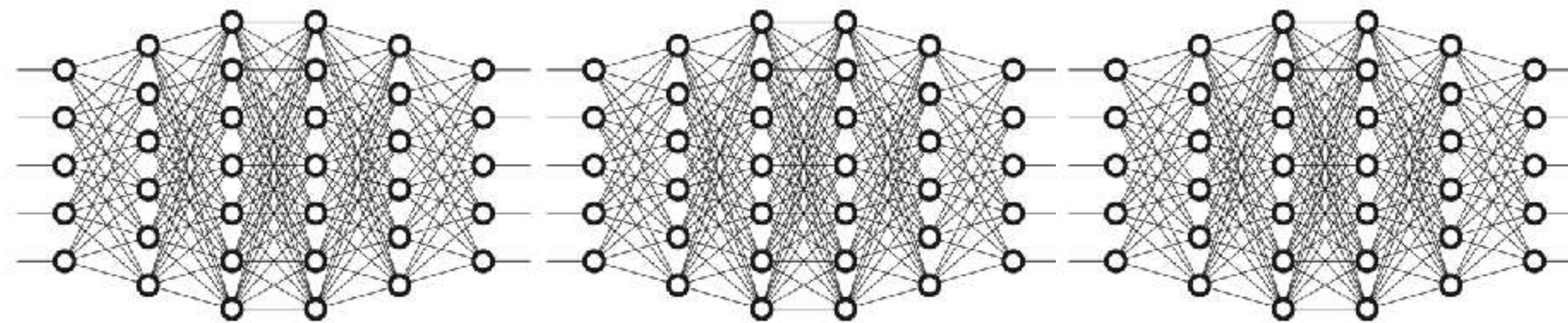




# CPSC 425: Computer Vision



## Lecture 22: Neural Networks 3

# Menu for Today

## Topics:

- **Neural Networks** part 3
- Weight **Initialization**
- **Normalization**
- Preventing **Overfitting**

## Readings:

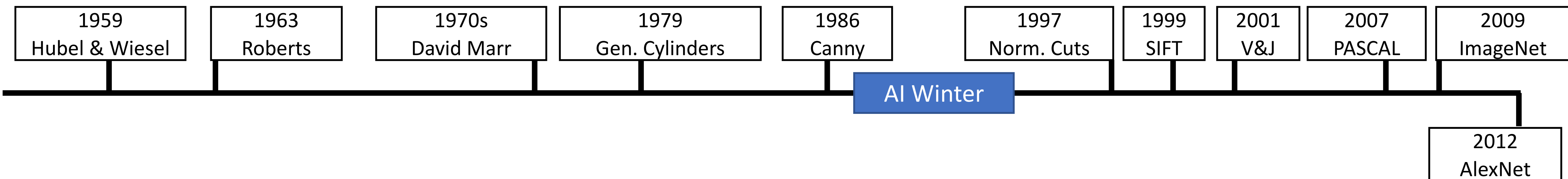
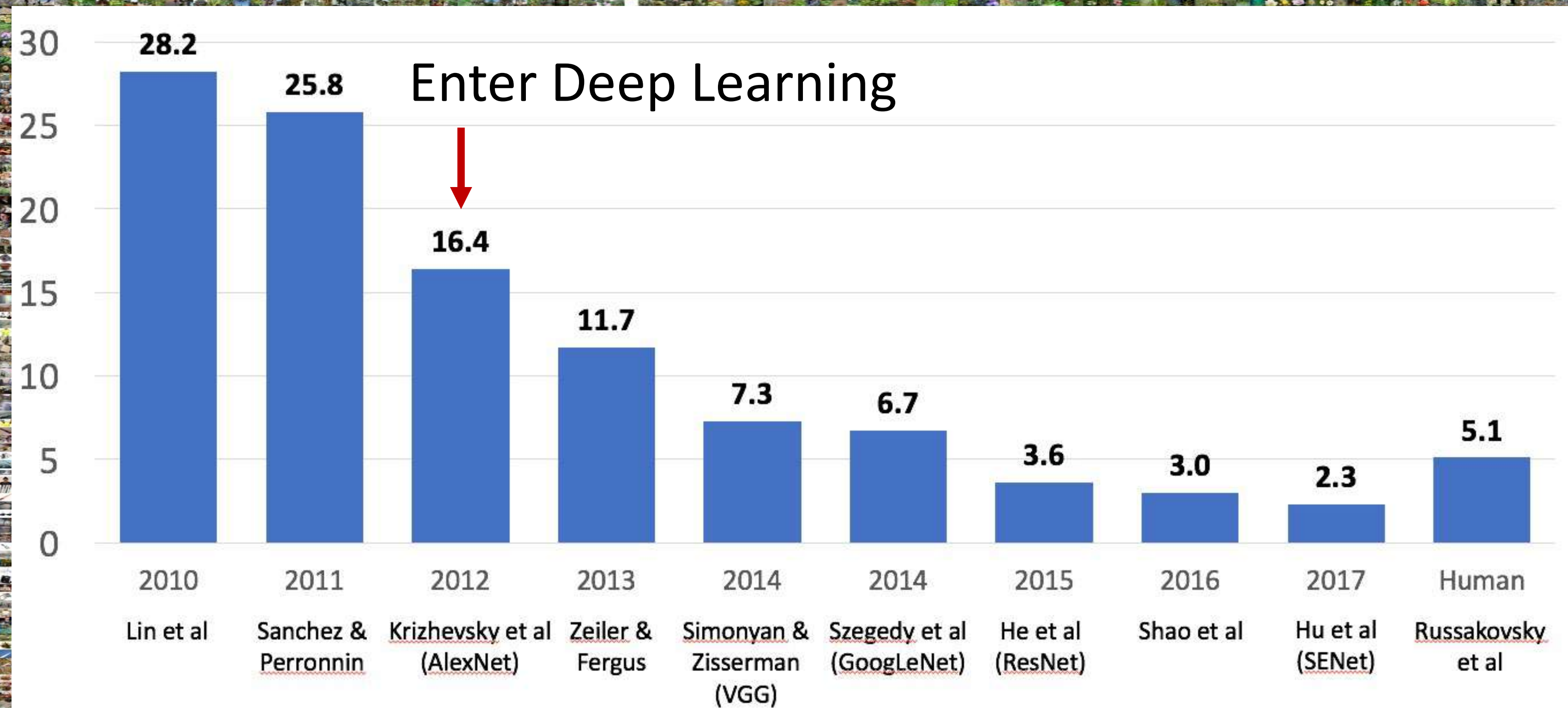
- **Today's** Lecture: Szeliski 5.1.3, 5.3-5.4, Justin Johnson Michigan EECS 498/598

## Reminders:

- **Quiz 6** April 7th
- **Assignment 6:** due Apr 10th <— watch out!

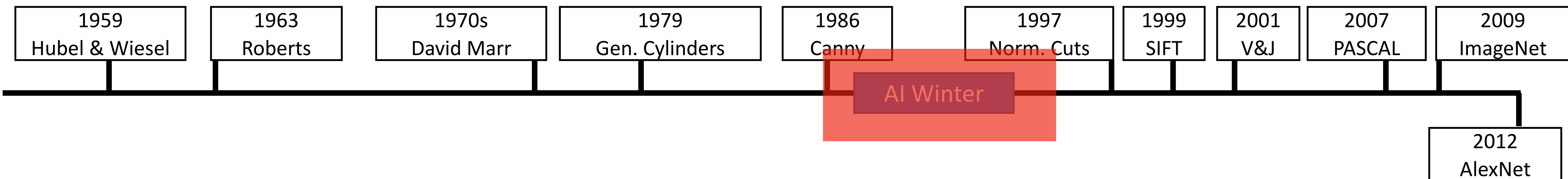
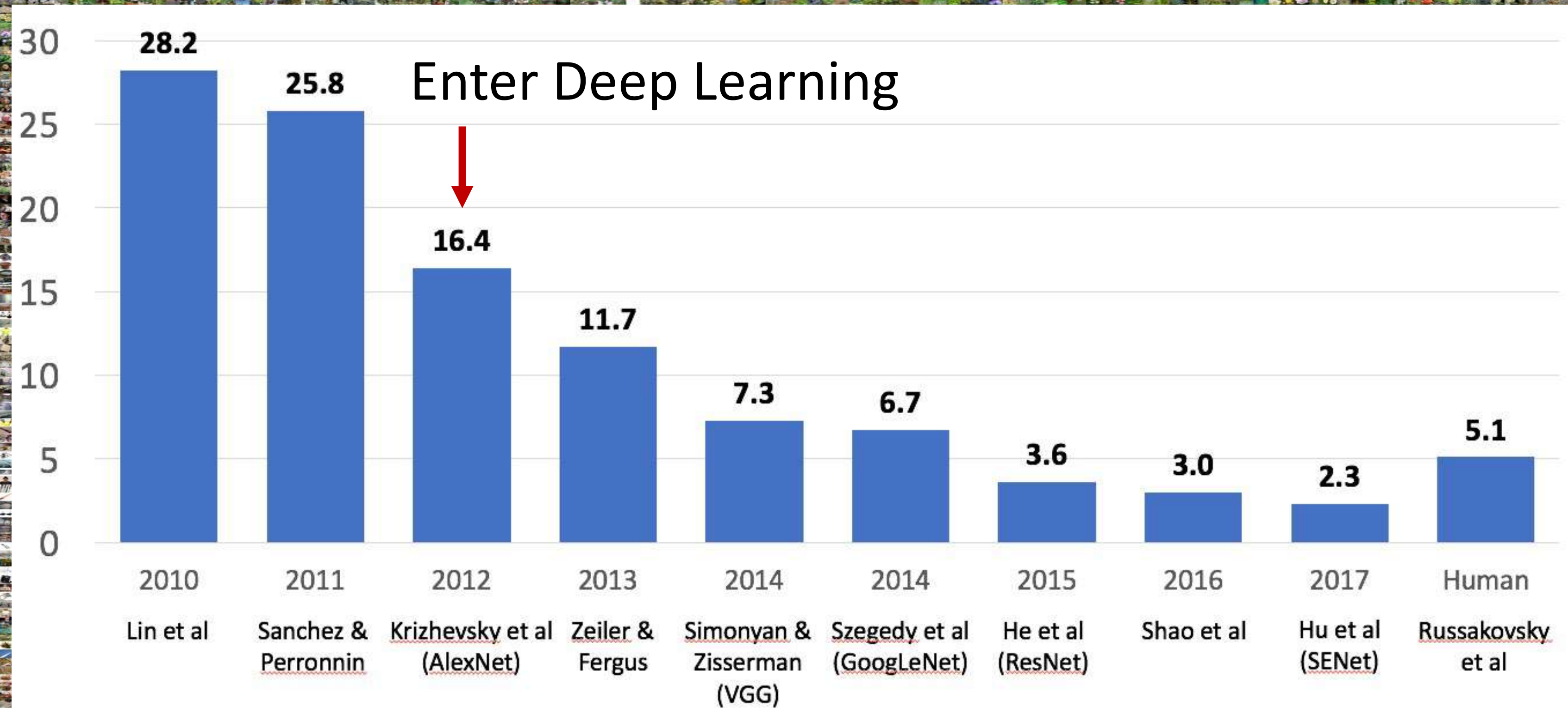


# IMAGENET Large Scale Visual Recognition Challenge





# IMAGENET Large Scale Visual Recognition Challenge







So why now?



# Rise of large datasets

The logo for ImageNet, featuring the word "IMAGENET" in a sans-serif font. The letter "A" is replaced by a small graphic of three colored squares (green, orange, red) connected by lines, resembling a simple neural network or a stylized letter.

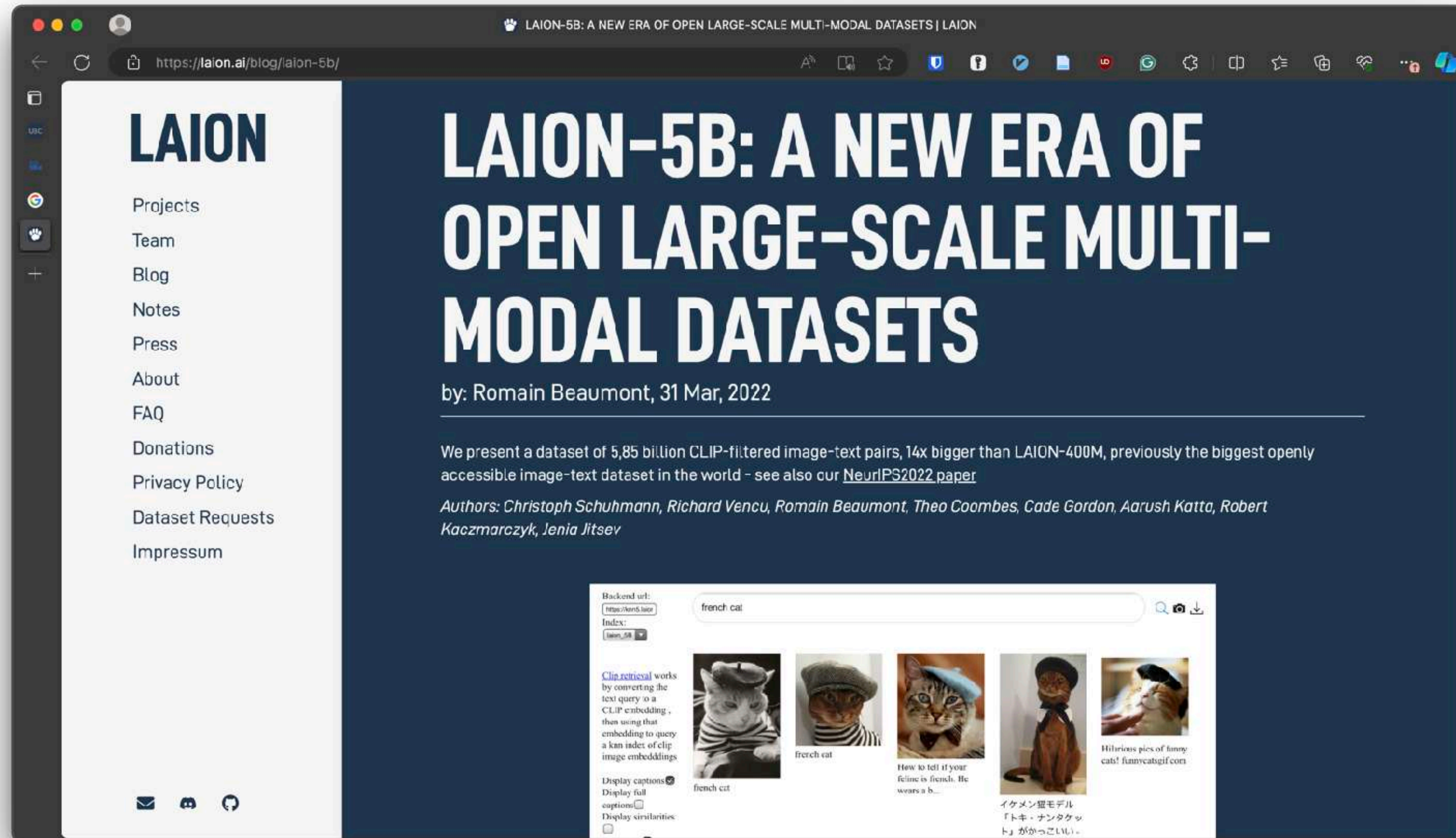
[www.image-net.org](http://www.image-net.org)

**22K** categories and **14M** images

- Animals
  - Bird
  - Fish
  - Mammal
  - Invertebrate
- Plants
  - Tree
  - Flower
  - Food
  - Materials
- Structures
  - Artifact
  - Tools
  - Appliances
  - Structures
- Person
  - Scenes
  - Indoor
  - Geological Formations
  - Sport Activities



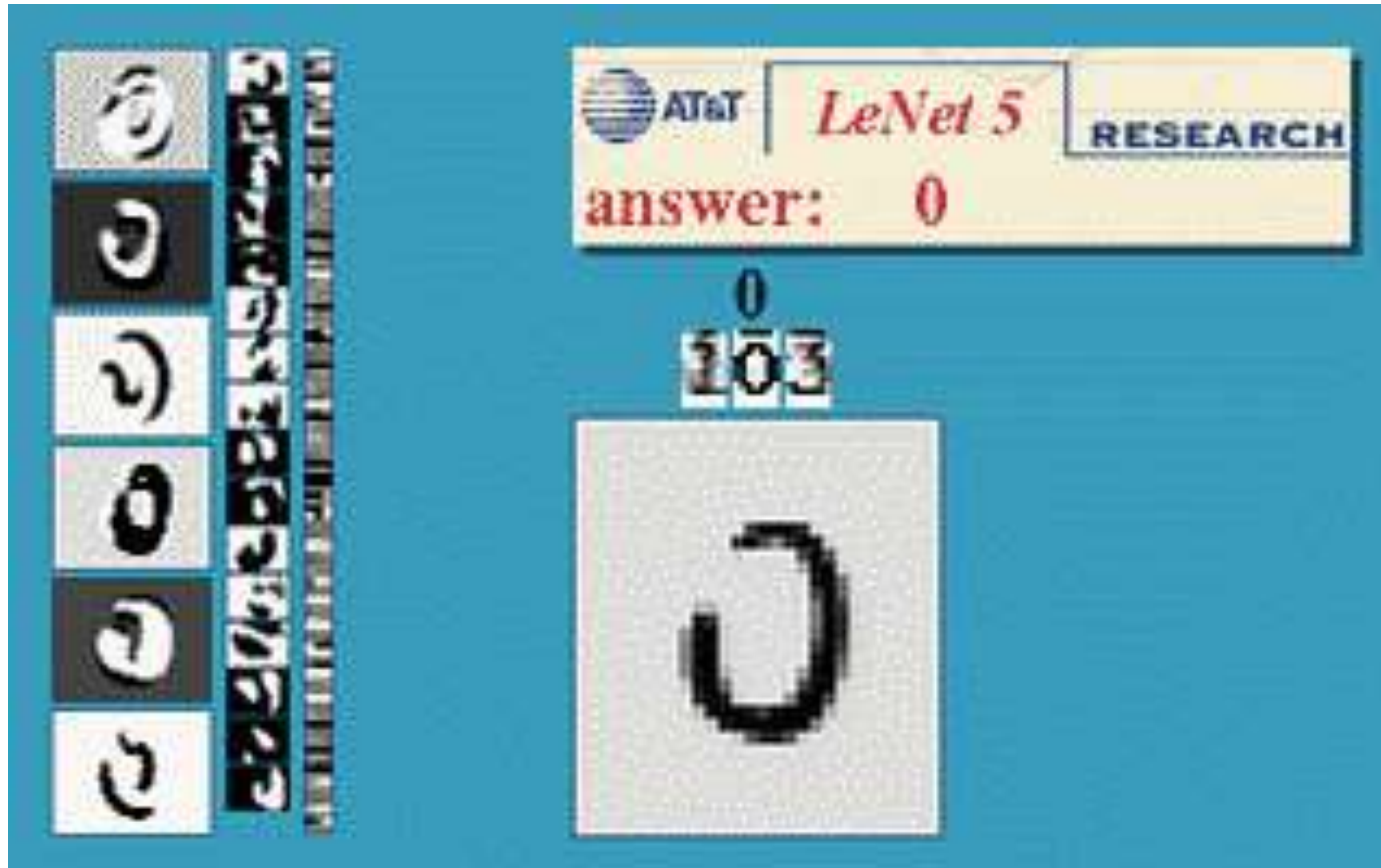
# Rise of large datasets





# Clever architectures

## Convolutional neural networks

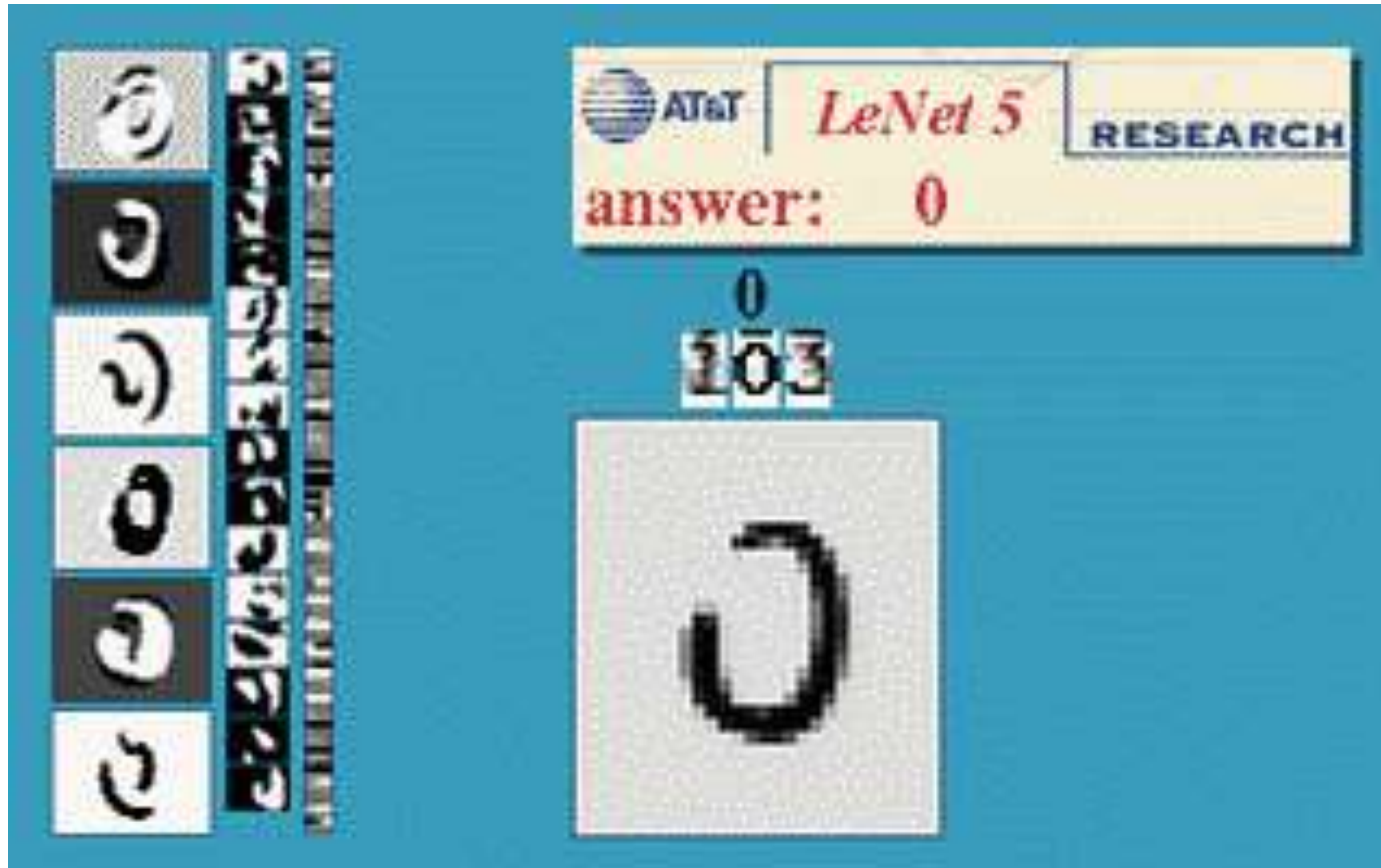


[Lecun, Bottou, Bengio, and Haffner, "Gradient-Based Learning Applied to Document Recognition", 1998]



# Clever architectures

## Convolutional neural networks

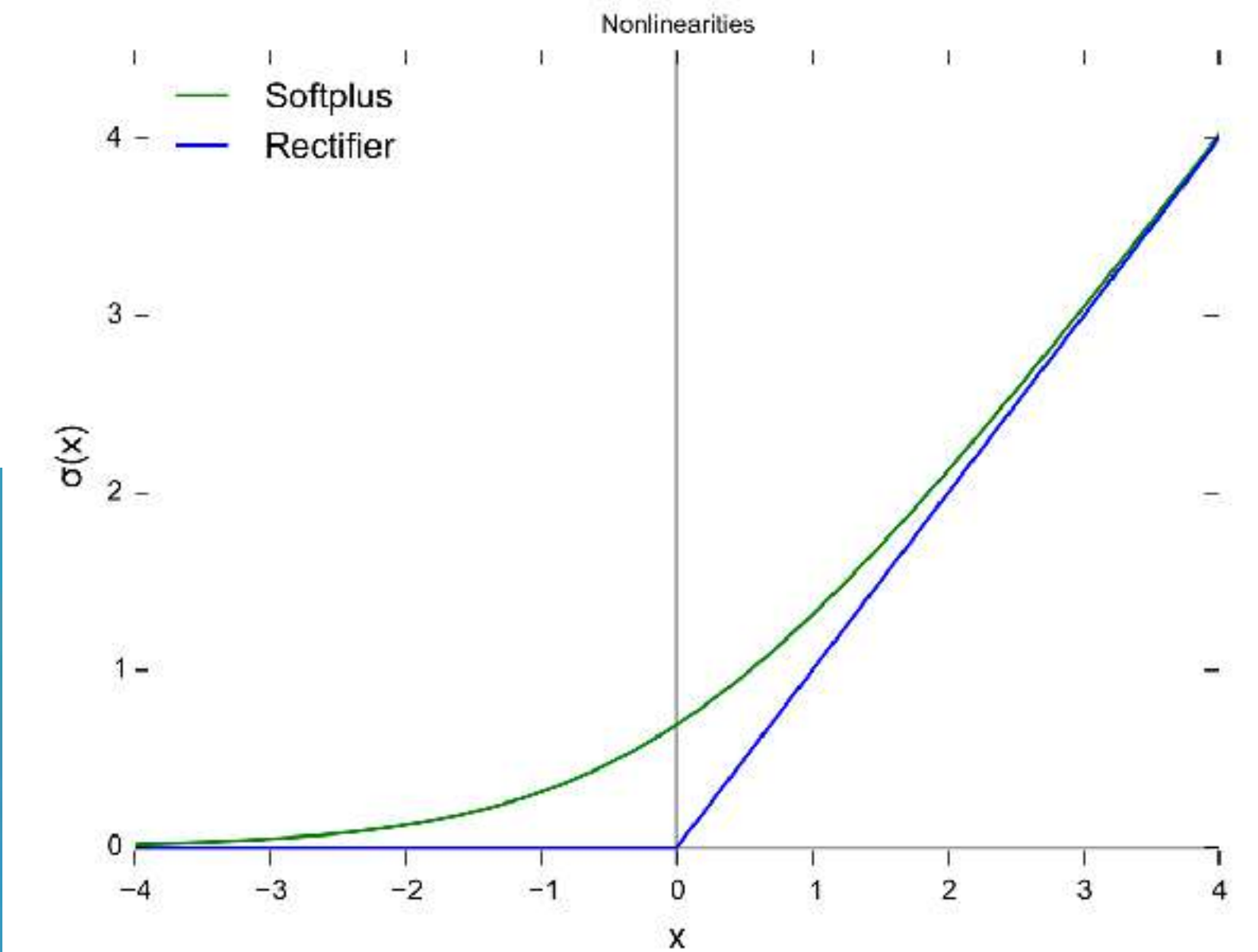
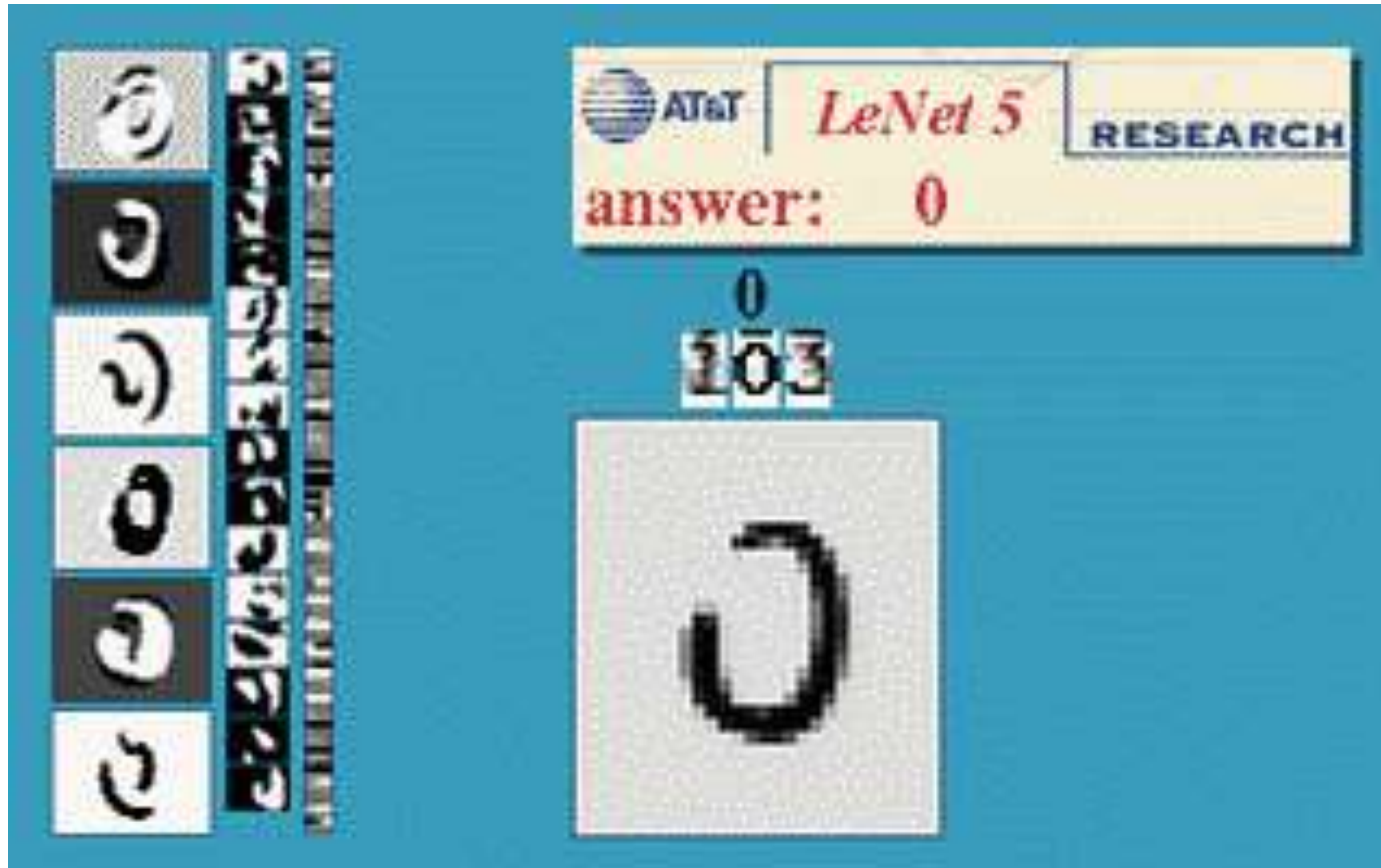


[Lecun, Bottou, Bengio, and Haffner, "Gradient-Based Learning Applied to Document Recognition", 1998]



# Clever architectures

## Convolutional neural networks



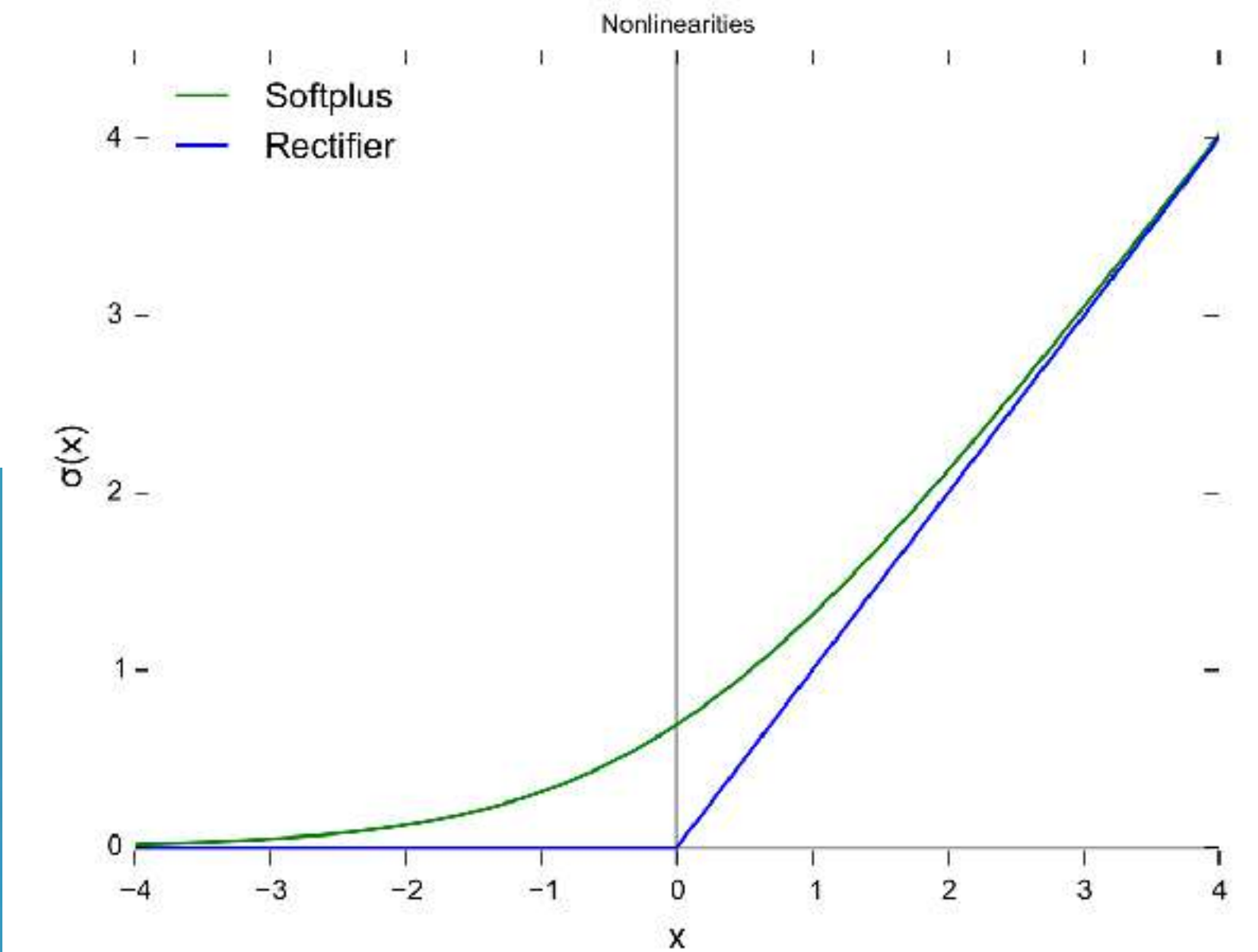
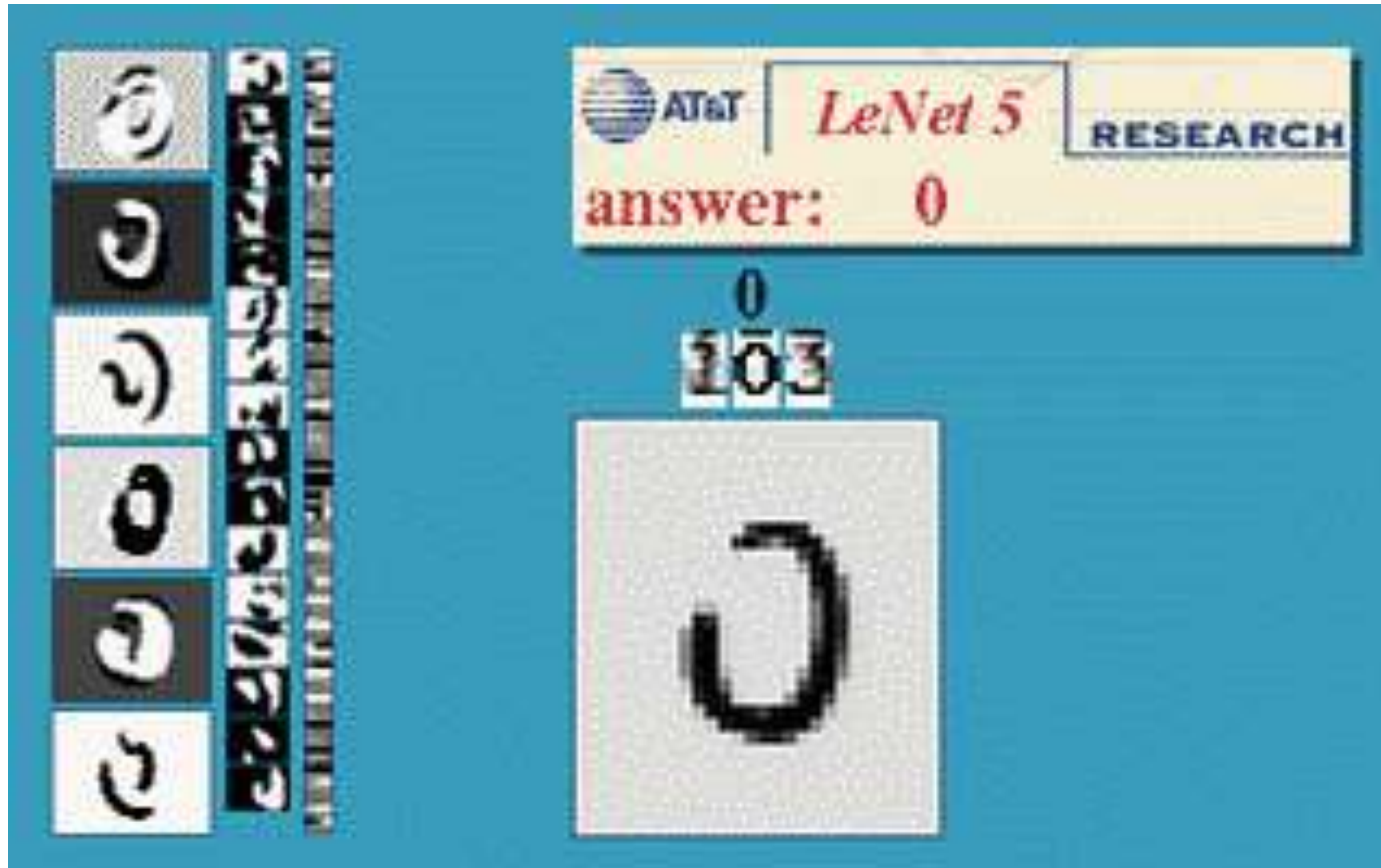
[Nair and Hinton, “Rectified Linear Units Improve Restricted Boltzmann Machines”, 2010]

[Lecun, Bottou, Bengio, and Haffner, “Gradient-Based Learning Applied to Document Recognition”, 1998]



# Clever architectures

## Convolutional neural networks



[Nair and Hinton, “Rectified Linear Units Improve Restricted Boltzmann Machines”, 2010]

[Lecun, Bottou, Bengio, and Haffner, “Gradient-Based Learning Applied to Document Recognition”, 1998]



# Clever architectures

Transformers, Vaswani et al., 2017

## Attention is all you need

Authors Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, Illia Polosukhin

Publication date 2017

Journal Advances in neural information processing systems

Volume 30

Description The dominant sequence transduction models are based on complex recurrent or convolutional neural networks in an encoder and decoder configuration. The best performing such models also connect the encoder and decoder through an attention mechanism. We propose a novel, simple network architecture based solely on an attention mechanism, dispensing with recurrence and convolutions entirely. Experiments on two machine translation tasks show these models to be superior in quality while being more parallelizable and requiring significantly less time to train. Our single model with 165 million parameters, achieves 27.5 BLEU on English-to-German translation, improving over the existing best ensemble result by over 1 BLEU. On English-to-French translation, we outperform the previous single state-of-the-art with model by 0.7 BLEU, achieving a BLEU score of 41.1.

