CPSC 340: Machine Learning and Data Mining

Convolutional Neural Networks Fall 2020

Admin – Final Lectures

- Exam to appear at 5pm Monday on course website.
 - Roughly the same format as the midterm
 - Due at midnight
- I will finish the "testable content" of the course today.
- Monday/Wednesday
 - Automatic differentiation
 - Presentations from project teams

Last Lectures: Deep Learning

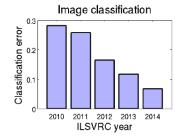
We've been discussing neural network / deep learning models:

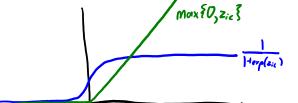
$$y_{i} = V^{T} h(W^{(n)} h(W^{(m-1)} h(----W^{(2)} h(W^{(1)} x_{i})) \cdots))$$

- We discussed unprecedented vision/speech performance.
- We discussed methods to make SGD work better:
 - Parameter initialization and data transformations.



Alternative non-linear functions like ReLU.





"Residual" Networks (ResNets)

Impactful recent idea is residual networks (ResNets):

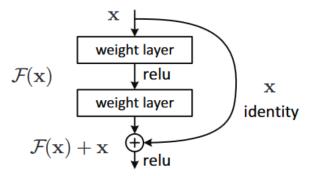


Figure 2. Residual learning: a building block.

- You can take previous (non-transformed) layer as input to current layer.
 - Also called "skip connections" or "highway networks".
- Non-linear part of the network only needs to model residuals.
 - Non-linear parts are just "pushing up or down" a linear model in various places.
- This was a key idea behind first methods that used 100+ layers.
 - Evidence that biological networks have skip connections like this.

DenseNet

- More recent variation is "DenseNets":
 - Each layer can see all the values from many previous layers.
 - Gets rid of vanishing gradients.
 - May get same performance with fewer parameters/layers.

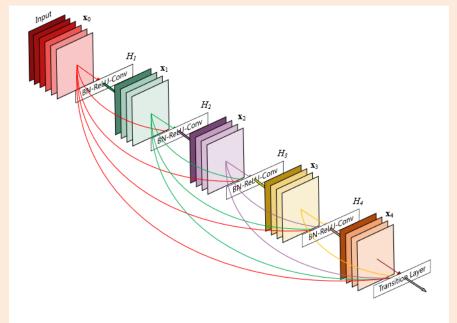


Figure 1: A 5-layer dense block with a growth rate of k=4. Each layer takes all preceding feature-maps as input.

https://arxiv.org/pdf/1512.03385v1.pdf

Deep Learning and the Fundamental Trade-Off

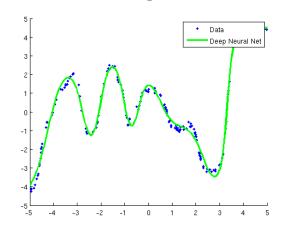
- Neural networks are subject to the fundamental trade-off:
 - With increasing depth, training error of global optima decreases.
 - With increasing depth, training error may poorly approximate test error.
- We want deep networks to model highly non-linear data.
 - But increasing the depth can lead to overfitting.
- How could GoogLeNet use 22 layers?
 - Many forms of regularization and keeping model complexity under control.
 - Unlike linear models, typically use multiple types of regularization.

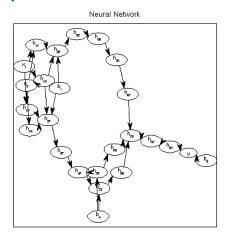
Standard Regularization

Traditionally, we've added our usual L2-regularizers:

$$f(v_1 W_1^{(3)} W_1^{(2)}) W_1^{(2)}) = \frac{1}{2} \sum_{i=1}^{8} \left(v_1 h(W_1^{(3)} h(W_1^{(2)} h(W_1^{(1)} x_i))) - y_i \right)^2 + \frac{1}{2} ||w_1^{(2)}||_F^2 + \frac{1}{2} ||w_1^{(2$$

- L2-regularization often called "weight decay" in this context.
 - Could also use L1-regularization: gives sparse network.





