

# Intelligent Systems (AI-2)

## Computer Science cpsc422, Lecture 31

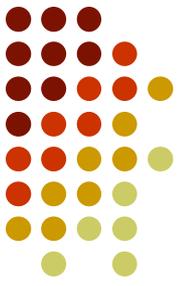
**March, 31, 2021**

**Slide source:** from Pedro Domingos UW & Markov Logic: An Interface Layer for Artificial Intelligence Pedro Domingos and Daniel Lowd University of Washington, Seattle

# Lecture Overview

- **MLN Recap**
- **Markov Logic: applications**
  - **Entity resolution**
  - **Statistical Parsing!**

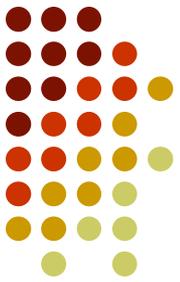
# Markov Logic: Definition



- A Markov Logic Network (MLN) is
  - a set of pairs  $(F, w)$  where
    - $F$  is a **formula** in first-order logic
    - $w$  is a **real number**
  - Together with a set  $C$  of **constants**,
- It defines a **Markov network** with
  - One *binary node* for each **grounding** of each **predicate** in the MLN
  - One *feature/factor* for each **grounding** of each **formula  $F$**  in the MLN, with the corresponding weight  $w$

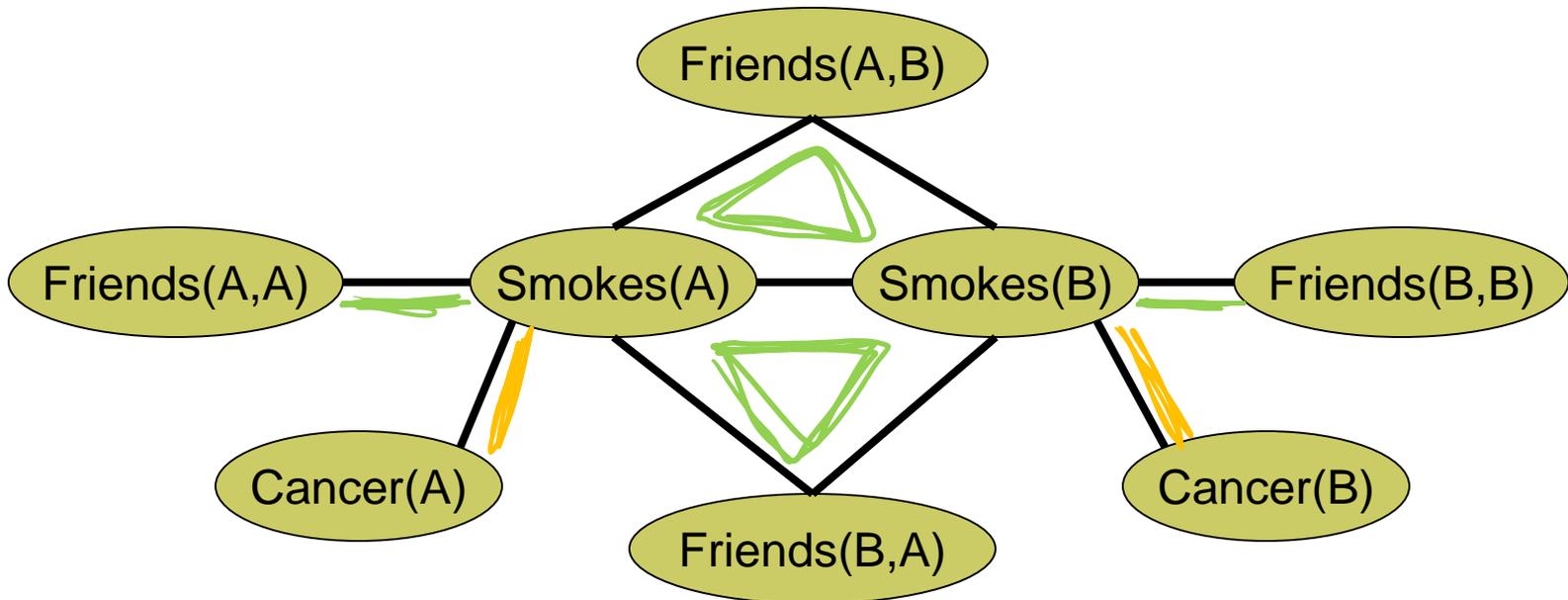
**Grounding:**  
substituting vars  
with constants

