Please get your iClickers — Quiz 4: 6 questions

Recap

2D Transformations

Transformation	Matrix	# DoF	Preserves	Icon
translation	$\left[egin{array}{c c} I & t \end{array} ight]_{2 imes 3}$	2	orientation	
rigid (Euclidean)	$\left[egin{array}{c c} oldsymbol{R} & oldsymbol{t} \end{array} ight]_{2 imes 3}$	3	lengths	
similarity	$\left[\begin{array}{c c}soldsymbol{R} & oldsymbol{t}\end{array}\right]_{2 imes 3}$	4	angles	
affine	$\left[\begin{array}{c} oldsymbol{A} \end{array} ight]_{2 imes 3}$	6	parallelism	
projective	$\left[egin{array}{c} ilde{oldsymbol{H}} \end{array} ight]_{3 imes 3}$	8	straight lines	

Projective Transformation

General 3x3 matrix transformation

$$\begin{bmatrix} x_1' \\ y_1' \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix}$$

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Lets try an example:

Projective Transformation

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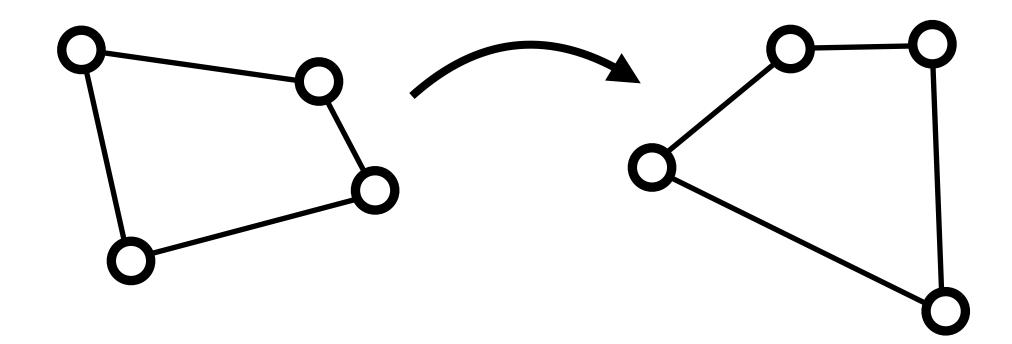
Lets try an example:

Divide by the last row:
$$\begin{bmatrix} 0 & 0 & 1 & 0.5 \\ 0 & 0.5 & 0 & 0.5 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

Compute H from Correspondences

Each match gives 2 equations to solve for 8 parameters

$$\begin{bmatrix} x_1' \\ y_1' \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix}$$



→ 4 correspondences to solve for **H** matrix

Solution uses Singular Value Decomposition (SVD)

In Assignment 4 you can compute this using cv2.findHomography

Example 1: Fitting a Line

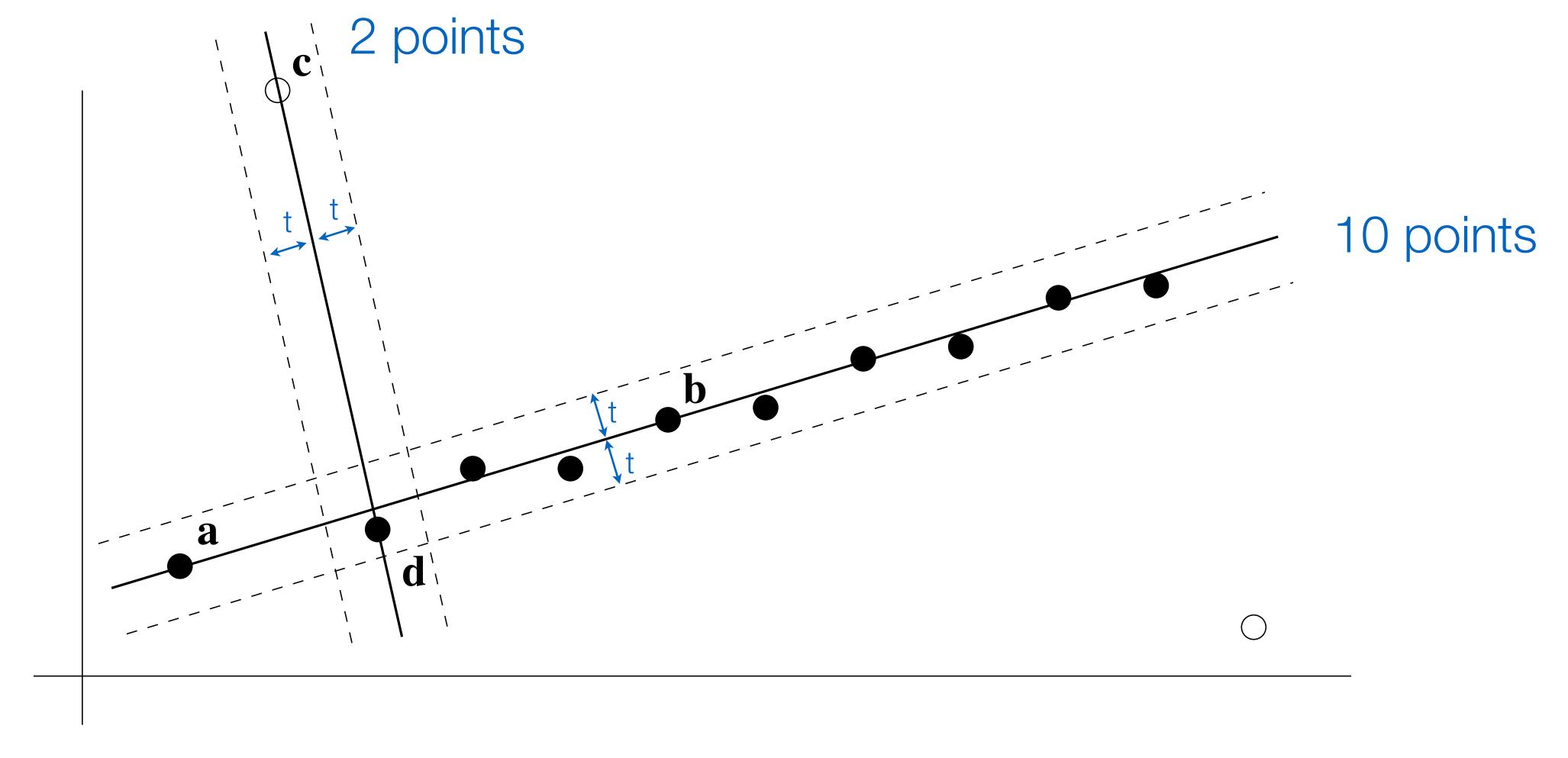


Figure Credit: Hartley & Zisserman

RANSAC (RANdom SAmple Consensus)

- 1. Randomly choose minimal subset of data points necessary to fit model (a sample)

 Fitting a Line: 2 points
- 2. Points within some distance threshold, t, of model are a **consensus set**. Size of consensus set is model's **support**
- 3. Repeat for N samples; model with biggest support is most robust fit
 - Points within distance t of best model are inliers
 - Fit final model to all inliers

RANSAC: How many samples? (p = 0.99)

Sample size	Proportion of outliers							
n	5%	10%	20%	25%	30%	40%	50%	
2	2	3	5	6	7	11	17	
3	3	4	7	9	11	19	35	
4	3	5	9	13	17	34	72	
5	4	6	12	17	26	57	146	
6	4	7	16	24	37	97	293	
7	4	8	20	33	54	163	588	
5 6 7 8	5	9	26	44	78	272	1177	

Figure Credit: Hartley & Zisserman



CPSC 425: Computer Vision

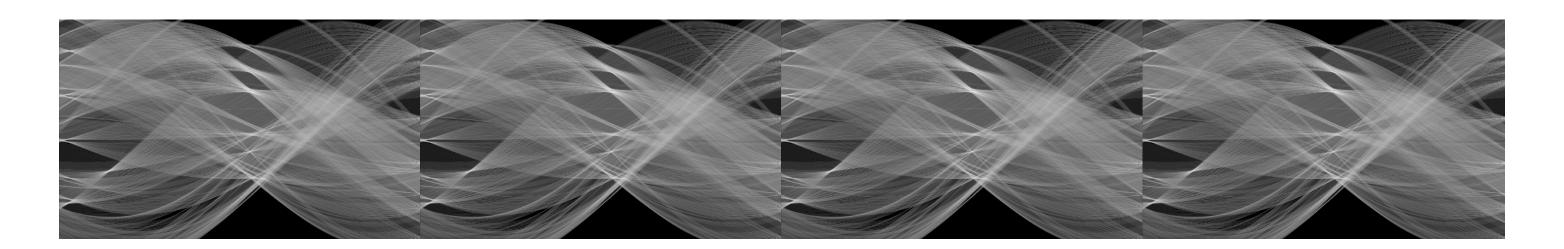


Image Credit: Ioannis (Yannis) Gkioulekas (CMU)

Lecture 14: Hough Transform

Menu for Today

Topics:

- Hough Transform
- Transformation Space Voting

Line Detection

Readings:

- Today's Lecture: Szeliski 7.4, Forsyth & Ponce 10.1

Reminders:

- Assignment 3: due Tomorrow!
- ICCV conference deadline is in 2 days aaaaaaaAA

Learning Goals

- 1. How to get multiple hypothesis
- 2. Voting-based strategies are useful

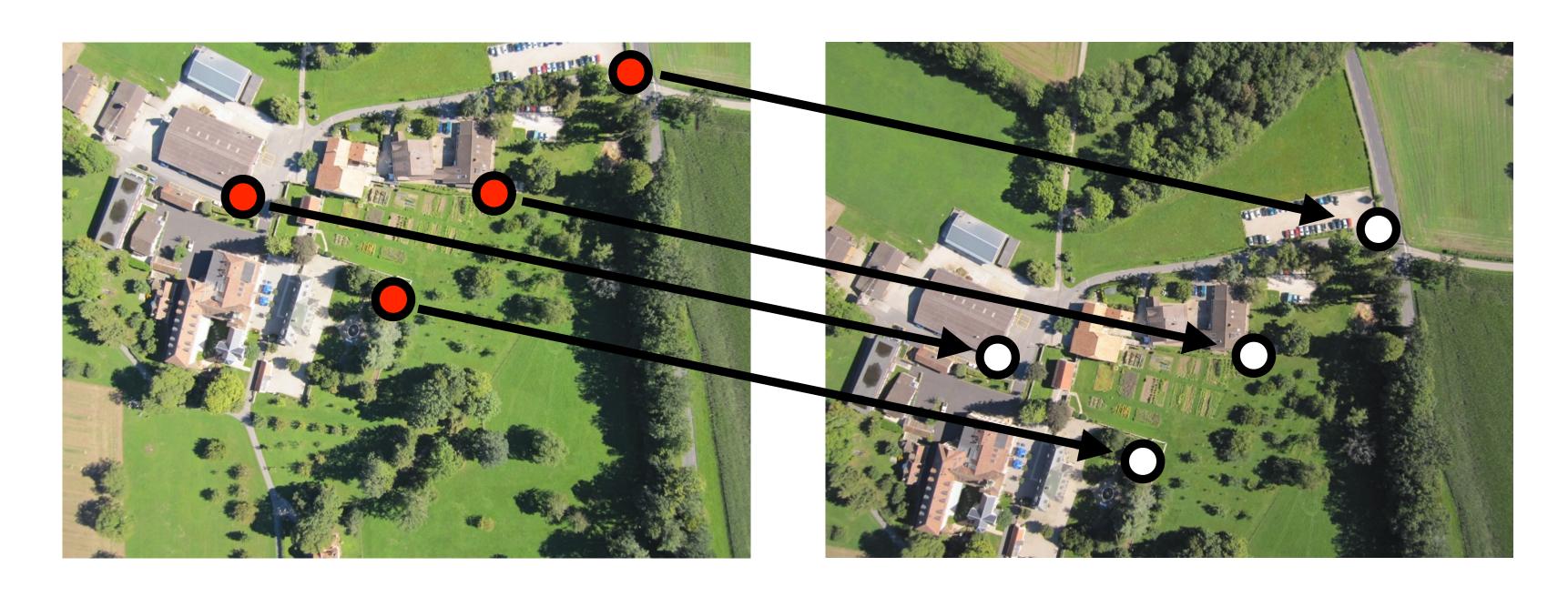
Image Alignment

Aim: Warp one image to align with another using a 2D transformation



Image Alignment

Step 1: Find correspondences (matching points) across two images



$$\mathbf{u} = \mathbf{H}\mathbf{x}$$

2 points for Similarity

3 for Affine

4 for Homography

Image Alignment

Step 2: Compute the transformation to align the two images



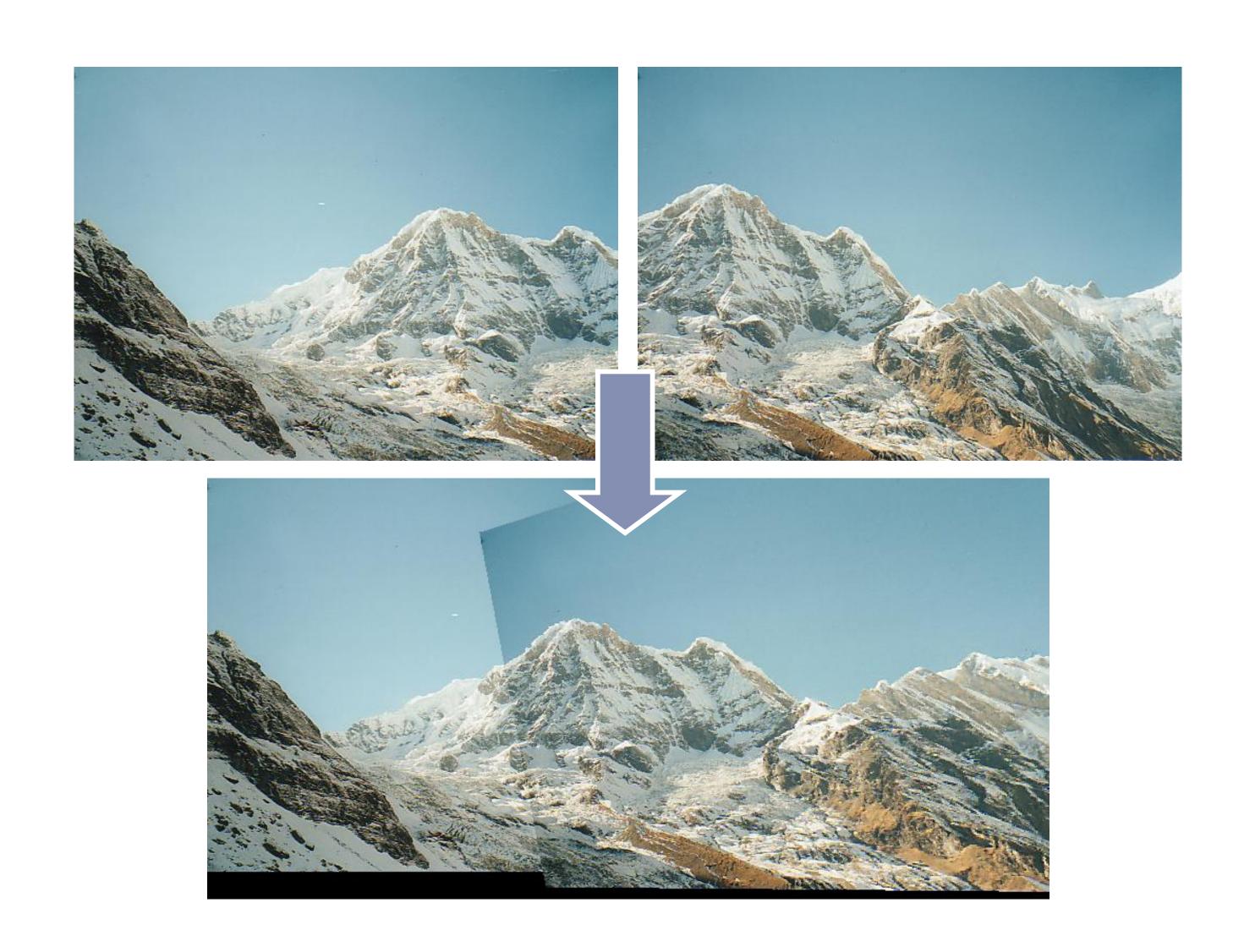
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RANSAC is very useful for variety of applications

2-view Rotation Estimation

Final rotation estimation



Example: Photo Tourism



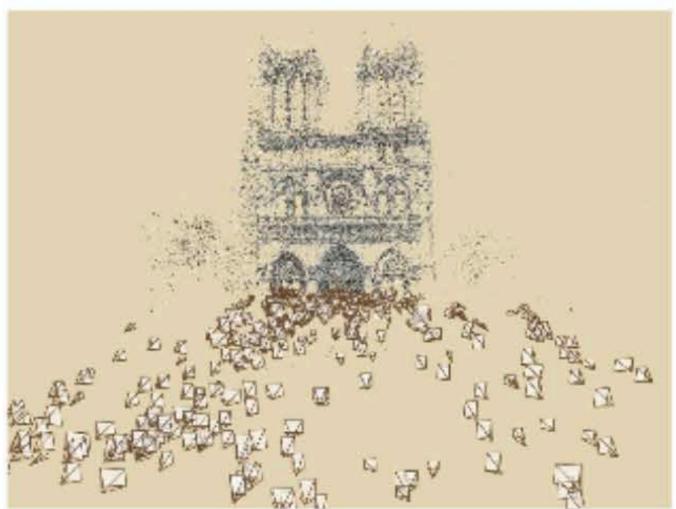




Figure credit: Snavely et al. 2006

Takes as input unstructured collections of photographs and reconstructs each photo's viewpoint and a sparse 3D model of the scene

Uses both SIFT and RANSAC

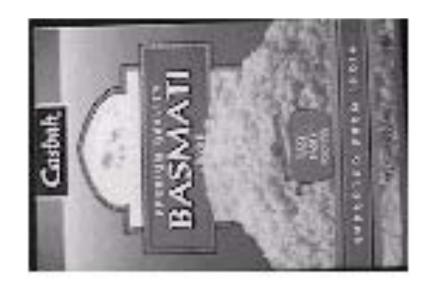
Example: Photo Tourism

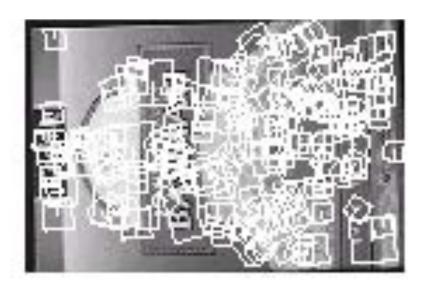


[Agarwal, Furukawa, Snavely, Curless, Seitz, Szeliski, 2010]

Object Instance Recognition

Database of planar objects

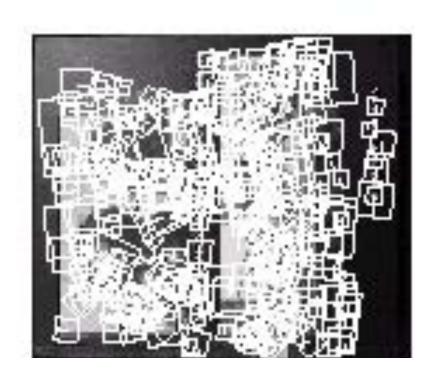












Instance recognition





Discussion of RANSAC

Advantages:

- General method suited for a wide range of model fitting problems
- Easy to implement and easy to calculate its failure rate

Disadvantages:

- Only handles a moderate percentage of outliers without cost blowing up
- Many real problems have high rate of outliers (but sometimes selective choice of random subsets can help)
- Hard to deal with multiple solutions (e.g., object detection with many objects)

The Hough transform can handle high percentage of outliers

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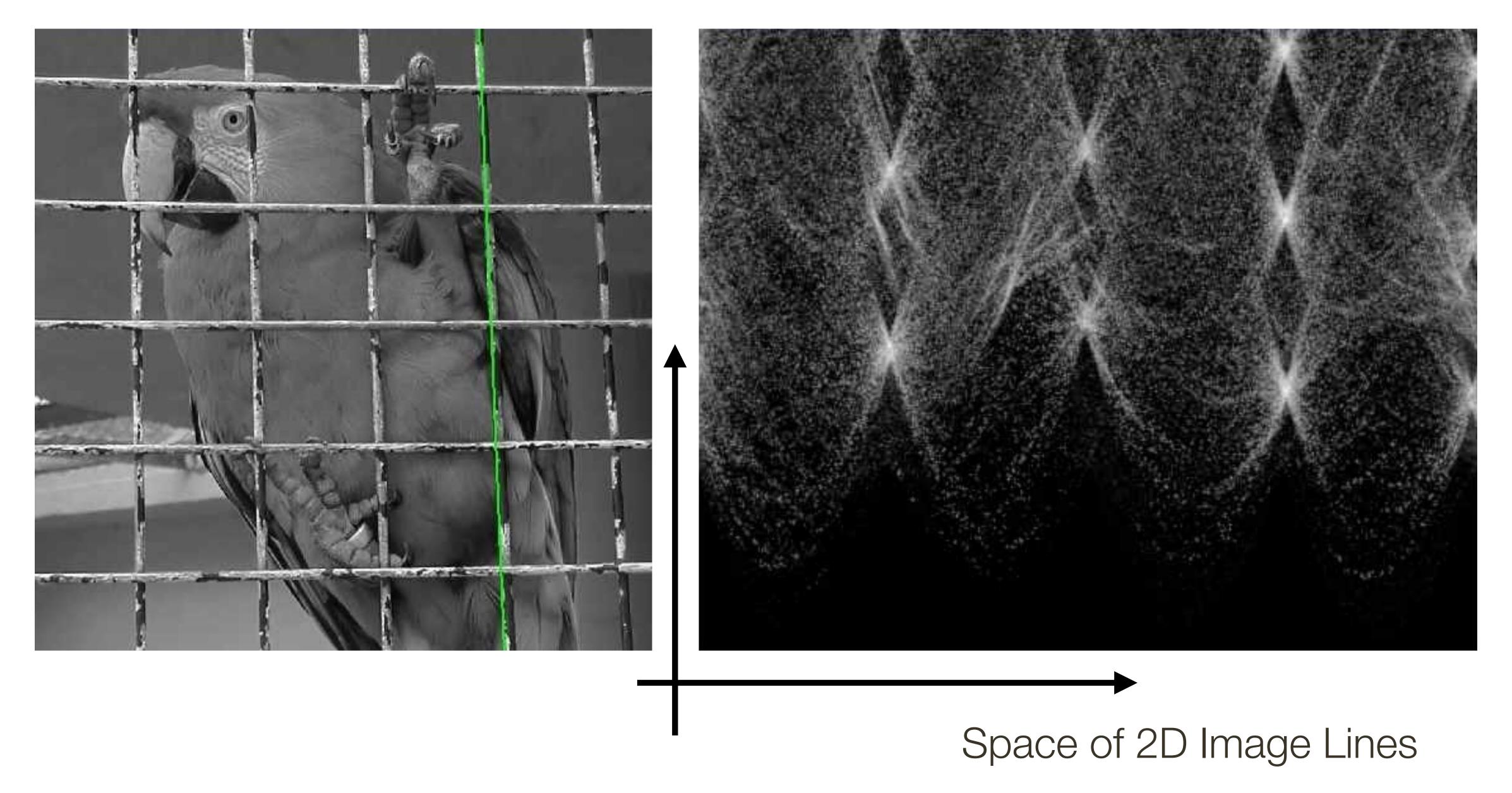
Hough Transform: Motivation



How to find lines in this image?

Hough Transform: Motivation

Votes / Probability Distribution



Hough Transform

Idea of Hough transform:

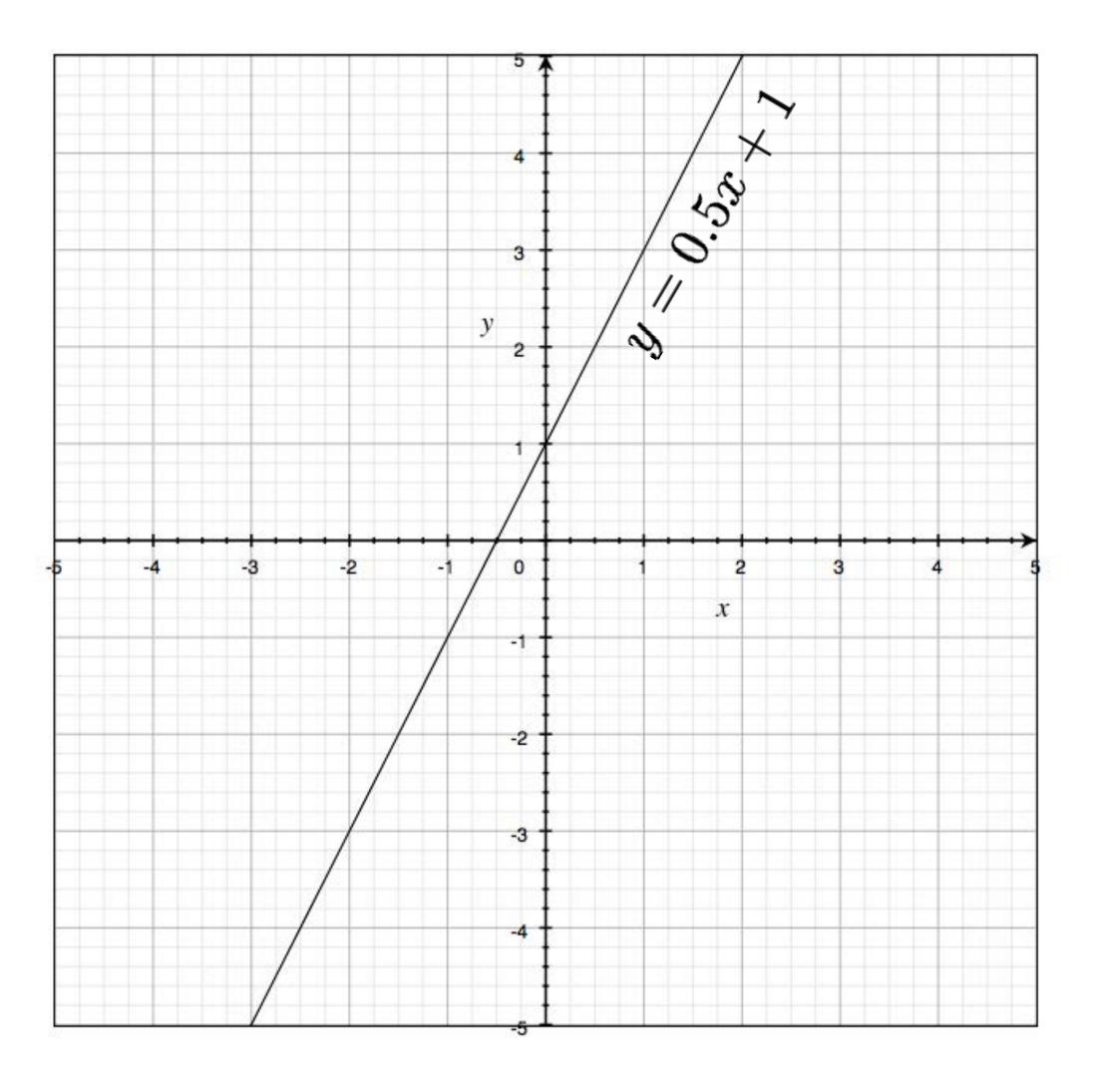
- For each token / data point vote for all models to which it could belong
- Return models that get many votes / distribution of possible models

Example: For each point, vote for all lines that could pass through it; the true lines will pass through many points and so receive many votes

c.f. **RANSAC** which optimizes a **single hypothesis** by maximizing the number of inliers (though modifications exist to find multiple instances of a model)

Lines: Slope intercept form

$$y=mx+b$$
slope y-intercept



Hough Transform: Image and Parameter Space

variables
$$y = mx + b$$
 $y = mx + b$ parameters

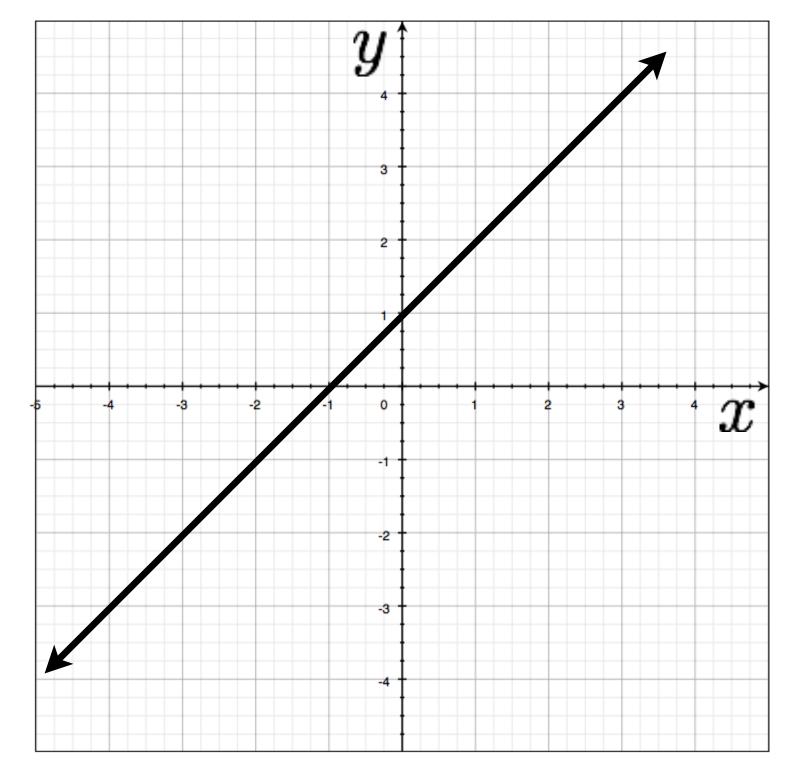


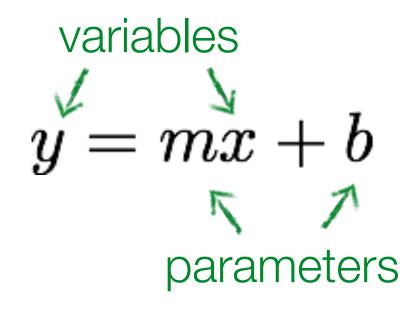
Image space

Hough Transform: Image and Parameter Space

a line

becomes a

point



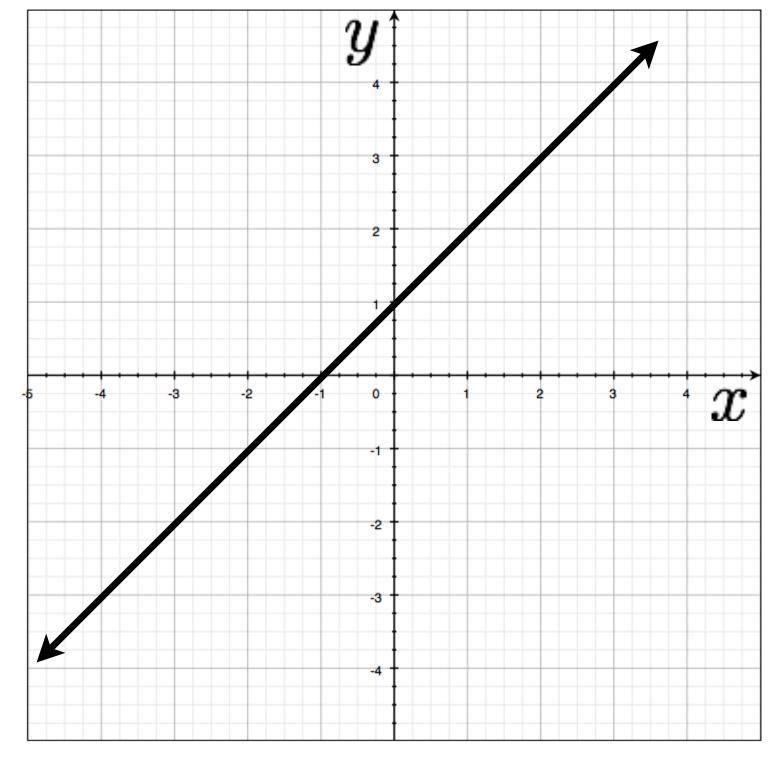
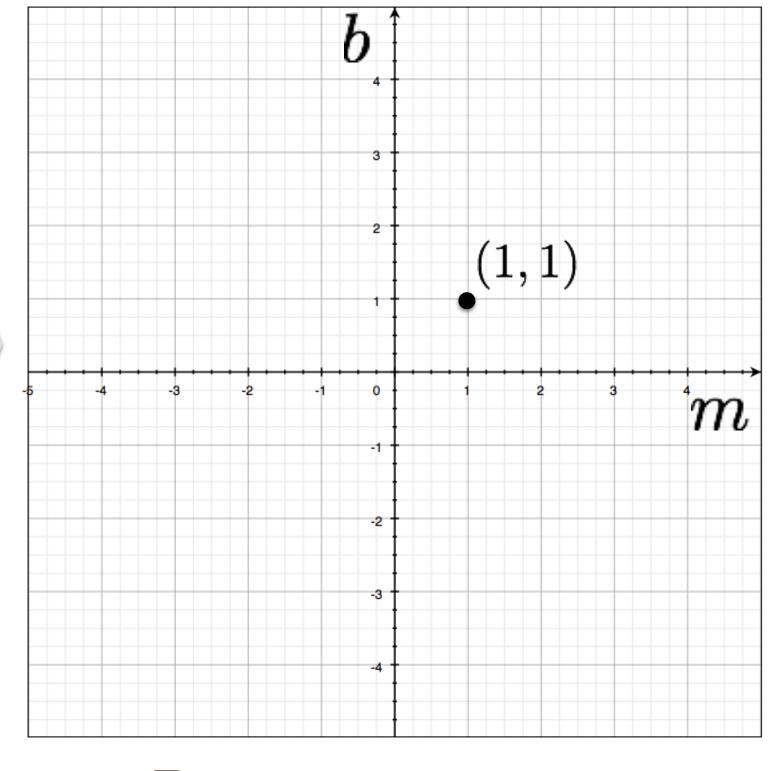