Standard Regularization

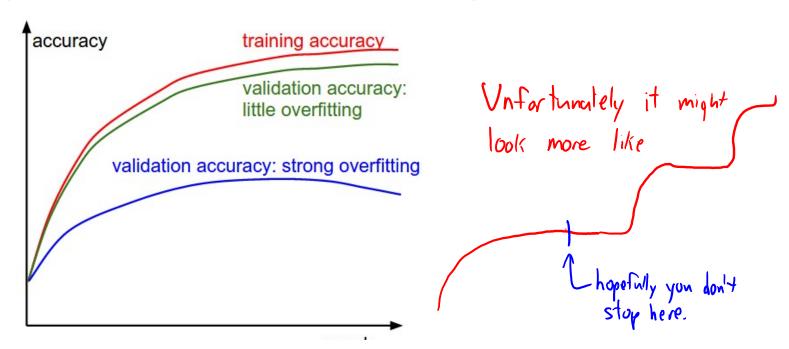
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- L2-regularization often called "weight decay" in this context.
 - Could also use L1-regularization: gives sparse network.
- Hyper-parameter optimization gets expensive:
 - Try to optimize validation error in terms of λ_1 , λ_2 , λ_3 , λ_4 .
 - In addition to step-size, number of layers, size of layers, initialization.
- Recent result:
 - Adding a regularizer in this way creates bad local optima.

Early Stopping

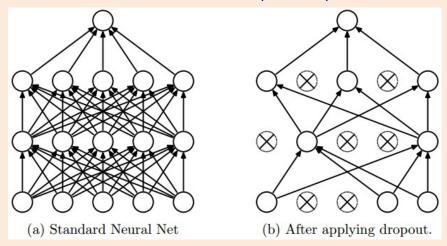
- Another common type of regularization is "early stopping":
 - Monitor the validation error as we run stochastic gradient.
 - Stop the algorithm if validation error starts increasing.



http://cs231n.github.io/neural-networks-3/

Dropout

- Dropout is a more recent form of explicit regularization:
 - On each iteration, randomly set some x_i and z_i to zero (often use 50%).

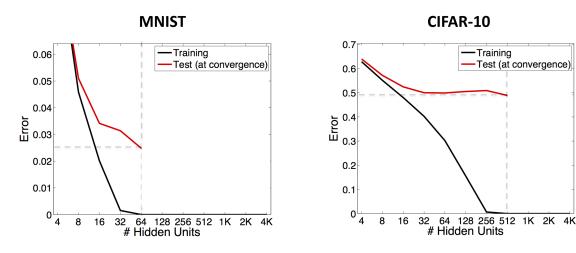


- Adds invariance to missing inputs or latent factors
 - Encourages distributed representation rather than relying on specific z_i.
- Can be interpreted as an ensemble over networks with different parts missing.
- After a lot of success, dropout may already be going out of fashion.

http://www.cs.toronto.edu/~rsalakhu/papers/srivastava14a.pdf

"Hidden" Regularization in Neural Networks

Fitting single-layer neural network with SGD and no regularization:

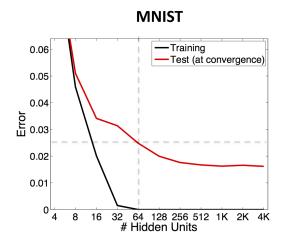


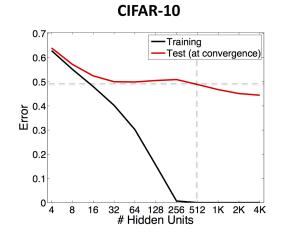
- Training goes to 0 with enough units: we're finding a global min.
- What should happen to training and test error for larger #hidden?

https://www.neyshabur.net/papers/inductive_bias_poster.pdf

"Hidden" Regularization in Neural Networks

Fitting single-layer neural network with SGD and no regularization:





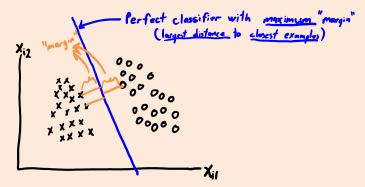
- Test error continues to go down!?! Where is fundamental trade-off??
- There exist global mins with large #hidden units have test error = 1.
 - But among the global minima, SGD is somehow converging to "good" ones.

Implicit Regularization of SGD

- There is growing evidence that using SGD regularizes parameters.
 - We call this the "implicit regularization" of the optimization algorithm.
- Beyond empirical evidence, we know this happens in simpler cases.
- Example of implicit regularization:
 - Consider a least squares problem where there exists a 'w' where Xw=y.
 - Residuals are all zero, we fit the data exactly.
 - You run [stochastic] gradient descent starting from w=0.
 - Converges to solution Xw=y that has the minimum L2-norm.
 - So using SGD is equivalent to L2-regularization here, but regularization is "implicit".

Implicit Regularization of SGD

- Example of implicit regularization:
 - Consider a logistic regression problem where data is linearly separable.
 - We can fit the data exactly.
 - You run gradient descent from any starting point.
 - Converges to max-margin solution of the problem.
 - So using gradient descent is equivalent to encouraging large margin.