# MLN features

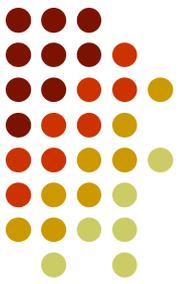


- 1.5  $\forall x \text{Smokes}(x) \Rightarrow \text{Cancer}(x)$
- 1.1  $\forall x, y \text{Friends}(x, y) \Rightarrow (\text{Smokes}(x) \Leftrightarrow \text{Smokes}(y))$

Two constants: **Anna** (A) and **Bob** (B)



# MLN: parameters



- For each grounded formula  $i$  we have a **factor**

$$\Phi_i(pw) = e^{w_i f_i(pw)}$$

← possible world

$w_i$  weight of formula

- Same for all the groundings of the same formula

$$f_i(pw) = \begin{cases} 1 & \text{when formula is true in } pw \\ 0 & \text{otherwise} \end{cases}$$

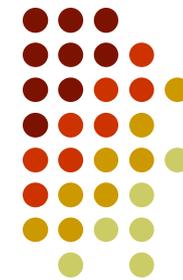
1.5  $\forall x \text{ Smokes}(x) \Rightarrow \text{Cancer}(x)$

$$f(\text{Smokes}(x), \text{Cancer}(x)) = \begin{cases} 1 & \text{if } \text{Smokes}(x) \Rightarrow \text{Cancer}(x) \\ 0 & \text{otherwise} \end{cases}$$