Image space

variables

$$y - mx = b$$

parameters



Parameter space

Hough Transform: Image and Parameter Space

variables
$$y = mx + b$$
 $y = mx + b$ parameters

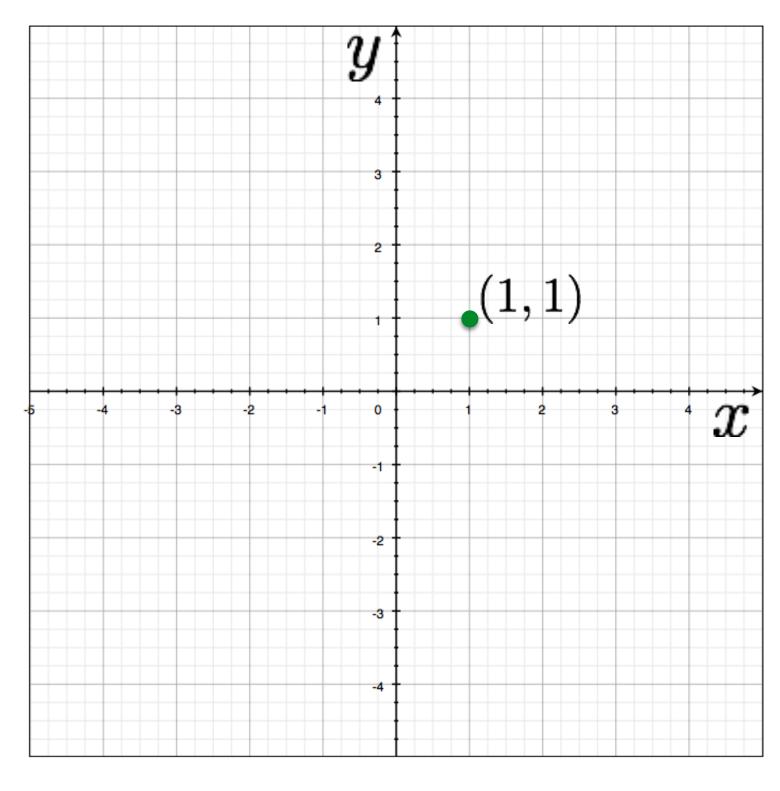


Image space

What would a **point** in image space become in **parameter space**?

variables
$$y = mx + b$$
 $y = mx + b$ parameters

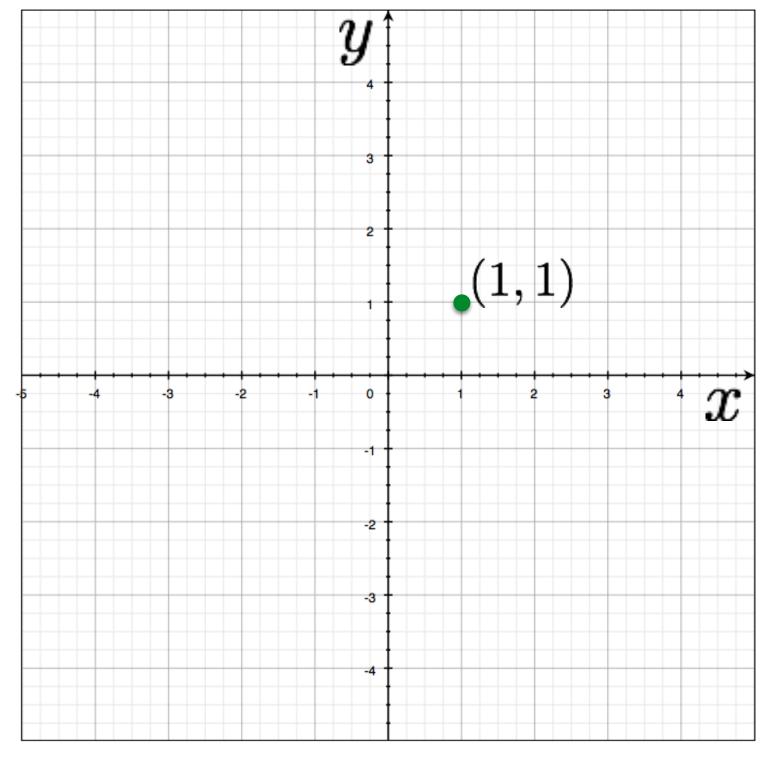
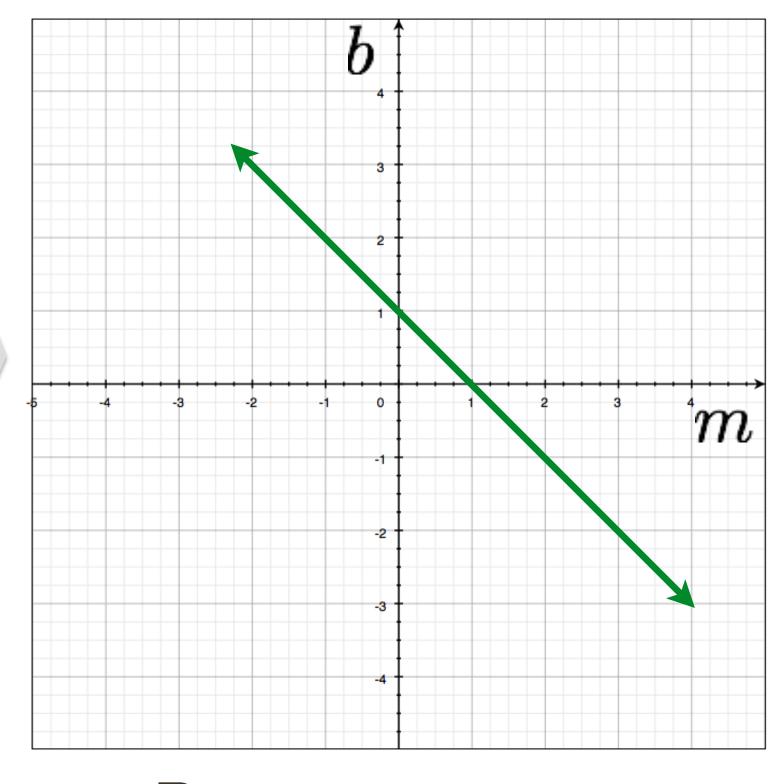


Image space

variables

$$y - mx = b$$

parameters



a point

becomes a

line

Parameter space

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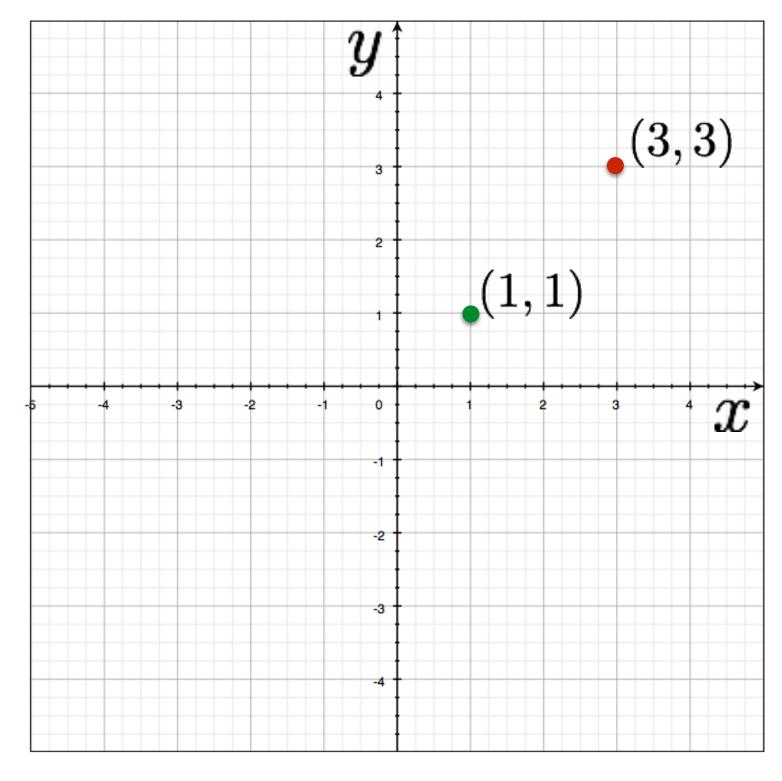
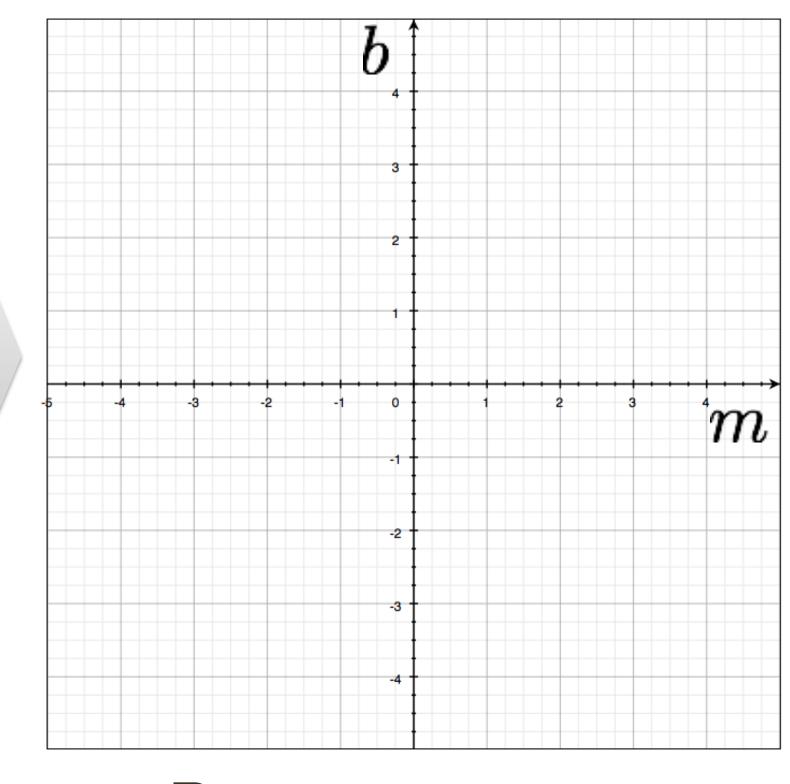


Image space

variables

$$y - mx = b$$

parameters



two

points?

Parameter space

variables
$$y = mx + b$$
 $y = mx + b$ parameters

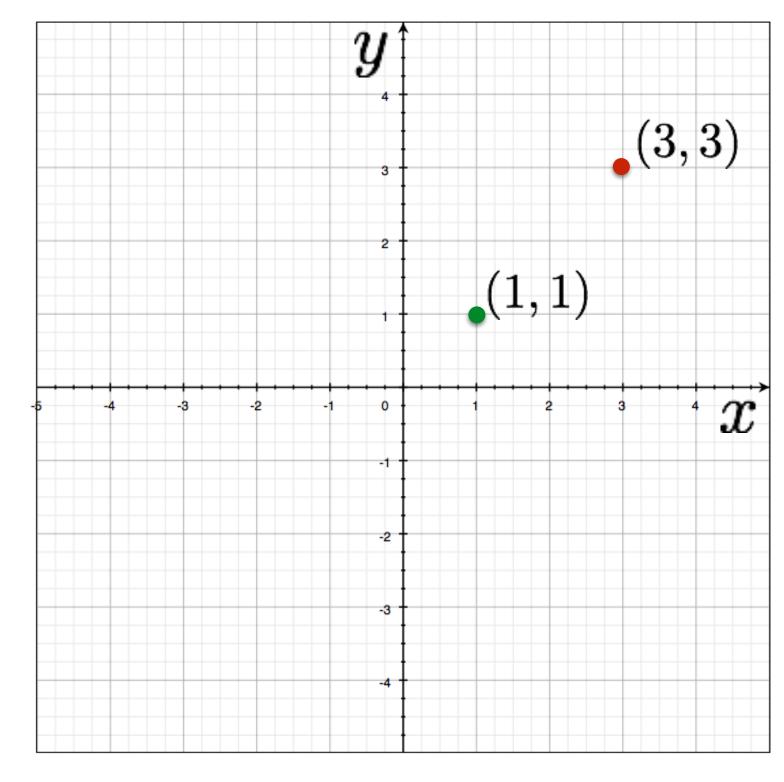
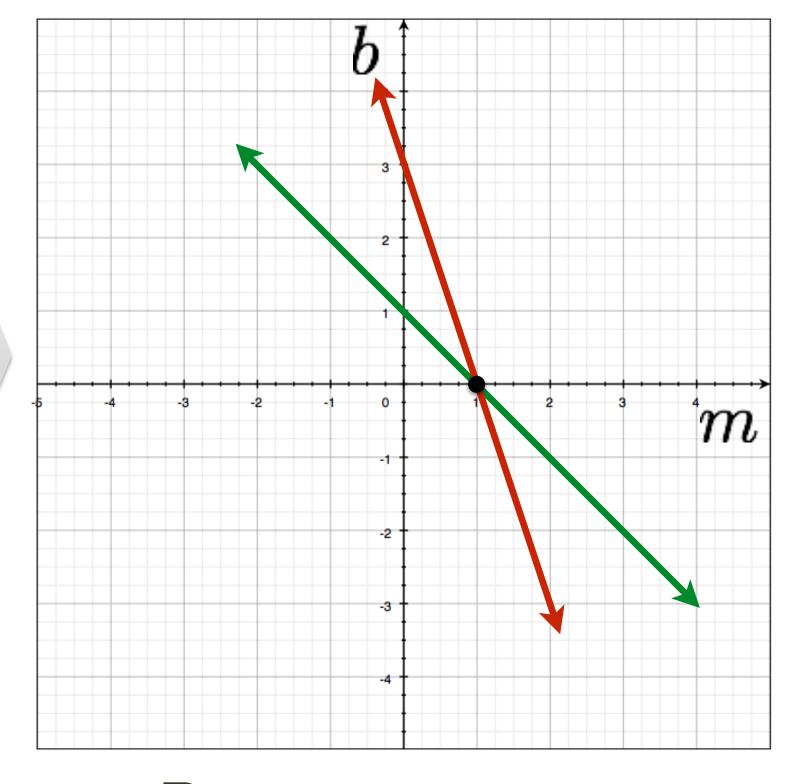


Image space

variables

$$y - mx = b$$

parameters



two

points?

Parameter space

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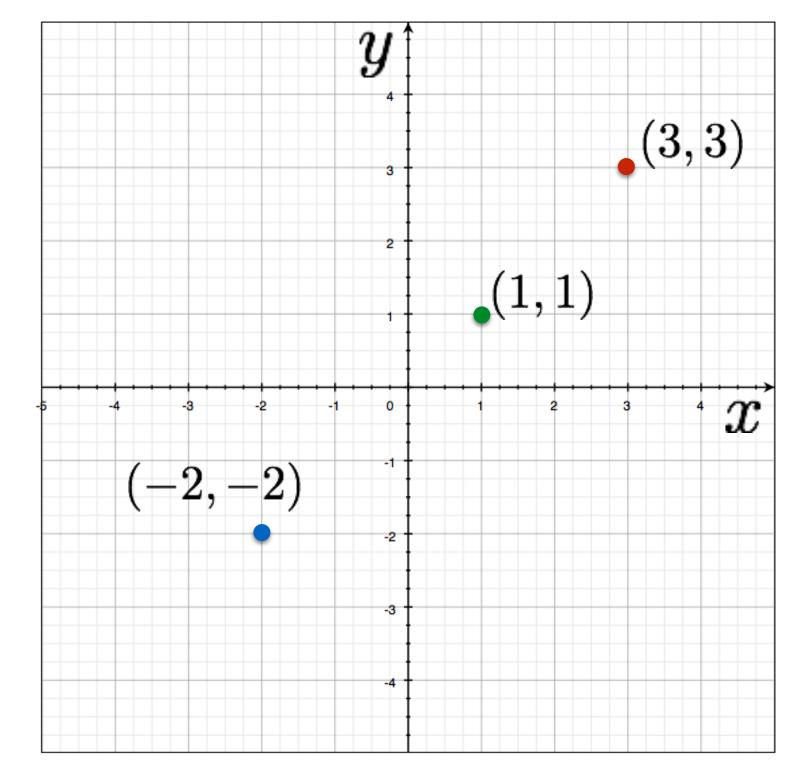
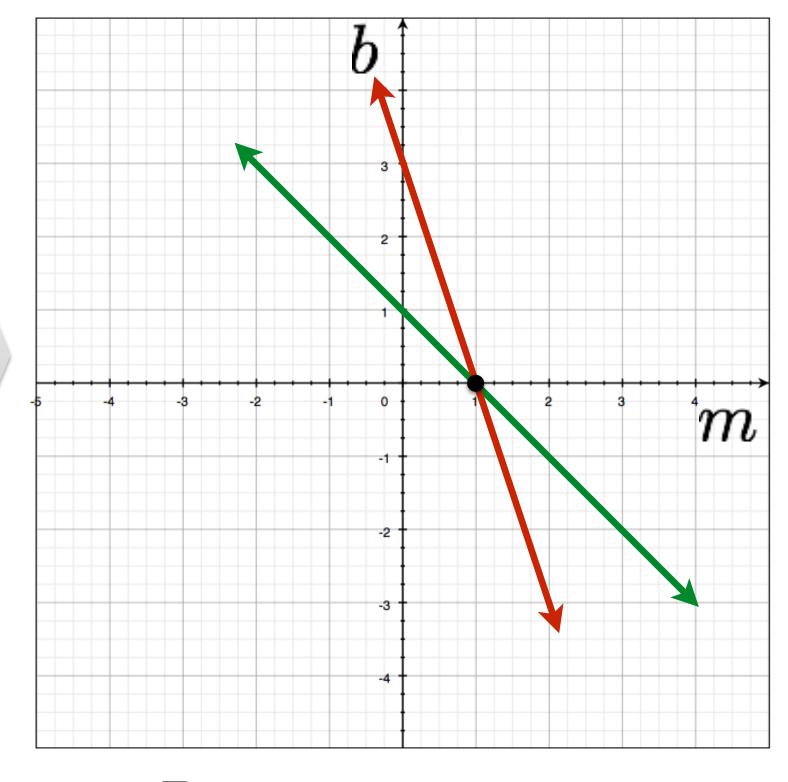


Image space

variables

$$y - mx = b$$
 \uparrow

parameters



three

points?

Parameter space

variables
$$y = mx + b$$
 $y = mx + b$ parameters

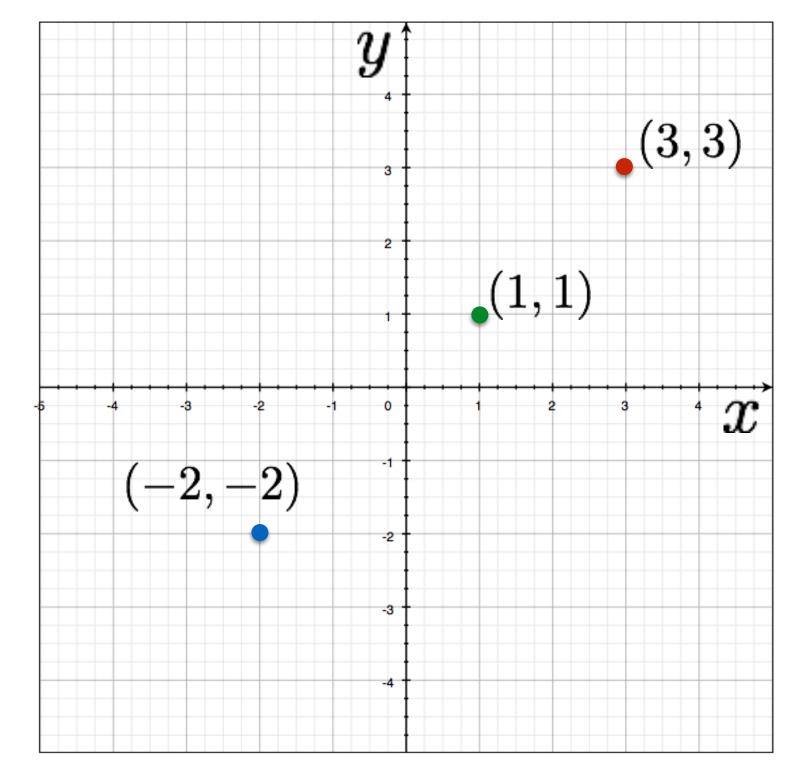
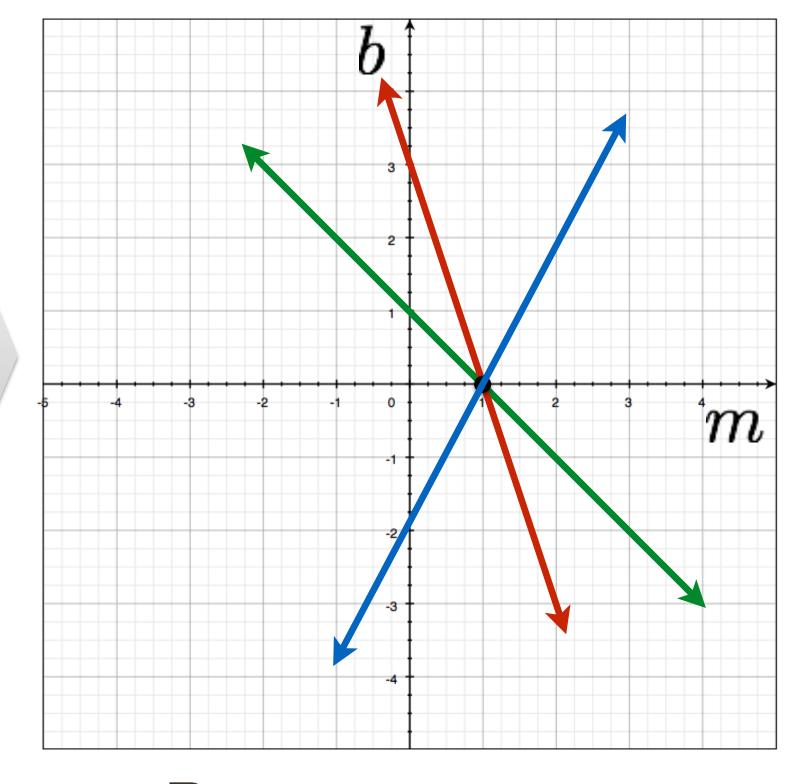


Image space

variables

$$y - mx = b$$
 \uparrow

parameters



three

points?

Parameter space

variables
$$y = mx + b$$
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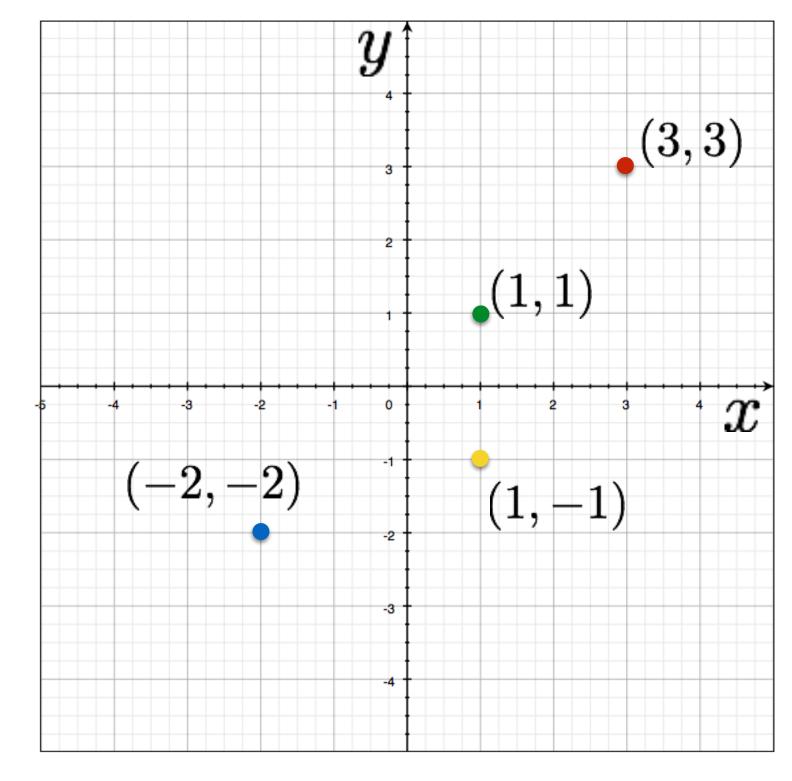
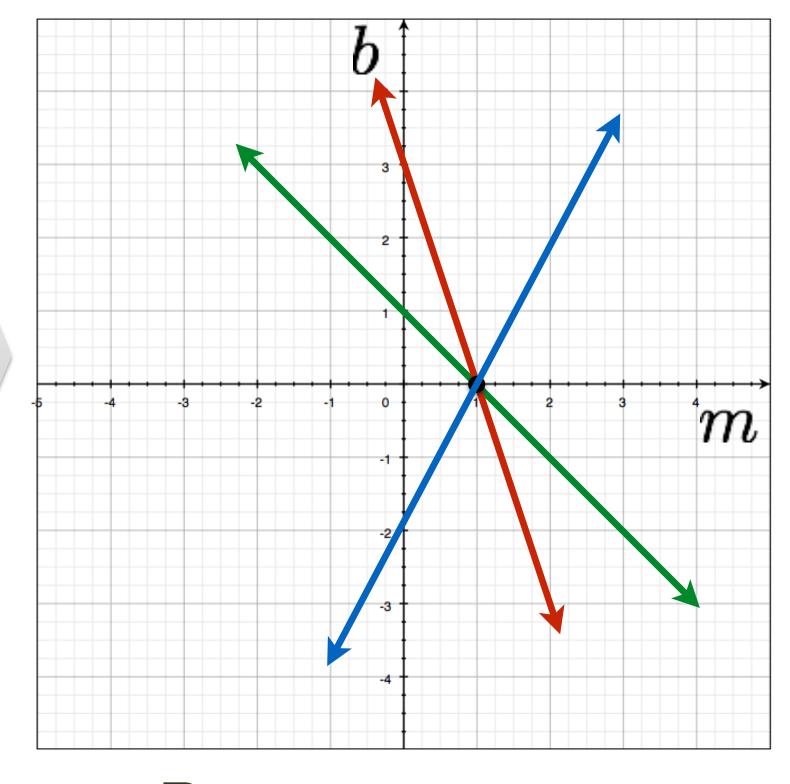


Image space

variables

$$y - mx = b$$
 \uparrow

parameters



four

points?

Parameter space

variables
$$y = mx + b$$
 $y = mx + b$ parameters

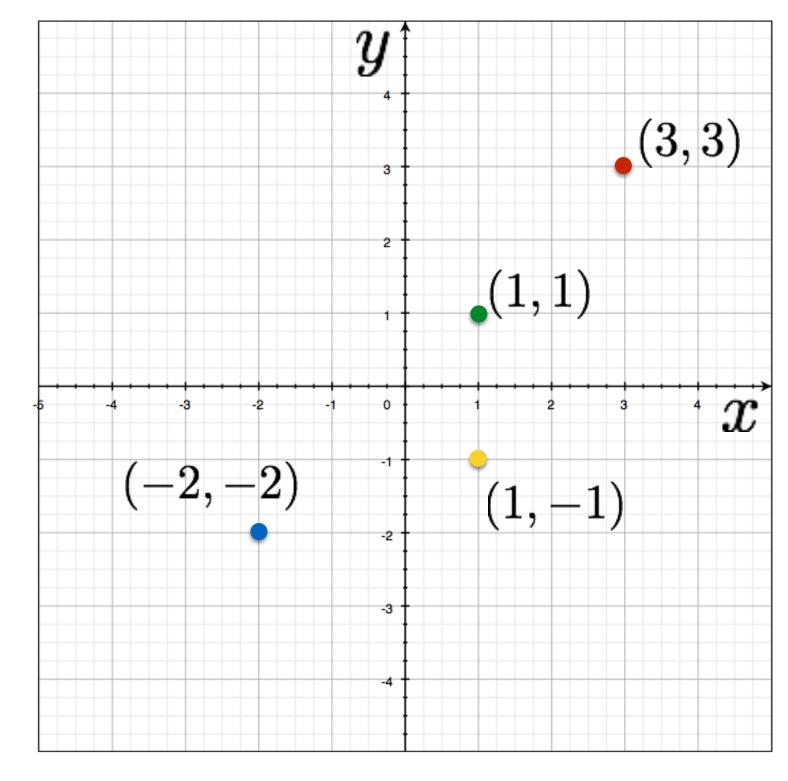
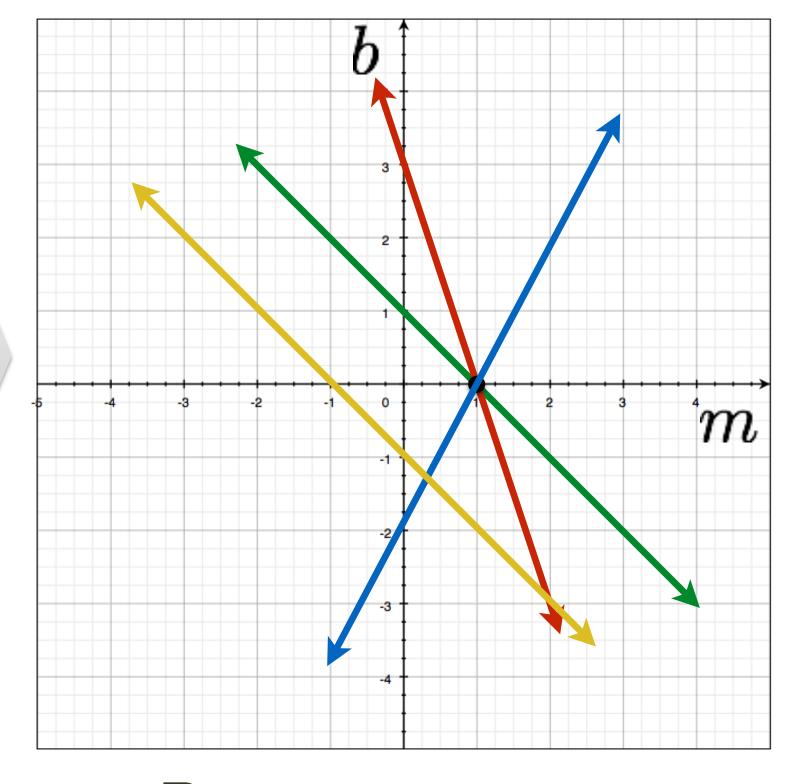


Image space

variables

$$y - mx = b$$
 \uparrow

parameters

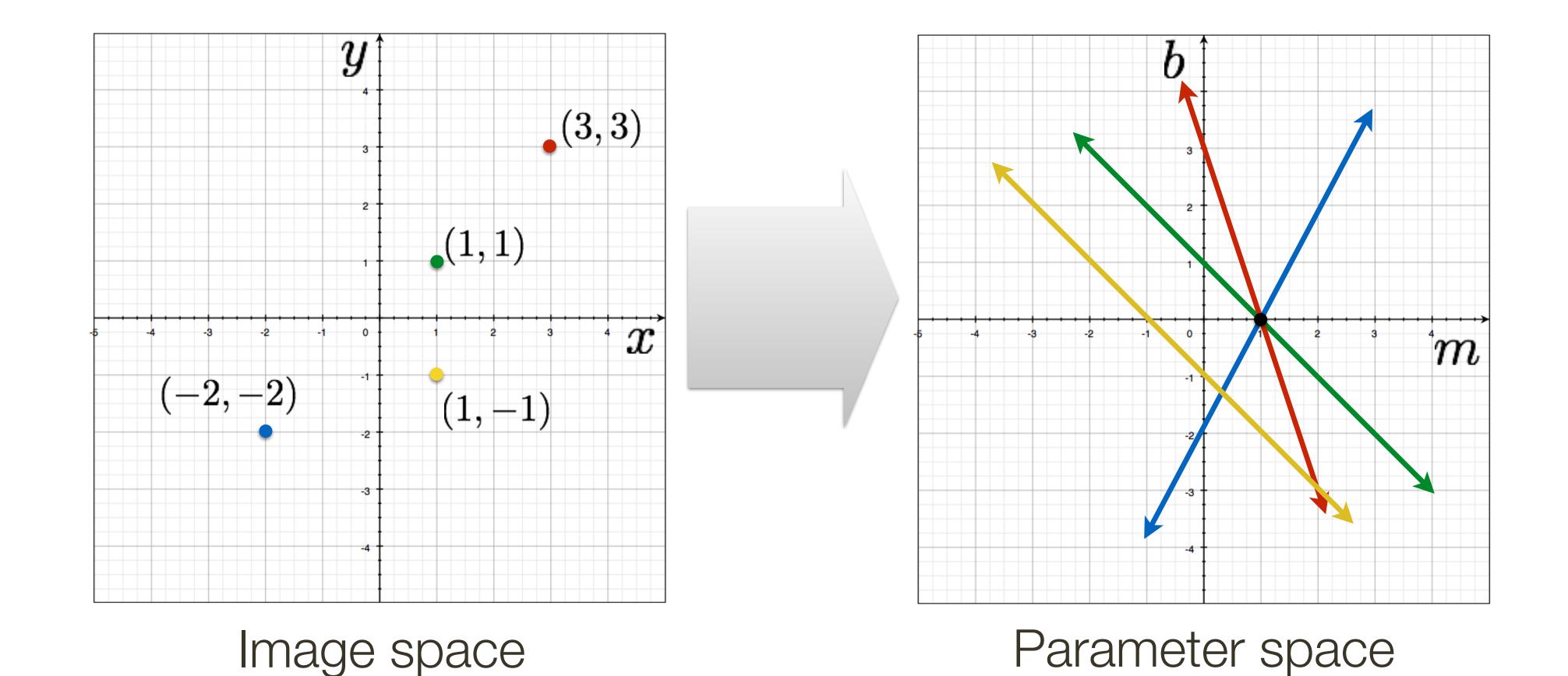


four

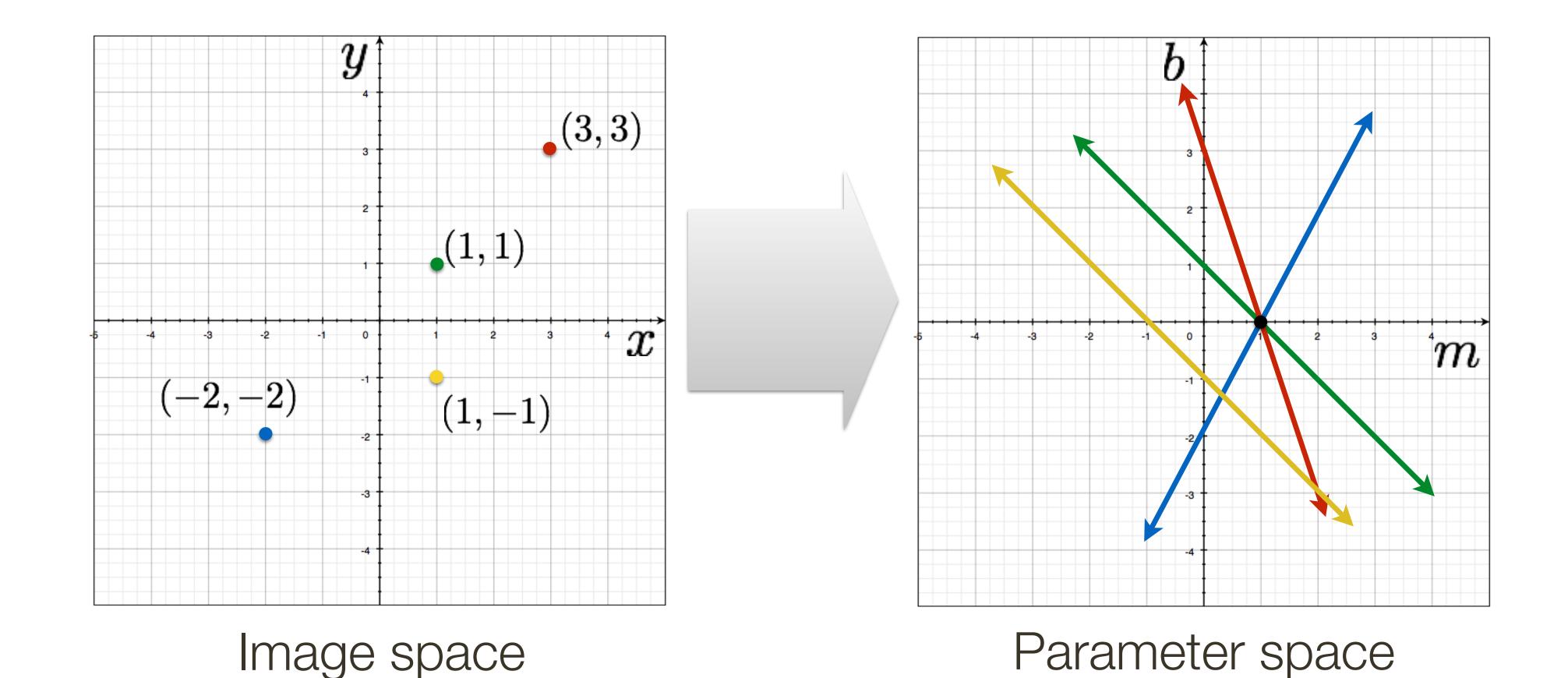
points?