Total citations Cited by 87925

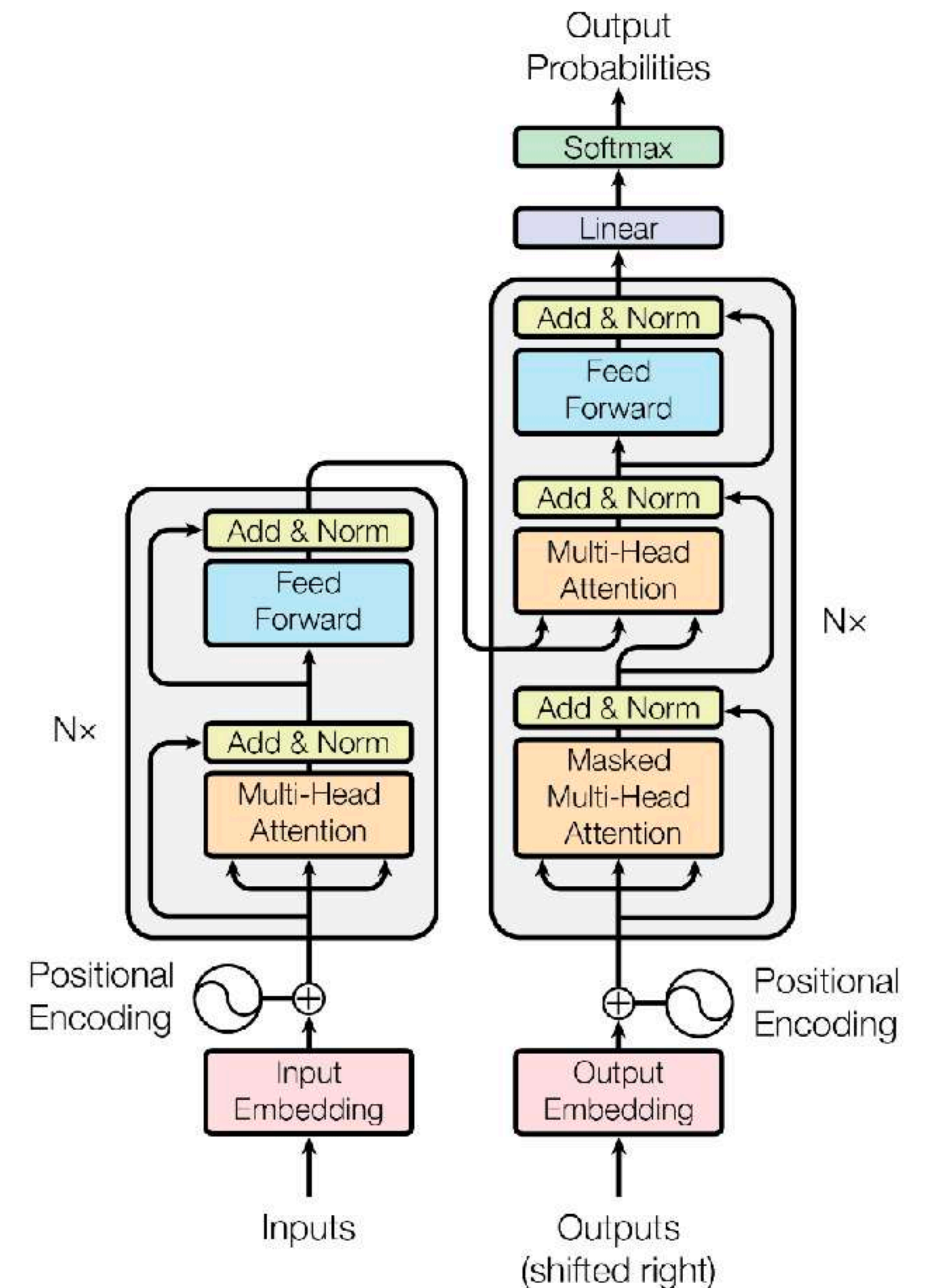
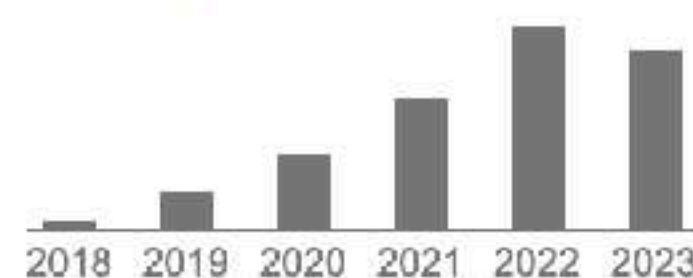


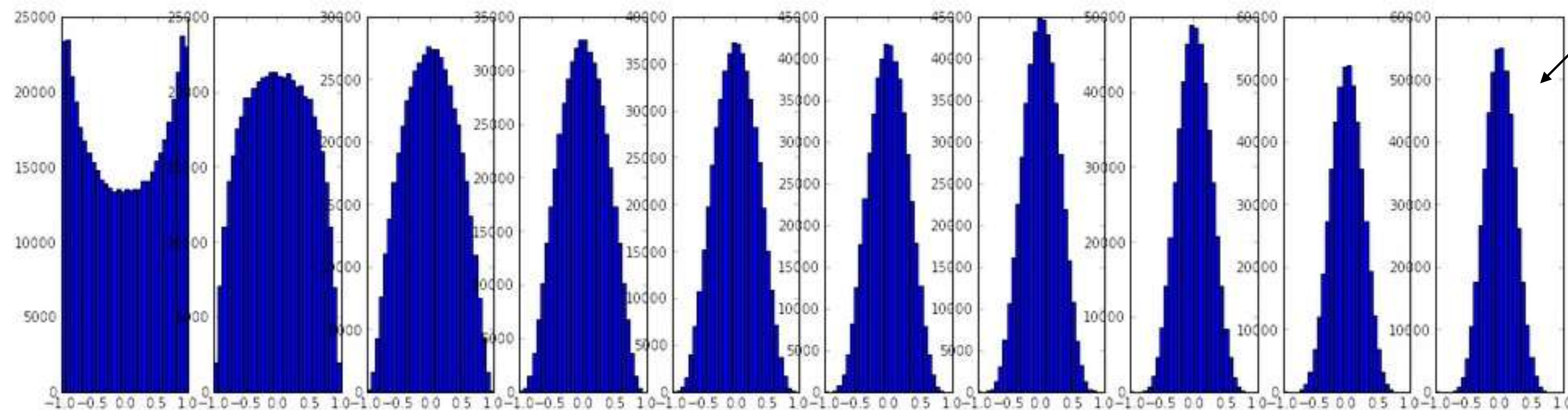
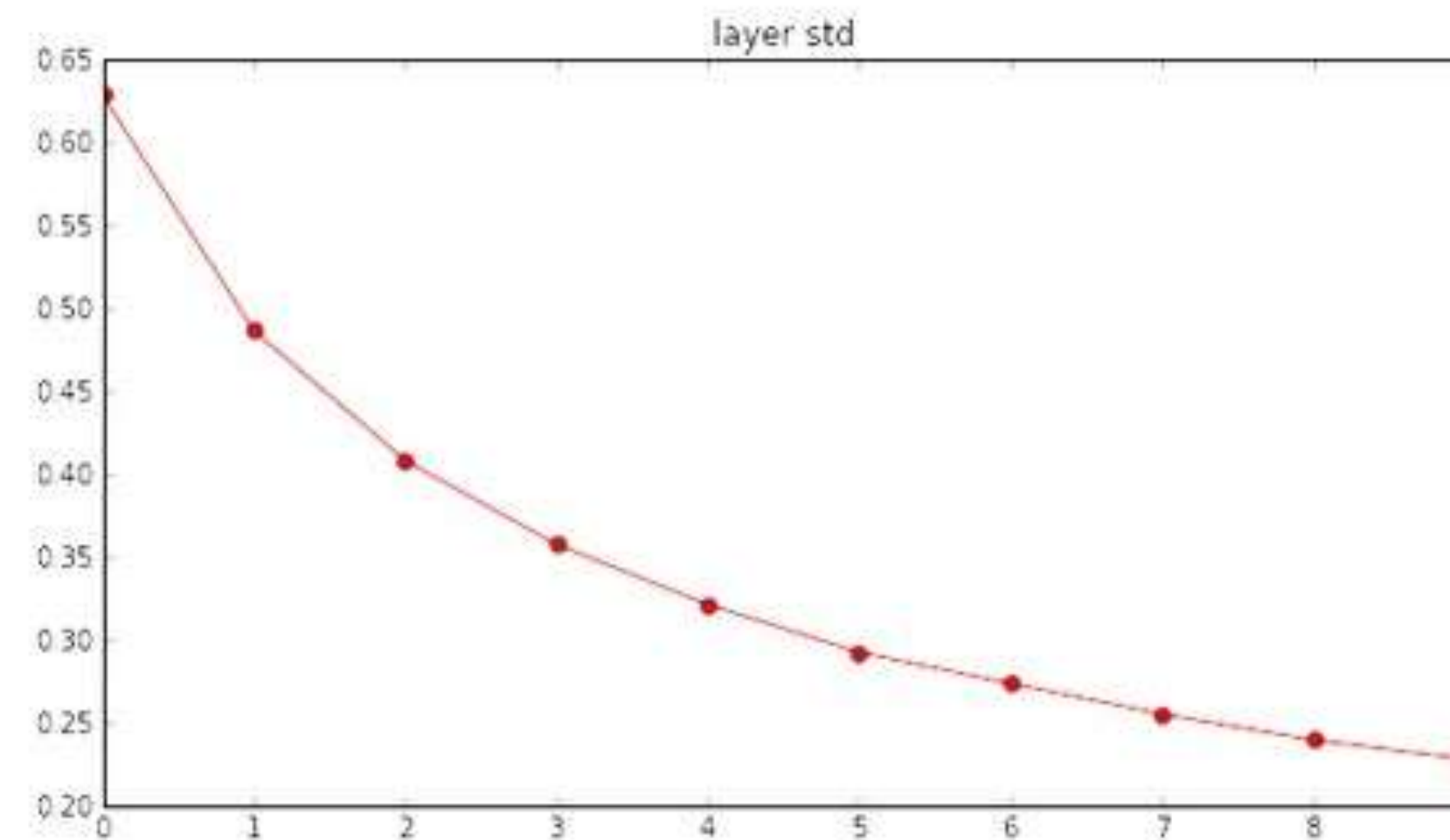
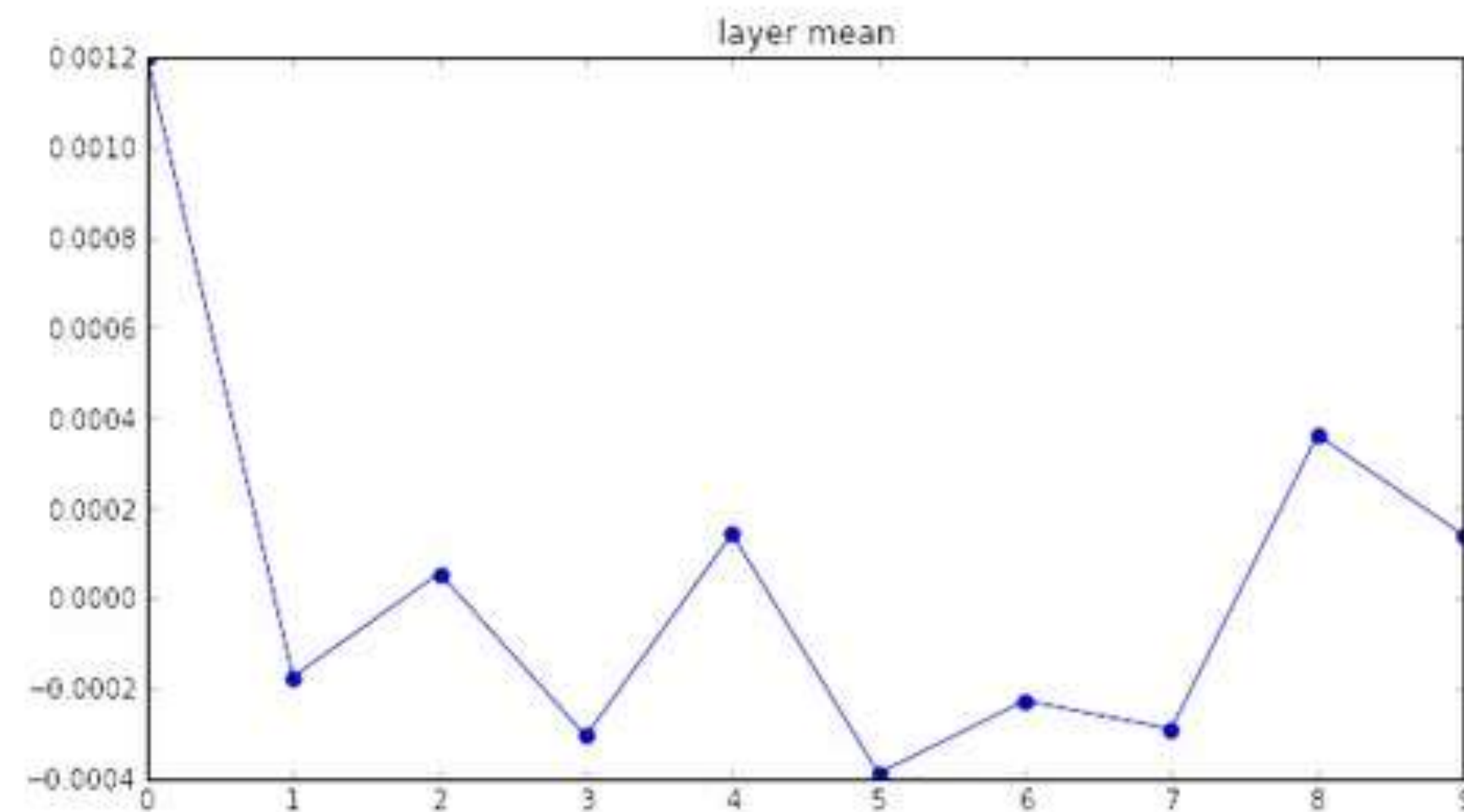
Figure 1: The Transformer - model architecture.



# Proper initialization schemes

Much more important than you think

“Xavier initialization”  
[Glorot et al., 2010]



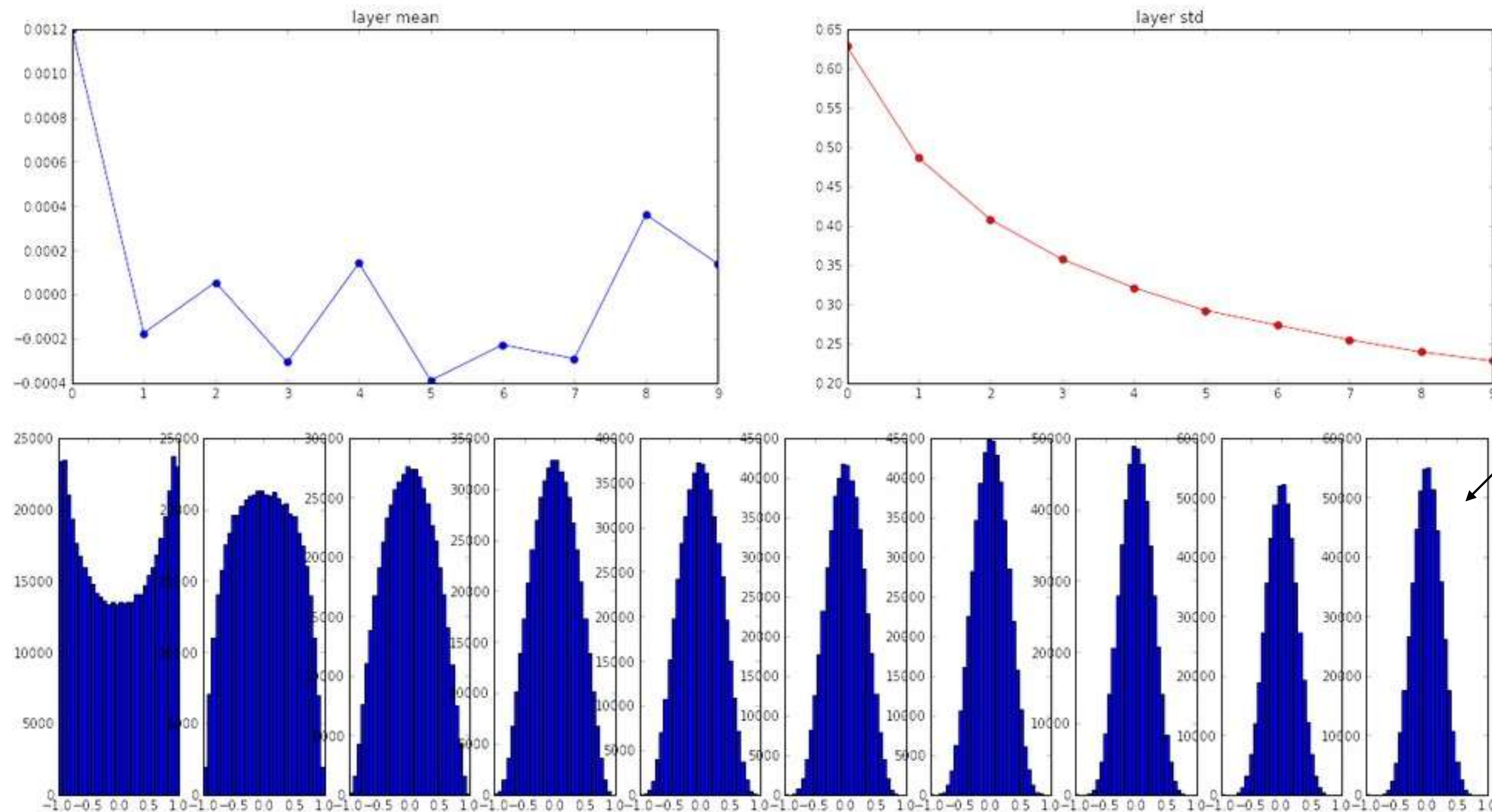
Neuron activations are  
well spread



# Proper initialization schemes

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Neuron activations are  
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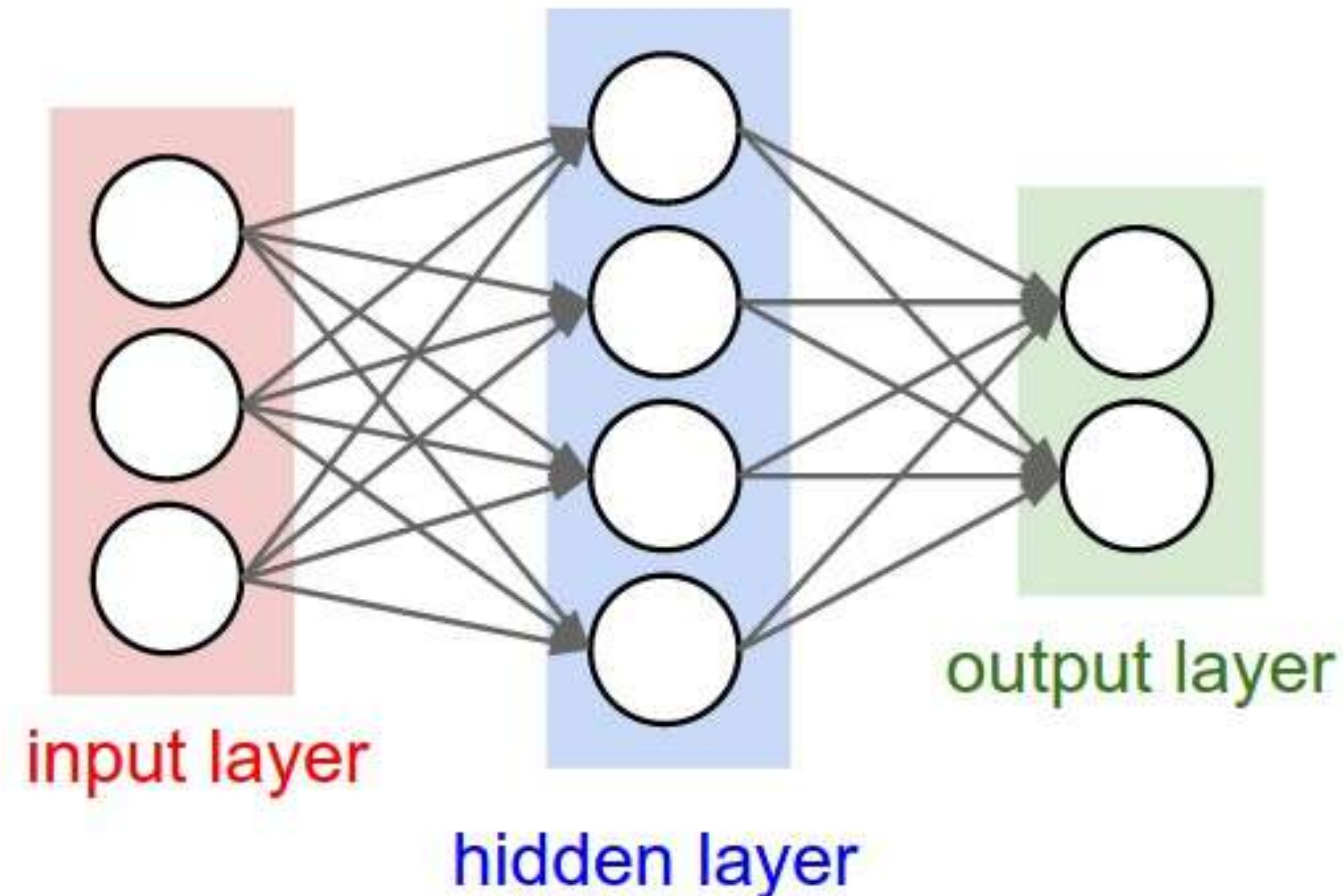
# Weight initialization



# Weight initialization

A look into ways things can go wrong

Q: what happens when  $W=0$  init is used?





# Weight initialization

A look into ways things can go wrong

First idea: **Small random numbers**  
(gaussian with zero mean and  $1e-2$  standard deviation)

```
W = 0.01* np.random.randn(D,H)
```

Works ~okay for small networks, but problems with deeper networks.



We  
A loc

```

27 parser.add_argument("--img_size", type=int, default=32, help="size of each image dimension")
28 parser.add_argument("--channels", type=int, default=1, help="number of image channels")
29 parser.add_argument("--sample_interval", type=int, default=1000, help="number of image channels")
30 opt = parser.parse_args()
31 print(opt)
32
33 cuda = True if torch.cuda.is_available() else False
34
35
36 def weights_init_normal(m):
37     classname = m.__class__.__name__
38     if classname.find("Conv") != -1:
39         torch.nn.init.normal_(m.weight.data, 0.0, 0.02)
40     elif classname.find("BatchNorm") != -1:
41         torch.nn.init.normal_(m.weight.data, 1.0, 0.02)
42         torch.nn.init.constant_(m.bias.data, 0.0)
43
44
45 class Generator(nn.Module):
46     def __init__(self):
47         super(Generator, self).__init__()
48
49         self.init_size = opt.img_size // 4
50         self.ll = nn.Sequential(nn.Linear(opt.latent_dim, 128 * self.init_size * 2))

```



# Weight initialization

A look into ways things can go wrong

Let's look at  
some  
activation  
statistics

E.g. 10-layer net with  
500 neurons on each  
layer, using tanh non-  
linearities, and initializing  
as described in last slide.

```
# assume some unit gaussian 10-D input data
D = np.random.randn(1000, 500)
hidden_layer_sizes = [500]*10
nonlinearities = ['tanh']*len(hidden_layer_sizes)

act = {'relu':lambda x:np.maximum(0,x), 'tanh':lambda x:np.tanh(x)}
Hs = {}
for i in xrange(len(hidden_layer_sizes)):
    X = D if i == 0 else Hs[i-1] # input at this layer
    fan_in = X.shape[1]
    fan_out = hidden_layer_sizes[i]
    W = np.random.randn(fan_in, fan_out) * 0.01 # layer initialization

    H = np.dot(X, W) # matrix multiply
    H = act[nonlinearities[i]](H) # nonlinearity
    Hs[i] = H # cache result on this layer

# look at distributions at each layer
print 'input layer had mean %f and std %f' % (np.mean(D), np.std(D))
layer_means = [np.mean(H) for i,H in Hs.iteritems()]
layer_stds = [np.std(H) for i,H in Hs.iteritems()]
for i,H in Hs.iteritems():
    print 'hidden layer %d had mean %f and std %f' % (i+1, layer_means[i], layer_stds[i])

# plot the means and standard deviations
plt.figure()
plt.subplot(121)
plt.plot(Hs.keys(), layer_means, 'ob-')
plt.title('layer mean')
plt.subplot(122)
plt.plot(Hs.keys(), layer_stds, 'or-')
plt.title('layer std')

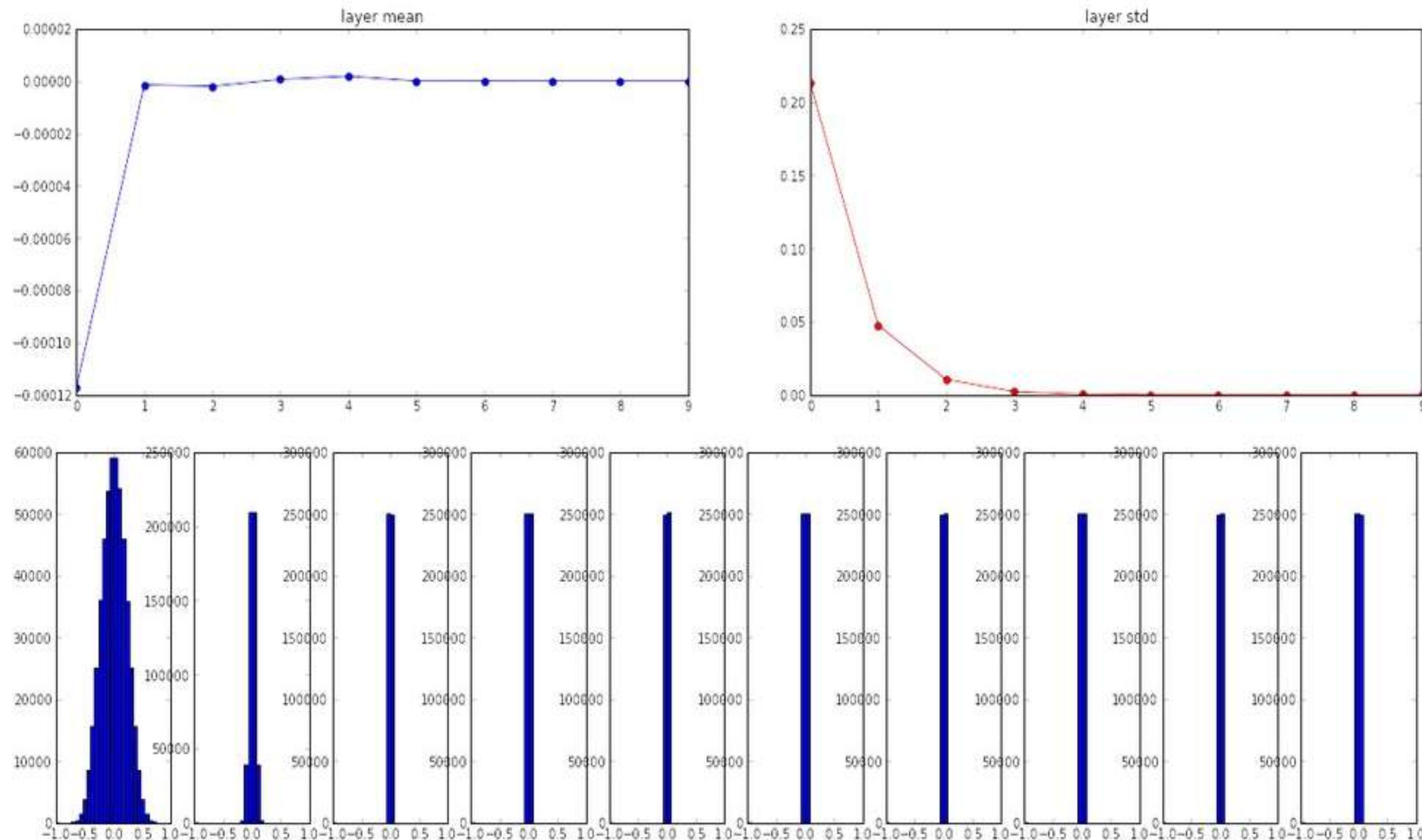
# plot the raw distributions
plt.figure()
for i,H in Hs.iteritems():
    plt.subplot(1,len(Hs),i+1)
    plt.hist(H.ravel(), 30, range=(-1,1))
```

Init with small random numbers



# Weight initialization

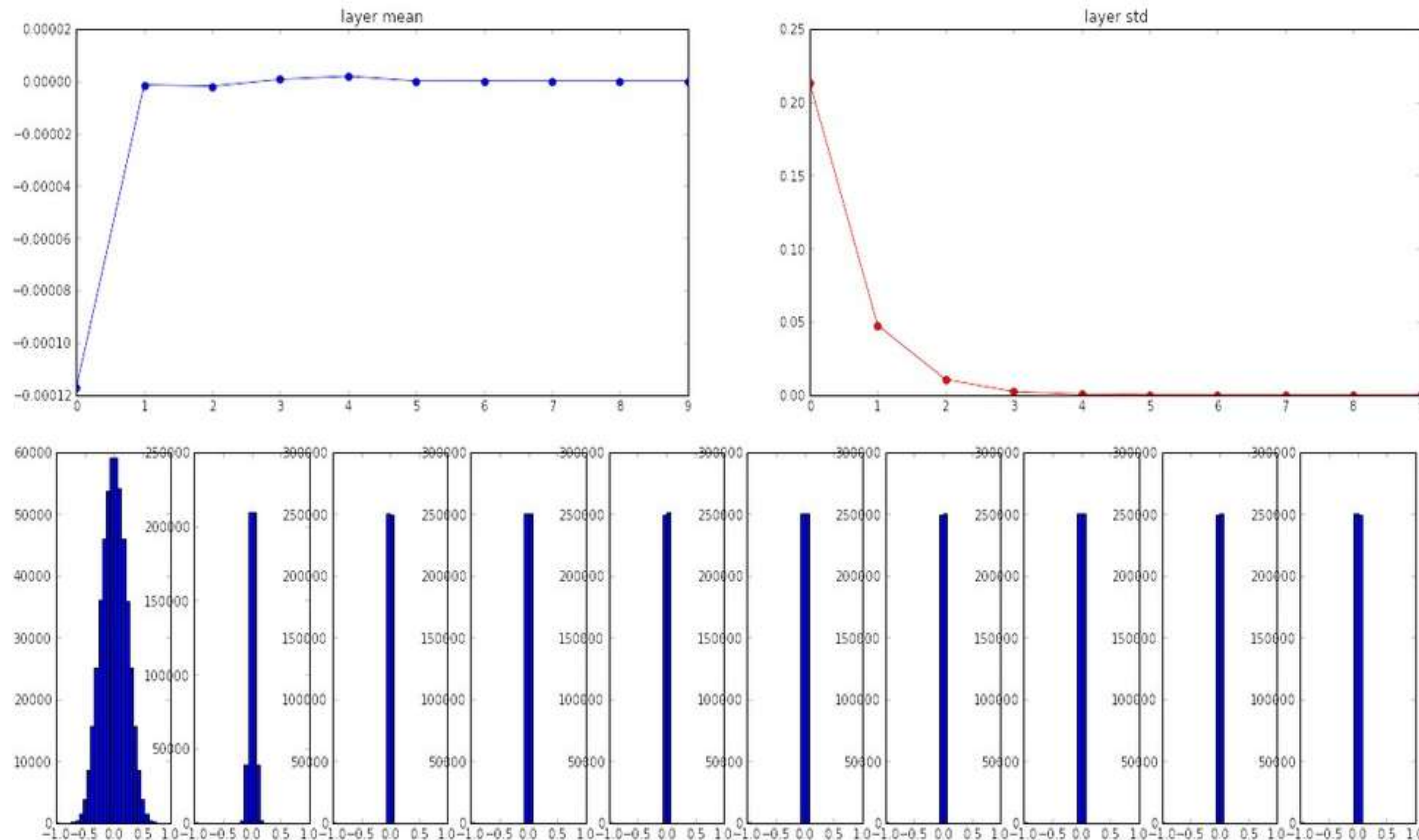
A look into ways things can go wrong





# Weight initialization

A look into ways things can go wrong



All activations  
become zero!

Q: think about the  
backward pass.  
What do the  
gradients look like?

Hint: think about backward  
pass for a  $W \cdot X$  gate.

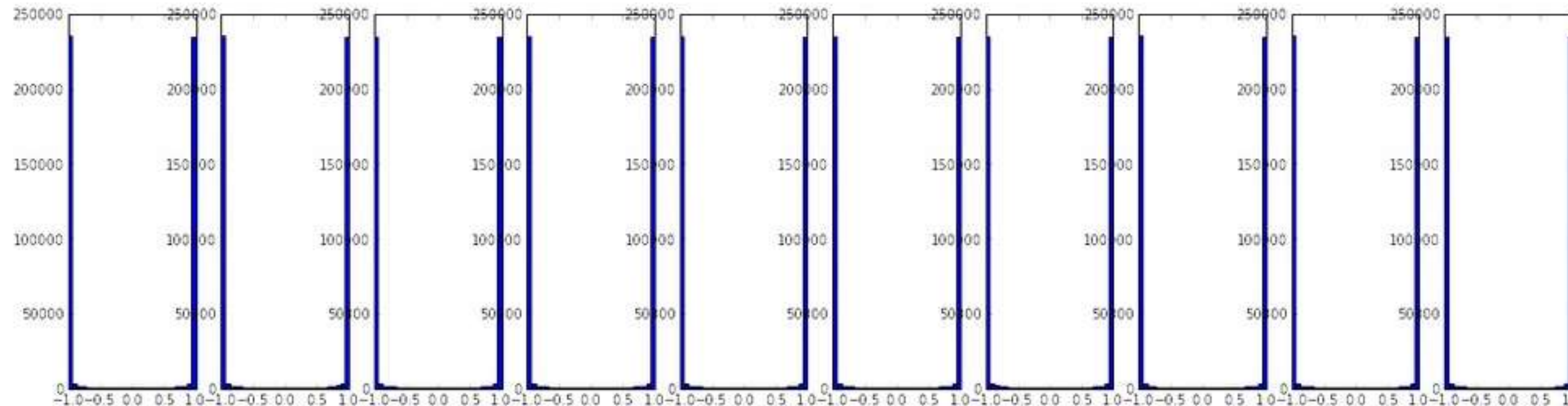
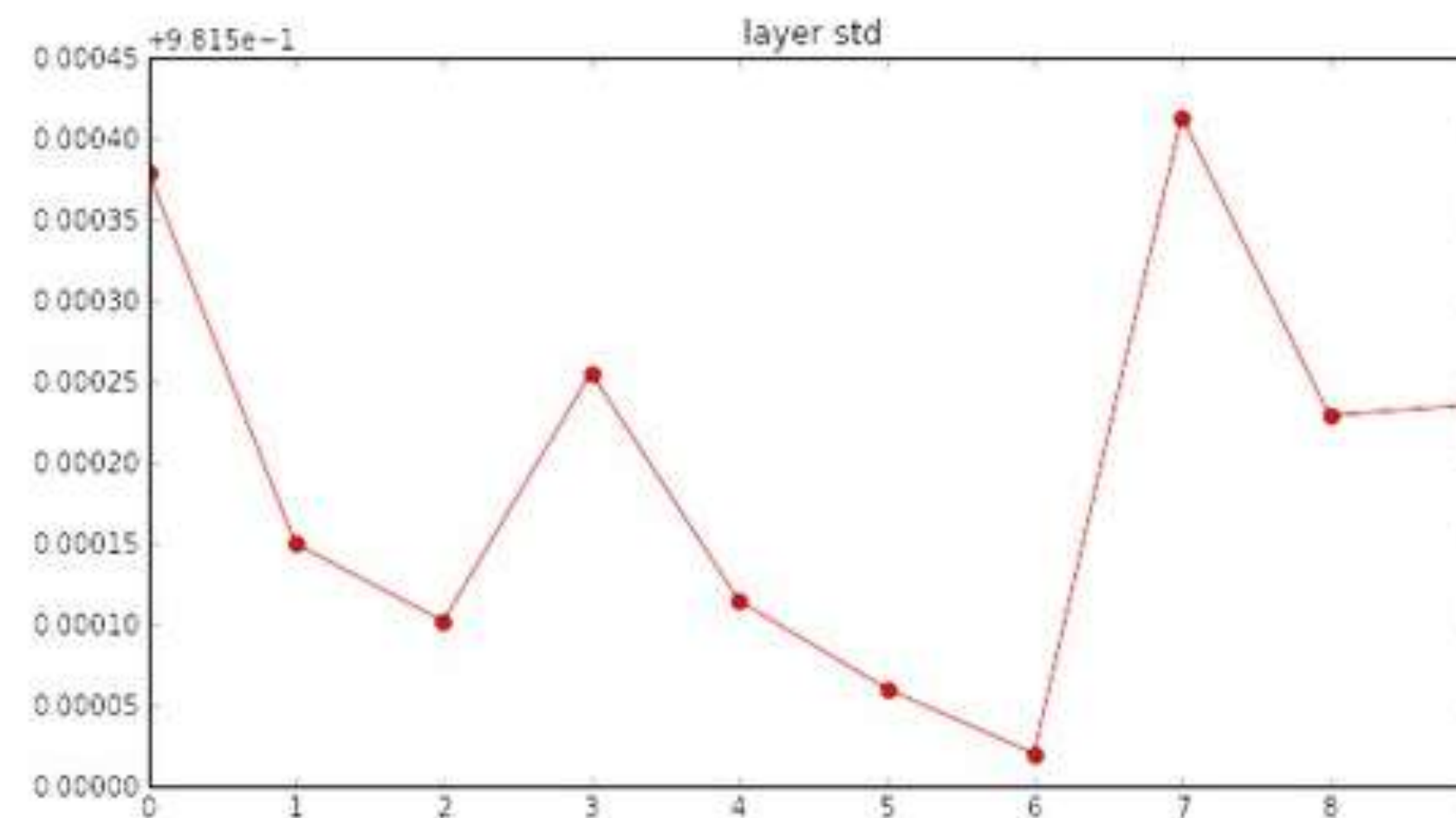
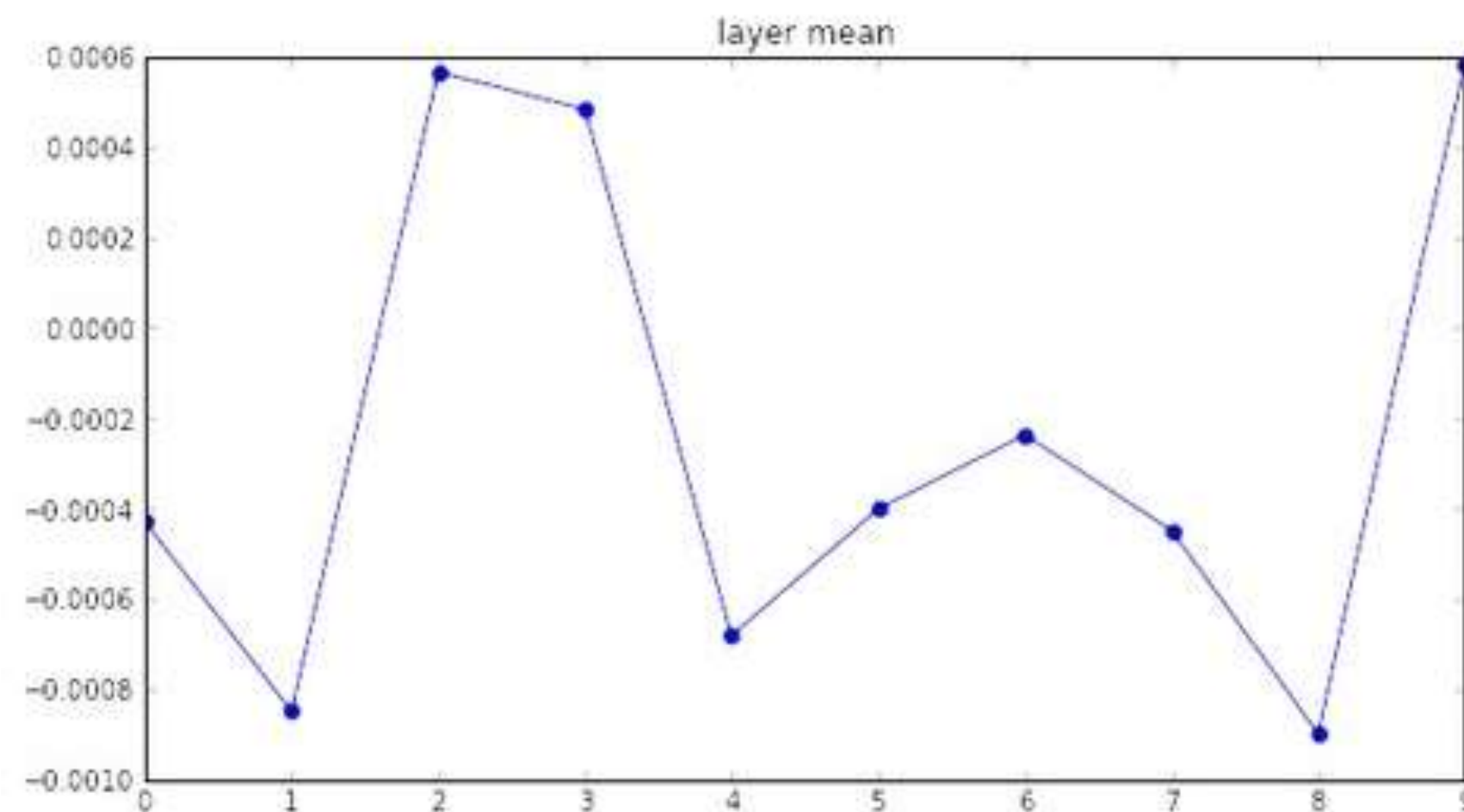


# Weight initialization

A look into ways things can go wrong

```
W = np.random.randn(fan_in, fan_out) * 1.0 # layer initialization
```

\*1.0 instead of \*0.01



Almost all neurons  
completely saturated,  
either -1 and 1.  
Gradients will be all  
zero.