Similar result known for boosting.

(pause)

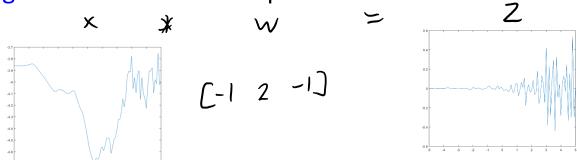
Deep Learning "Tricks of the Trade"

- We've discussed heuristics to make deep learning work:
 - Parameter initialization and data transformations.
 - Setting the step size(s) in stochastic gradient and using momentum.
 - RestNets and alternative non-linear functions like ReLU.
 - Different forms of regularization:
 - L2-regularization, early stopping, dropout, implicit regularization from SGD.
- These are often still not enough to get deep models working.
- Deep computer vision models are all convolutional neural networks:
 - The W^(m) are very sparse and have repeated parameters ("tied weights").
 - Drastically reduces number of parameters (speeds training, reduces overfitting).

1D Convolution as Matrix Multiplication

• 1D convolution:

– Takes signal 'x' and filter 'w' to produces vector 'z':



— Can be written as a matrix multiplication:

1D Convolution as Matrix Multiplication

Each element of a convolution is an inner product:

$$Z_{i} = \sum_{j=-m}^{m} w_{j} \times_{i + j}$$

$$= w^{T} \times_{(i-m':j+m)}$$

$$= \widetilde{w}^{T} \times \text{ where } \widetilde{w} = [0 \ 0 \ 0 \]$$

So convolution is a matrix multiplication (I'm ignoring boundaries):

$$z = W_x$$
 where $W = \begin{bmatrix} 0 & w & w & 0 & 0 & 0 \\ 0 & 0 & w & w & w & 0 & 0 \\ 0 & 0 & 0 & w & w & w & w & 0 & 0 \end{bmatrix}$ matrix can be very sparse and only has $2m+1$ variables.

The shorter 'w' is, the more sparse the matrix is.

2D Convolution as Matrix Multiplication

2D convolution:

— Signal 'x', filter 'w', and output 'z' are now all images/matrices:

$$x + w = z$$



$$\begin{bmatrix} -2 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix}$$



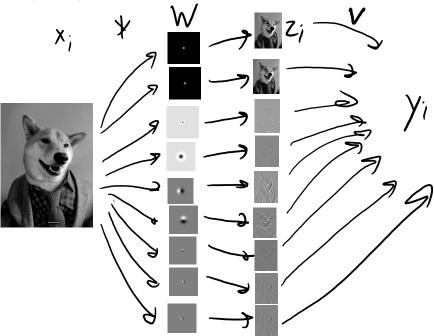
– Vectorized 'z' can be written as a matrix multiplication with vectorized 'x':

- Consider training neural networks on 256 by 256 images.
 - This is 256 by 256 by $3 \approx 200,000$ inputs.
- If first layer has k=10,000, then it has about 2 billion parameters.
 - We want to avoid this huge number (due to storage and overfitting).
- Key idea: make Wx_i act like several convolutions (to make it sparse):
 - 1. Each row of W only applies to part of x_i .

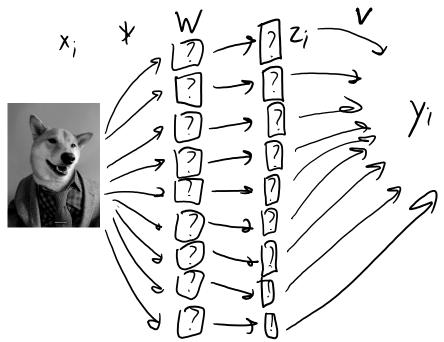
1. Each row of W only applies to part of
$$x_i$$
.
2. Use the same parameters between rows. $w_i = [0 \ 0 \ 0 \ w_i = [0 \ 0 \ 0 \ w]$

Forces most weights to be zero, reduces number of parameters.

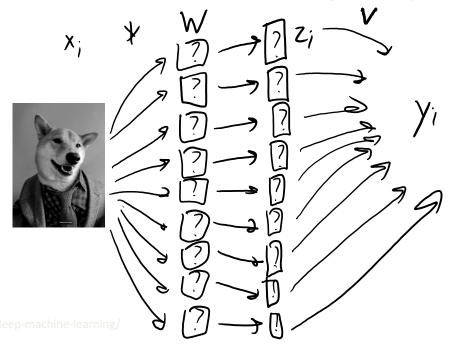
- Classic vision methods uses fixed convolutions as features:
 - Usually have different types/variances/orientations.
 - Can do subsampling or take maxes across locations/orientations/scales.

