

GROUP HOMEWORK 9, CPSC 421/501, FALL 2021

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Please note:

- (1) You must justify all answers; no credit is given for a correct answer without justification.
- (2) Proofs should be written out formally.
- (3) Homework that is difficult to read may not be graded.
- (4) You may work together on homework in groups of up to four, **but you must submit a single homework as a group submission under Gradescope.**

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- (1) Problem 8.7.2(a) of the handout Uncomputability OR Ruining the Suprises in CPSC421.
 - (2) Problem 8.7.3 of the handout Uncomputability OR Ruining the Suprises in CPSC421; you can summarize the main points, since this is easy once you get used to working with oracle Turing machines.
 - (3) Problem 8.7.4 of the handout Uncomputability OR Ruining the Suprises in CPSC421.
 - (4) Show that if a connected graph has no odd length cycles, then it can be (legally) 2-coloured.
 - (5) Problem 7.8 [Sip]: show that the language, CONNECTED, of (descriptions of standardized) undirected graphs that are connected can be decided by a Turing machine in polynomial time; you may use the algorithm in [Sip], or any other algorithm that works.

Bonus problem worth additional an additional 20%, and solutions will not be released:

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- (6) Let $M = (Q, \Sigma, \Gamma, \delta, q_0, q_{\text{acc}}, q_{\text{rej}})$ be a Turing machine that (1) is a decider (i.e., always halts in either the accept or reject state), and (2) cannot change the contents of any of its tape cells, in the sense that for all $q \in Q$ and $\gamma \in \Gamma$, if

$$\delta(q, \gamma) = (q', \gamma', \mu),$$

so that $q' \in Q$, $\gamma' \in \Gamma$, $\sigma \in \Sigma$, $\mu \in \{L, R\}$, then necessarily $\gamma' = \gamma$. Show that the language that M decides is a regular language. [Problem courtesy of Ryan Mansour, November 2021.]

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