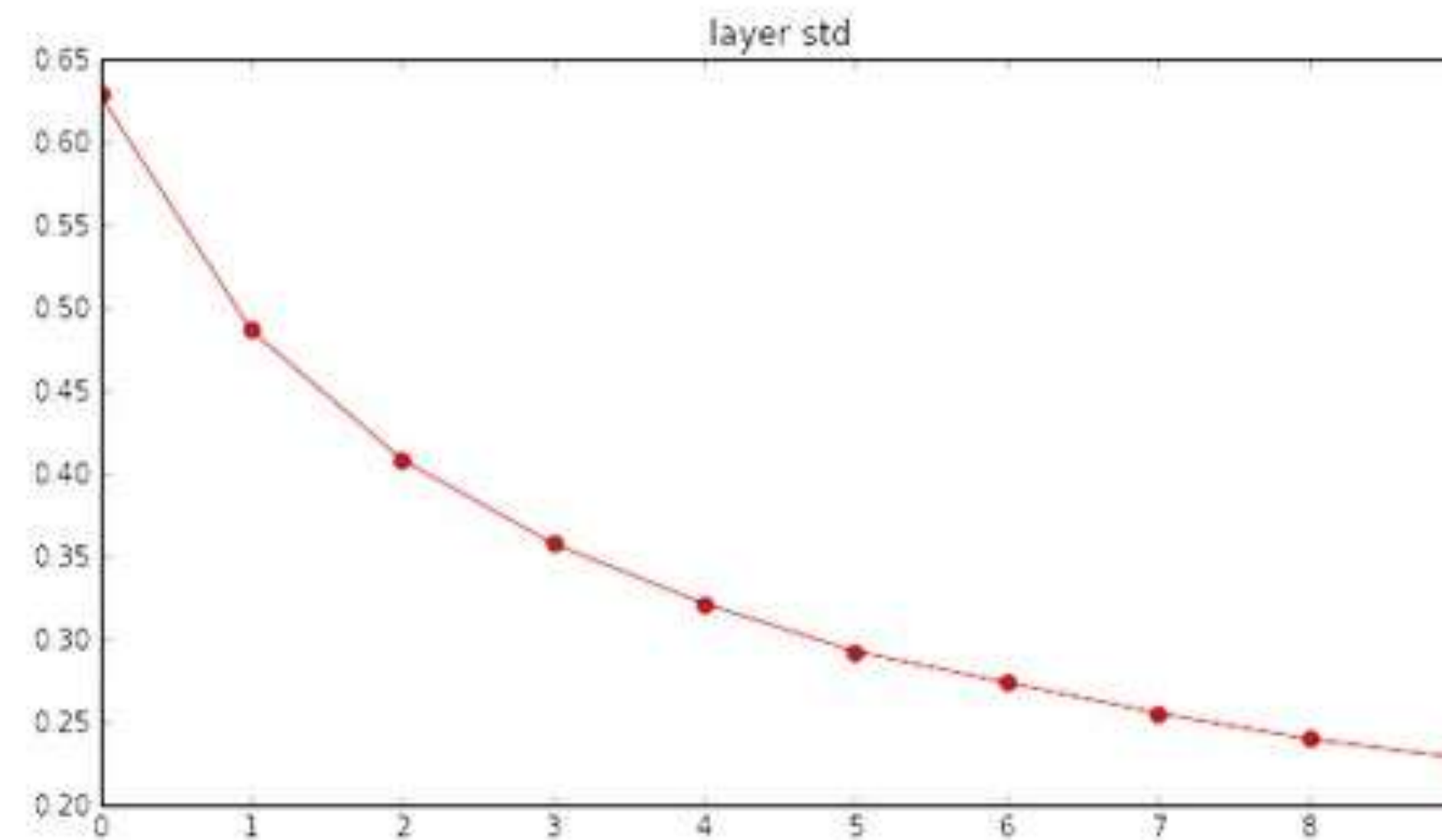
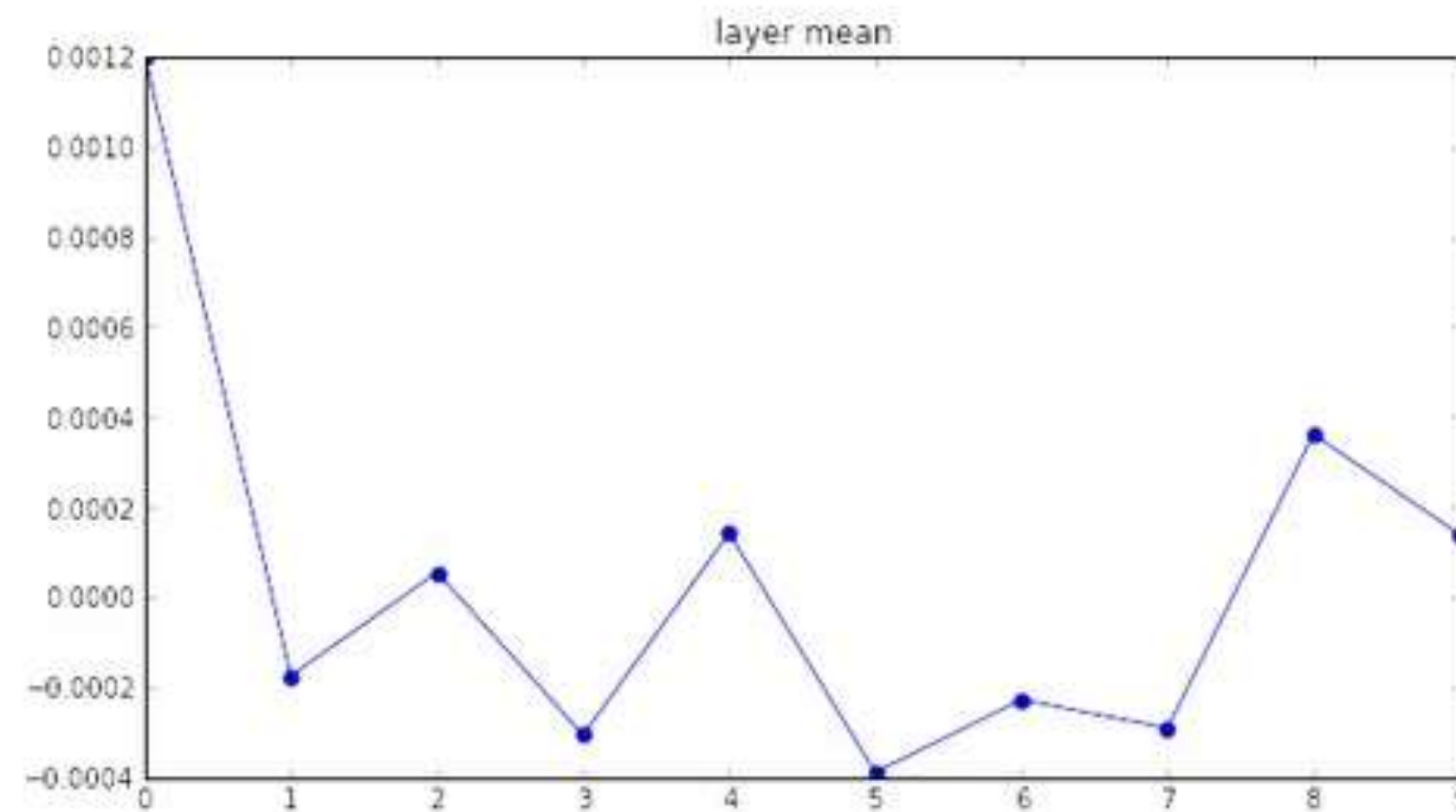


# Weight initialization

Glorot initialization [Glorot et al., 2010]

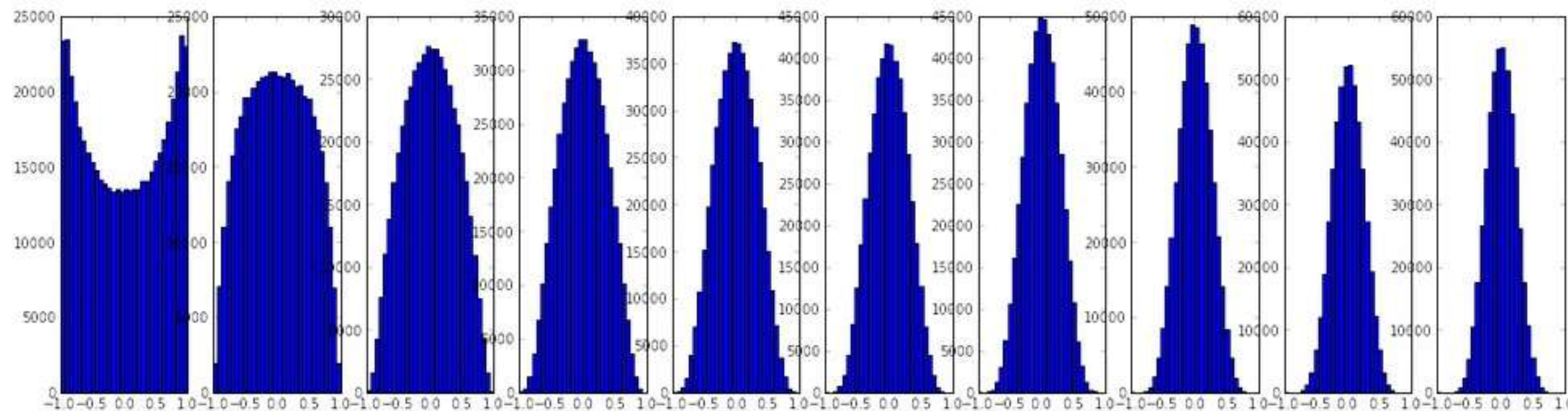
```
W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in) # layer initialization
```

Some number according to “*fan in*”



Statistically motivated

Good for tanh



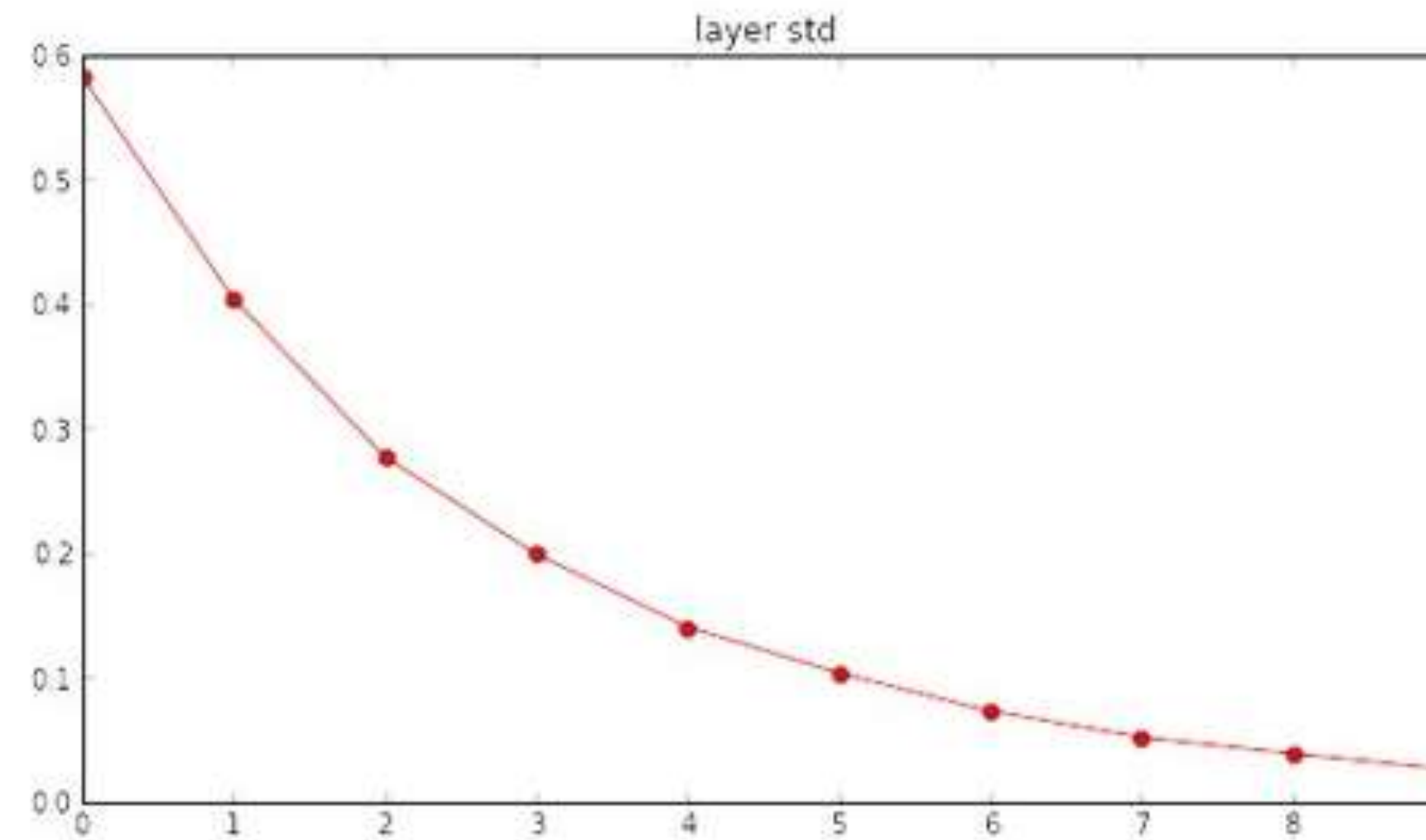
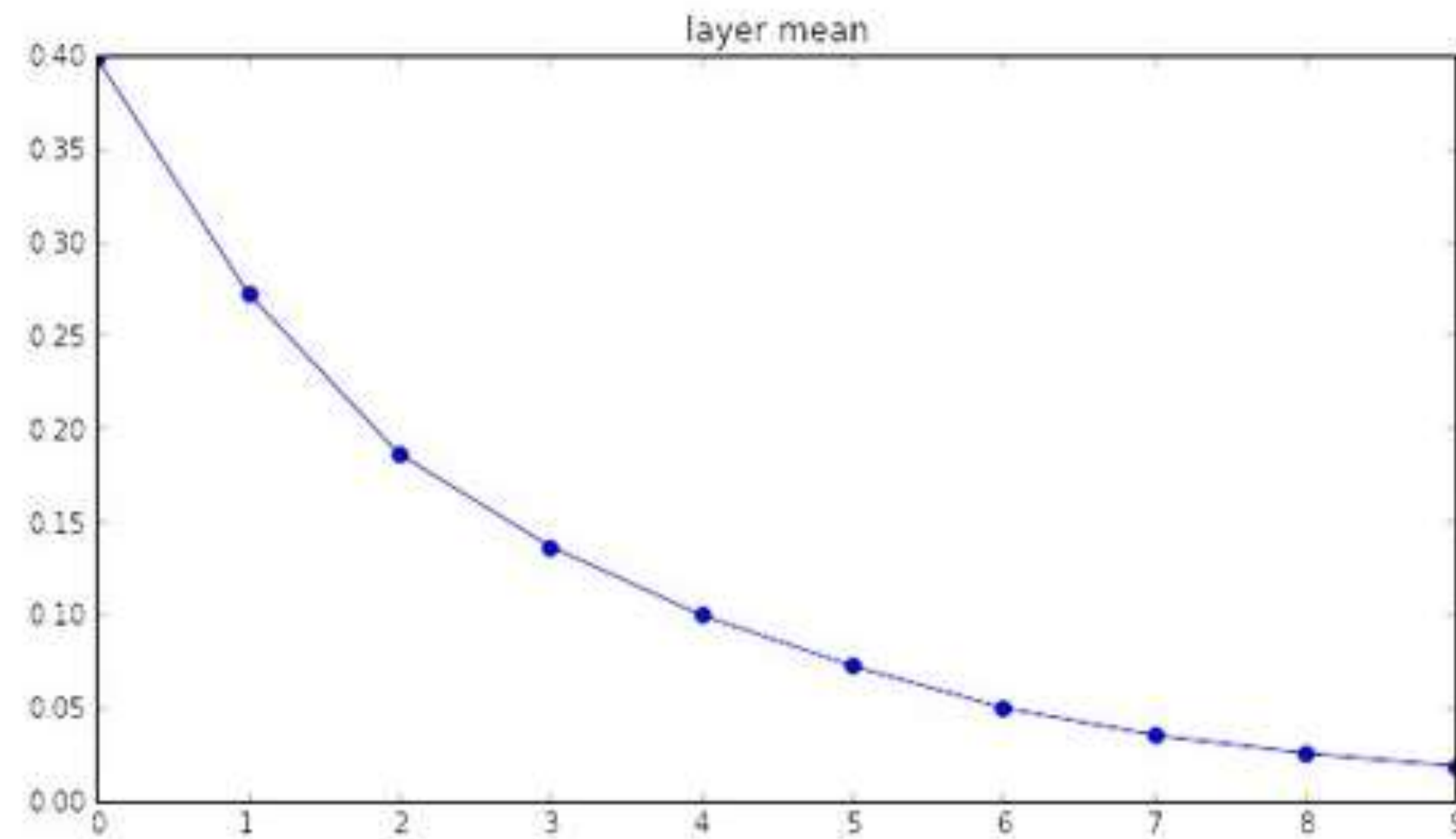


# Weight initialization

Glorot initialization [Glorot et al., 2010]

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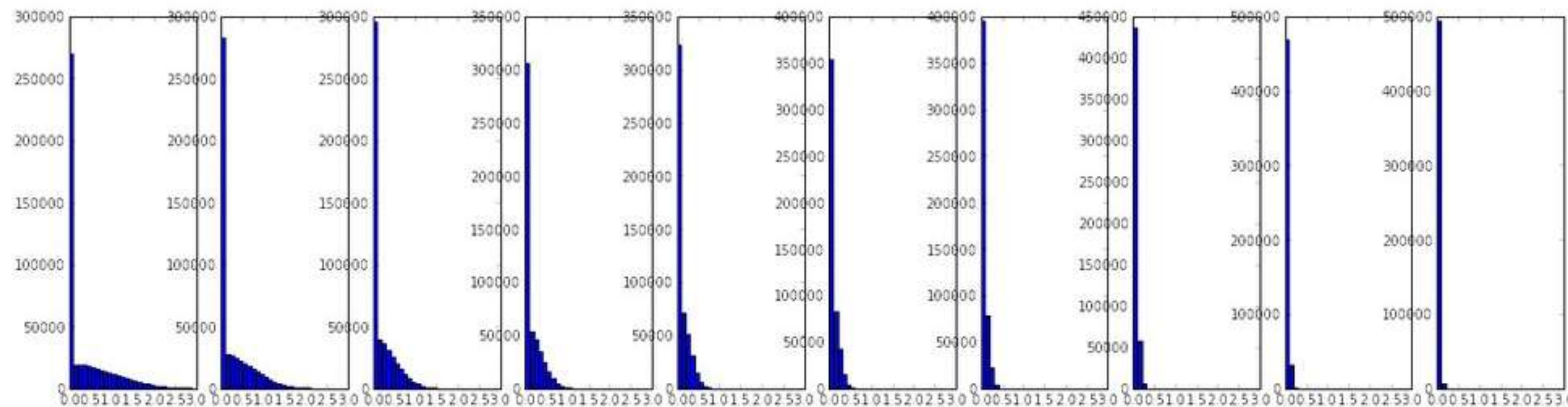
Some number according to “*fan in*”



Statistically motivated

Good for tanh

Not so good for ReLU



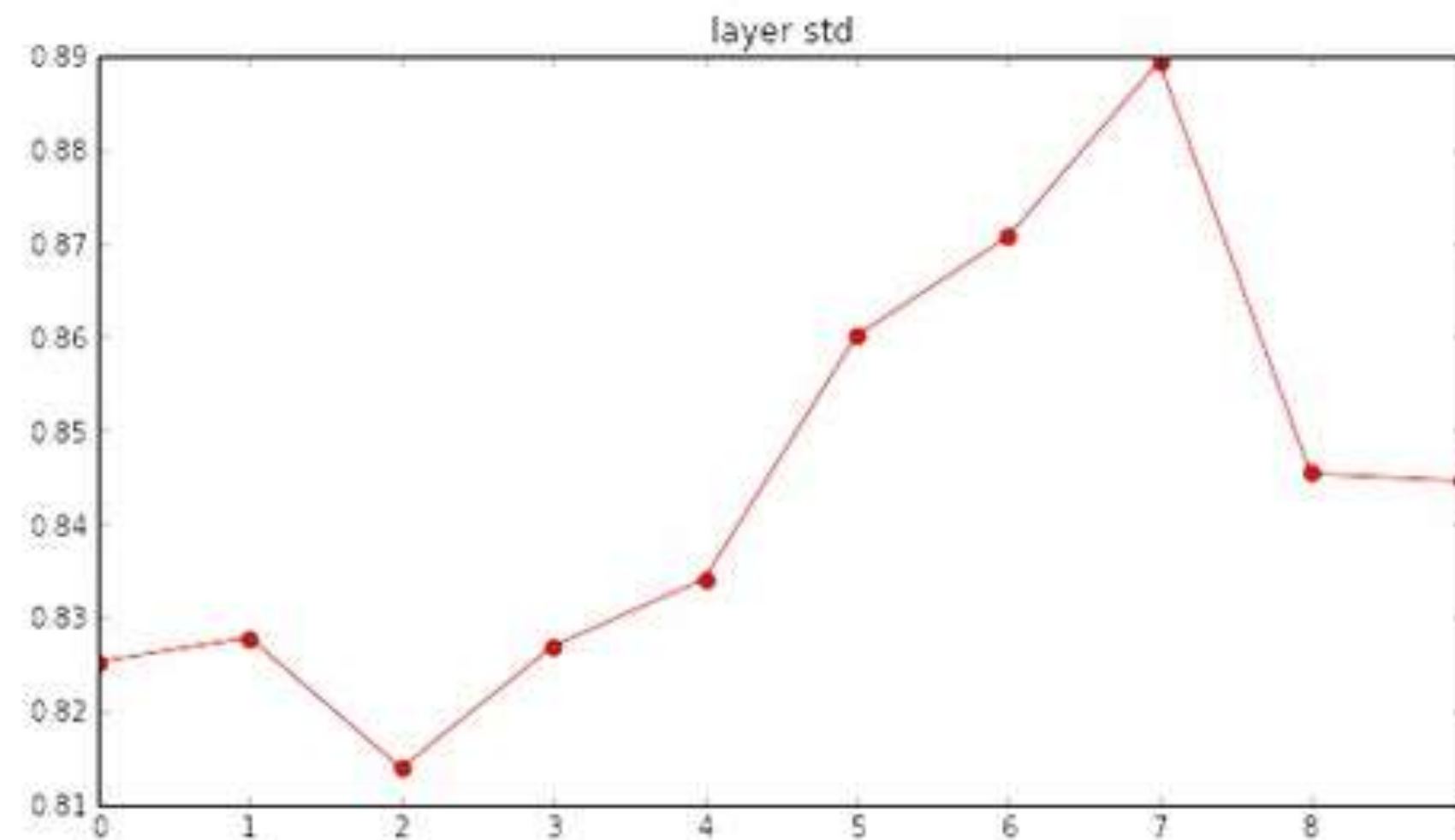
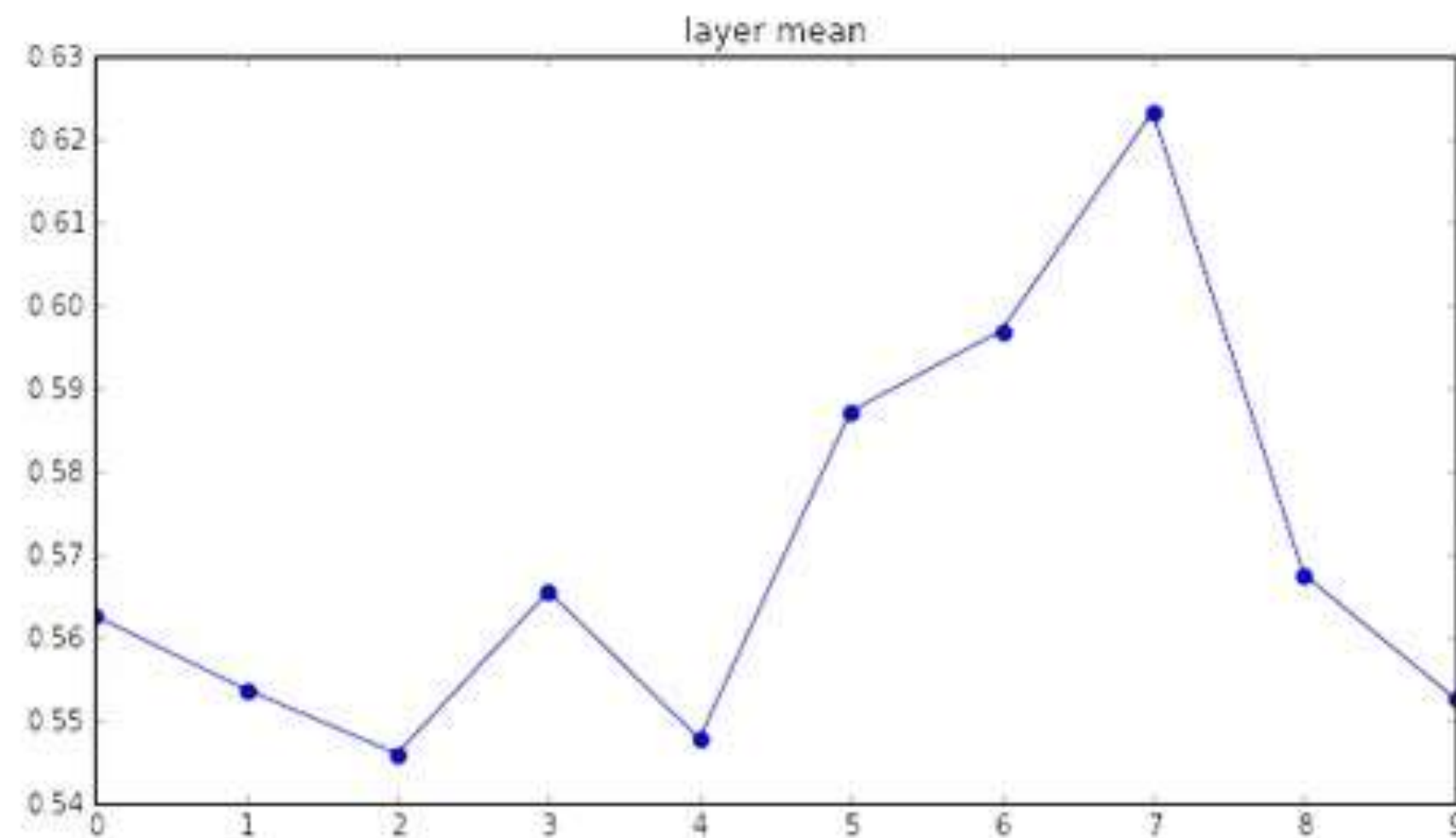


# Weight initialization

He initialization [He et al., 2015]

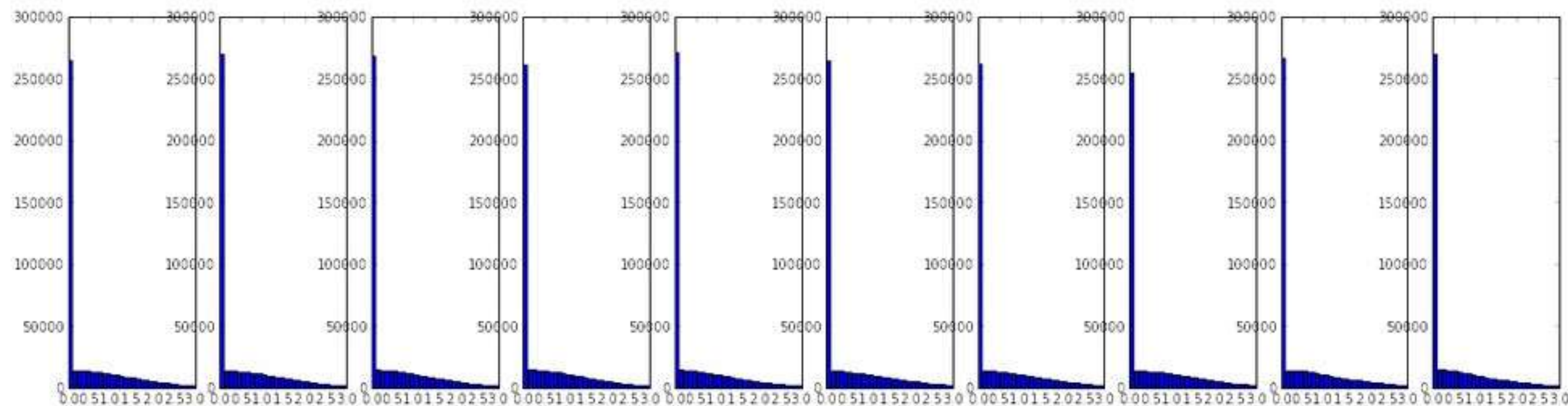
```
W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in/2) # layer initialization
```

magic number 2



Statistically motivated

Good for ReLU



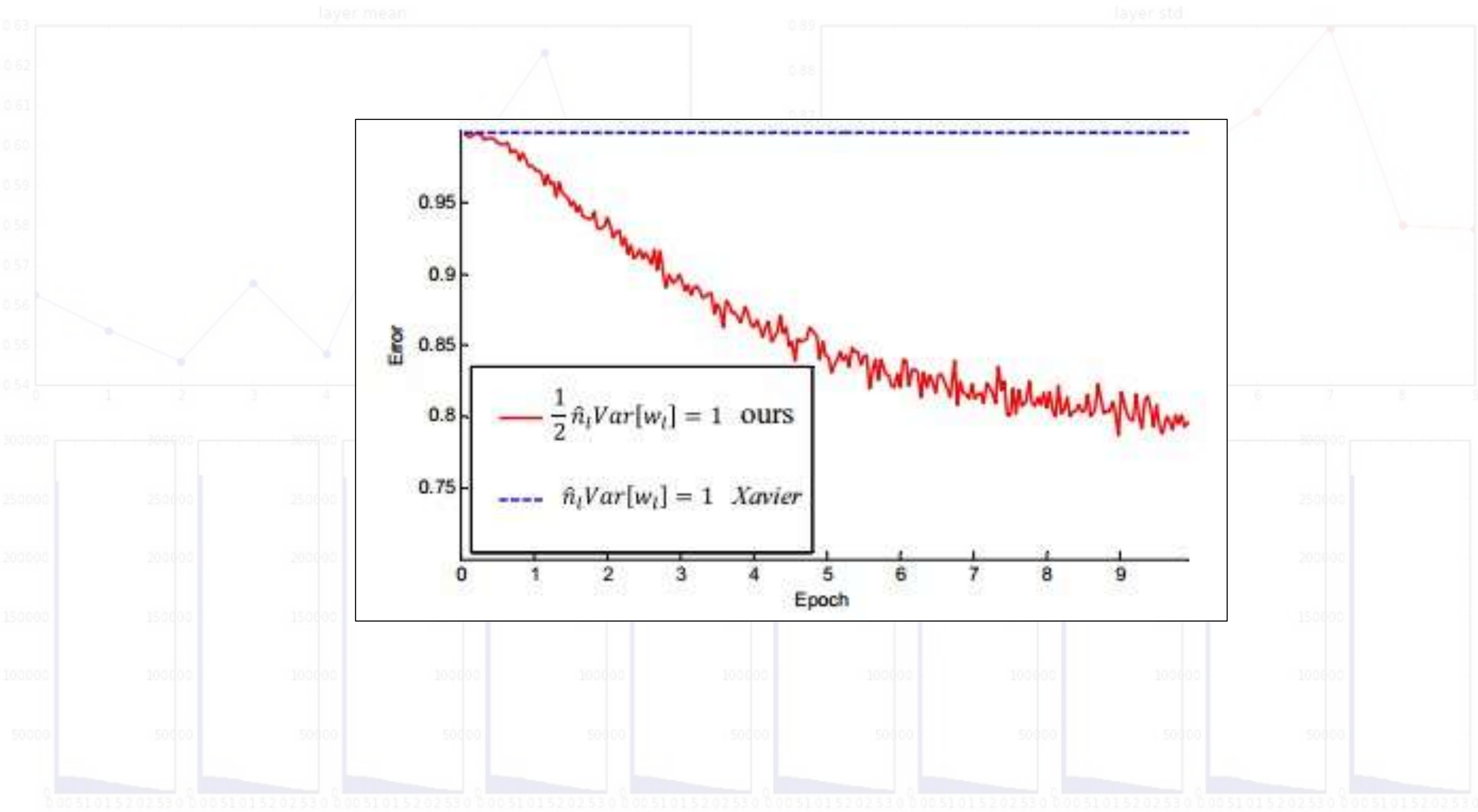


# Weight initialization

He initialization [He et al., 2015]

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W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in/2) # layer initialization
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magic number 2



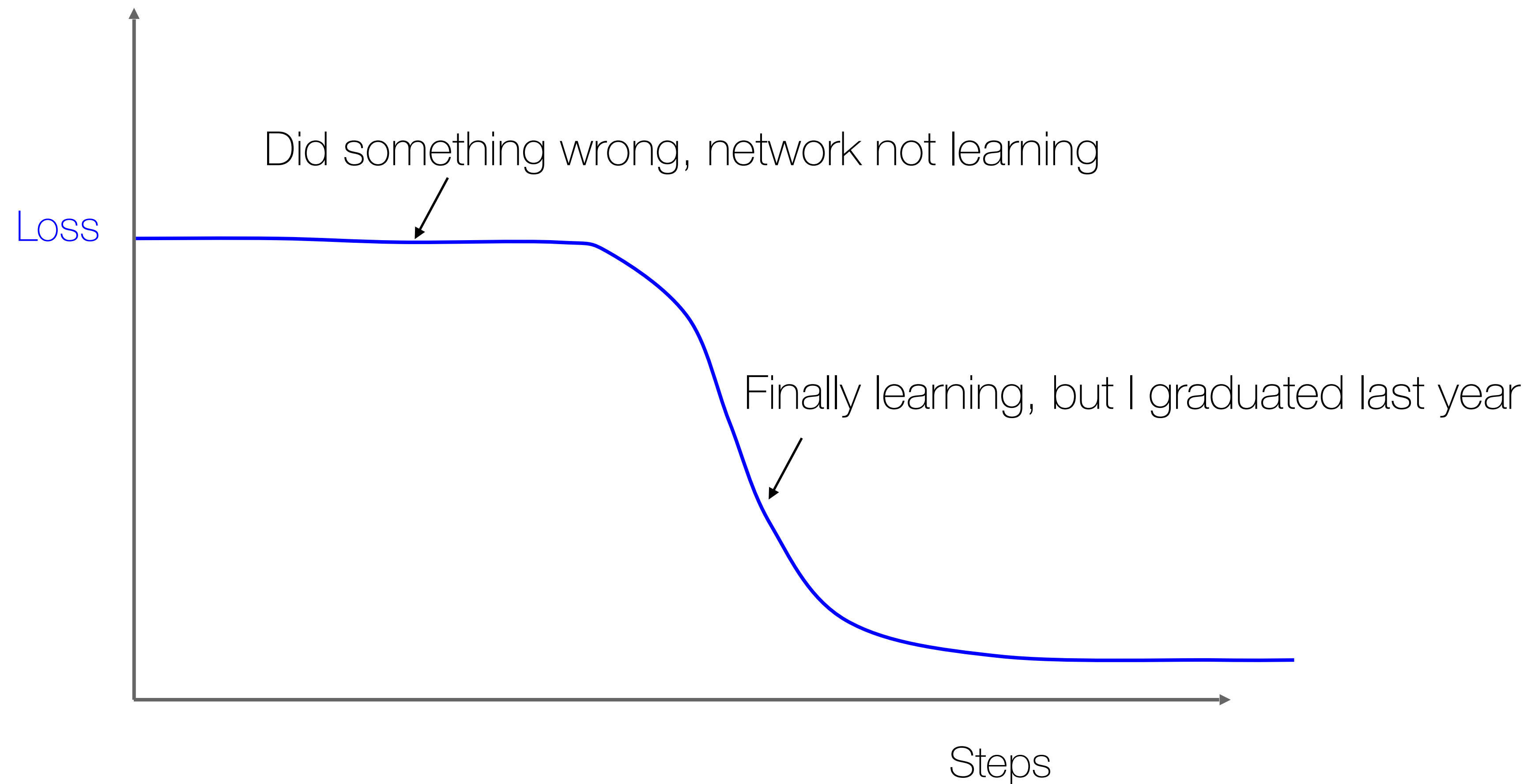
Statistically motivated

Good for ReLU



# Recall: But it is never that easy

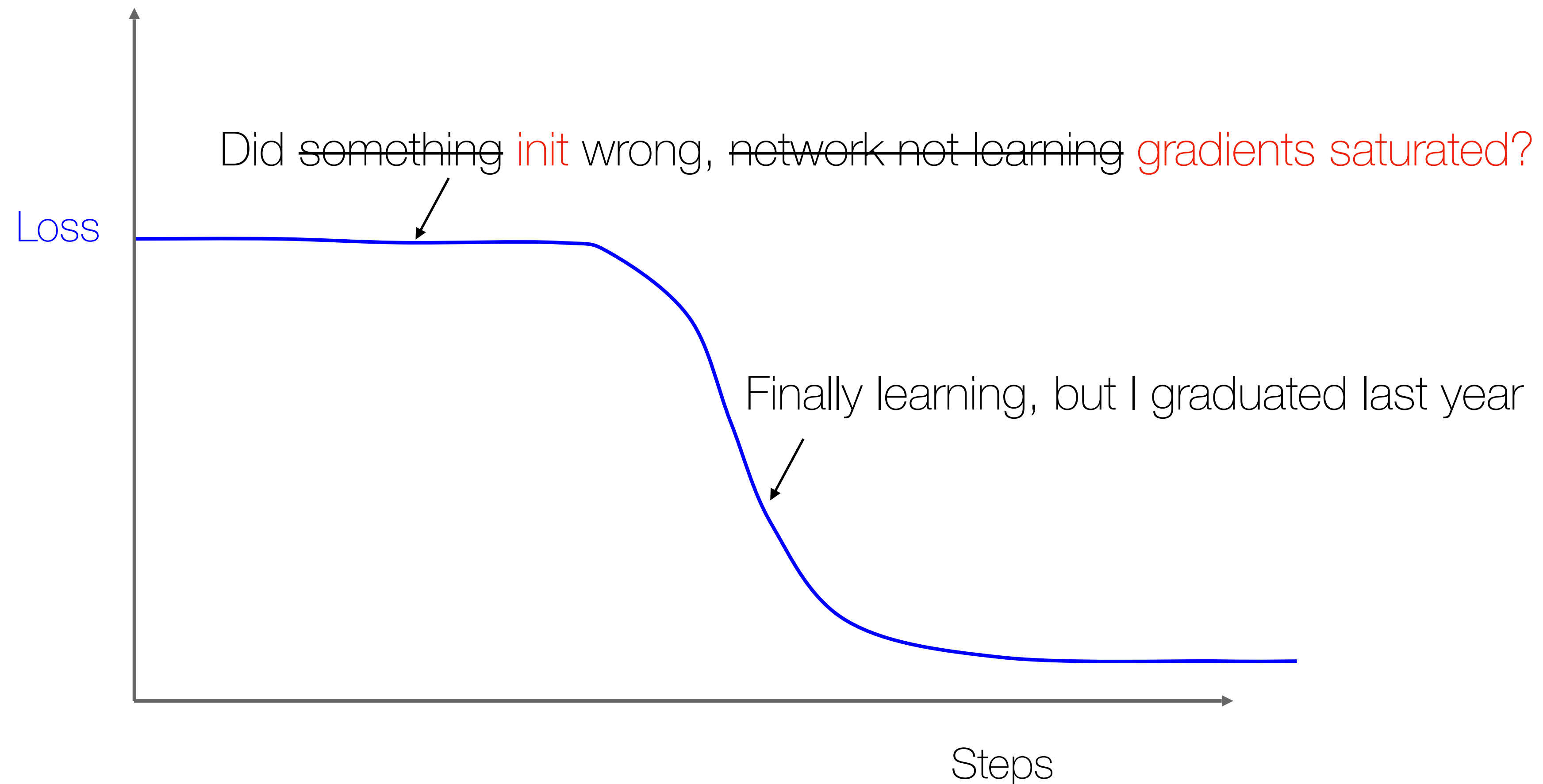
A typical sad loss curve





# Recall: But it is never that easy

A typical sad loss curve







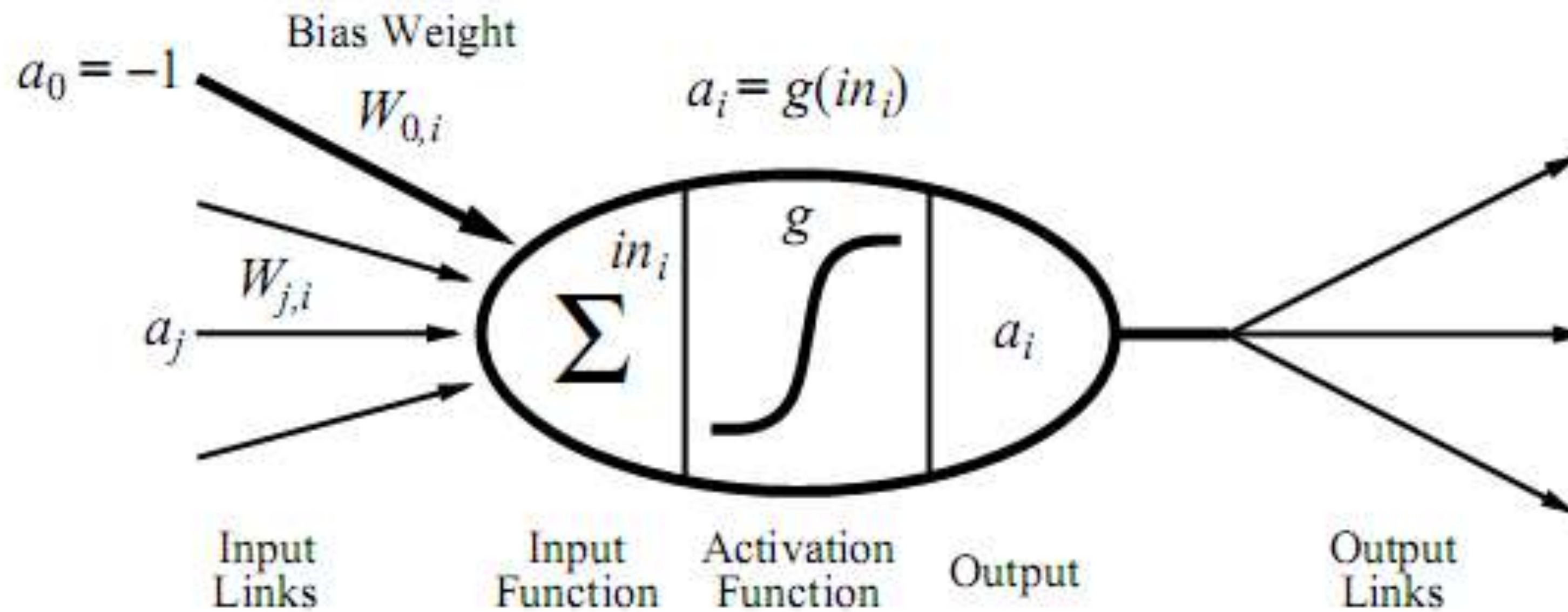
# Normalization



# Batch normalization [\[Ioffe and Szegedy, 2015\]](#)

Recall...

$$a_i \leftarrow g(in_i) = g(\sum_j W_{j,i} a_j)$$



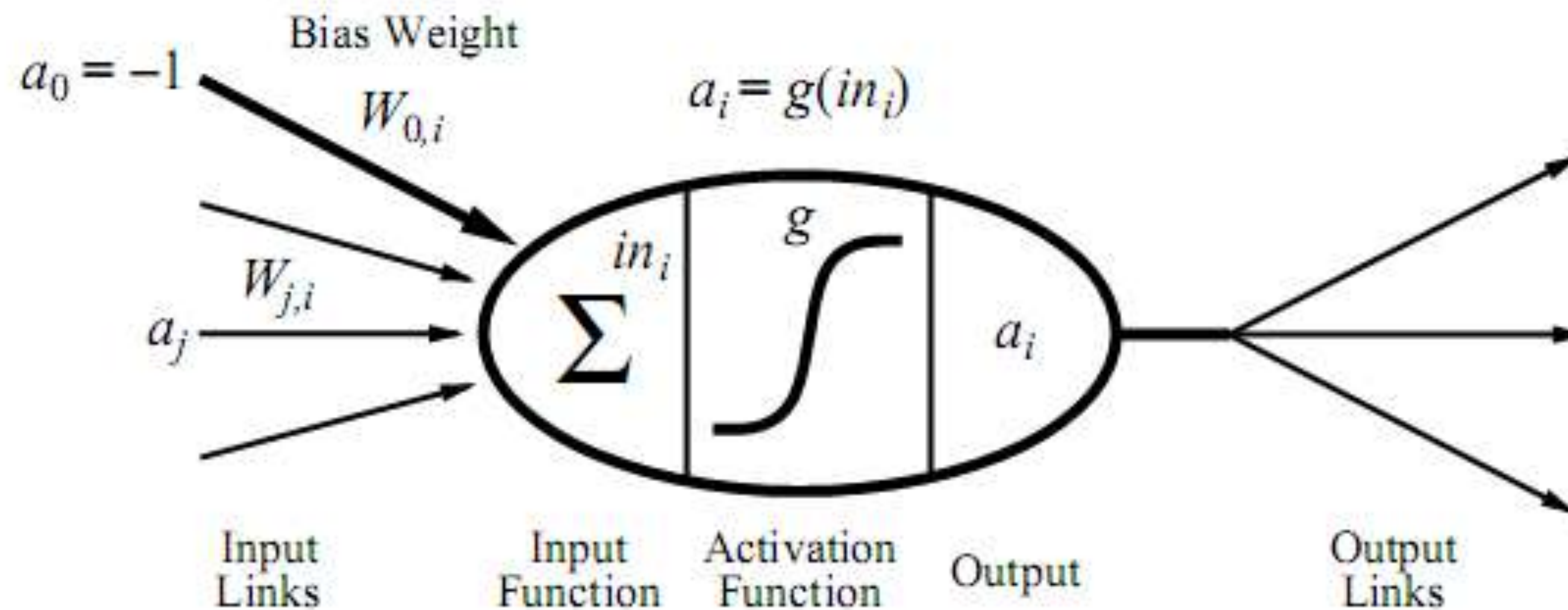


# Batch normalization [Ioffe and Szegedy, 2015]

Recall...