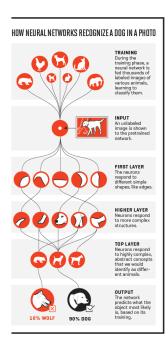


- Convolutional neural networks learn the convolutions:
 - Learning 'W' and 'v' automatically chooses types/variances/orientations.
 - Don't pick from fixed convolutions, but learn the elements of the filters.



- Convolutional neural networks learn the convolutions:
 - Learning 'W' and 'v' automatically chooses types/variances/orientations.
 - Can do multiple layers of convolution to get deep hierarchical features.





- Convolutional Neural Networks classically have 3 layer "types":
 - Fully connected layer: usual neural network layer with unrestricted W.

$$W^{(n)} = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

$$\vdots \\ w_k \end{bmatrix}$$

- Convolutional Neural Networks classically have 3 layer "types":
 - Fully connected layer: usual neural network layer with unrestricted W.
 - Convolutional layer: restrict W to act like several convolutions.

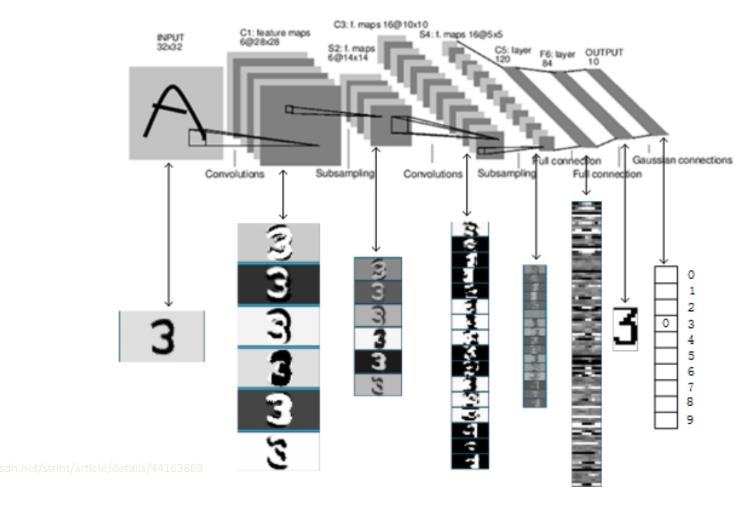
- Convolutional Neural Networks classically have 3 layer "types":
 - Fully connected layer: usual neural network layer with unrestricted W.
 - Convolutional layer: restrict W to act like several convolutions.
 - Pooling layer: combine results of convolutions.
 - Can add some invariance or just make the number of parameters smaller.

• Usual choice is 'max pooling':

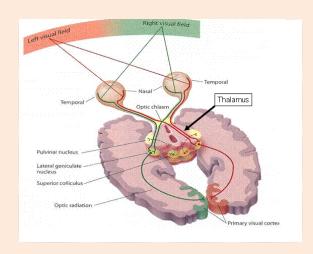
2:

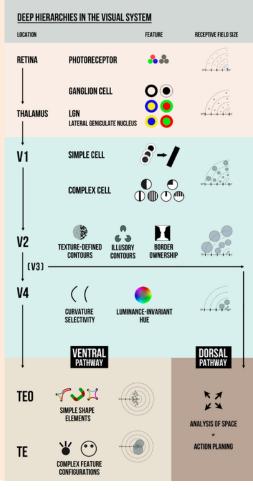
Maximums
over 2x2
reighbourhoods 5 3

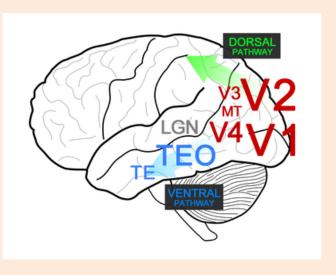
LeNet for Optical Character Recognition



Deep Hierarchies in the Visual System

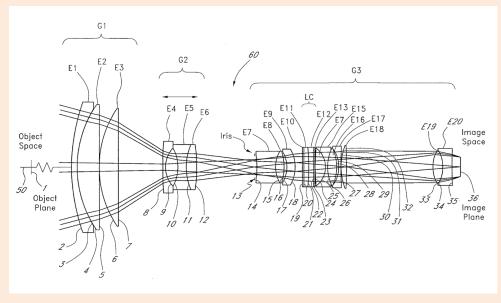


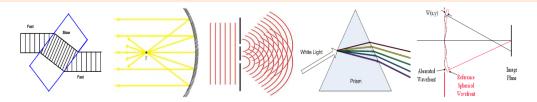




http://www.strokenetwork.org/newsletter/articles/vision.htm https://en.wikibooks.org/wiki/Sensory_Systems/Visual_Signal_Processing

