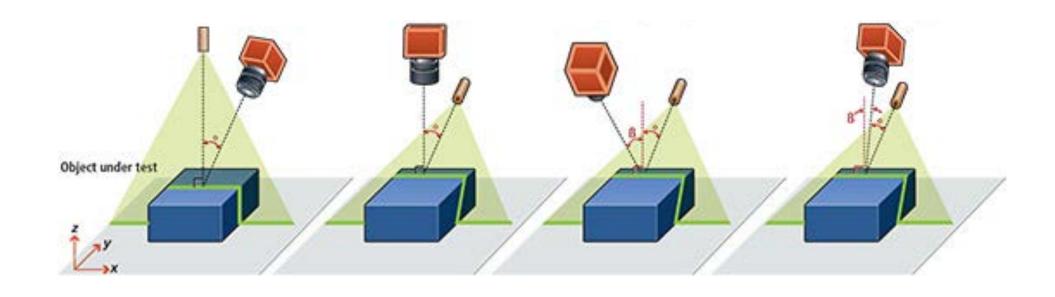


#### THE UNIVERSITY OF BRITISH COLUMBIA

# **CPSC 425: Computer Vision**



(slide credits / thanks to Bob Woodham, Jim Little, Fred Tung, Leonid Sigal, and Matthew Brown)

Lecture 2: Image Formation

## Waitlisted Students

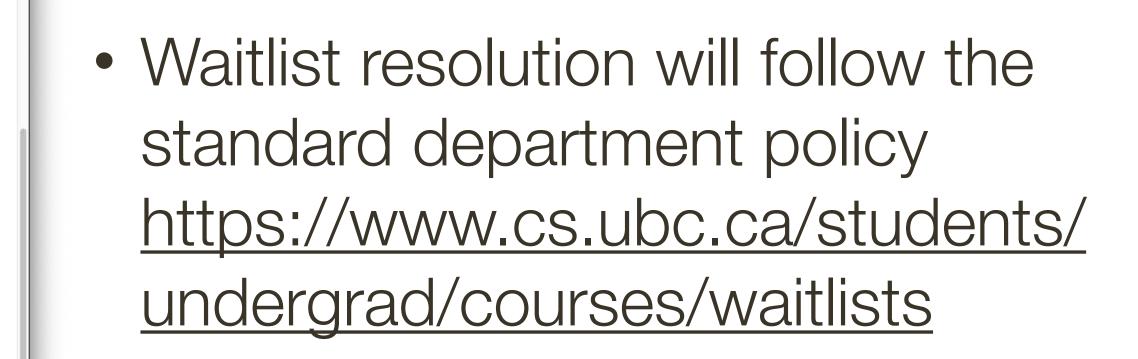
# All course materials will be on the public webpage, and there will be + no graded assessment before add drop deadline (Jan 17th)

🗾 😳 🖞 🕂

Kwang Moo Yi @ University of British Columbia Home Te	eam Publications	Teaching	Openings G	GitHub
Prerequisites				
MATH 200, MATH 221 and either (a) CPSC 221 or (b) CPSC 260, EECE 320.				
Textbook				
Recommended but NOT required.				
<ul> <li>Computer Vision: Algorithms and Applications, 2nd edition, by R. Szeliski, 20</li> <li>Computer Vision: A Modern Approach, 2nd edition, by D.A. Forsyth and J. Pol</li> </ul>				
<ul> <li>Understanding Deep Learning, Simon J.D. Prince, 2023</li> </ul>				
Understanding Deep Learning, Simon J.D. Prince, 2023     Assignments				
Assignments Assignments are to be done individually by each student. We will be actively lookir zero-tolerance on any case, and will not make any distinctions between those who				
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Assignments are to be done individually by each student. We will be actively lookir zero-tolerance on any case, and will not make any distinctions between those who it! Assignment Assignment 0: Introduction to Python for Computer Vision (optional)		eceived help. <b>Available</b> Jan 6	And frankly, it's no <b>Due</b> Jan 15 (optiona	ot worth
Assignments are to be done individually by each student. We will be actively lookin zero-tolerance on any case, and will not make any distinctions between those who it! Assignment Assignment 0: Introduction to Python for Computer Vision (optional) Assignment 1: Image Filtering and Hybrid Images		Available Jan 6 Jan 13	And frankly, it's no <b>Due</b> Jan 15 (optiona Jan 29	ot worth
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of the term, such as travel, moderate illness, conflicts with other courses, extracurricular obligations, job interviews, etc. Thus, additional late days will NOT be granted except under truly exceptional circumstances. If an assignment is submitted late and a student has used up all of her/his

### https://www.cs.ubc.ca/~kmyi/teaching/cpsc425/



## **This Lecture**

**Topics:** Image Formation

- Image Formation
- Cameras and Lenses

**Readings:** 

- Next Lecture: Forsyth & Ponce (2nd ed.) 4.1, 4.5

#### - Projection

- Today's Lecture: Szeliski Chapter 2, Forsyth & Ponce (2nd ed.) 1.1.1 – 1.1.3





### Lecture 2: Goal

# To understand how images are formed

(and develop relevant mathematical concepts and abstractions)

## What is **Computer Vision**?

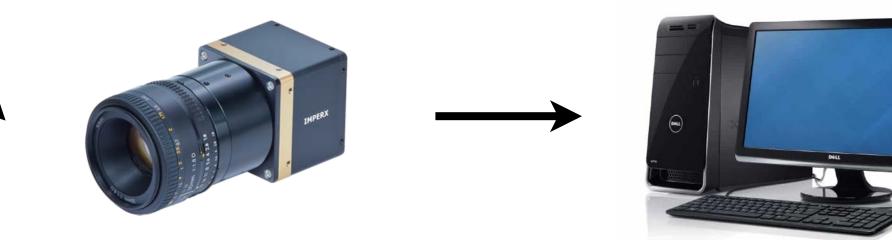
### Compute vision, broadly speaking, is a research field aimed to enable computers to process and interpret visual data, as sighted humans can.

**Sensing** Device









**Interpreting** Device





#### Interpretation

flamephoenix1991/8376271918

blue sky, trees, fountains, UBC, ...

5



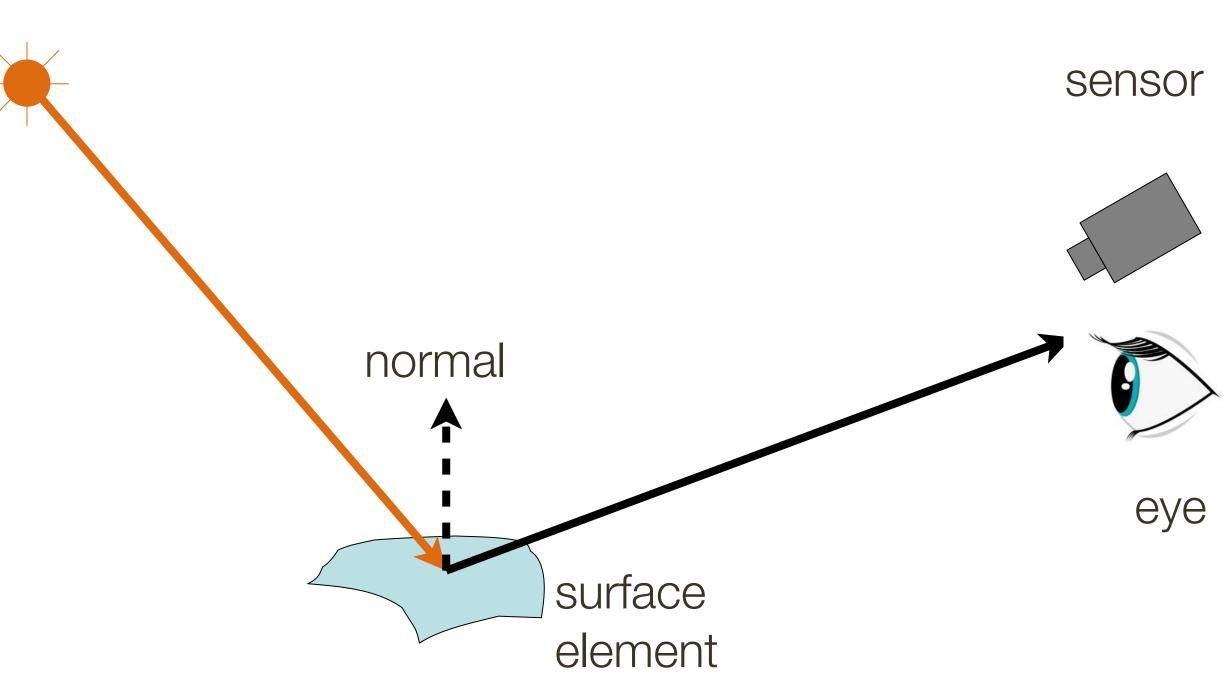
## Overview: Image Formation, Cameras and Lenses

source

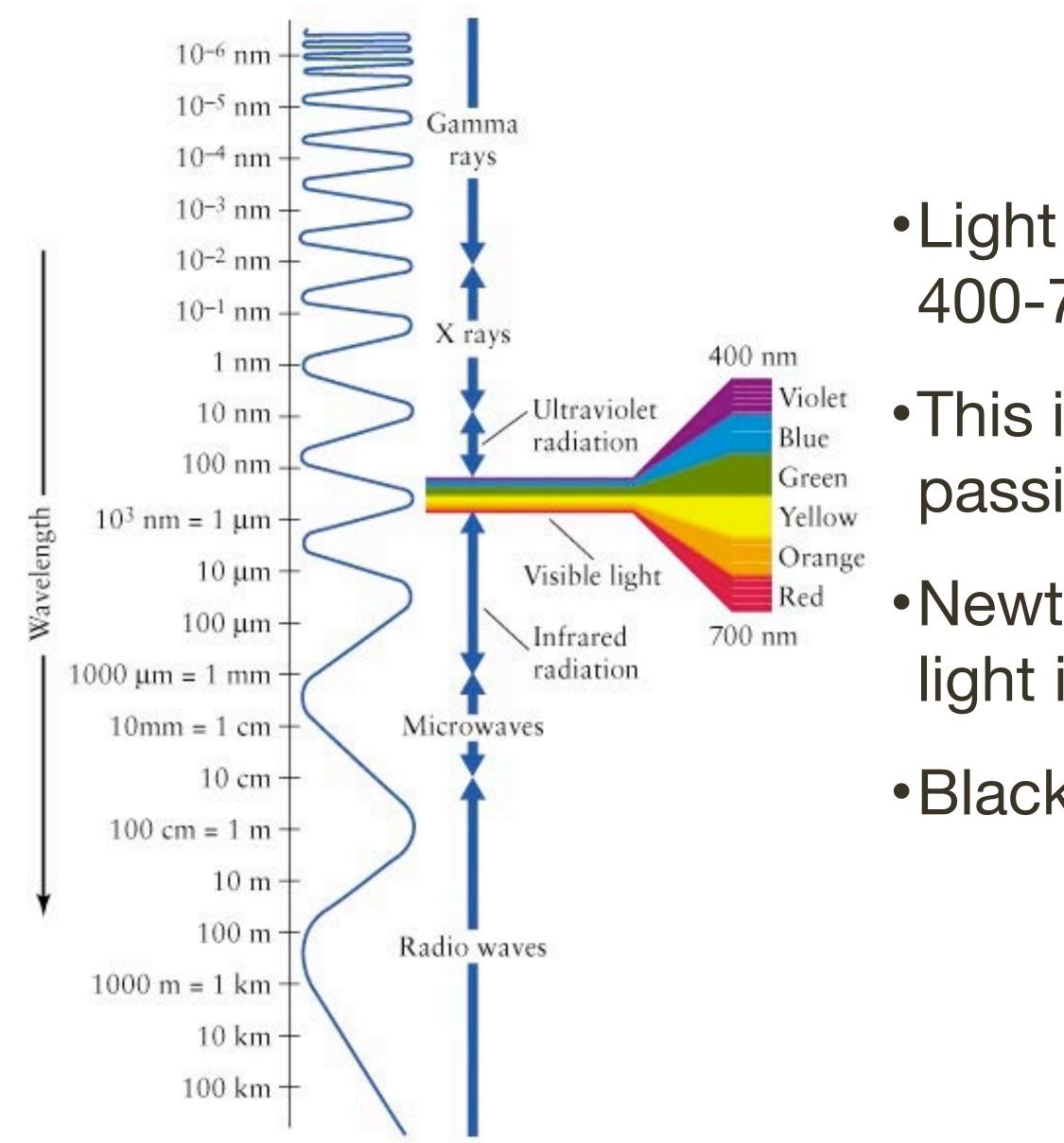
The image formation process that produces a particular image depends on

- Lighting condition
- Scene geometry
- Surface properties
- Camera optics and viewpoint

### Sensor (or eye) captures amount of light reflected from the object



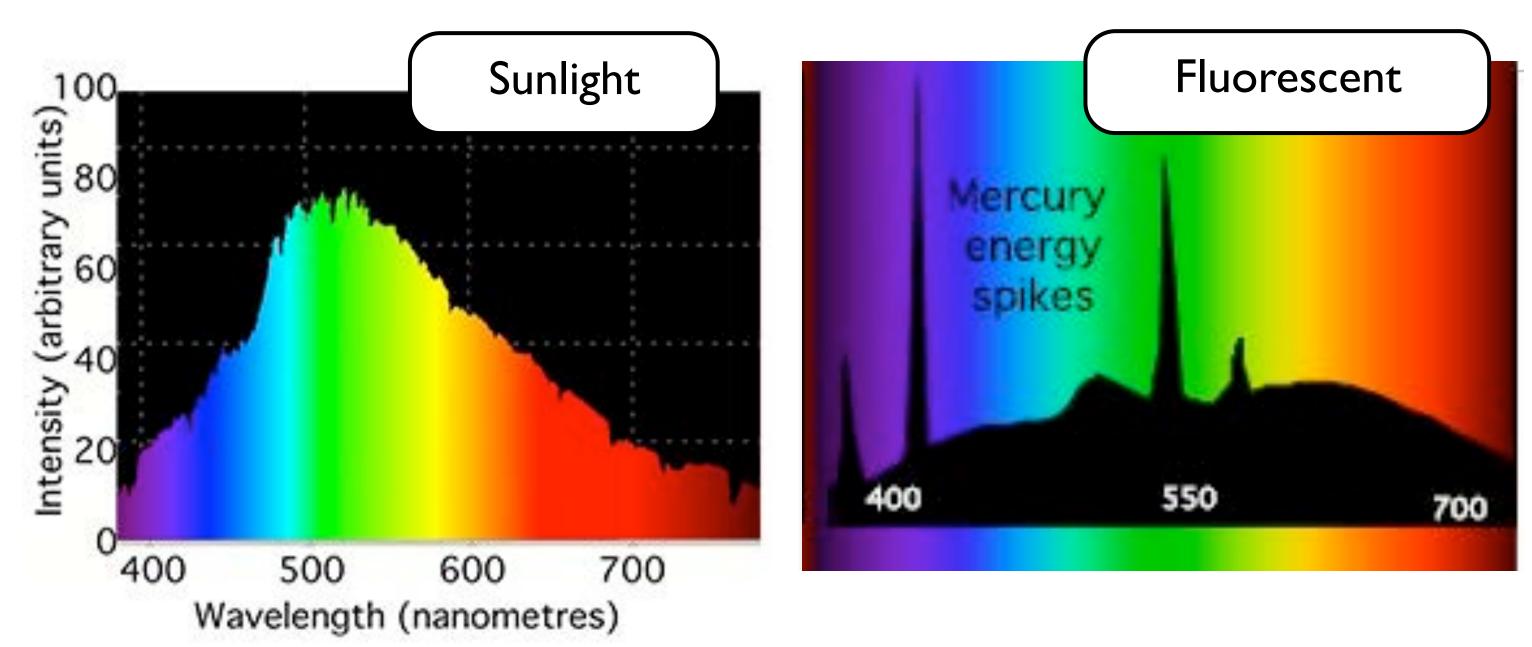
## Light and Color



- •Light is electromagnetic radiation in the 400-700nm band
- This is the peak in the spectrum of sunlight passing through the atmosphere
- Newton's Prism experiment showed that white light is composed of all frequencies
- Black is the absence of light!

9

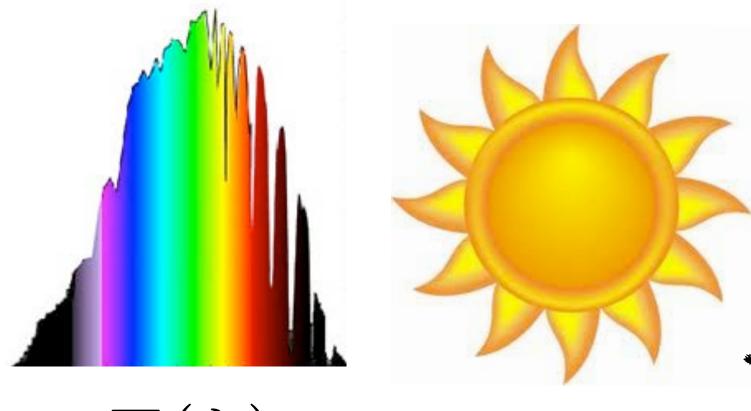
## Spectral Power Distribution



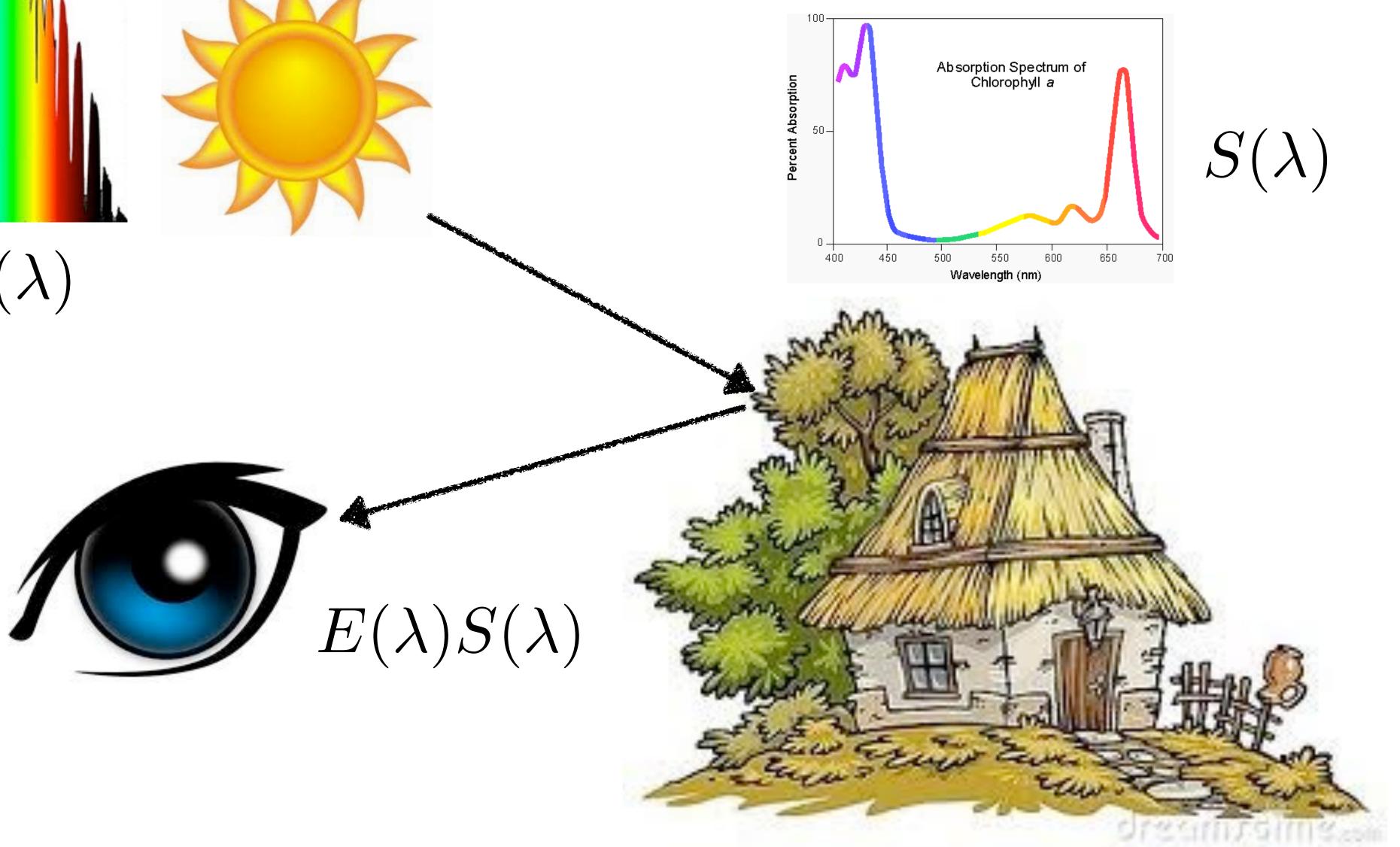
- •The spectral distribution of energy in a light ray determines its colour
- Surfaces reflect light energy according to a spectral distribution as well
- The combination of incident spectra and reflectance spectra determines the light colour

[scratchapixel.com]

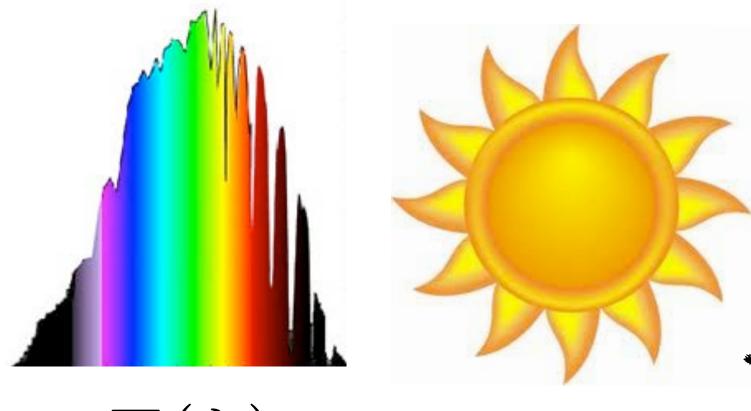
### Spectral Reflectance Example



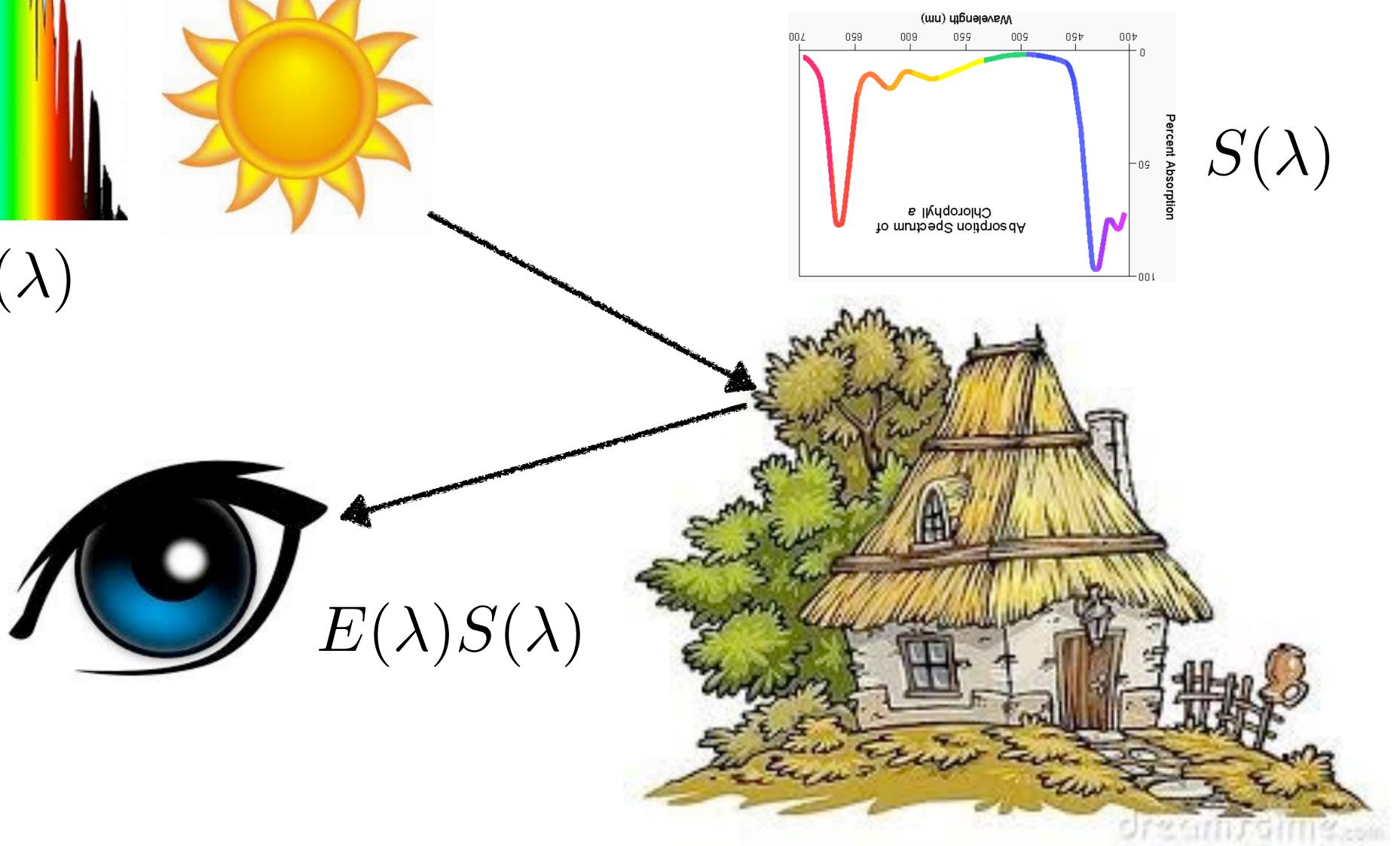
 $E(\lambda)$ 



### Spectral Reflectance Example



 $E(\lambda)$ 



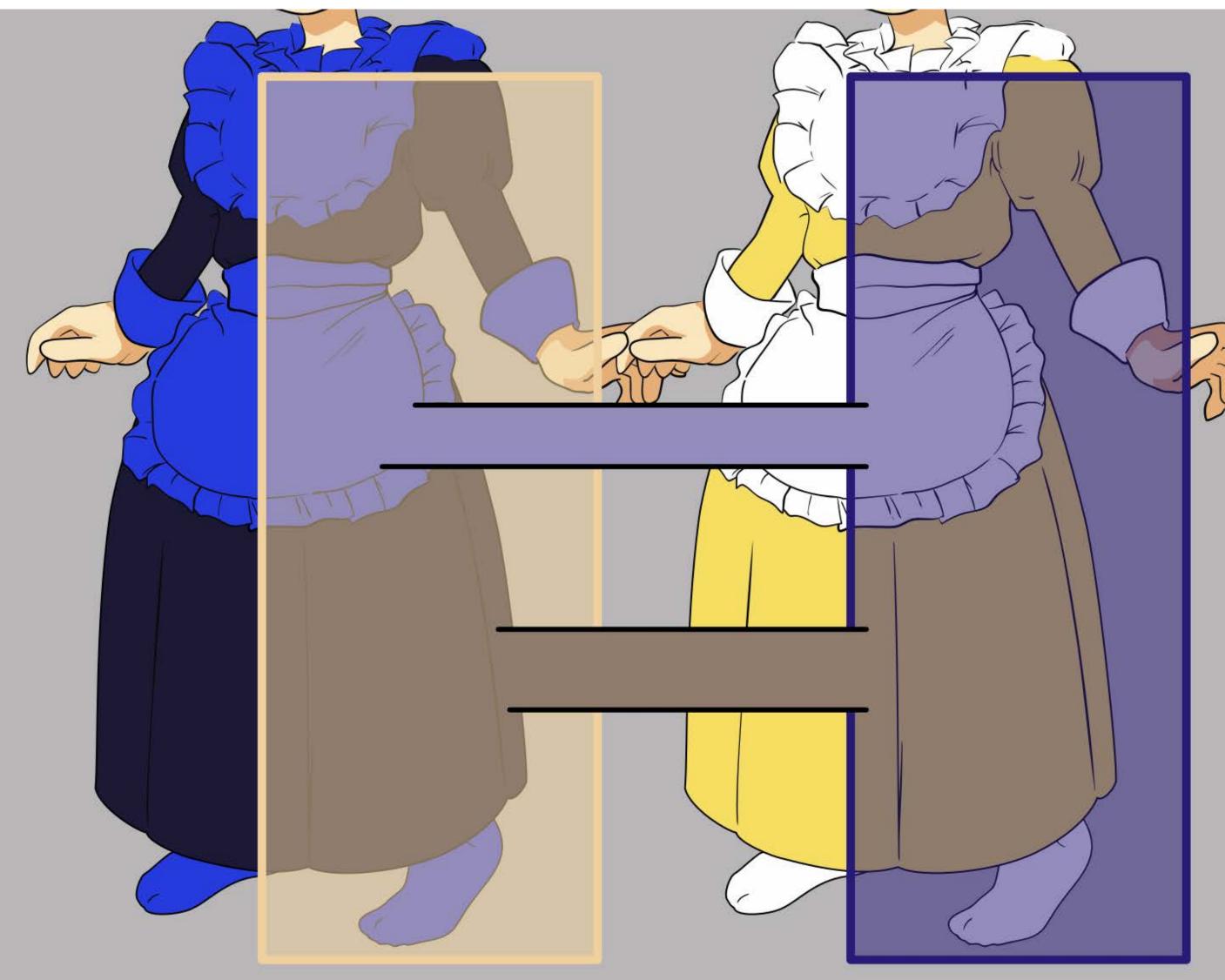
## Our brains already knows this



https://en.wikipedia.org/wiki/The\_dress

## Our brains already knows this





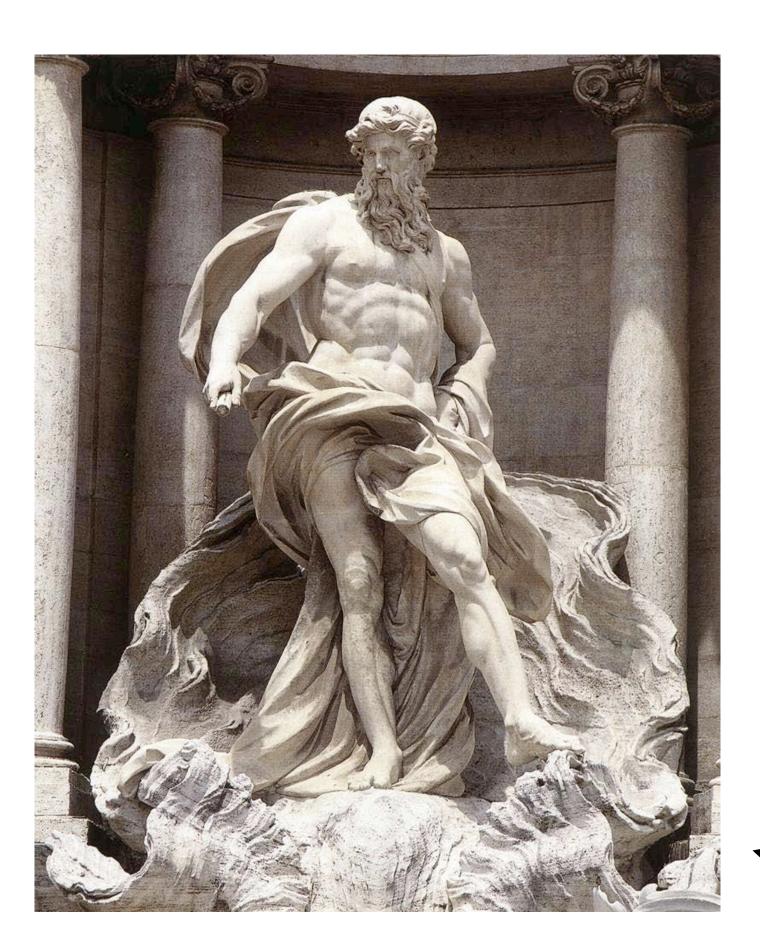
https://en.wikipedia.org/wiki/The\_dress

Figure design by Kasuga~jawiki; vectorization by Editor at Large; "The dress" modification by Jahobr, CC-BY-SA 2.5 Generic



### Surface Reflectance

• Reflected intensity also depends on geometry: surface orientation, viewer position, shadows, etc.