Linear operations should cancel out

$$a_i \leftarrow g(in_i) = g(\sum_j W_{j,i} a_j)$$





# Batch normalization [Ioffe and Szegedy, 2015]

Forcing a zero-mean and unit standard deviation

consider a batch of activations at some layer. To make each dimension unit gaussian, apply:

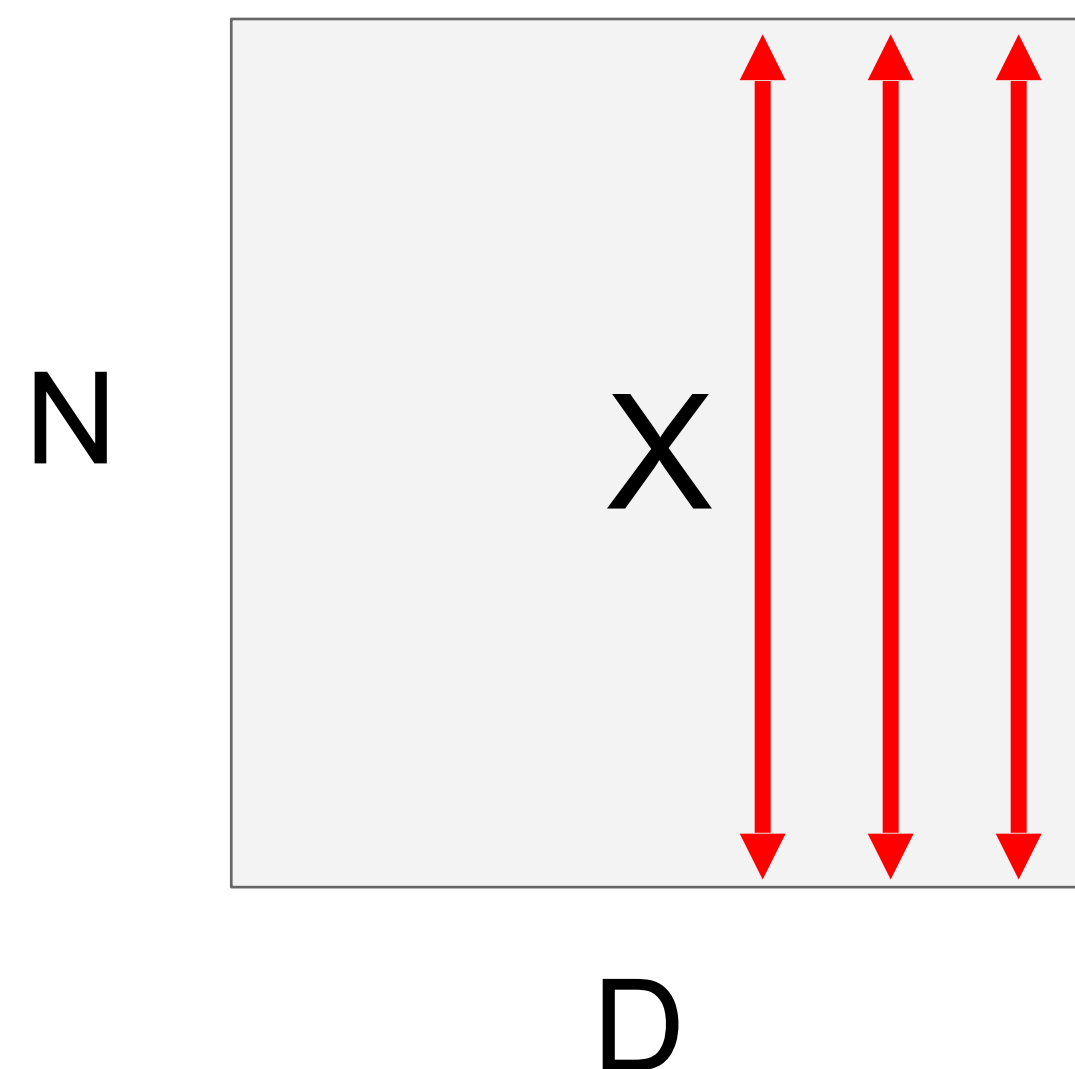
$$\hat{x}^{(k)} = \frac{x^{(k)} - \mathbb{E}[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$

this is a linear differentiable function...



# Batch normalization [Ioffe and Szegedy, 2015]

Forcing a zero-mean and unit standard deviation



1. Compute the empirical mean and variance independently for each dimension.

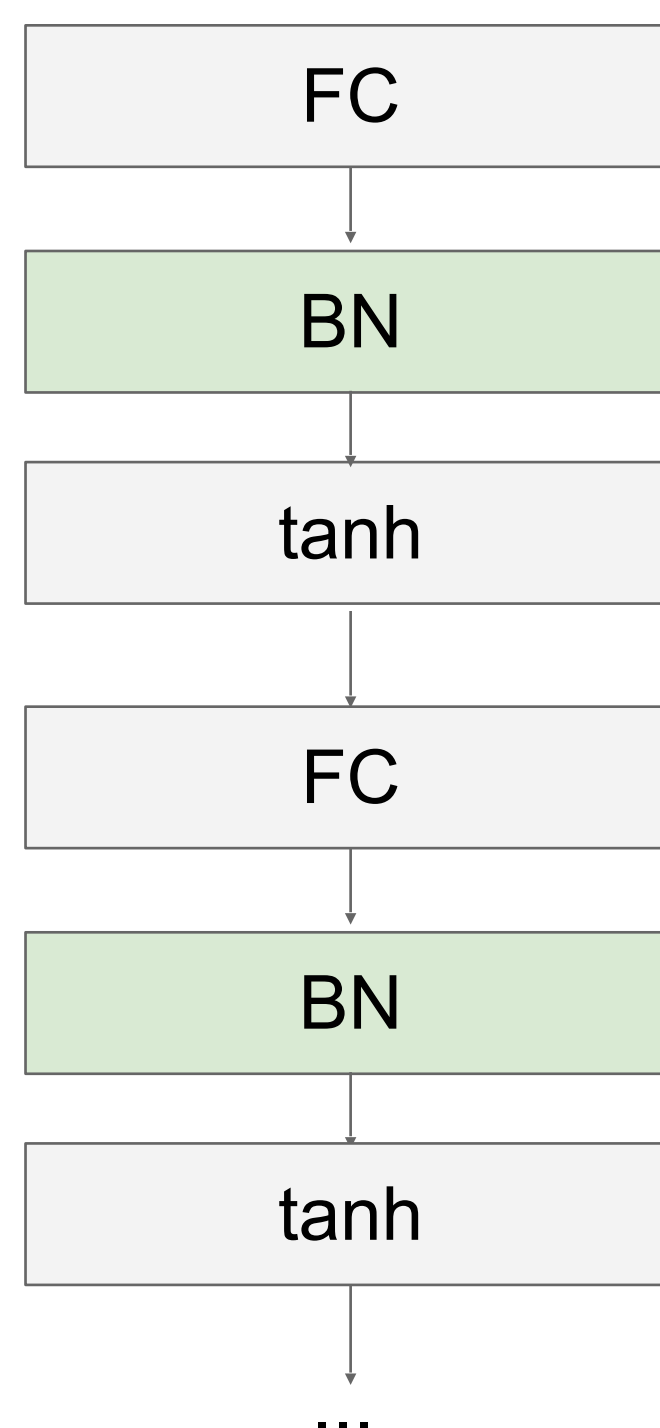
2. Normalize

$$\hat{x}^{(k)} = \frac{x^{(k)} - \mathbb{E}[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$



# Batch normalization [Ioffe and Szegedy, 2015]

Forcing a zero-mean and unit standard deviation



Usually inserted after Fully Connected or Convolutional layers, and before nonlinearity.

$$\hat{x}^{(k)} = \frac{x^{(k)} - \mathbb{E}[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$



# Batch normalization [Ioffe and Szegedy, 2015]

Introducing learnable scale / shift

$$\hat{x}^{(k)} = \frac{x^{(k)} - \mathbf{E}[x^{(k)}]}{\sqrt{\mathbf{Var}[x^{(k)}]}}$$

And then allow the network to squash the range if it wants to:

$$y^{(k)} = \gamma^{(k)} \hat{x}^{(k)} + \beta^{(k)}$$

Note, the network can learn:

$$\gamma^{(k)} = \sqrt{\mathbf{Var}[x^{(k)}]}$$

$$\beta^{(k)} = \mathbf{E}[x^{(k)}]$$

to recover the identity mapping.



# Batch normalization [Ioffe and Szegedy, 2015]

Introducing learnable scale / shift

IMPORTANT: At test time, we don't have these — use training time stats

$$\hat{x}^{(k)} = \frac{x^{(k)} - \mathbf{E}[x^{(k)}]}{\sqrt{\mathbf{Var}[x^{(k)}]}}$$

And then allow the network to squash the range if it wants to:

$$y^{(k)} = \gamma^{(k)} \hat{x}^{(k)} + \beta^{(k)}$$

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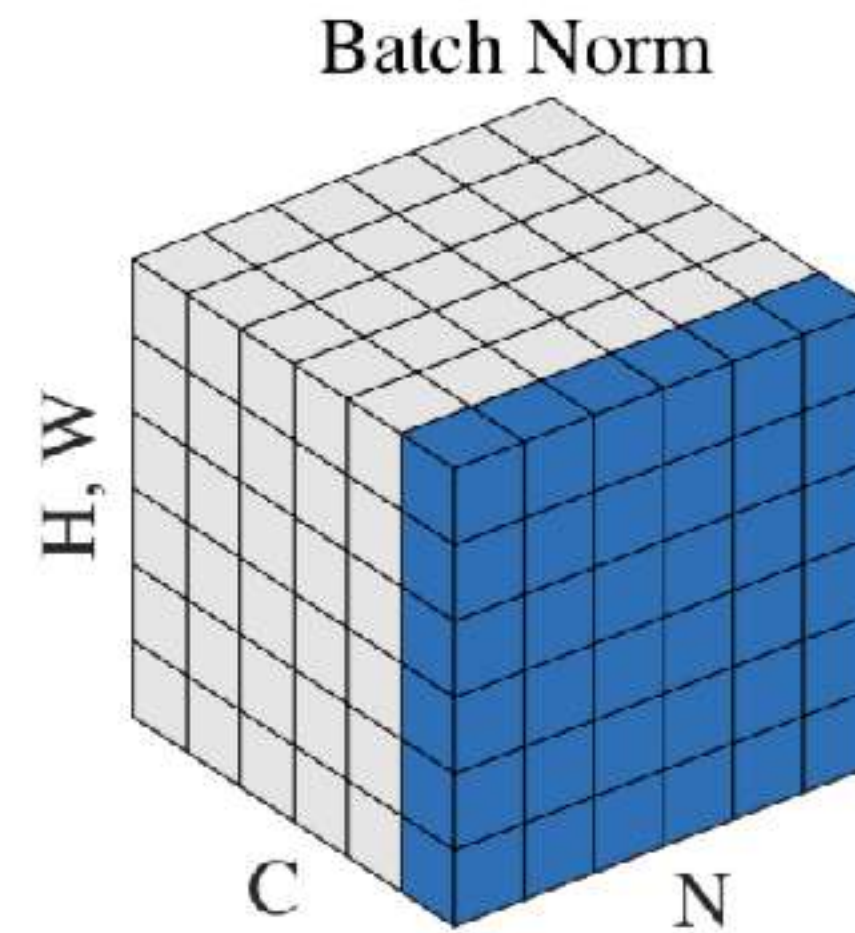
to recover the identity mapping.



# Other normalization techniques

## Batch Normalization

Skipped in class  
(outside of scope)





Skipped in class  
(outside of scope)

# Other normalization techniques

## Batch Normalization

Batch Normalization for  
**fully-connected** networks

$$\begin{aligned}
 &\mathbf{x} : \mathbf{N} \times \mathbf{D} \\
 &\text{Normalize} \quad \downarrow \\
 &\boldsymbol{\mu}, \boldsymbol{\sigma} : \mathbf{1} \times \mathbf{D} \\
 &\boldsymbol{\gamma}, \boldsymbol{\beta} : \mathbf{1} \times \mathbf{D} \\
 &\mathbf{y} = \boldsymbol{\gamma}(\mathbf{x} - \boldsymbol{\mu}) / \boldsymbol{\sigma} + \boldsymbol{\beta}
 \end{aligned}$$

Batch Normalization for  
**convolutional** networks  
(Spatial Batchnorm, BatchNorm2D)

$$\begin{aligned}
 &\mathbf{x} : \mathbf{N} \times \mathbf{C} \times \mathbf{H} \times \mathbf{W} \\
 &\text{Normalize} \quad \downarrow \quad \downarrow \quad \downarrow \\
 &\boldsymbol{\mu}, \boldsymbol{\sigma} : \mathbf{1} \times \mathbf{C} \times \mathbf{1} \times \mathbf{1} \\
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 \end{aligned}$$



Skipped in class  
(outside of scope)

# Other normalization techniques

## Batch Normalization

Batch Normalization for  
**fully-connected** networks

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Batch Normalization for  
**convolutional** networks  
(Spatial Batchnorm, BatchNorm2D)

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 \end{aligned}$$

This is why train/test needs to be different



Skipped in class  
(outside of scope)

# Other normalization techniques

## Batch Normalization

Batch Normalization for  
**fully-connected** networks

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Batch Normalization for  
**convolutional** networks  
(Spatial Batchnorm, BatchNorm2D)

$$\begin{aligned}
 &\mathbf{x} : \mathbf{N} \times \mathbf{C} \times \mathbf{H} \times \mathbf{W} \\
 &\text{Normalize} \\
 &\boldsymbol{\mu}, \boldsymbol{\sigma} : \mathbf{1} \times \mathbf{C} \times \mathbf{1} \times \mathbf{1} \\
 &\boldsymbol{\gamma}, \boldsymbol{\beta} : \mathbf{1} \times \mathbf{C} \times \mathbf{1} \times \mathbf{1} \\
 &\mathbf{y} = \boldsymbol{\gamma}(\mathbf{x} - \boldsymbol{\mu}) / \boldsymbol{\sigma} + \boldsymbol{\beta}
 \end{aligned}$$

Always watch out when implementing!!!

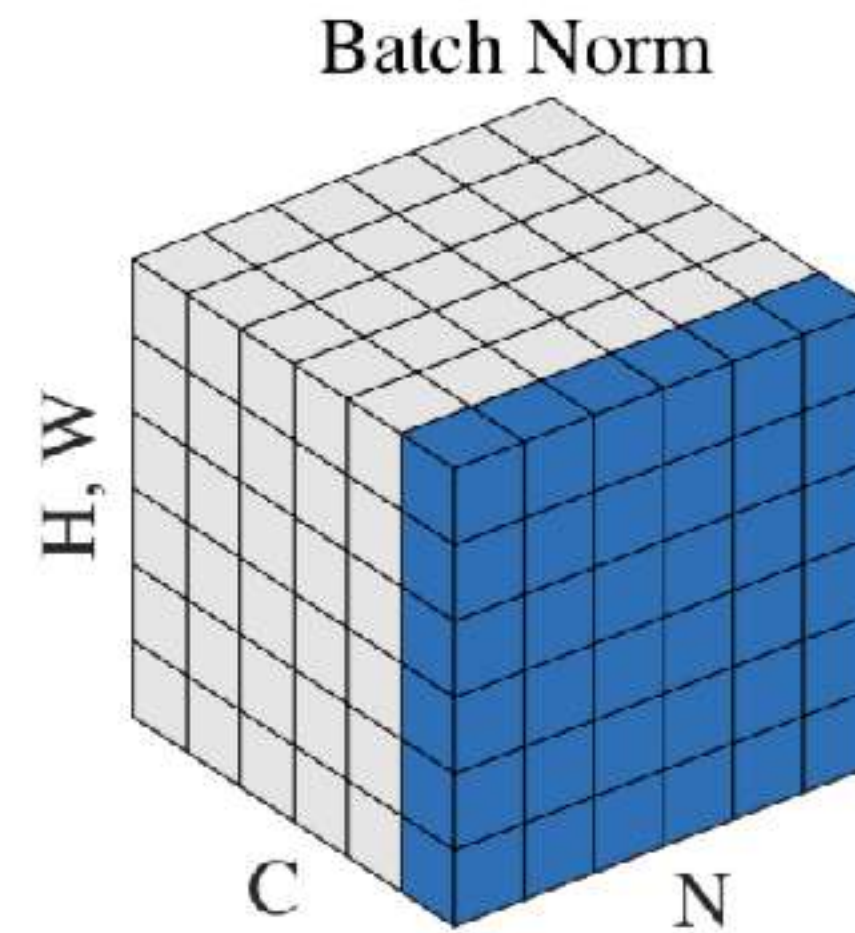
This is why train/test needs to be different



# Other normalization techniques

## Batch Normalization

Skipped in class  
(outside of scope)

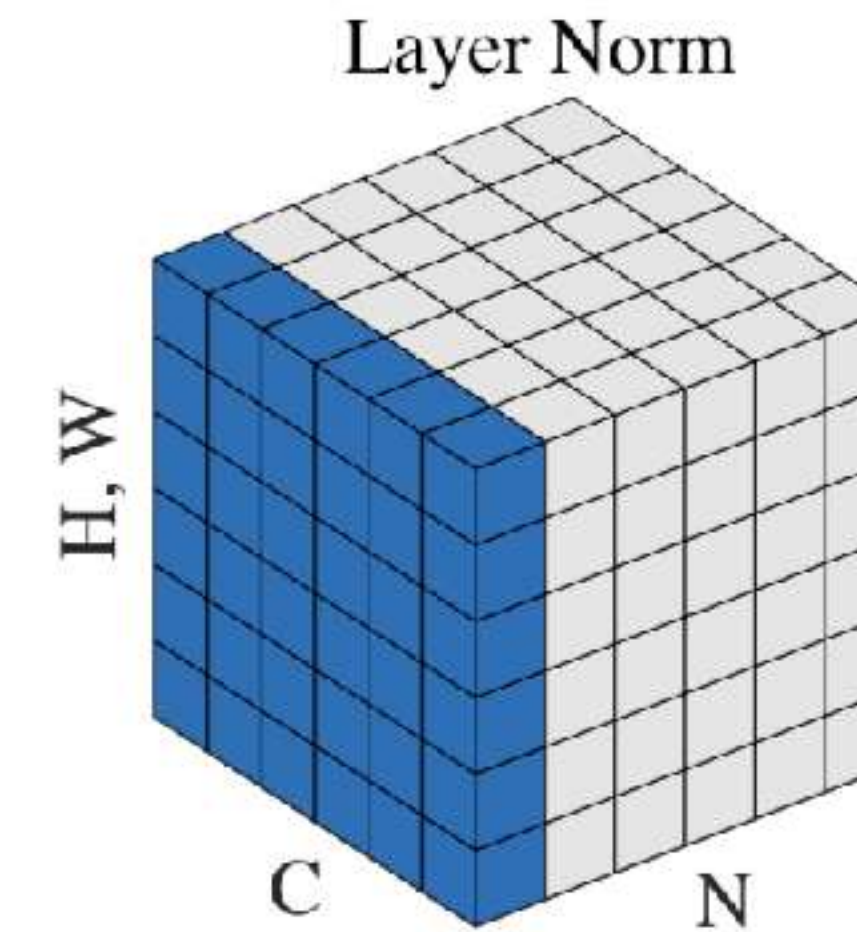
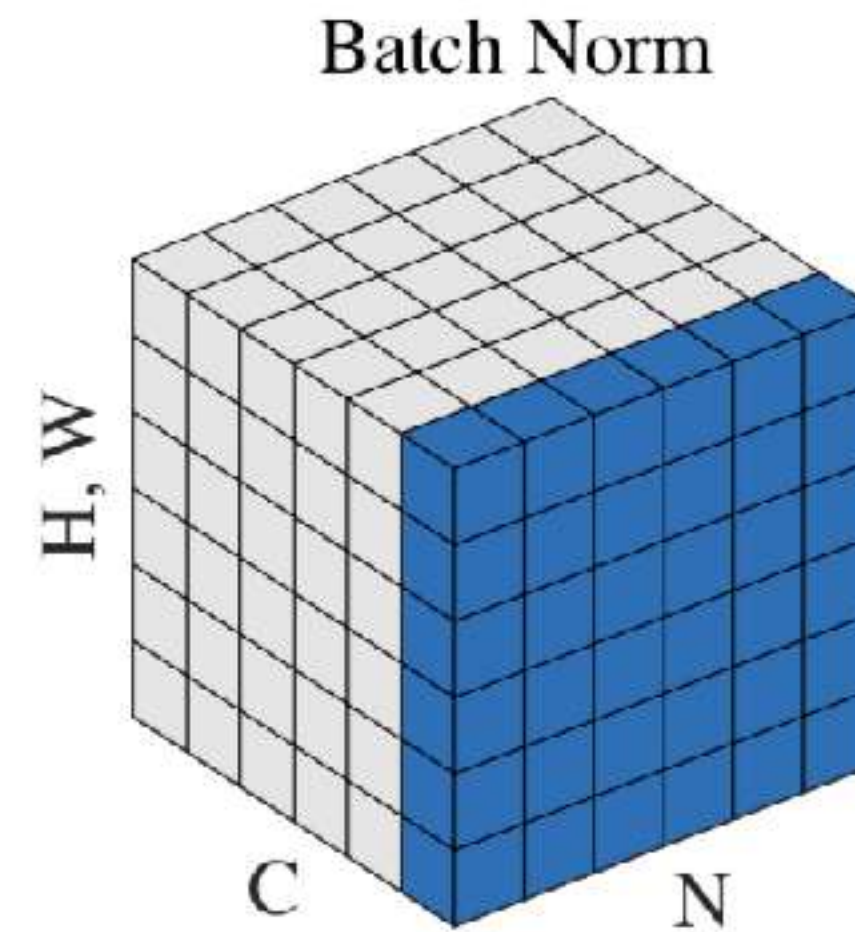




Skipped in class  
(outside of scope)

# Other normalization techniques

## Layer Normalization





Skipped in class  
(outside of scope)

# Other normalization techniques

## Layer Normalization

Batch Normalization for  
**fully-connected** networks

$$\begin{array}{l}
 \mathbf{x} : \mathbf{N} \times \mathbf{D} \\
 \text{Normalize} \quad \downarrow \\
 \boldsymbol{\mu}, \boldsymbol{\sigma} : \mathbf{1} \times \mathbf{D} \\
 \gamma, \beta : \mathbf{1} \times \mathbf{D} \\
 \mathbf{y} = \gamma(\mathbf{x} - \boldsymbol{\mu}) / \boldsymbol{\sigma} + \beta
 \end{array}$$

**Layer Normalization** for  
fully-connected networks  
Same behavior at train and test!  
Can be used in recurrent networks

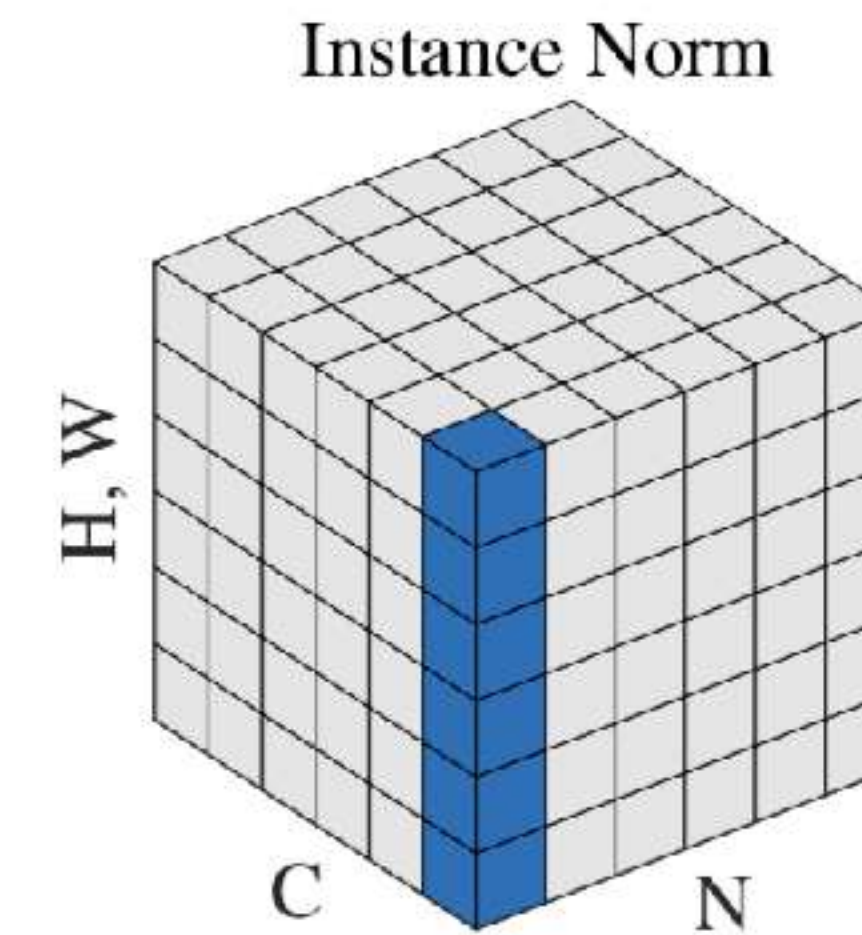
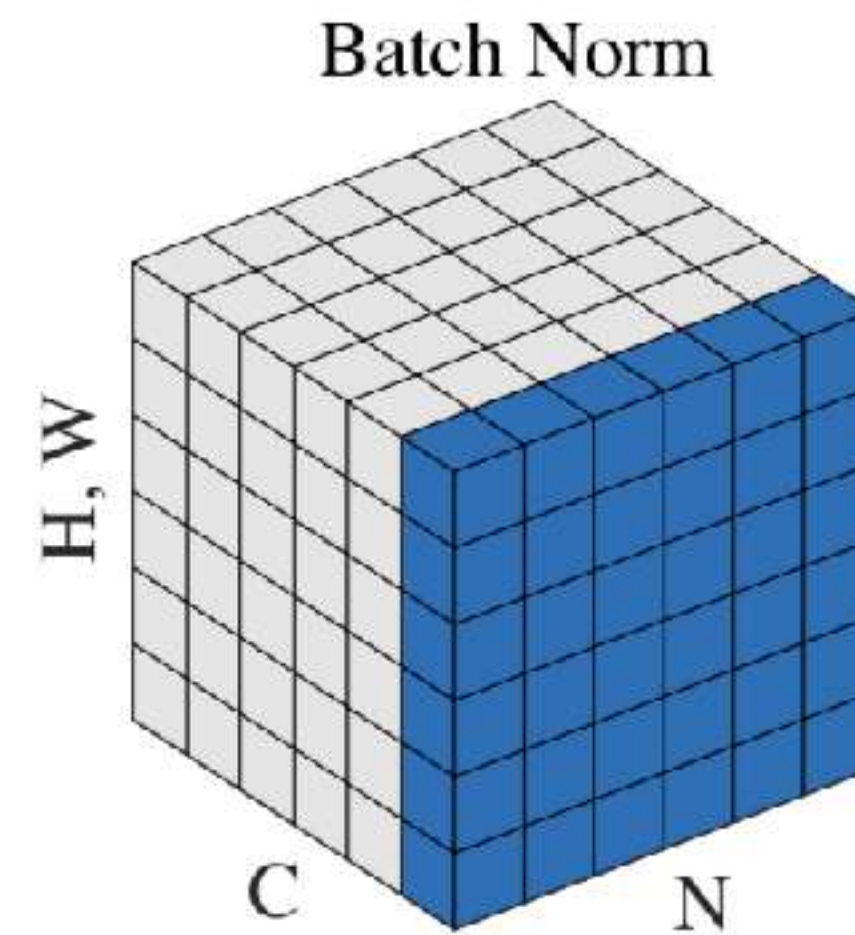
$$\begin{array}{l}
 \mathbf{x} : \mathbf{N} \times \mathbf{D} \\
 \text{Normalize} \quad \downarrow \\
 \boldsymbol{\mu}, \boldsymbol{\sigma} : \mathbf{N} \times \mathbf{1} \\
 \gamma, \beta : \mathbf{1} \times \mathbf{D} \\
 \mathbf{y} = \gamma(\mathbf{x} - \boldsymbol{\mu}) / \boldsymbol{\sigma} + \beta
 \end{array}$$



Skipped in class  
(outside of scope)

# Other normalization techniques

## Instance Normalization



Skipped in class  
(outside of scope)

# Other normalization techniques

## Instance Normalization

**Batch Normalization** for  
convolutional networks

$$\begin{array}{l}
 \mathbf{x} : N \times C \times H \times W \\
 \text{Normalize} \quad \downarrow \quad \downarrow \quad \downarrow \\
 \boldsymbol{\mu}, \boldsymbol{\sigma} : 1 \times C \times 1 \times 1 \\
 \gamma, \beta : 1 \times C \times 1 \times 1 \\
 \mathbf{y} = \gamma (\mathbf{x} - \boldsymbol{\mu}) / \boldsymbol{\sigma} + \beta
 \end{array}$$

**Instance Normalization** for  
convolutional networks  
Same behavior at train / test!

$$\begin{array}{l}
 \mathbf{x} : N \times C \times H \times W \\
 \text{Normalize} \quad \downarrow \quad \downarrow \\
 \boldsymbol{\mu}, \boldsymbol{\sigma} : N \times C \times 1 \times 1 \\
 \gamma, \beta : 1 \times C \times 1 \times 1 \\
 \mathbf{y} = \gamma (\mathbf{x} - \boldsymbol{\mu}) / \boldsymbol{\sigma} + \beta
 \end{array}$$

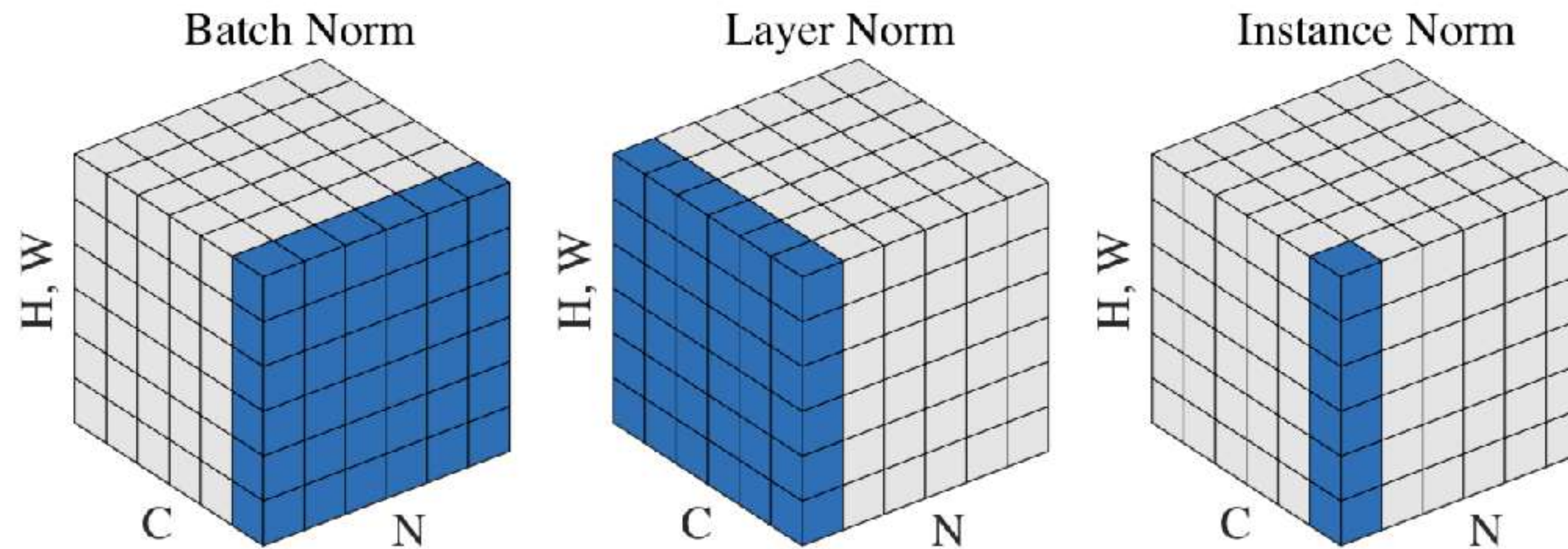
Ulyanov et al, Improved Texture Networks: Maximizing Quality and Diversity in Feed-forward Stylization and Texture Synthesis, CVPR 2017



Skipped in class  
(outside of scope)

# Other normalization techniques

## Group Normalization

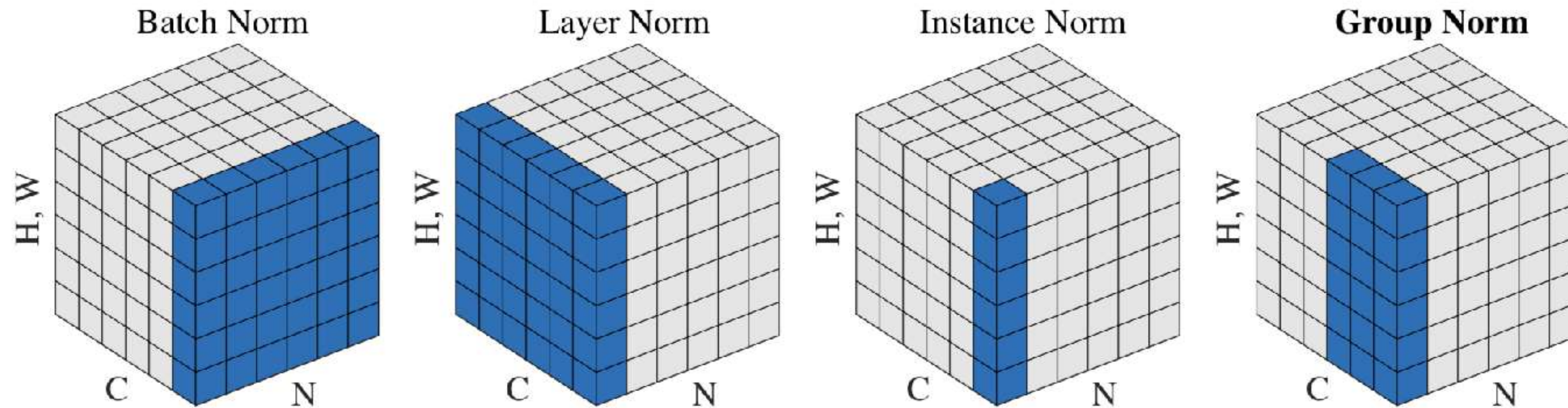




Skipped in class  
(outside of scope)

# Other normalization techniques

## Group Normalization

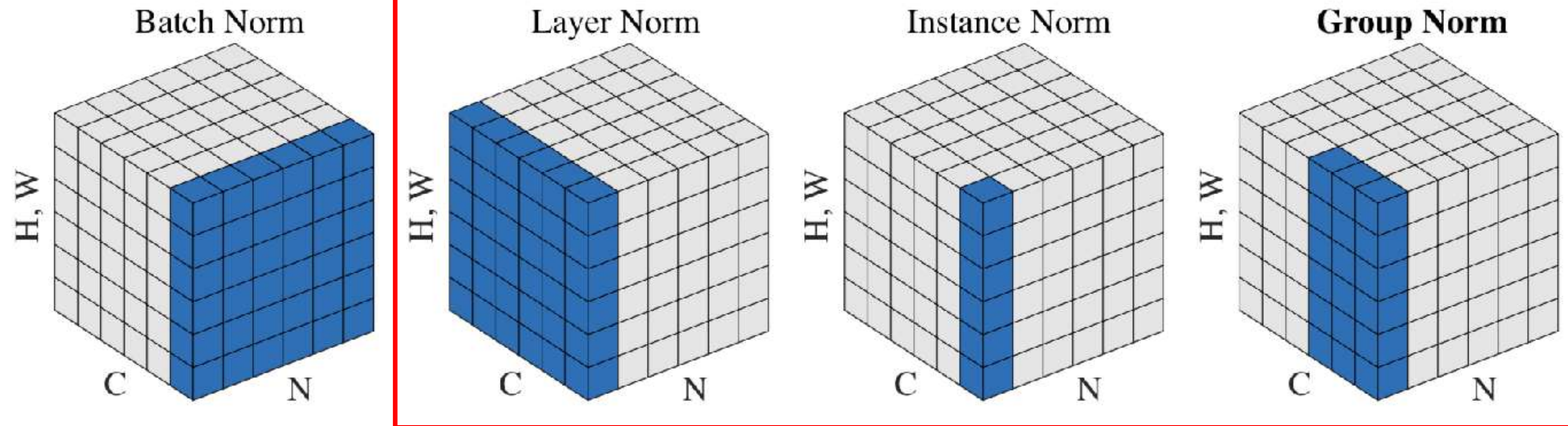




Skipped in class  
(outside of scope)

# Other normalization techniques

## Group Normalization



No train/test-time differences.