Parameter space

How would you find the best fitting line?



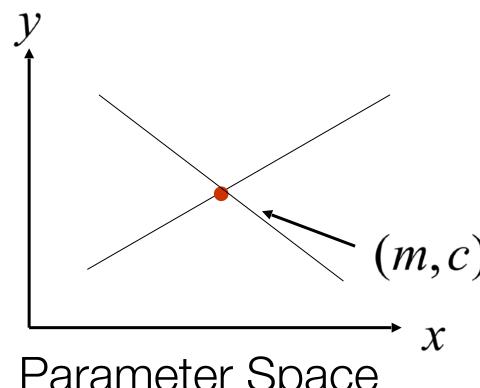
Is this method robust to measurement noise? clutter?



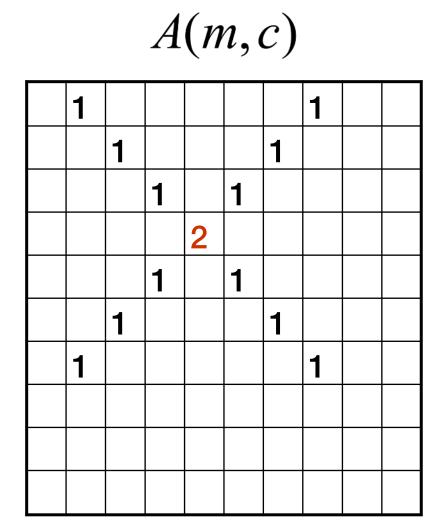
Line Detection by Hough Transform

Algorithm:

- 1. Quantize Parameter Space(m,c)
- 2. Create Accumulator Array A(m,c)
- 3.Set $A(m,c) = 0 \quad \forall m,c$
- 4. For each image edge (x_i, y_i) For each element in A(m,c)If (m,c) lies on the line: $c = -x_i m + y_i$ Increment A(m,c) = A(m,c) + 1
- 5. Find local maxima in A(m,c)

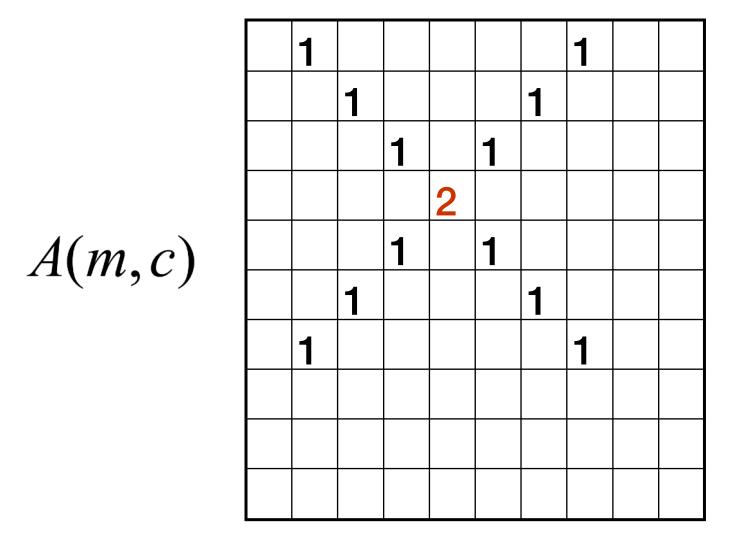


Parameter Space



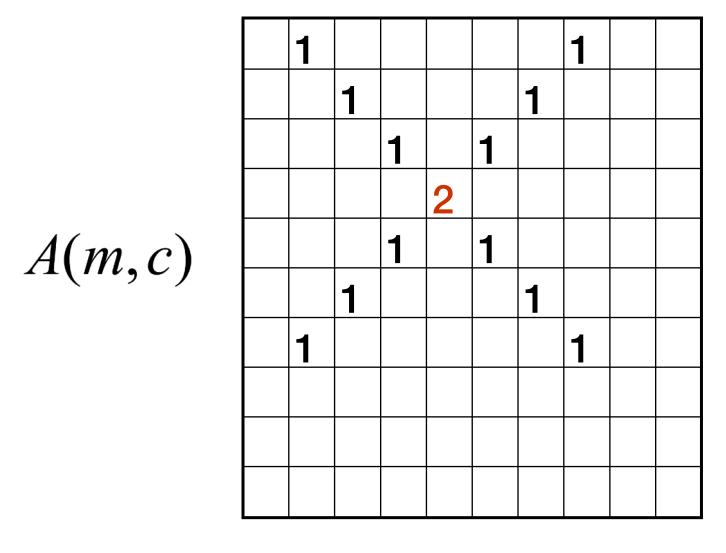
Problems with Parametrization

How big does the accumulator need to be for the parameterization (m,c)?



Problems with Parametrization

How big does the accumulator need to be for the parameterization (m,c)?



The space of m is huge!

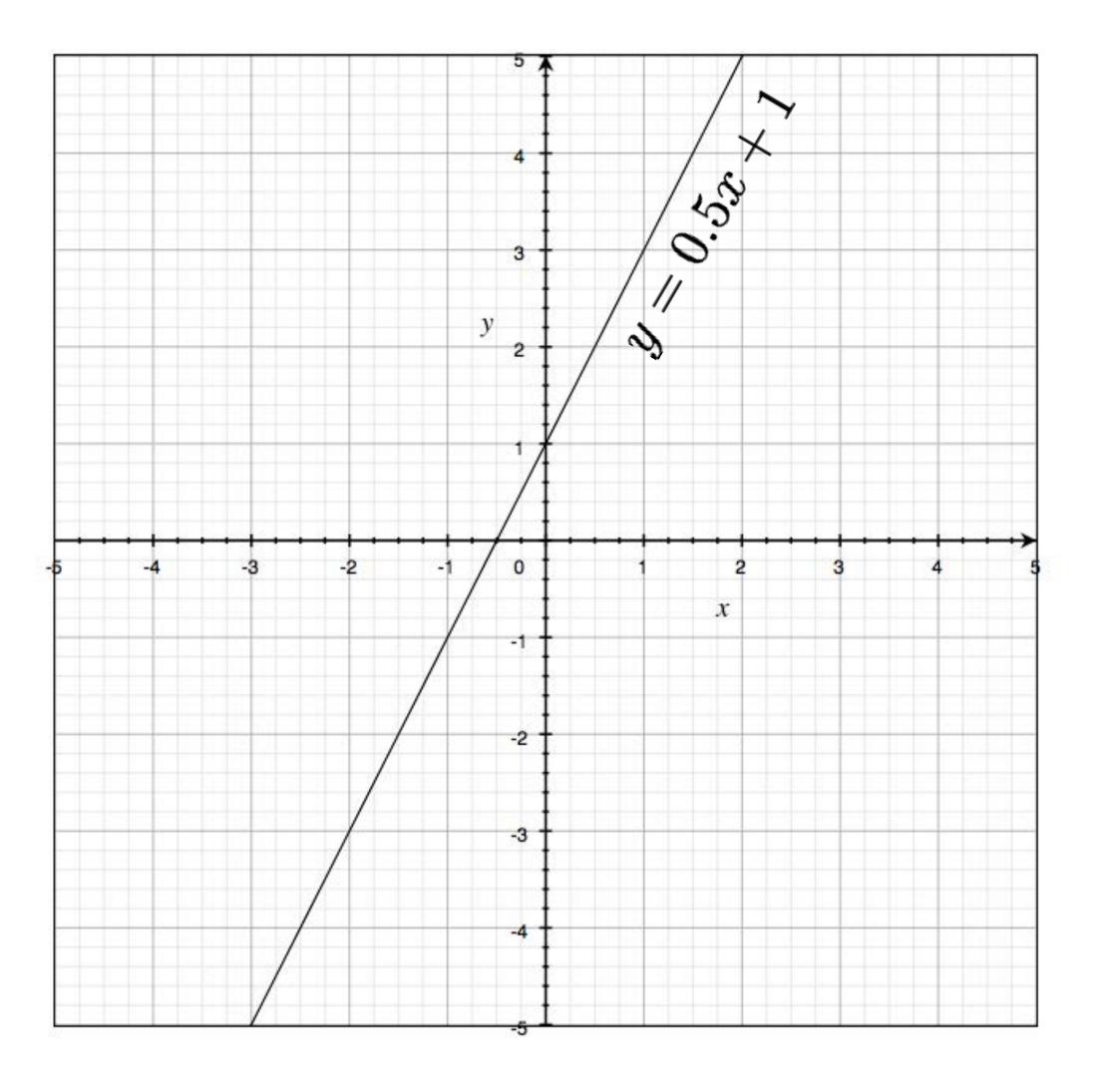
The space of c is huge!

$$-\infty \leq m \leq \infty$$

$$-\infty \leq c \leq \infty$$

Lines: Slope intercept form

$$y=mx+b$$
slope y-intercept



Lines: Normal form

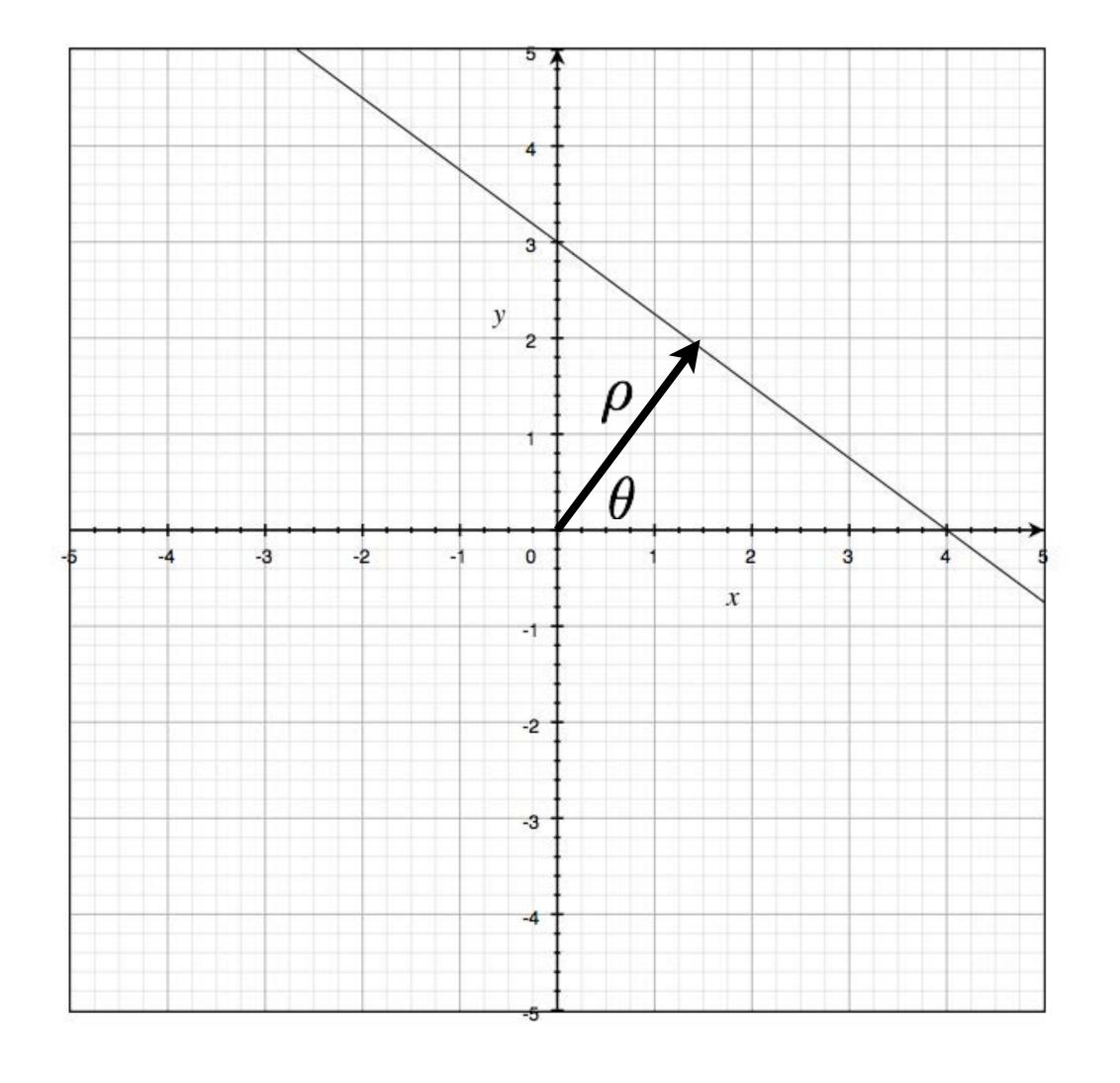
$$x\cos(\theta) + y\sin(\theta) = \rho$$

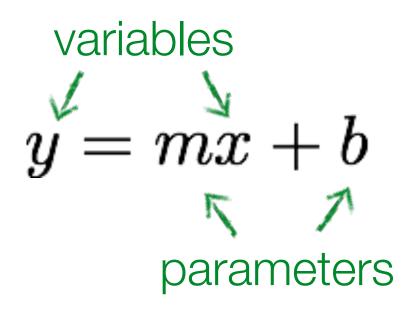
Forsyth/Ponce convention

$$x\cos(\theta) + y\sin(\theta) + r = 0$$

$$r \ge 0$$

$$0 \le \theta \le 2\pi$$





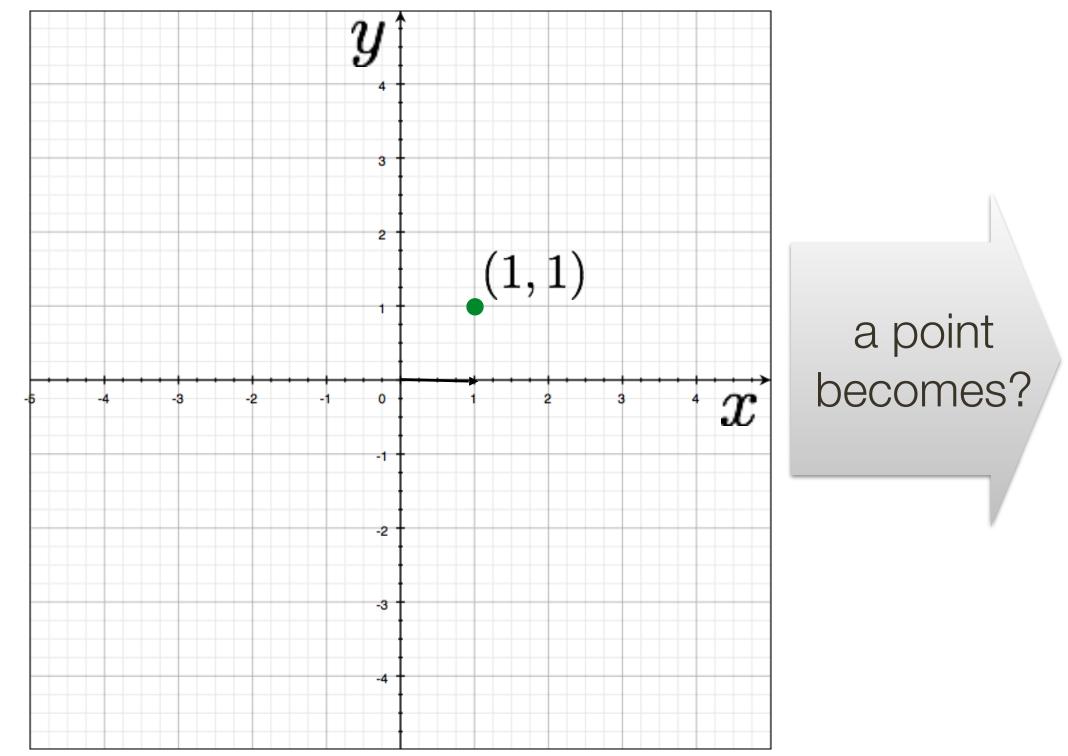
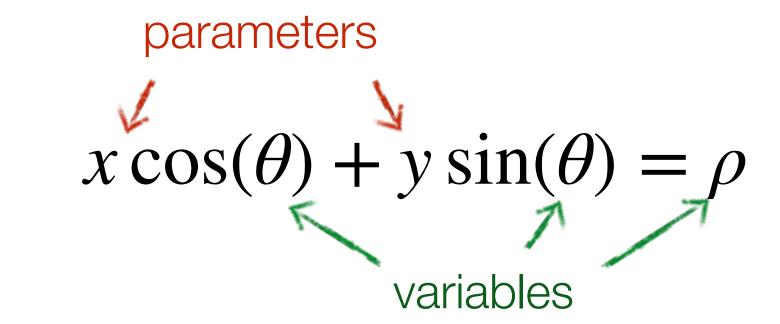
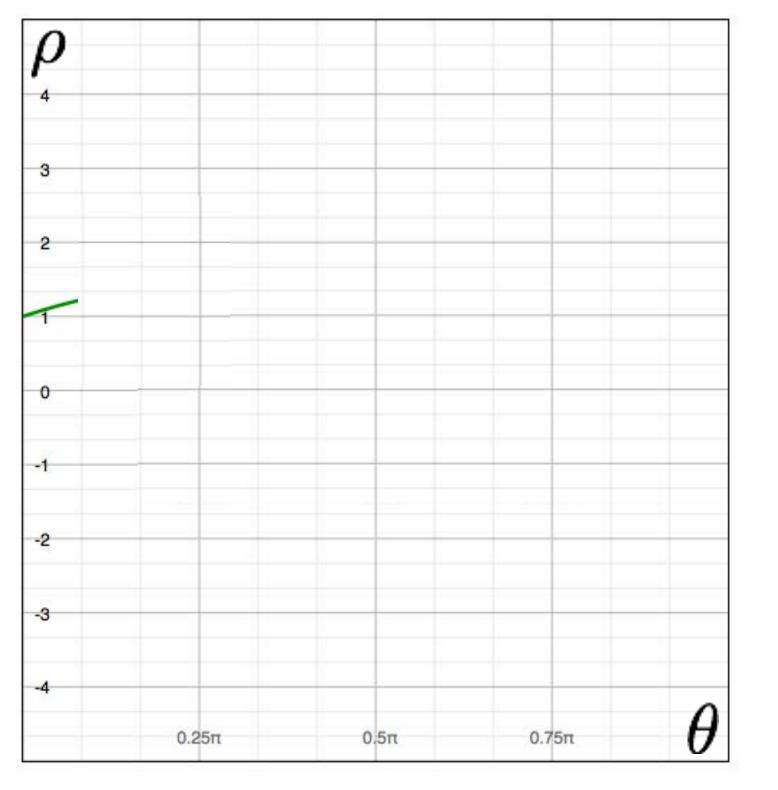
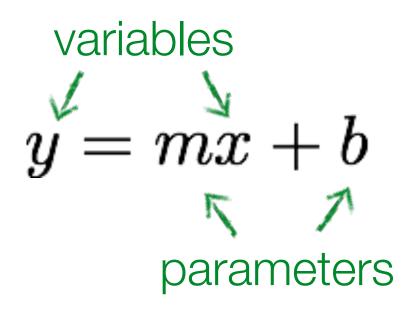


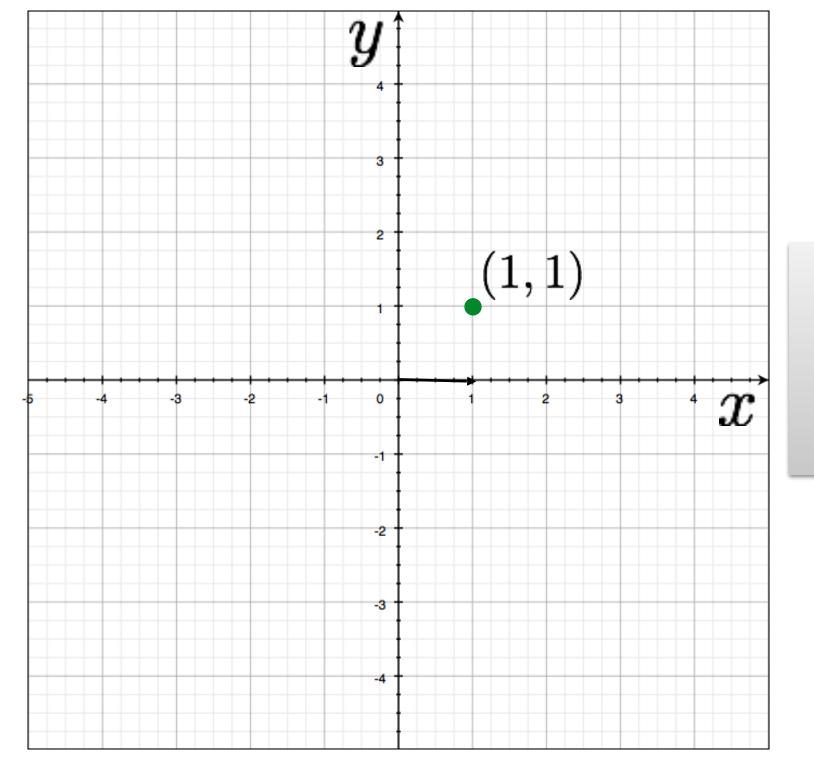
Image space





Parameter space





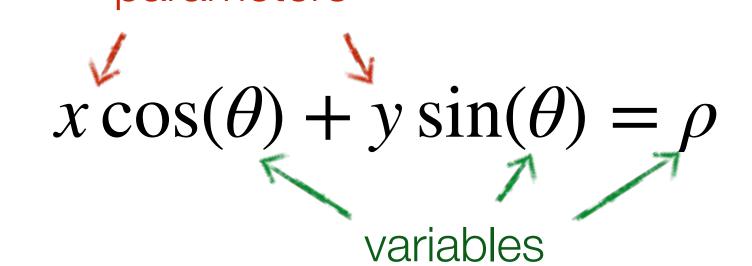
a point

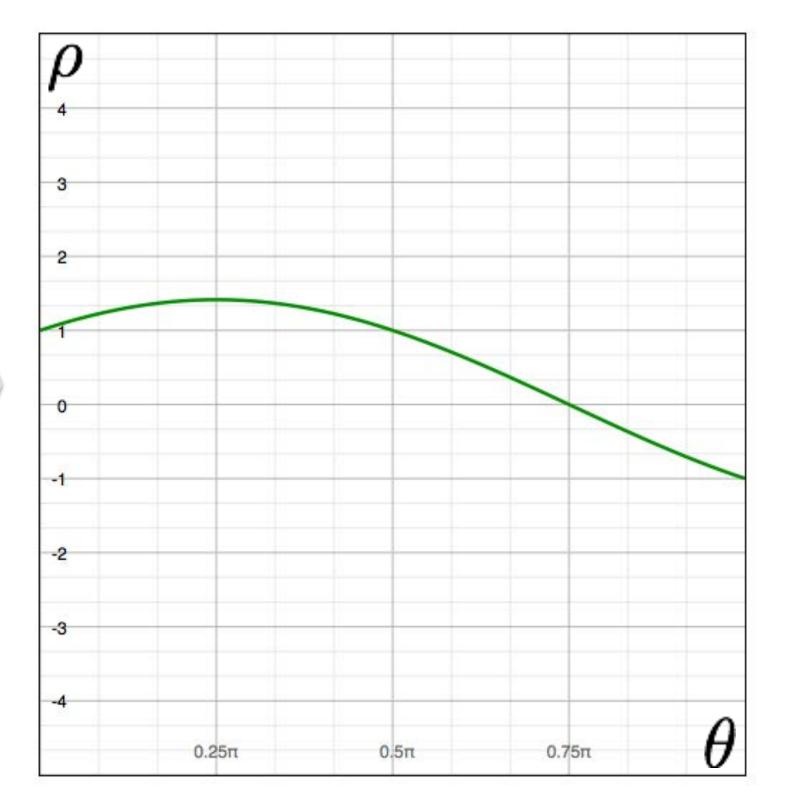
becomes

a wave

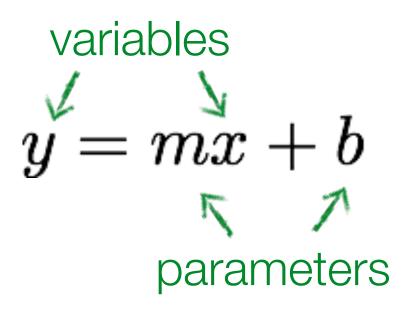
Image space

parameters





Parameter space



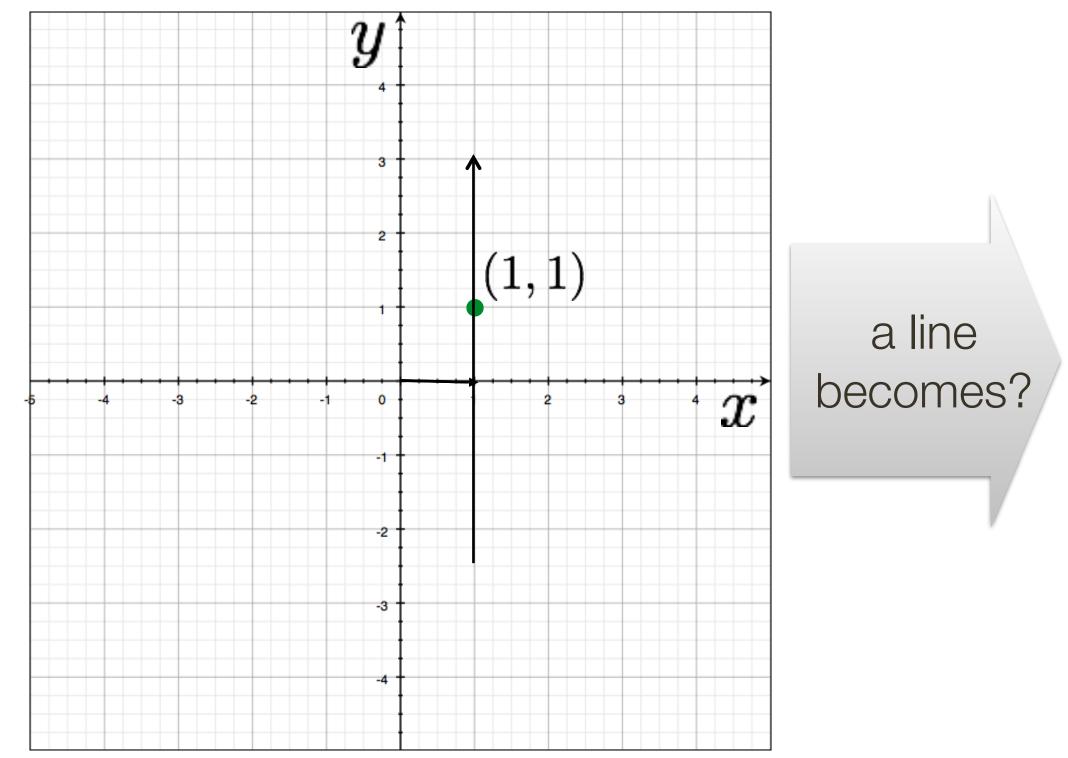
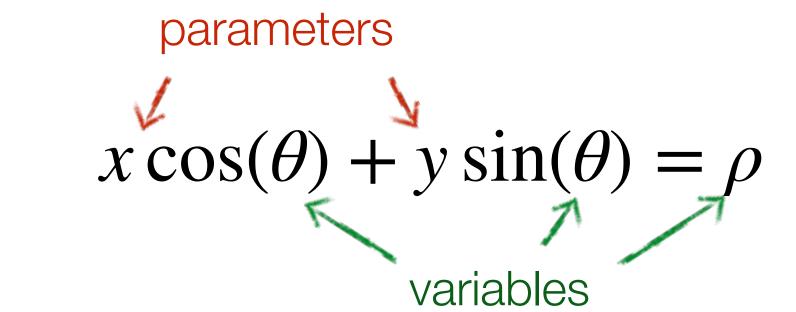
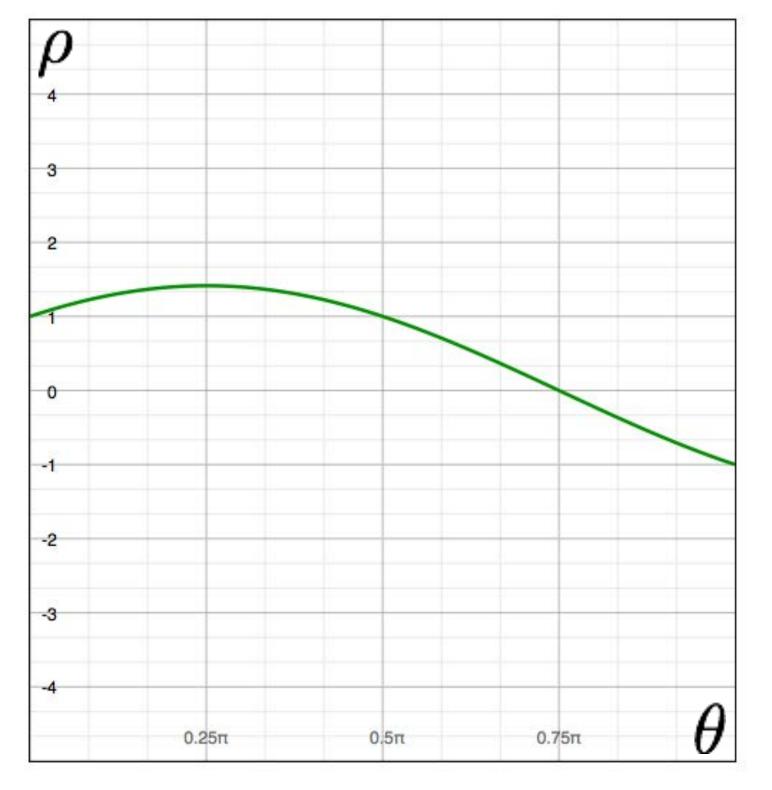
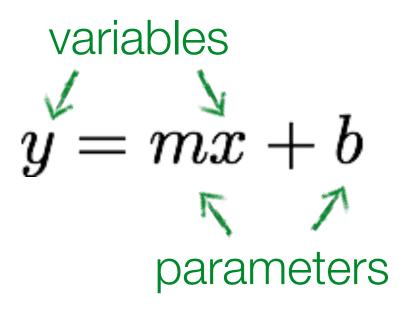