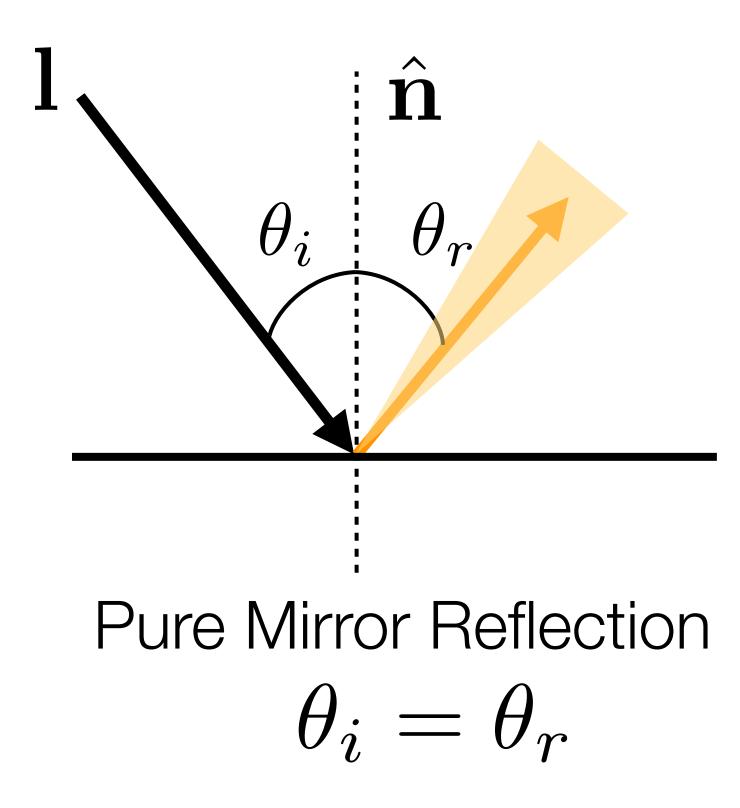


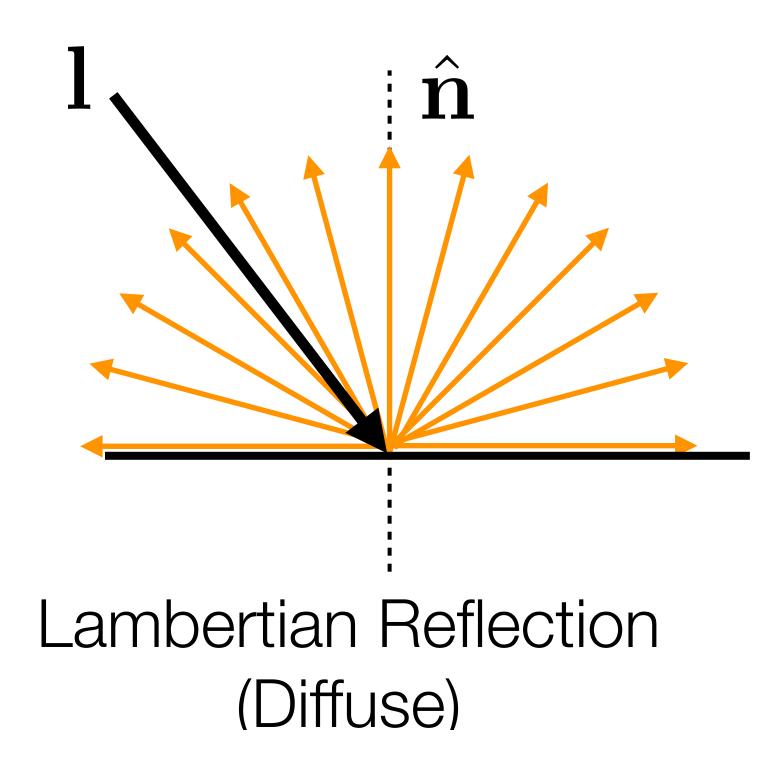


It also depends on surface properties, e.g., diffuse or specular

## Diffuse and Specular Reflection

- A pure mirror reflects light along a line symmetrical about the surface normal A pure diffuse surface scatters light equally in all directions



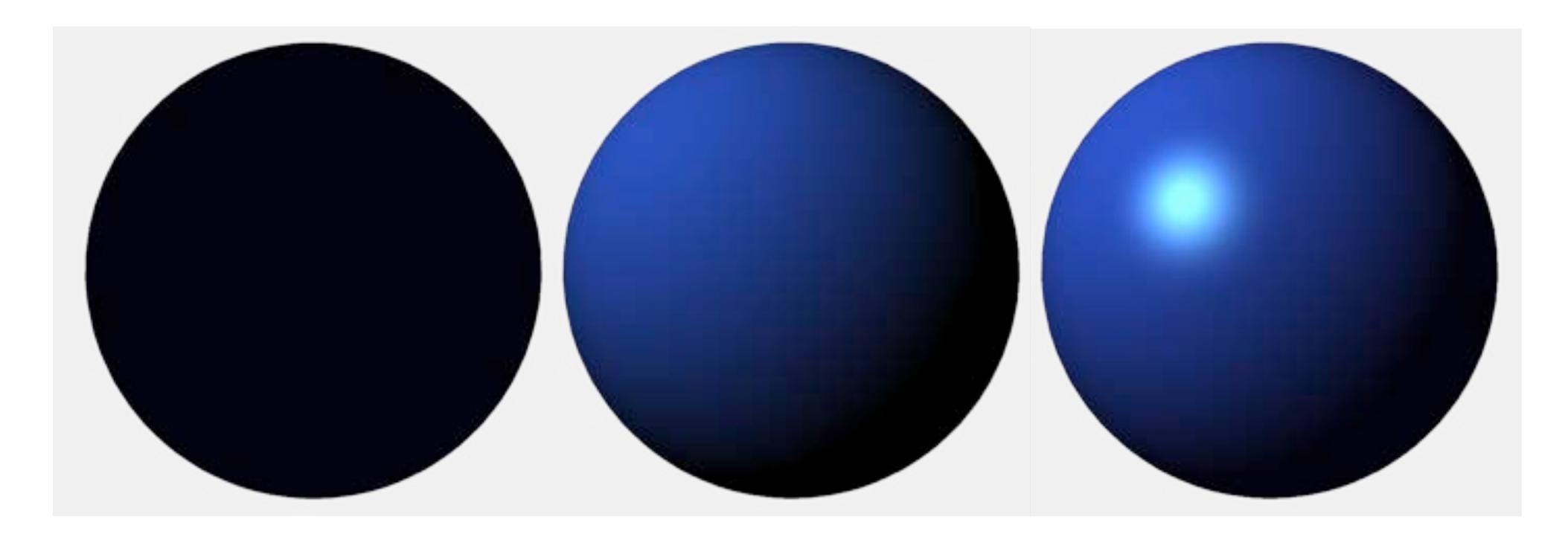


**Specular** surfaces directly reflect over a small angle



## Diffuse and Specular Reflection

• A sphere lit with ambient, +diffuse, +specular reflectance



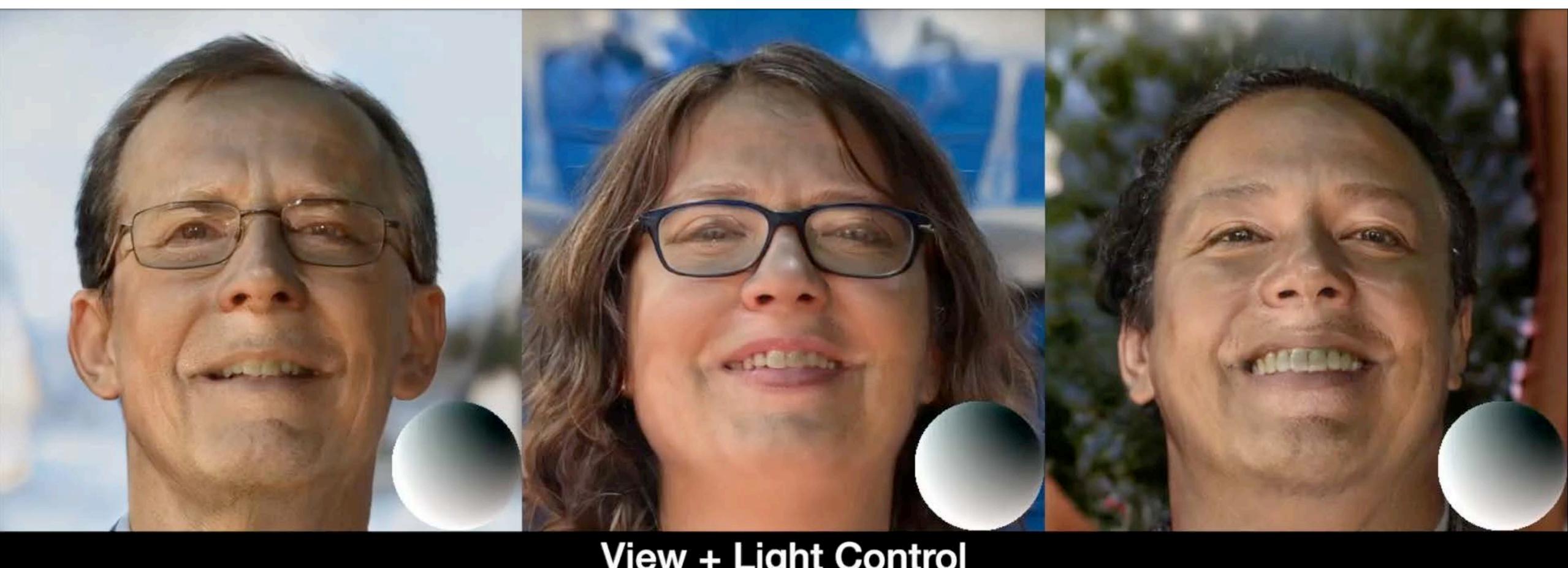
#### Ambient

#### +Diffuse



# Diffuse and Specular Reflection

• A motivating example that uses this model

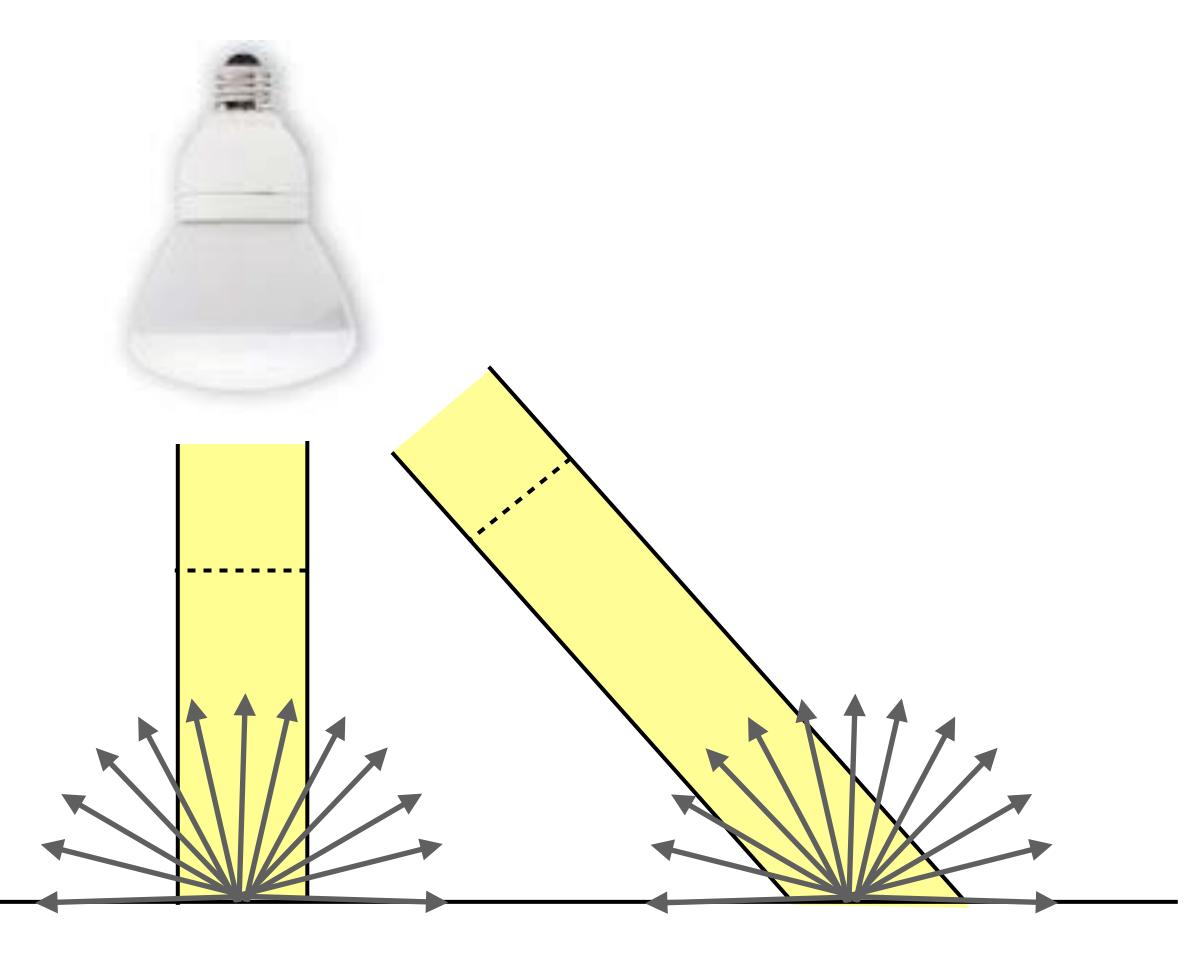


#### View + Light Control

[Video from https://machinelearning.apple.com/research/neural-3d-relightable reproduced for educational purposes]

## Diffuse Reflection

- Light is reflected equally in all directions (Lambertian surface)
- between the light and the surface...

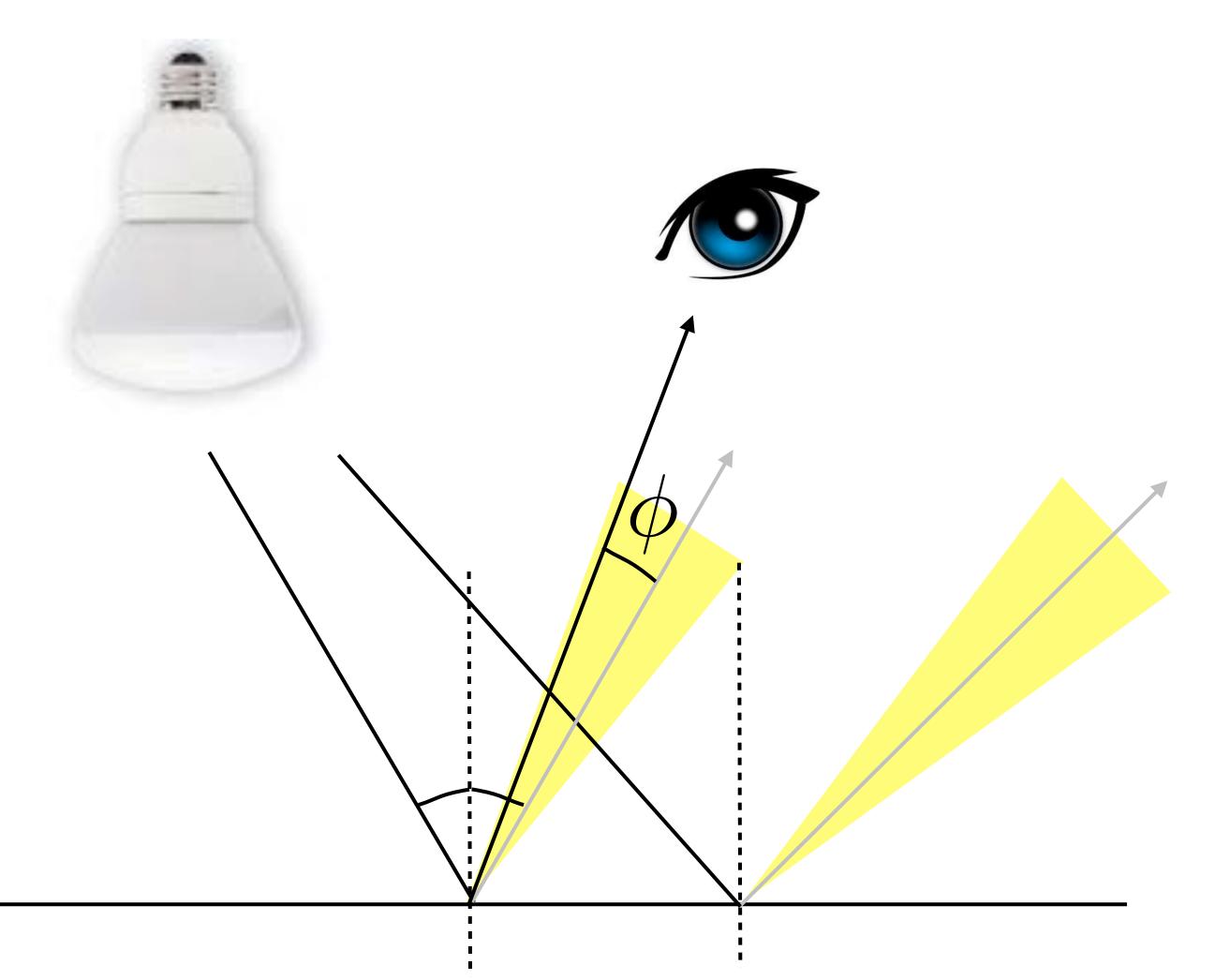




### But the amount of light reaching unit surface area depends on the angle

## Specular Reflection

- Light reflected strongly around the mirror reflection direction
- Intensity depends on viewer position

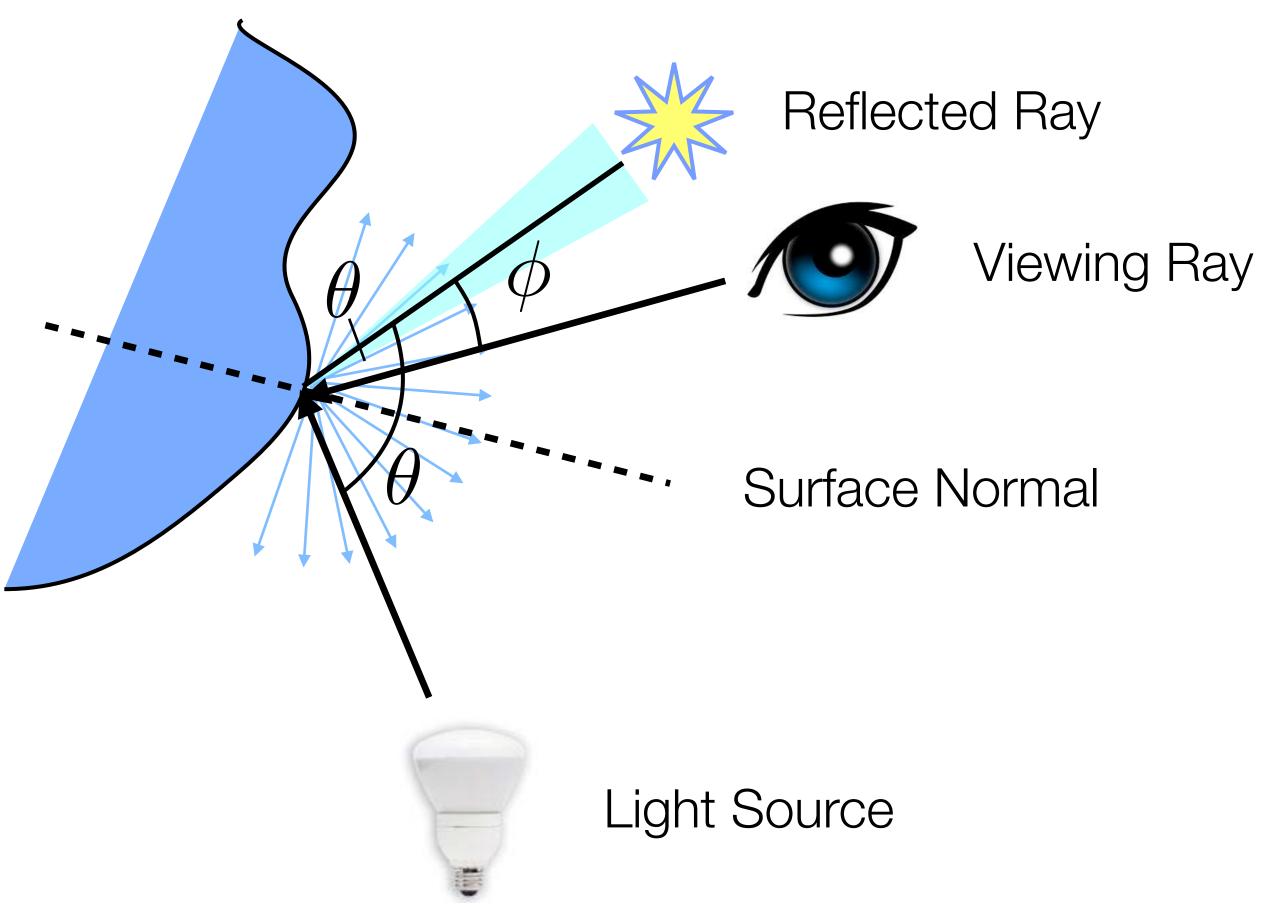




## Phong Illumination Model

Includes ambient, diffuse and specular reflection 

$$I = k_a i_a + k_d i_a$$



 $d\cos\theta + k_s i_s\cos^{\alpha}\phi$ 

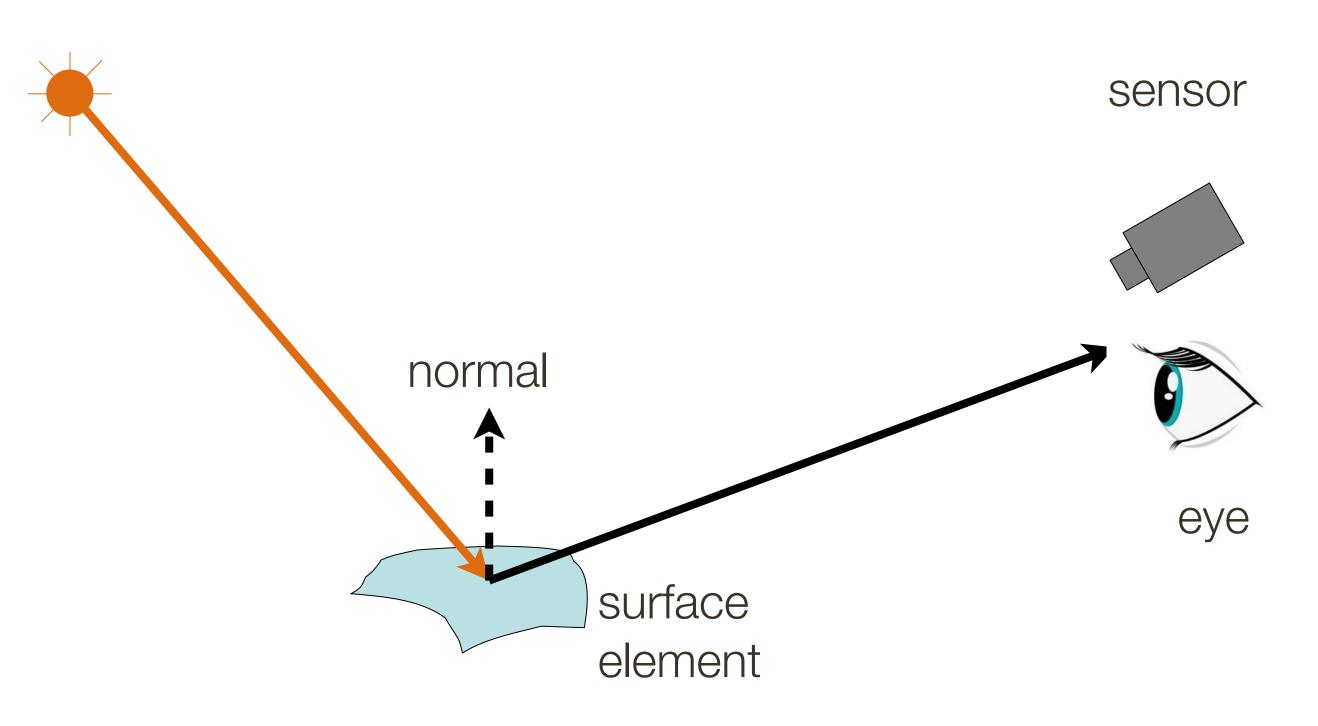
## **Overview:** Image Formation, Cameras and Lenses Coming back to here...

