GROUP HOMEWORK 5, CPSC 421/501, FALL 2020

JOEL FRIEDMAN

Copyright: Copyright Joel Friedman 2020. Not to be copied, used, or revised without explicit written permission from the copyright owner.

Please note:

- (1) You must justify all answers; no credit is given for a correct answer without justification.
- (2) Proofs should be written out formally.
- (3) Homework that is difficult to read may not be graded.
- (4) You may work together on homework in groups of up to four, **but you** must submit a single homework as a group submission under Gradescope.

(1) (a) Let L be a regular language over Σ , and let $w \in \Sigma$. Show that $L \cup \{w\}$ is regular.

(b) Let L be a regular language over Σ , and let $w \in \Sigma$. Show that $L \setminus \{w\}$ is regular.

(c) Let L be a nonregular language over Σ , and let $w \in \Sigma$. Show that $L \cup \{w\}$ is nonregular.

(d) Let L be a nonregular language over Σ , and let $w \in \Sigma$. Show that $L \setminus \{w\}$ is nonregular.

(2) Prove the following statements, or prove that they are false by giving a counterexample.

(a) The union of two regular languages is regular.

(b) The union of two nonregular languages is regular.

(c) The union of a nonregular language and a regular language is nonregular

(d) The concatenation of a nonregular language and a regular language is nonregular.

(3) Give a formal description (by a state diagram, or table of δ values, or a list of δ values) of a Turing machine that recognizes the language over $\Sigma = \{0, 1\}$ given by

 $L = \{w \in \{0,1\}^* \mid w \text{ has more 0's than 1's}\}.$

Make sure to explain how your machine works, and what each state "means" in terms of your algorithm; make sure that it is clear what are the values of $Q, \Gamma, q_0, q_{\text{accept}}, q_{\text{reject}}$.

Department of Computer Science, University of British Columbia, Vancouver, BC V6T 1Z4, CANADA.

E-mail address: jf@cs.ubc.ca URL: http://www.cs.ubc.ca/~jf