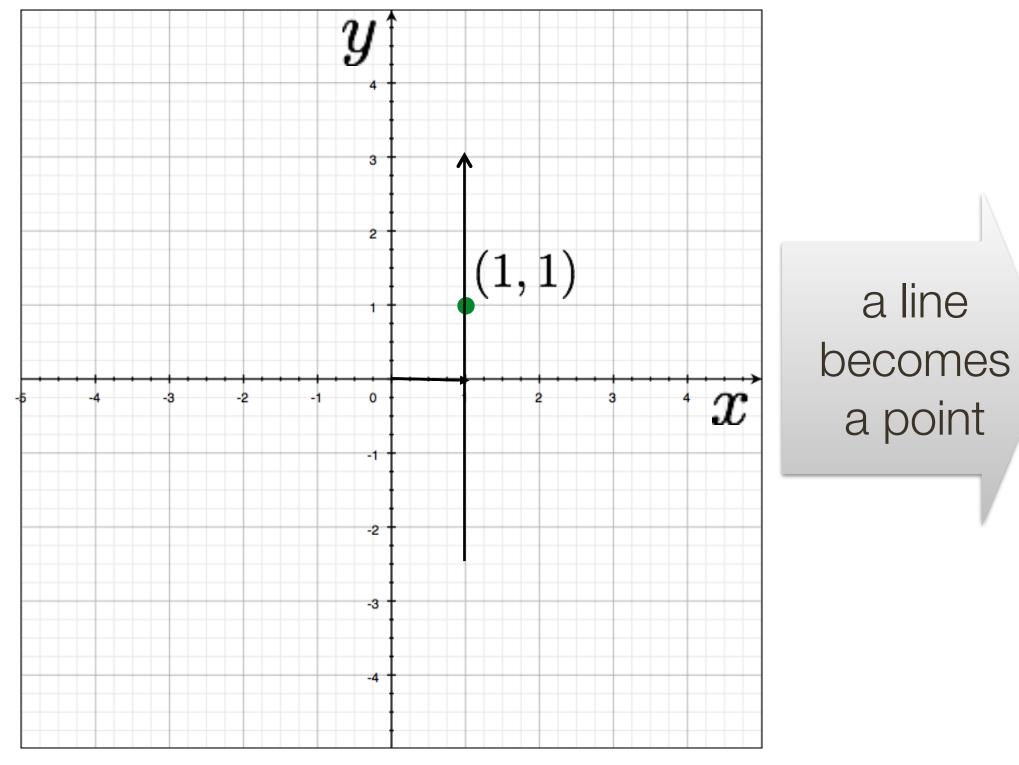
Image space





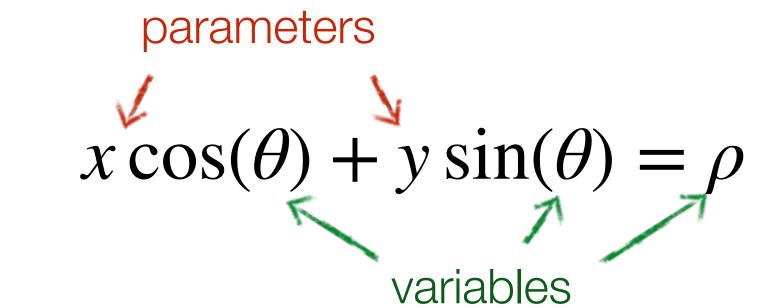
Parameter space

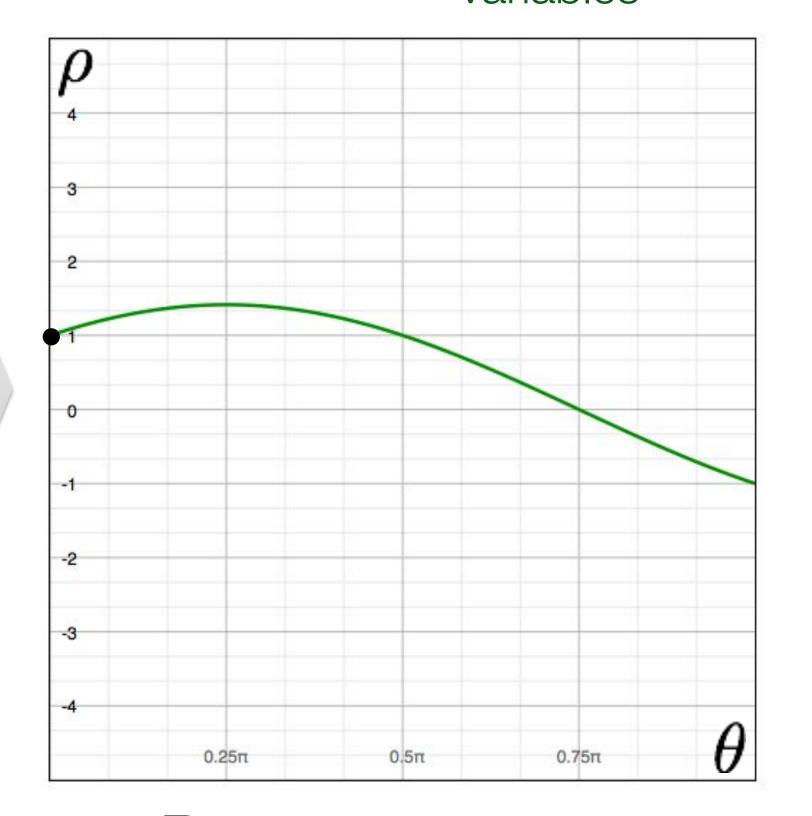




a line

Image space





Parameter space

Hough Transform for Lines (switching to books notation)

Idea: Each point votes for the lines that pass through it

— A line is the set of points, (x, y), such that

$$x\cos(\theta) + y\sin(\theta) = \rho$$

— Different choices of θ , r give different lines

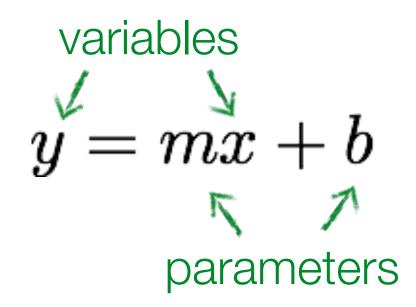
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- Different choices of θ , r give different lines
- For any (x, y) there is a one parameter family of lines through this point. Just let (x, y) be constants and for each value of θ the value of r will be determined
- Each point enters votes for each line in the family
- If there is a line that has lots of votes, that will be the line passing near the points that voted for it



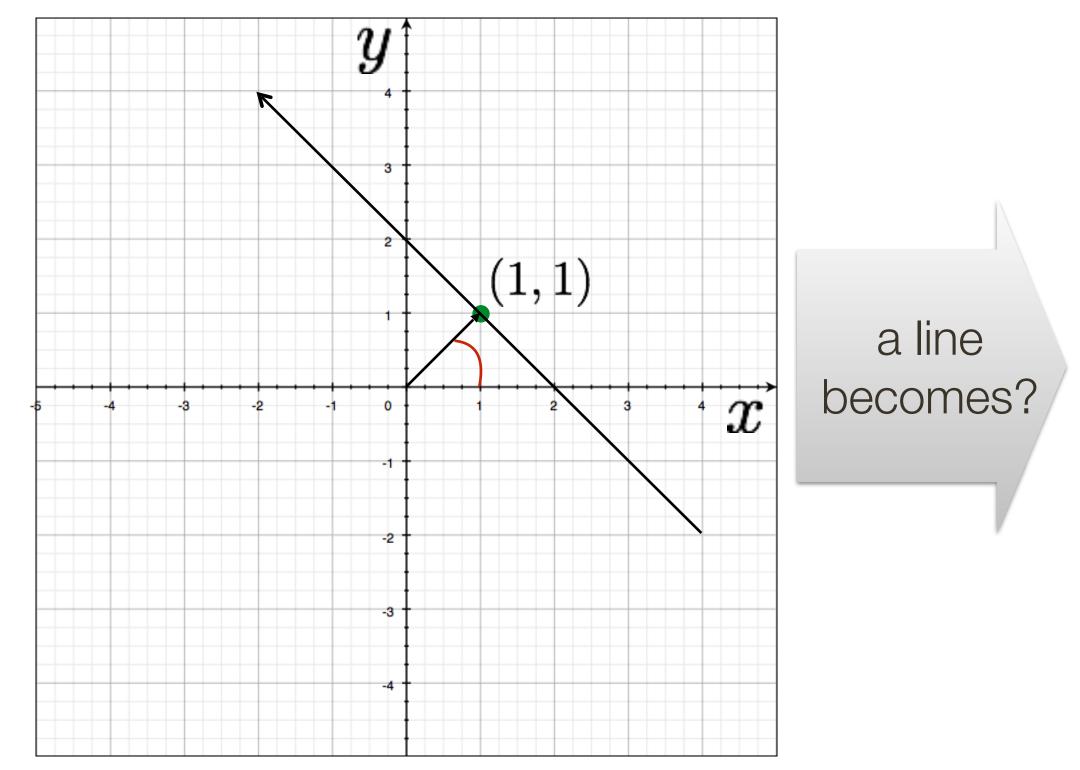
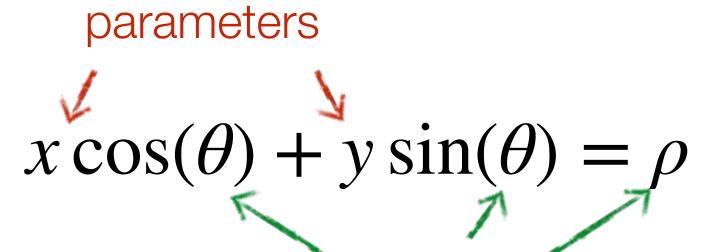
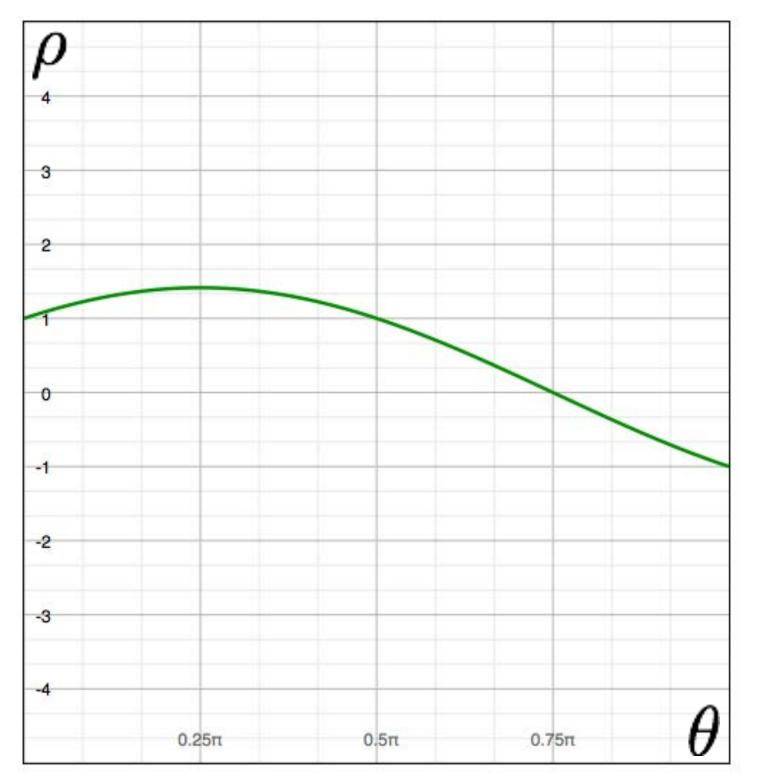


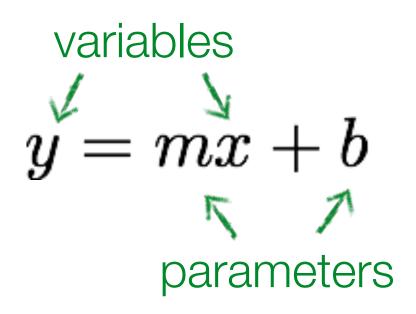
Image space

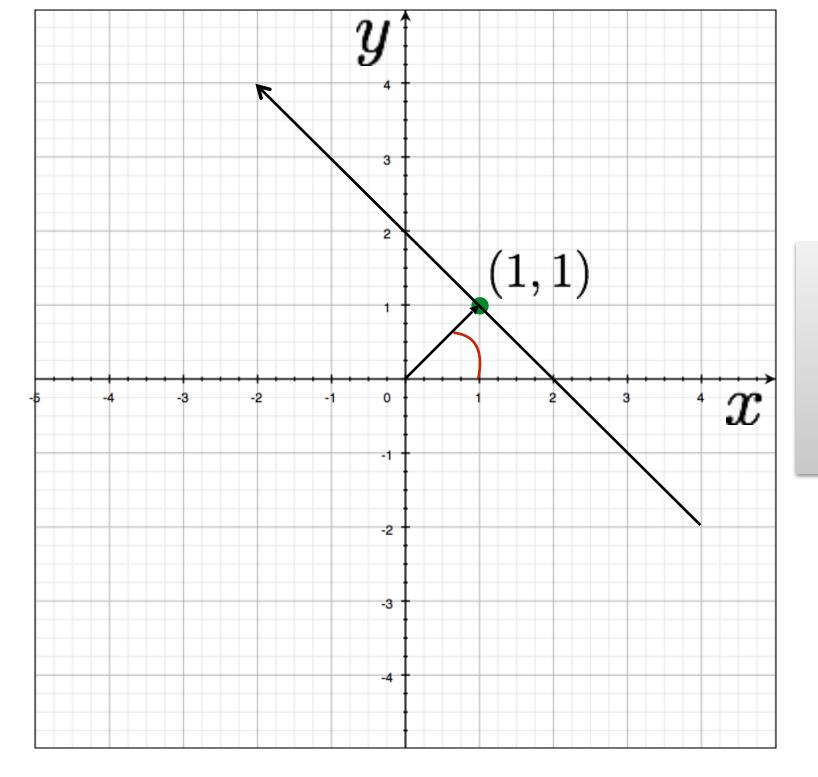


variables



Parameter space



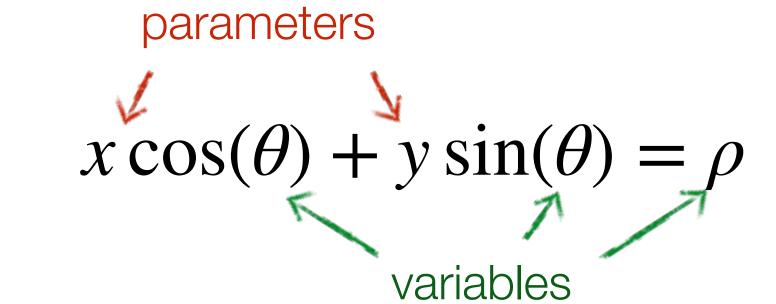


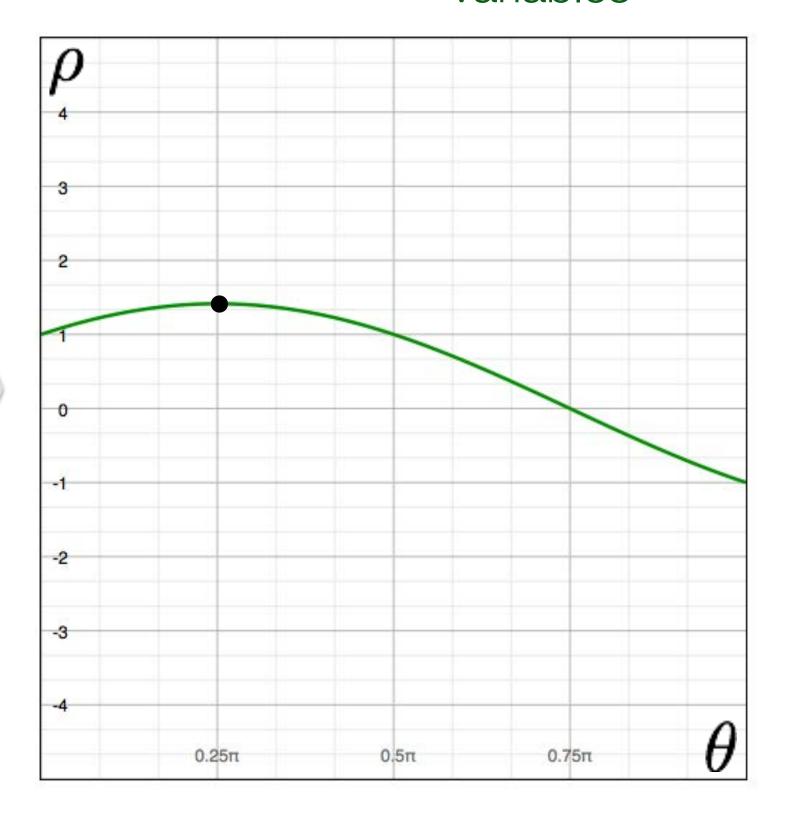
a line

becomes

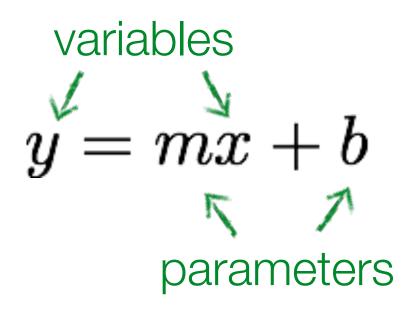
a point

Image space





Parameter space



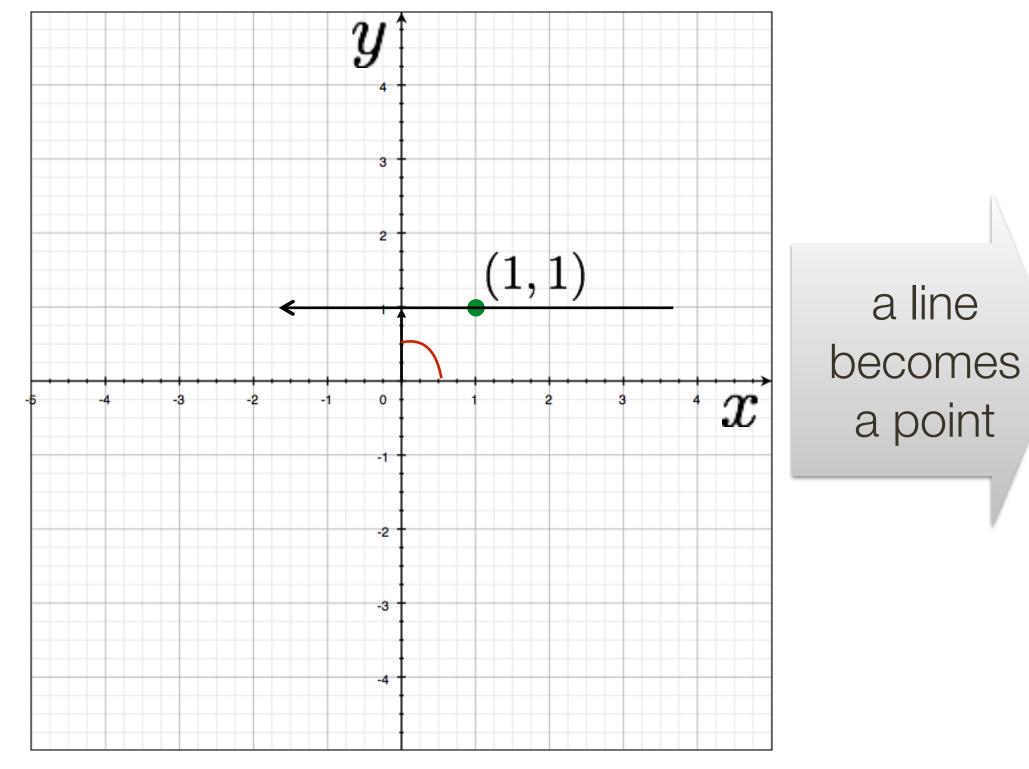
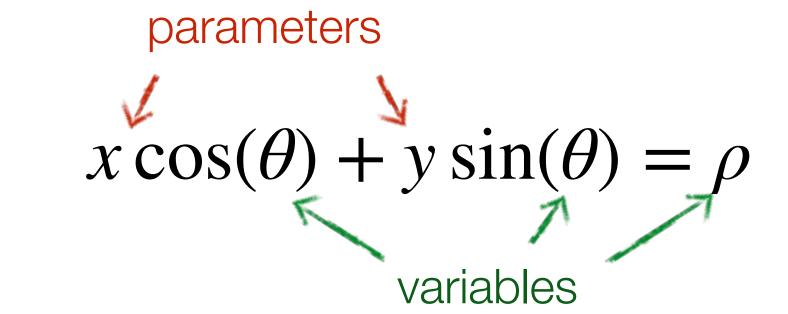
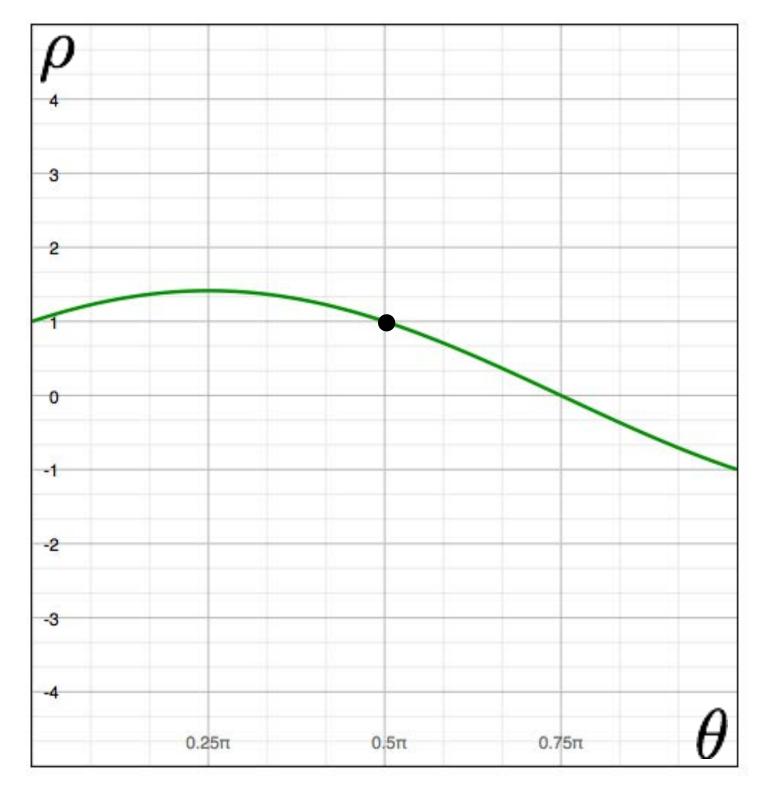
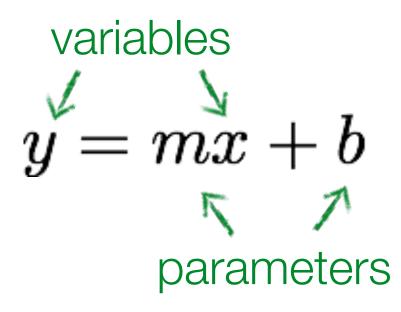


Image space





Parameter space



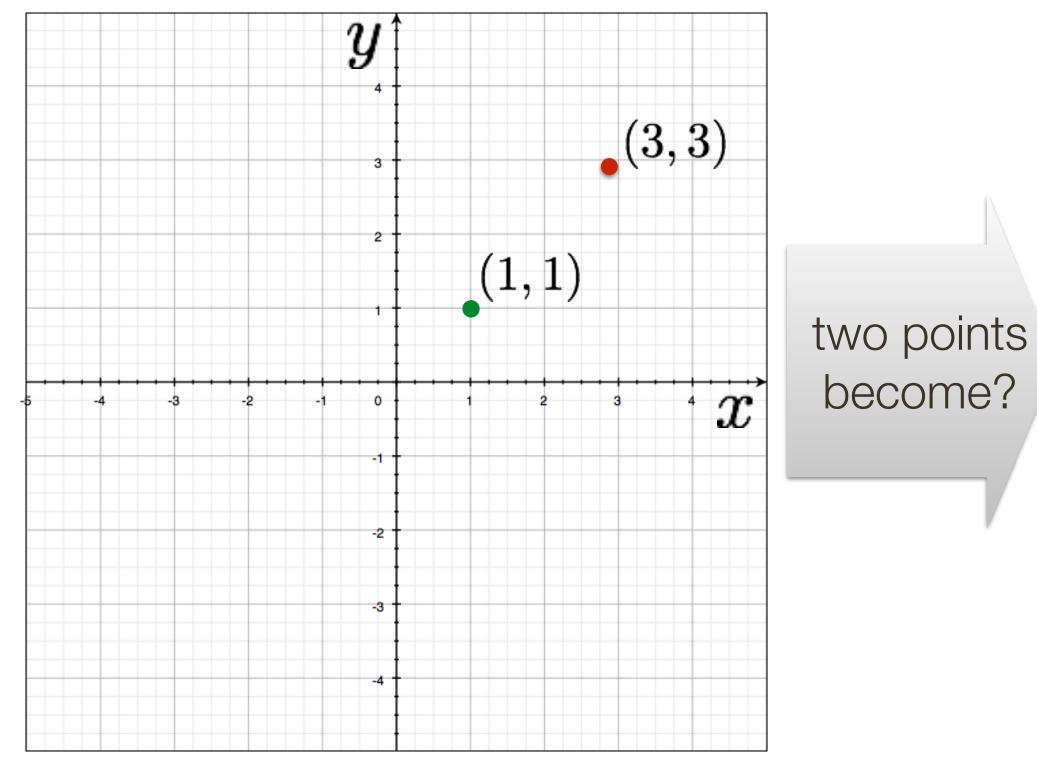
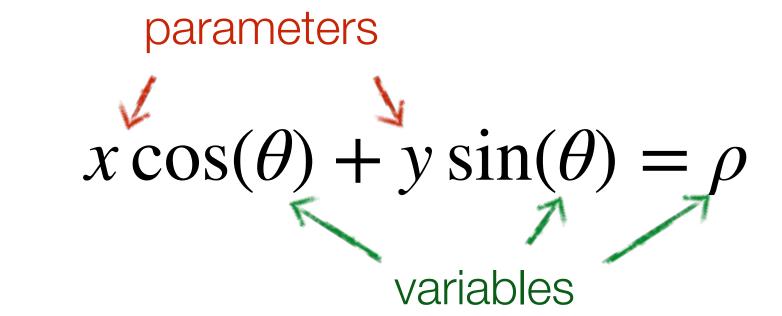
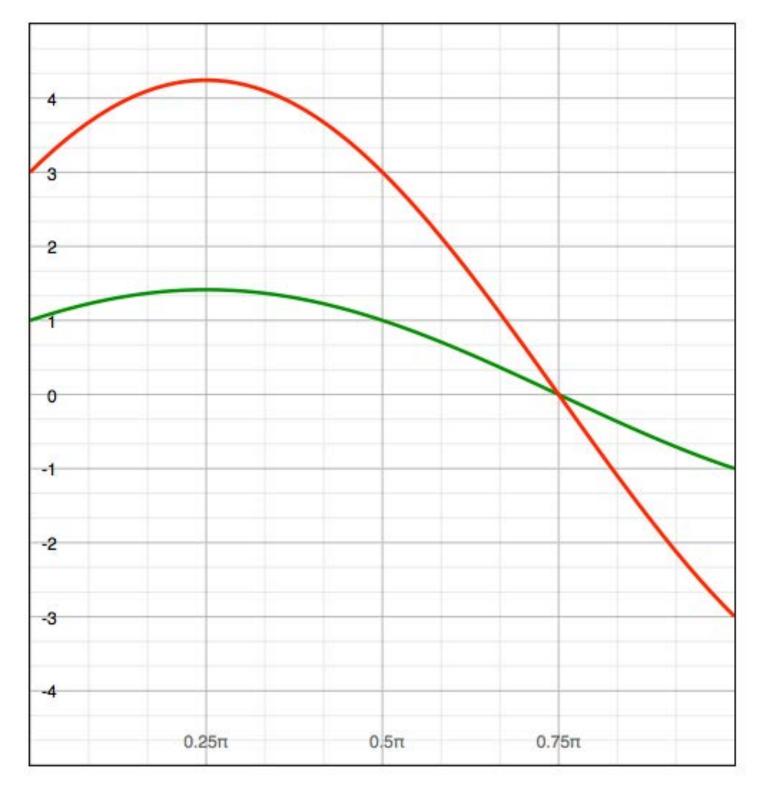
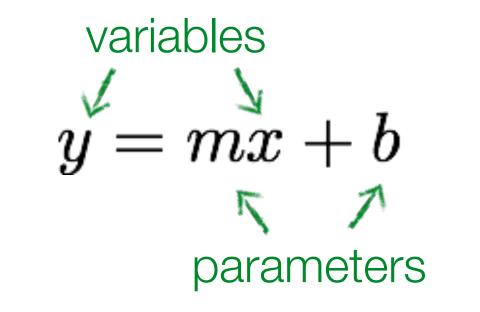


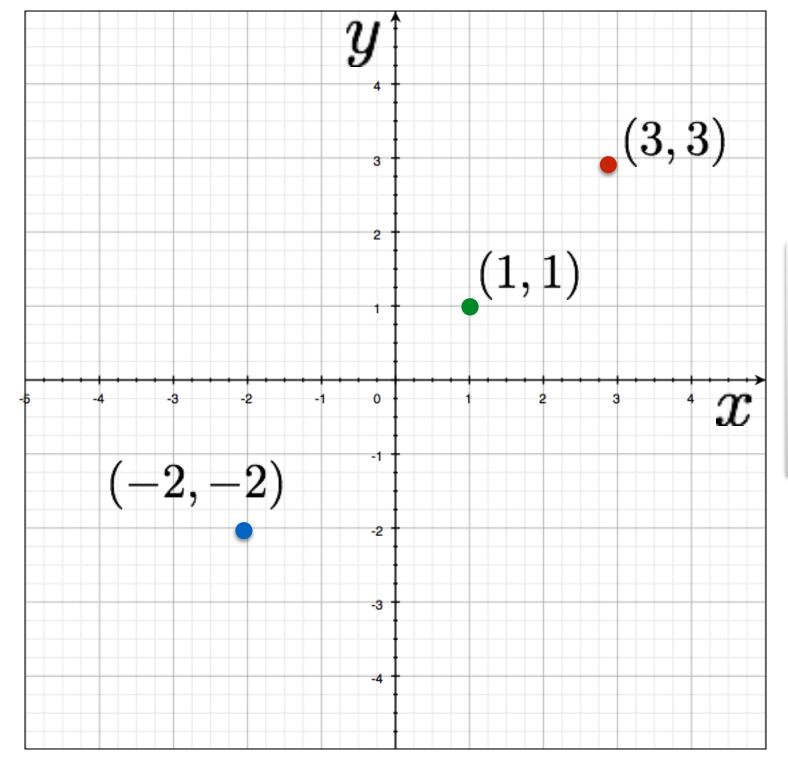
Image space





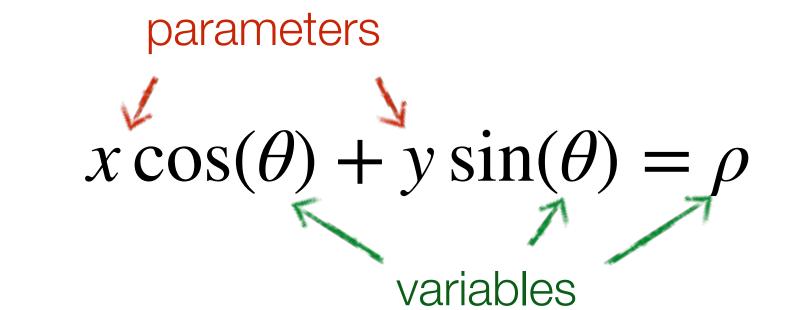
Parameter space





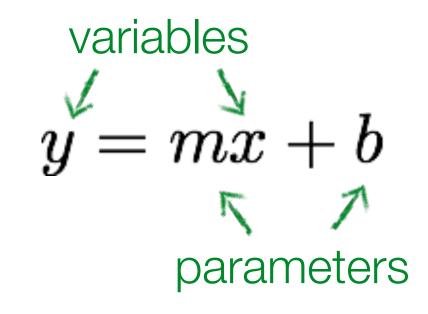
become?

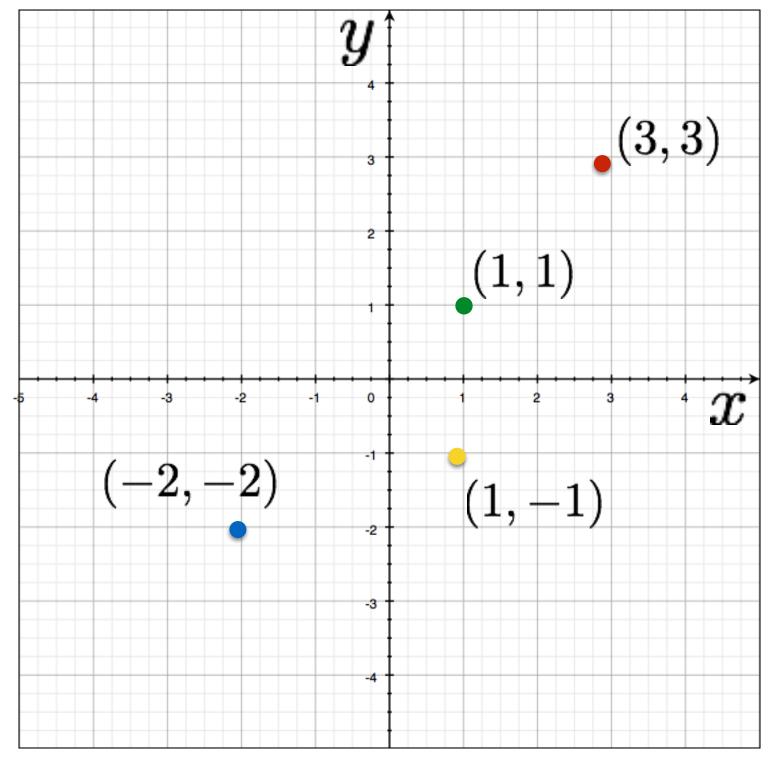
Image space





Parameter space

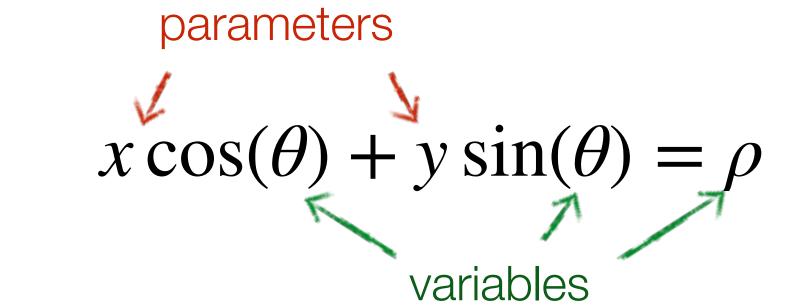




four points

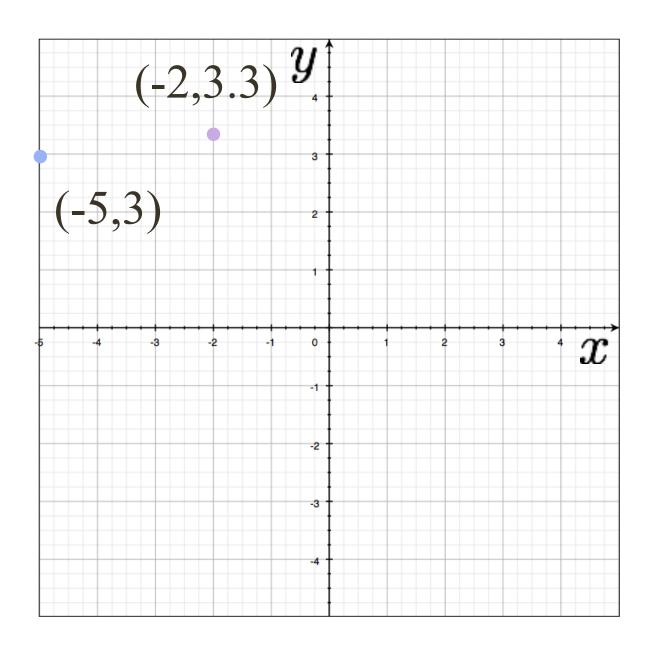
become?