- Lighting condition
- Scene geometry
- Surface properties
- Camera optics and viewpoint

### Sensor (or eye) captures amount of light reflected from the object

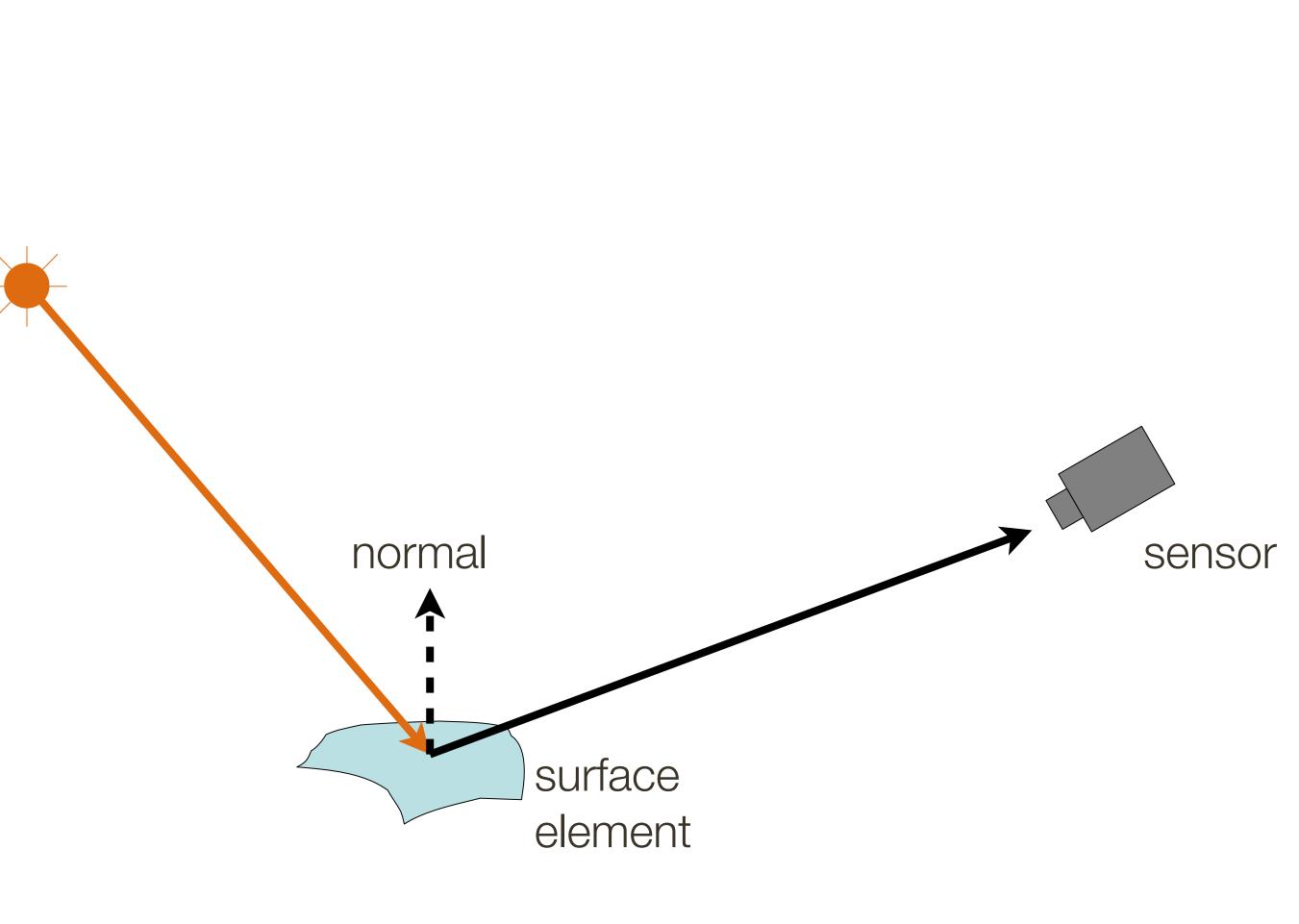
source

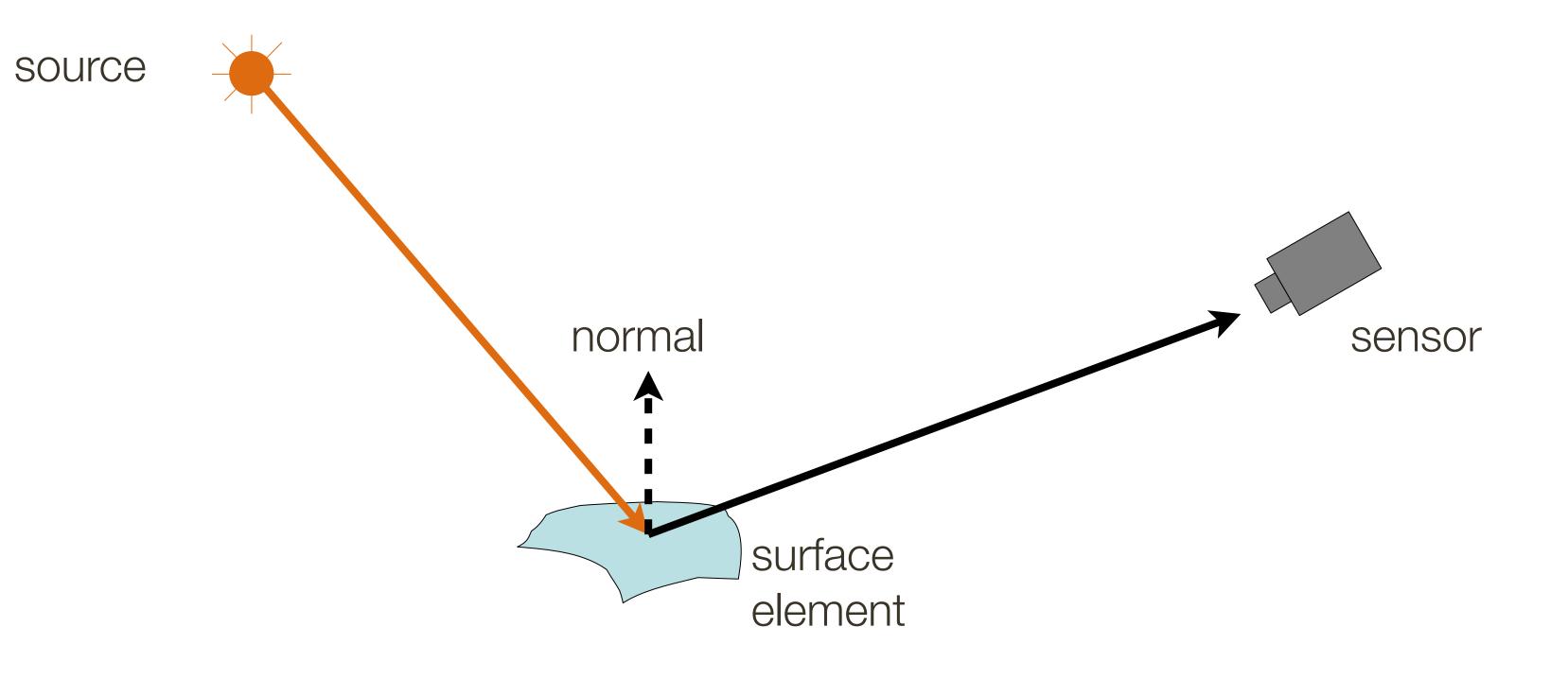
#### The **image formation process** that produces a particular image depends on

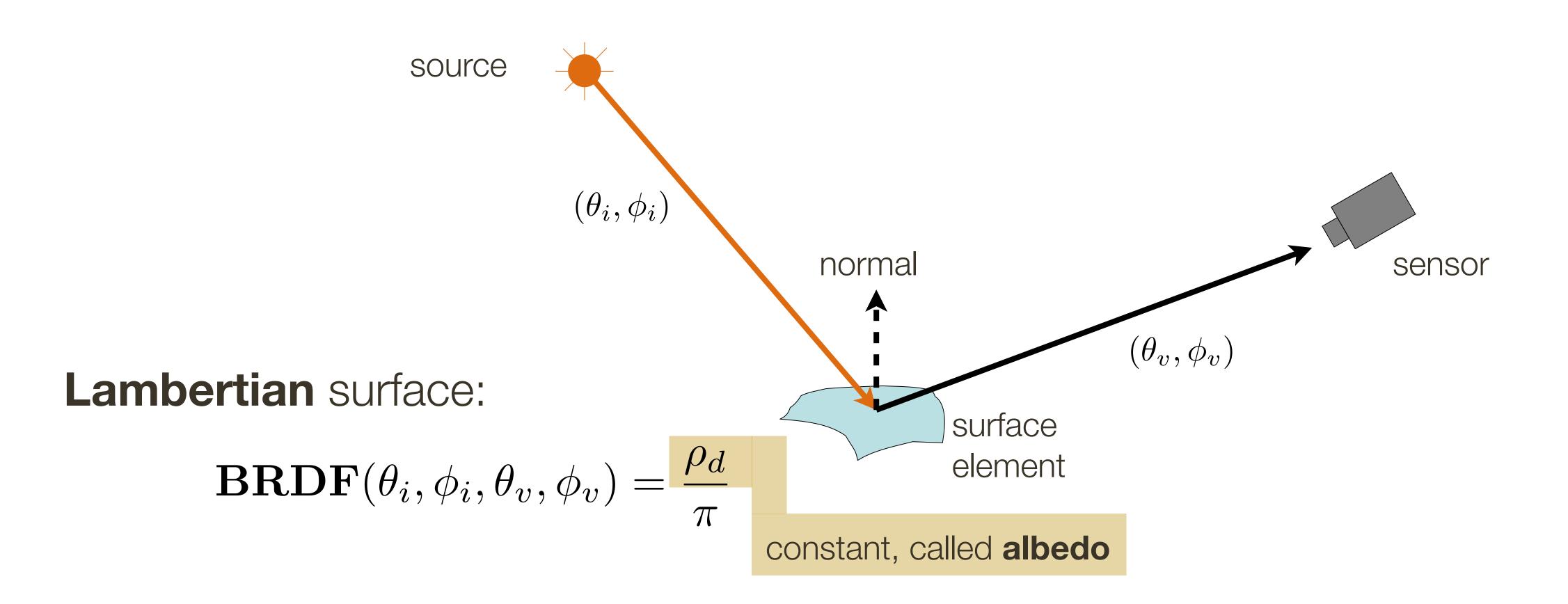




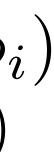




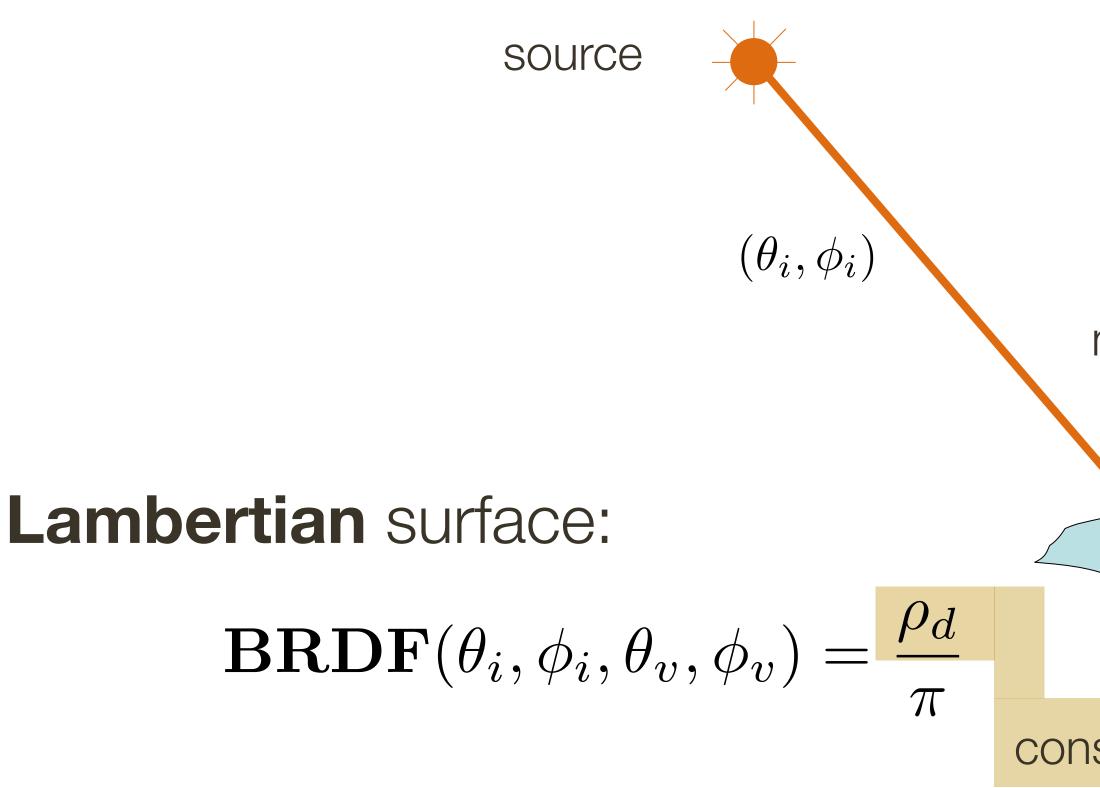




### Surface reflection depends on both the **viewing** $(\theta_v, \phi_v)$ and **illumination** $(\theta_i, \phi_i)$ direction, with Bidirectional Reflection Distribution Function: **BRDF** $(\theta_i, \phi_i, \theta_v, \phi_v)$

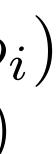




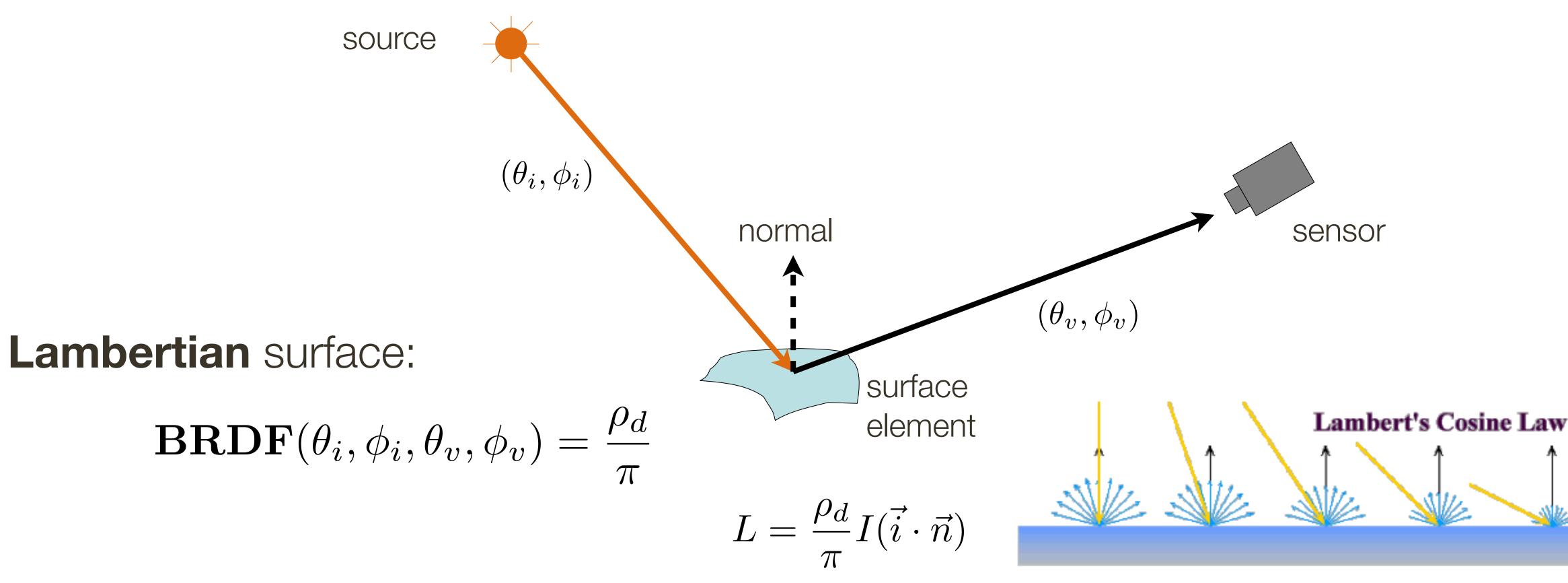


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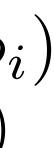
			Surface type	Typical value
			Fresh asphalt	0.03 - 0.04
			Open ocean	0.06
			Conifer forest (summer)	0.08 – 0.15
			Worn asphalt	0.12
			Deciduous trees	0.15 - 0.18
normal		Sand	0.15 – 0.45	
A			Tundra	0.18 - 0.25
		$( heta_v, \phi_v)$	Agricultural crops	0.18 - 0.25
		(0,0,0)	Bare soil	0.17
SUr	) surface element		Green grass	0.20 - 0.25
			Dessert sand	0.30 - 0.40
			Snow	0.40 - 0.90
			Ocean ice	0.50 - 0.70
stant, called	albedo		Fresh snow	0.80 - 0.90





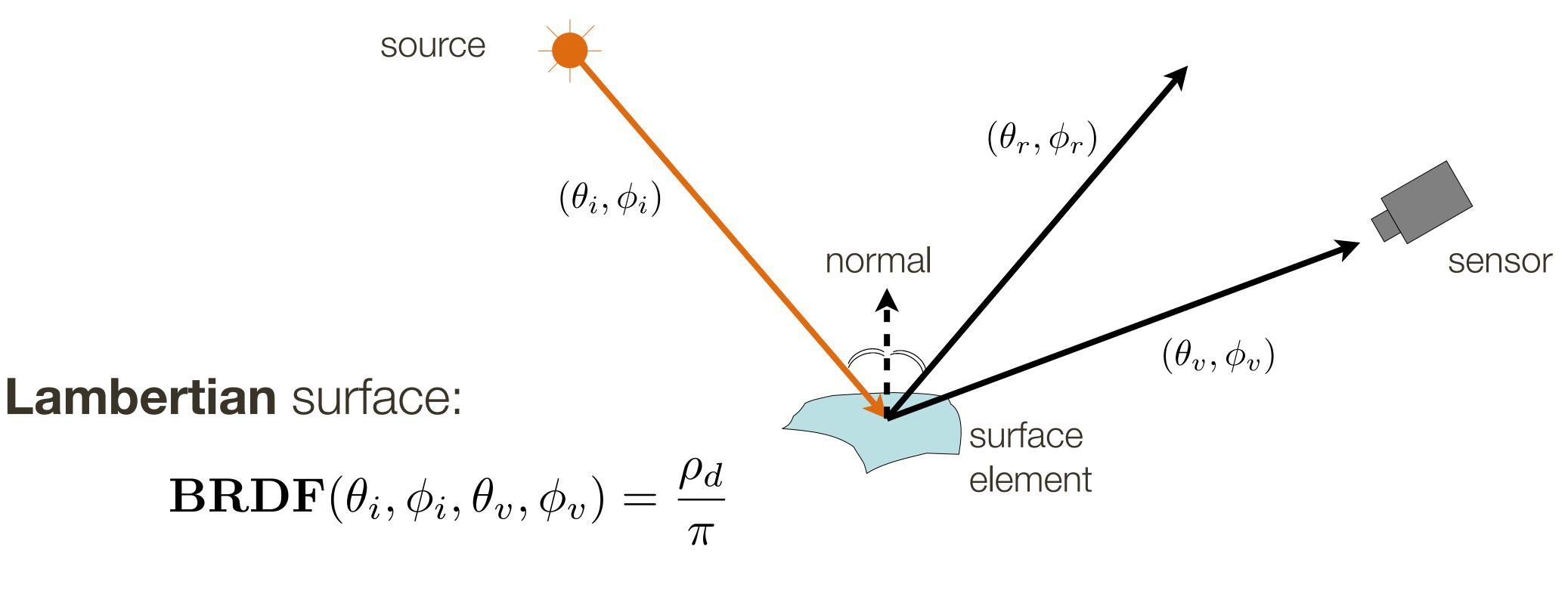


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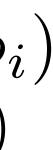




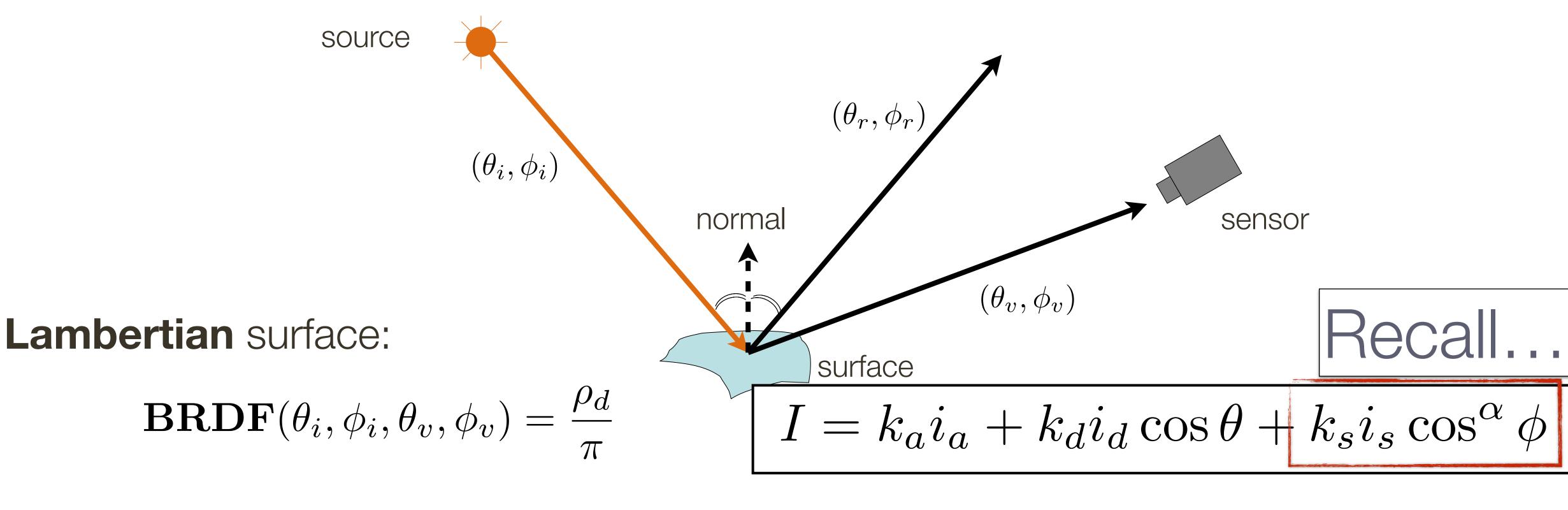


**Mirror** surface: all incident light reflected in one directions  $(\theta_v, \phi_v) = (\theta_r, \phi_r)$ 

#### Surface reflection depends on both the viewing $(\theta_v, \phi_v)$ and illumination $(\theta_i, \phi_i)$ direction, with Bidirectional Reflection Distribution Function: **BRDF** $(\theta_i, \phi_i, \theta_v, \phi_v)$

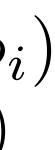






**Mirror** surface: all incident light reflected in one directions  $(\theta_v, \phi_v) = (\theta_r, \phi_r)$ 

### Surface reflection depends on both the viewing $(\theta_v, \phi_v)$ and illumination $(\theta_i, \phi_i)$ direction, with Bidirectional Reflection Distribution Function: **BRDF**( $\theta_i, \phi_i, \theta_v, \phi_v$ )





## Reflectance in Vision



## Reflectance in Graphics

[Video is from https://www.youtube.com/watch?v=AdTxrggo8e8 reproduced for educational purposes]



#### Old school **film** camera



#### **Digital** CCD/CMOS camera



### Let's say we have a sensor ...

### **Digital** CCD/CMOS camera



# digital sensor (CCD or CMOS)

Slide Credit: Ioannis (Yannis) Gkioulekas (CMU)



## ... and the **object** we would like to photograph



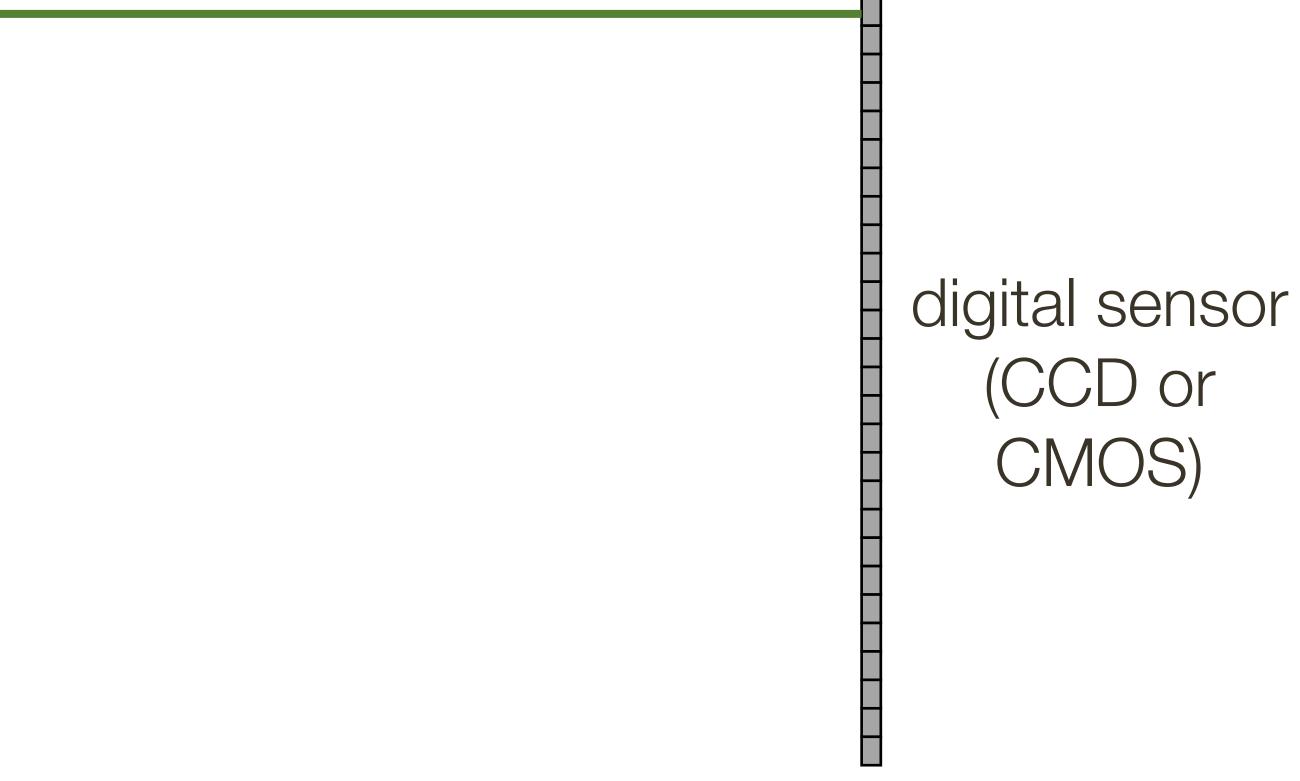
### real-world object

What would an image taken like this look like?

digital sensor (CCD or CMOS)