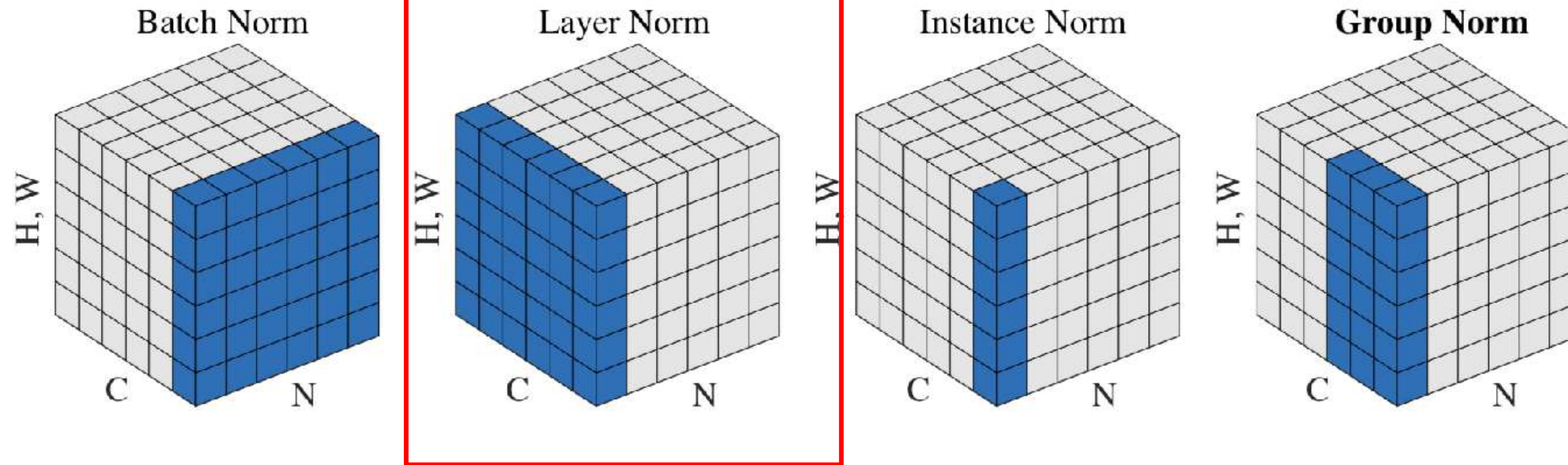
Much preferred in my opinion.



Skipped in class  
(outside of scope)

# Other normalization techniques

## Group Normalization



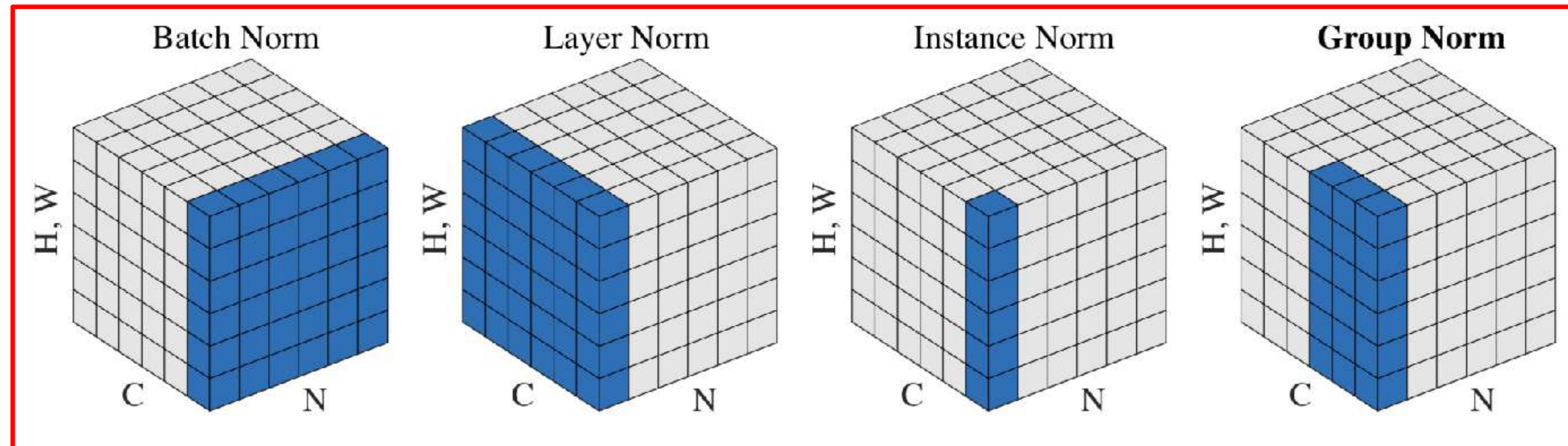
Can be implemented using PyTorch's Group norm.



Skipped in class  
(outside of scope)

# Other normalization techniques

## Group Normalization

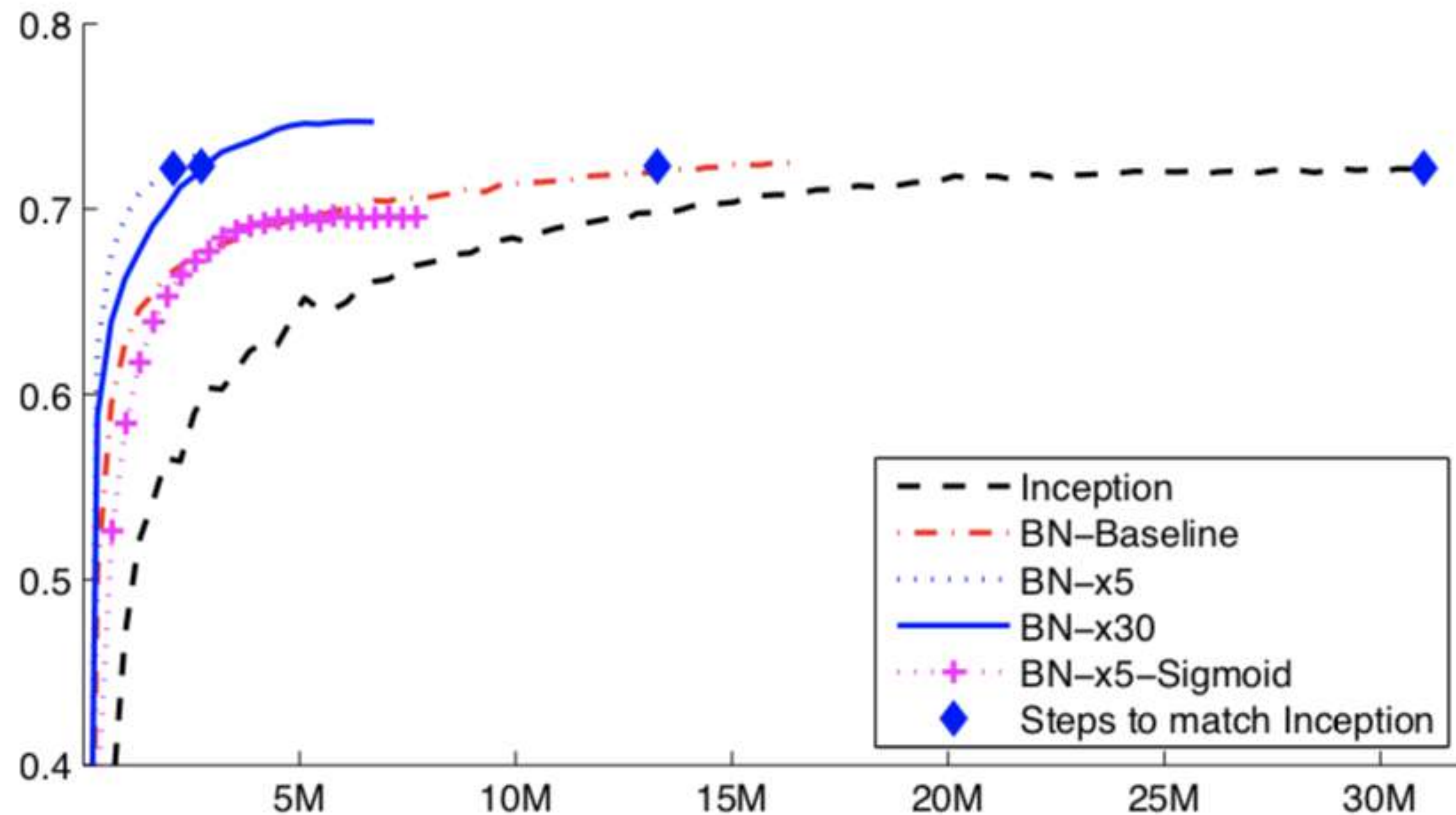


Choice of normalization should be data dependent

By the way . . . with normalization  
something else also happens

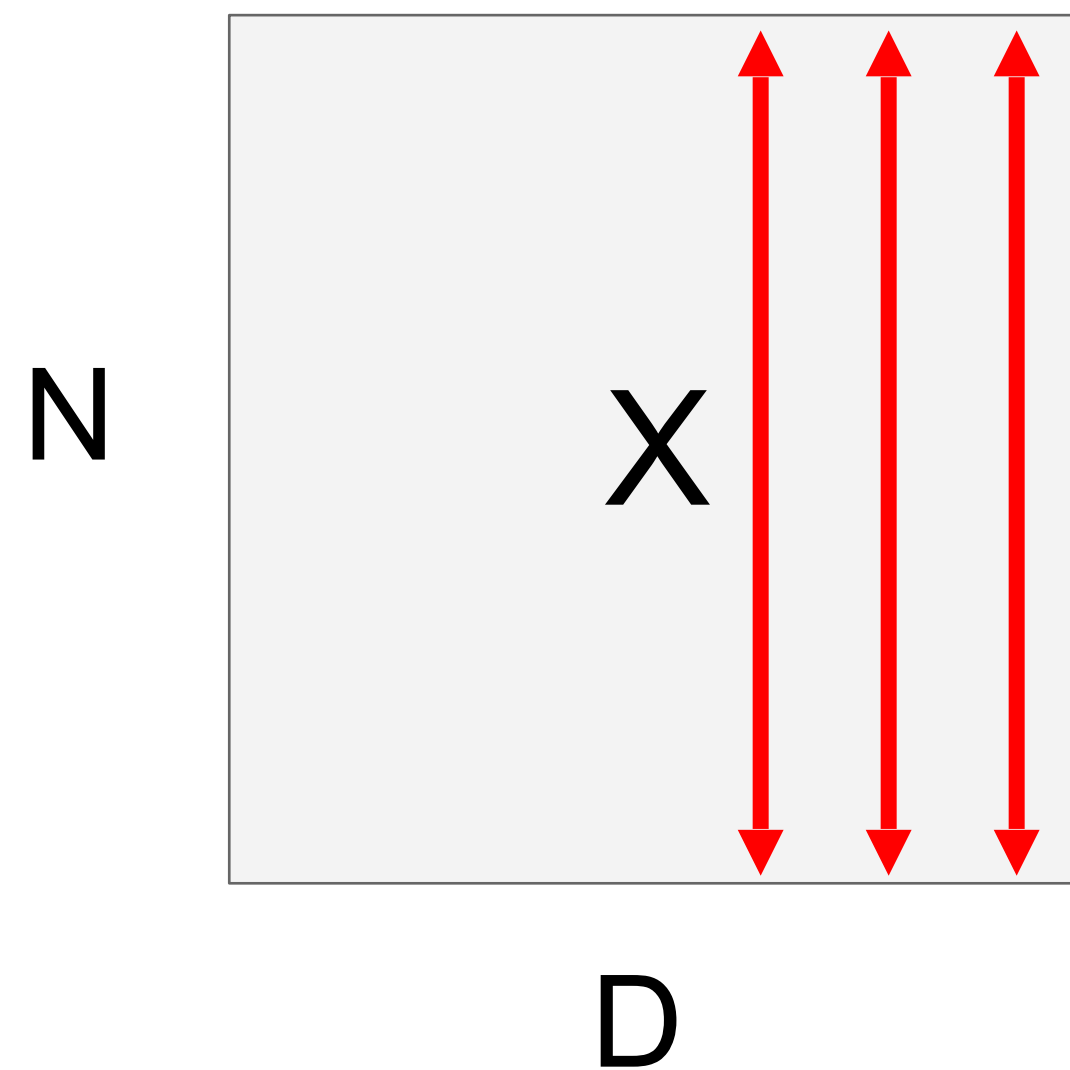


# Batch normalization



# Batch normalization

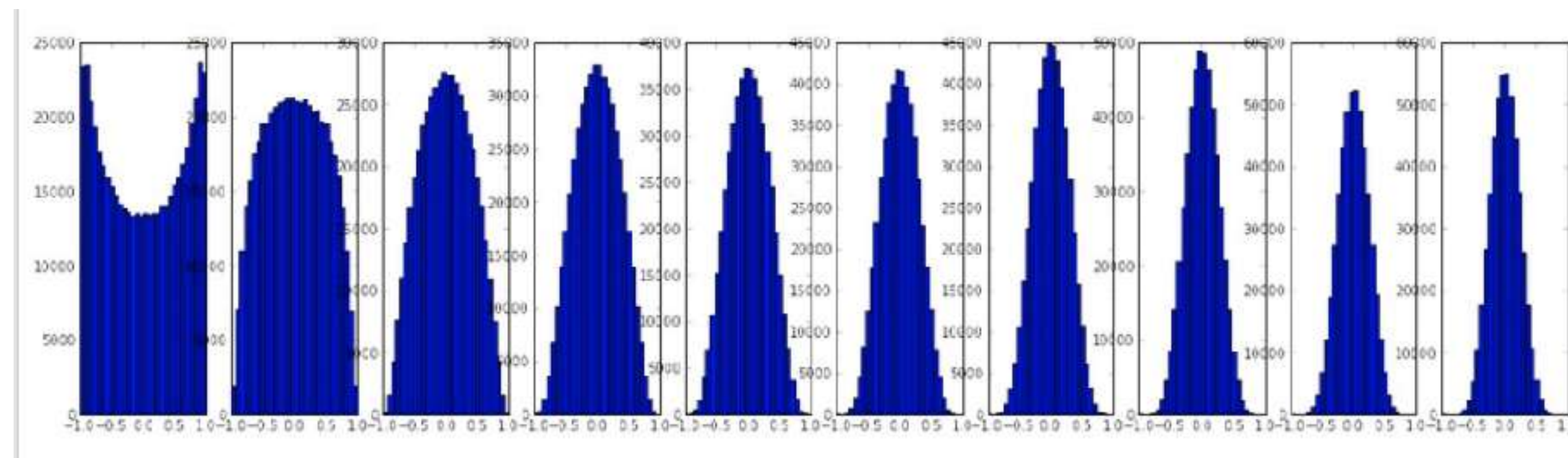
Recall...



1. compute the empirical mean and variance independently for each dimension.

2. Normalize

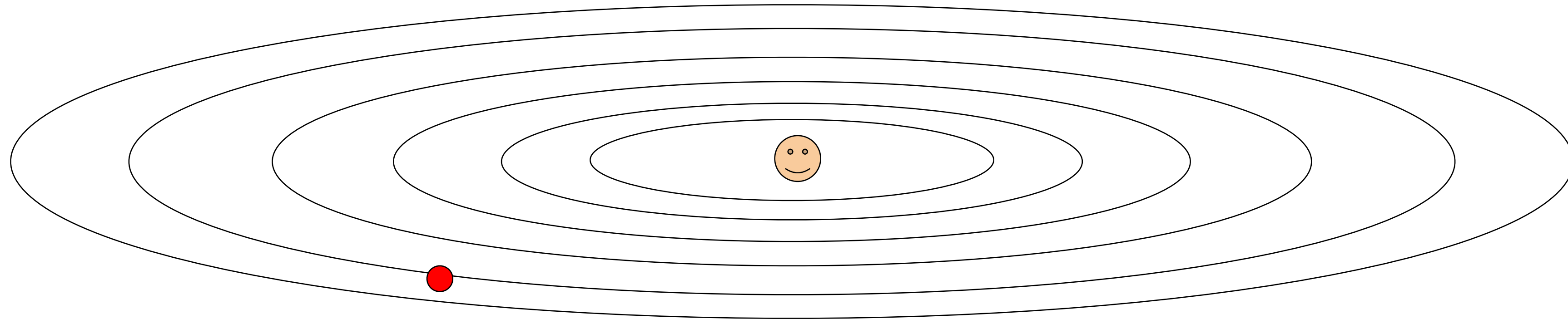
$$\hat{x}^{(k)} = \frac{x^{(k)} - \mathbb{E}[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$



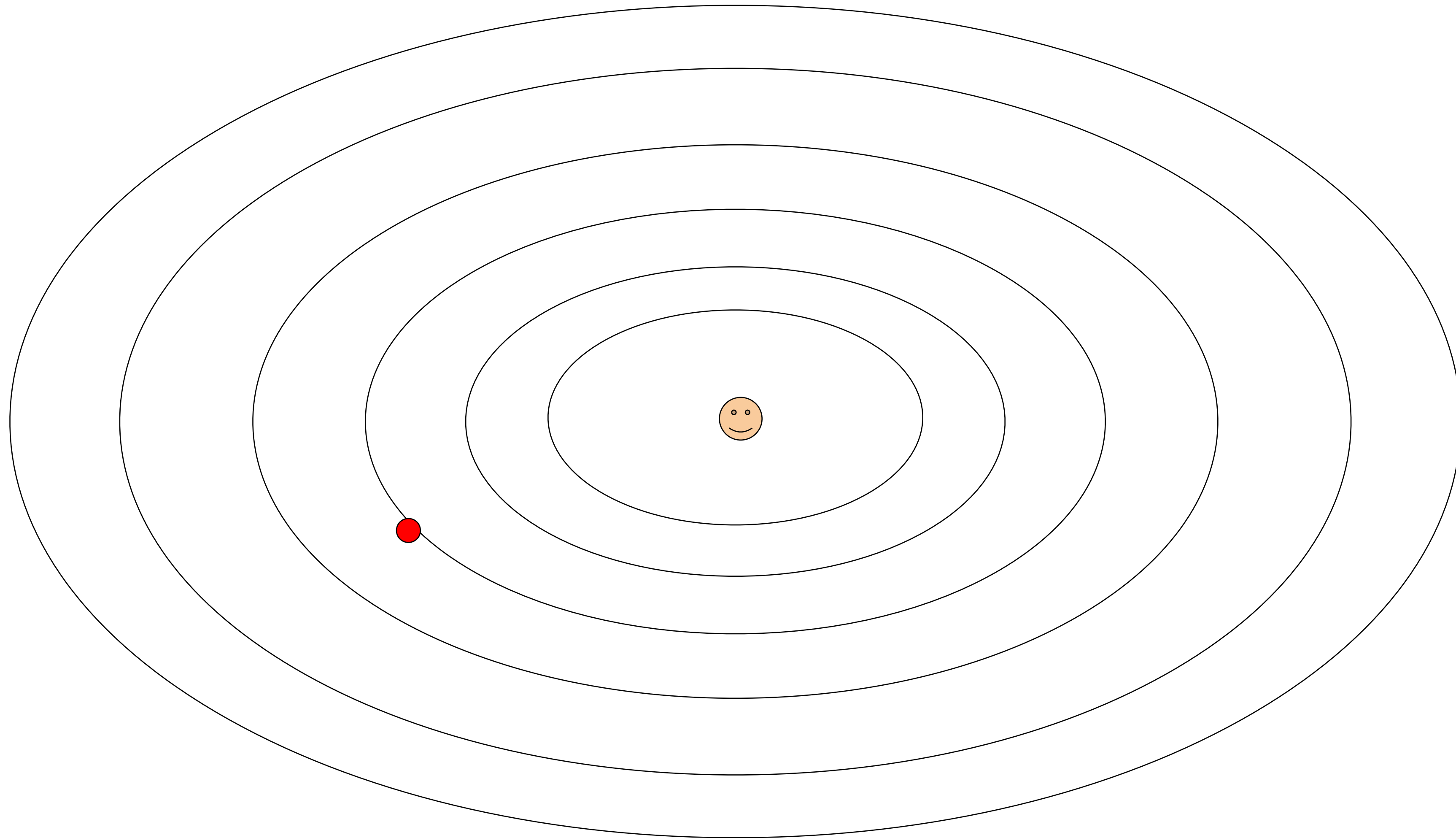


# Batch normalization

This imbalance between  
dimensions is the problem



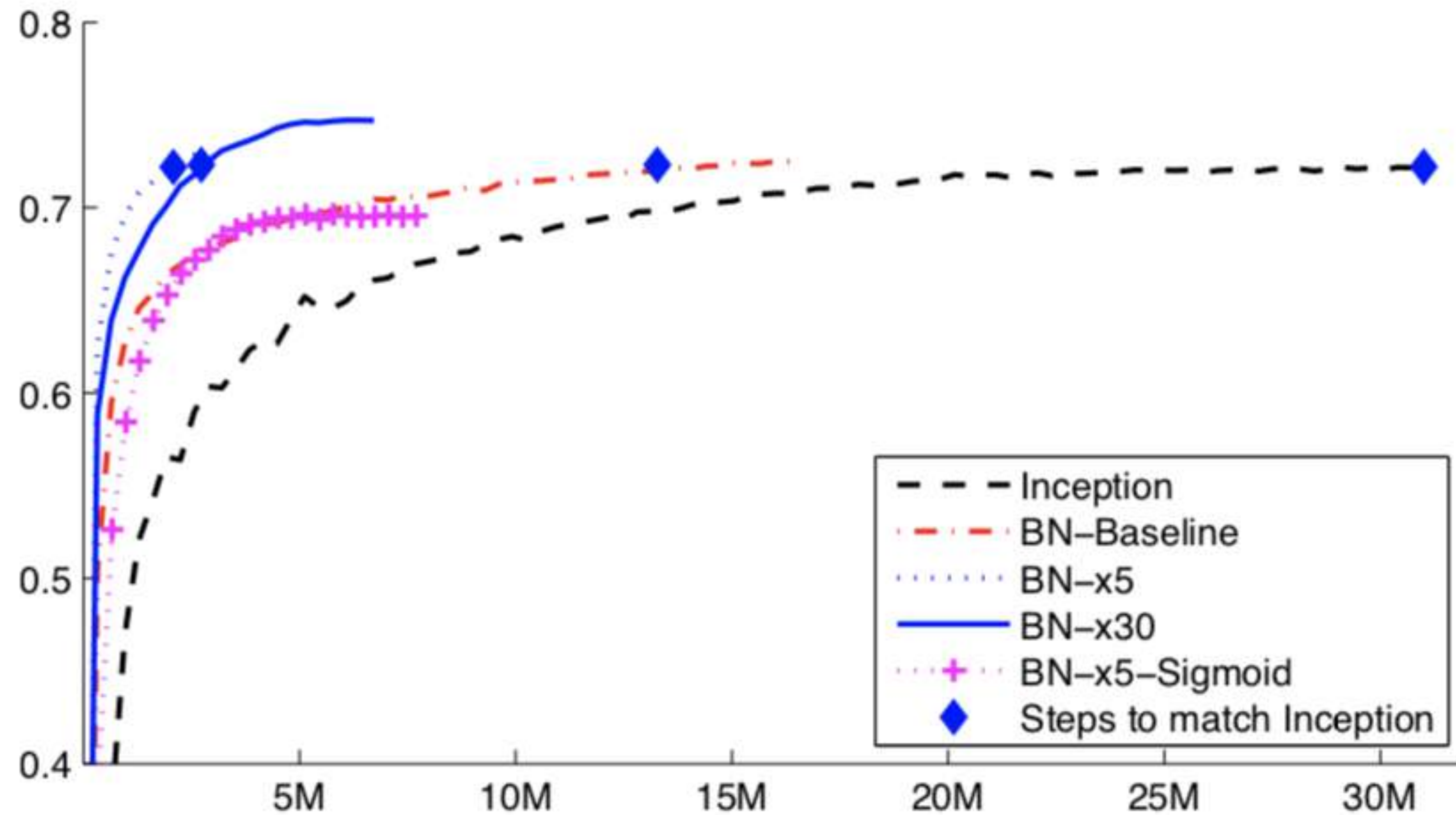
# Batch normalization



Let's artificially make it like this!



# Batch normalization

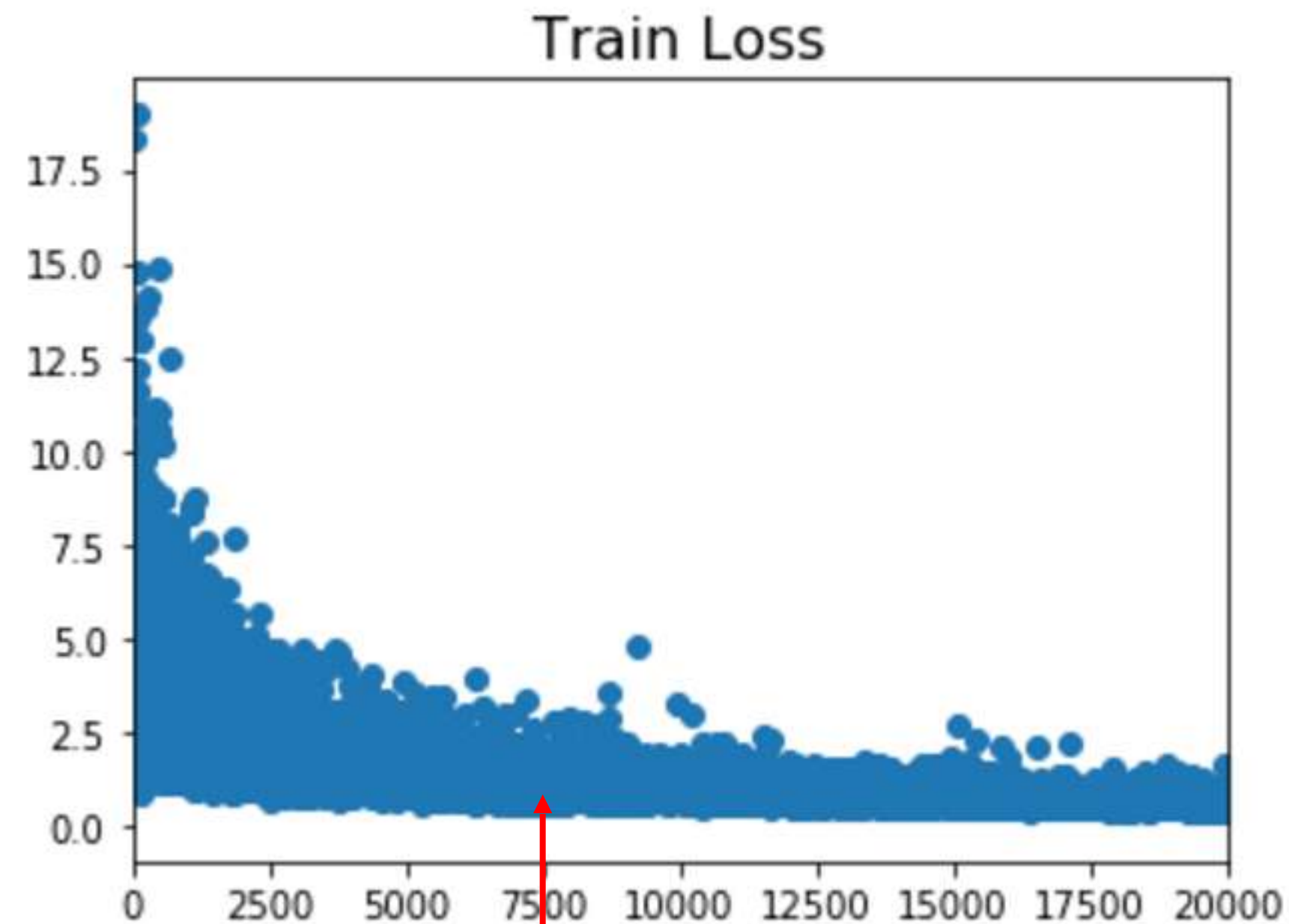


# Preventing overfitting

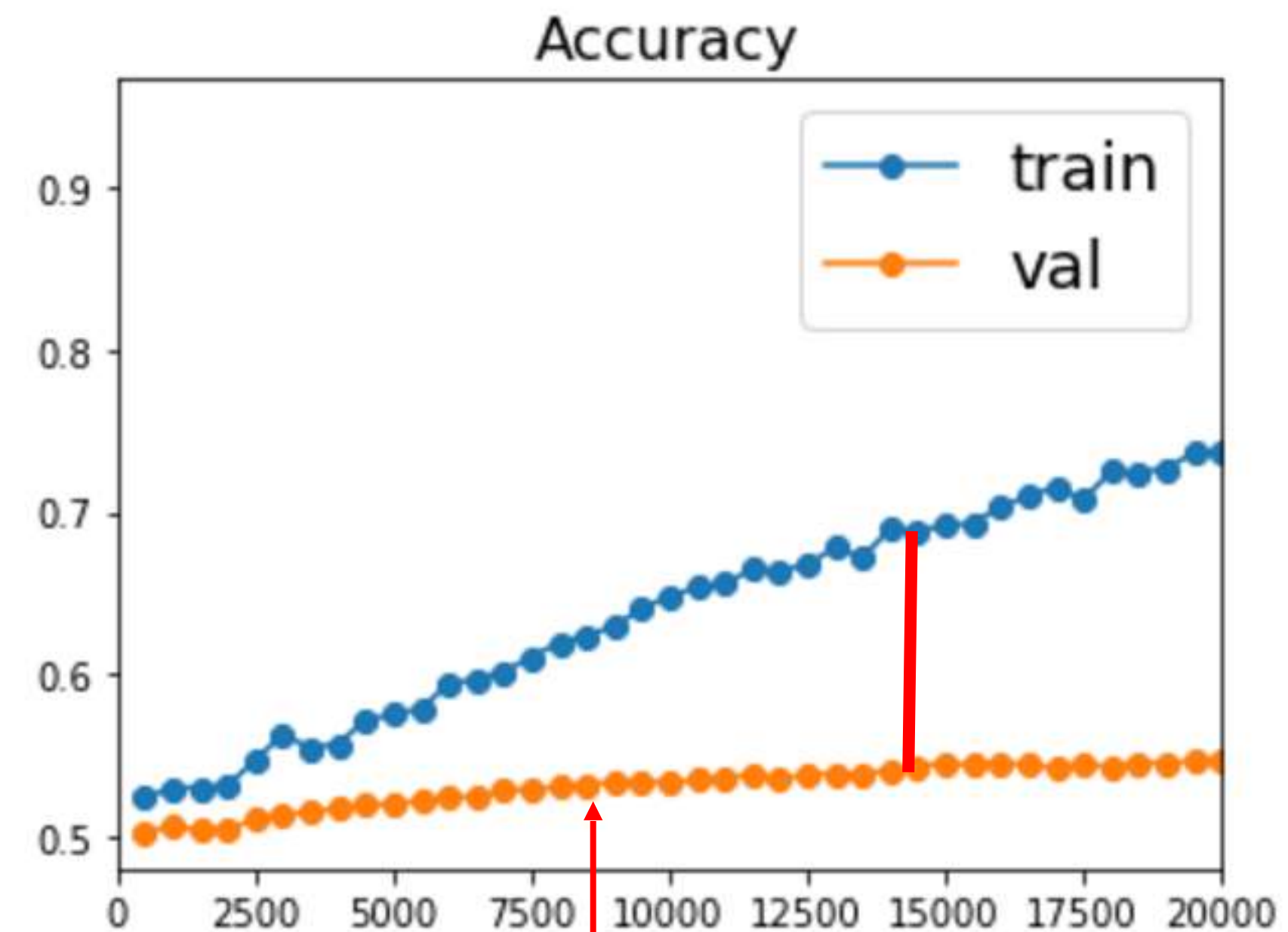


# Beyond training loss

Recall the other problem



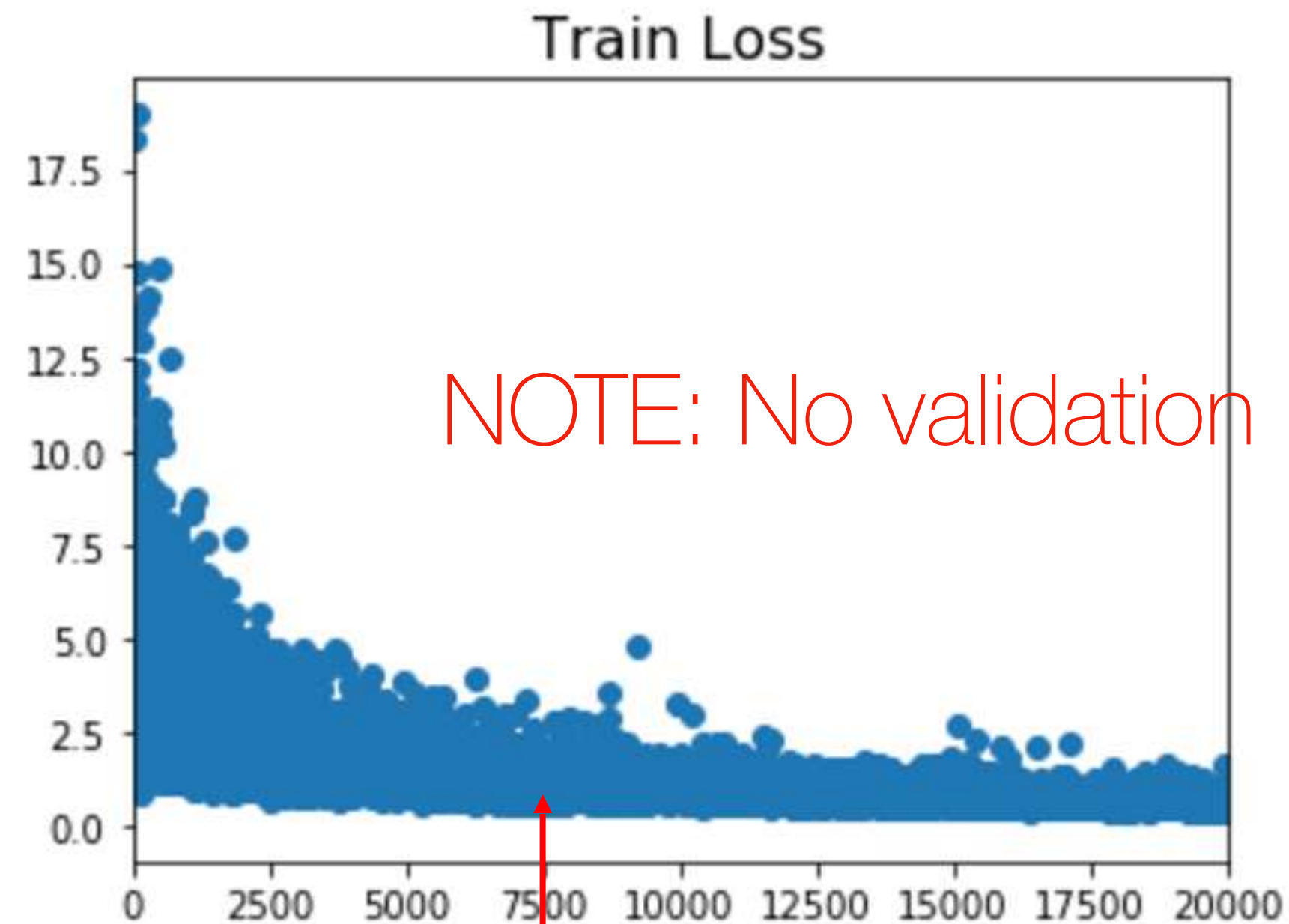
Better optimization  
algorithms help reduce  
training loss



But we really care about error  
on new data - how to reduce  
the gap?

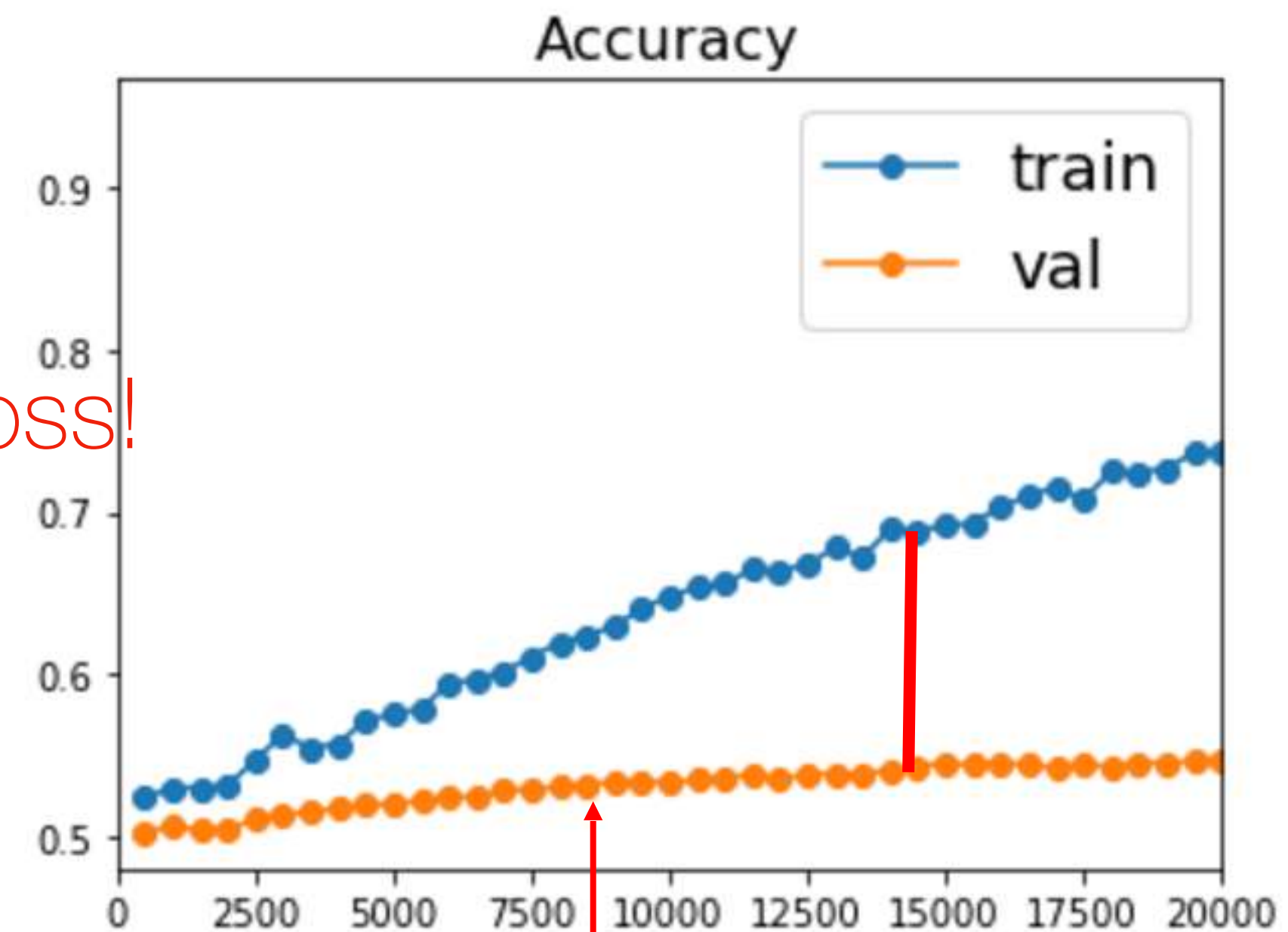
# Beyond training loss

Recall the other problem



NOTE: No validation loss!

Better optimization  
algorithms help reduce  
training loss



But we really care about error  
on new data - how to reduce  
the gap?



