

## INDIVIDUAL HOMEWORK 3, CPSC 421/501, FALL 2020

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Please note:

- (1) You must justify all answers; no credit is given for a correct answer without justification.
- (2) Proofs should be written out formally.
- (3) Homework that is difficult to read may not be graded.
- (4) You may work together on homework in groups of up to four, **but you must write up your own solutions individually and must acknowledge with whom you worked.** You must also acknowledge any sources you have used beyond the textbook and two articles on the class website.

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- (1) Build a DFA that recognizes the language

$$L = \{w \in \{a, b\}^* \mid w \text{ has } aab \text{ as a substring}\},$$

and explain how your DFA works.

- (2) Build an NFA with three states that recognizes the language  $L = \{aa, aaa, ab\}^*$  and explain how your NFA works.

**Bonus Question, Worth an Extra 10 out of 100 Points for Homework 2**

[Solutions to this problem will not be released. Bonus questions tend to be more difficult than the usual course material and will not appear on any exam.]

(3) Give a bijection  $f: [2]^{\mathbb{N}} \rightarrow [3]^{\mathbb{N}}$  (and explain/prove that  $f$  is a bijection). [Recall that if  $S, T$  are sets,  $T^S$  refers to the set of functions from  $S$  to  $T$ .]

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