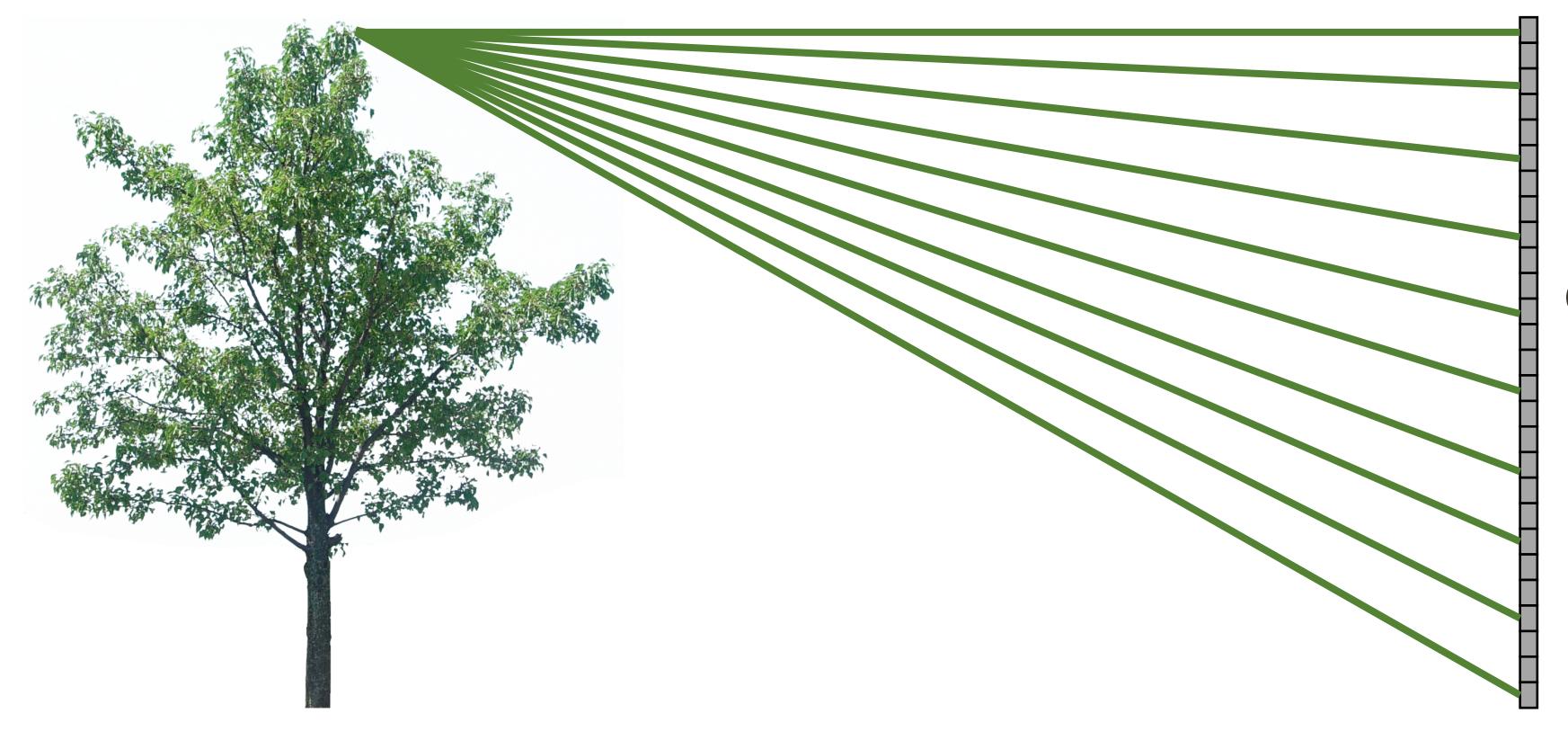


### real-world object





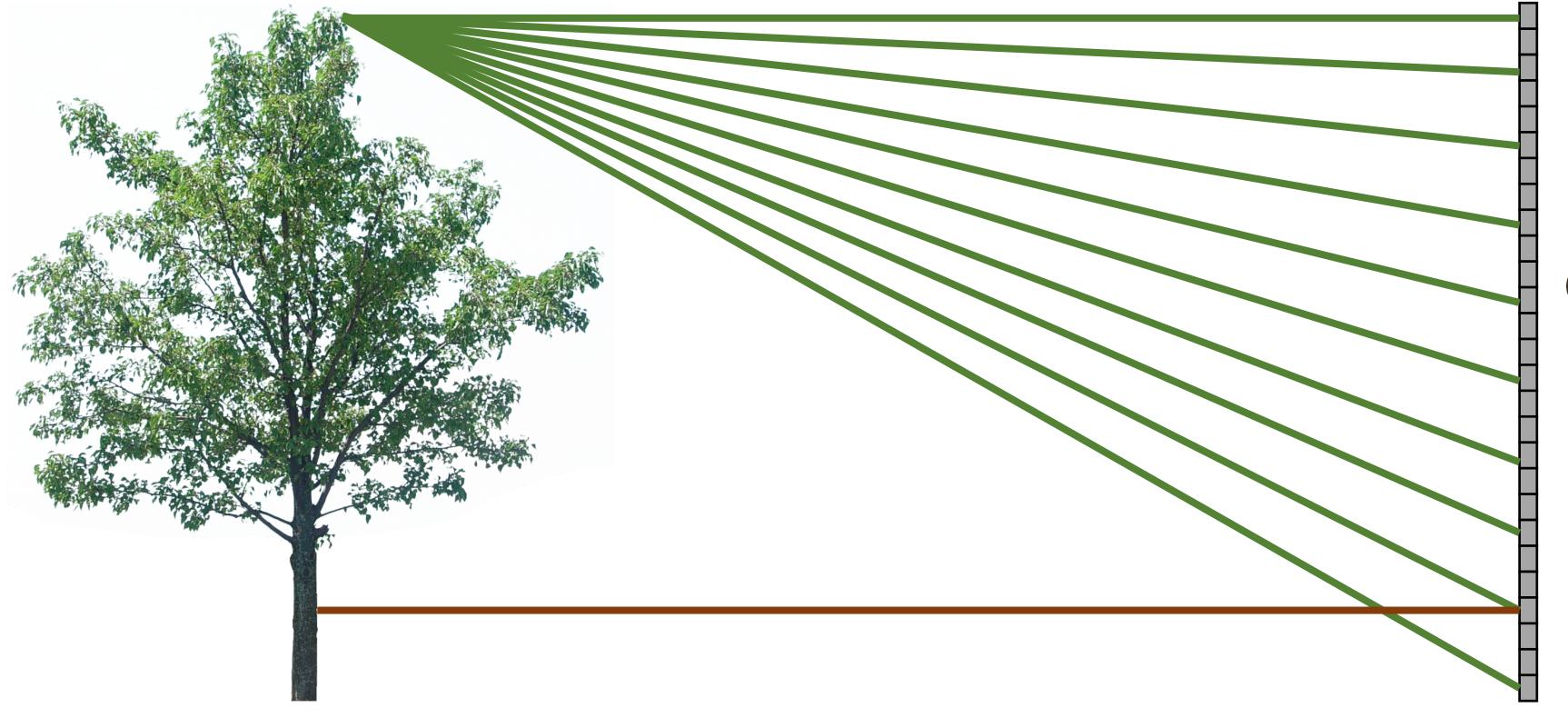
### real-world object





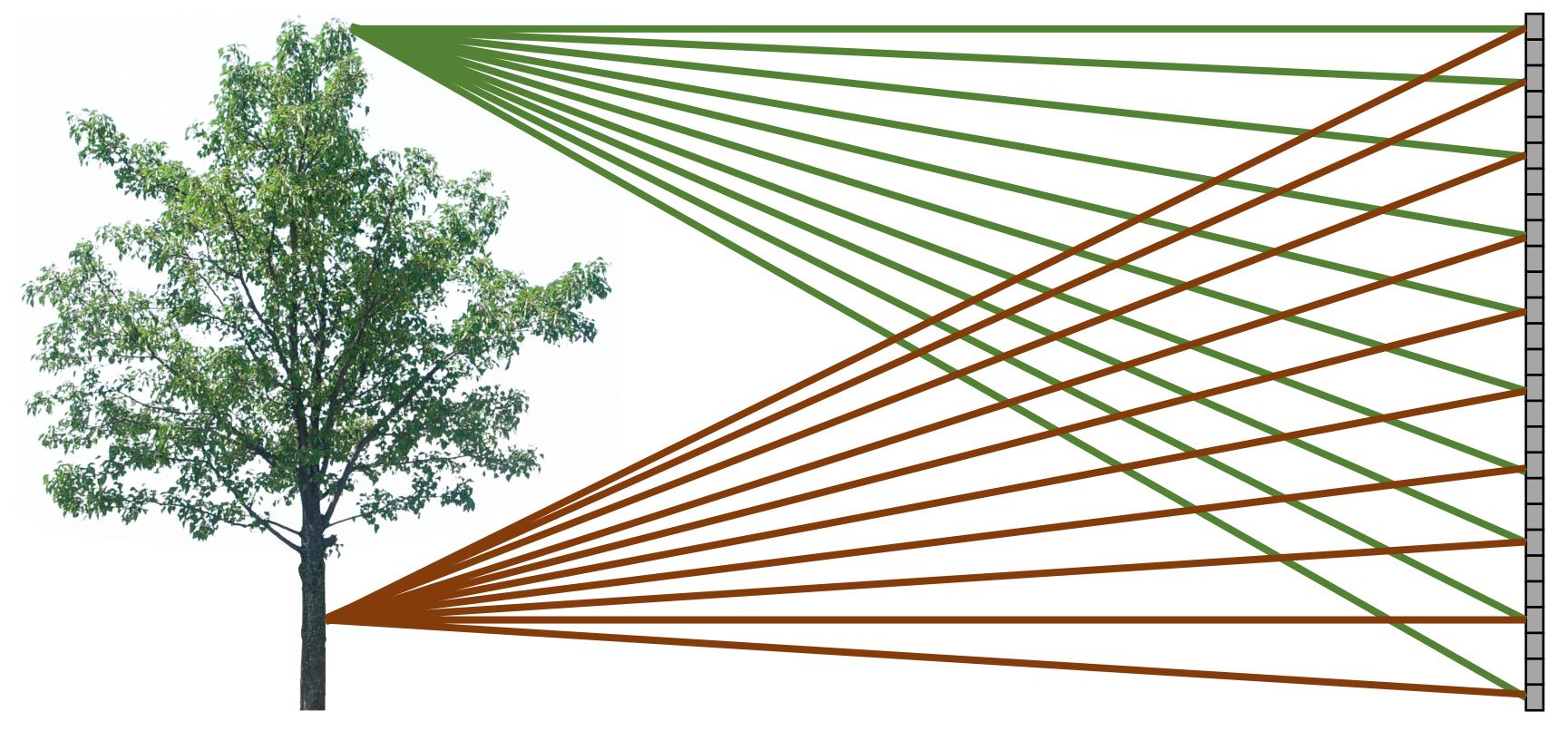


### real-world object



### digital sensor (CCD or CMOS)





#### All scene points contribute to all sensor pixels

### real-world object

### digital sensor (CCD or CMOS)



### **Bare-sensor** imaging

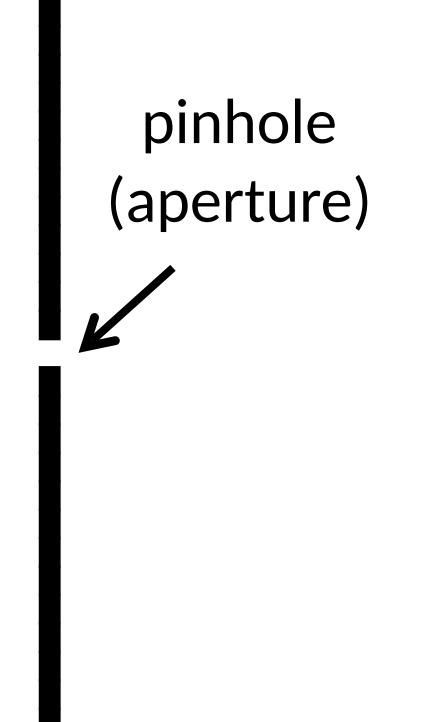


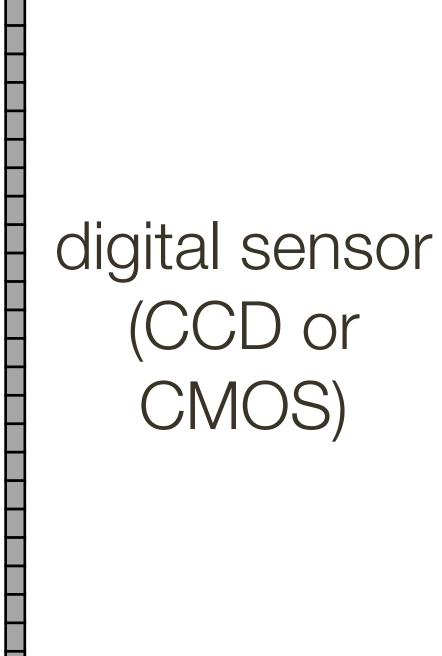
#### All scene points contribute to all sensor pixels



#### real-world object

barrier (diaphragm)

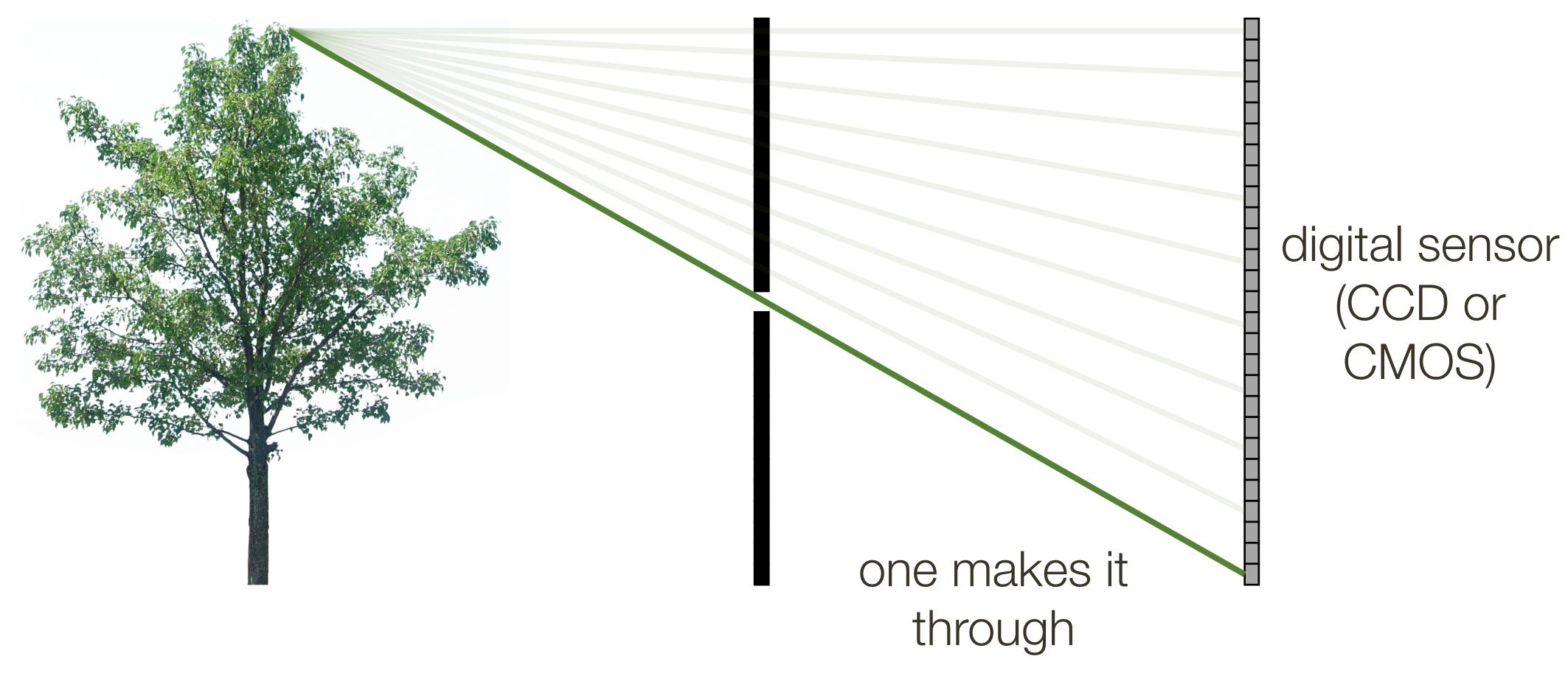




What would an image taken like this look like?



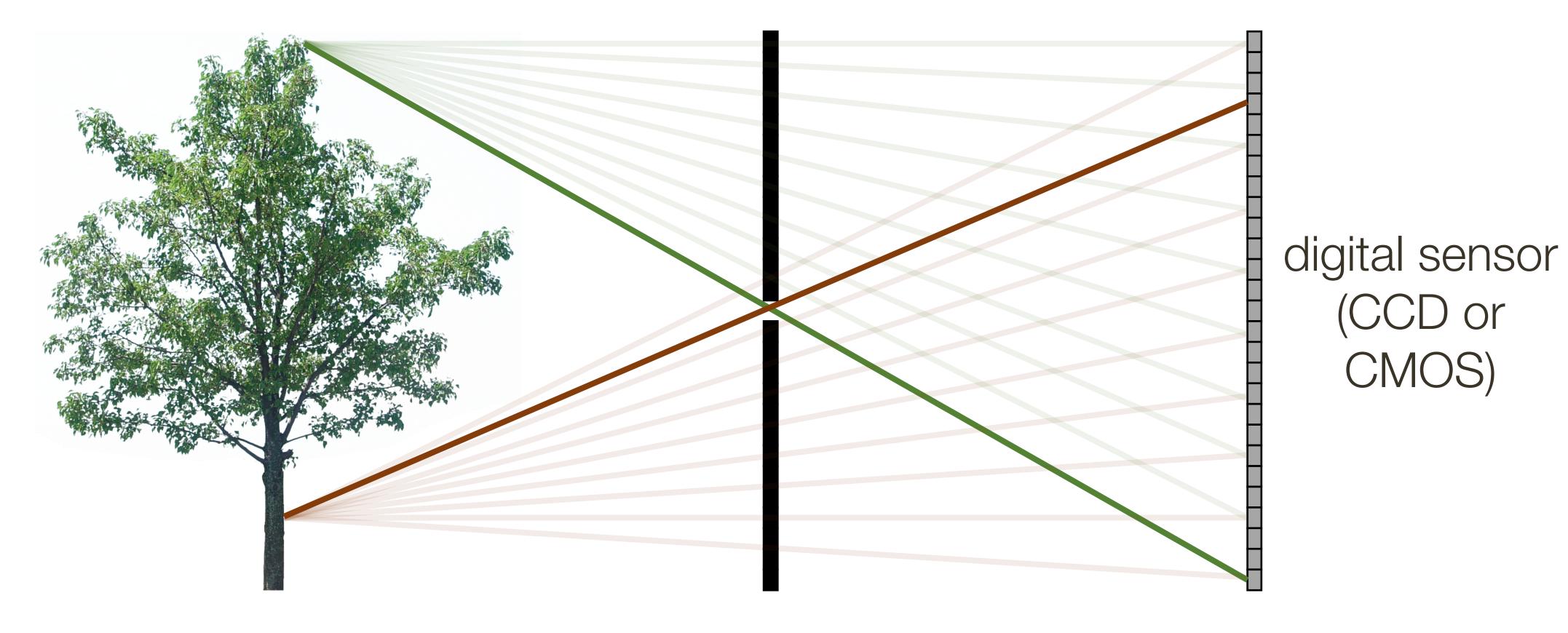
#### real-world object



#### most rays are blocked







#### Each scene point contributes to only one sensor pixel



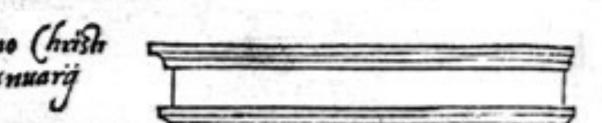
### **Camera Obscura** (latin for "dark chamber")

illum in tabula per radios Solis, quam in cœlo contingit: hoc eft, fi in cœlo superior pars deliquiù patiatur, in radiis apparebit inferior deficere, vt ratio exigit optica.

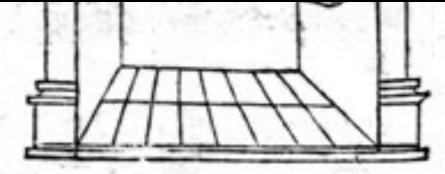
Solis delignium Anno (hrish 15 4.4. Die 24: Januari

Sic nos exacté Anno . 1544 . Louanii celipfim Solis observauimus, inuenimusq; deficere paulo plus g dex-

Reinerus Gemma-Frisius observed an eclipse of the sun at Louvain on January 24, 1544. He used this illustration in his book, "De Radio Astronomica et Geometrica," 1545. It is thought to be the first published illustration of a camera obscura.



principles behind the pinhole camera or camera obscura were first mentioned by Chinese philosopher Mozi (Mo-Ti) (470 to 390 BCE)



Credit: John H., Hammond, "Th Camera Obscure, A Chronicle"



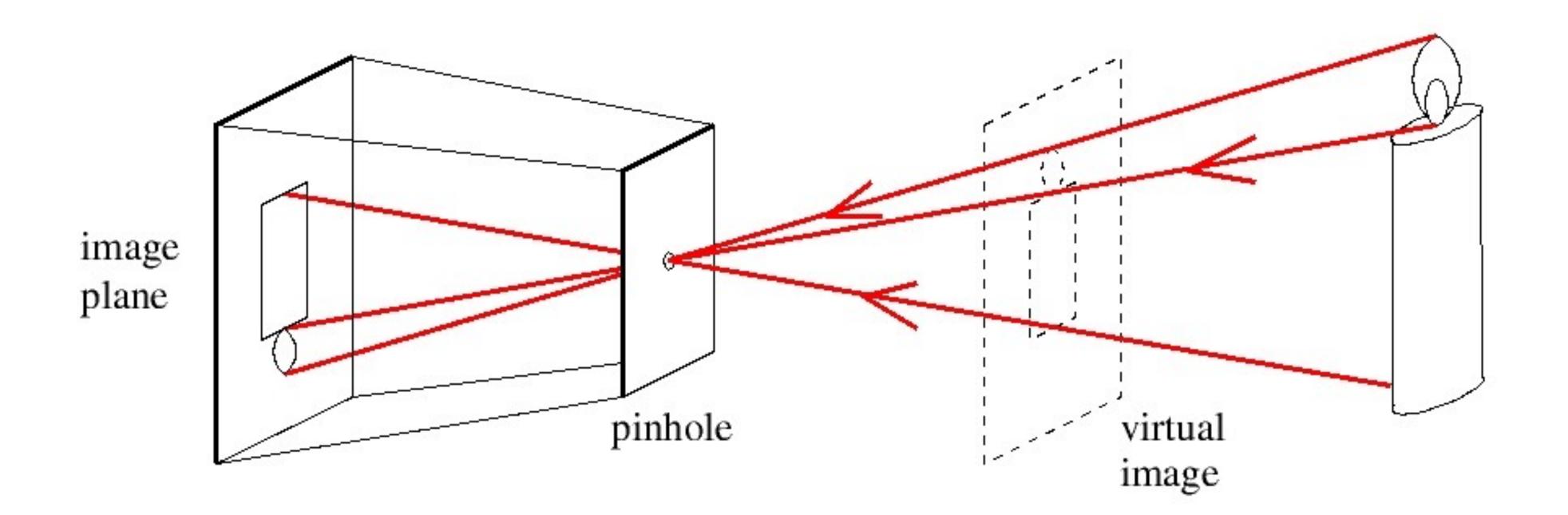
### First Photograph on Record

#### La table servie



#### Credit: Nicéphore Niepce, 1822

A pinhole camera is a box with a small hole (aperture) in it



Forsyth & Ponce (2nd ed.) Figure 1.2

### Image Formation



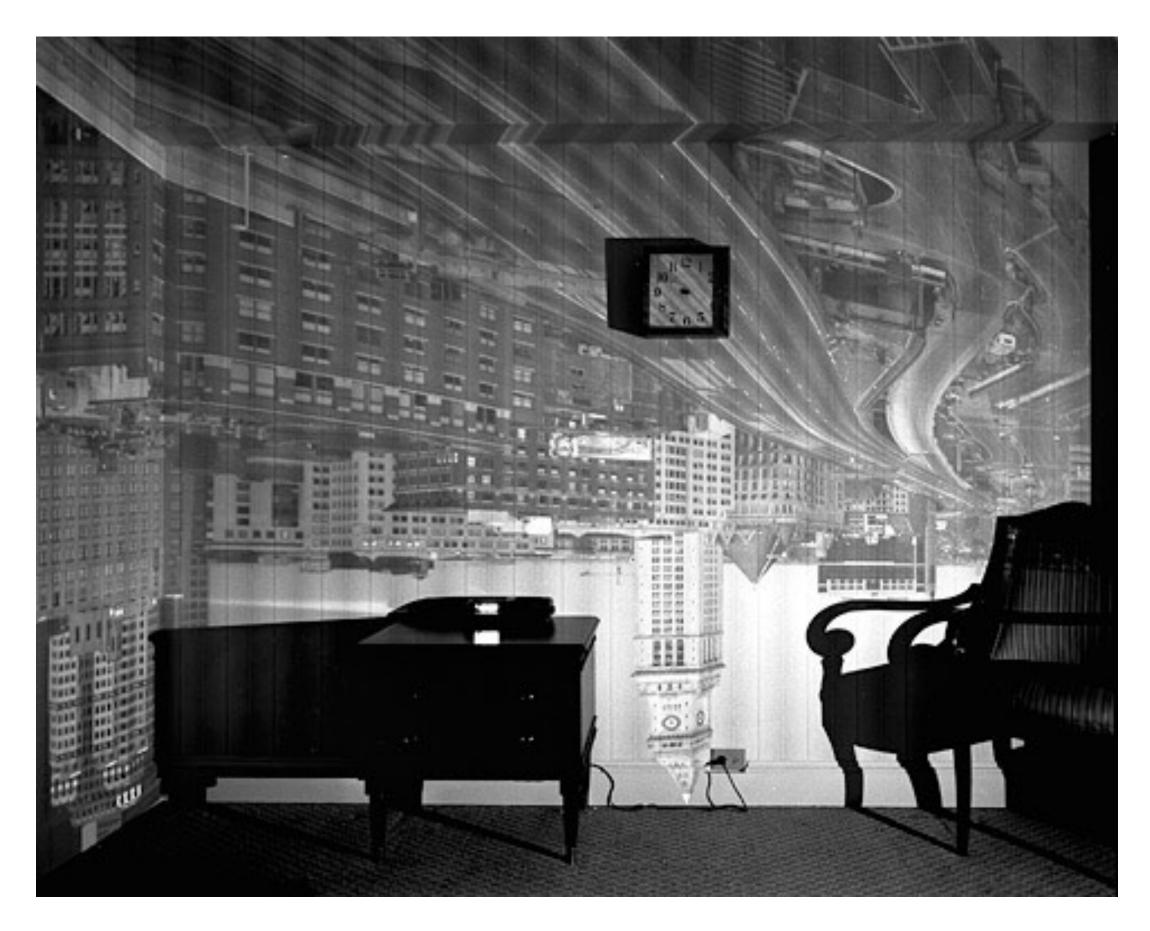
#### Forsyth & Ponce (2nd ed.) Figure 1.1

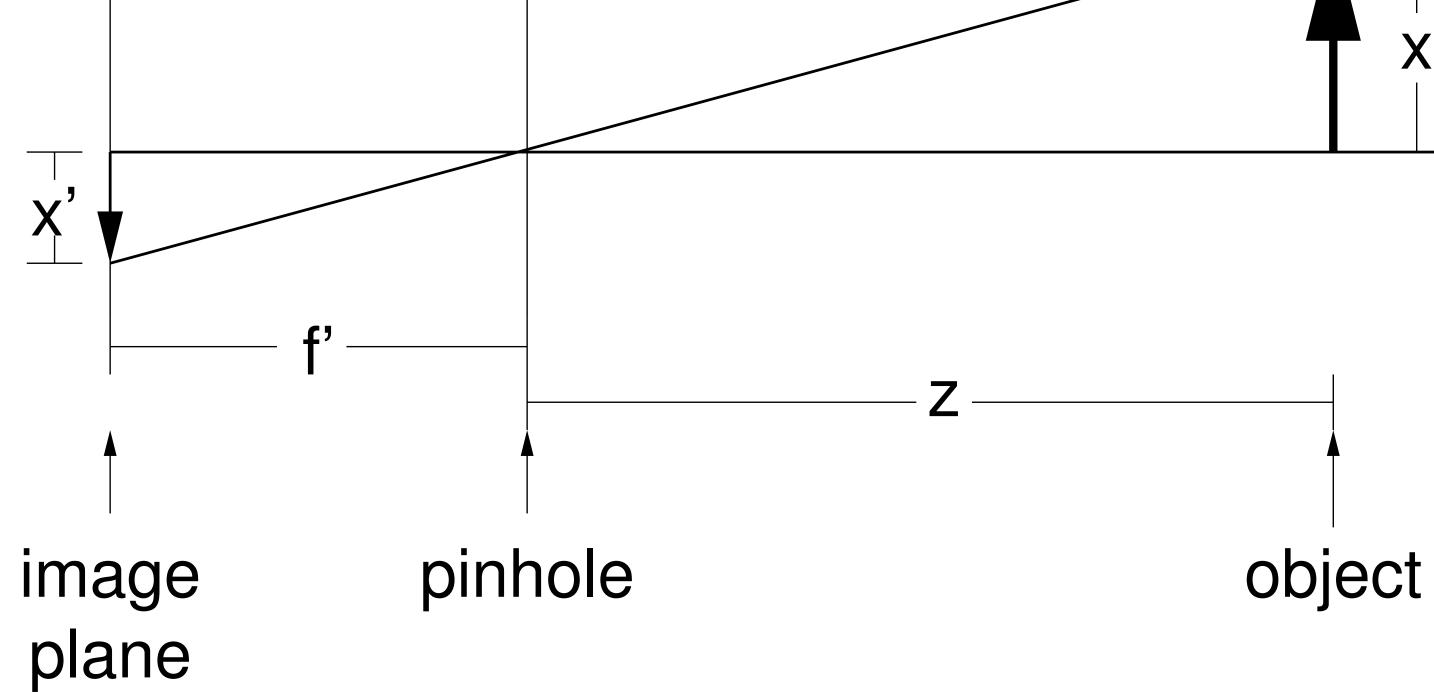
Credit: US Navy, Basic Optics and Optical Instruments. Dover, 1969