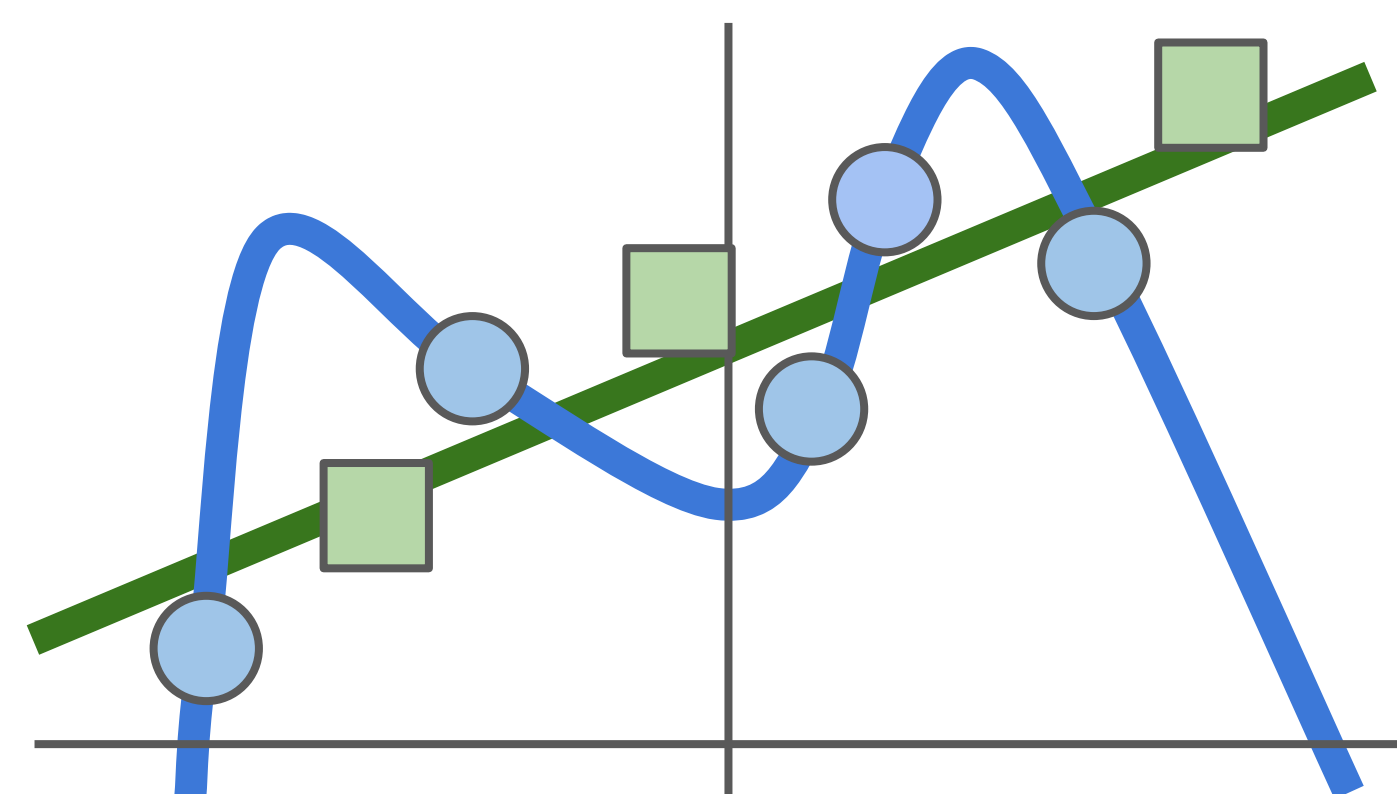
# A typical approach to overfitting

## Regularization

$$L(W) = \underbrace{\frac{1}{N} \sum_{i=1}^N L_i(f(x_i, W), y_i)}_{\text{Data loss}} + \underbrace{\lambda R(W)}_{\text{Regularization}}$$

**Data loss:** Model predictions should match training data

**Regularization:** Model should be “simple”, so it works on test data  $\|\mathbf{W}\|_2^2$



**Occam's Razor:**  
*“Among competing hypotheses, the simplest is the best”*  
 William of Ockham, 1285 - 1347

# Common regularizers

$$L = \frac{1}{N} \sum_{i=1}^N \sum_{j \neq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1) + \lambda R(W)$$

In common use:

**L2 regularization**

$$R(W) = \sum_k \sum_l W_{k,l}^2 \quad (\text{Weight decay})$$

L1 regularization

$$R(W) = \sum_k \sum_l |W_{k,l}|$$

Elastic net (L1 + L2)

$$R(W) = \sum_k \sum_l \beta W_{k,l}^2 + |W_{k,l}|$$



# Common regularizers

$$L = \frac{1}{N} \sum_{i=1}^N \sum_{j \neq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1) + \lambda R(W)$$

In common use:

**L2 regularization**

$$R(W) = \sum_k \sum_l W_{k,l}^2 \quad (\text{Weight decay})$$

L1 regularization

$$R(W) = \sum_k \sum_l |W_{k,l}|$$

Elastic net (L1 + L2)

$$R(W) = \sum_k \sum_l \beta W_{k,l}^2 + |W_{k,l}|$$

# Common regularizers

My personal warning against L2

$$L = \frac{1}{N} \sum_{i=1}^N \sum_{j \neq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1) + \lambda R(W)$$

In common use:

**L2 regularization**

$$R(W) = \sum_k \sum_l W_{k,l}^2 \quad (\text{Weight decay})$$

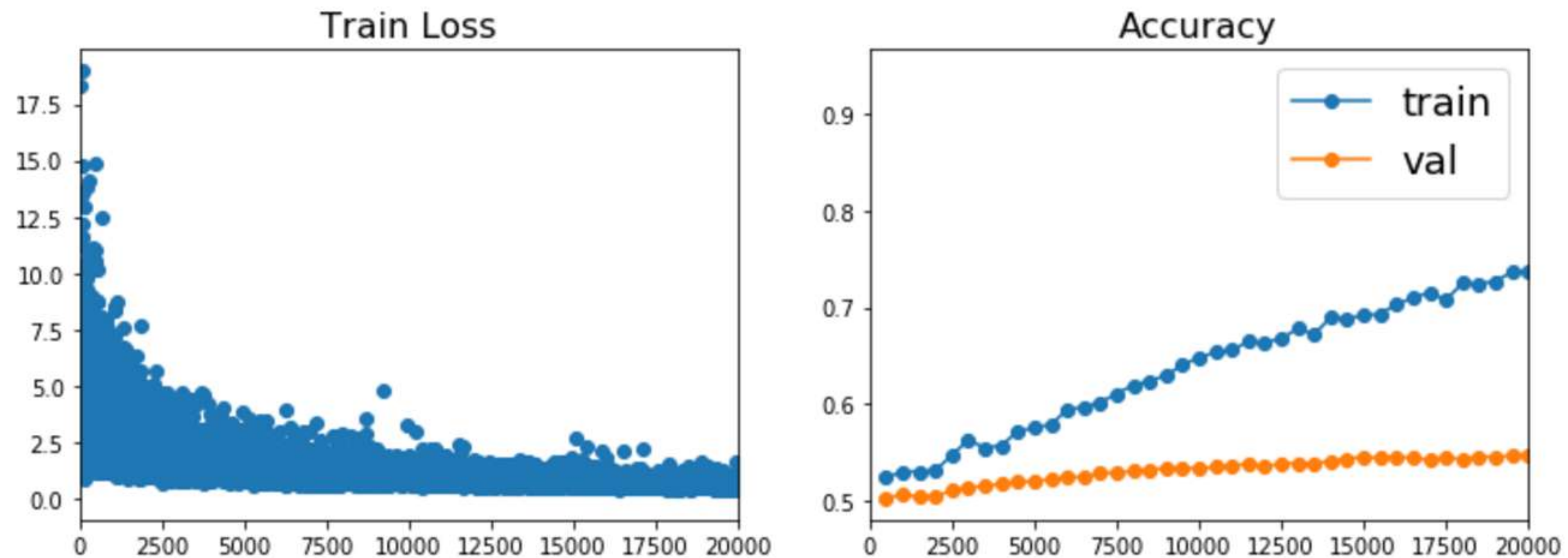
**L1 regularization**

$$R(W) = \sum_k \sum_l |W_{k,l}|$$

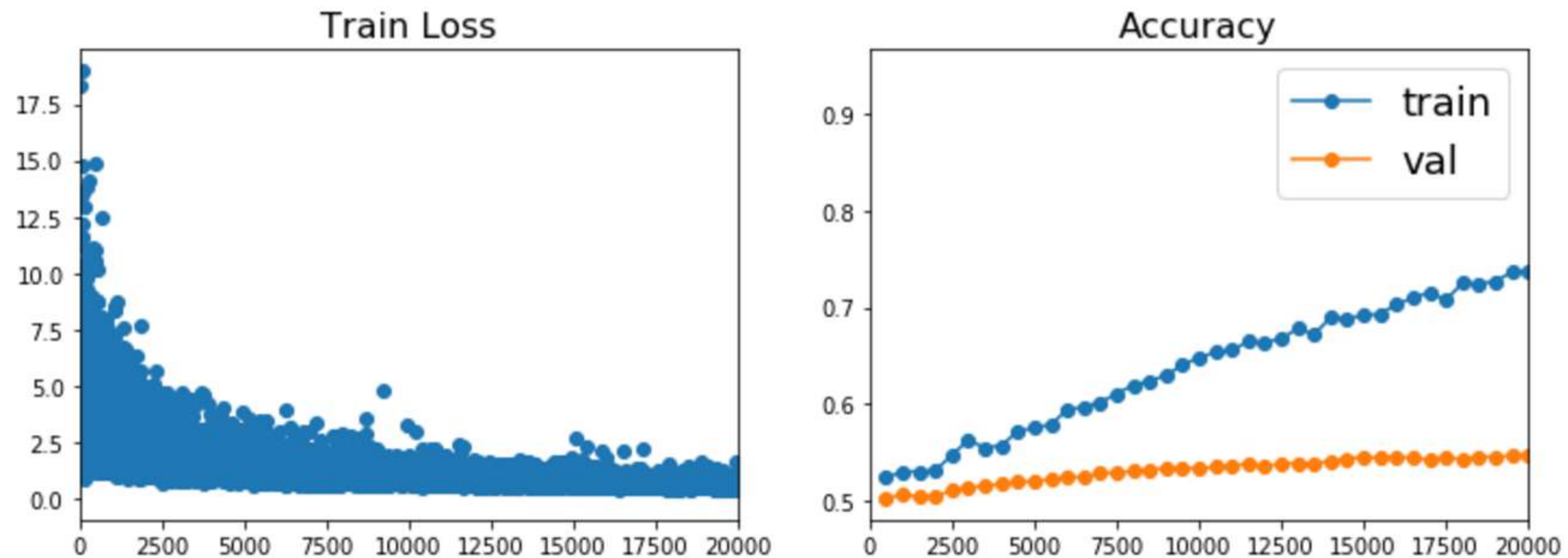
Ela [Laarhoven, 2017](#), “However, we show that L2 regularization has **no regularizing effect when combined with normalization**. Instead, regularization has an influence on the scale of weights, and thereby on the effective learning rate.”



# Why does this happen in the first place?



# Why does this happen in the first place?



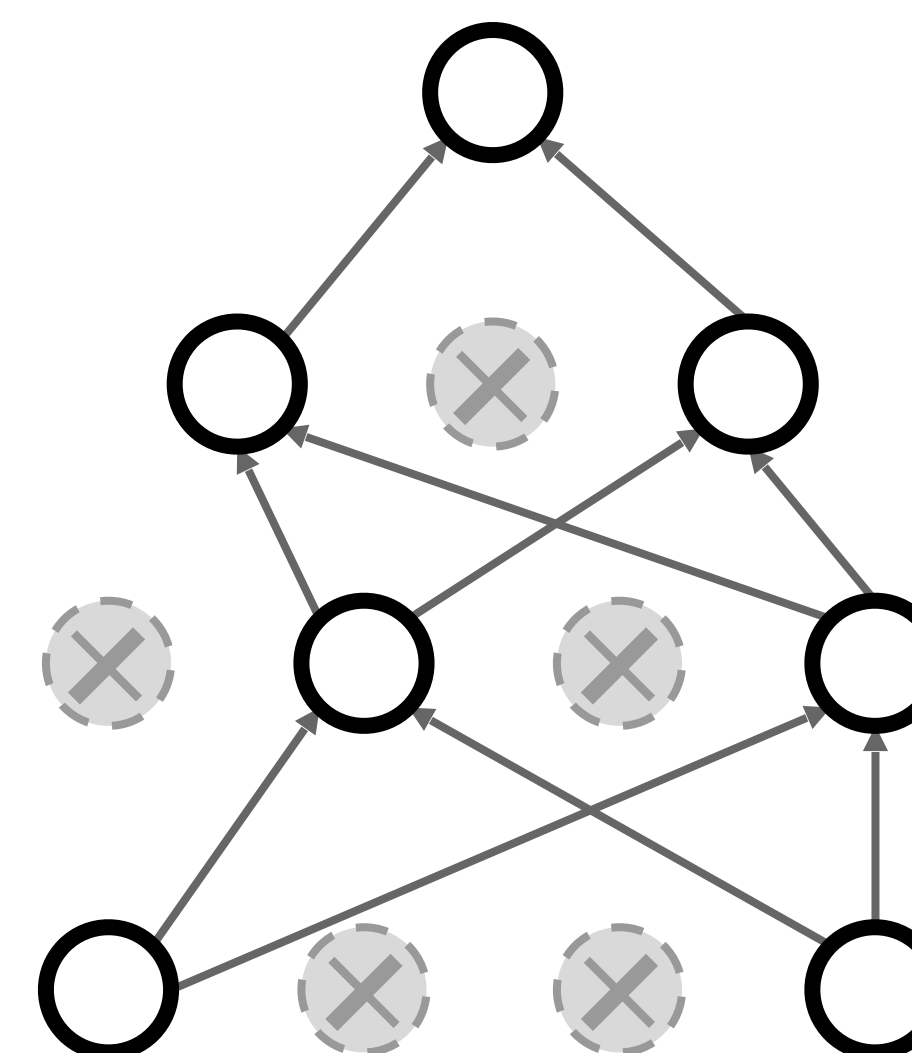
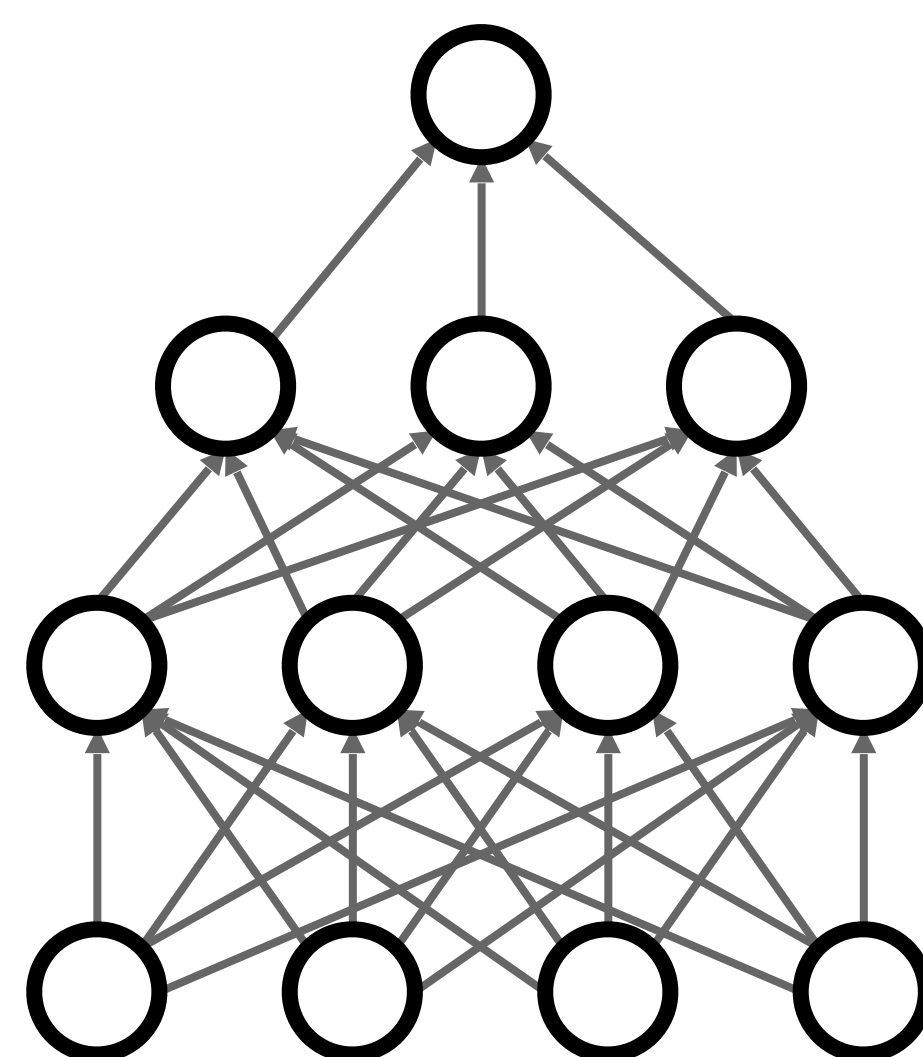
Can we somehow encode  
uncertainty in data?



# Regularization: Dropout

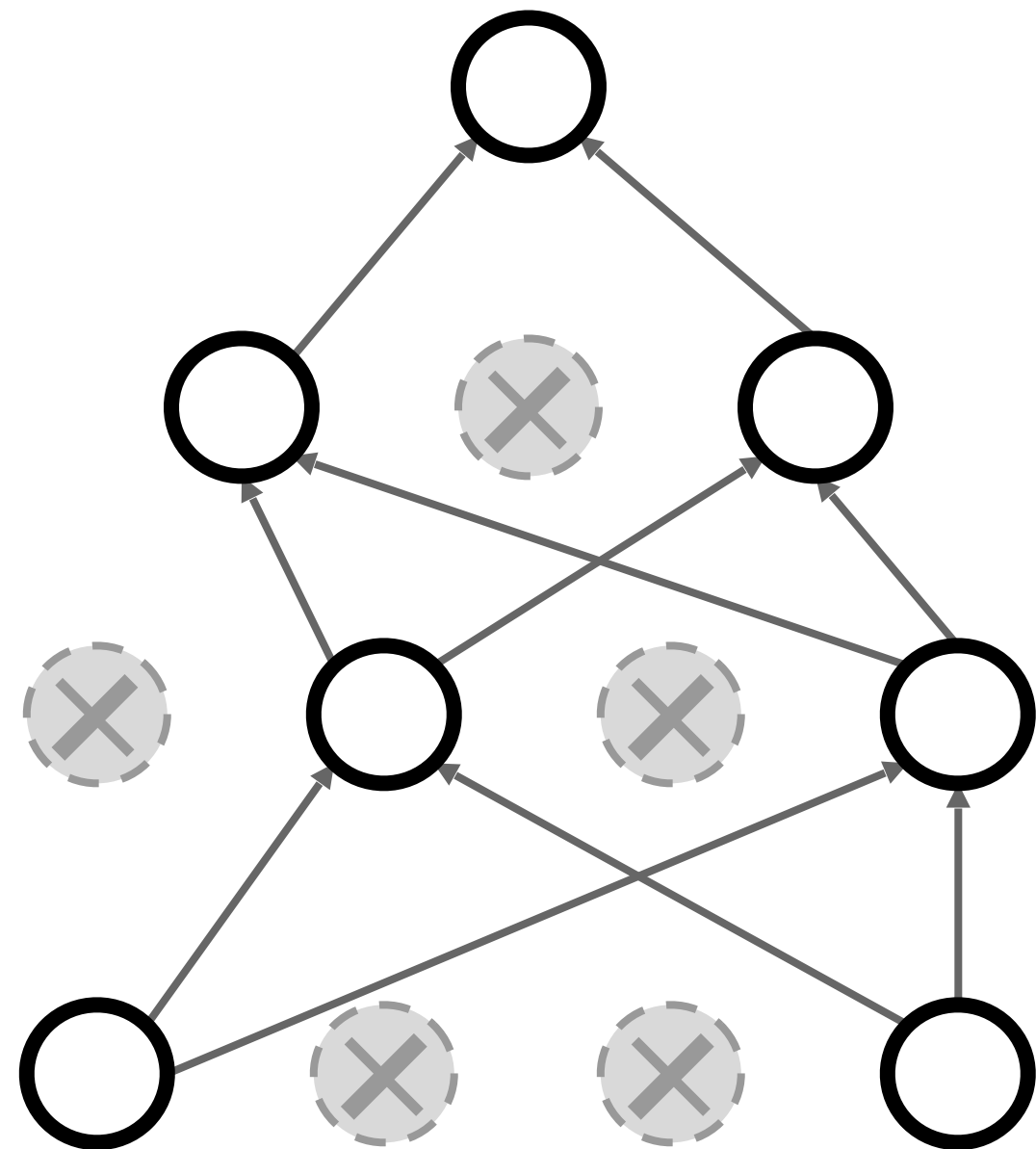
Making it impossible to trust the data 100%

In each forward pass, randomly set some neurons to zero  
Probability of dropping is a hyperparameter; 0.5 is common



# Regularization: Dropout

Making it impossible to trust the data 100%



Forces the network to have a redundant representation;  
Prevents co-adaptation of features

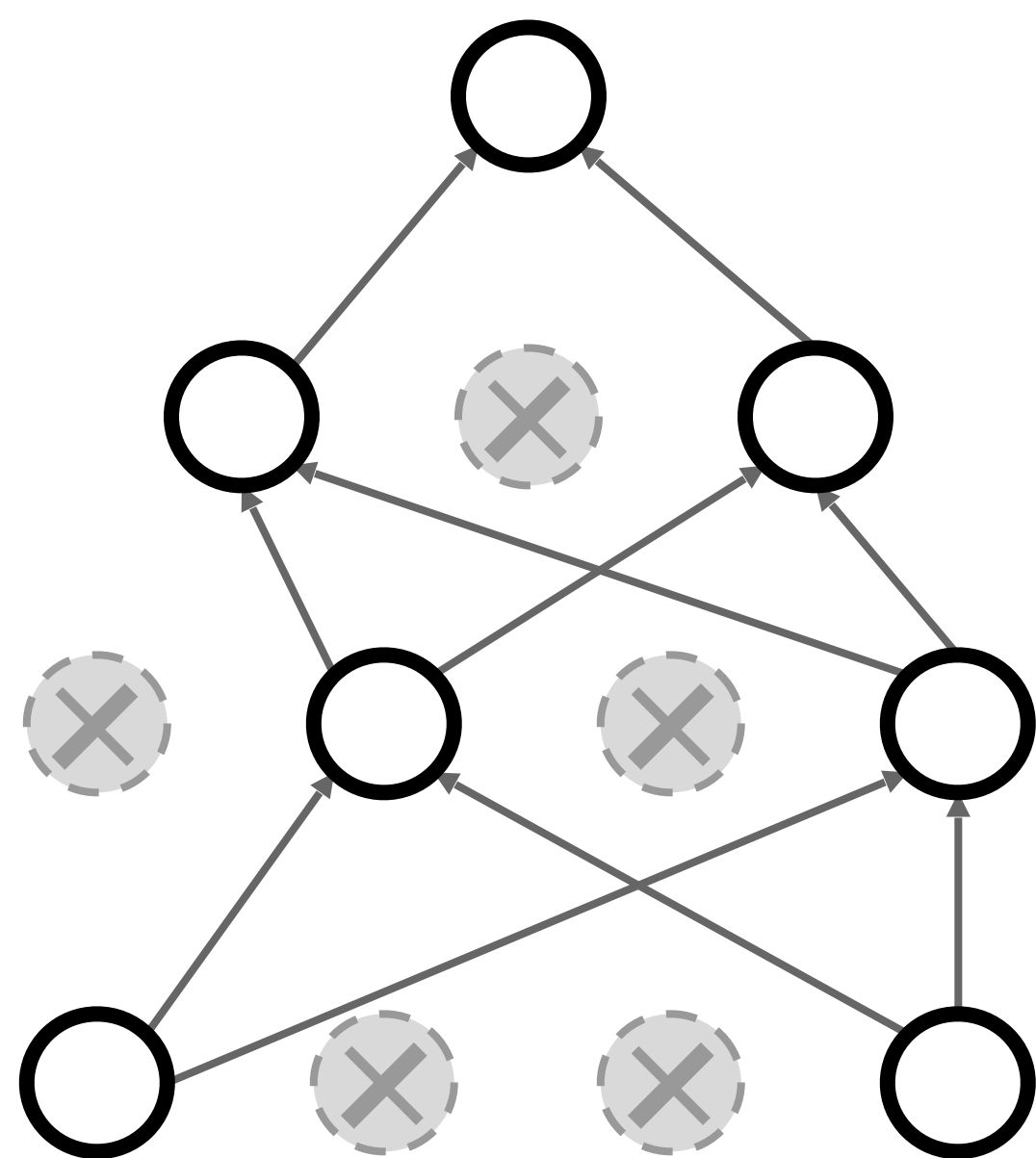




Skipped in class  
(outside of scope)

# Regularization: Dropout

Making it impossible to trust the data 100%



Another interpretation:

Dropout is training a large **ensemble** of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has  $2^{4096} \sim 10^{1233}$  possible masks!

Only  $\sim 10^{82}$  atoms in the universe...

Skipped in class

# Regularization: Dropout at **test** time (outside of scope)

Again the train / test gap

Dropout makes our output random!

Output (label)      Input (image)

$$\boxed{y} = f_W(\boxed{x}, \boxed{z})$$

Random mask

Want to “average out” the randomness at test-time

$$y = f(x) = E_z[f(x, z)] = \int p(z) f(x, z) dz$$

But this integral seems hard ...



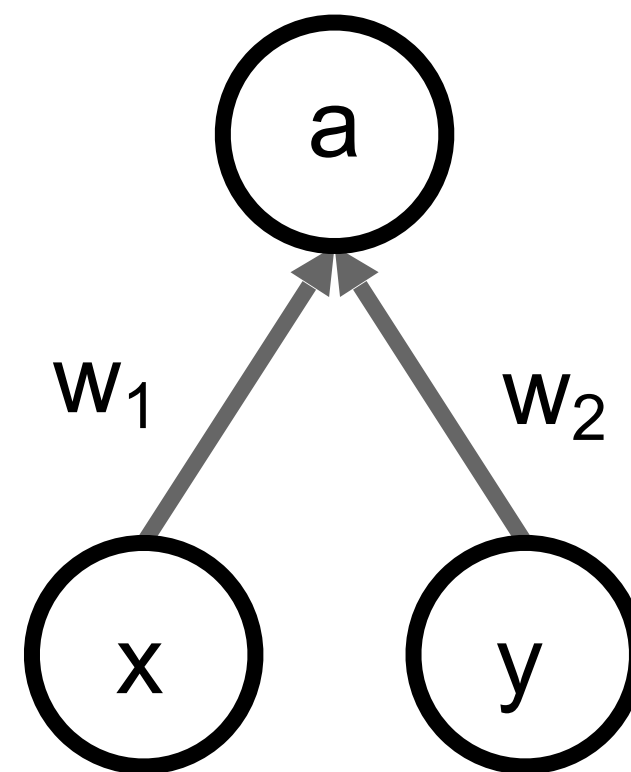
Skipped in class

# Regularization: Dropout at **test** time (outside of scope)

An approximate solution

Want to approximate the integral  $y = f(x) = E_z [f(x, z)] = \int p(z) f(x, z) dz$

Consider a single neuron.



Skipped in class

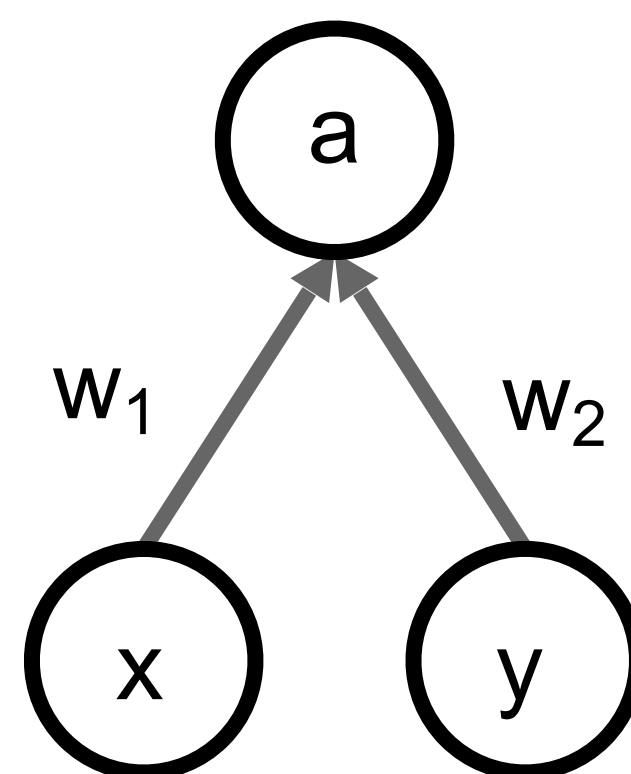
# Regularization: Dropout at **test** time (outside of scope)

An approximate solution

Want to approximate the integral  $y = f(x) = E_z[f(x, z)] = \int p(z)f(x, z)dz$

Consider a single neuron.

At test time we have:  $E[a] = w_1x + w_2y$



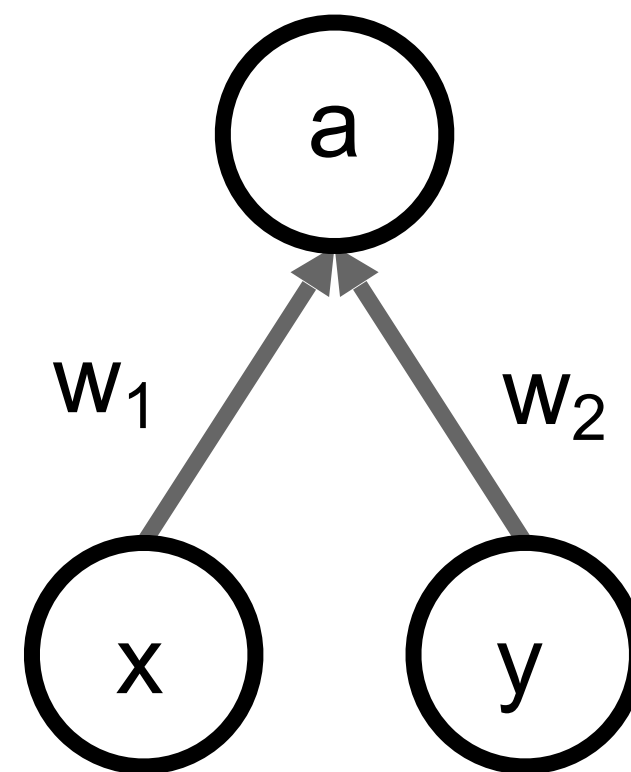


# Regularization: Dropout at **test** time (outside of scope)

An approximate solution

Want to approximate the integral  $y = f(x) = E_z [f(x, z)] = \int p(z) f(x, z) dz$

Consider a single neuron.



At test time we have:  $E[a] = w_1 x + w_2 y$

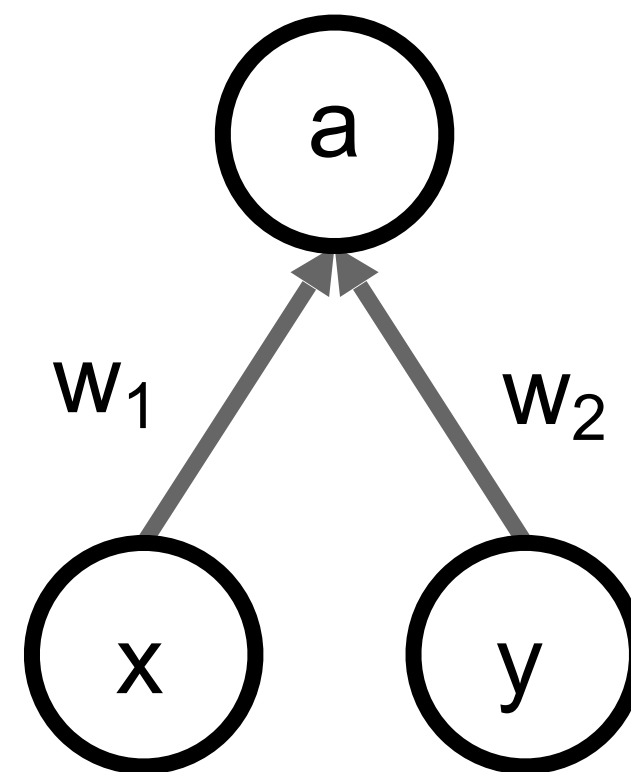
During training we have: 
$$E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0y) + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2 y) = \frac{1}{2}(w_1 x + w_2 y)$$

# Regularization: Dropout at **test** time (outside of scope)

An approximate solution

Want to approximate the integral  $y = f(x) = E_z [f(x, z)] = \int p(z) f(x, z) dz$

Consider a single neuron.



At test time we have:  $E[a] = w_1 x + w_2 y$

During training we have:

$$\begin{aligned}
 E[a] &= \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0y) \\
 &\quad + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2 y) \\
 &= \frac{1}{2}(w_1 x + w_2 y)
 \end{aligned}$$

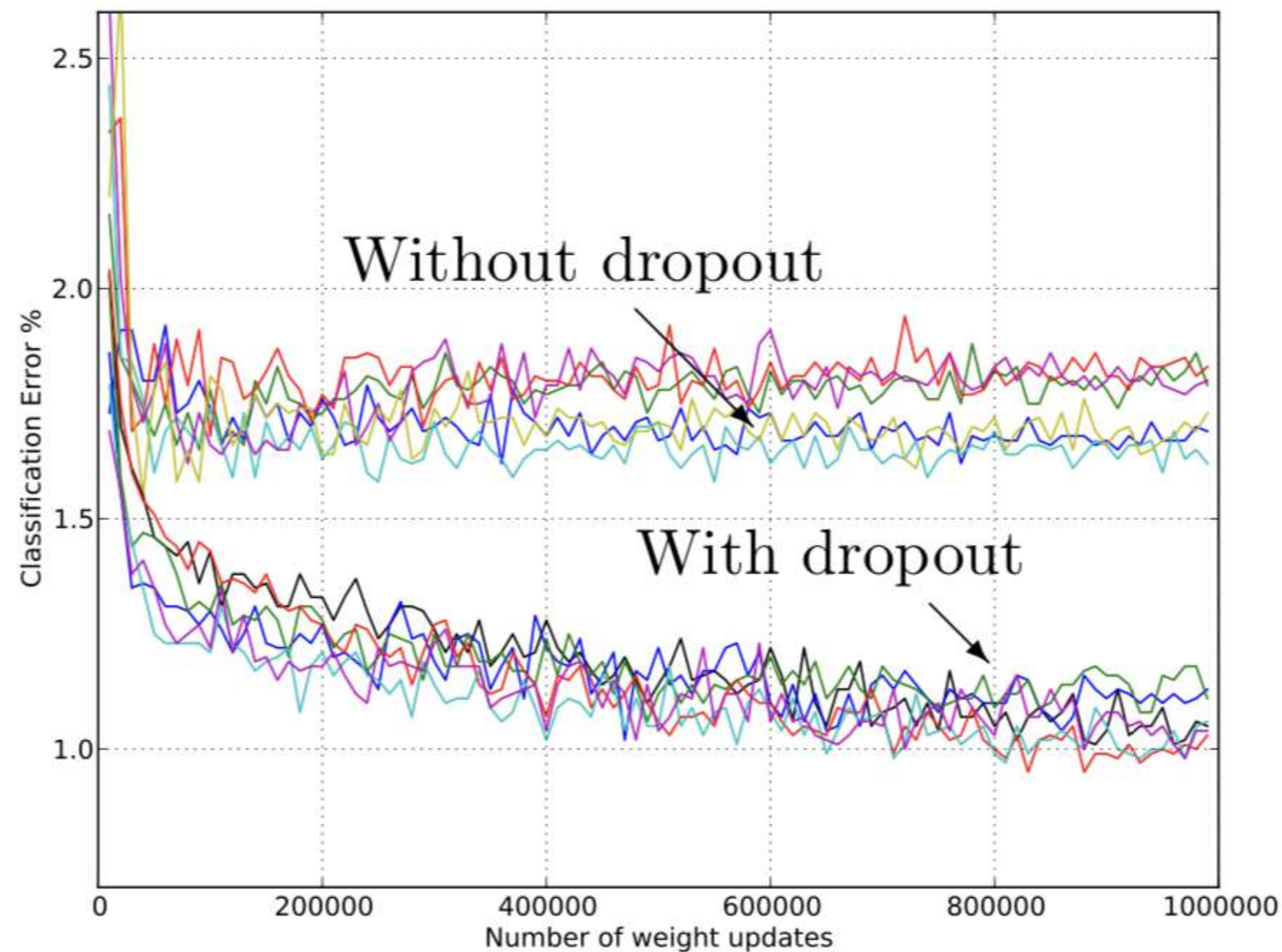
At test time, **multiply** by dropout probability



Skipped in class  
(outside of scope)

# Regularization: Dropout

How good is it?



Srivastava et al, "Dropout: A simple way to prevent neural networks from overfitting", JMLR 2014

Based on slides for [Stanford cs231n](https://stanford.edu/~jlmr/cs231n/) by Li, Jonson, and Young. Modified and reused with permission

Skipped in class

# Regularization: A common pattern (outside of scope)

**Training:** Add some kind of randomness

$$y = f_W(x, z)$$

**Testing:** Average out randomness  
(sometimes approximate)

$$y = f(x) = E_z[f(x, z)] = \int p(z) f(x, z) dz$$



Skipped in class

# Regularization: A common pattern (outside of scope)

**Training:** Add some kind of randomness

$$y = f_W(x, z)$$

**Testing:** Average out randomness  
(sometimes approximate)

$$y = f(x) = E_z[f(x, z)] = \int p(z) f(x, z) dz$$

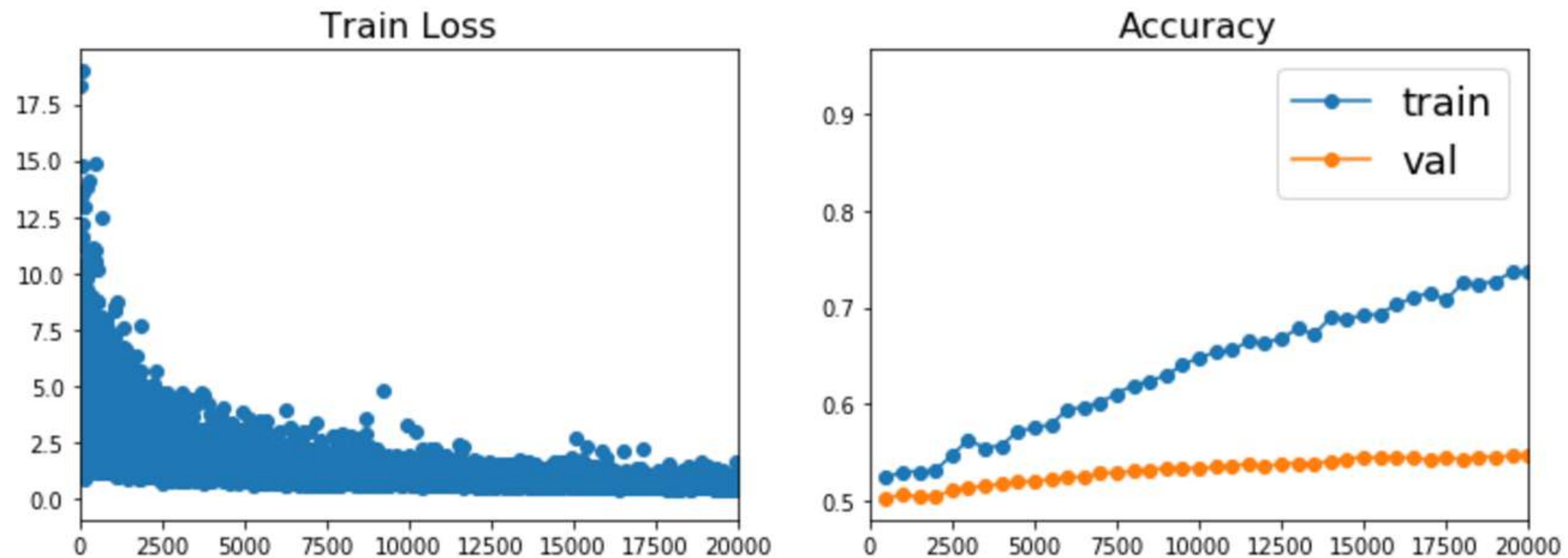
**Example:** Batch Normalization

**Training:** Normalize using stats  
from random minibatches

**Testing:** Use fixed stats to  
normalize

Skipped in class

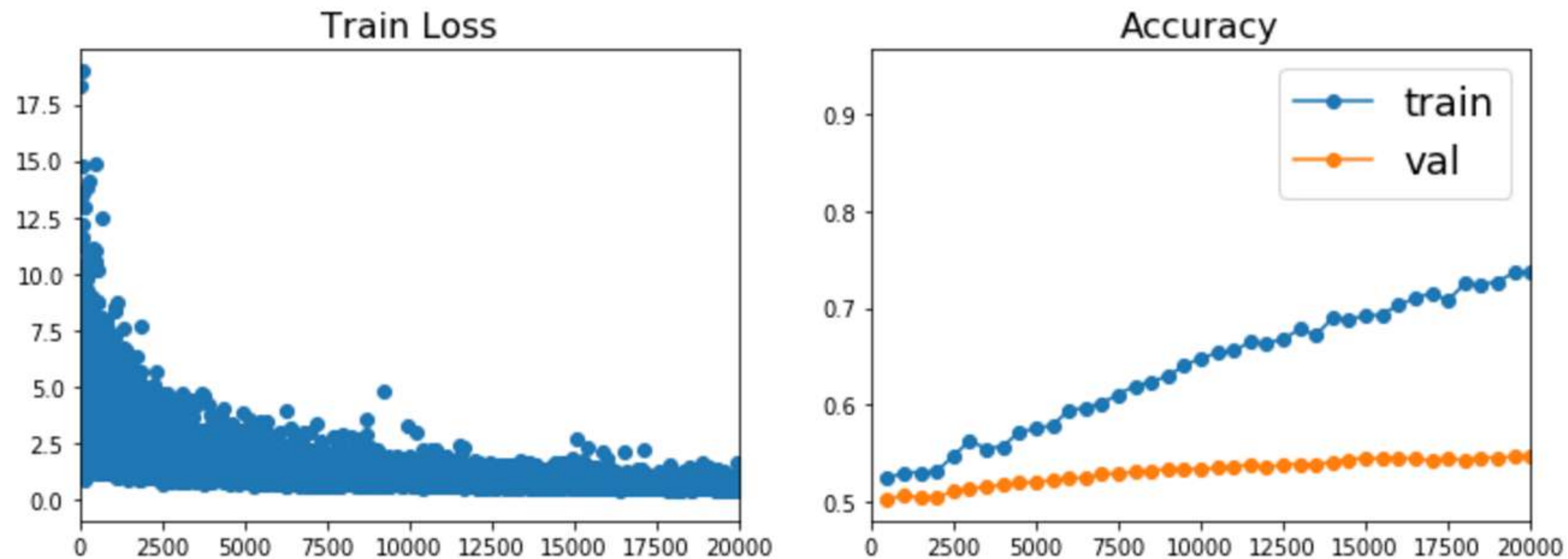
Why does this happen in the first place? (outside of scope)





Skipped in class

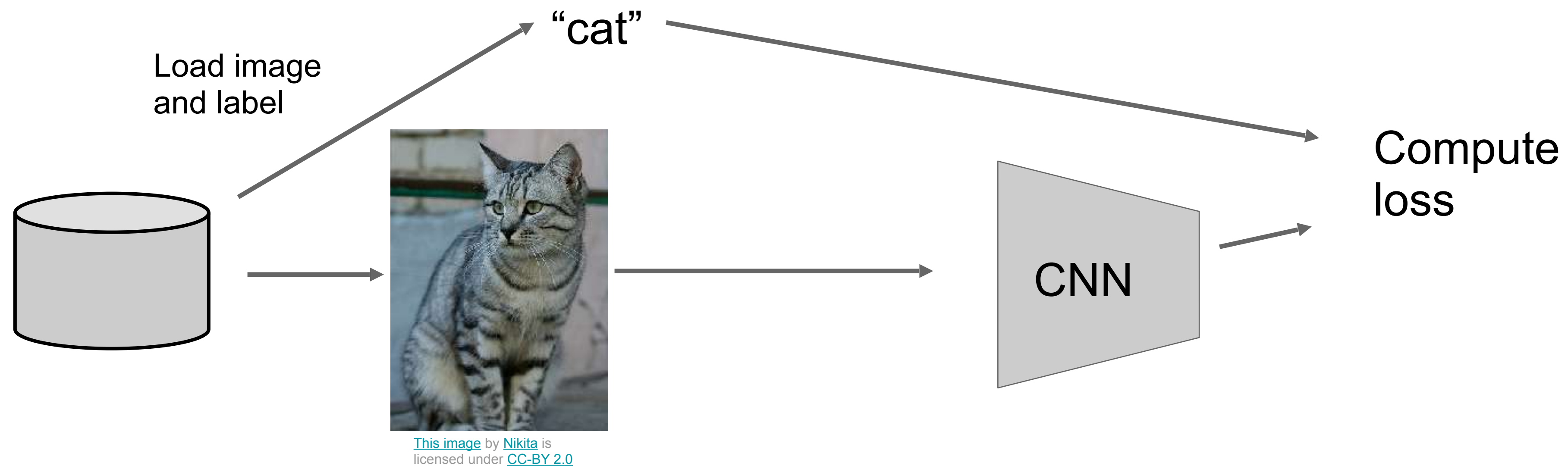
Why does this happen in the first place? (outside of scope)



How can we have more data?