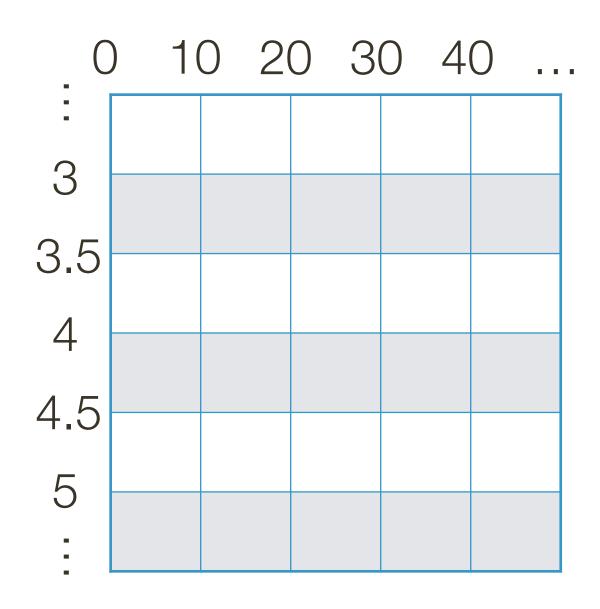
Image space

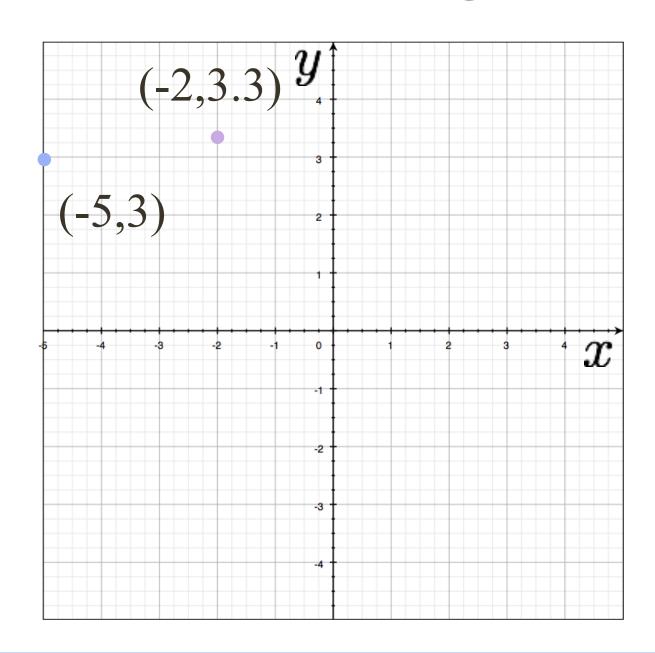




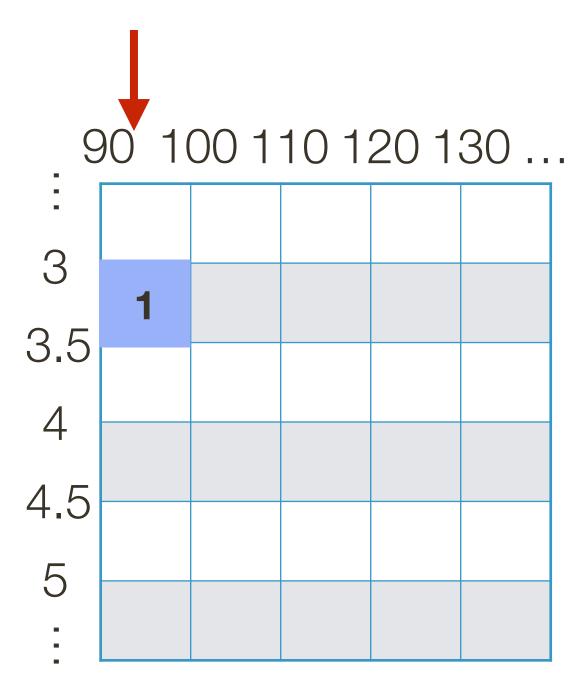
Parameter space

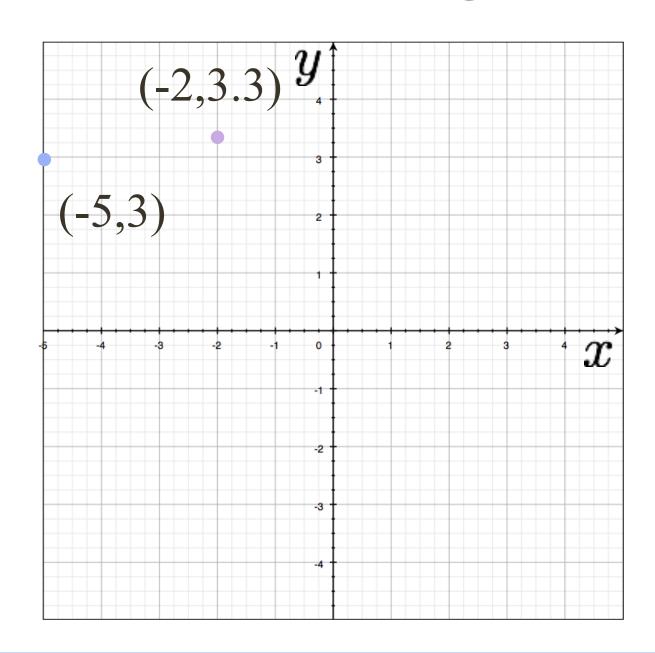




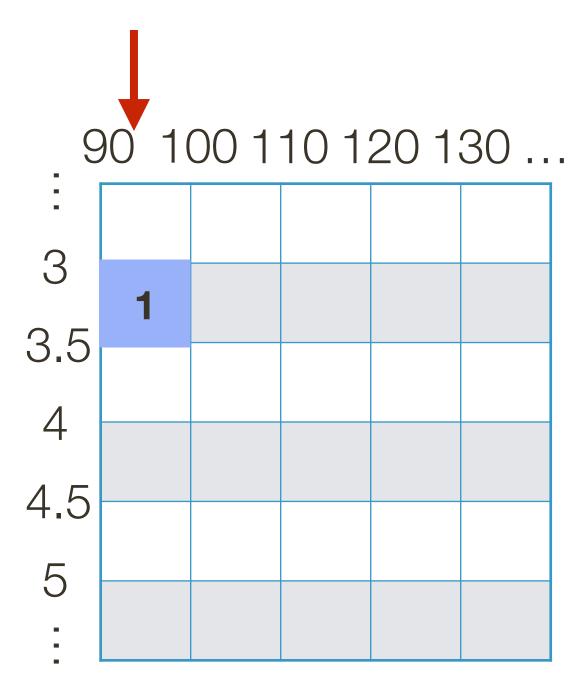


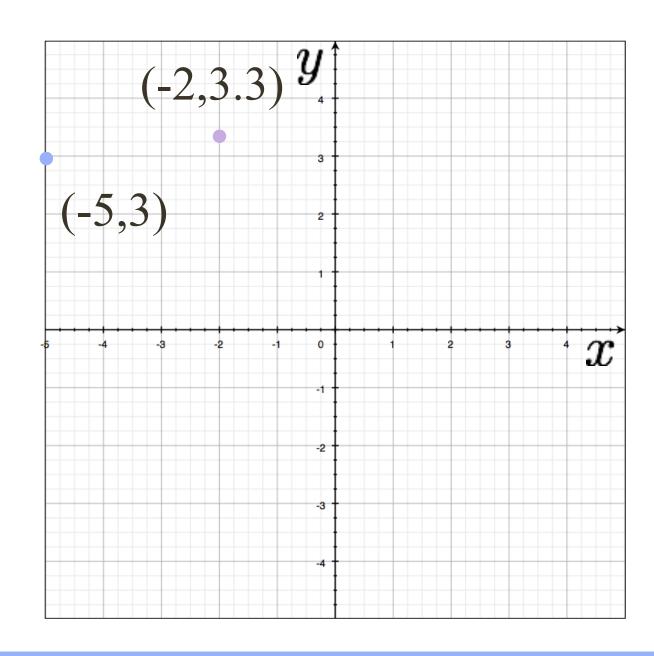






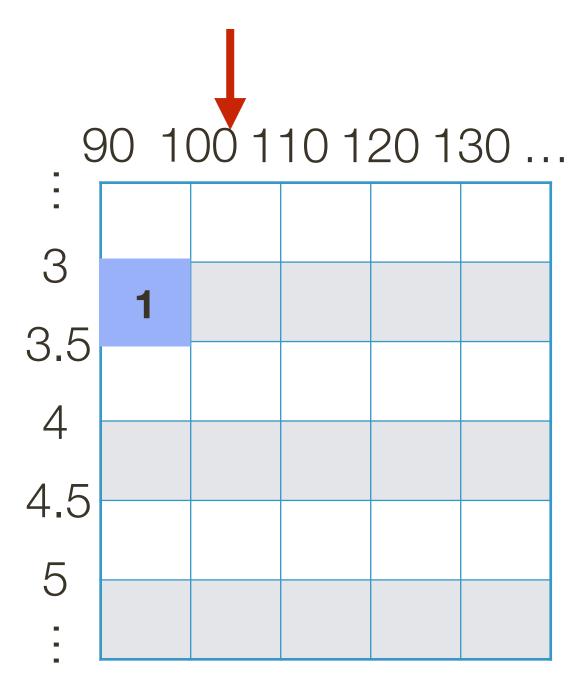


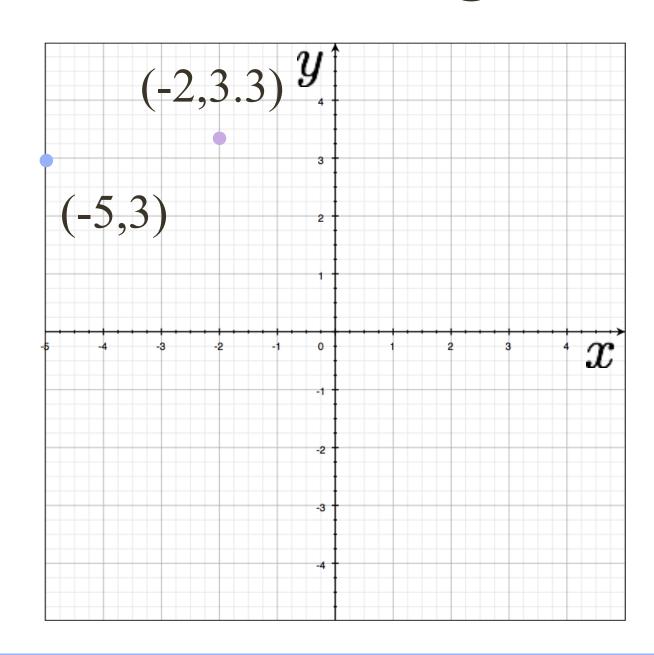






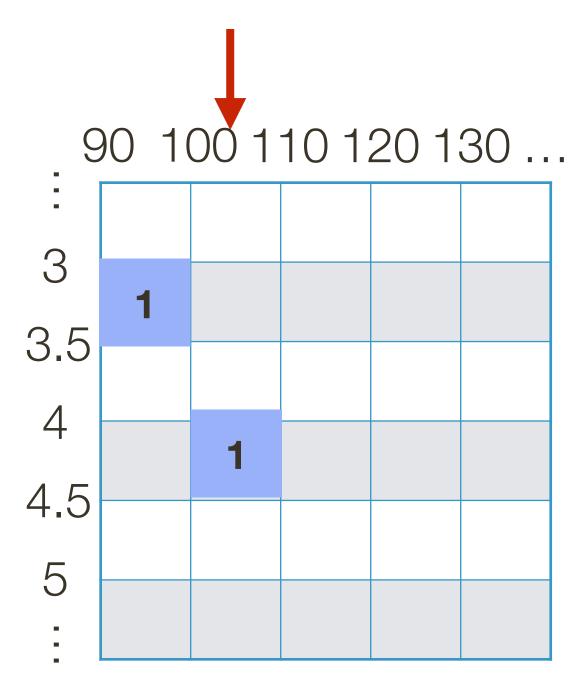
$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

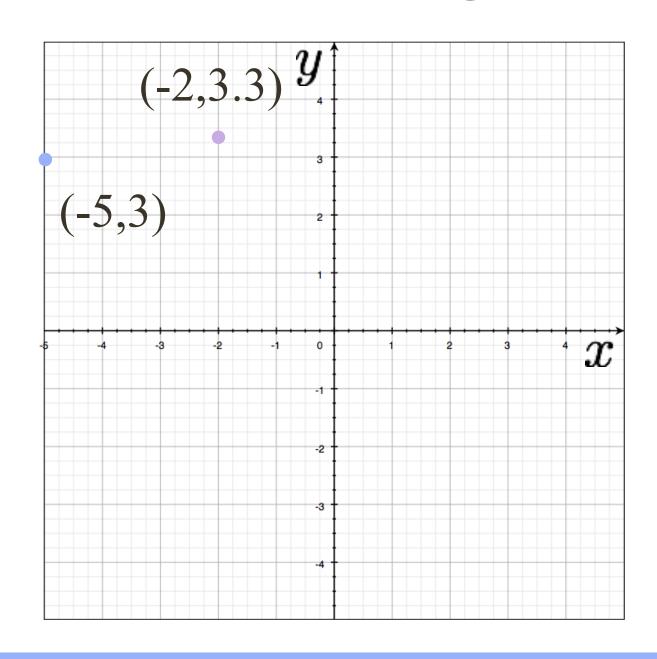






$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

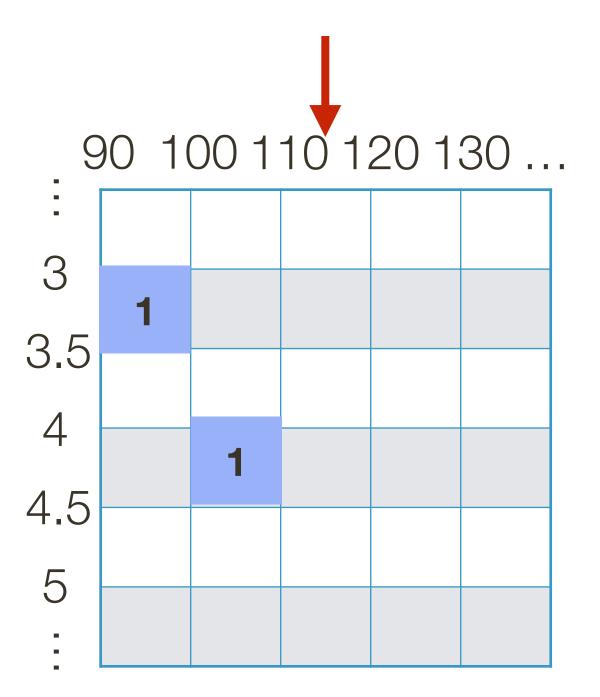


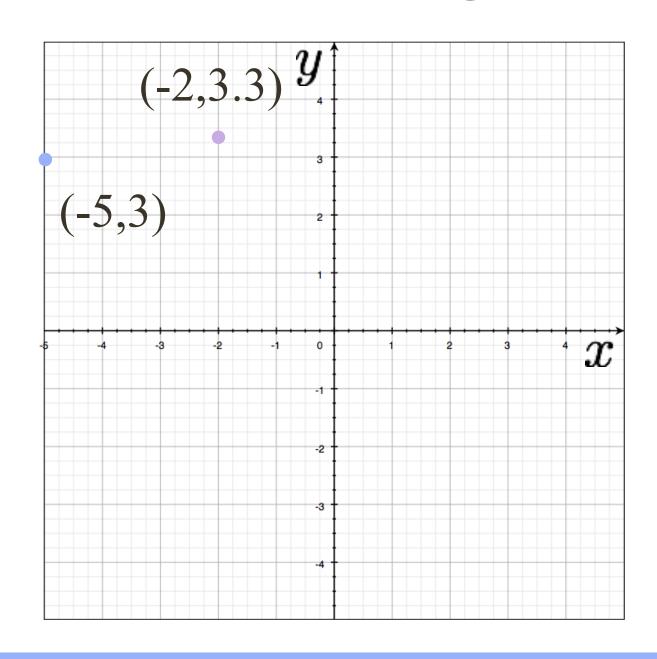


$$-5\cos(95^\circ) + 3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.42$$

$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

$$-5\cos(115^\circ) + 3\sin(115^\circ) + r = 0 \rightarrow r \approx 4.83$$

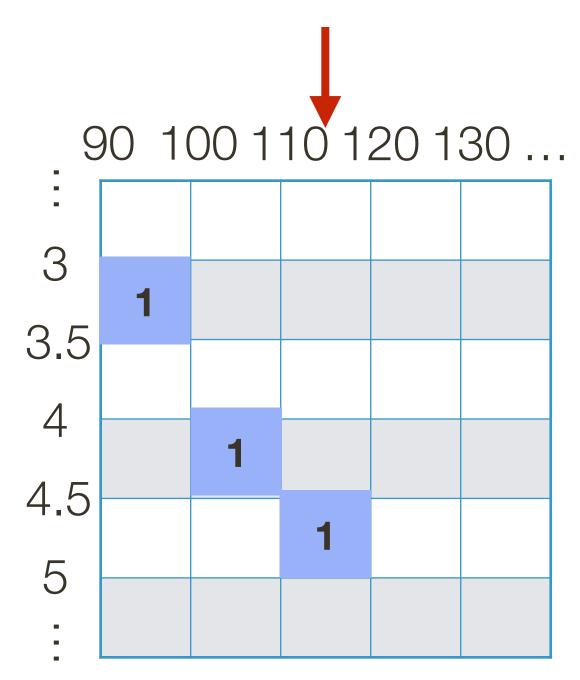


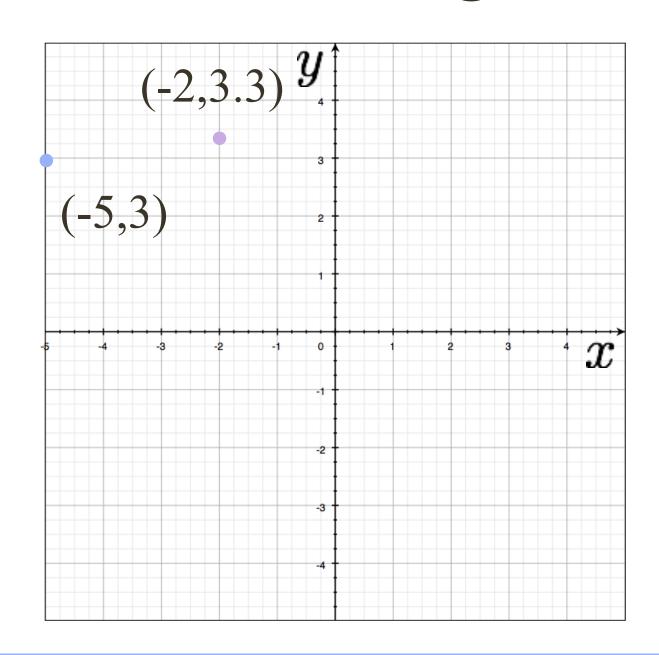


$$-5\cos(95^\circ) + 3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.42$$

$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

$$-5\cos(115^\circ) + 3\sin(115^\circ) + r = 0 \rightarrow r \approx 4.83$$

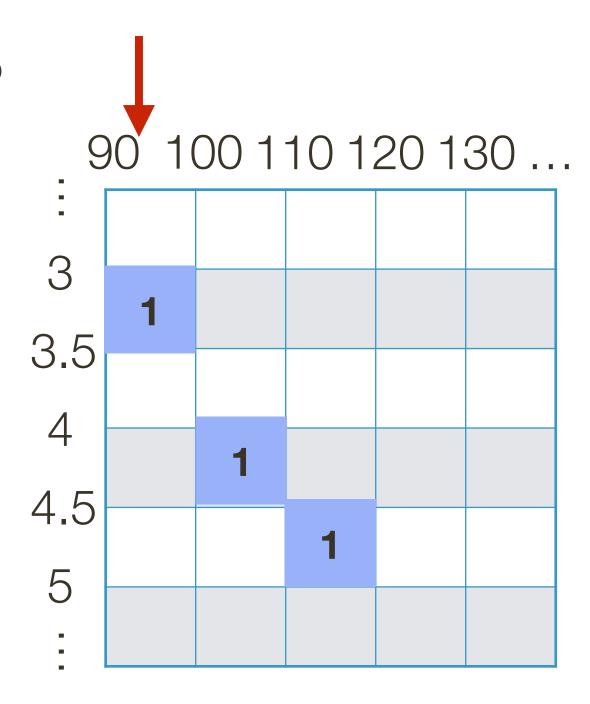




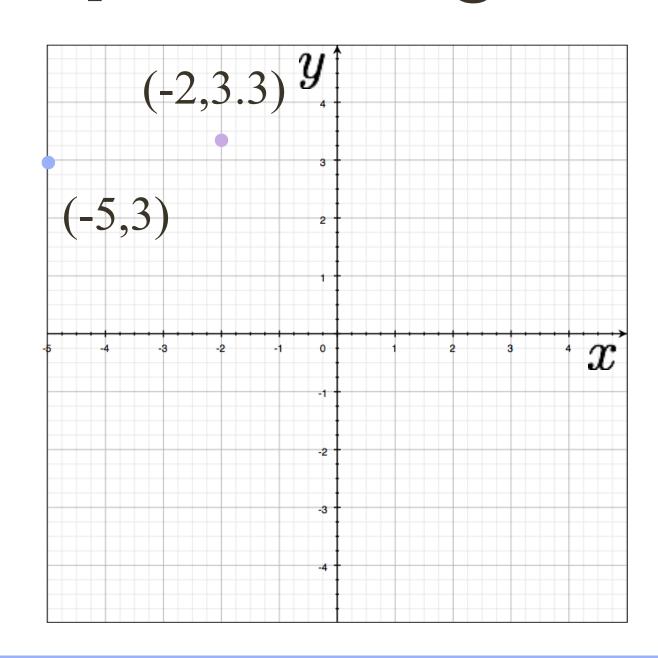


$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

$$-5\cos(115^\circ) + 3\sin(115^\circ) + r = 0 \rightarrow r \approx 4.83$$



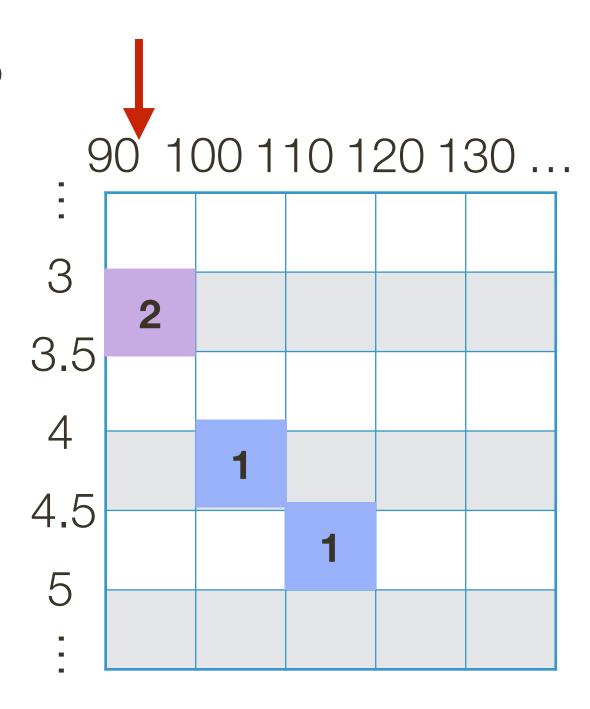
 $-2\cos(95^\circ) + 3.3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.46$



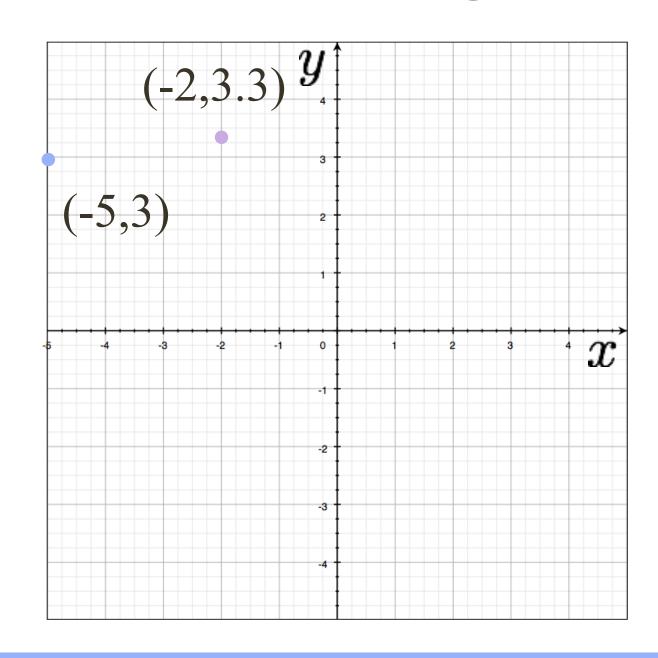


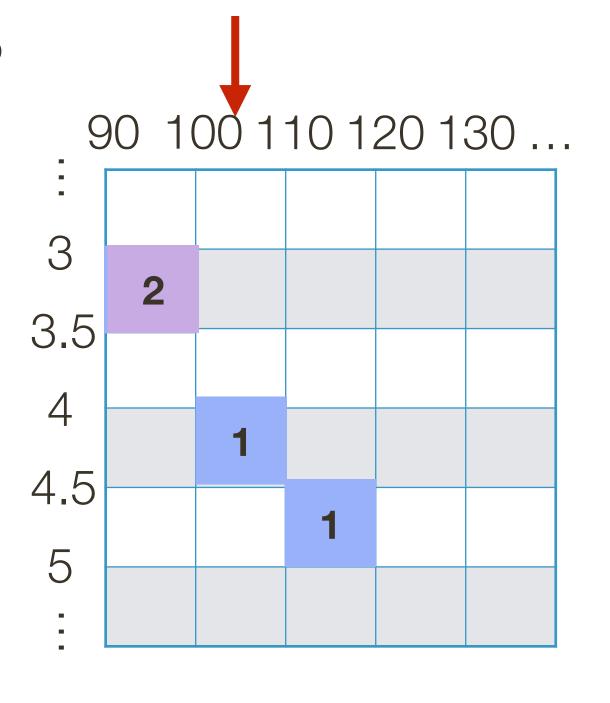
$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

$$-5\cos(115^\circ) + 3\sin(115^\circ) + r = 0 \rightarrow r \approx 4.83$$



 $-2\cos(95^\circ) + 3.3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.46$





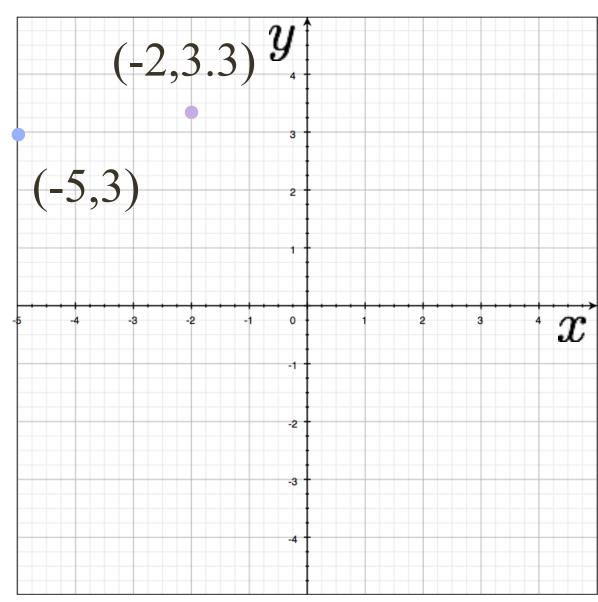
$$-5\cos(95^\circ) + 3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.42$$

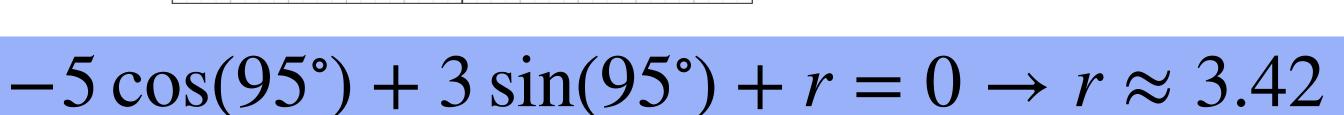
$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

$$-5\cos(115^\circ) + 3\sin(115^\circ) + r = 0 \rightarrow r \approx 4.83$$

$$-2\cos(95^\circ) + 3.3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.46$$

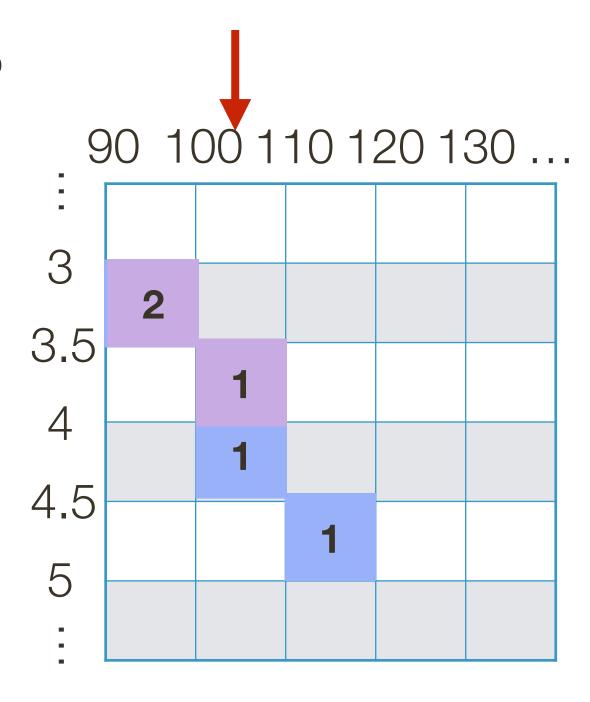
$$-2\cos(105^\circ) + 3.3\sin(105^\circ) + r = 0 \rightarrow r \approx 3.71$$