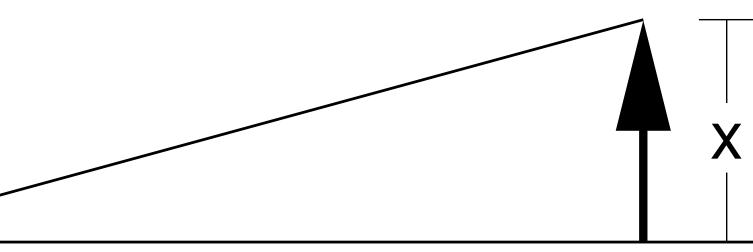
### Accidental Pinhole Camera



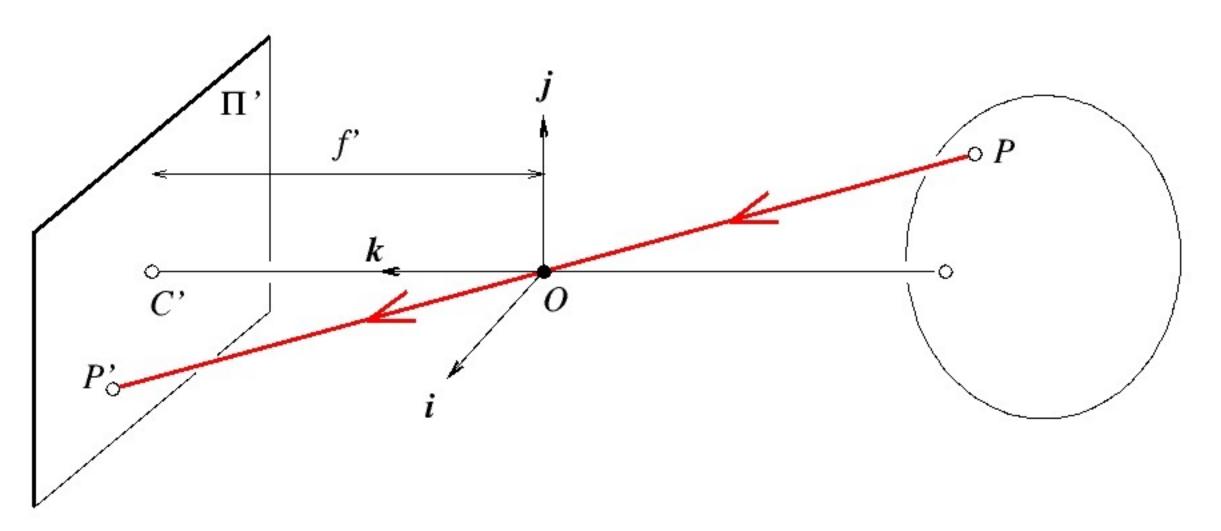








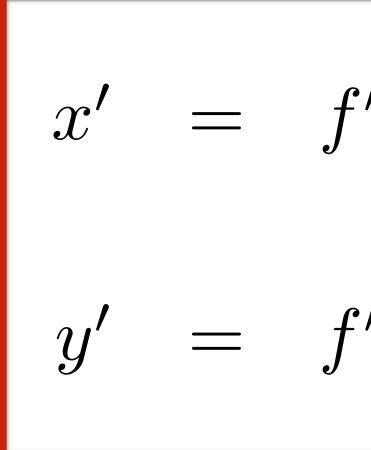
### **Perspective** Projection



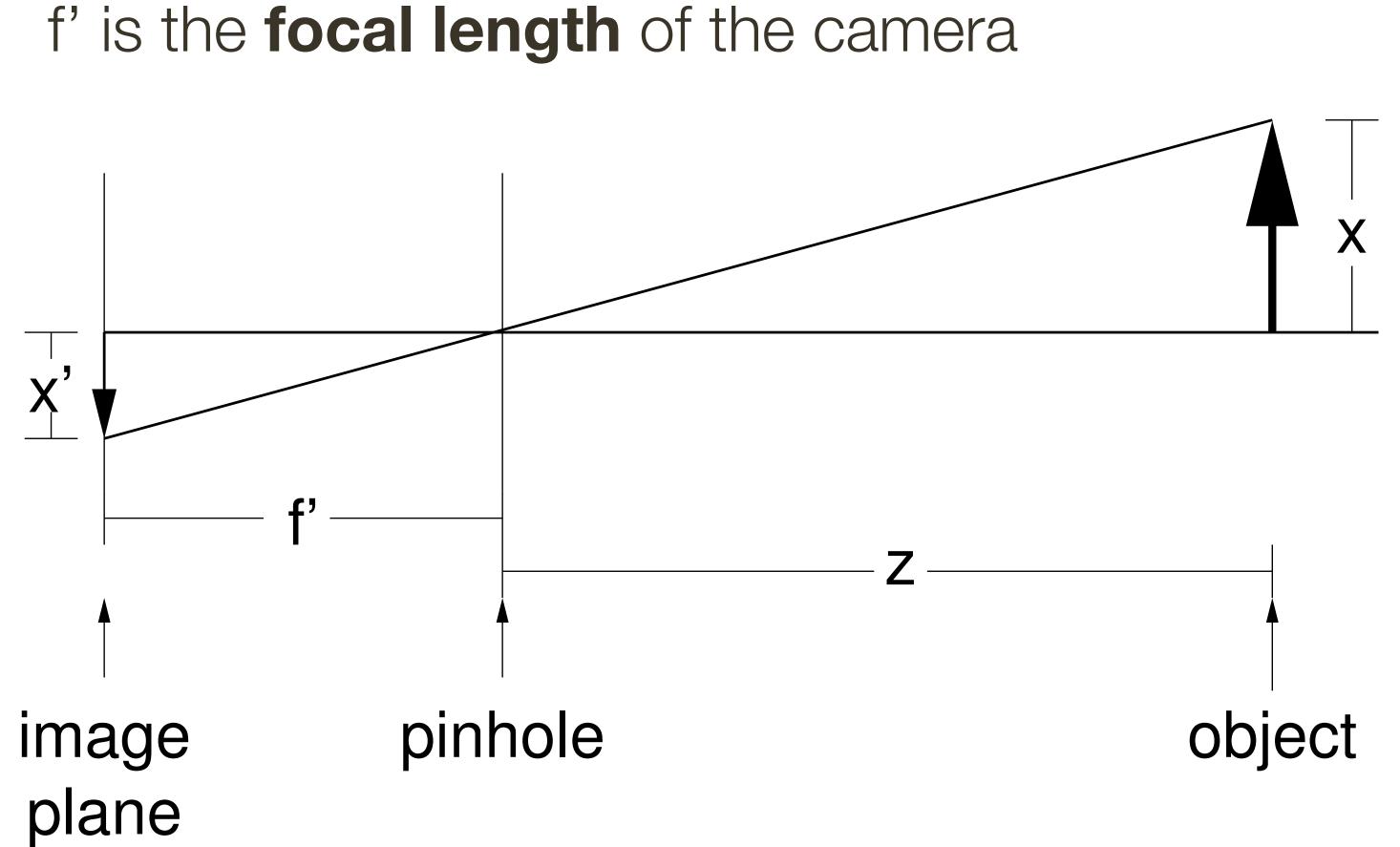
#### 3D object point

$$P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

## Forsyth & Ponce (1st ed.) Figure 1.4 projects to 2D image point $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$ where



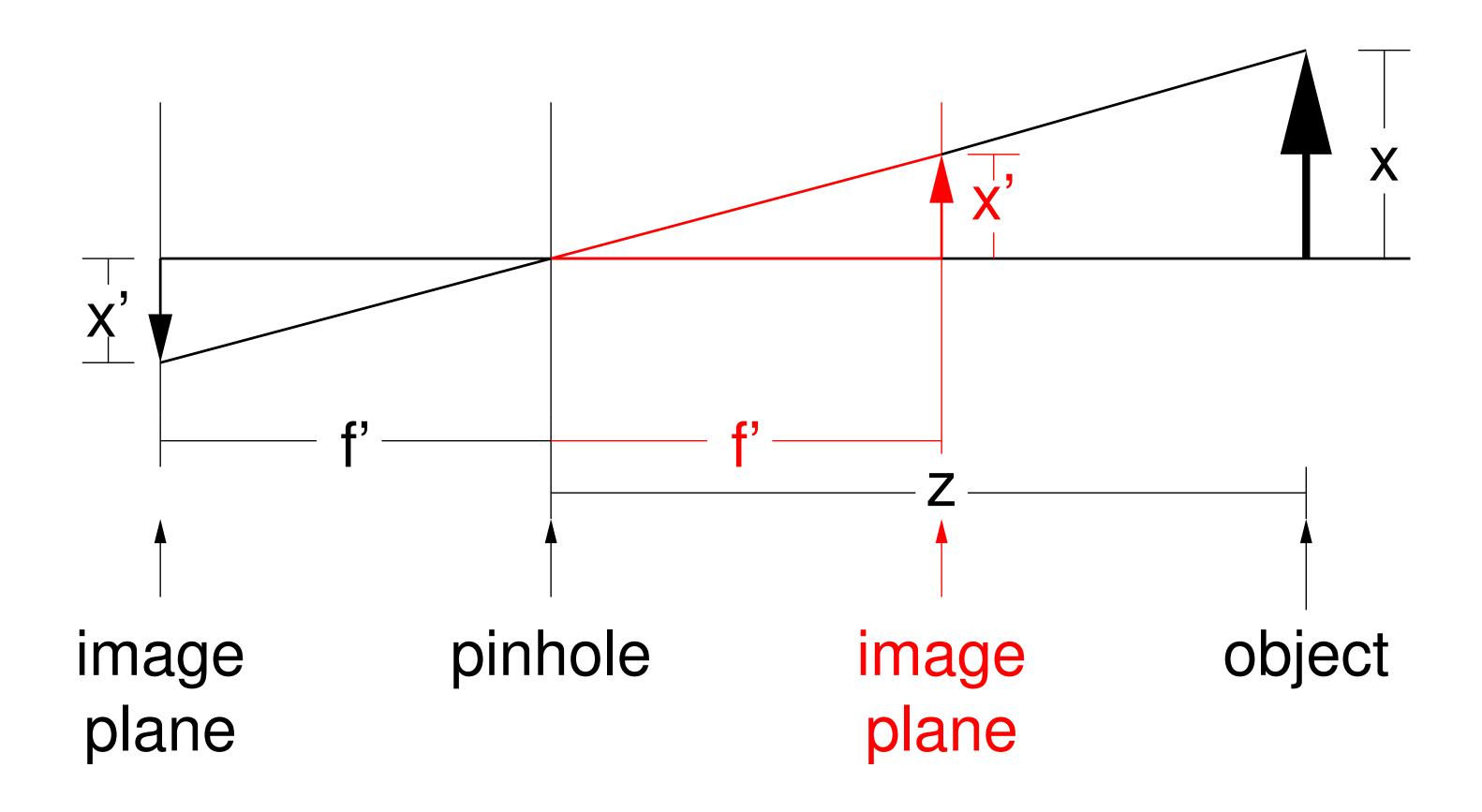




Note: In a pinhole camera we can adjust the focal length, all this will do is change the size of the resulting image



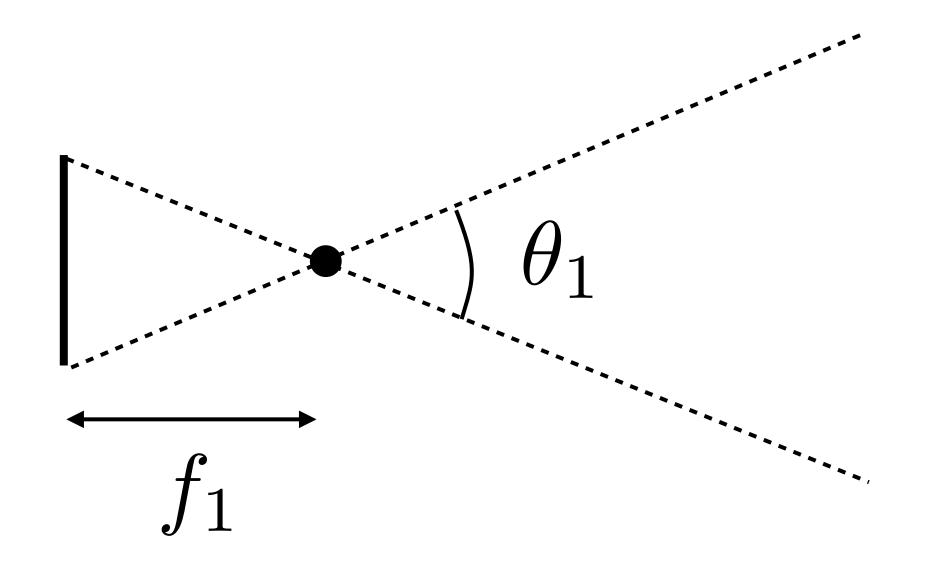
It is convenient to think of the **image plane** being in front of the pinhole



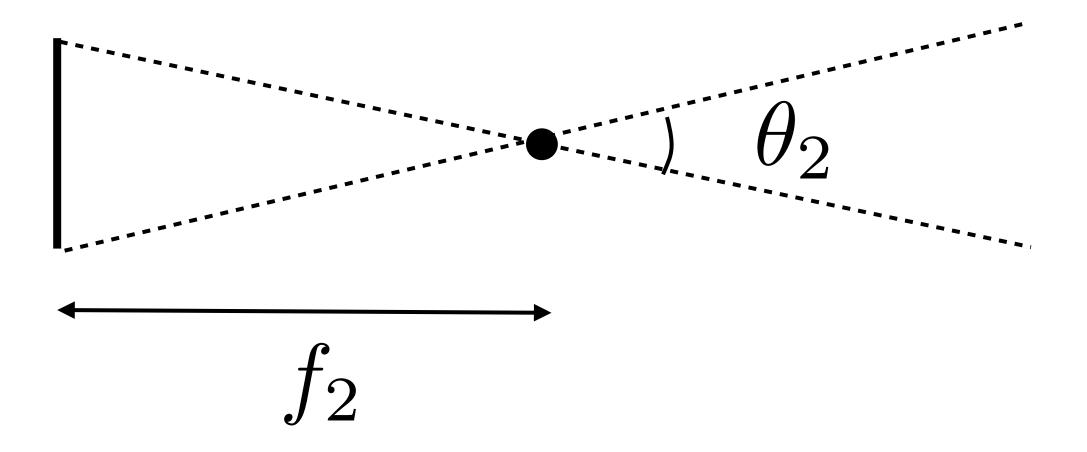
#### What happens if object moves towards the camera? Away from the camera?

### Focal Length

• For a fixed sensor size, focal length determines the field of view (fov)

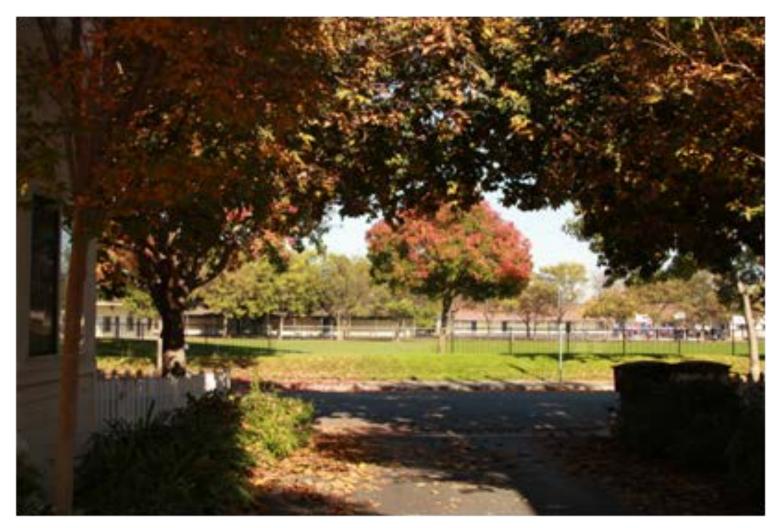




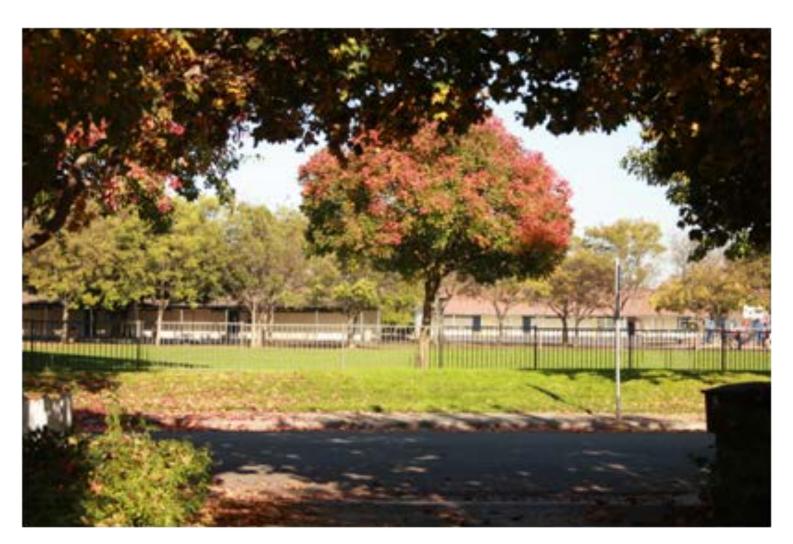


Sensor size Q: What is the field of view of a full-frame (35mm) camera

### Focal Length



#### 28 mm



#### 50 mm

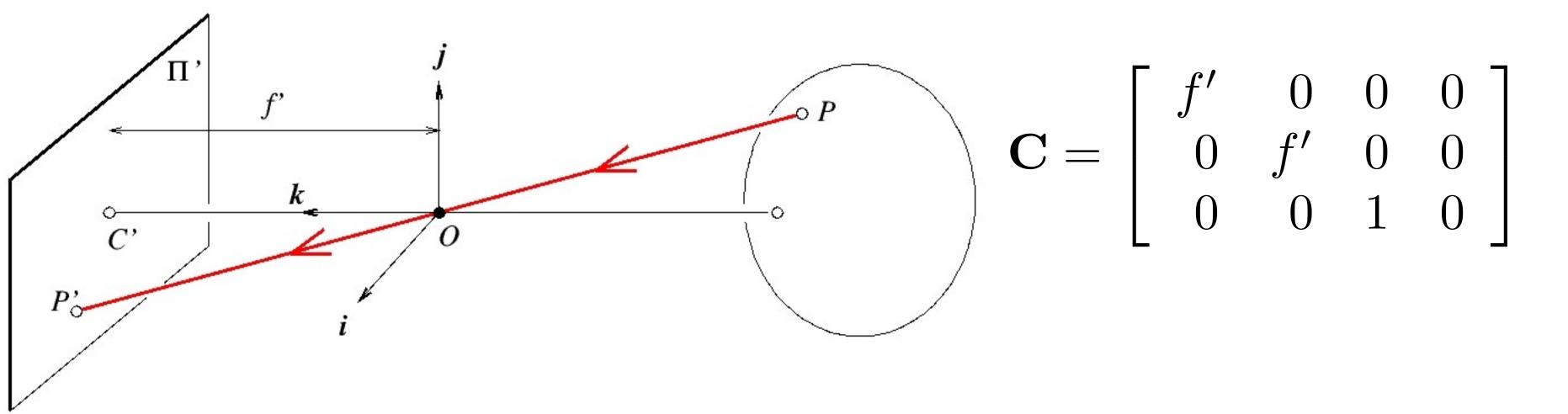


#### 35 mm

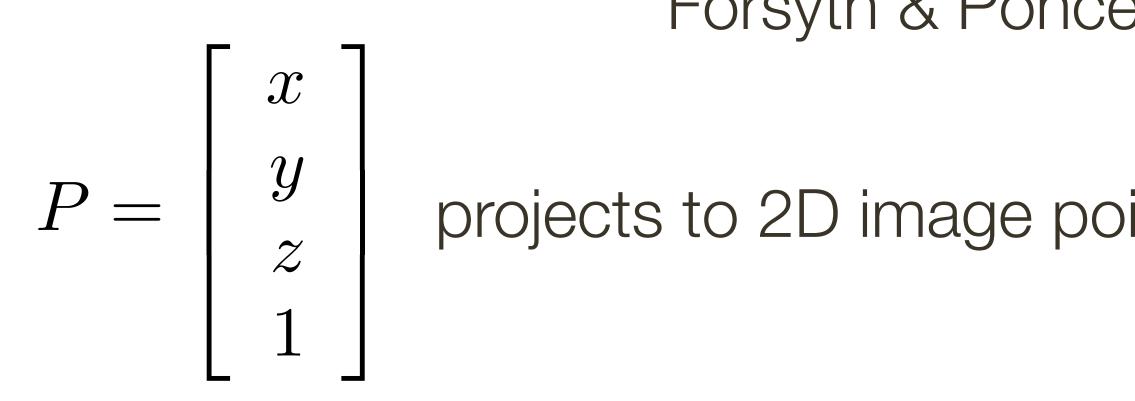


#### 70 mm

### **Perspective** Projection: Matrix Form



#### 3D object point



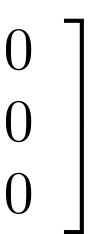


#### **Camera** Matrix

#### Forsyth & Ponce (1st ed.) Figure 1.4

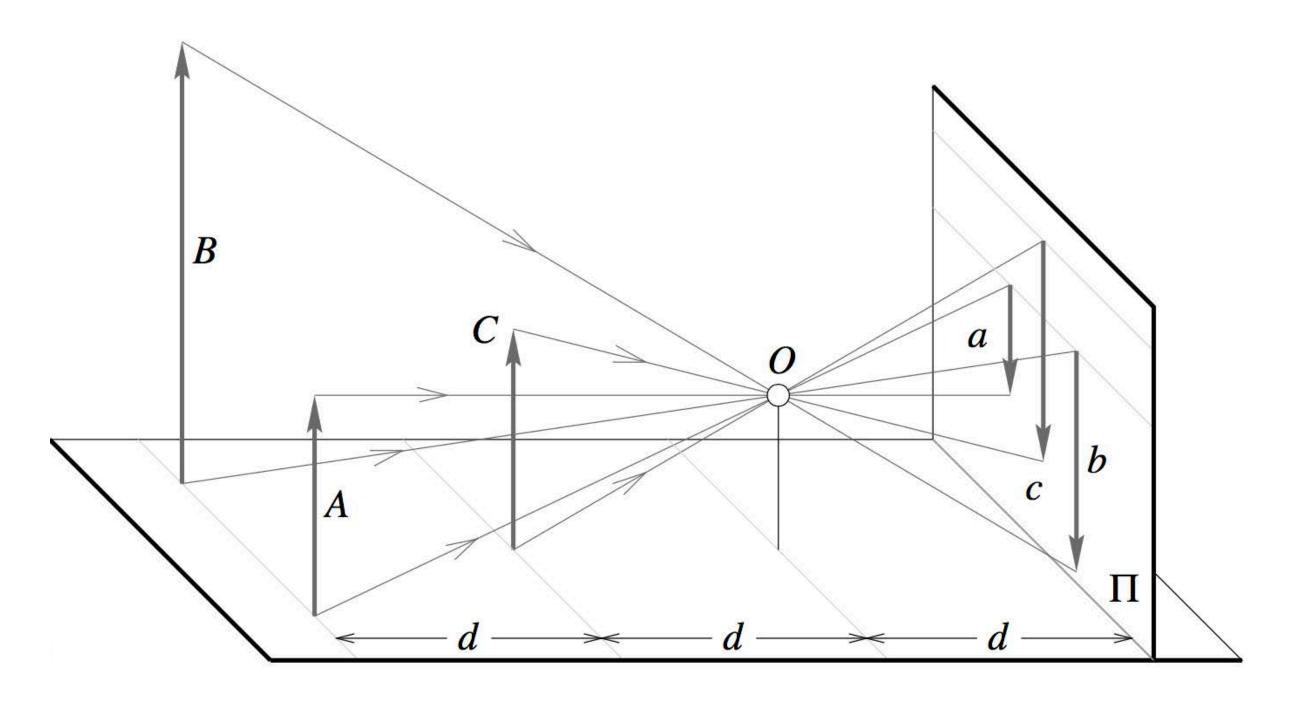
pint 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $\mathbf{S}P' = \mathbf{C}P$ 

(s is a scale factor)



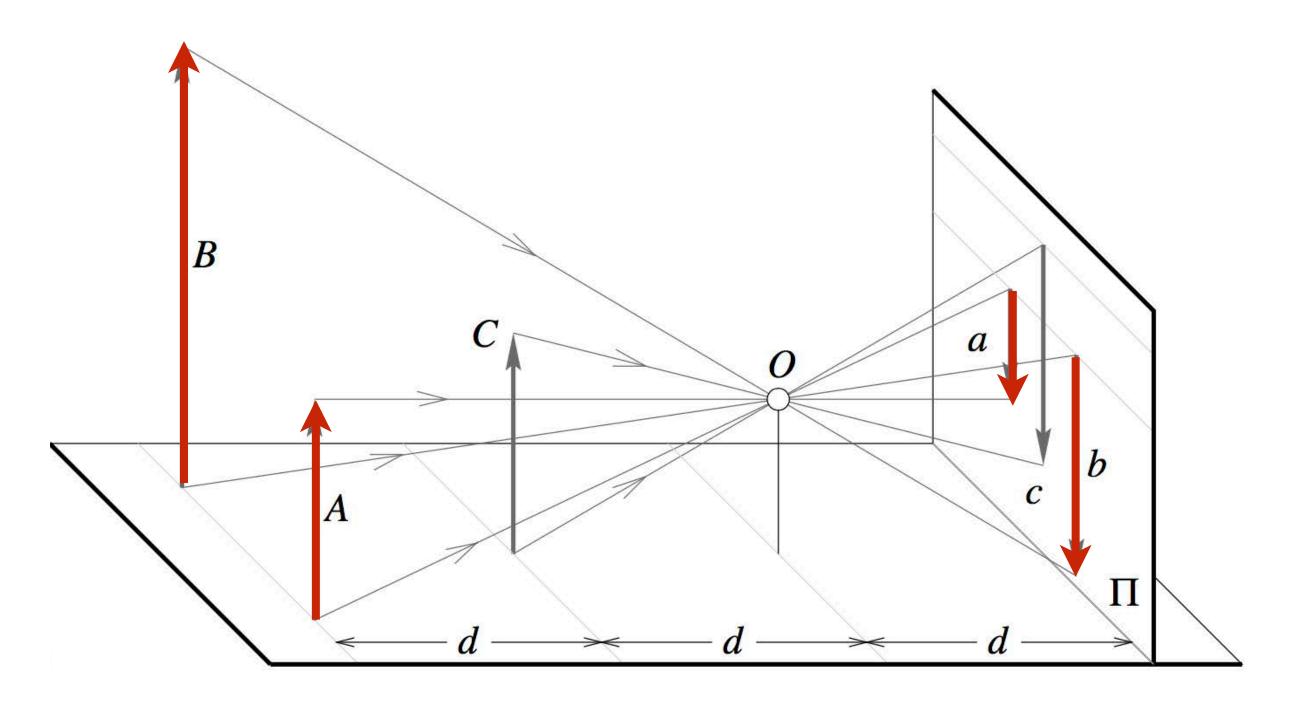


#### Far objects appear smaller than close ones



Forsyth & Ponce (2nd ed.) Figure 1.3a

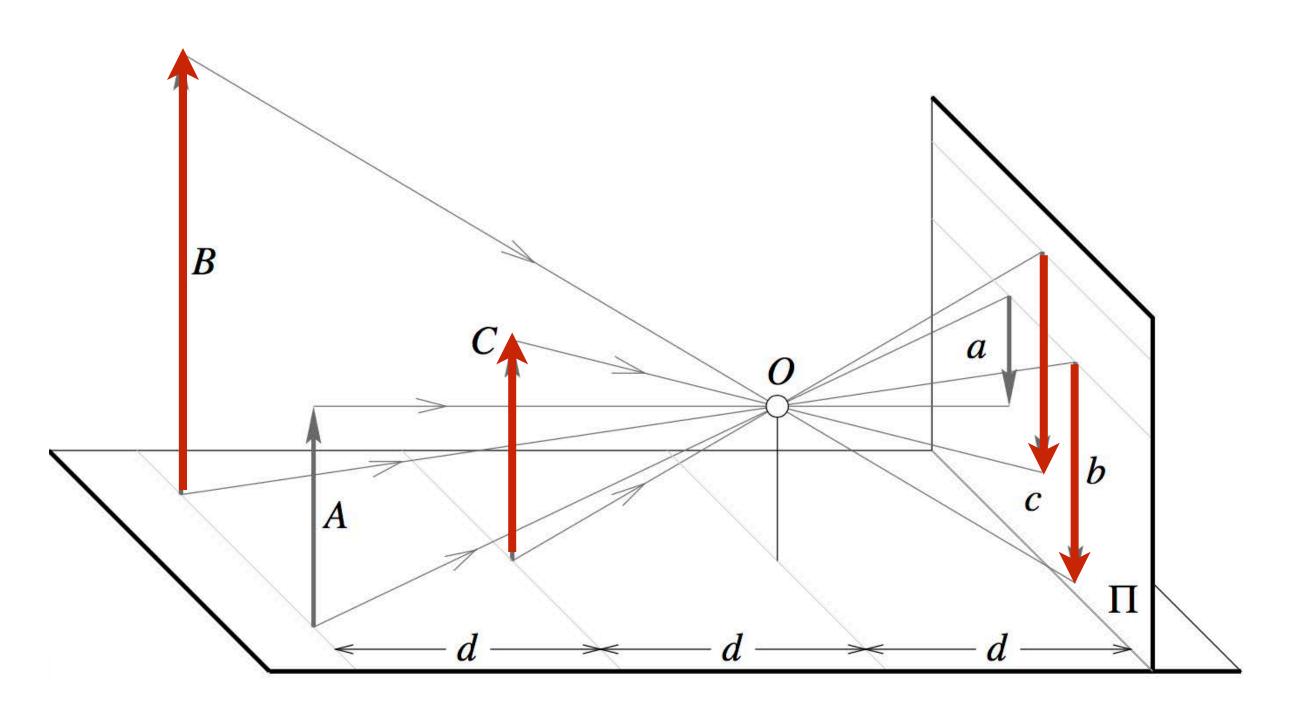
#### Far objects appear smaller than close ones