$pw_1$  ...  
 Smokes(A) T  
 Cancer(A) F  $e^0 = 1$

$pw_2$  ...  $e^{1.5}$   
 Smokes(A) T  
 Cancer(A) T

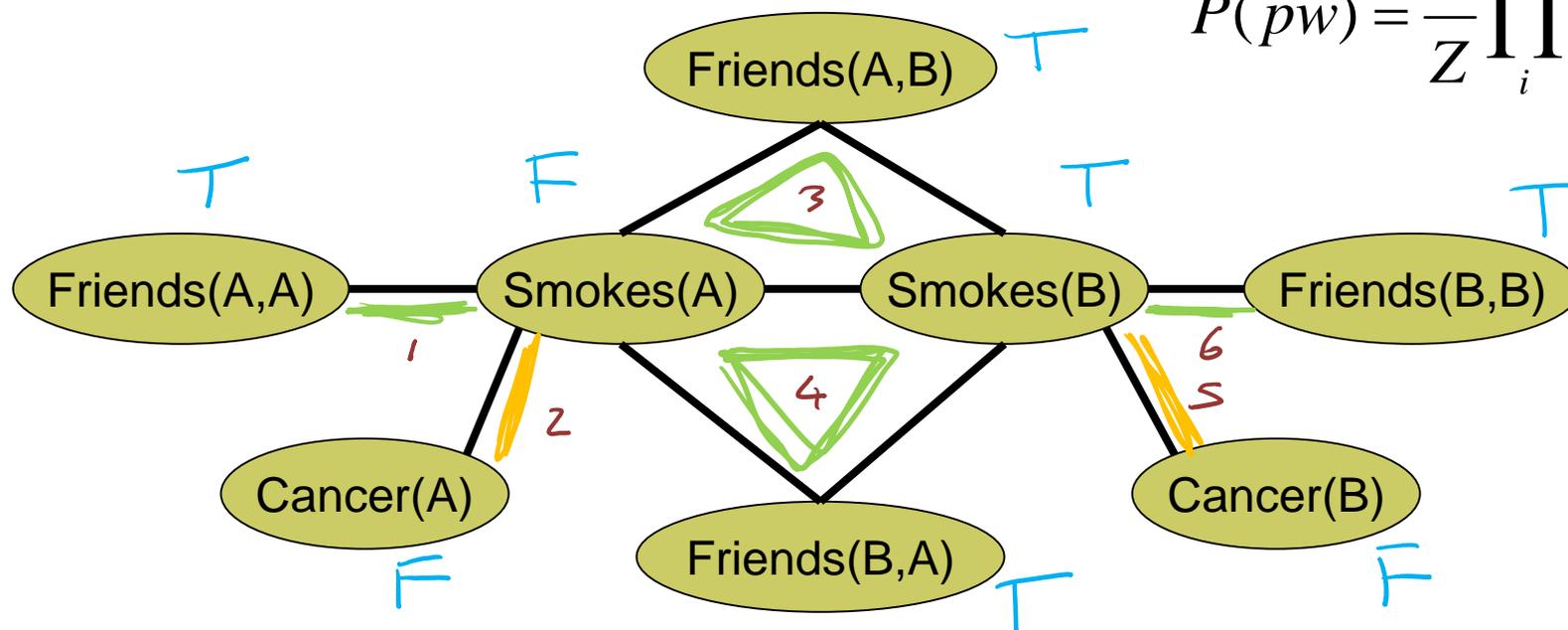
# MLN: prob. of possible world



- 1.5  $\forall x \text{ Smokes}(x) \Rightarrow \text{Cancer}(x)$
- 1.1  $\forall x, y \text{ Friends}(x, y) \Rightarrow (\text{Smokes}(x) \Leftrightarrow \text{Smokes}(y))$

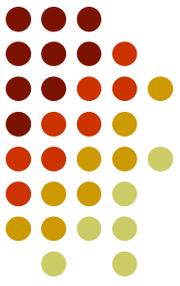
Two constants: **Anna** (A) and **Bob** (B)

$$P(pw) = \frac{1}{Z} \prod_i \Phi_i(pw)$$



$$P(pw) = \left( e^{1.1} * e^{1.1} * e^0 * e^0 * e^{1.5} * e^0 \right) / Z$$

# MLN: prob. Of possible world



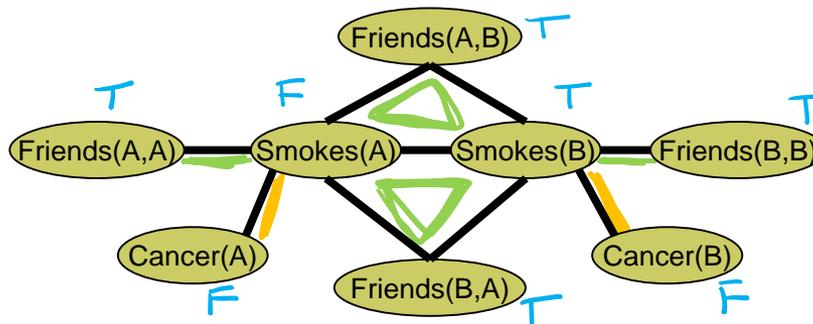
- ① 1.5  $\forall x \text{ Smokes}(x) \Rightarrow \text{Cancer}(x)$
- ② 1.1  $\forall x, y \text{ Friends}(x, y) \Rightarrow (\text{Smokes}(x) \Leftrightarrow \text{Smokes}(y))$

- Probability of a world  $pw$ :

$$P(pw) = \frac{1}{Z} \exp \left( \sum_i w_i n_i(pw) \right)$$

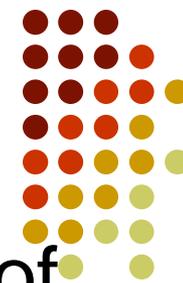
Weight of formula  $i$

No. of true groundings of formula  $i$  in  $pw$



$$P(pw) = \left( \underbrace{e^{1.1} * e^{1.1}}_{n_2(pw)=2} * e^0 * e^0 * \underbrace{e^{1.5} * e^0}_{n_1(pw)=1} \right)^{\frac{1}{Z}}$$

# Inference in MLN



- Most likely interpretation maximizes the sum of weights of satisfied formulas (MaxWalkSAT)

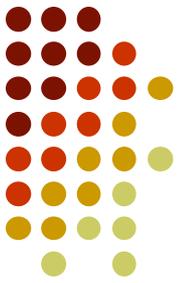
$$\arg \max_{pw} \sum_i w_i n_i(pw)$$

- P(**Formula**) = ? (Sampling interpretations)
- P(**ground literal** | **conjunction of ground literals**)...  
Gibbs sampling on relevant sub-network

