GROUP HOMEWORK 4, CPSC 421/501, FALL 2025

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Please note:

- (1) You must justify all answers; no credit is given for a correct answer without justification.
- (2) Proofs should be written out formally.
- (3) You do not have to use LaTeX for homework, but homework that is too difficult to read will not be graded.
- (4) You may work together on homework in groups of up to four, but you must submit a single homework as a group submission under Gradescope.
- (0) Who are your group members? Please print if writing by hand.
- (1) Let VALID-PYTHON be the set of ASCII strings that are valid Python programs. L be the language

$$L = \{ p \in \text{VALID-PYTHON} \mid p \text{ accepts at least one input} \},$$

i.e.,

 $L = \{ p \in \text{VALID-PYTHON} \mid \exists i \in \text{ASCII}^* \text{ such that } p \text{ accepts } i \}.$

- (a) Show that L is recognizable.
- (b) Show that L is undecidable. [Hint: assume that L is decidable. Consider class notes 09 17, pages 8–10.]
- (2) In class we discussed how to run a finite number of Python programs "in parallel." Say that $p_1, p_2, \ldots \in ASCII^*$ is an infinite sequence of (valid) Python programs. Let
- (1) $L = \{i \in ASCII^* \mid \exists j \in \mathbb{N} \text{ such that } p_j \text{ accepts } i\}$
 - (a) Show that L is recognizable.
 - (b) Show that there exist programs p_1, p_2, \ldots such that L as in (1) is undecidable. [Hint: Assume that L is decidable; use the decidability of L to decide ACCEPTANCE.]

- (3) Exercise 9.3.1 on the handout "Uncomputability in CPSC421/501."
- (4) Exercise 9.3.2(b) on the handout "Uncomputability in CPSC421/501."

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