Size is **inversely** proportions to distance

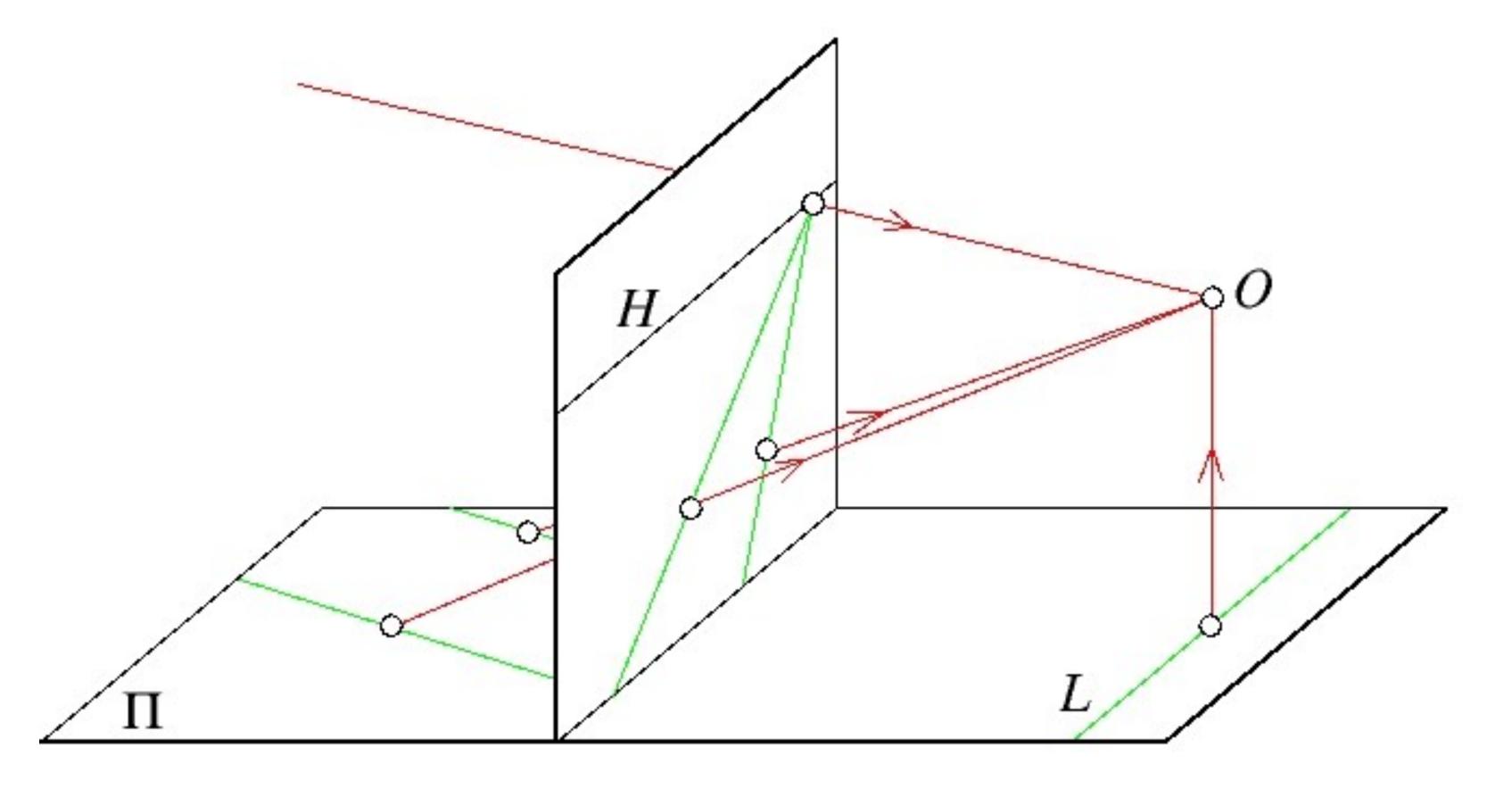
Forsyth & Ponce (2nd ed.) Figure 1.3a

Far objects appear smaller than close ones



Forsyth & Ponce (2nd ed.) Figure 1.3a

Parallel lines meet at a point (vanishing point)

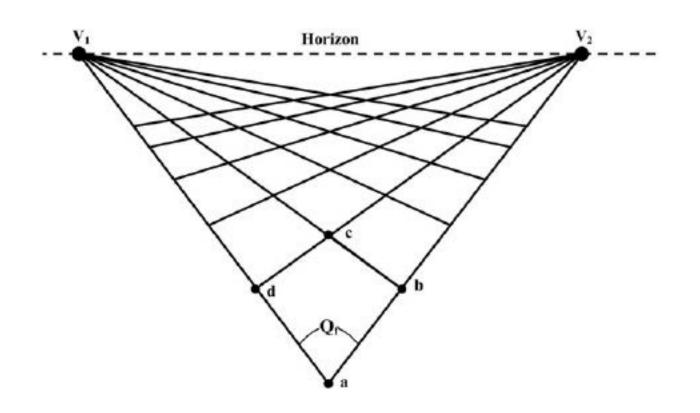


#### Forsyth & Ponce (1st ed.) Figure 1.3b

- Each set of parallel lines meets at a different point
- the point is called the **vanishing point**

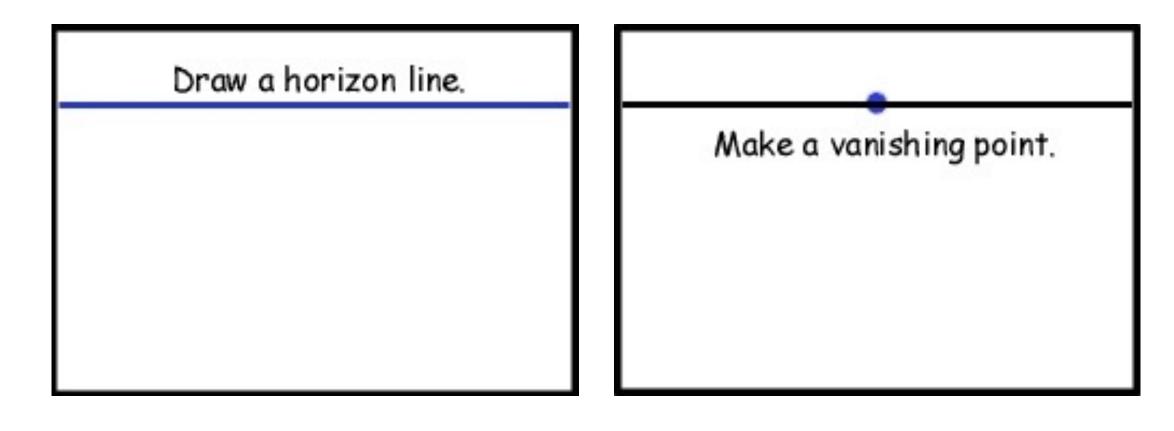
Each set of parallel lines meets at a different point - the point is called the **vanishing point** 

Sets of parallel lines on the same plane lead to **collinear** vanishing points - the line is called a **horizon** for that plane

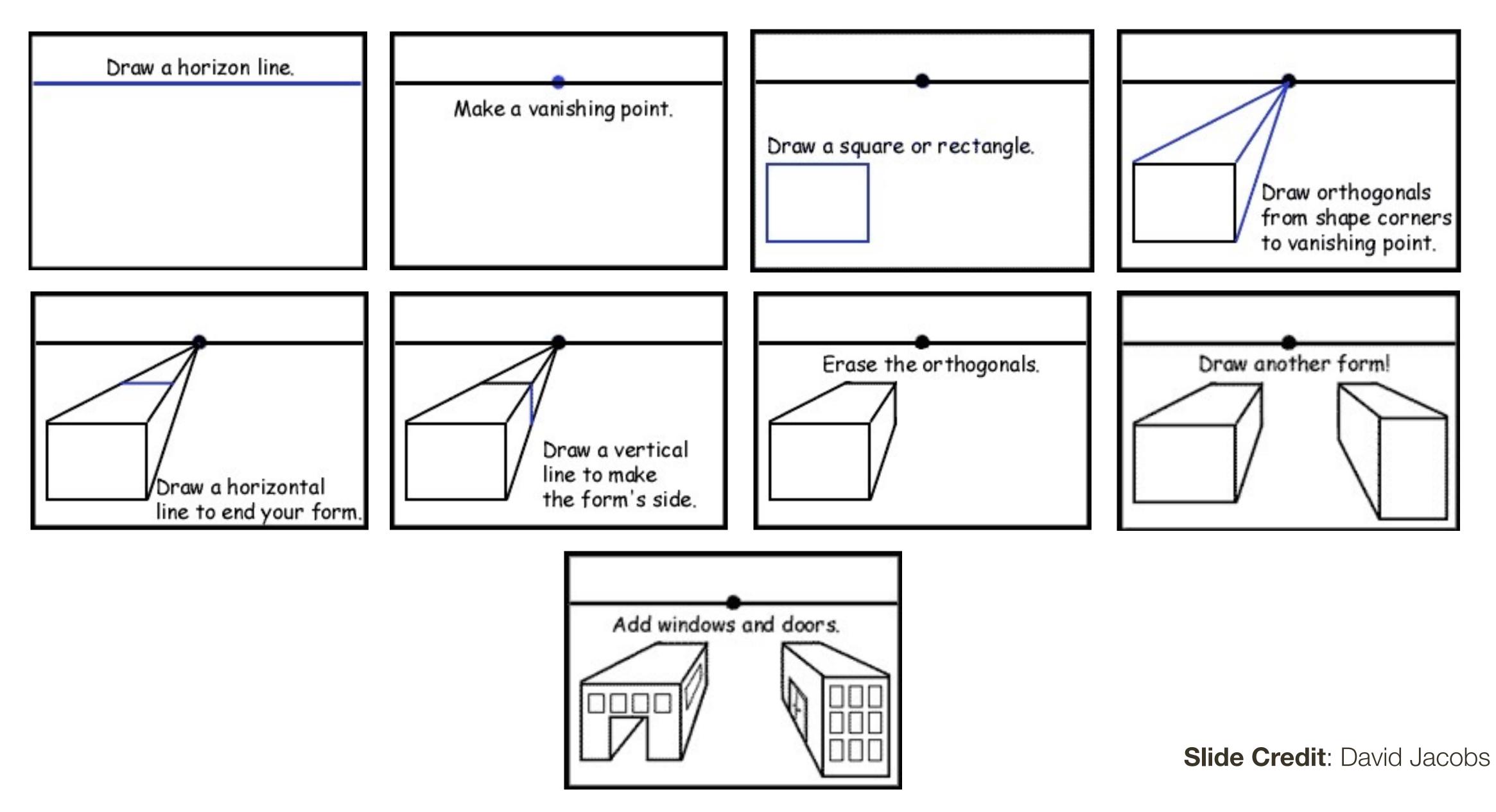


Draw a horizon line.

Slide Credit: David Jacobs



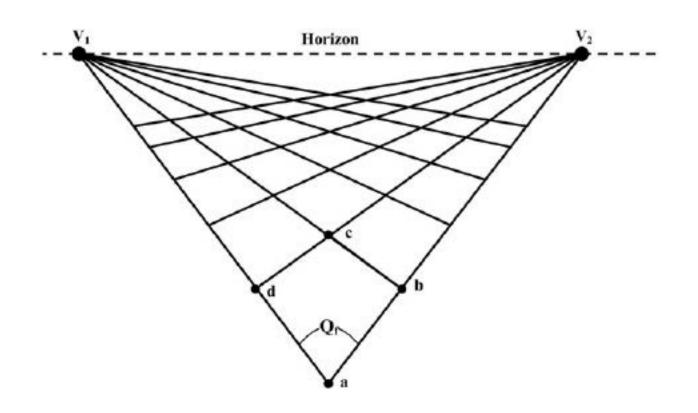
Slide Credit: David Jacobs



Each set of parallel lines meets at a different point - the point is called the **vanishing point** 

Sets of parallel lines on the same plane lead to **collinear** vanishing points — the line is called a **horizon** for that plane

A good way to **spot fake images**  scale and perspective do not work vanishing points behave badly



### Spotting fake images with Vanishing Points



Generated Image

Shadow Errors

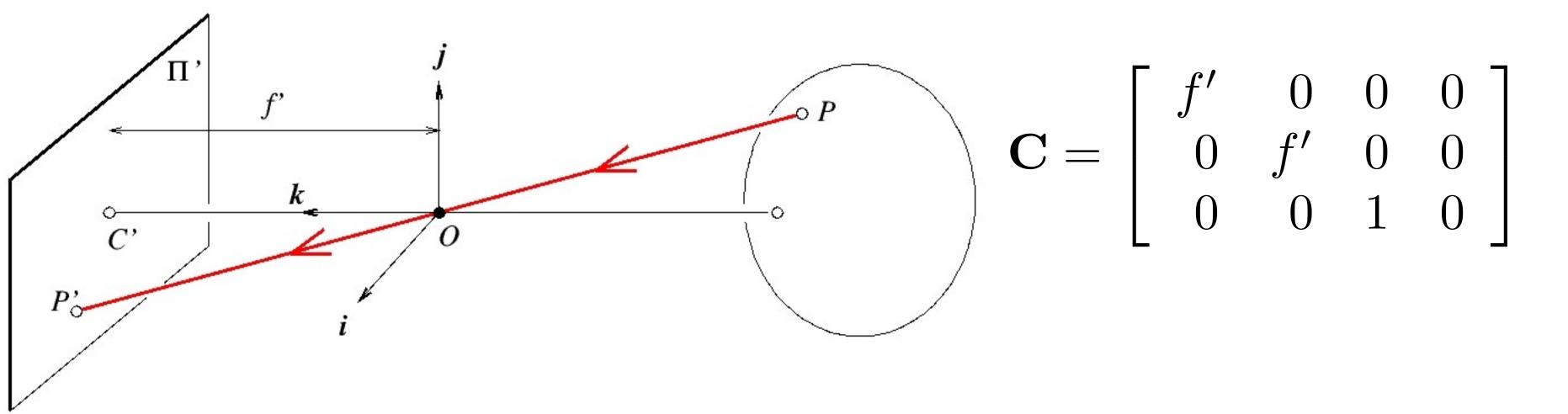
Detected Shadow Errors

[Sarkar et al., 2023, Image from https://projective-geometry.github.io/ reproduced for educational purposes.]

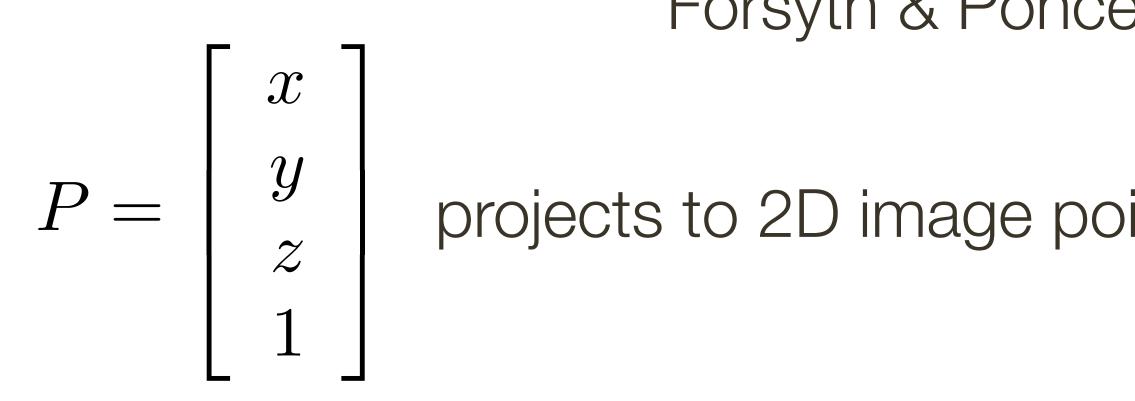
Vanishing Point Errors

**Detected Perspective Errors** 

### **Perspective** Projection: Matrix Form



#### 3D object point



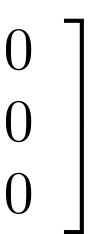


#### **Camera** Matrix

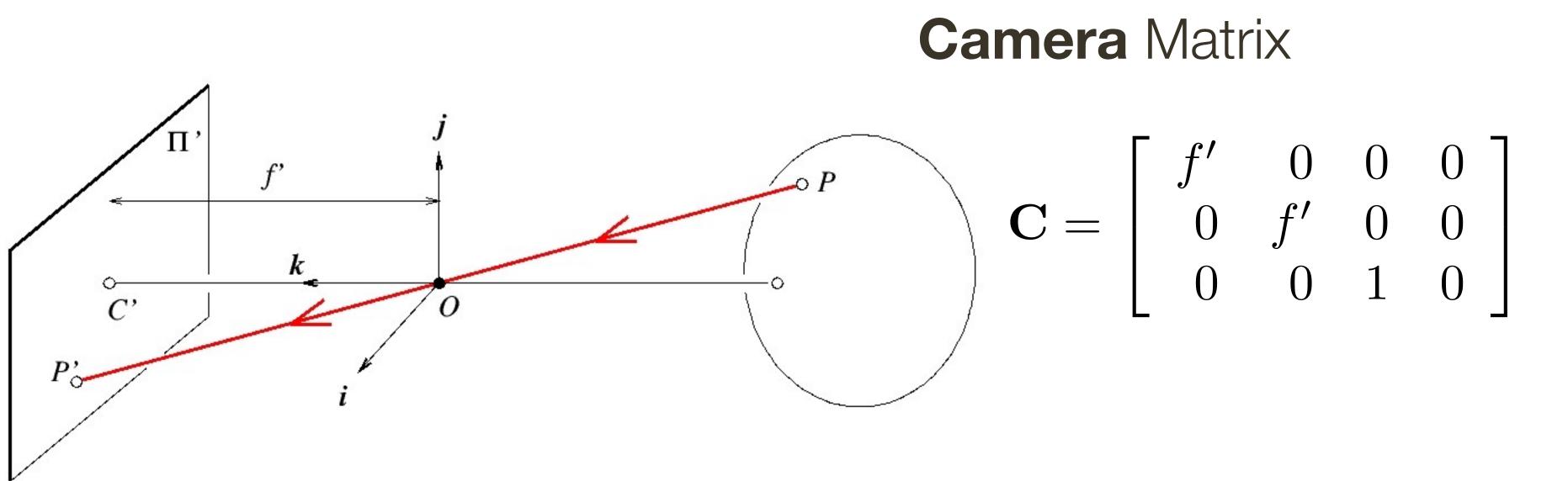
#### Forsyth & Ponce (1st ed.) Figure 1.4

pint 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $\mathbf{S}P' = \mathbf{C}P$ 

(s is a scale factor)







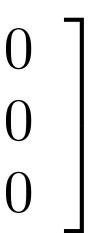
#### 3D object point

 ${\mathcal X}$  $egin{array}{c} y \ z \end{array}$ P =

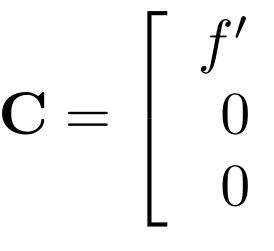
projects to 2D image po

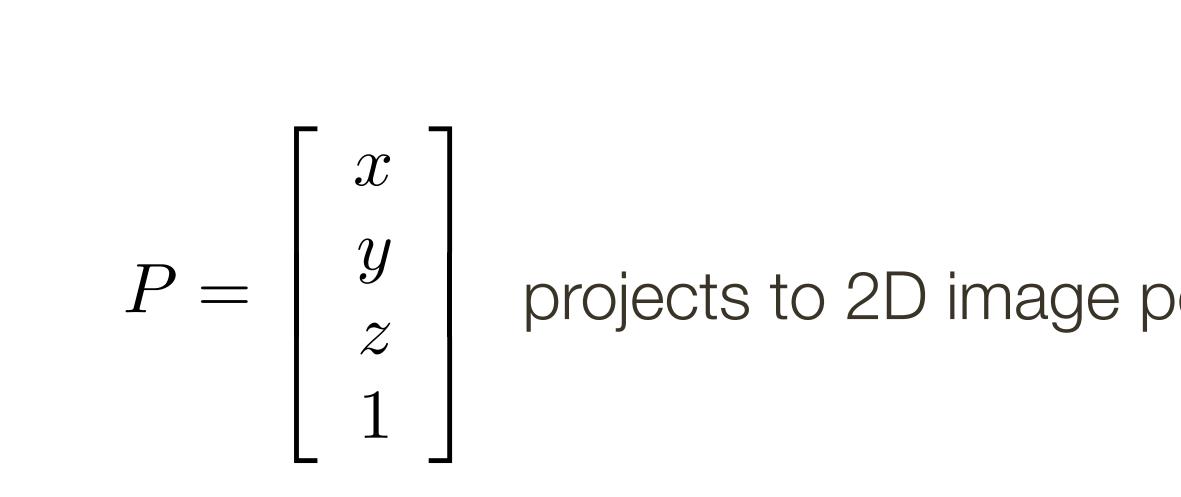
#### Forsyth & Ponce (1st ed.) Figure 1.4

pint 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $P' = \mathbf{C}P$ 



#### **Camera** Matrix





## $\mathbf{C} = \begin{bmatrix} f' & 0 & 0 & 0 \\ 0 & f' & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$

point 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $P' = \mathbf{C}P$ 

#### **Camera** Matrix

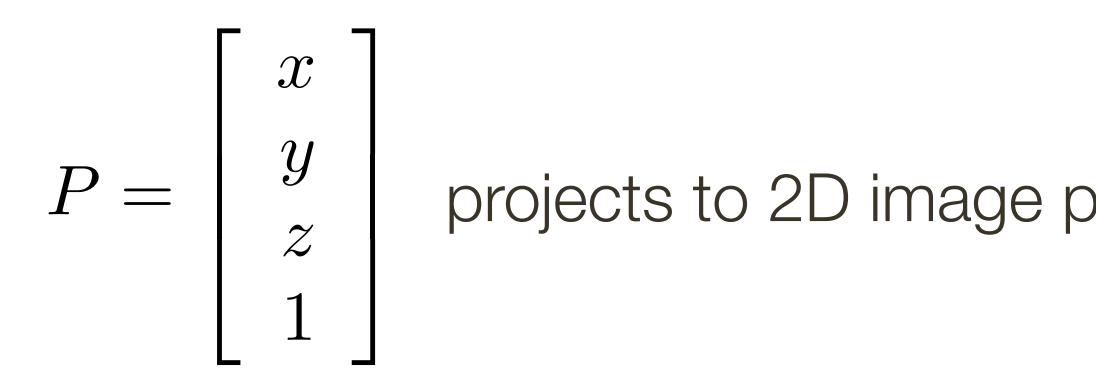
projects to 2D image

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- $\mathbf{C} = \left[ \begin{array}{cccc} f' & 0 & 0 & 0 \\ 0 & f' & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right]$
- Pixels are squared / lens is perfectly symmetric
  - Sensor and pinhole perfectly aligned
  - Coordinate system centered at the pinhole

point 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $P' = \mathbf{C}P$ 

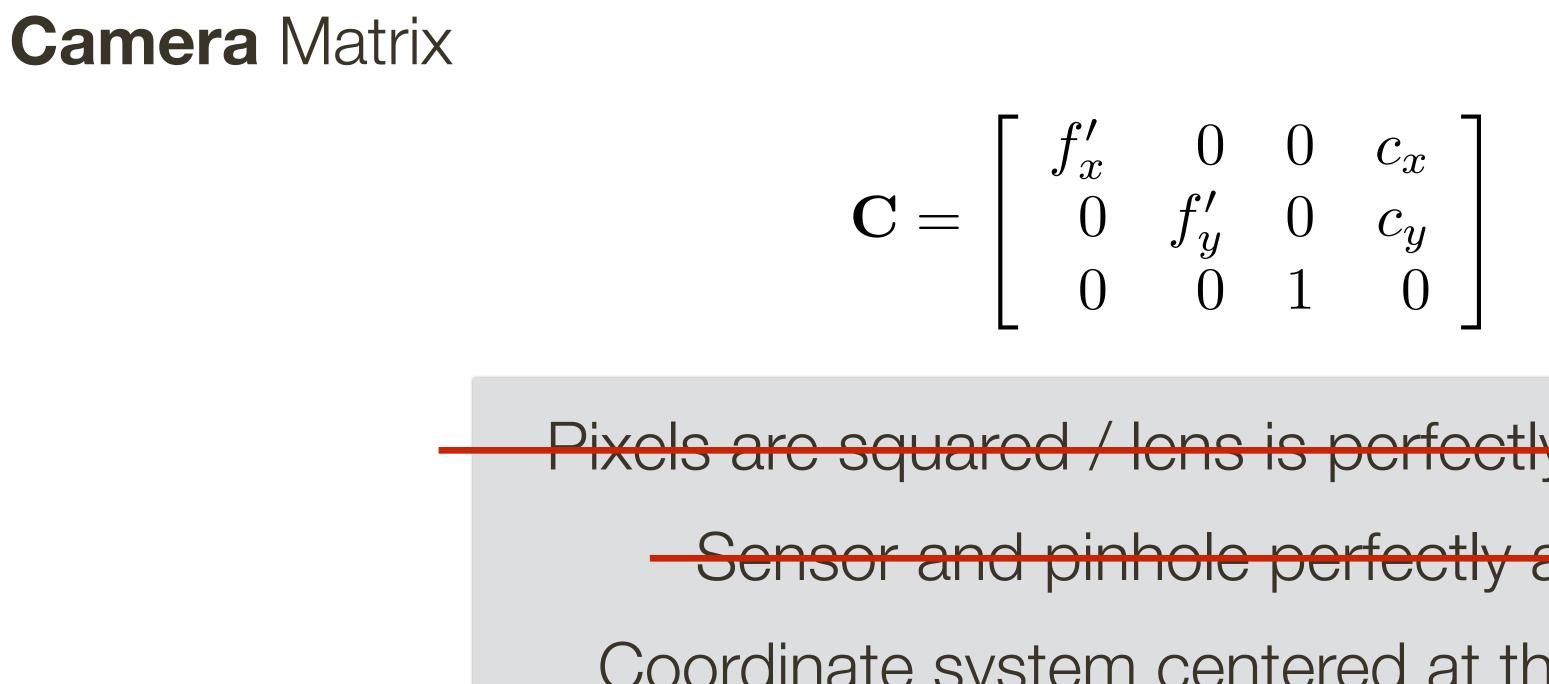
#### **Camera** Matrix



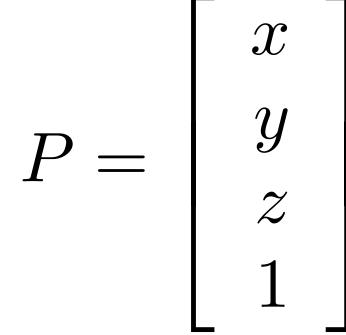
## $\mathbf{C} = \begin{bmatrix} f'_x & 0 & 0 & 0 \\ 0 & f'_y & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$

- Pixels are squared / lens is perfectly symmetric
  - Sensor and pinhole perfectly aligned
  - Coordinate system centered at the pinhole

point 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $P' = \mathbf{C}P$ 

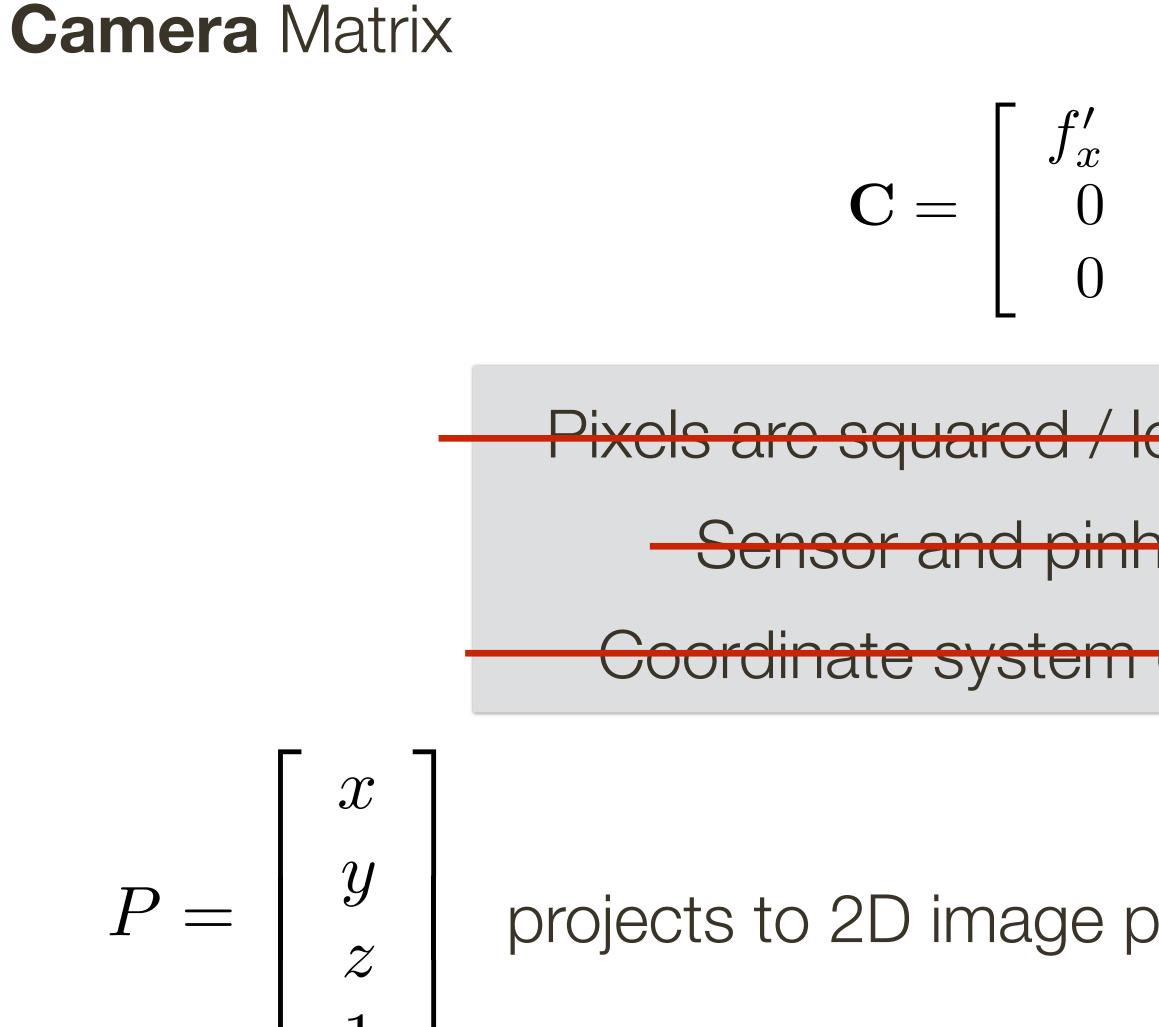


 $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix} \text{ projects to 2D image } \mathfrak{r}$ 



