



Bidding in Second-Price Auctions

Game Theory Course: Jackson, Leyton-Brown & Shoham

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Second-Price



Theorem

Truth-telling is a dominant strategy in a second-price auction.

- In fact, we know this already (do you see why?)
- However, we'll look at a simpler, direct proof.

Second-Price proof

Theorem

Truth-telling is a dominant strategy in a second-price auction.

Proof.

Assume that the other bidders bid in some arbitrary way. We must show that *i*'s best response is always to bid truthfully. We'll break the proof into two cases:

- Bidding honestly, *i* would win the auction
- 2. Bidding honestly, *i* would lose the auction







• Bidding honestly, i is the winner

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- Bidding honestly, i is the winner
- If i bids higher, he will still win and still pay the same amount





- Bidding honestly, i is the winner
- If *i* bids higher, he will still win and still pay the same amount
- If *i* bids lower, he will either still win and still pay the same amount...



- Bidding honestly, i is the winner
- If *i* bids higher, he will still win and still pay the same amount
- If *i* bids lower, he will either still win and still pay the same amount...or lose and get utility of zero.





• Bidding honestly, i is not the winner





- Bidding honestly, i is not the winner
- If *i* bids lower, he will still lose and still pay nothing





- Bidding honestly, i is not the winner
- If *i* bids lower, he will still lose and still pay nothing
- If *i* bids higher, he will either still lose and still pay nothing...



- Bidding honestly, i is not the winner
- If *i* bids lower, he will still lose and still pay nothing
- If *i* bids higher, he will either still lose and still pay nothing...or win and pay more than his valuation.

English and Japanese auctions

- A much more complicated strategy space
 - extensive form game
 - bidders are able to condition their bids on information revealed by others
 - in the case of English auctions, the ability to place jump bids
- intuitively, though, the revealed information doesn't make any difference in the IPV setting.



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Theorem

Under the independent private values model (IPV), it is a dominant strategy for bidders to bid up to (and not beyond) their valuations in both Japanese and English auctions.



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