# Lecture Overview

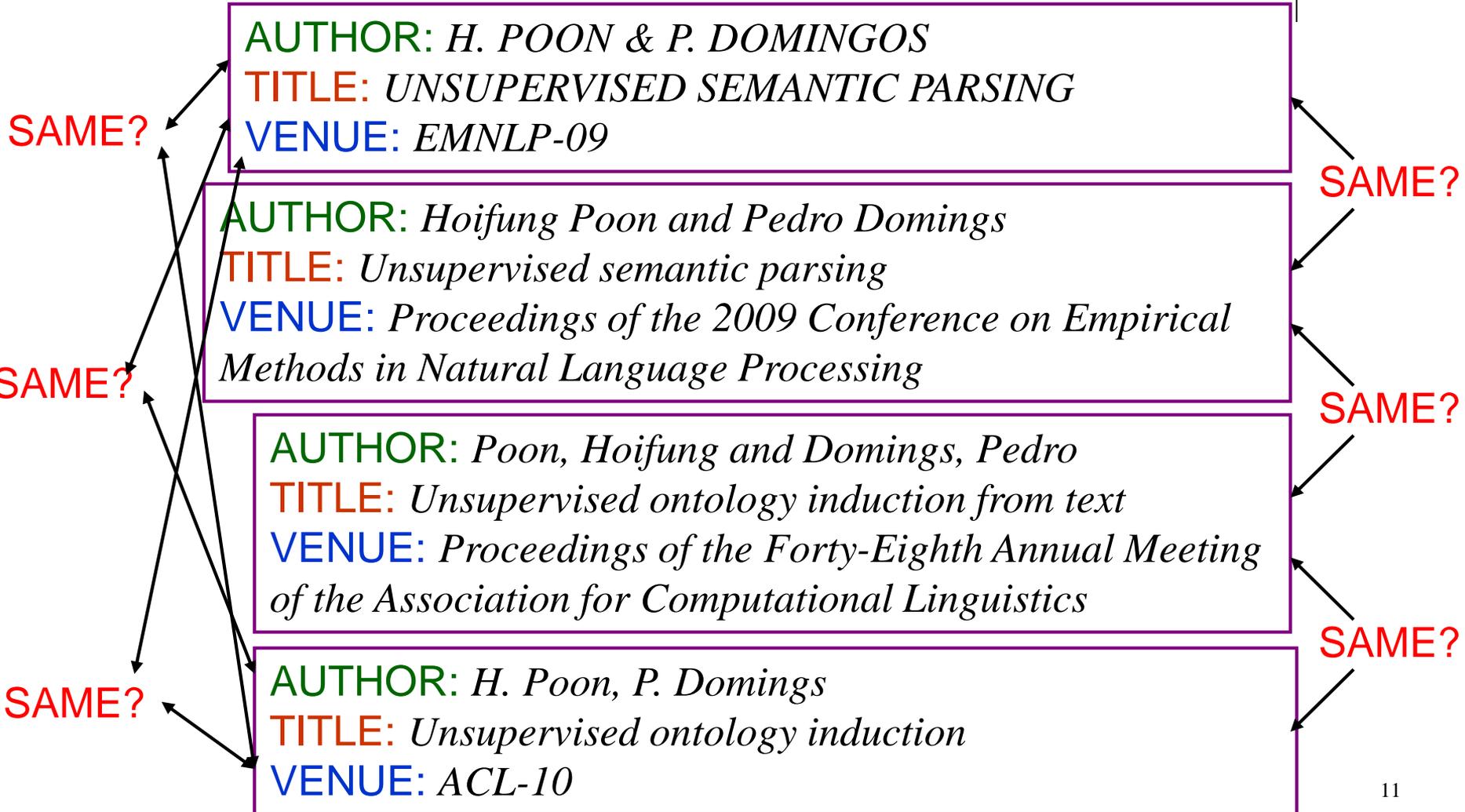
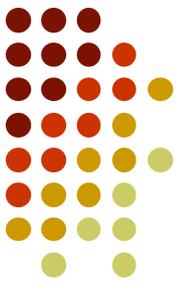
- Recap MLN
- **Markov Logic: applications**
  - **Entity resolution**
  - **Statistical Parsing!**