Skipped in class

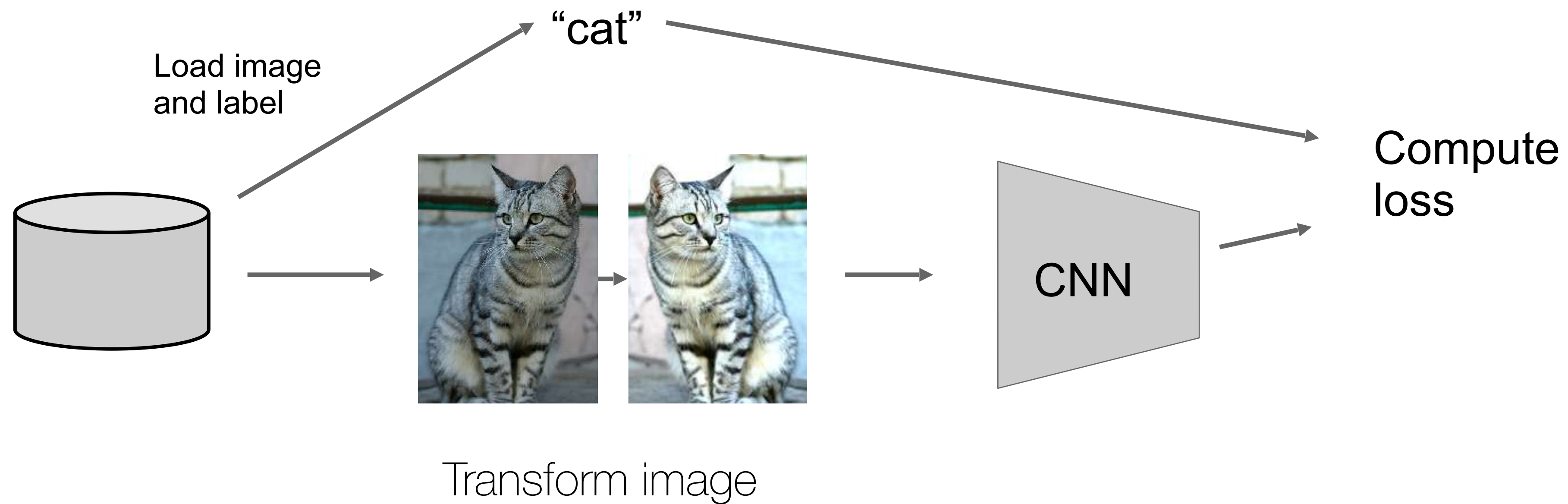
# Regularization: Data augmentation (outside of scope)





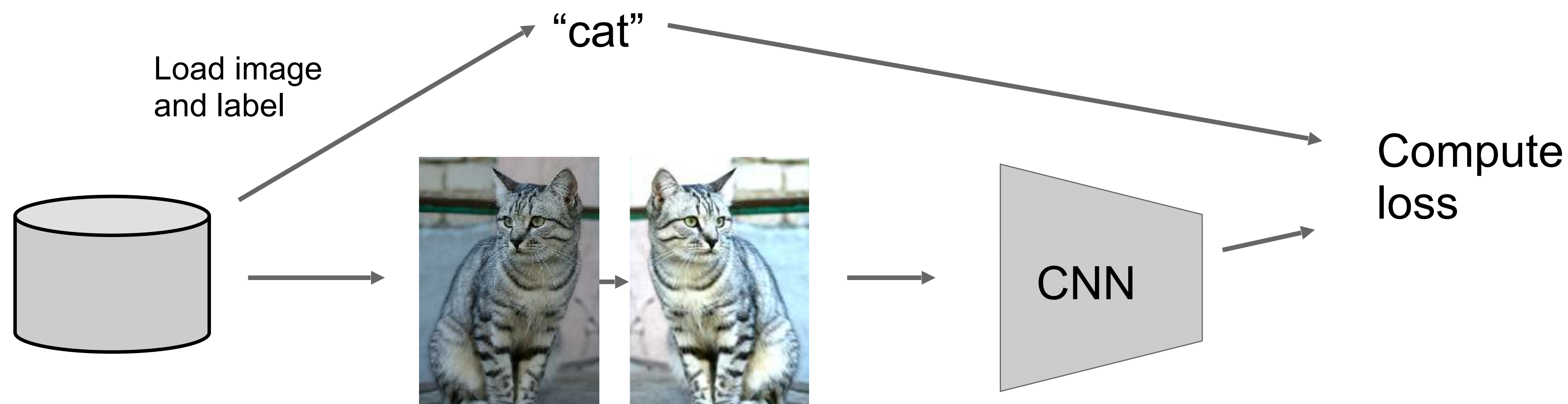
Skipped in class

# Regularization: Data augmentation (outside of scope)



Skipped in class

# Regularization: Data augmentation (outside of scope)

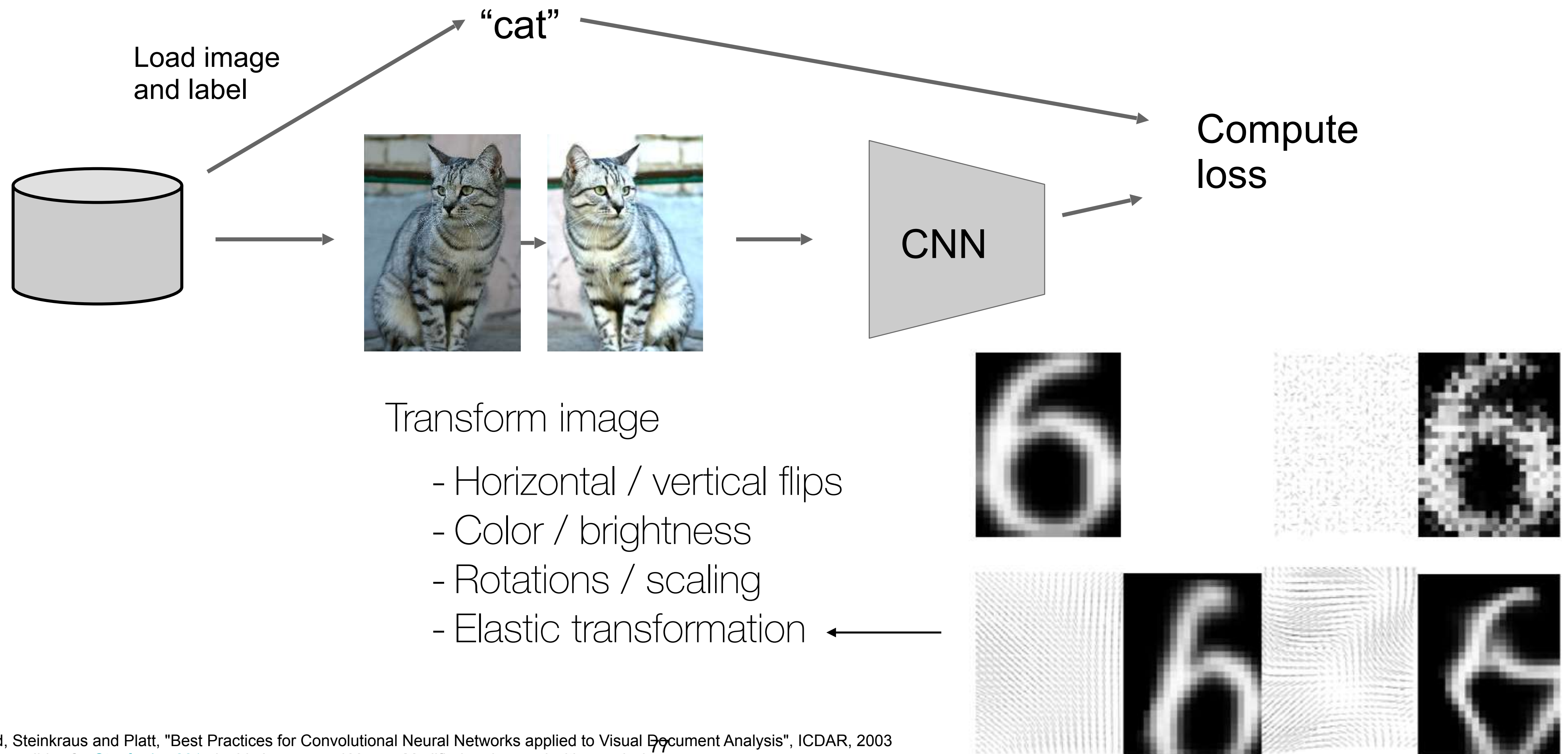


Transform image

- Horizontal / vertical flips
- Color / brightness
- Rotations / scaling
- Elastic transformation

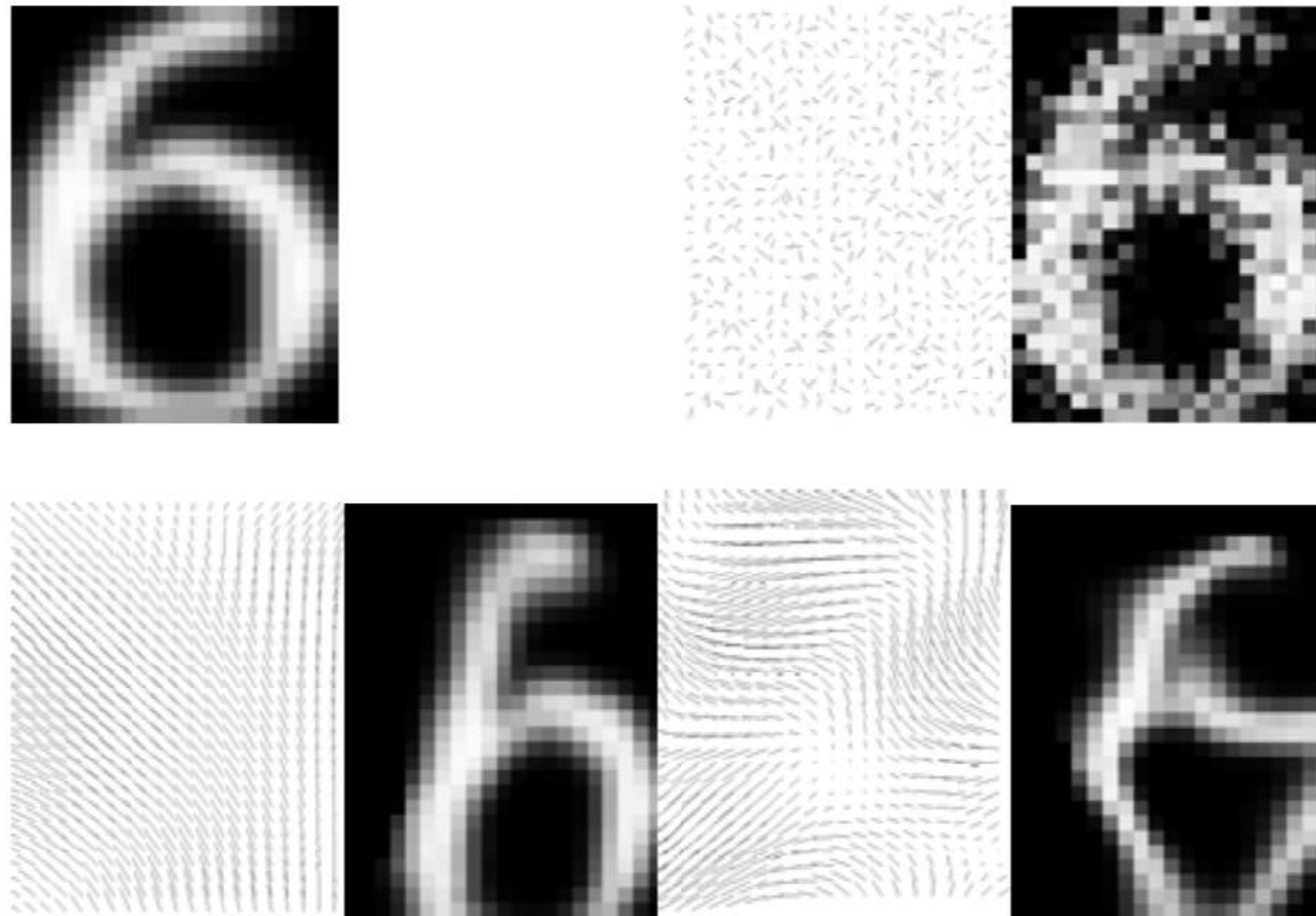


## Regularization: Data augmentation (outside of scope)



## Regularization: Data augmentation (outside of scope)

### Elastic deformations



1. Create random displacement field with uniform distribution

2. Smooth the displacement field with a Gaussian

Figures copyright IEEE, 2003. Reproduced for educational purposes.



# Regularization: Data augmentation (outside of scope)

## Elastic deformations

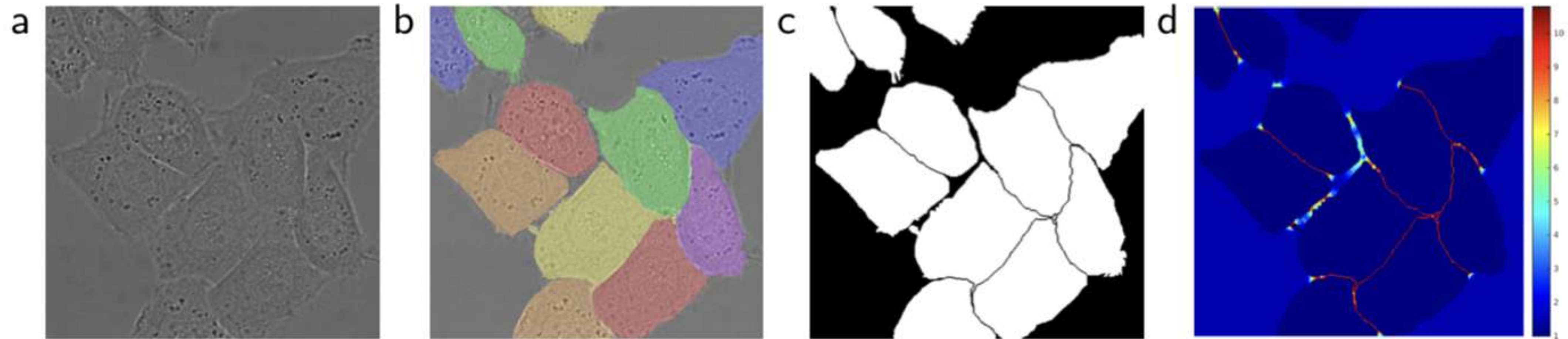
| Algorithm         | Distortion   | Error       | Ref.       |
|-------------------|--------------|-------------|------------|
| 2 layer MLP (MSE) | affine       | 1.6%        | [3]        |
| SVM               | affine       | 1.4%        | [9]        |
| Tangent dist.     | affine+thick | 1.1%        | [3]        |
| Lenet5 (MSE)      | affine       | 0.8%        | [3]        |
| Boost. Lenet4 MSE | affine       | 0.7%        | [3]        |
| Virtual SVM       | affine       | 0.6%        | [9]        |
| 2 layer MLP (CE)  | none         | 1.6%        | this paper |
| 2 layer MLP (CE)  | affine       | 1.1%        | this paper |
| 2 layer MLP (MSE) | elastic      | 0.9%        | this paper |
| 2 layer MLP (CE)  | elastic      | 0.7%        | this paper |
| Simple conv (CE)  | affine       | 0.6%        | this paper |
| Simple conv (CE)  | elastic      | <b>0.4%</b> | this paper |

**Table 1. Comparison between various algorithms.**



# Regularization: Data augmentation (outside of scope)

## Elastic deformations

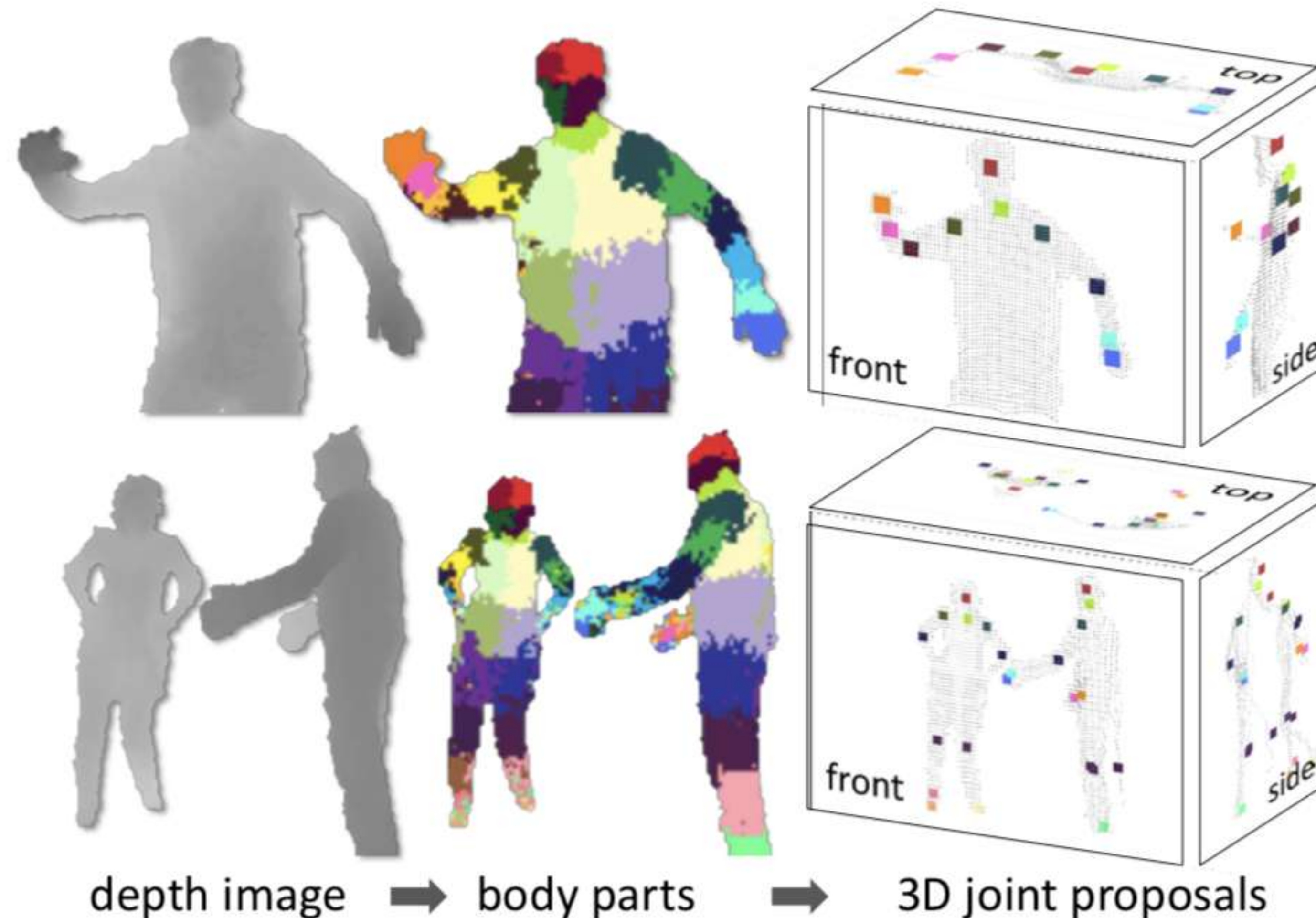


| Name             | PhC-U373      | DIC-HeLa      |
|------------------|---------------|---------------|
| IMCB-SG (2014)   | 0.2669        | 0.2935        |
| KTH-SE (2014)    | 0.7953        | 0.4607        |
| HOUS-US (2014)   | 0.5323        | -             |
| second-best 2015 | 0.83          | 0.46          |
| u-net (2015)     | <b>0.9203</b> | <b>0.7756</b> |



# Regularization: Data augmentation (outside of scope)

Synthetic data





# Regularization: Data augmentation (outside of scope)

Synthetic data + generative models



Unlabeled Real Images

Simulated images



Unlabeled Real Images

Simulated images



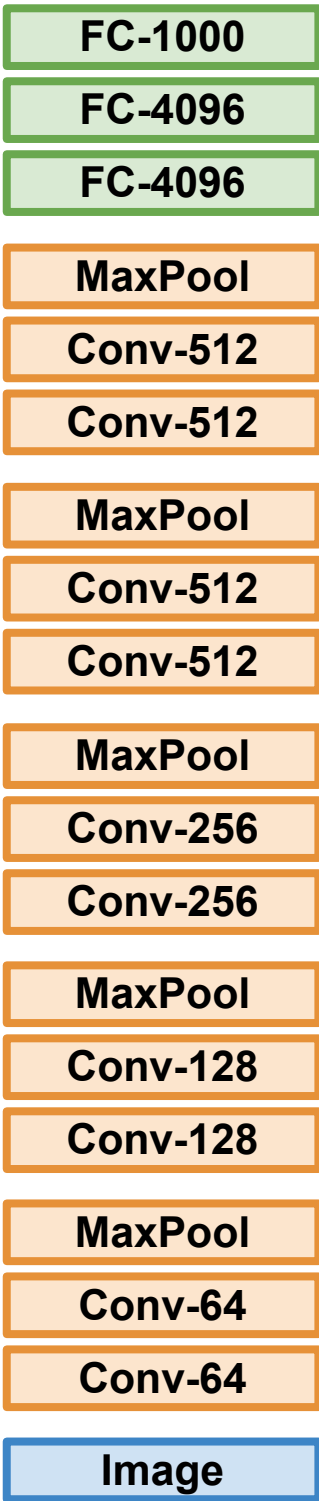


Douhan et al, "DeCAF: A Deep Convolutional Activation  
Feature for Generic Visual Recognition", ICML 2014  
Razavian et al, "CNN Features Off-the-Shelf: An  
Astounding Baseline for Recognition", CVPR Workshops  
2014

Skipped in class  
(outside of scope)

# Using pretrained networks

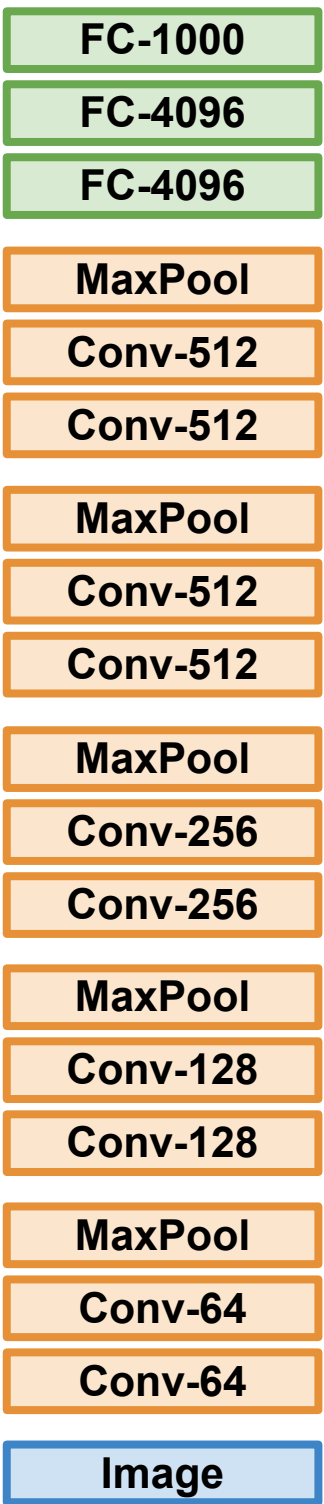
## 1. Train on Imagenet



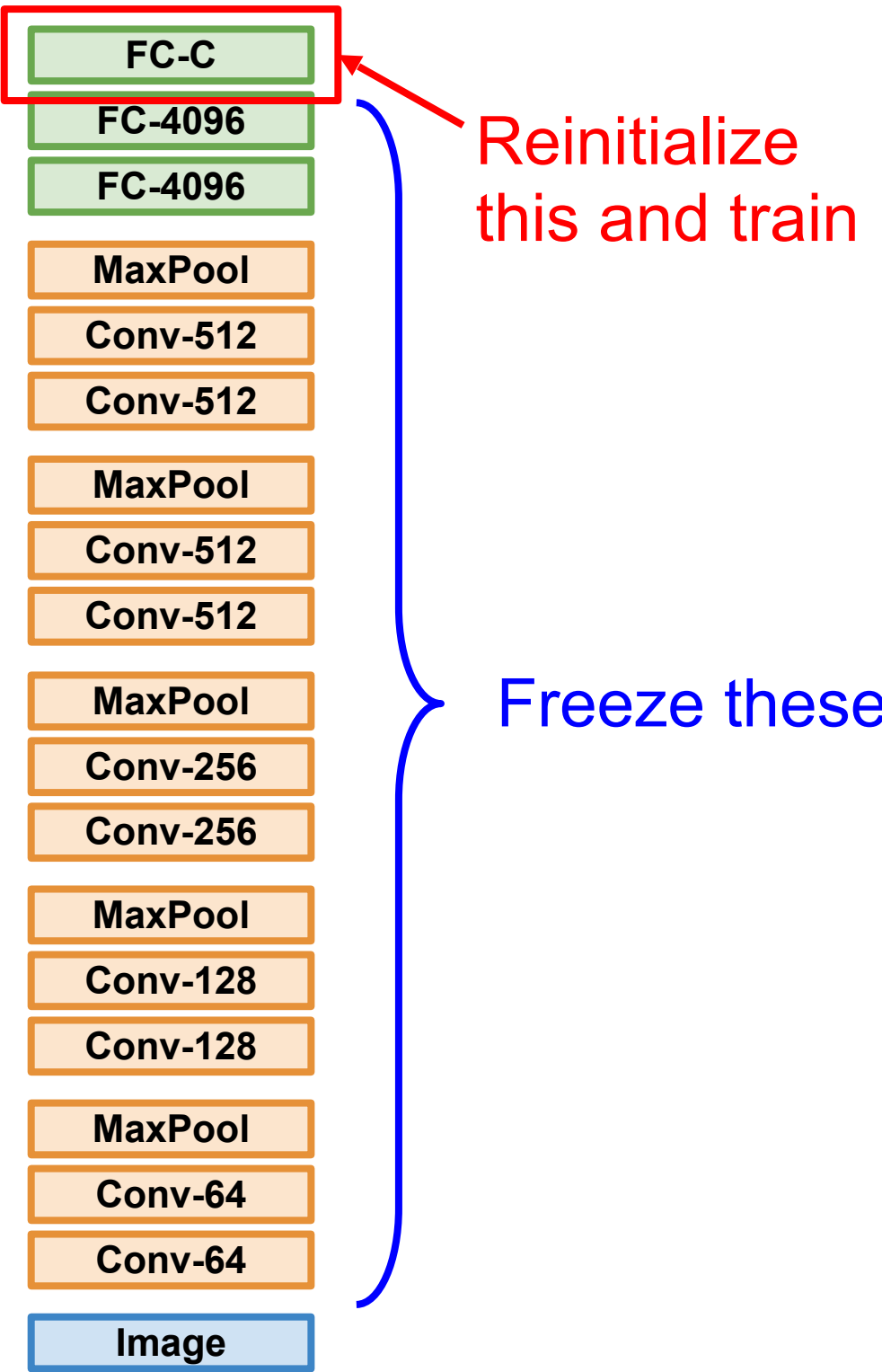
Skipped in class  
(outside of scope)

# Using pretrained networks

## 1. Train on Imagenet



## 2. Small Dataset (C classes)

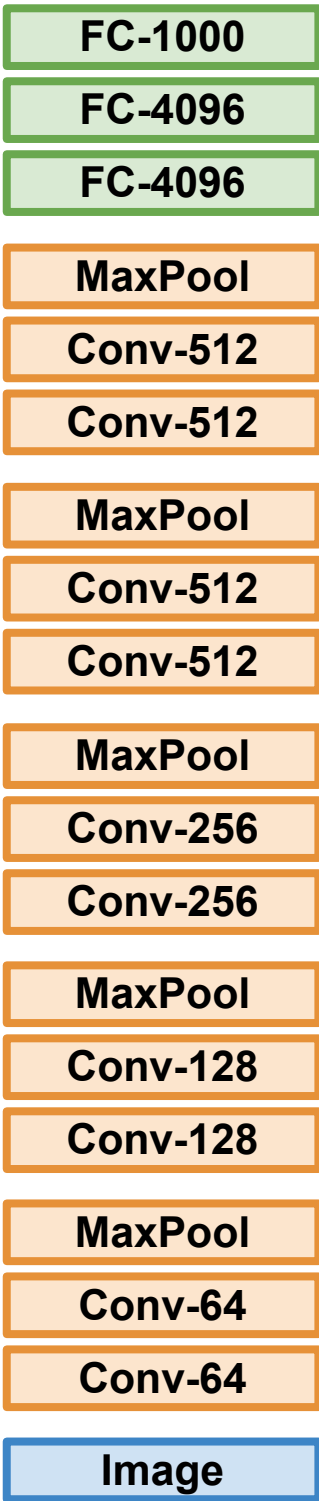




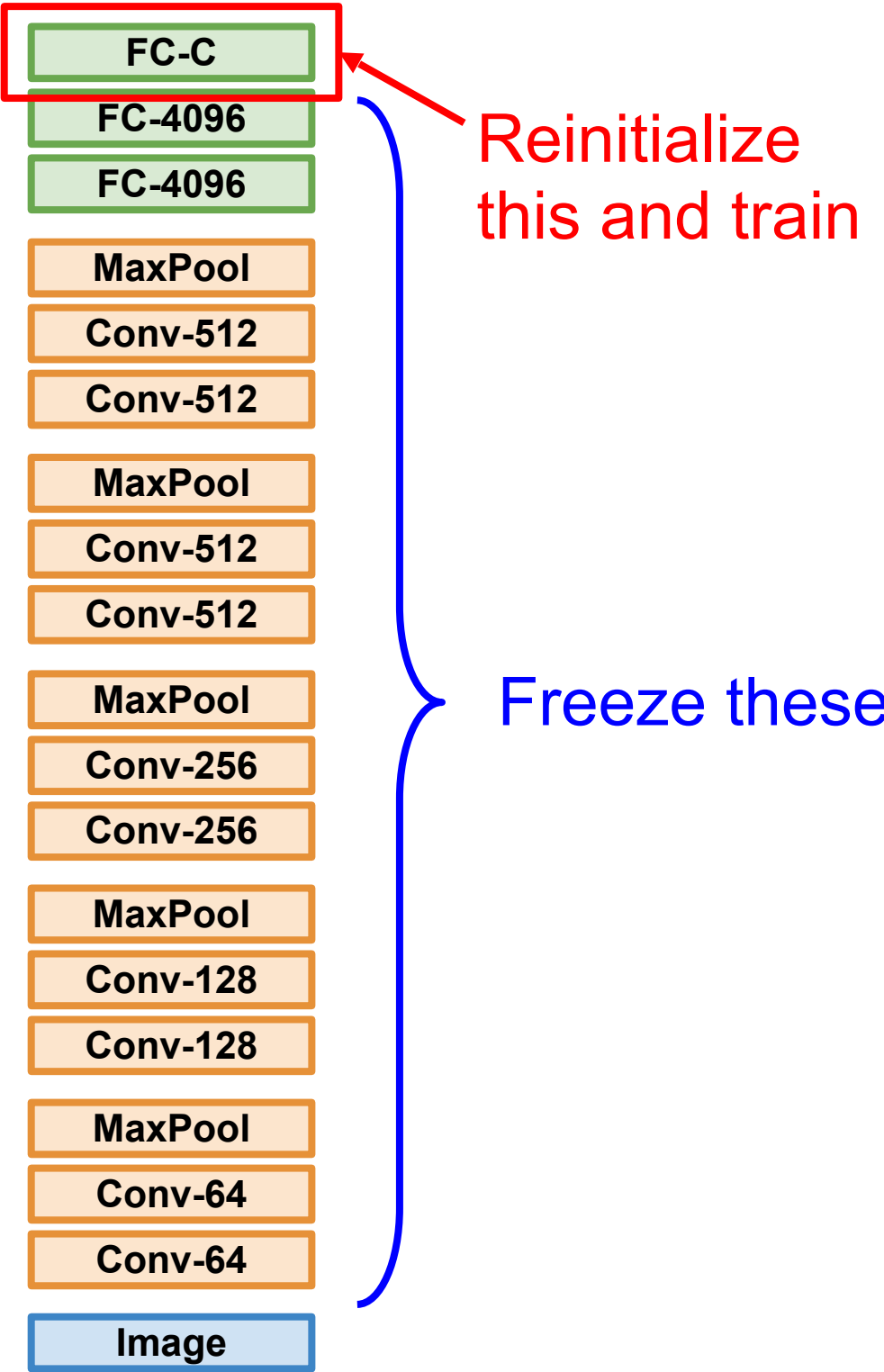
# Using pretrained networks

Skipped in class  
(outside of scope)

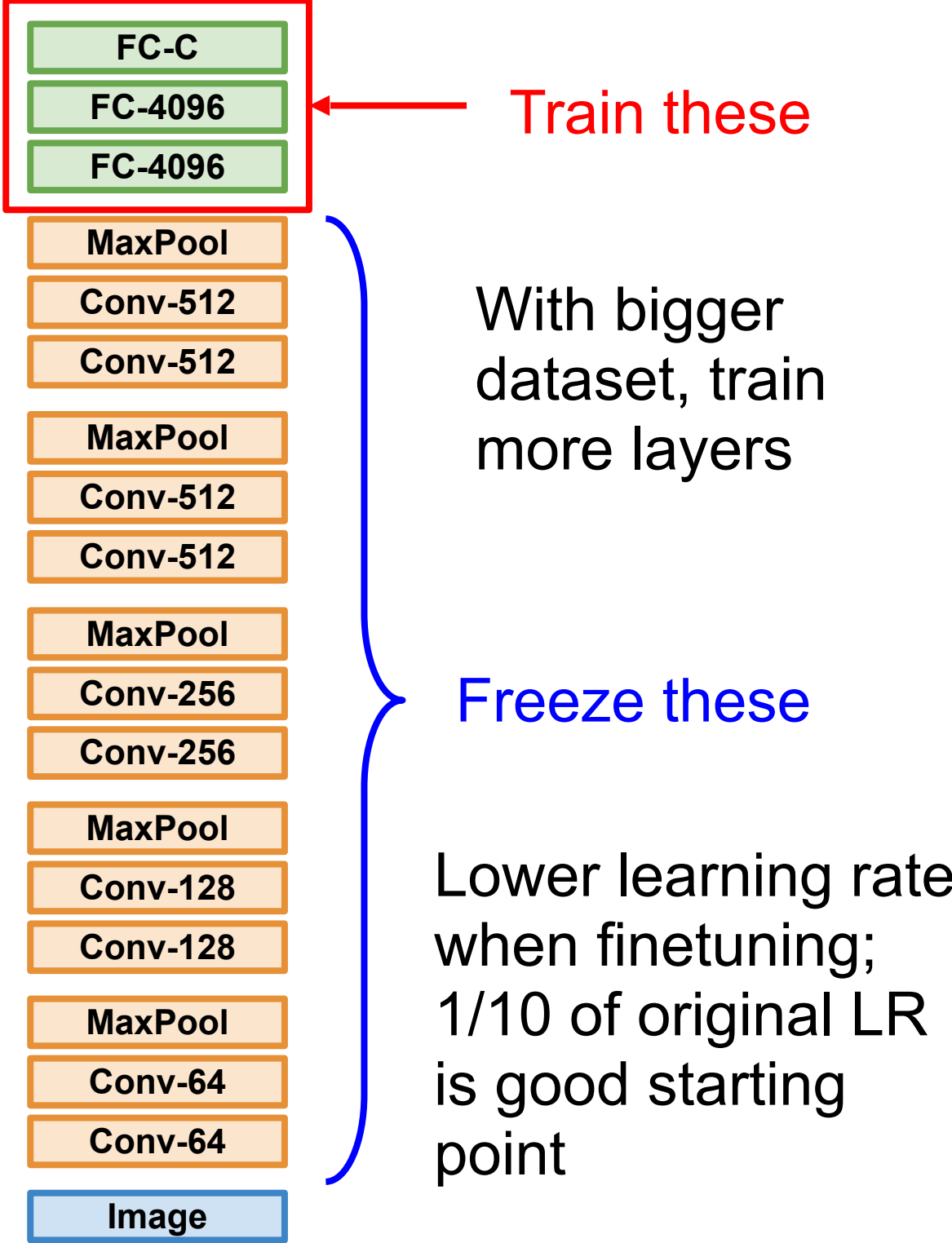
1. Train on Imagenet



2. Small Dataset (C classes)



3. Bigger dataset







# Large generative models

Skipped in class  
(outside of scope)







# Large generative models

Skipped in class  
(outside of scope)





# Fishing information within SD

Skipped in class  
(outside of scope)