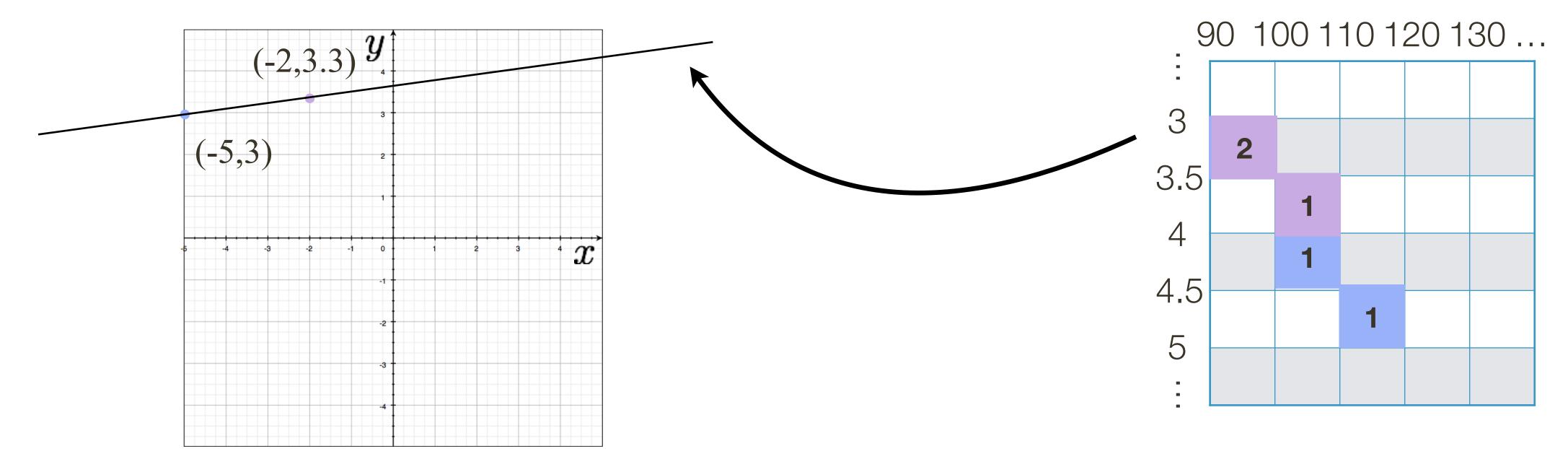
$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

$$-5\cos(115^\circ) + 3\sin(115^\circ) + r = 0 \rightarrow r \approx 4.83$$



$$-2\cos(95^\circ) + 3.3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.46$$

$$-2\cos(105^\circ) + 3.3\sin(105^\circ) + r = 0 \rightarrow r \approx 3.71$$



$$-5\cos(95^\circ) + 3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.42$$

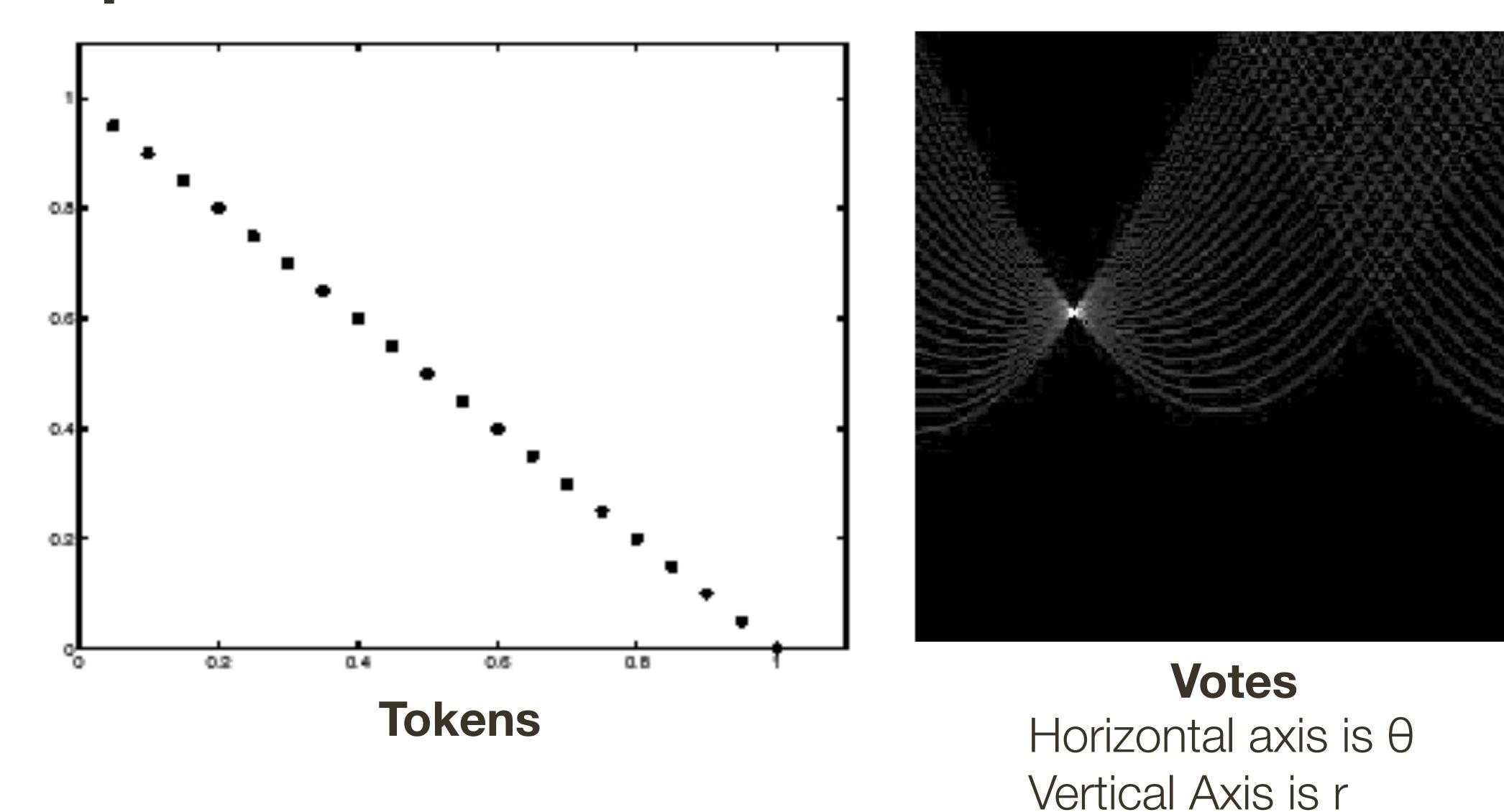
$$-5\cos(105^\circ) + 3\sin(105^\circ) + r = 0 \rightarrow r \approx 4.18$$

$$-5\cos(115^\circ) + 3\sin(115^\circ) + r = 0 \rightarrow r \approx 4.83$$

$$-2\cos(95^\circ) + 3.3\sin(95^\circ) + r = 0 \rightarrow r \approx 3.46$$

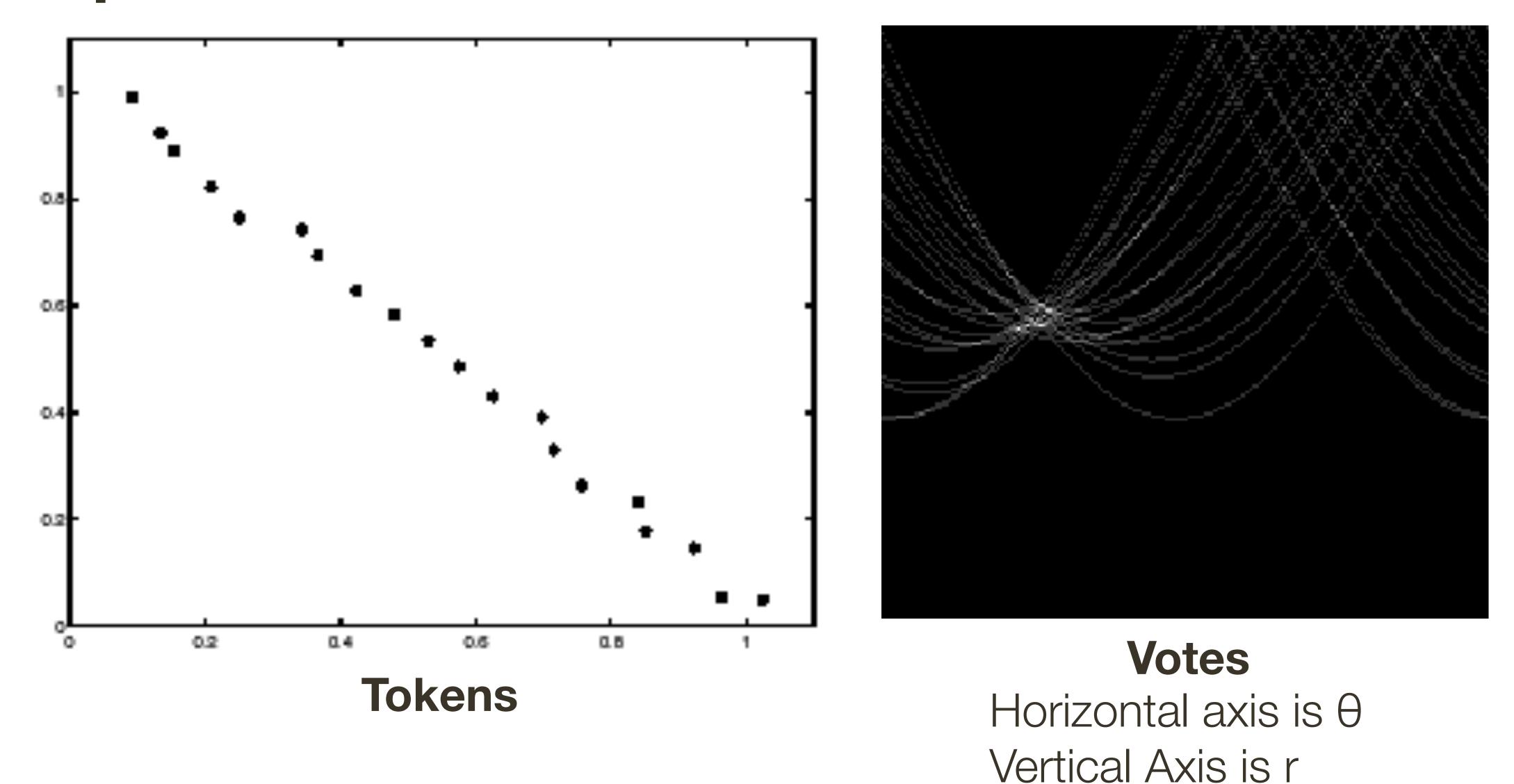
$$-2\cos(105^\circ) + 3.3\sin(105^\circ) + r = 0 \rightarrow r \approx 3.71$$

Example: Clean Data



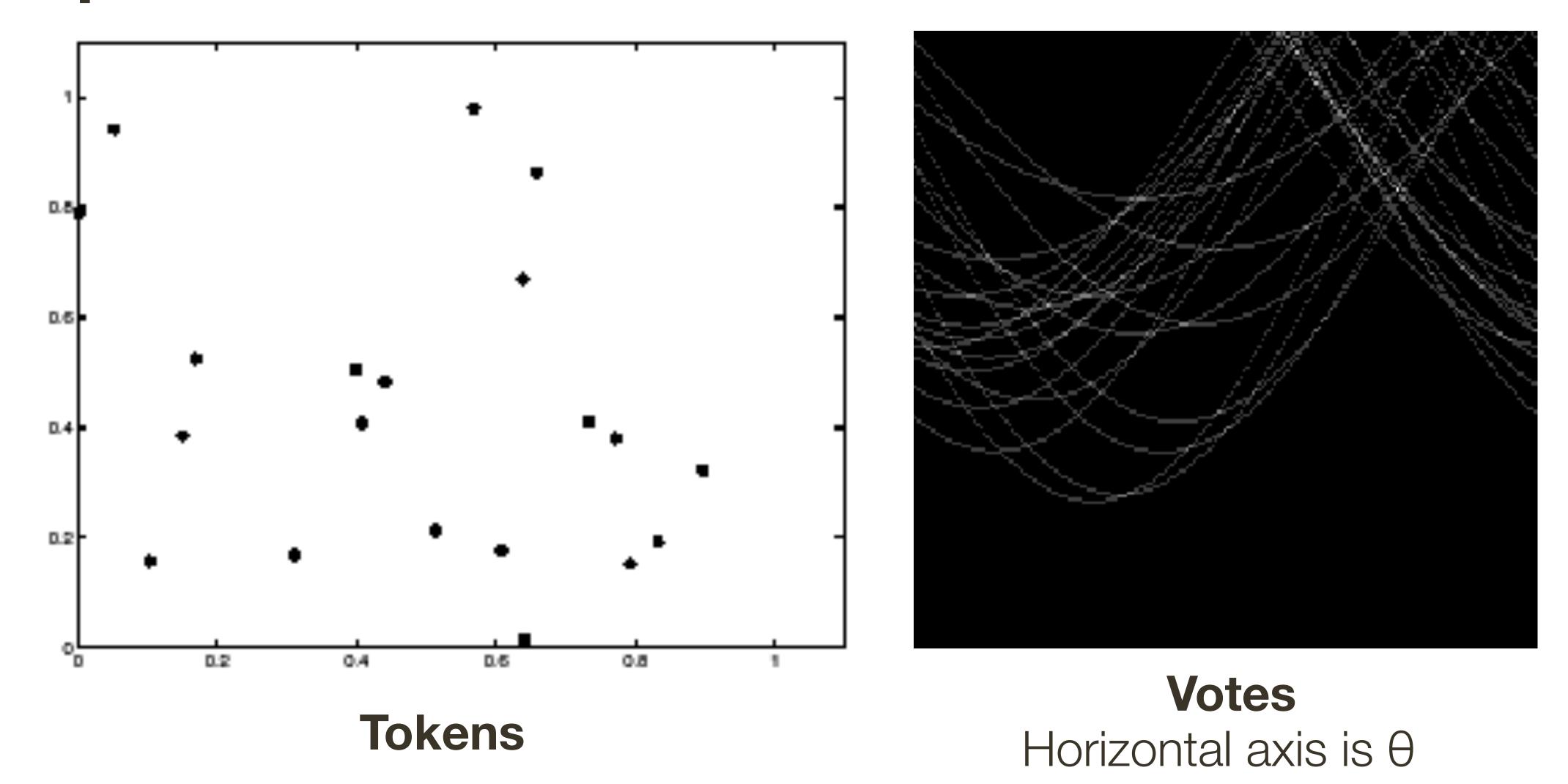
Forsyth & Ponce (2nd ed.) Figure 10.1 (Top)

Example: Some Noise



Forsyth & Ponce (2nd ed.) Figure 10.1 (Bottom)

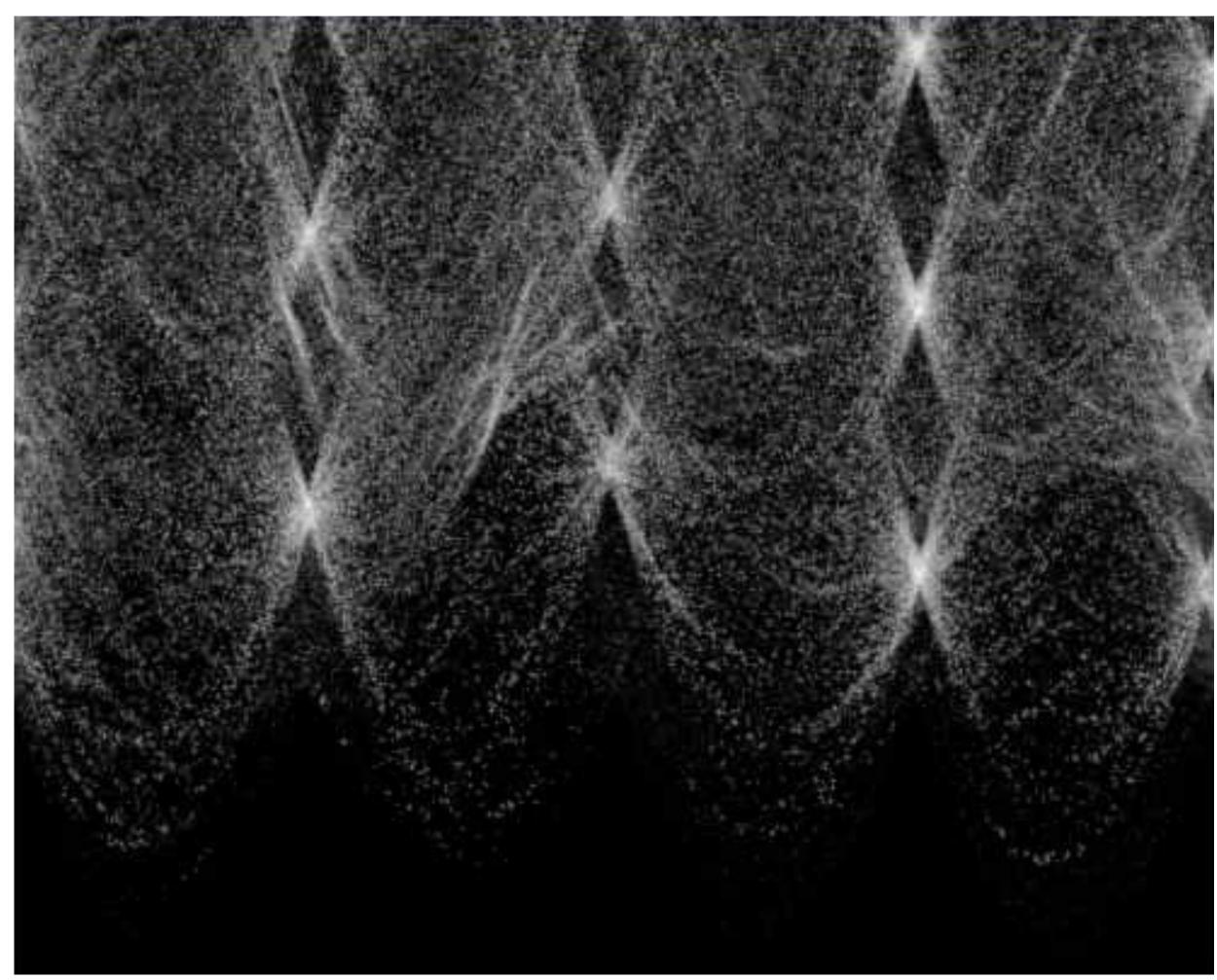
Example: Too Much Noise



Vertical Axis is r Forsyth & Ponce (2nd ed.) Figure 10.2

Real World Example

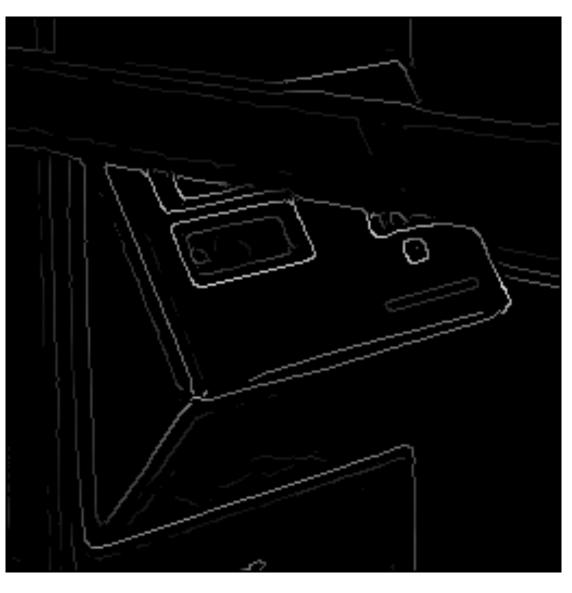




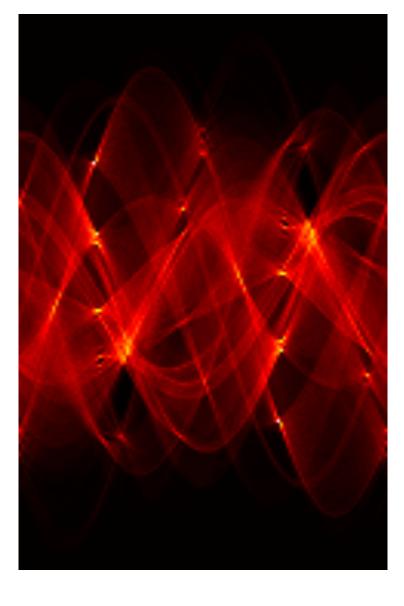
Real World Example



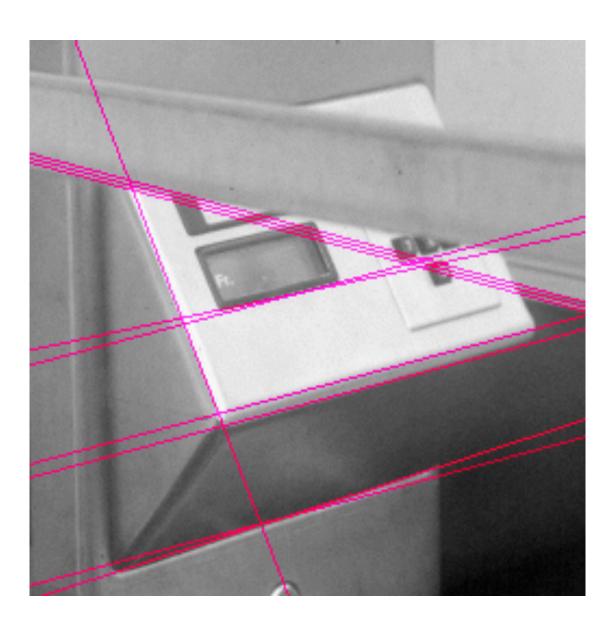
Original



Edges



Parameter space



Hough Lines

Mechanics of Hough Transform

- 1. Construct a quantized array to represent θ and r
- 2. For each point, render curve (θ , r) into this array adding one vote at each cell

Difficulties:

— How big should the cells be? (too big, and we merge quite different lines; too small, and noise causes lines to be missed)

How many lines?

- Count the peaks in the Hough array
- Treat adjacent peaks as a single peak

Some Practical Details of Hough Transform

It is best to **vote** for the two closest bins in each dimension, as the locations of the bin boundaries are arbitrary

— This means that peaks are "blurred" and noise will not cause similar votes to fall into separate bins

Can use a hash table rather than an array to store the votes

- This means that no effort is wasted on initializing and checking empty bins
- It avoids the need to predict the maximum size of the array, which can be non-rectangular

Hough Transform: Transformation Space Voting

Sometimes a single point / measurement can vote on the entire transformation

e.g., **SIFT** keypoint matches with **location, scale and orientation** vote on the 4 parameters of a **similarity transform** (x,y,s,theta)

In this case, the votes of each sample can be seen as a distribution in the parameter space of the transformation

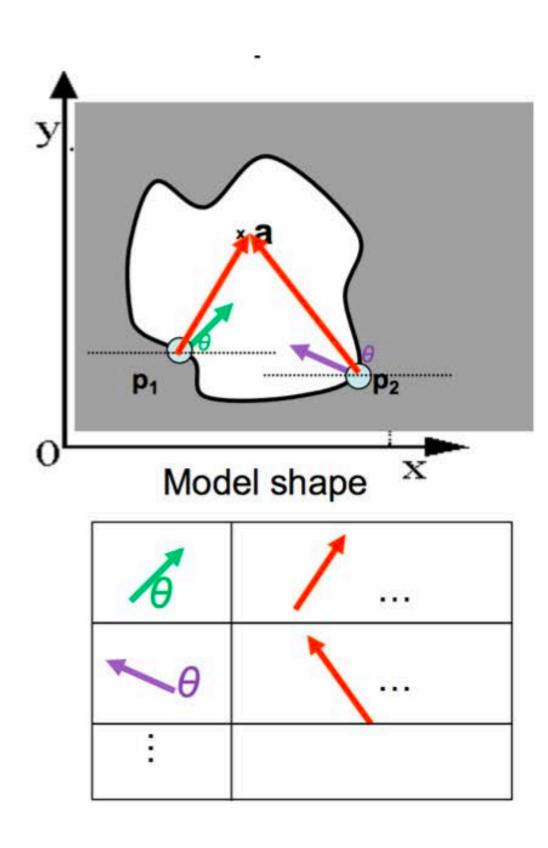
This can be effective in preventing noise in the distribution, e.g., edge detections with orientation can vote on **single lines** rather than **all lines** that pass through a point.

Generalized Hough Transform

What if we want to detect an arbitrary geometric shape?

Generalized Hough Transform

What if we want to detect an arbitrary geometric shape?



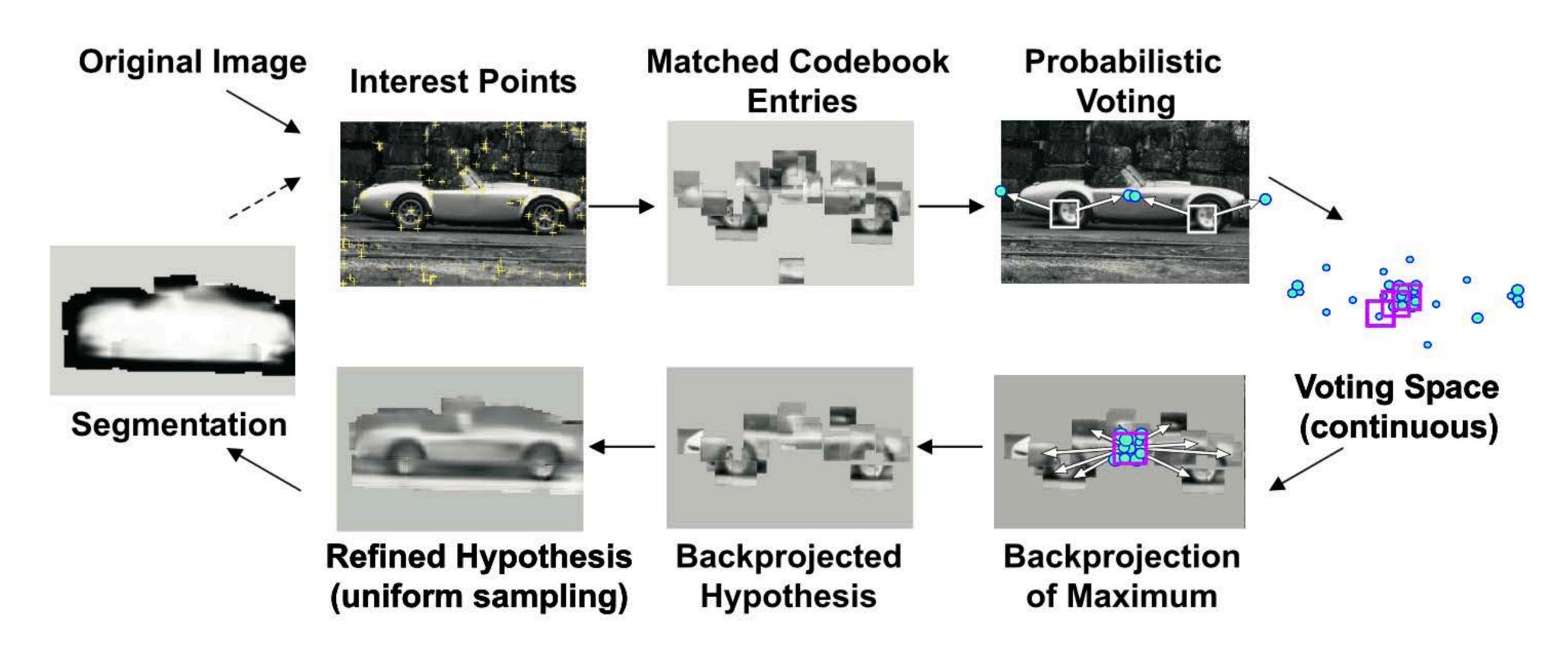
Offline procedure:

At each boundary point, compute displacement vector: $\mathbf{r} = \mathbf{a} - \mathbf{p_i}$.

Store these vectors in a table indexed by gradient orientation θ .

Dana H. Ballard, Generalizing the Hough Transform to Detect Arbitrary Shapes, 1980

Combined object detection and segmentation using an implicit shape model. Image patches cast weighted votes for the object centroid.



B. Leibe, A. Leonardis, and B. Schiele, Combined Object Categorization and Segmentation with an Implicit Shape Model, ECCV Workshop on Statistical Learning in Computer Vision 2004

Basic Idea:

- Find interest points/keypoints in an image (e.g., SIFT Keypoint detector or Corners)
- Match patch around each interest point to a training patch (e.g., SIFT Descriptor)
- Vote for object center given that training instances
- Find the patches that voted for the peaks (back-project)

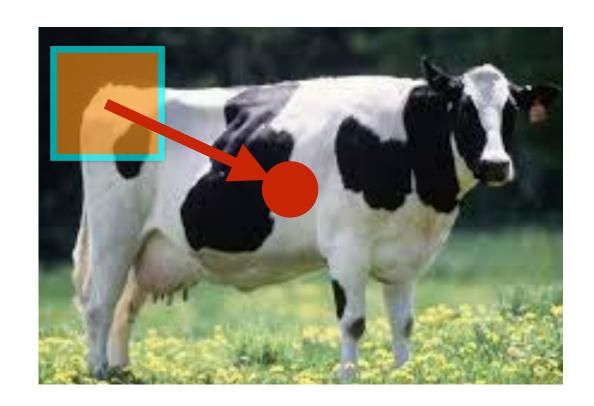


Image Index	Keypoint Index	Keypoint Detection (4D)	Keypoint Description (128D)	Offset to Centroid
Image 1	1	[x, y, s, Theta]	[]	[x,y]

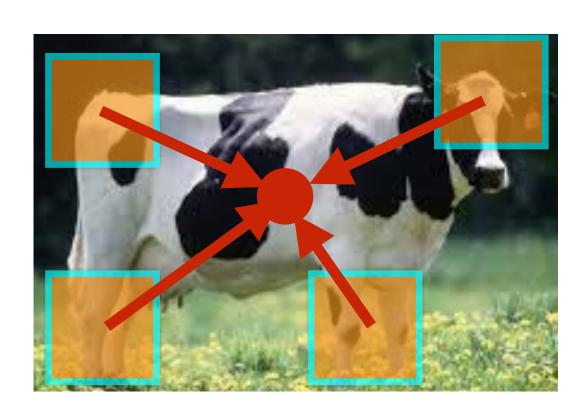
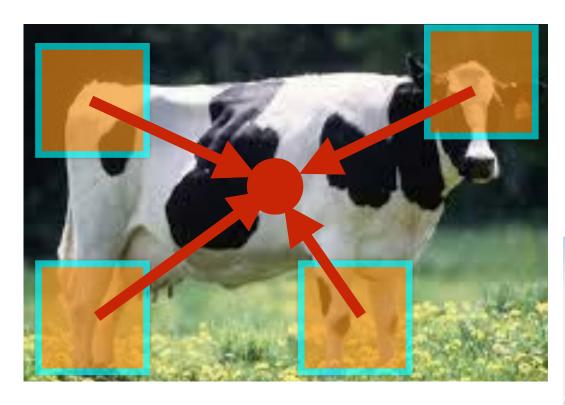
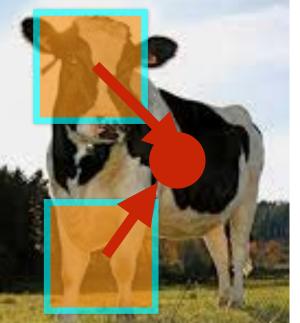


Image Index	Keypoint Index	Keypoint Detection (4D)	Keypoint Description (128D)	Offset to Centroid
Image 1	1 2	[x, y, s, Theta]	[]	[x,y]
Image 1		[x, y, s, Theta]	[]	[x,y]
	265			
Image 1		[x, y, s, Theta]	[]	[x,y]





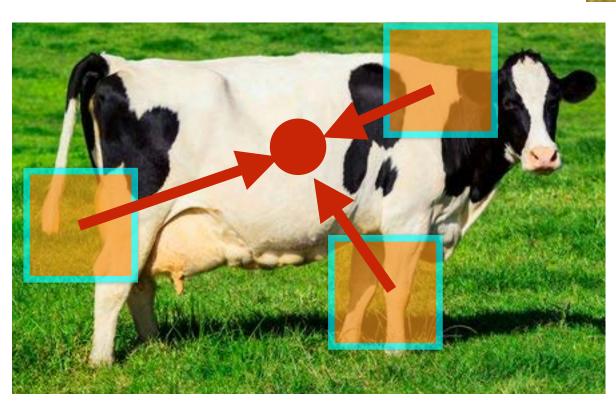


Image Index	Keypoint Index	Keypoint Detection (4D)	Keypoint Description (128D)	Offset to Centroid
Image 1 Image 1	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y]
Image 1	265	[x, y, s, Theta]	[]	[x,y]
Image 2 Image 2	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y] [x,y]
Image 2	645	[x, y, s, Theta]	 []	[x,y]
Image K Image K	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y] [x,y]
Image K	134	[x, y, s, Theta]	[]	[x,y]