- Pixels are squared / lens is perfectly symmetric
  - Sensor and pinhole perfectly aligned
  - Coordinate system centered at the pinhole

point 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $P' = \mathbf{C}P$ 



$$\begin{bmatrix} 0 & 0 & c_x \\ f'_y & 0 & c_y \\ 0 & 1 & 0 \end{bmatrix} \mathbb{R}_{4 \times 4}$$

Pixels are squared / lens is perfectly symmetric

Sensor and pinhole perfectly aligned

Coordinate system centered at the pinhole

point 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $P' = \mathbf{C}P$ 

#### **Camera** Matrix

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

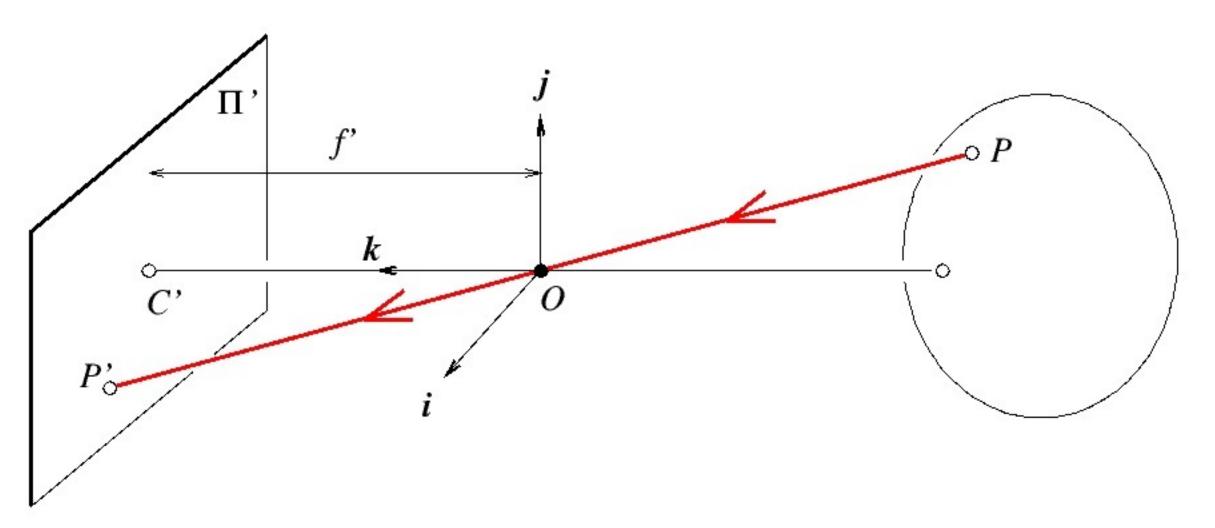
projects to 2D image projects

## $\mathbf{C} = \begin{bmatrix} f'_{x} & 0 & 0 & c_{x} \\ 0 & f'_{y} & 0 & c_{y} \\ 0 & 0 & 1 & 0 \end{bmatrix} \mathbb{R}_{4 \times 4}$

#### **Camera calibration** is the process of estimating the parameters of the camera matrix based on a set of 3D-2D correspondences (usually requires a pattern whose structure and size are known)

point 
$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix}$$
 where  $P' = \mathbf{C}P$ 

### **Perspective** Projection

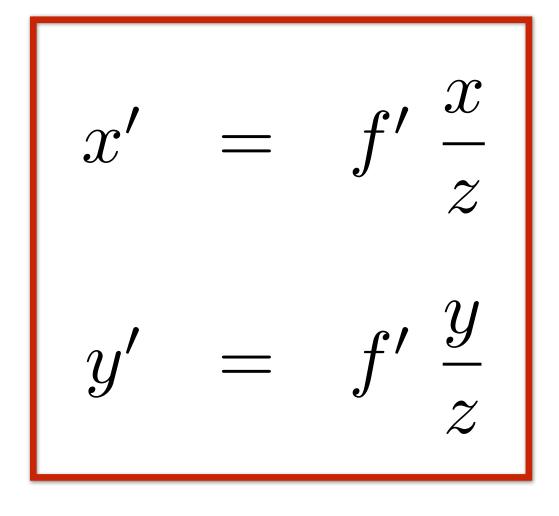


#### 3D object point

 $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$  projects to 2D image point  $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$  where

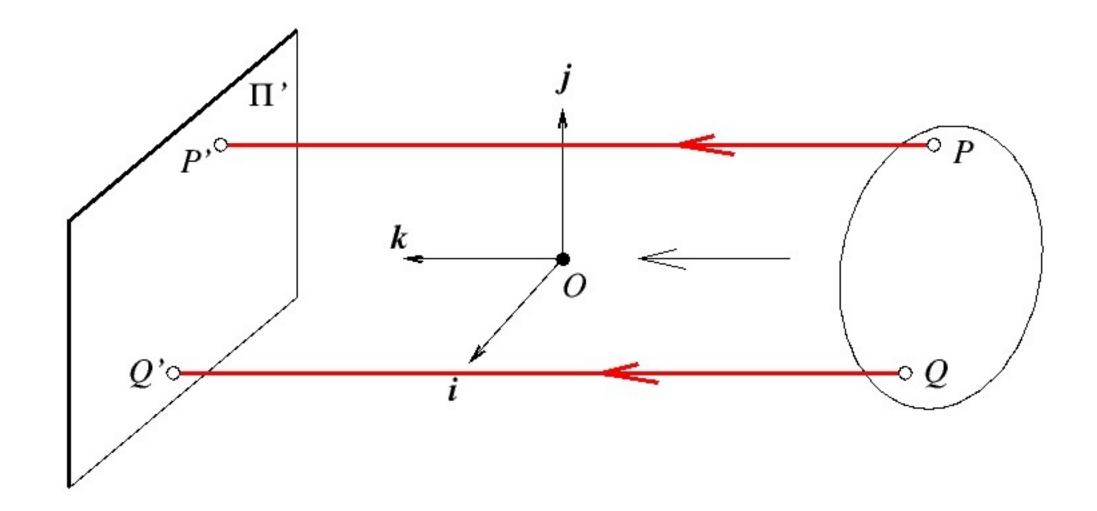
**Note:** this assumes world coordinate frame at the optical center (pinhole) and aligned with the image plane, image coordinate frame aligned with the camera coordinate frame

# Forsyth & Ponce (1st ed.) Figure 1.4





# **Orthographic** Projection



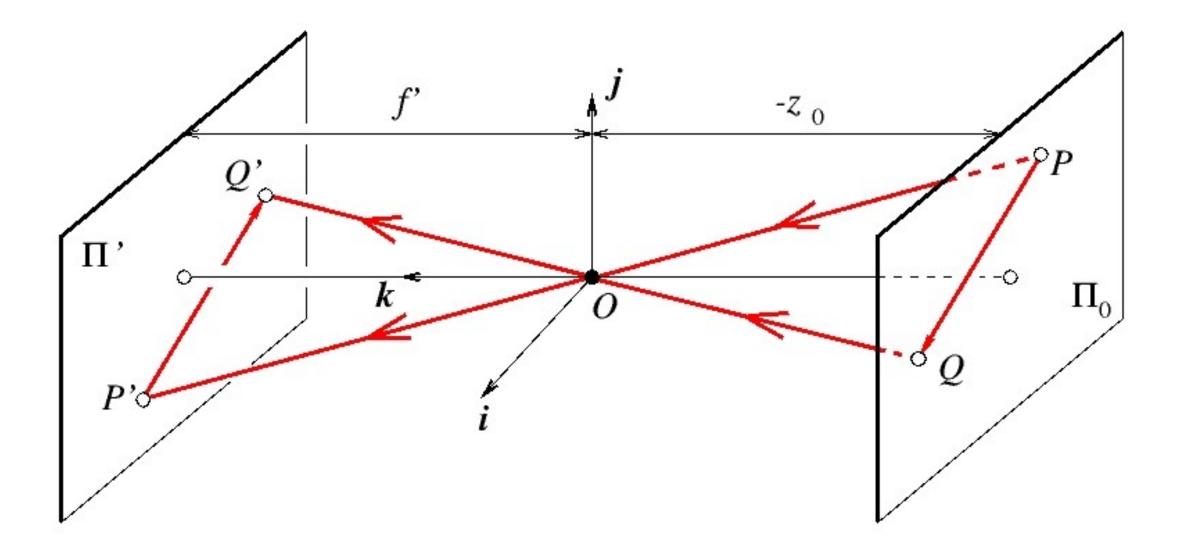
3D object point 
$$P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$
 projects to 2D image point  $P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$ 

where

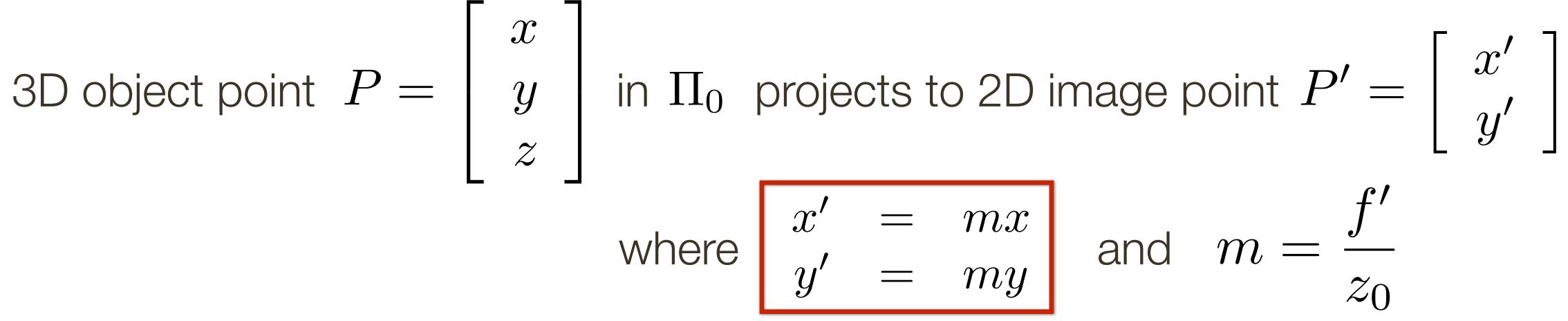
### Forsyth & Ponce (1st ed.) Figure 1.6

### Weak Perspective





### Forsyth & Ponce (1st ed.) Figure 1.5



# Summary of Projection Equations

3D object point  $P = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$  projects t

# Perspective

### Weak Perspective

Orthographic

to 2D image point 
$$P' = \begin{bmatrix} x' \\ y' \end{bmatrix}$$
 where

$$x' = f' \frac{x}{z}$$

$$y' = f' \frac{y}{z}$$

$$x' = mx$$

$$m = \frac{f'}{z_0}$$

$$y' = my$$

$$x' = x$$

$$y' = y$$

# **Projection Models:** Pros and Cons

- Weak perspective (including orthographic) has simpler mathematics accurate when object is small and/or distant
- useful for recognition

**Perspective** is more accurate for real scenes

details of a particular camera

- When **maximum accuracy** is required, it is necessary to model additional
- use perspective projection with additional parameters (e.g., lens distortion)

# Projection Illusion



### Our brains also know this perspective model very well!

# Why **Not** a Pinhole Camera?

- If pinhole is **too big** then many directions are averaged, blurring the image
- If pinhole is **too small** then diffraction becomes a factor, also blurring the image
- Generally, pinhole cameras are **dark**, because only a very small set of rays from a particular scene point hits the image plane
- Pinhole cameras are **slow**, because only a very small amount of light from a particular scene point hits the image plane per unit time

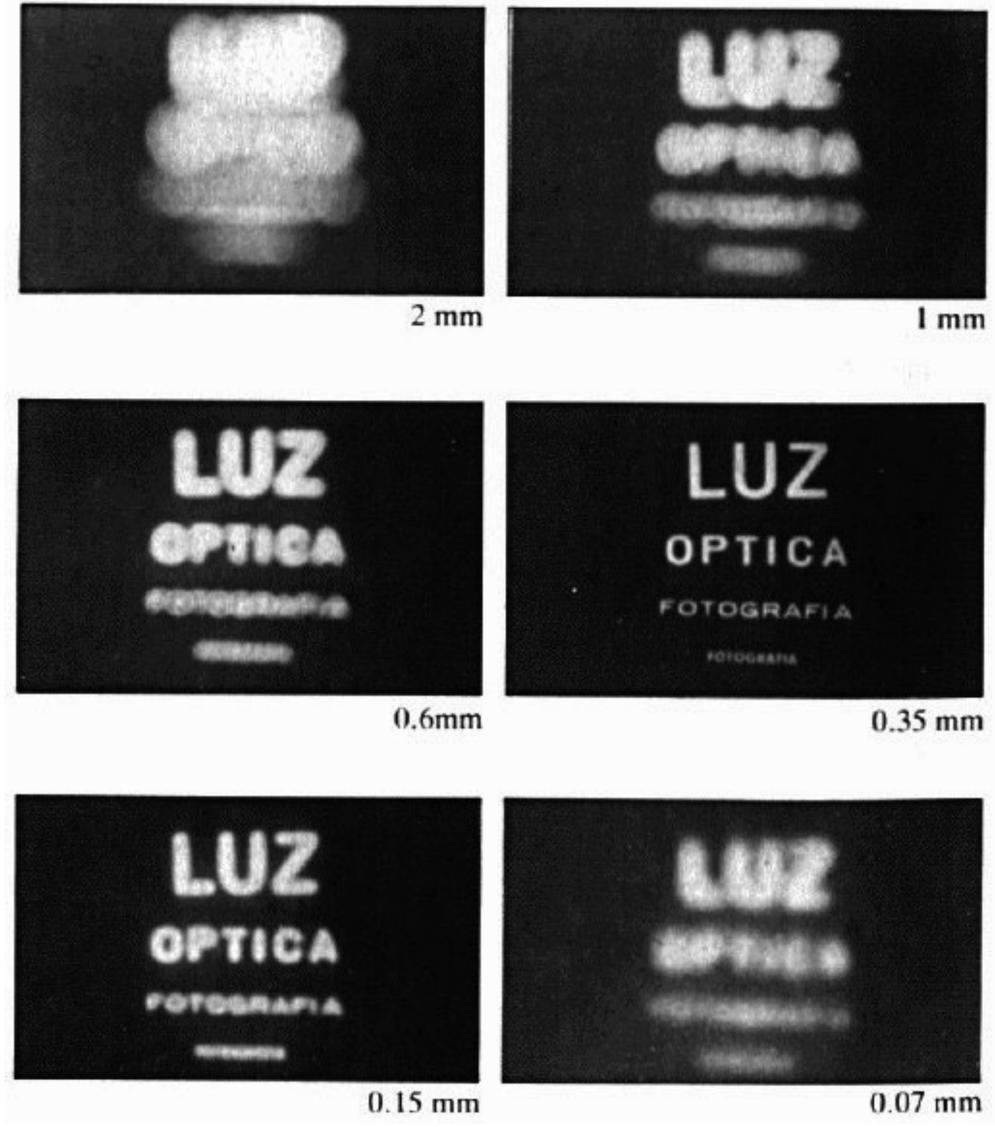
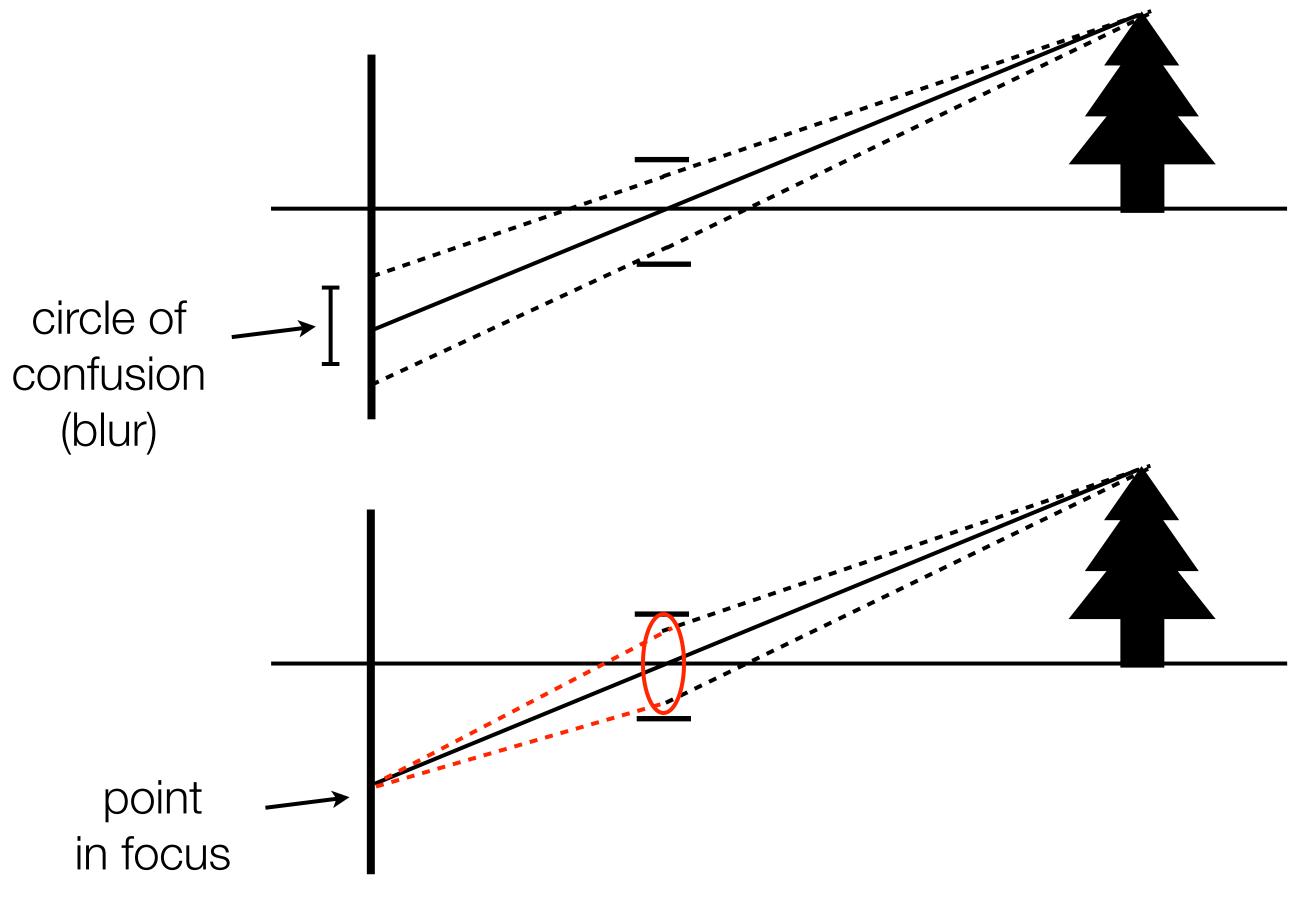


Image Credit: Credit: E. Hecht. "Optics," Addison-Wesley, 1987



### Reason for Lenses

### A real camera must have a finite aperture to get enough light, but this causes blur in the image

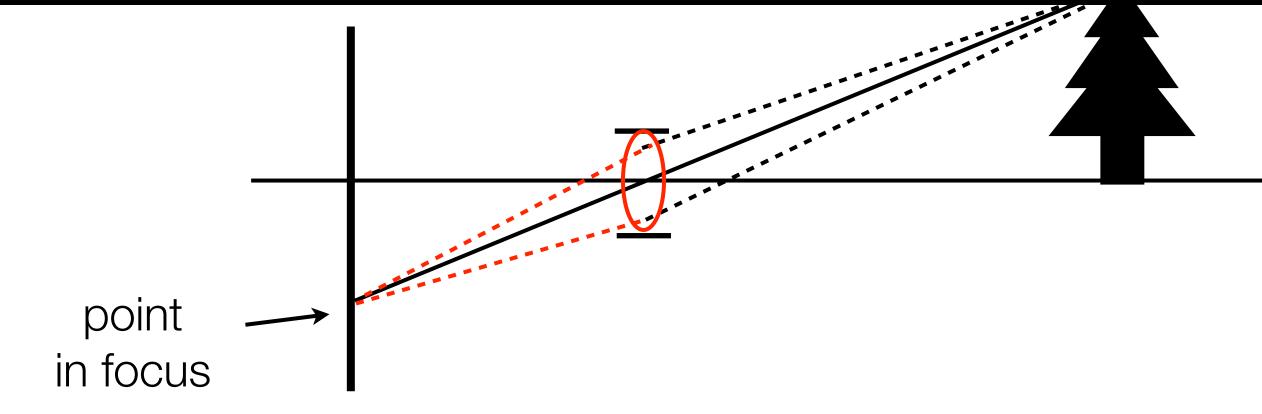


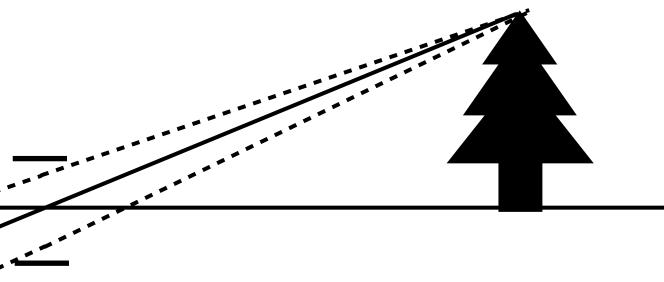
### Solution: use a lens to focus light onto the image plane

### Reason for **Lenses**

### A real camera must have a finite aperture to get enough light, but this causes blur in the image



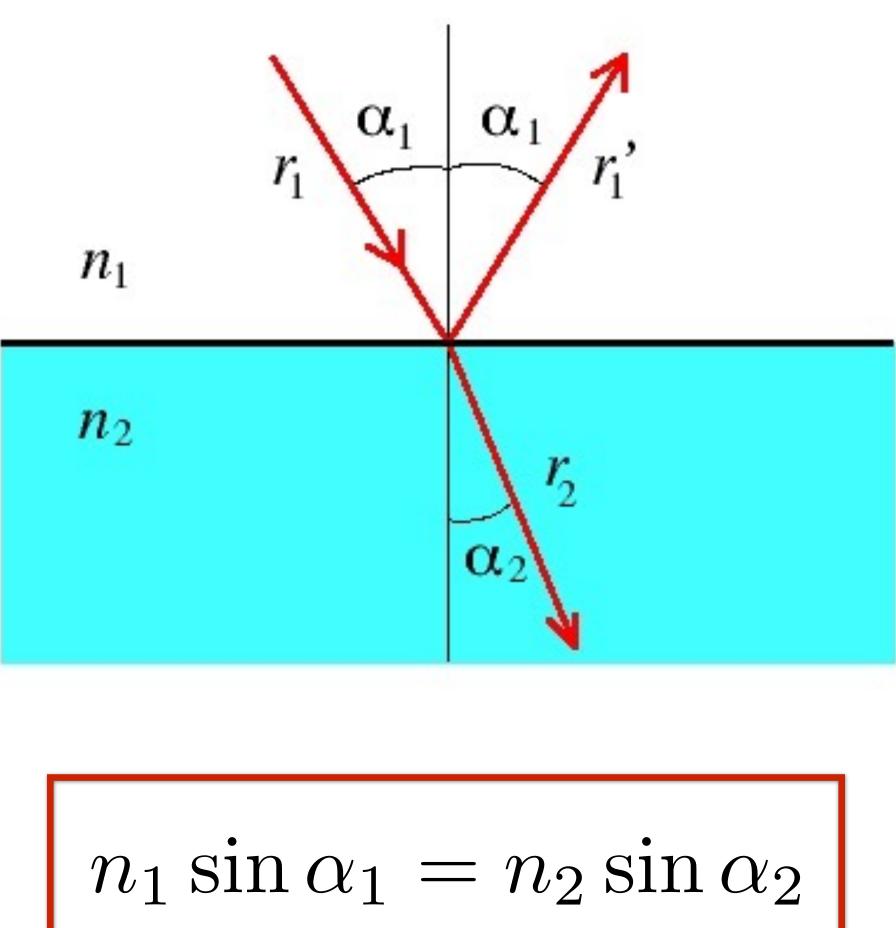




### The role of a lens is to capture more light while preserving, as much as possible, the abstraction of an ideal pinhole camera.

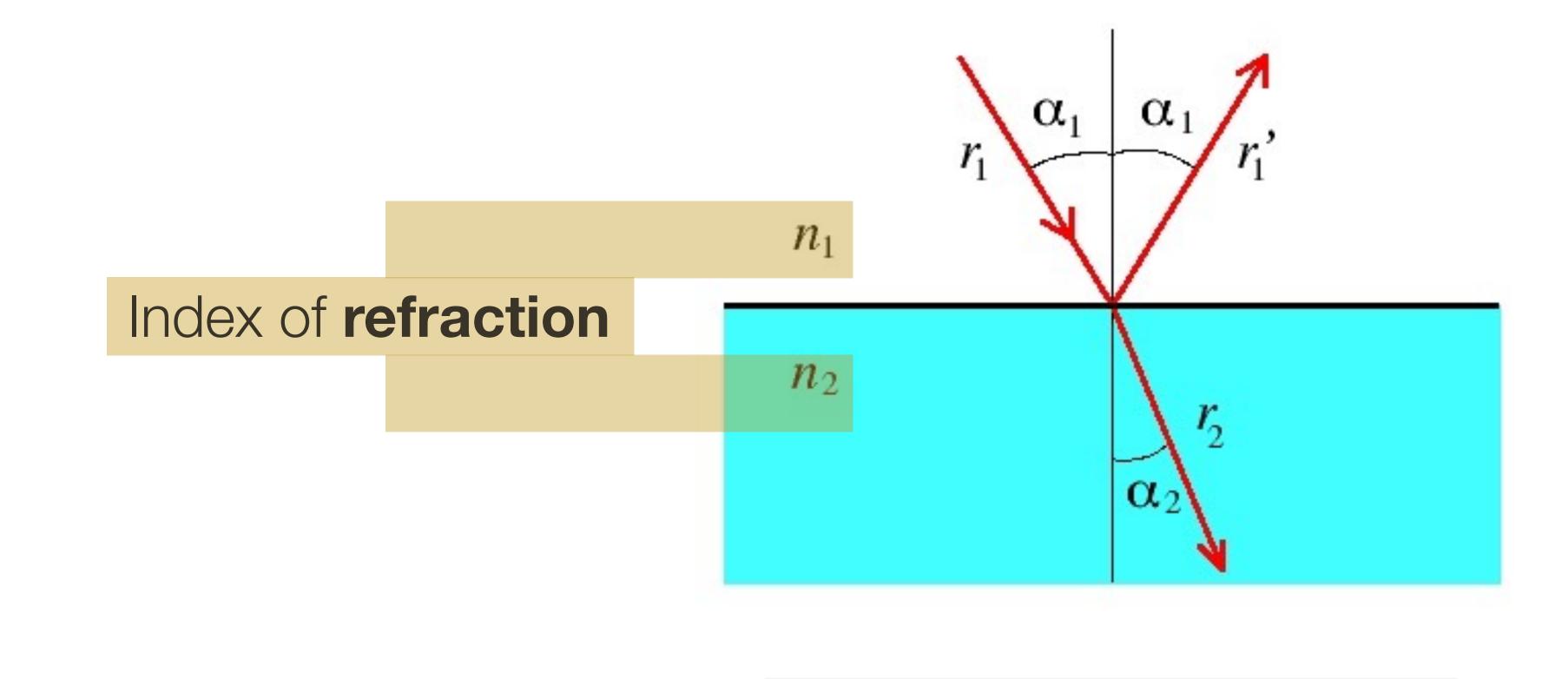
**Solution**: use a **lens** to focus light onto the image plane