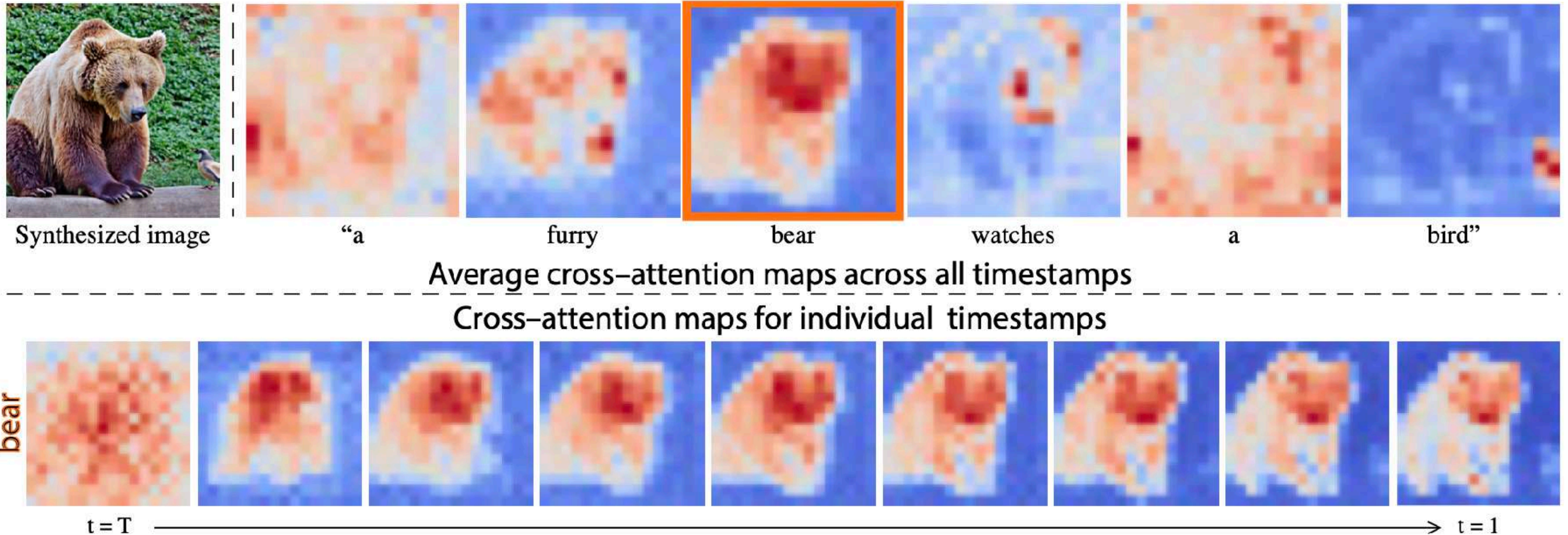


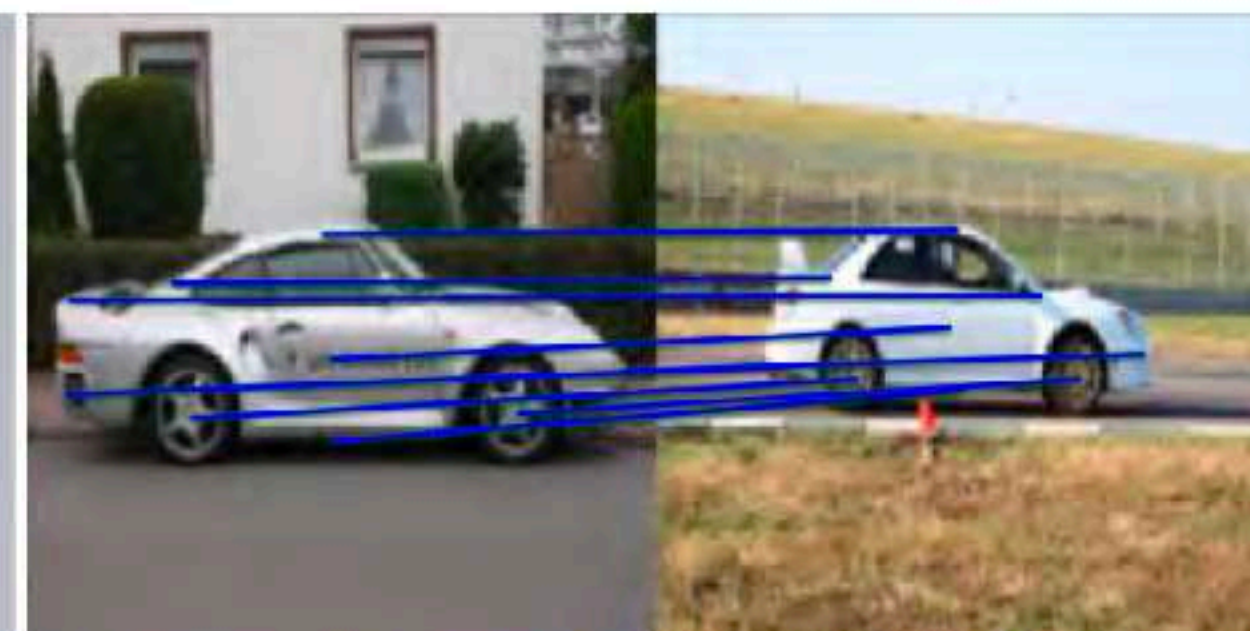
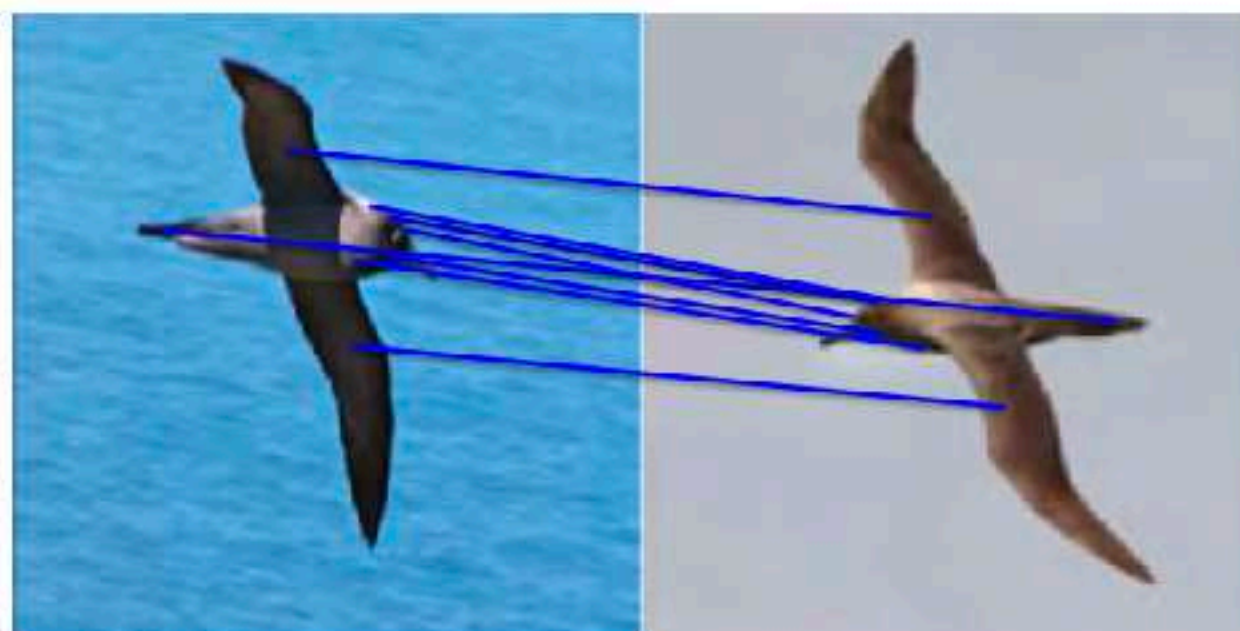
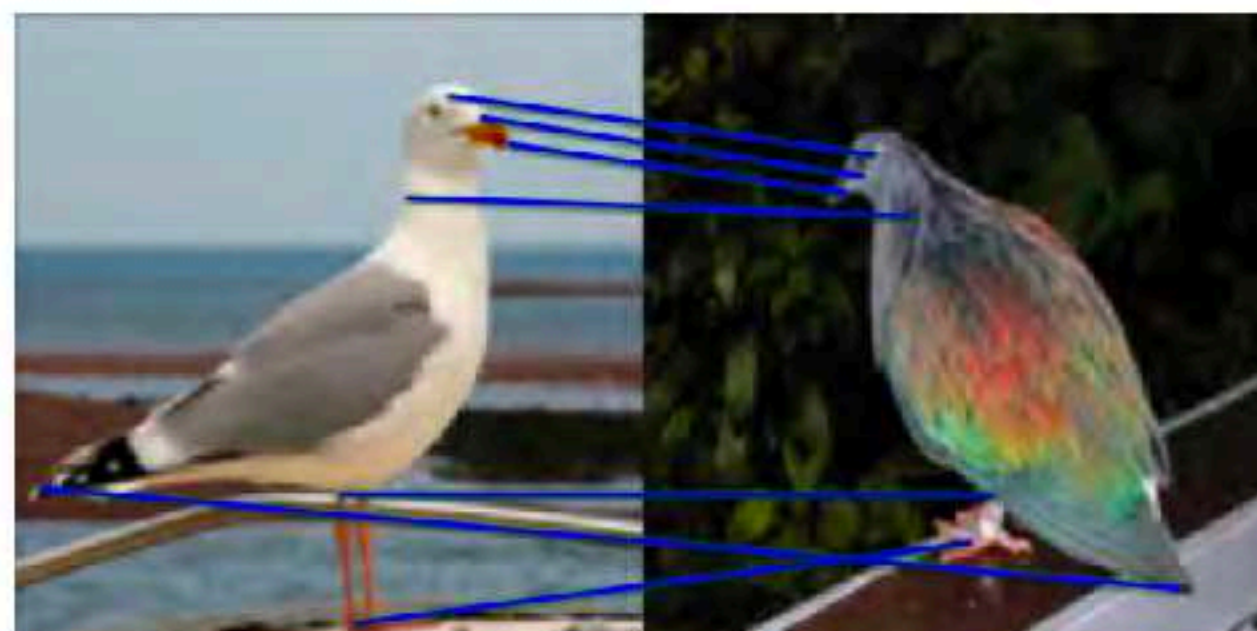
Image from [Hertz et al., ICLR, 2023]



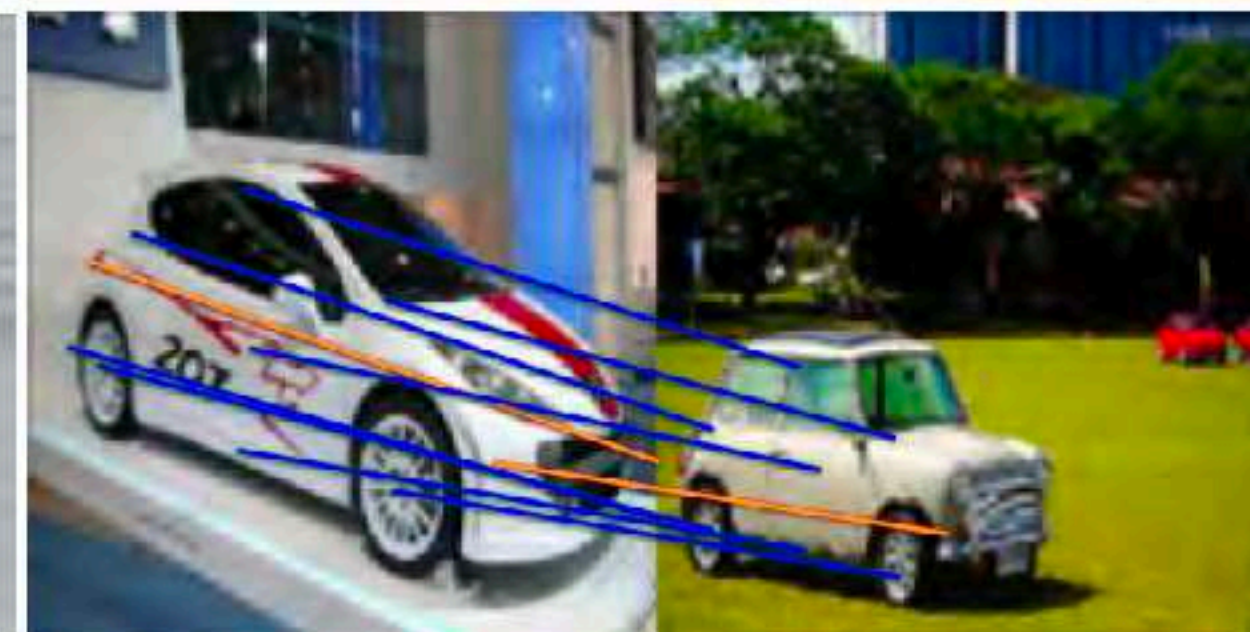
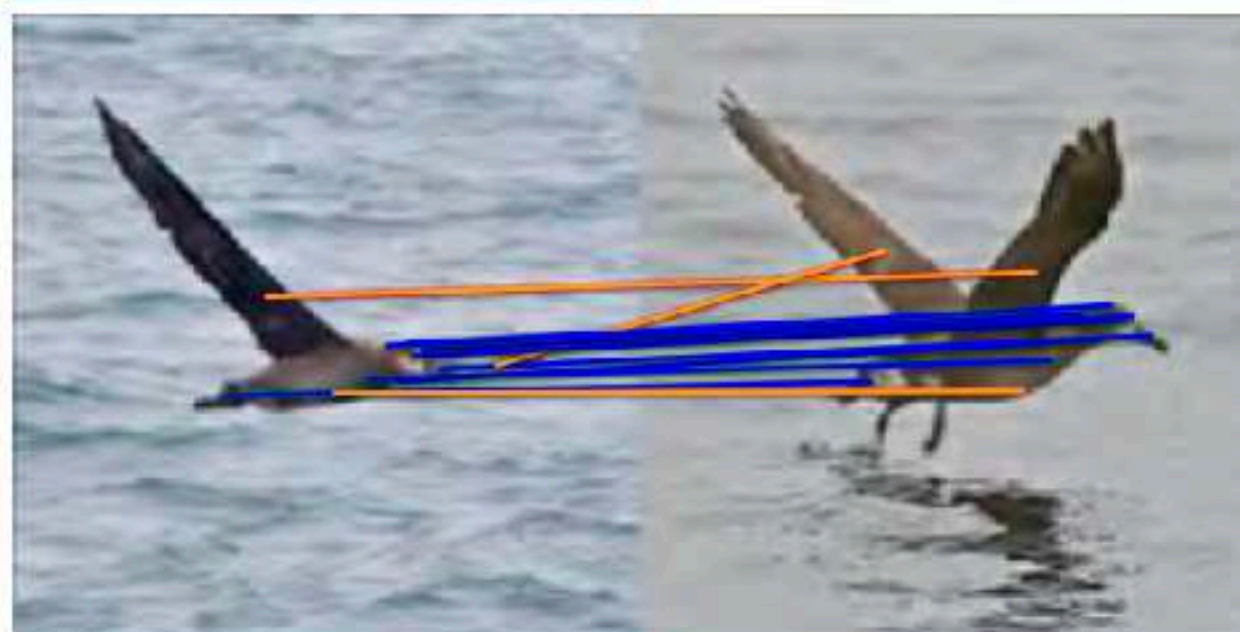
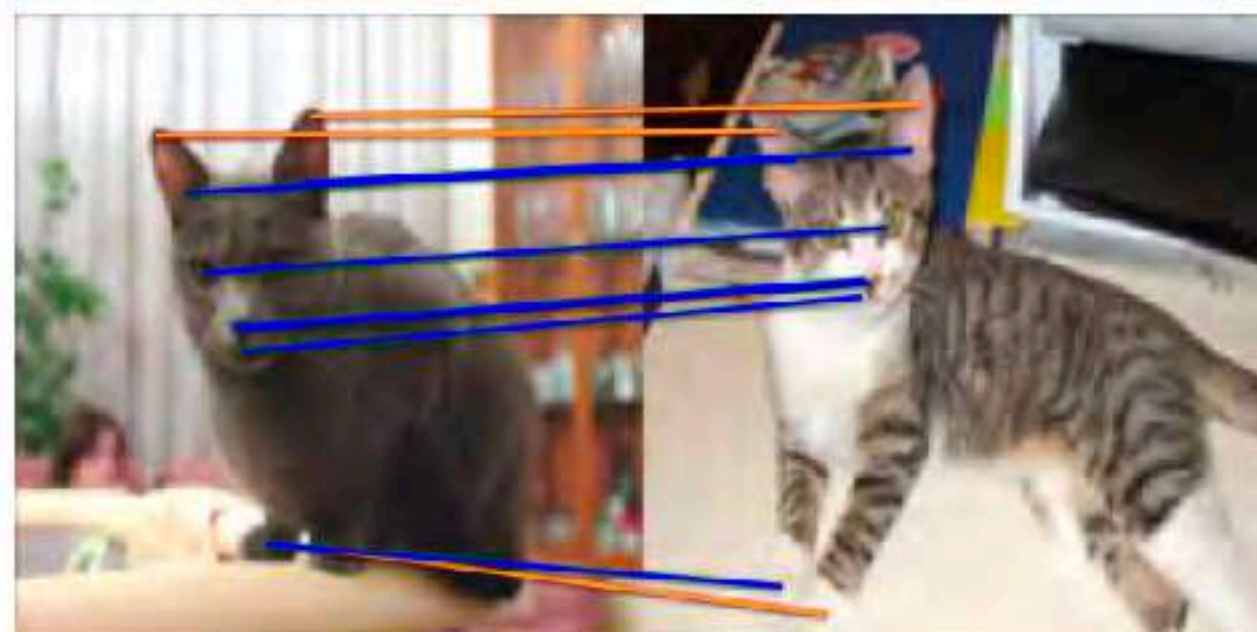
# Correspondences from SD

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(outside of scope)

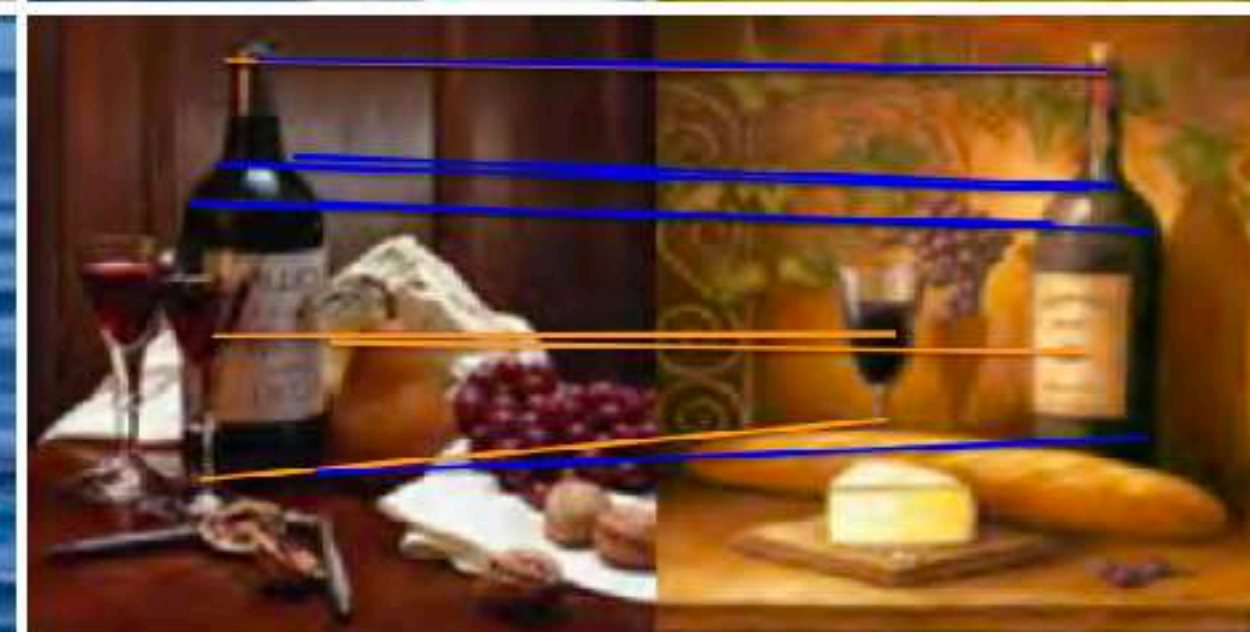
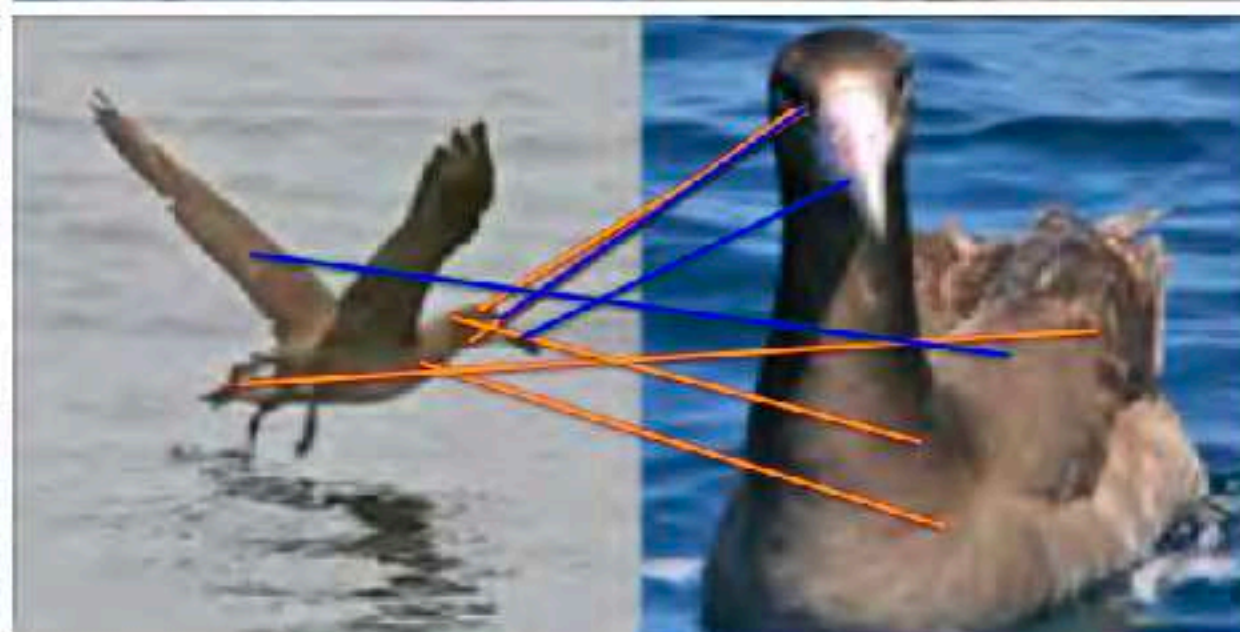
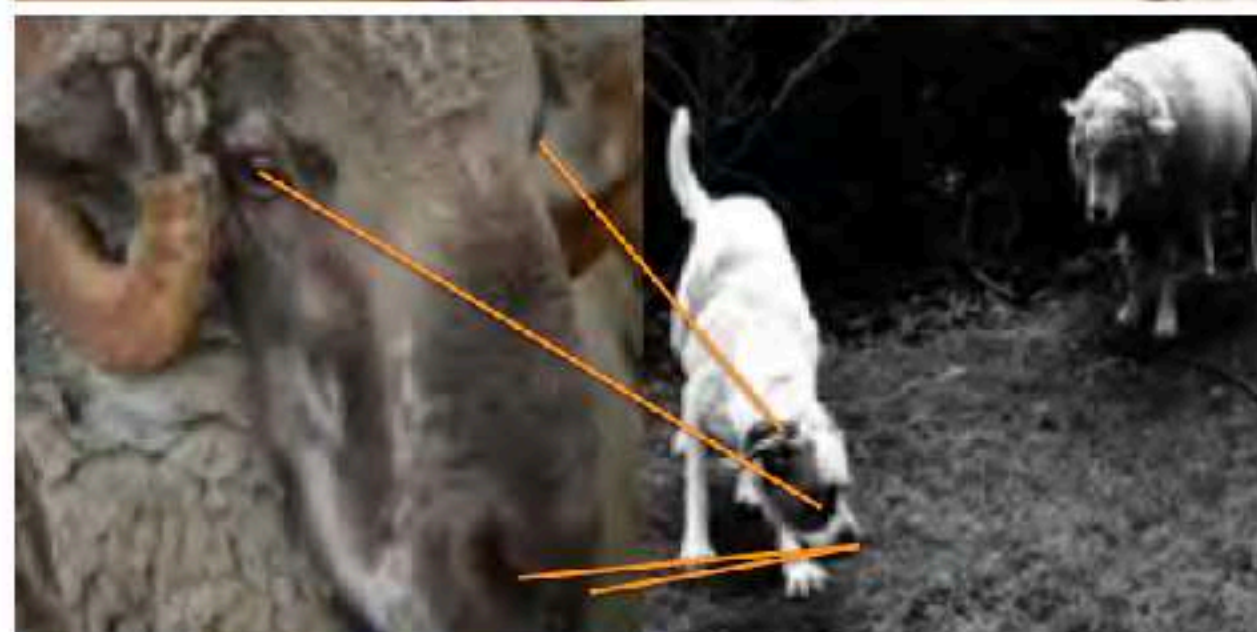
Successful



Mixed



Failure



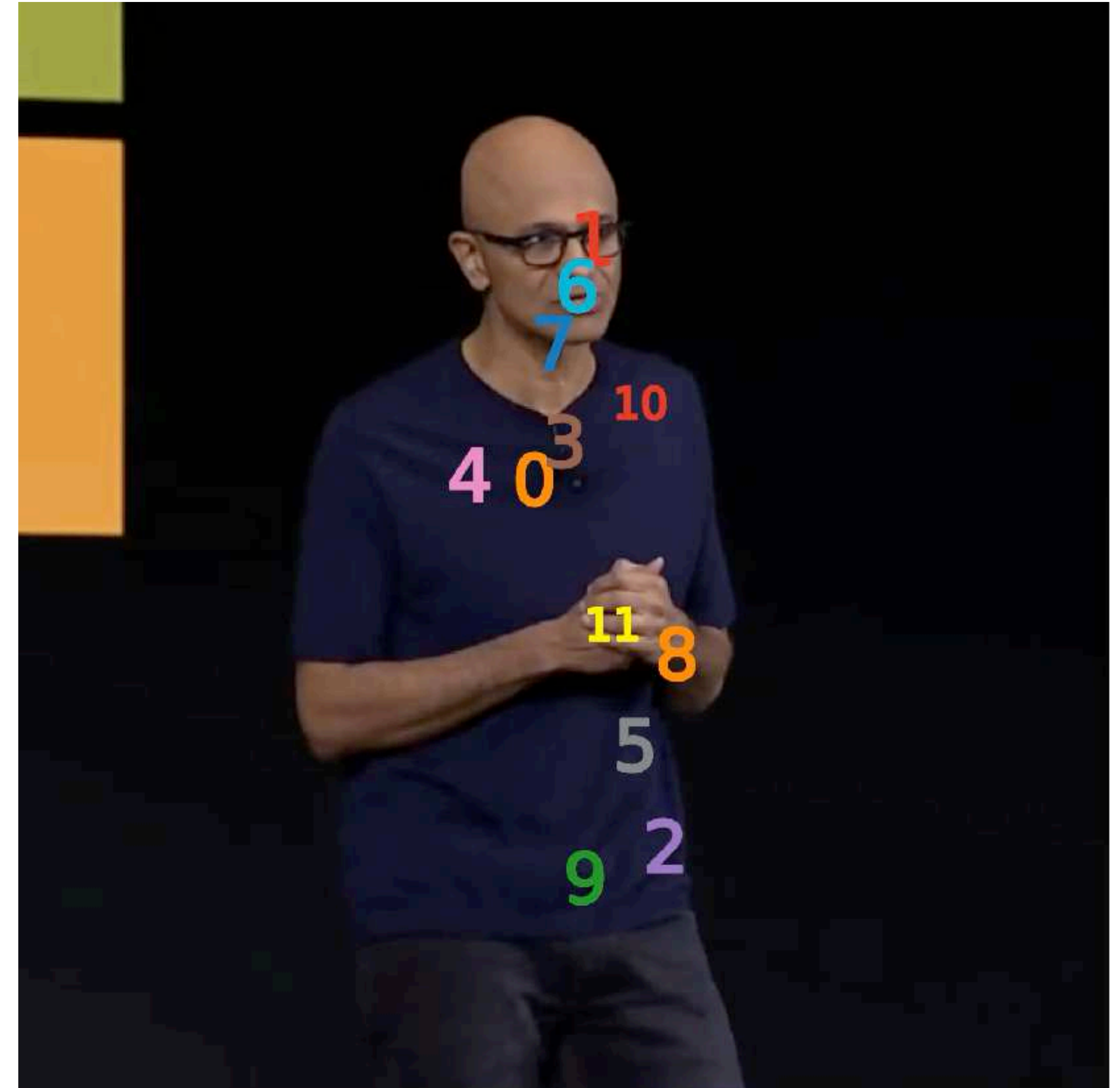
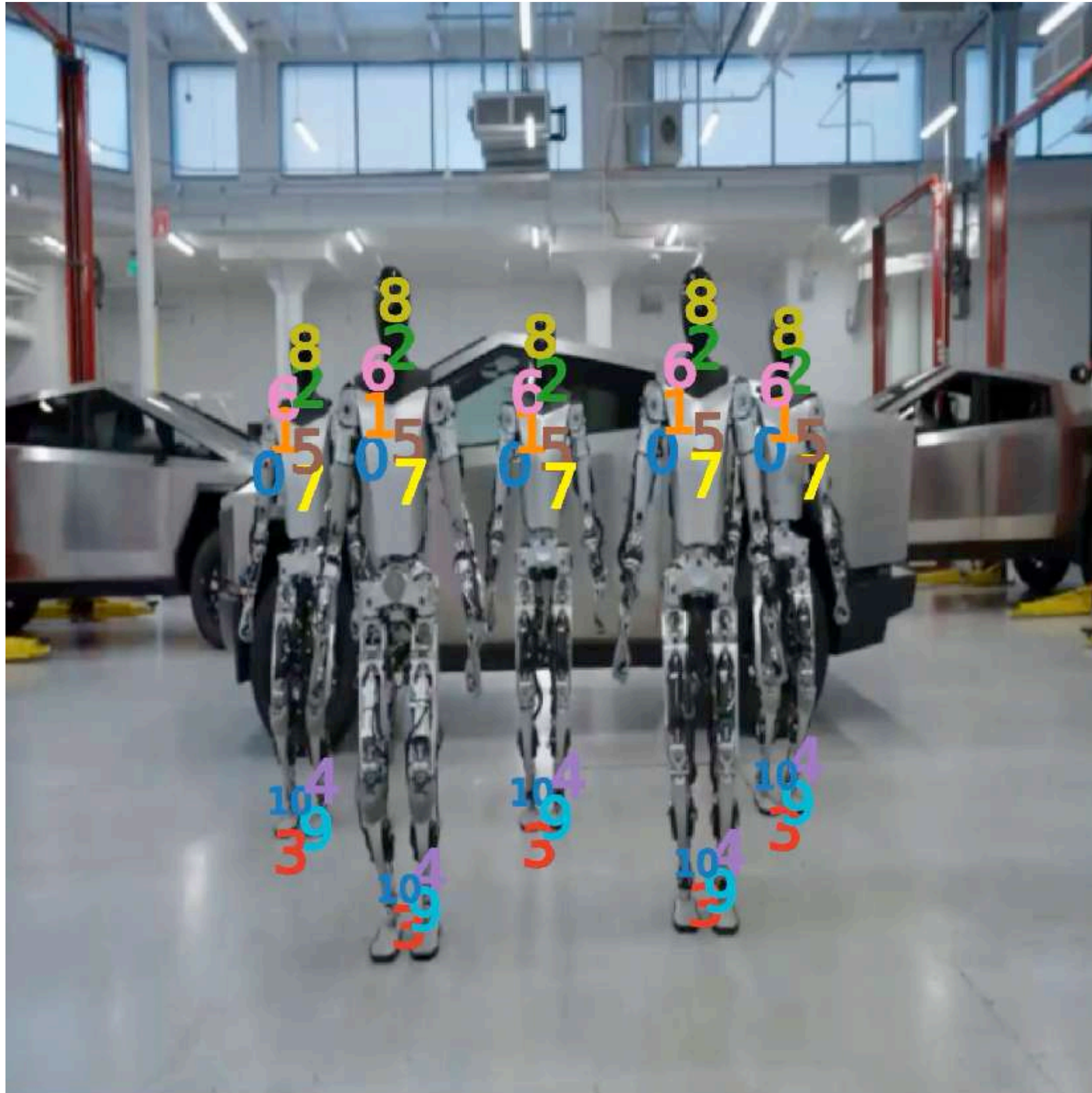
Spair-71k

CUB-200

PF-Willow



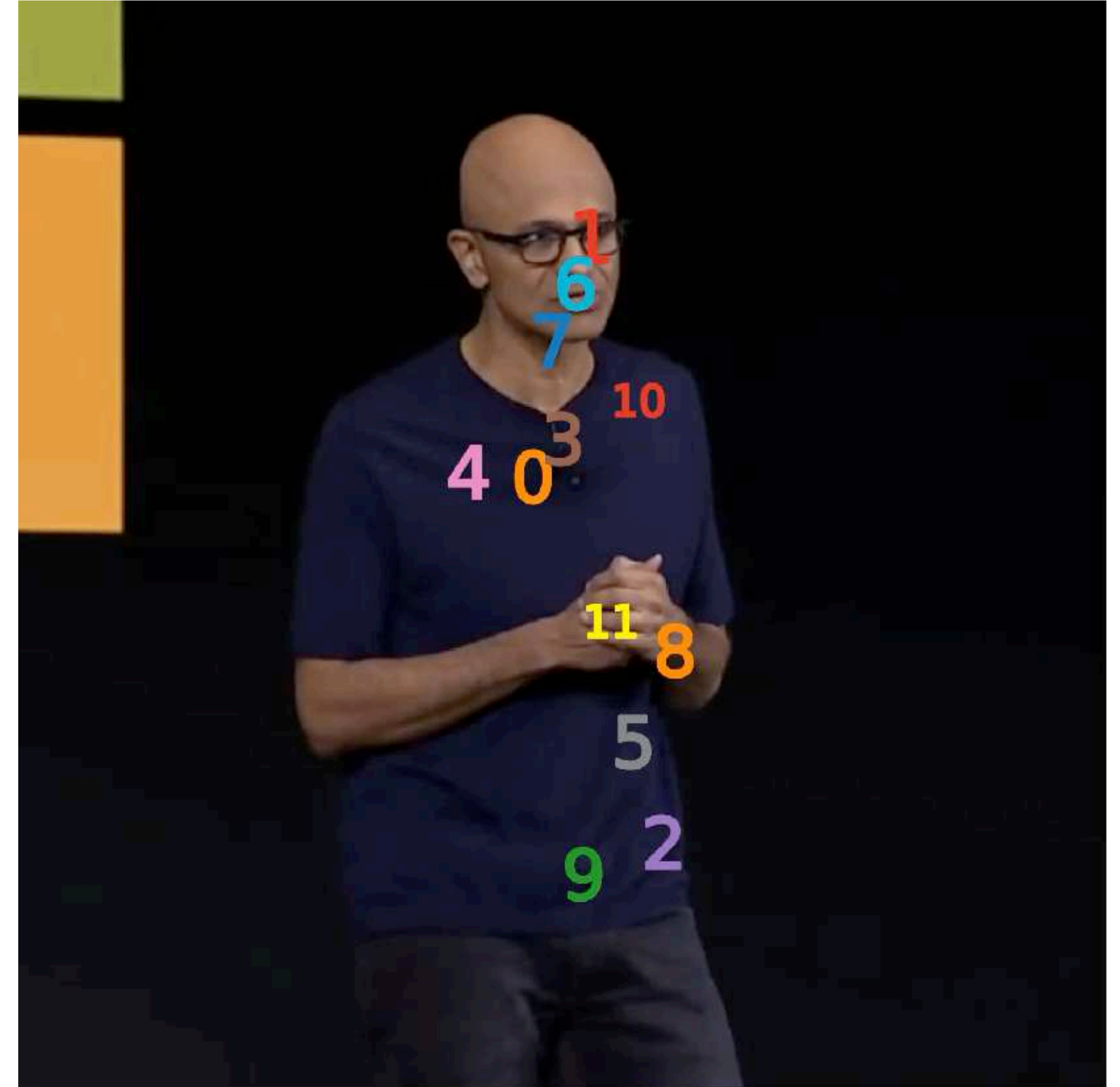
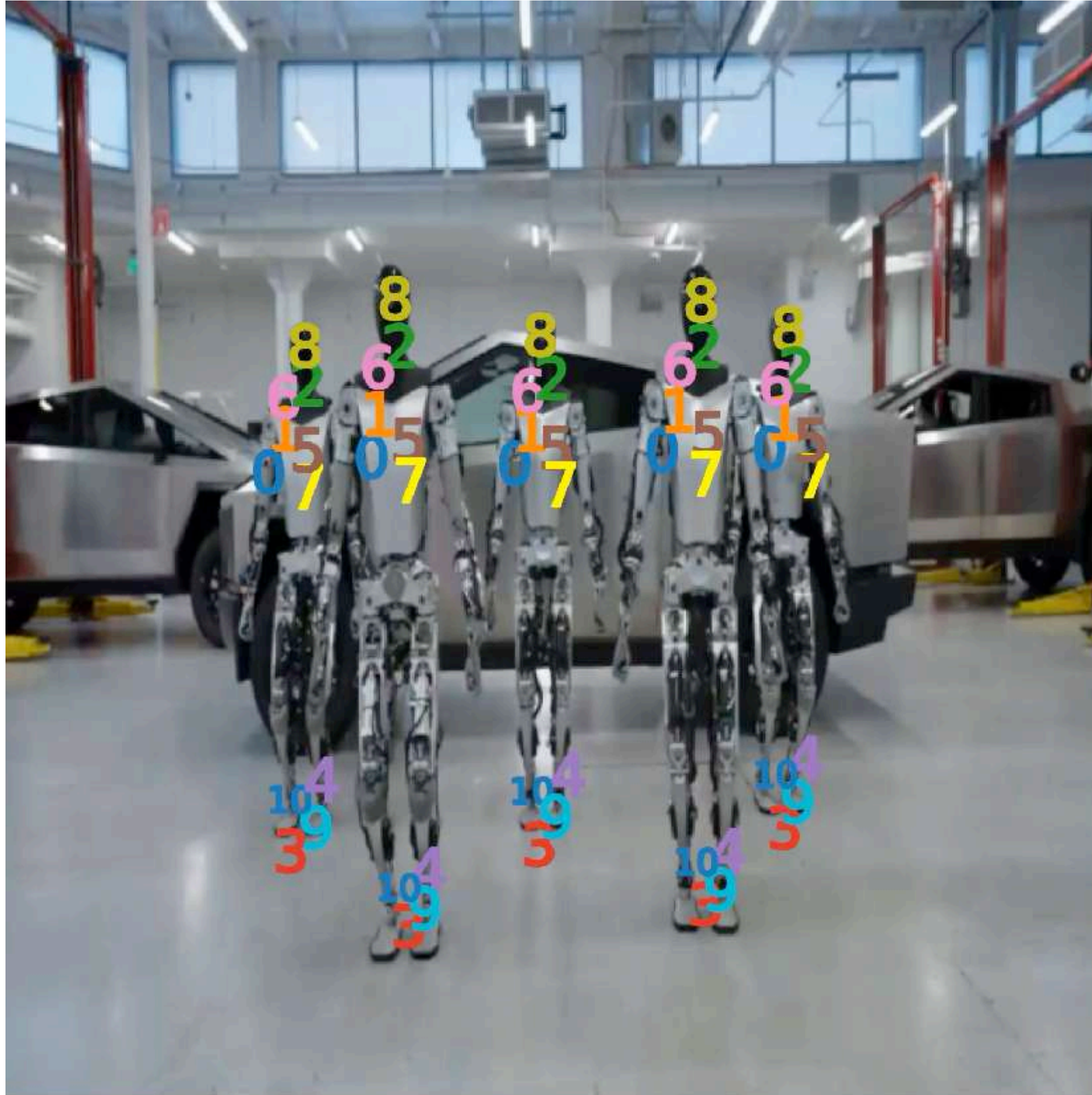
# Keypoints from SD (Skipped in class outside of scope)







# Keypoints from SD (Skipped in class outside of scope)





# Text-to-3D from SD (Skipped in class outside of scope)

**Input**

**Multi-view images**



*“A pepperoni pizza with arms and legs”*

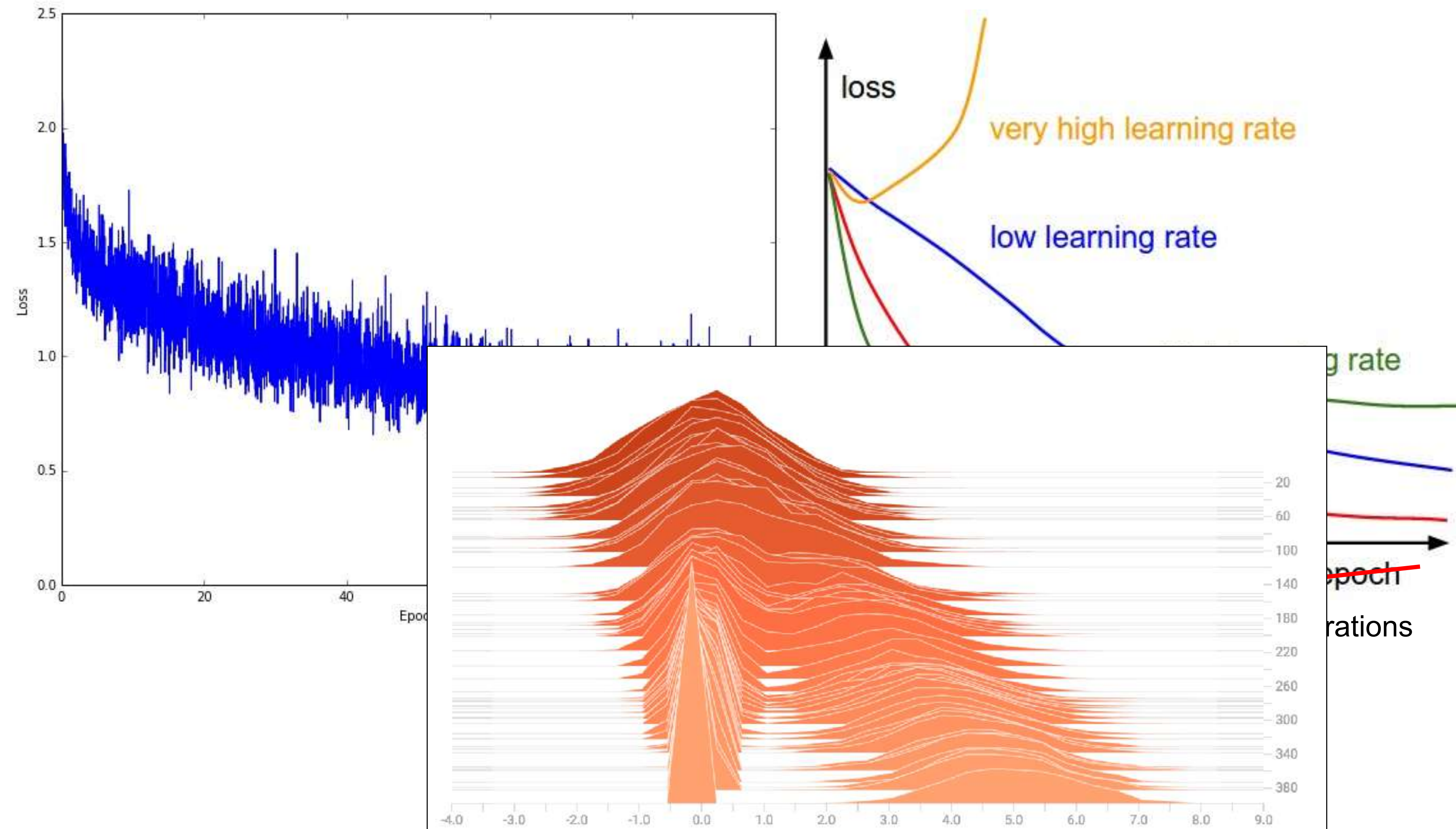


*“A cute squirrel”*



Skipped in class

Visualize VISUALIZE VISUALIZE (outside of scope)



More on Neural Networks

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(outside of scope)

Lots more to learn! A good place to start is

**Justin Johnson**, University of Michigan, EECS 498/598, e.g.,  
<https://web.eecs.umich.edu/~justincj/teaching/eecs498/WI2022/>



# Training Neural Nets: **Clever** Hans

Skipped in class  
(outside of scope)





# Training Neural Nets: **Clever** Hans

Skipped in class  
(outside of scope)



Hans could get 89% of the math questions right



# Training Neural Nets: **Clever** Hans

Skipped in class  
(outside of scope)



Hans could get 89% of the math questions right