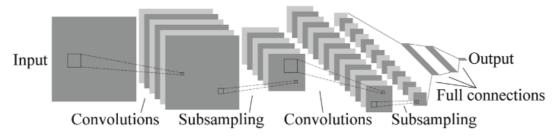
Deep Hierarchies in Optics





http://www.argmin.net/2018/01/25/optics/

Classic convolutional neural network (LeNet):



Visualizing the "activations" of the layers:

- http://scs.ryerson.ca/~aharley/vis/conv
- http://cs231n.stanford.edu



Summary

- ResNets include untransformed previous layers.
 - Network focuses non-linearity on residual, allows huge number of layers.
- Regularization is crucial to neural net performance:
 - L2-regularization, early stopping, dropout, implicit regularization of SGD.
- Convolutional neural networks:
 - Restrict W^(m) matrices to represent sets of convolutions.
 - Often combined with max (pooling).
- Next time: automatic differentiation

(End of testable content for final exam)

CPSC 340: Overview

- 1. Intro to supervised learning (using counting and distances).
 - Training vs. testing, parametric vs. non-parametric, ensemble methods.
 - Fundamental trade-off, no free lunch, universal consistency.
- 2. Intro to unsupervised learning (using counting and distances).
 - Clustering, outlier detection, finding similar items.
- 3. Linear models and gradient descent (for supervised learning)
 - Loss functions, change of basis, regularization, feature selection.
 - Gradient descent and stochastic gradient.
- 4. Latent-factor models (for unsupervised learning)
 - Typically using linear models and gradient descent.
- 5. Neural networks (for supervised and multi-layer latent-factor models).

Topics from Previous Years

- Slides for other topics that were covered in previous years:
 - Ranking: finding "highest ranked" training examples (Google PageRank).
 - Semi-supervised: using unlabeled data to help supervised learning.
 - Sequence mining: approximate matching of patterns in large sequences.
- In previous years we did a course review on the last day:
 - Overview of topics covered in 340, and topics coming in 540.
 - Slides here: this could help with studying for the final.

CPSC 330 vs. 340

- CPSC 330: "Applied Machine Learning".
 - Not intended as a sequel to 340 (or even a prequel).
- There is some overlap in content, but focus is different:
 - More emphasis on the other steps of the data processing pipeline:
 - Data cleaning, feature extraction, reproducible workflows, communicating results.
 - More emphasis of "how to use packages", less on "how stuff works".
- If you found 340 too hard to keep up with, 330 might make sense.
 - In this situation, tell your friends about 330.

CPSC 330 vs. 440

CPSC 440.

- Intended as a direct sequel to 340.
- We're basically starting with CNNs and going from there.

• Main focuses:

- What if y_i is a sentence or an image or a protein?
- Giving you the background to understand the latest advances.

• Prerequisites:

- Expect you to know everything in this course and CPSC 320.
- This course is now listed as CPSC 440.
 - I removed topics related to optimization research from the course.

CPSC 540 Topics

- Review of machine learning fundamentals.
- Differentiable programming and end-to-end learning.
- Density estimation and the exponential family.
- Conditional independence and Bayesian statistics.
- Markov and hidden-Markov models.
- Graphical models and deep structured models.
- Monte Carlo approximation and Markov chain Monte Carlo.
- Non-conjugate and hierarchical Bayesian models.
- Mixture models and expectation maximization.
- Variational inference.
- Empirical Bayes and advanced Monte Carlo methods.
- Non-parametric Bayes and deep generative models.

Other ML-Related Courses

- CPSC 406:
 - Numerical optimization algorithms (like gradient descent).
- CPSC 422:
 - Includes topics like time series and reinforcement learning.
- CPSC 440:
 - Probabilistic machine learning (a follow-on to this course).
- CPSC 532R/533R:
 - Deep learning for vision, sound, and language.
- CPSC 532W:
 - Probabilistic programming.
- CPSC 533V:
 - Deep learning for computer graphics.
- CPSC 540:
 - Graduate-level machine learning (usually with a focus on optimization theory)
- EECE 592:
 - Deep learning and reinforcement learning.
- STAT 406:
 - Similar/complementary topics.
- STAT 460/461:
 - Advanced statistical issues (what happens when 'n' goes to ∞?)

Final Slide

• Good luck with finals/projects and the next steps!