### Snell's Law



$$n_1 = n_2 \sin \alpha_2$$

# Snell's Law



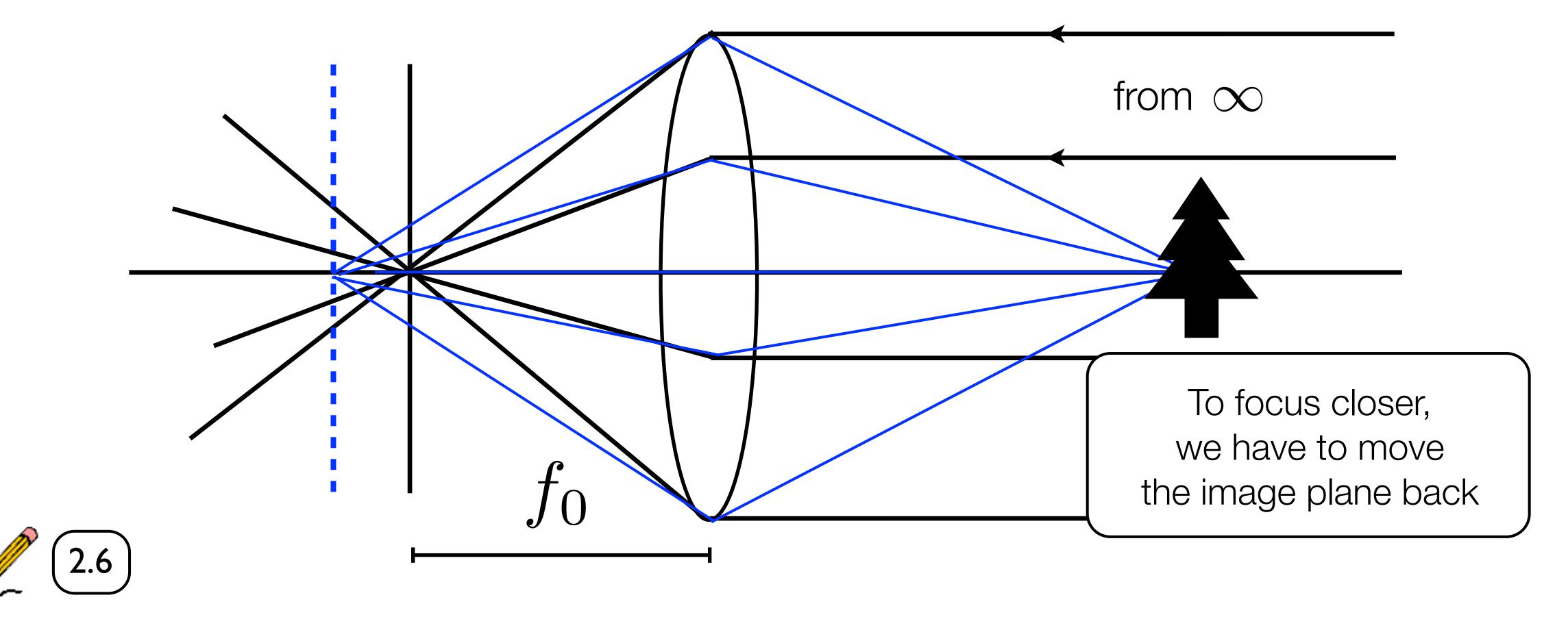
 $n_1 \sin lpha_1$ 

$$n_1 = n_2 \sin \alpha_2$$

82

# Lens Basics

- A lens focuses rays from infinity at the focal length of the lens
- Points passing through the centre of the lens are not bent



• We can use these 2 properties to find the **thin** lens equation

### Lens Basics

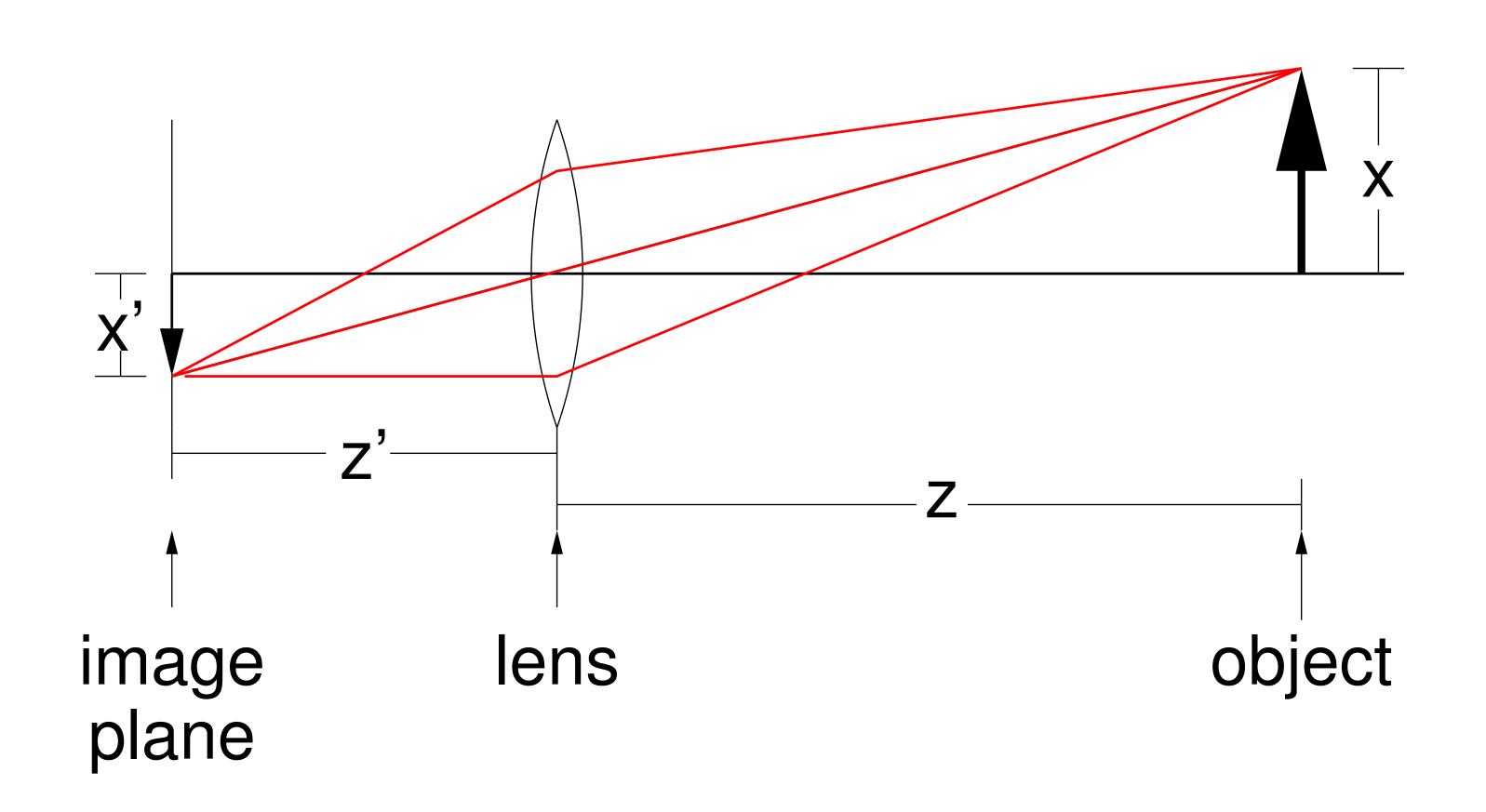
away. How far does the lens move?



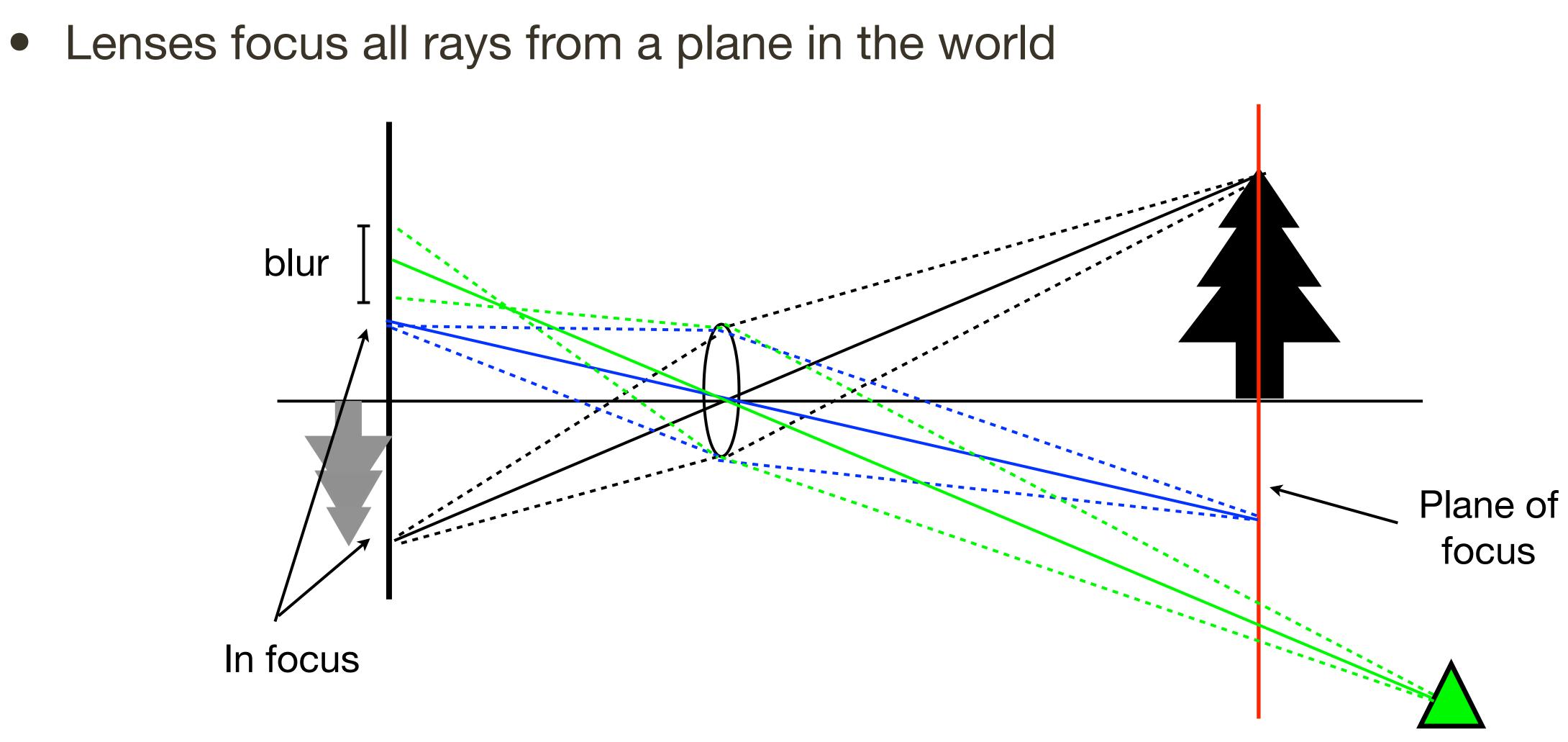


• A 50mm lens is focussed at infinity. It now moves to focus on something 5m

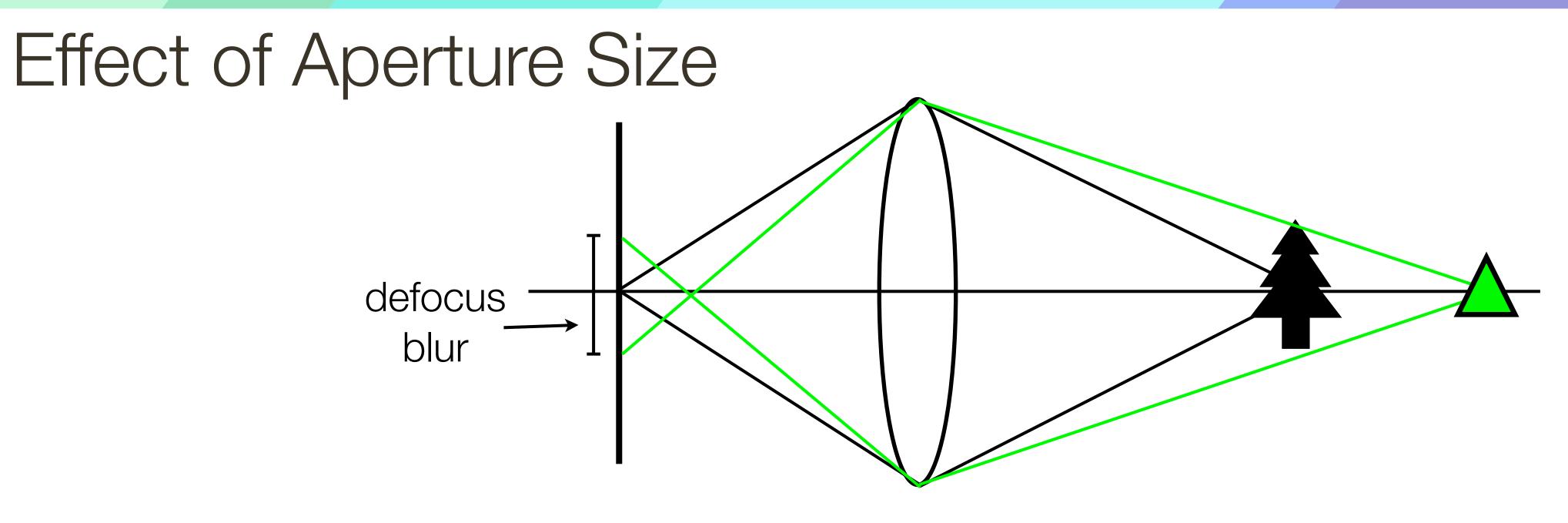
# Pinhole Model with Lens

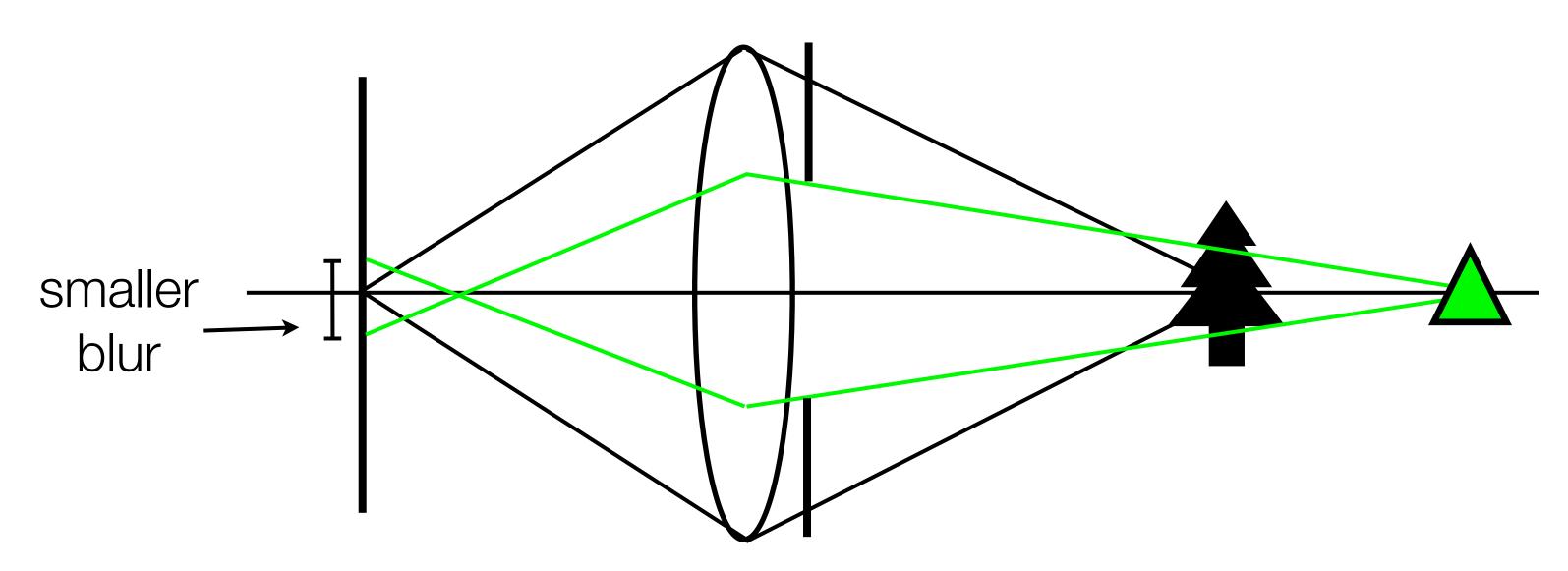


### Lens Basics



• Objects off the plane are blurred depending on distance





Smaller aperture  $\Rightarrow$  smaller blur, larger **depth of field** 

# Depth of Field

### • Photographers use large apertures to give small depth of field



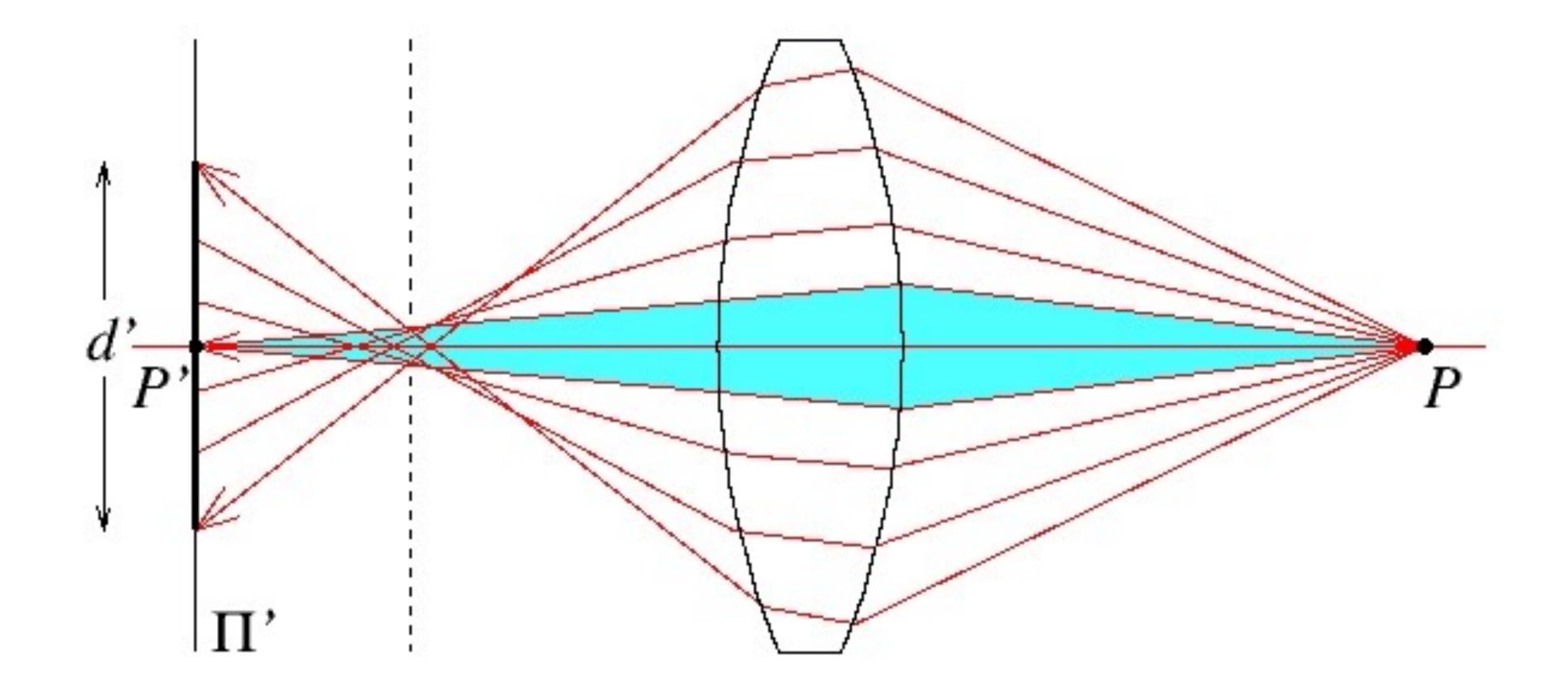
### Aperture size = f/N, $\Rightarrow$ large N = small aperture

### Real Lenses



- Real Lenses have multiple stages of positive and negative elements with differing refractive indices
- This can help deal with issues such as chromatic aberration (different colours bent by different amounts), vignetting (light fall off at image edge) and sharp imaging across the zoom range

### Spherical Aberration



### Forsyth & Ponce (1st ed.) Figure 1.12a

### Spherical Aberration

### Un-aberrated image

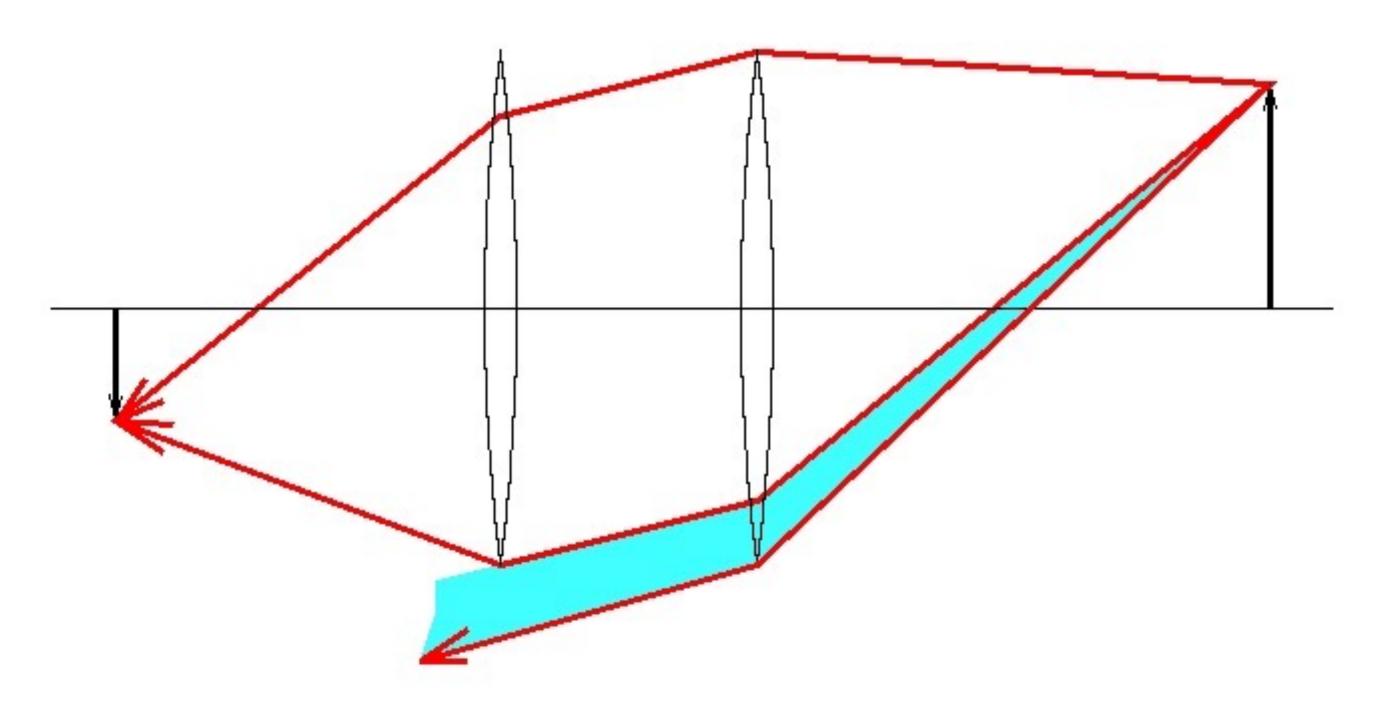


### Image from lens with Spherical Aberration



# Vignetting

### Vignetting in a two-lens system



### Forsyth & Ponce (2nd ed.) Figure 1.12

The shaded part of the beam never reaches the second lens

# Vignetting



Image Credit: Cambridge in Colour

# Chromatic Aberration

- Index of **refraction depends on wavelength**,  $\lambda$ , of light
- Light of different colours follows different paths
- Therefore, not all colours can be in equal focus

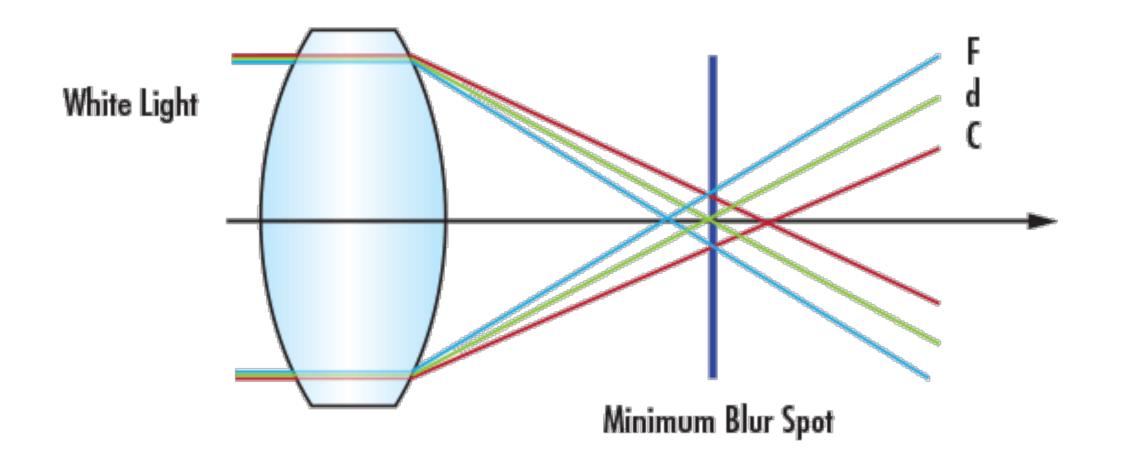
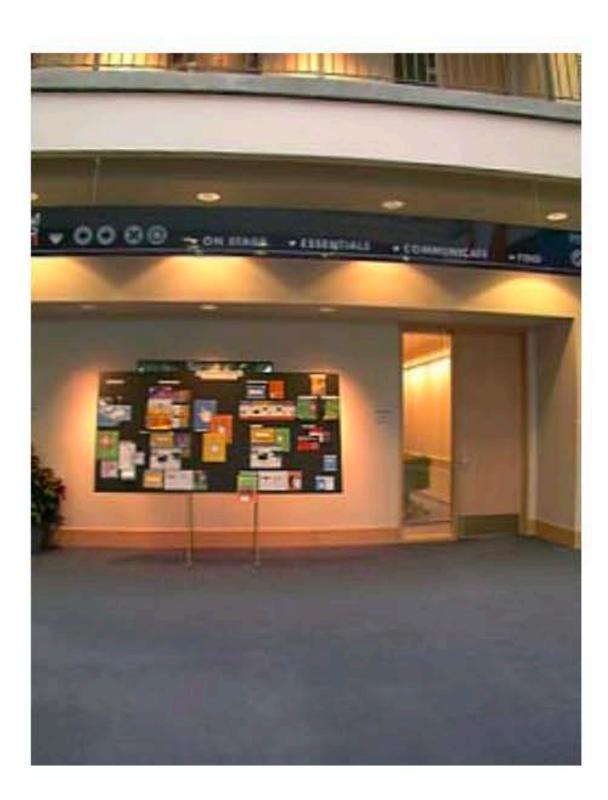




Image Credit: Trevor Darrell



### Lens **Distortion**





Lines in the world are no longer lines on the image, they are curves! 95

### Fish-eye Lens

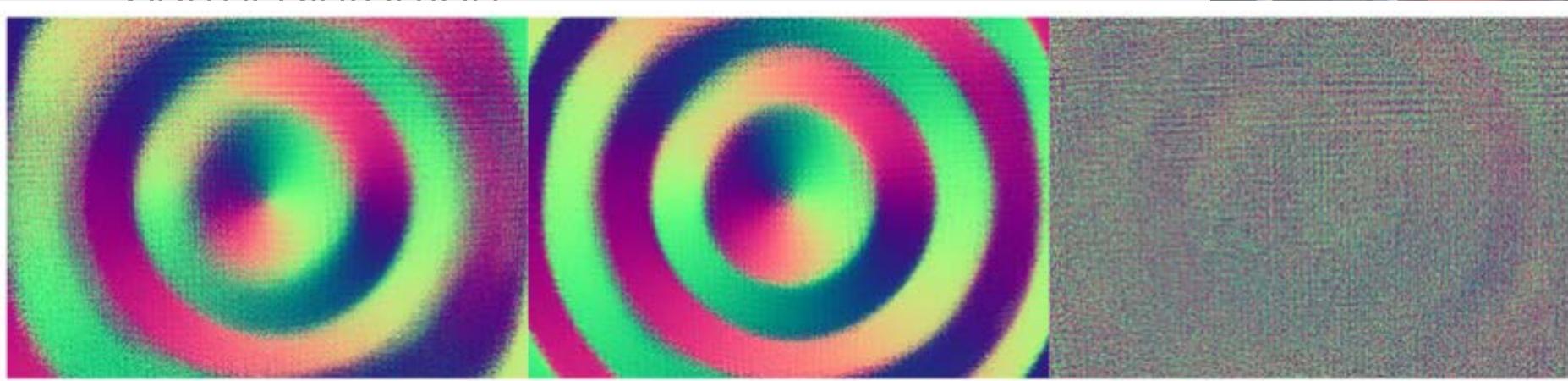


Szeliski (1st ed.) Figure 2.13



# Other (Possibly Significant) Lens Effects Scattering at the lens surface — Some light is reflected at each lens surface There are other geometric phenomena/distor — pincushion distortion

- harrel distortion



### Parametric calibration errors

Image from [Schöps et al., 2019]. Reproduced for educational purposes.

### [Schöps et al., 2020]

<u>nragsdale/3192314056/</u>

# Lecture Summary

— We discussed a "physics-based" approach to image formation. Basic abstraction is the **pinhole camera**.

 Lenses overcome limitations of the pinhole model while trying to preserve it as a useful abstraction

- Projection equations: **perspective**, weak perspective, orthographic
- Thin lens equation
- Some "aberrations and **distortions**" persist (e.g. spherical aberration, vignetting)