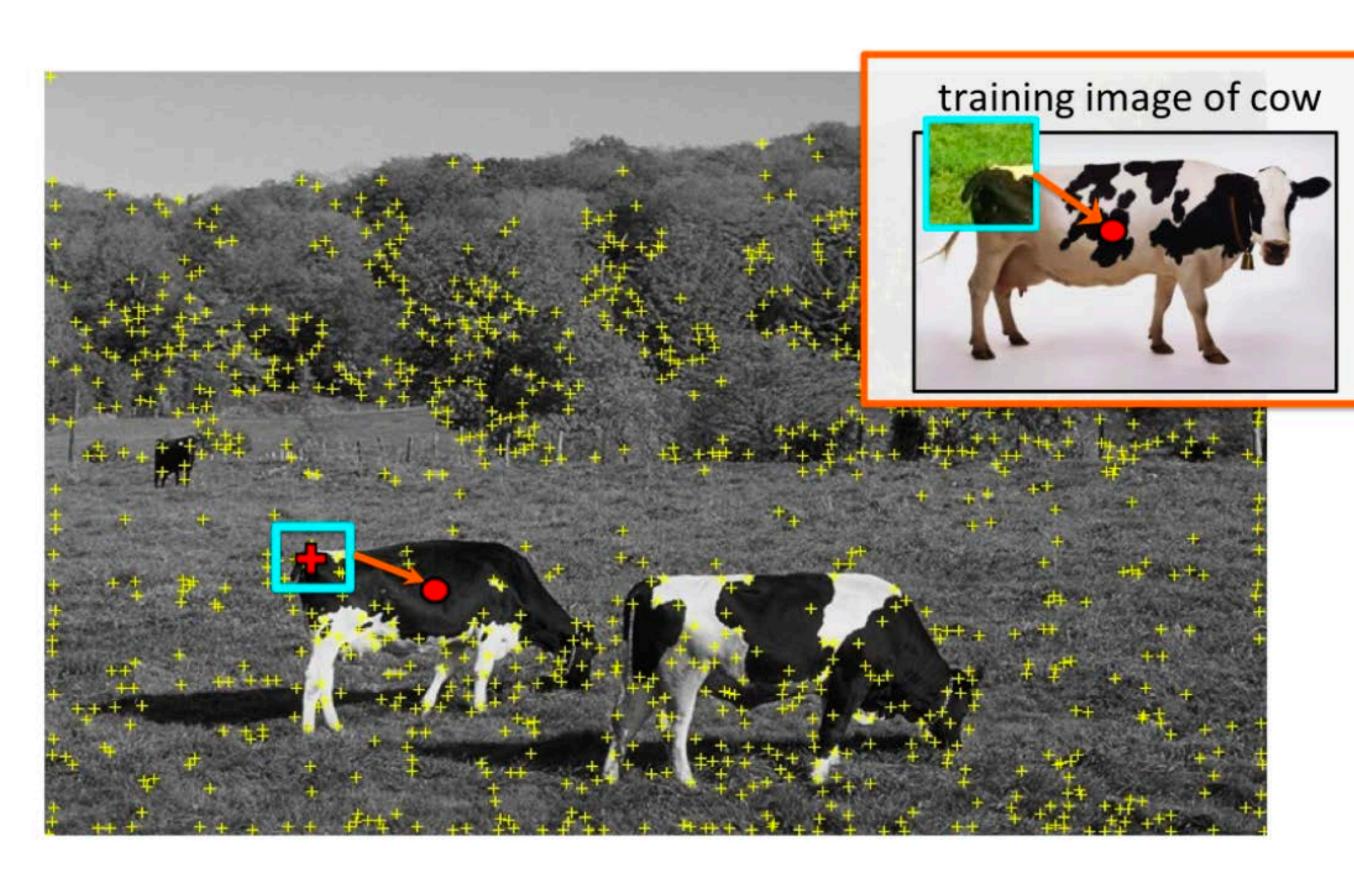


"Training" images of cows









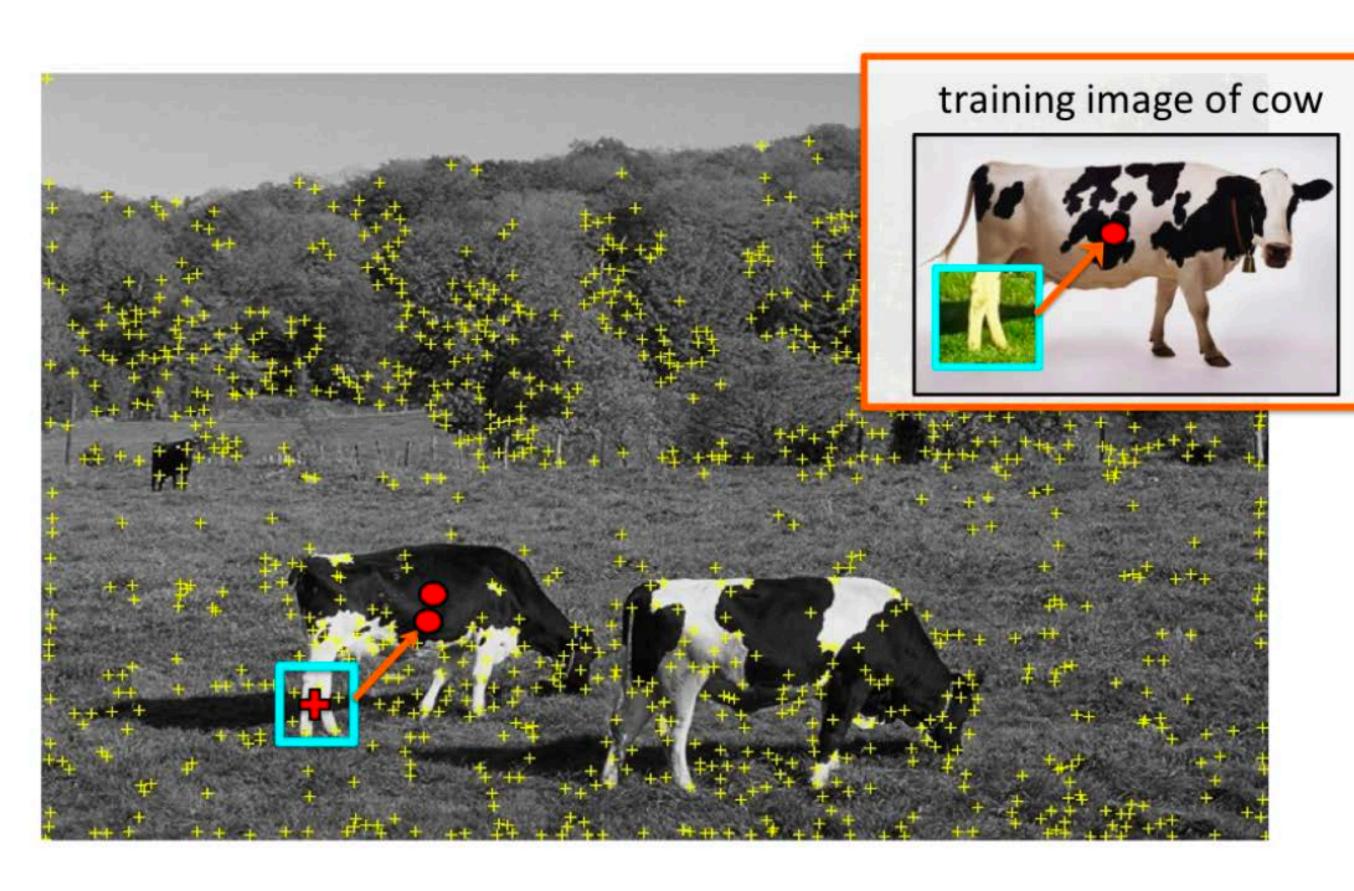
Vote for center of object

"Training" images of cows







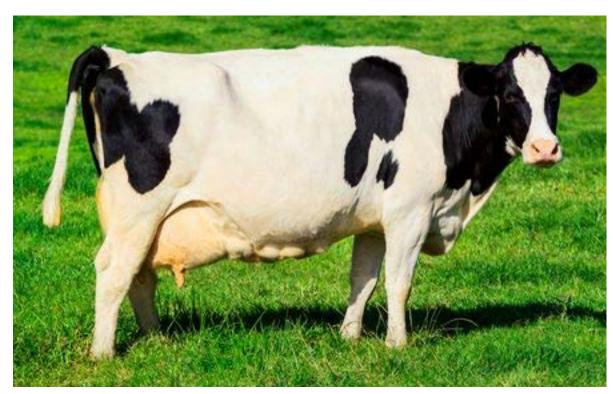


Vote for center of object

"Training" images of cows









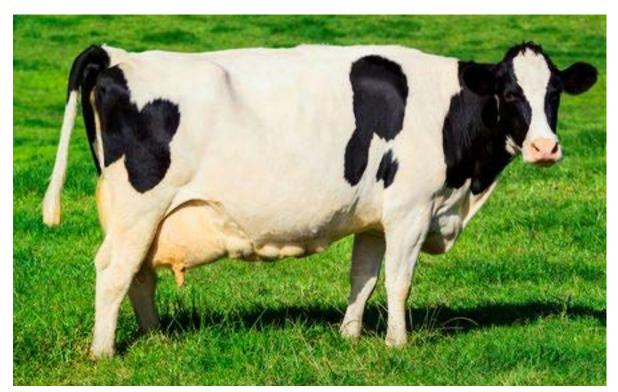
Vote for center of object

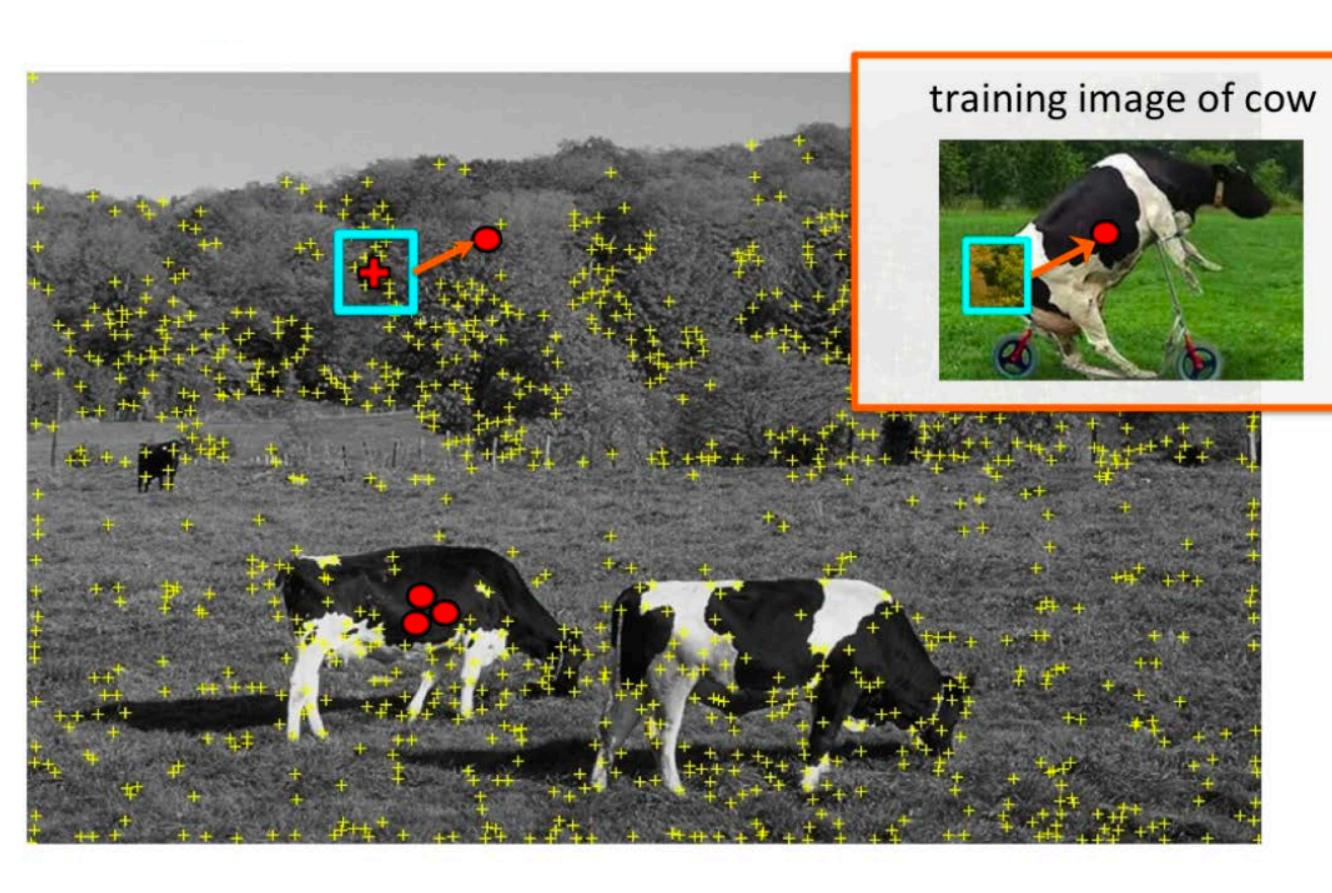
"Training" images of cows

"Testing" image









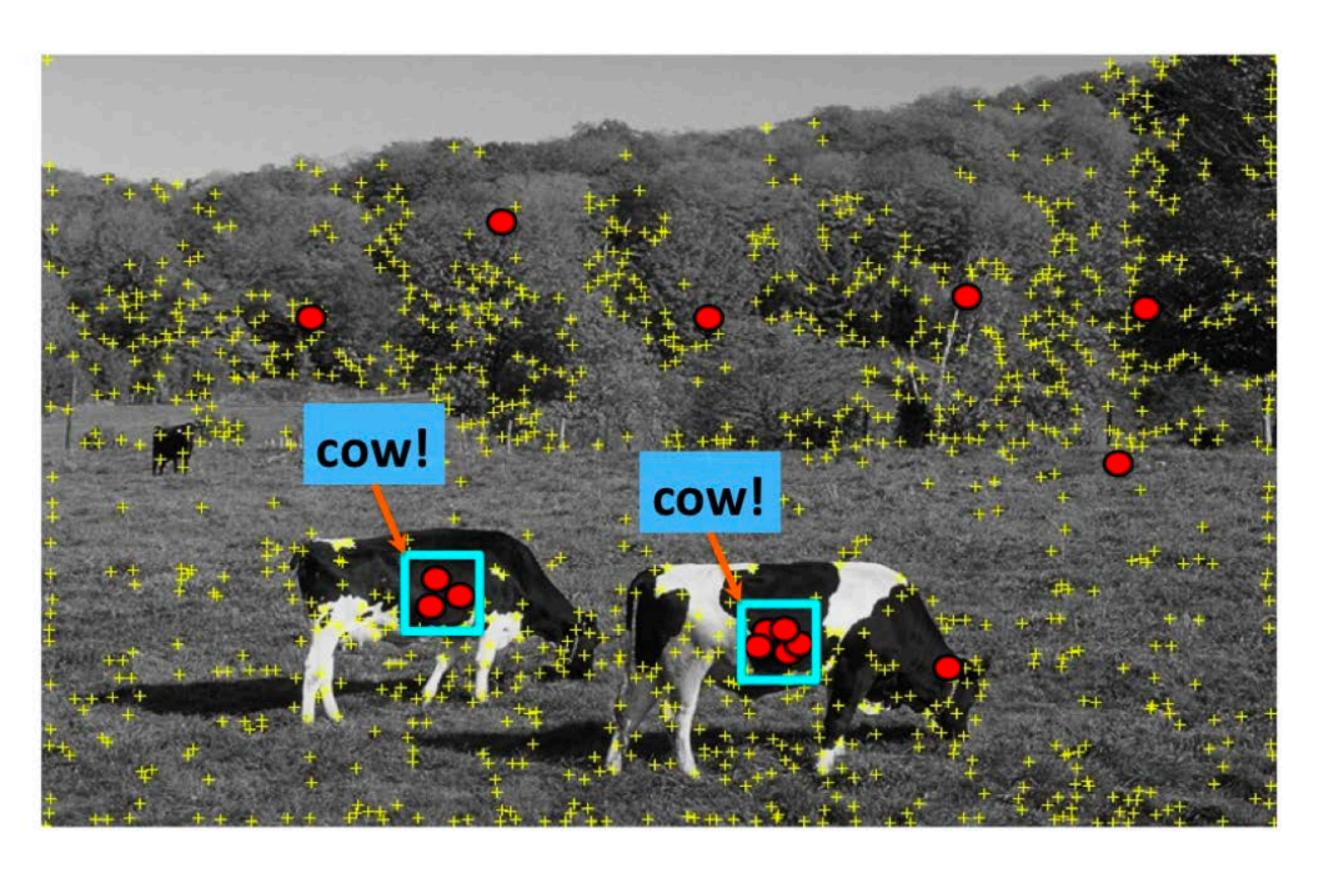
of course sometimes wrong votes are bound to happen

"Training" images of cows









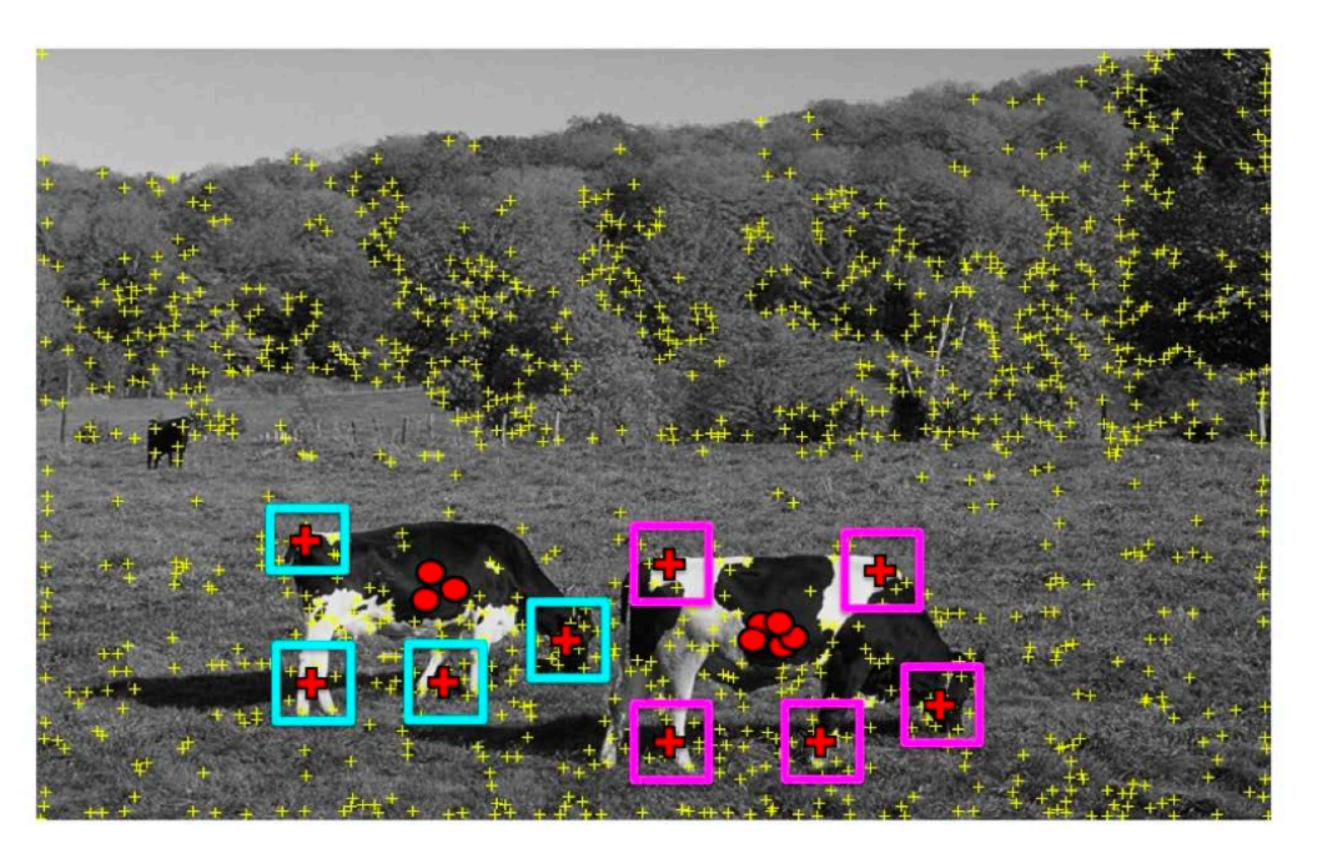
That's ok. We want only peaks in voting space.

"Training" images of cows









Find patches that voted for the peaks (back-project)

Image Index	Keypoint Index	Keypoint Detection (4D)	Keypoint Description (128D)	Offset to Centroid	
Image 1 Image 1	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y] [x,y]	
Image 1	265	[x, y, s, Theta]	[]	[x,y]	
Image 2 Image 2	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y] [x,y]	
Image 2	645	[x, y, s, Theta]	[]	[x,y]	
Image K Image K	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y] [x,y]	
Image K	134	[x, y, s, Theta]	[]	[x,y]	

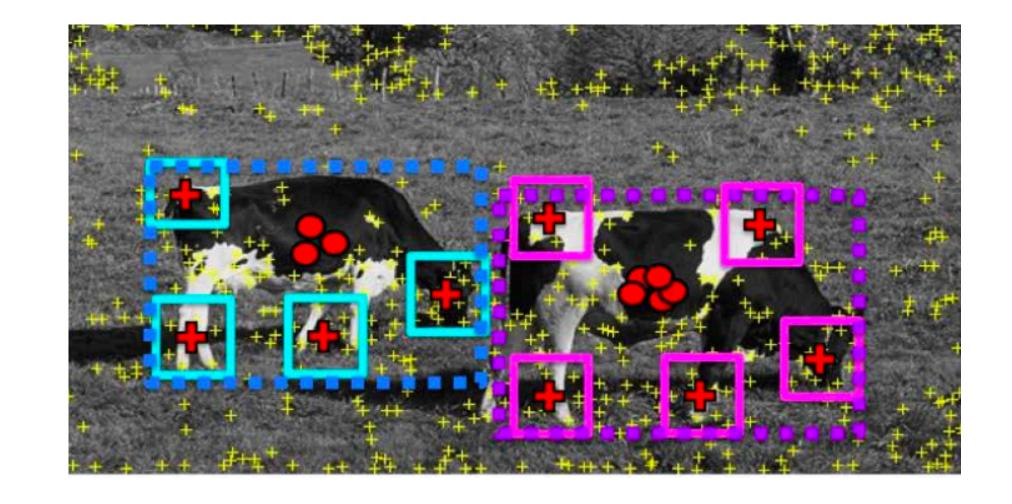
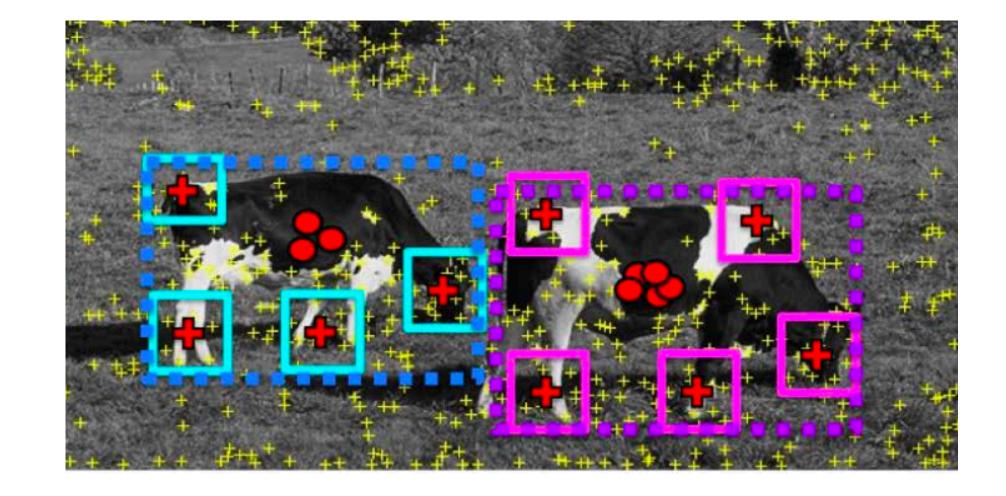


Image Index	Keypoint Index	Keypoint Detection (4D)	Keypoint Description (128D)	Offset to Centroid
Image 1	1	[x, y, s, Theta]	[]	[x,y]
Image 1	2	[x, y, s, Theta]	[]	[X,y]
Image 1	265	[x, y, s, Theta]	[]	[x,y]
lmage 2	1	[x, y, s, Theta]	[]	[x,y]
Image 2	2	[x, y, s, Theta]	[]	[X,y]
Image 2	645	[x, y, s, Theta]	[]	[X,y]
Image K	1	[x, y, s, Theta]	[]	[x,y]
Image K	2	[x, y, s, Theta]	[]	[x,y]
	1			
Image K	134	[x, y, s, Theta]	[]	$[\times,y]$



"Training" images of cows

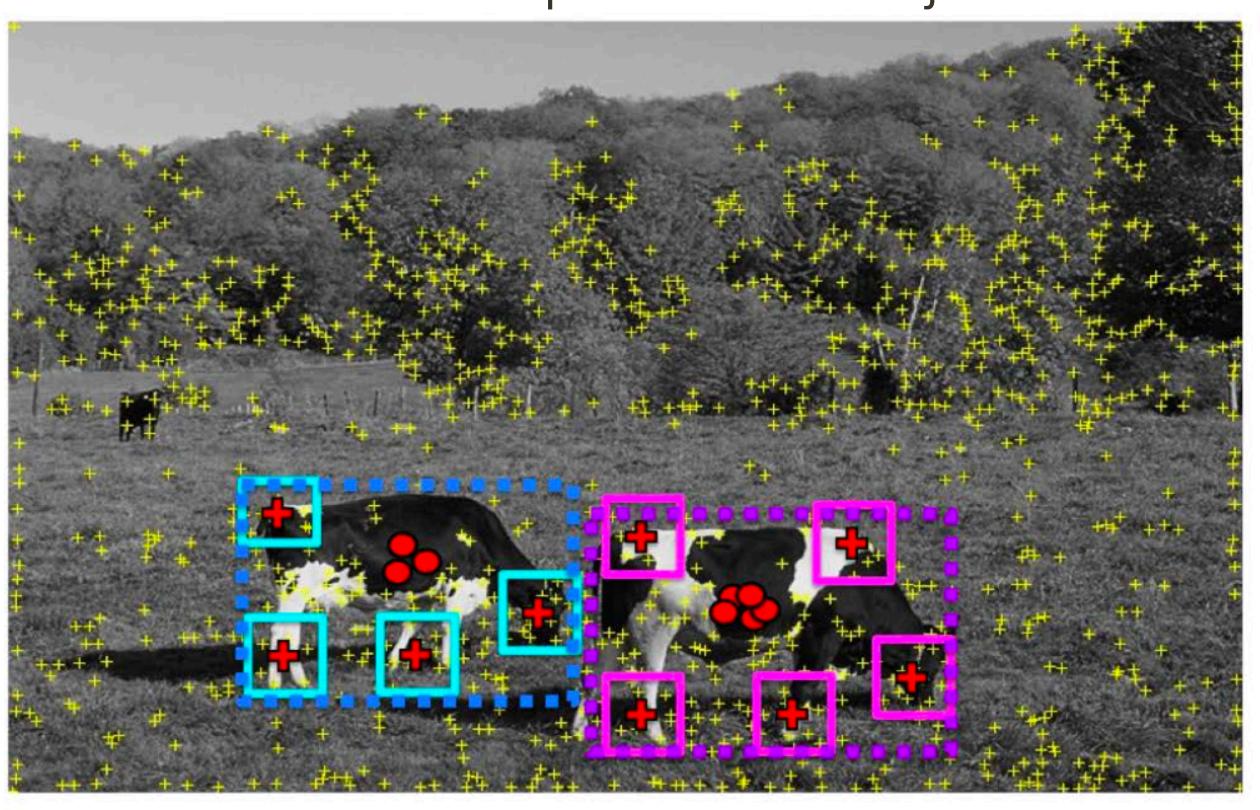






"Testing" image

box around patches = object



Find objects based on the back projected patches

"Training" images of cows



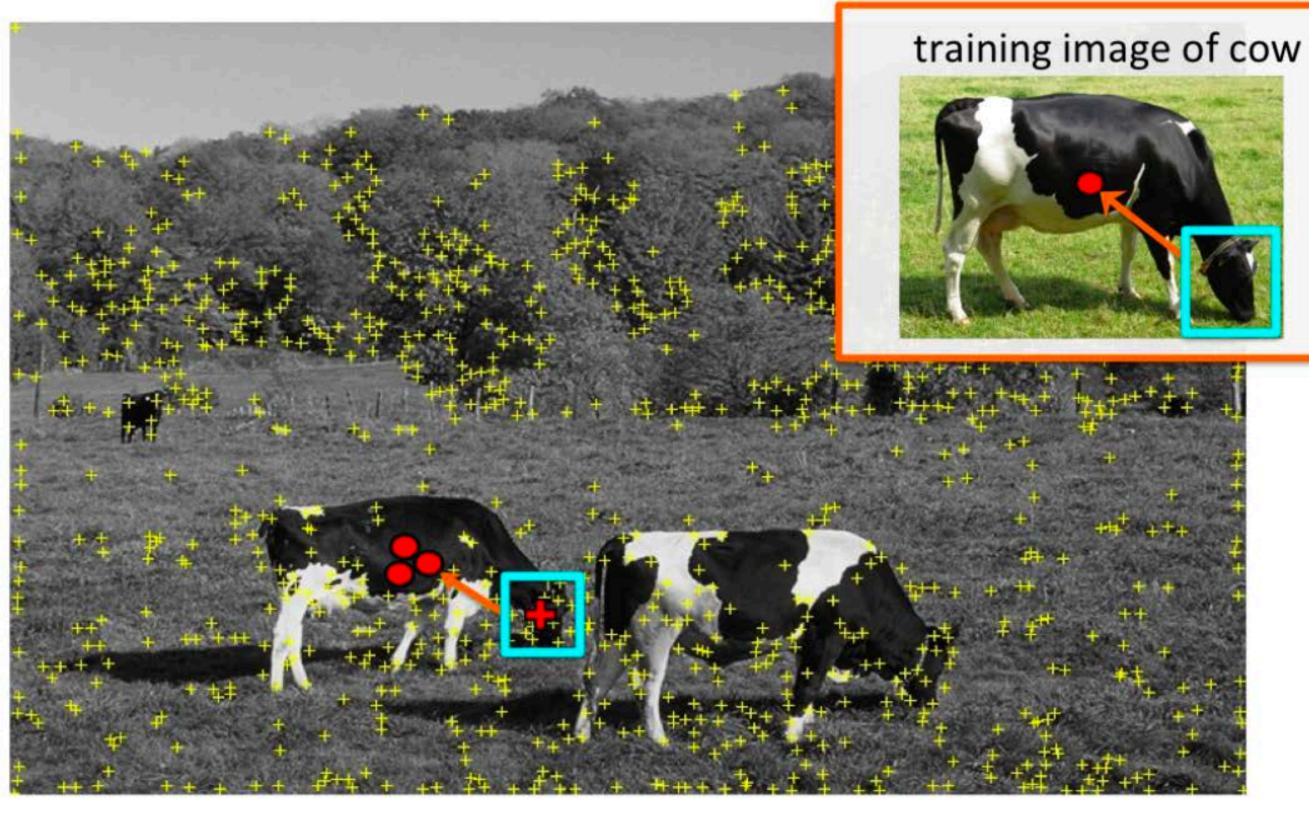
Really easy ... but slow ... how do we make it fast?







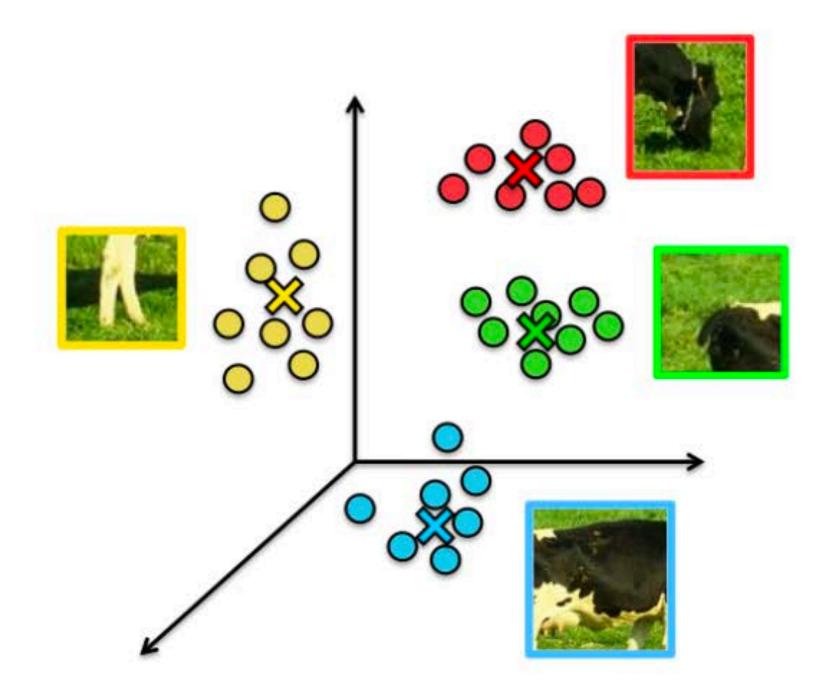




We need to match a patch around each yellow keypoint to all patches in all training images (slow)

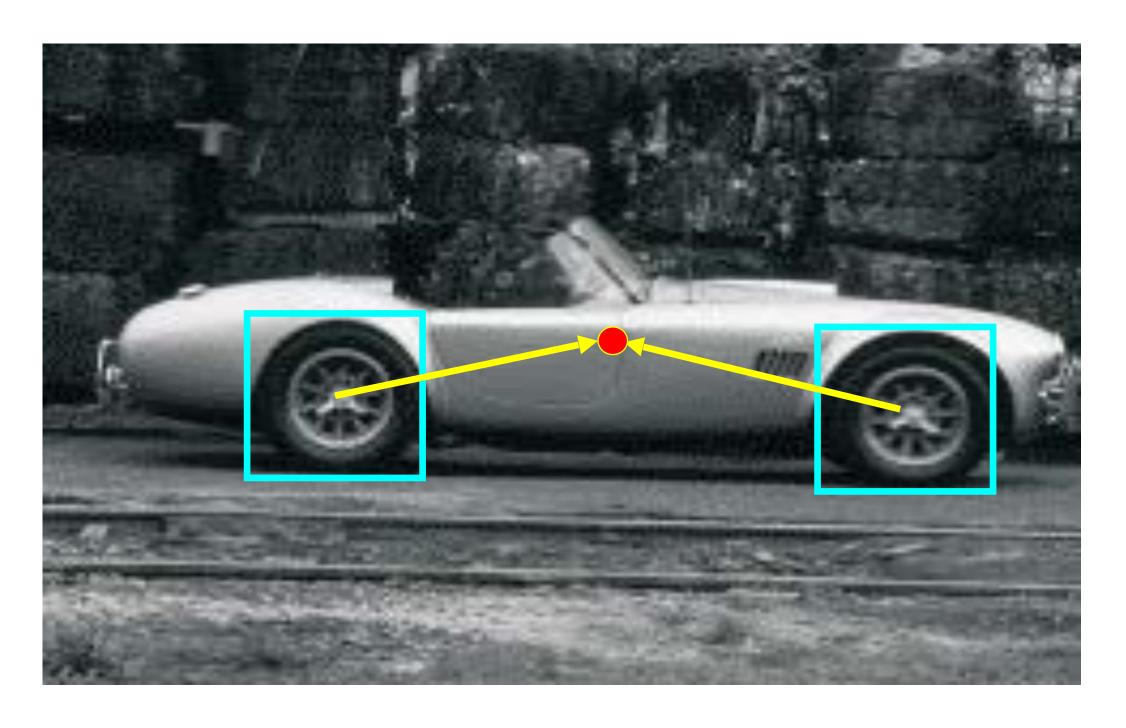
Visual Words

- Visual vocabulary (we saw this for retrieval)
- Compare each patch to a small set of visual words (clusters)

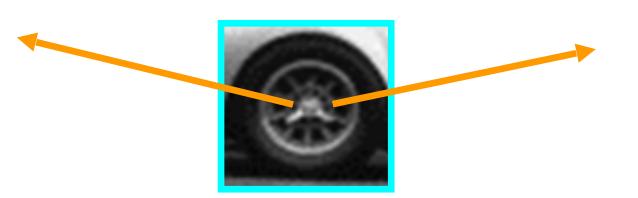


Visual words (visual codebook)!

