

GROUP HOMEWORK 7, CPSC 421/501, FALL 2020

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Please note:

- (1) You must justify all answers; no credit is given for a correct answer without justification.
- (2) Proofs should be written out formally.
- (3) Homework that is difficult to read may not be graded.
- (4) You may work together on homework in groups of up to four, **but you must submit a single homework as a group submission under Gradescope.**

(1) Let

$L = \{\langle M \rangle \mid M \text{ is a Turing machine that accepts at least one of its inputs}\}.$

- (a) Use the fact that A_{TM} is undecidable to prove that L is undecidable: assume that L is decidable by some (Turing machine) algorithm, and explain how you can use this algorithm as a subroutine to decide A_{TM} . [On 10_22 we proved that HALT_{TM} was undecidable by a similar method.]
 - (b) Is L recognizable? Explain.
 - (c) Is the complement of L recognizable? Explain.
- (2) Is NP closed under concatenation? Explain.
 - (3) Is NP closed under intersection? Explain.
 - (4) Show that if $P = NP$, then the complement of SAT lies in NP. [As of today, we do not know whether or not the complement of SAT lies in NP.]

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