

Sept 14, 2015

p4

Homework

Should ~~have~~ a rule

1

2

End of class: vote: proj vs. board

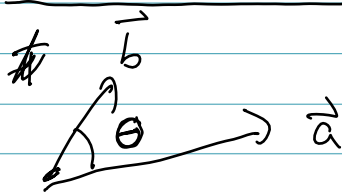
Homework this week: on common course webpage
=

12.1: Idea: if something is hard to understand in 3-d, try 2-d or 1-d.

12.2: Vectors:

E.g. $\langle 2, 1 \rangle$ in 2-d

$\langle -1, 3, 0 \rangle$ in 3-d



6

$$\vec{a} \cdot \vec{b} = |\vec{a}| \cdot |\vec{b}| \cdot (\cos \theta)$$

=

$\vec{a} \perp \vec{b}$ if

(1) $\vec{a} \cdot \vec{b} = 0$

(2) $\theta = \pm 90^\circ$



orthogonal, perpendicular

This week 12.3, 12.4

5

In 12.3 we will see why unit vectors are useful...

12.3 Dot Product:

$$\vec{a} \cdot \vec{b} = \langle a_1, a_2, a_3 \rangle \cdot \langle b_1, b_2, b_3 \rangle$$

$$= a_1 b_1 + a_2 b_2 + a_3 b_3$$

$$\langle 1, 2, 3 \rangle \cdot \langle 4, 5, 6 \rangle$$

$$= \langle 1 \cdot 4, 2 \cdot 5, 3 \cdot 6 \rangle = \langle 4, 10, 18 \rangle$$

$$= 4 + 10 + 18 = 14 + 18 = 32$$

[4]

$$\text{Force, Velocity} = \frac{\text{Displacement}}{\text{Time}}$$

$$|\langle a_1, a_2 \rangle| = \sqrt{a_1^2 + a_2^2}$$

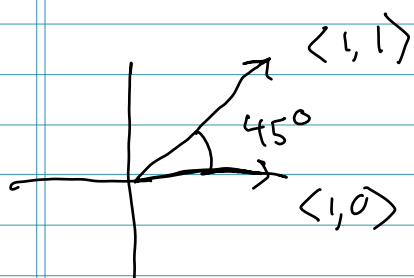
$$|\langle a_1, a_2, a_3 \rangle| = \sqrt{a_1^2 + a_2^2 + a_3^2}$$

Vector \vec{a} , unique unit vector

$$\vec{u} = \vec{a} / |\vec{a}| \text{ which}$$

① points in the dir. of \vec{a}

② has length 1.



$$\cos(45^\circ) = 1/\sqrt{2}$$

... ?

$$|\langle 1, 0 \rangle| = 1$$

$$|\langle 1, 1 \rangle| = \sqrt{1+1} = \sqrt{2}$$

$$\langle 1, 0 \rangle \cdot \langle 1, 1 \rangle = 1 \cdot 1 + 0 \cdot 1 = 1$$

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$$

[3]

Should have a reasonable to add & scale vectors:

$$\begin{aligned} \langle 1, 2 \rangle + \langle 3, 4 \rangle &= \langle 1+3, 2+4 \rangle \\ &= \langle 4, 6 \rangle \end{aligned}$$

$$5 \cdot \langle 1, 2 \rangle = \langle 5, 10 \rangle$$

Displacement!

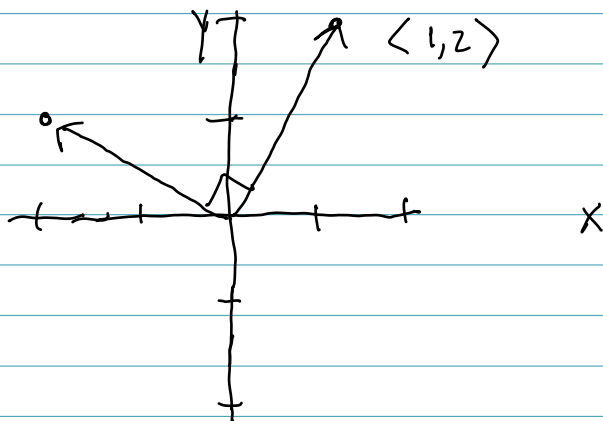
$$\begin{aligned} &\text{from } (3, 9) \text{ to } (7, 1) \\ &+ \langle 4, -8 \rangle \rightsquigarrow \langle 4, -8 \rangle \end{aligned}$$

[8]

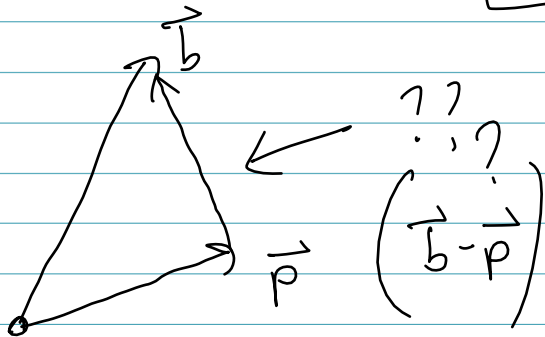
$$\langle 1, 2 \rangle \cdot \langle -2, 1 \rangle$$

$$= (1)(-2) + (2)(1) = -2 + 2 = 0$$

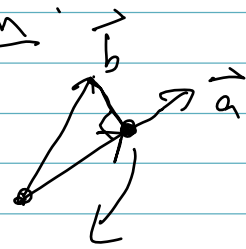
$$\langle 1, 2 \rangle \perp \langle -2, 1 \rangle$$



[7]

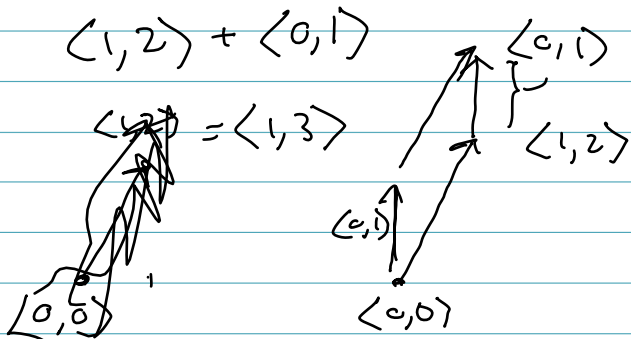


Projection:



$\text{proj}_{\vec{a}} \vec{b}$ = "part of \vec{b} can be explained by \vec{a} "

= closest vector to \vec{b} that points in the direction of \vec{a}



$\langle 1, 2 \rangle + \langle 0, 1 \rangle = \langle 1+0, 2+1 \rangle = \langle 1, 3 \rangle = \langle 0, 1 \rangle + \langle 1, 2 \rangle$