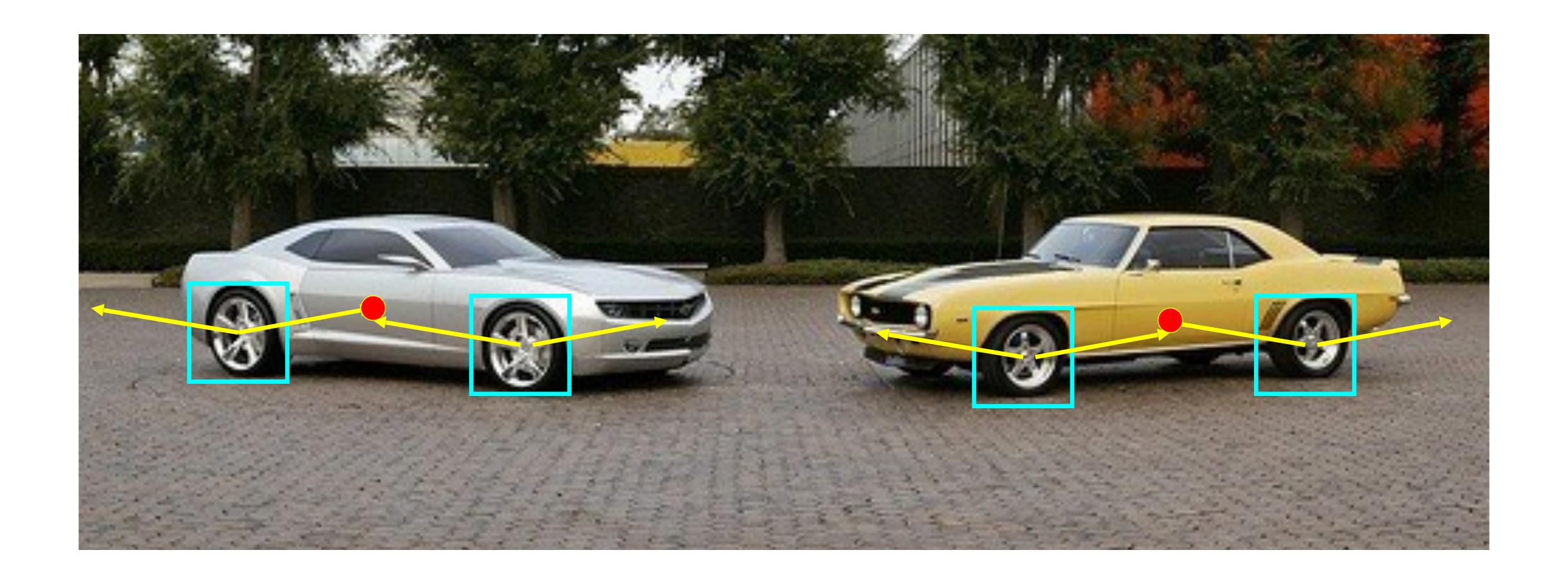
Index displacements by "visual codeword"



training image



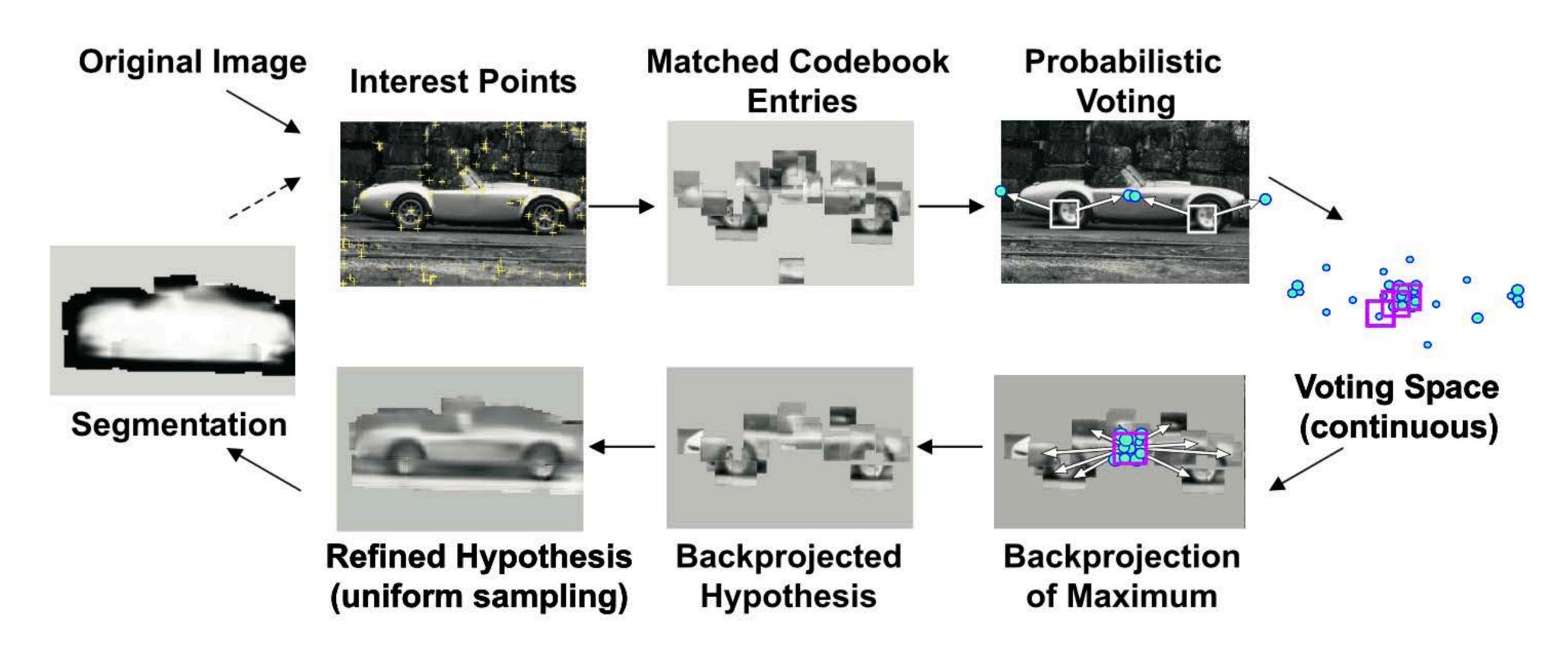
visual codeword with displacement vectors



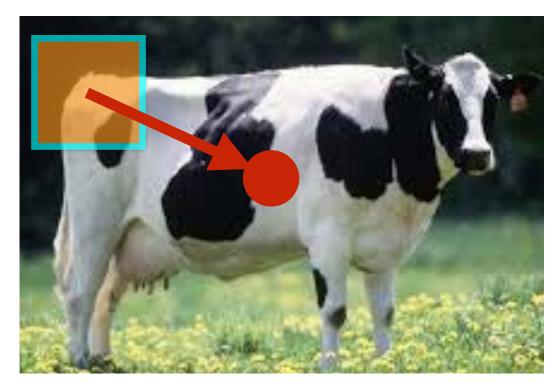
B. Leibe, A. Leonardis, and B. Schiele, Combined Object Categorization and Segmentation with an Implicit Shape Model, ECCV Workshop on Statistical Learning in Computer Vision 2004

Inferring Other Information: Segmentation

Combined object detection and segmentation using an implicit shape model. Image patches cast weighted votes for the object centroid.



B. Leibe, A. Leonardis, and B. Schiele, Combined Object Categorization and Segmentation with an Implicit Shape Model, ECCV Workshop on Statistical Learning in Computer Vision 2004



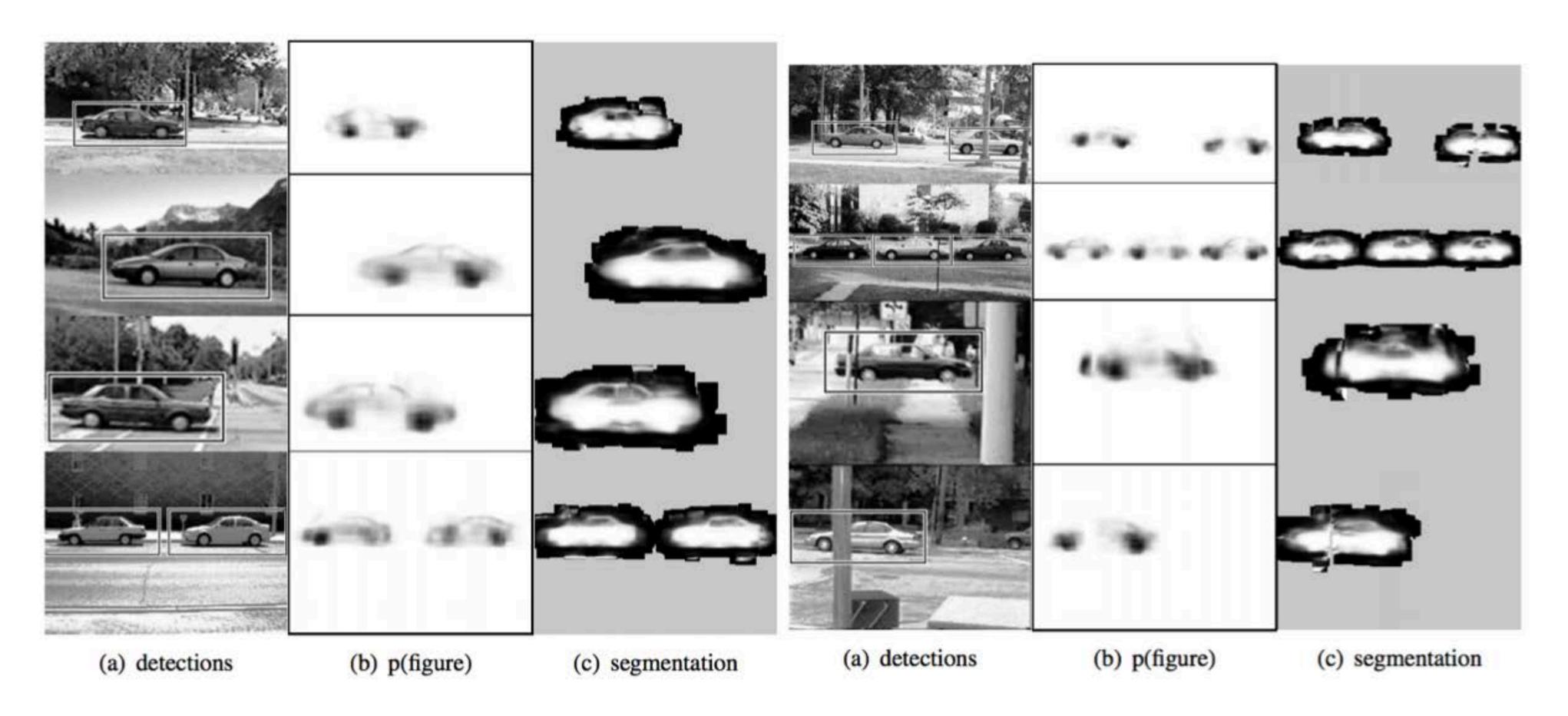




lmage Index	Keypoint Index	Keypoint Detection (4D)	Keypoint Description (128D)	Offset to Centroid	Segme
lmage 1 lmage 1	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y] [x,y]	
Image 1	265	[x, y, s, Theta]	 []	[x,y]	
Image 2 Image 2	1 2	[x, y, s, Theta] [x, y, s, Theta]		[x,y] [x,y]	
Image 2	645	[x, y, s, Theta]	[]	[x,y]	
Image K Image K	1 2	[x, y, s, Theta] [x, y, s, Theta]	[] []	[x,y] [x,y]	
Image K	134	[x, y, s, Theta]	 []	[x,y]	

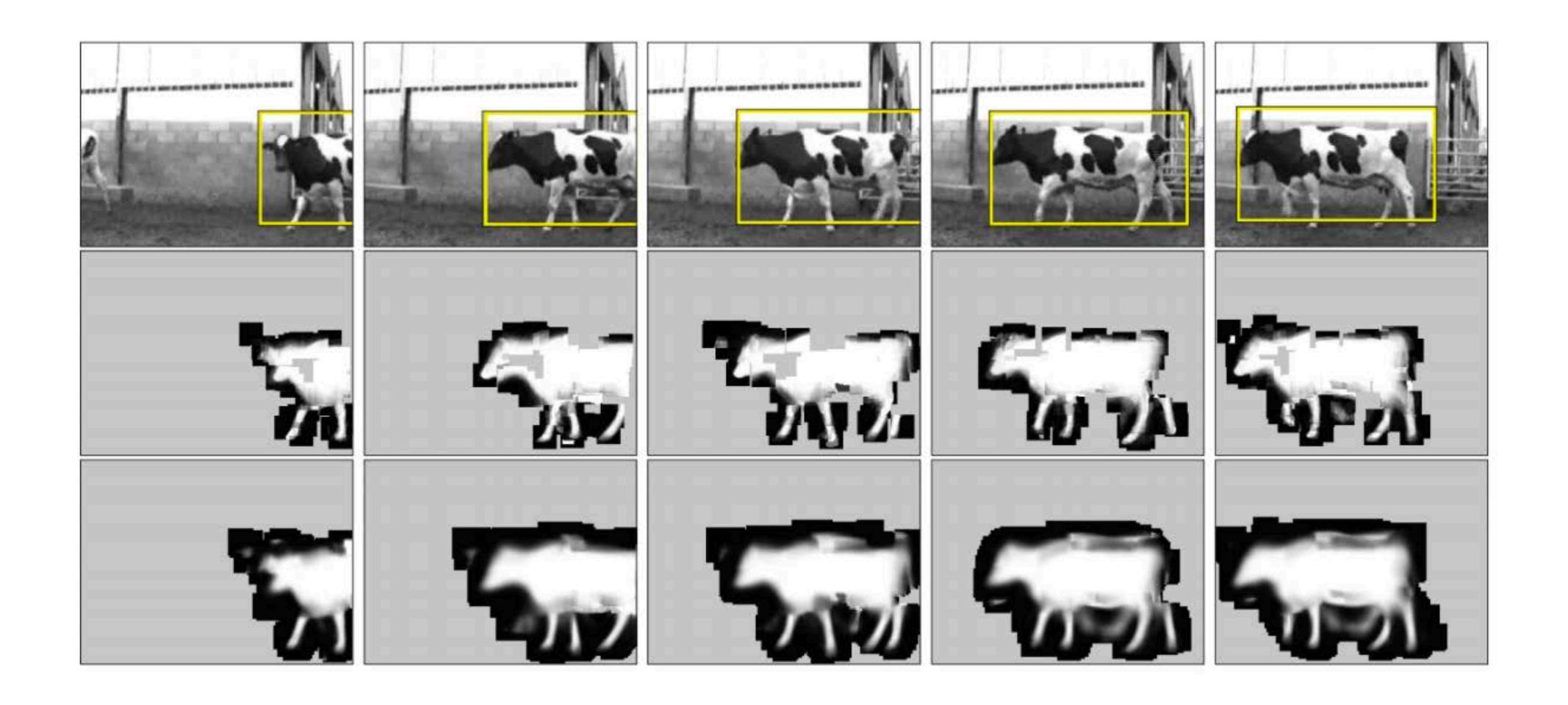
Inferring Other Information: Segmentation

Idea: When back-projecting, back-project labeled segmentations per training patch



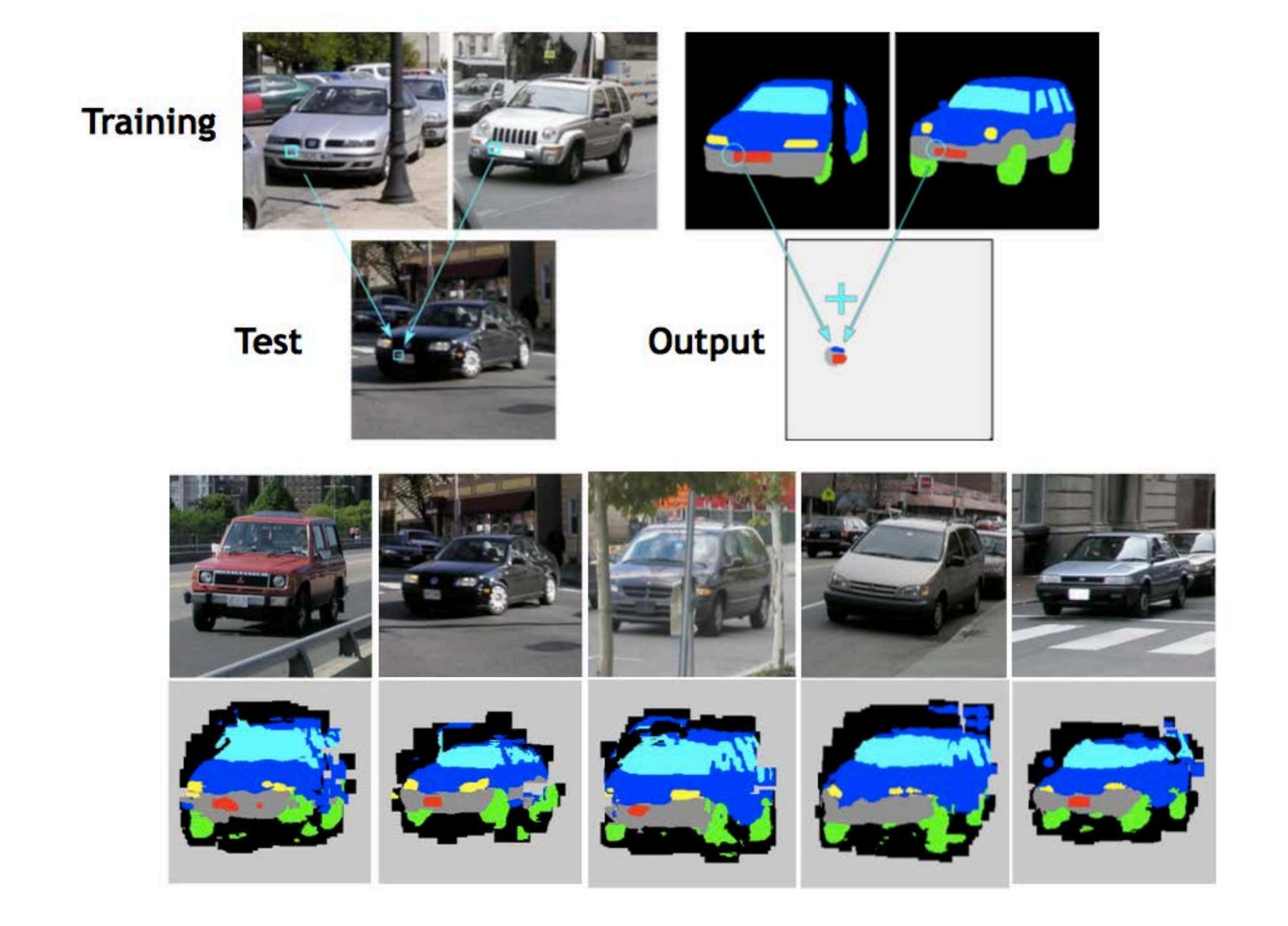
[Source: B. Leibe]

Inferring Other Information: Segmentation

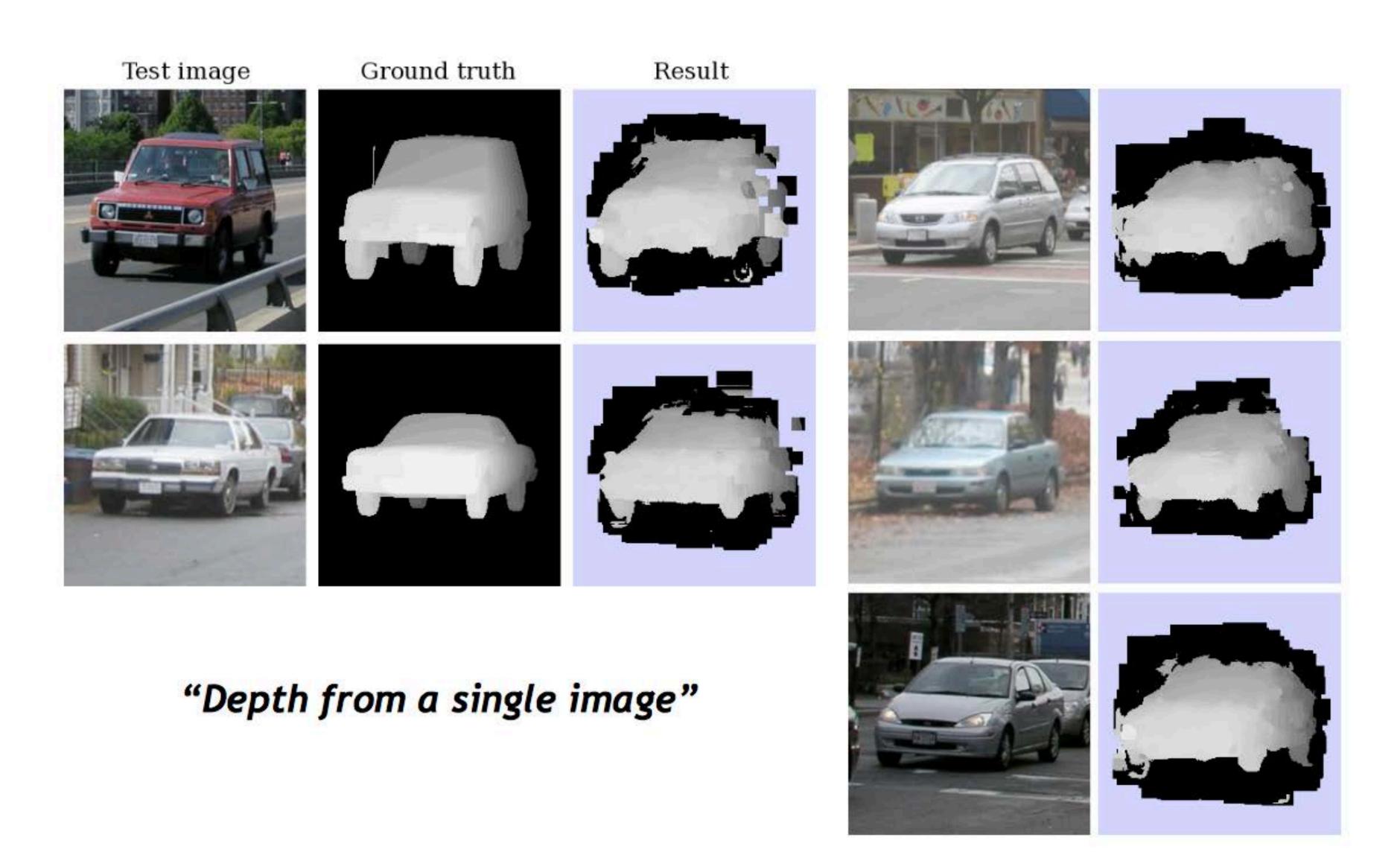


[Source: B. Leibe]

Inferring Other Information: Part Labels



Inferring Other Information: Depth



Example 2: Object Recognition — Boundary Fragments

Boundary fragments cast weighted votes for the object centroid. Also obtains an estimate of the object's contour.

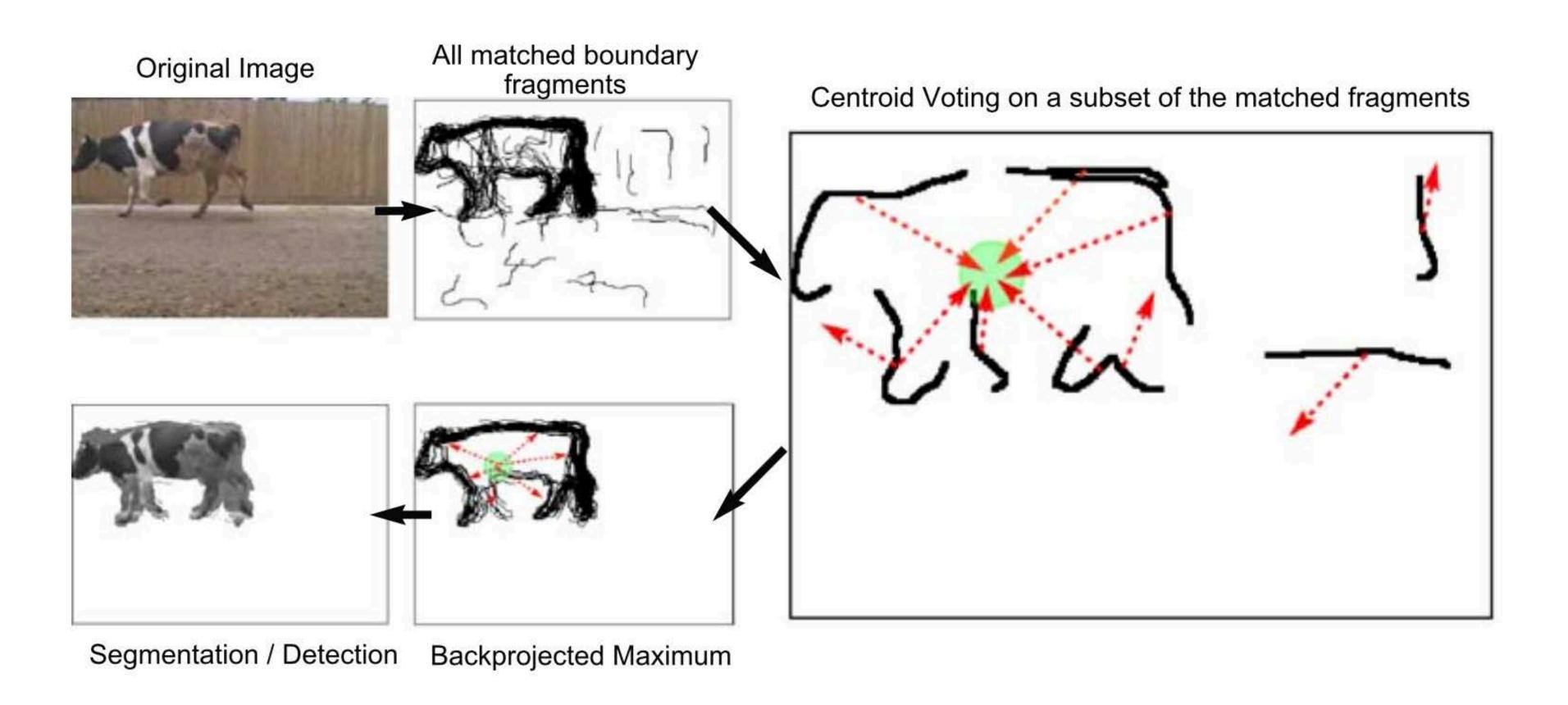


Image credit: Opelt et al., 2006

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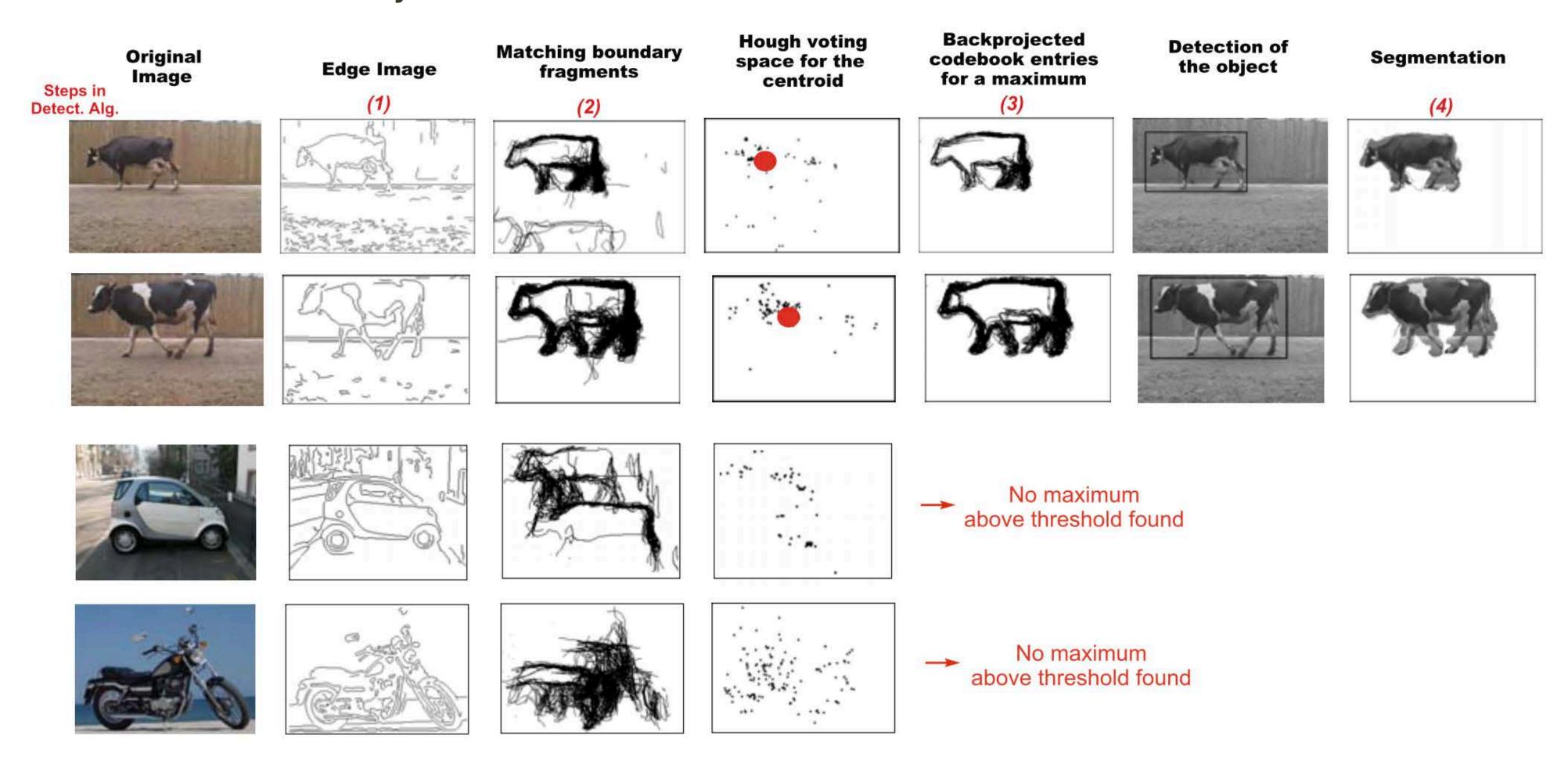


Image credit: Opelt et al., 2006

Example 3: Deep Hough Voting

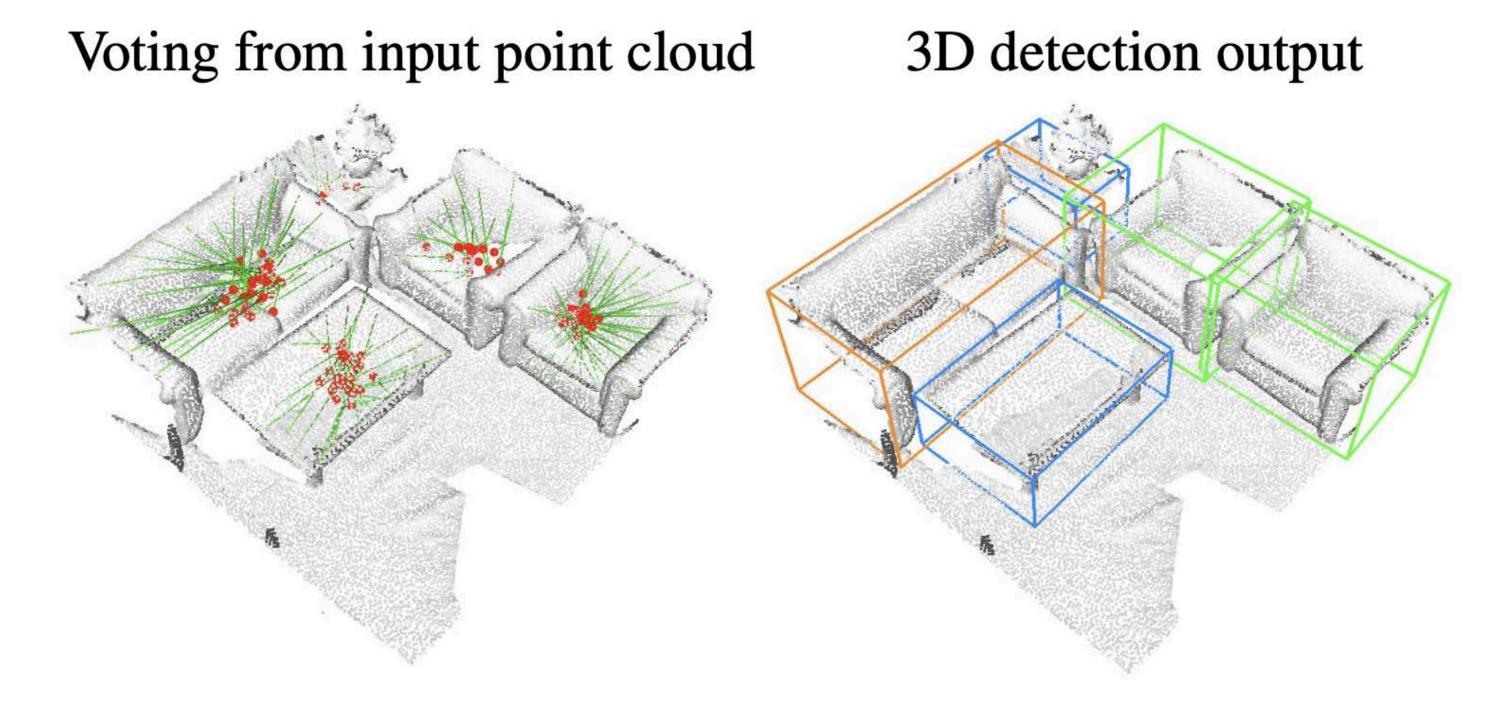


Figure 1. 3D object detection in point clouds with a deep Hough voting model. Given a point cloud of a 3D scene, our VoteNet votes to object centers and then groups and aggregates the votes to predict 3D bounding boxes and semantic classes of objects.

Summary of Hough Transform

Idea of Hough transform:

- For each token vote for all models to which the token could belong
- Return models that get many votes

e.g., For each point, vote for all lines that could pass through it; the true lines will pass through many points and so receive many votes

Advantages:

- Can handle high percentage of outliers: each point votes separately
- Can detect multiple instances of a model in a single pass

Disadvantages:

- Search time increases exponentially with the number of model parameters
- Can be tricky to pick a good bin size