# Entity Resolution

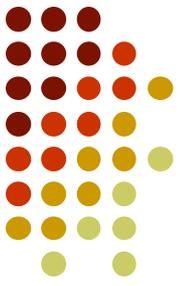


- Determining which observations correspond to the same real-world objects
- (e.g., database records, noun phrases, video regions, etc)
- Crucial importance in many areas (e.g., data cleaning, NLP, Vision)

# Entity Resolution: Example



# Entity Resolution (relations)



**Problem:** Given citation database, find duplicate records  
Each citation has author, title, and venue fields  
We have 10 relations

*provided as evidence*

**Author(bib, author)**

**Title(bib, title)**

**Venue(bib, venue)**

relate citations to their fields

**HasWord(author, word)**

**HasWord(title, word)**

**HasWord(venue, word)**

indicate which words are present  
in each field;

**SameAuthor(author, author)** represent field equality;

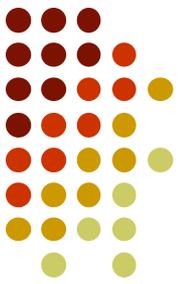
**SameTitle(title, title)**

**SameVenue(venue, venue)**

**SameBib(bib, bib)** represents citation equality;

*To be  
inferred*

# Entity Resolution (formulas)



Predict citation equality based on words in the fields

$\text{Title}(b1, t1) \wedge \text{Title}(b2, t2) \wedge$   
 $\text{HasWord}(t1, +\text{word}) \wedge \text{HasWord}(t2, +\text{word}) \Rightarrow$   
 $\text{SameBib}(b1, b2)$

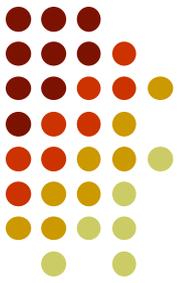
1000s  
of rules  
one for  
each word

(NOTE: +word is a shortcut notation, you actually have a rule for each word e.g.,  
 $\text{Title}(b1, t1) \wedge \text{Title}(b2, t2) \wedge$   
 $\text{HasWord}(t1, \text{"bayesian"}) \wedge$   
 $\text{HasWord}(t2, \text{"bayesian"}) \Rightarrow \text{SameBib}(b1, b2)$  )

Same 1000s of rules for **author**

Same 1000s of rules for **venue**

# Entity Resolution (formulas)



## Transitive closure

$\text{SameBib}(b1, b2) \wedge \text{SameBib}(b2, b3) \Rightarrow ???$

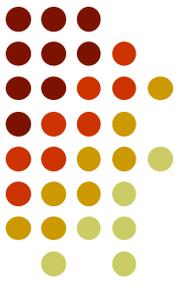
A.  $\text{SameBib}(b1, b2)$

B.  $\text{SameBib}(b1, b3)$

C.  $\text{SameAuthor}(a1, a2)$



# Entity Resolution (formulas)



## Transitive closure

$\text{SameBib}(b1, b2) \wedge \text{SameBib}(b2, b3) \Rightarrow \text{SameBib}(b1, b3)$

$\text{SameAuthor}(a1, a2) \wedge \text{SameAuthor}(a2, a3) \Rightarrow \text{SameAuthor}(a1, a3)$

*Same rule for title*

*Same rule for venue*

**Link fields equivalence to citation equivalence** – *e.g., if two citations are the same, their authors should be the same*

$\text{Author}(b1, a1) \wedge \text{Author}(b2, a2) \wedge \text{SameBib}(b1, b2) \Rightarrow \text{SameAuthor}(a1, a2)$

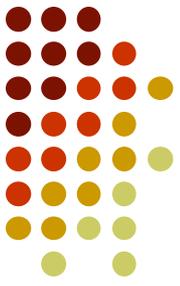
*...and that citations with the same author are more likely to be the same*

$\text{Author}(b1, a1) \wedge \text{Author}(b2, a2) \wedge \text{SameAuthor}(a1, a2) \Rightarrow \text{SameBib}(b1, b2)$

*Same rules for title*

*Same rules for venue*

# Benefits of MLN model



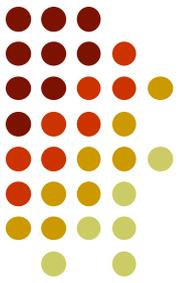
**Standard non-MLN approach:** build a classifier that given two citations tells you if they are the same or not, and then apply transitive closure

**New MLN approach:**

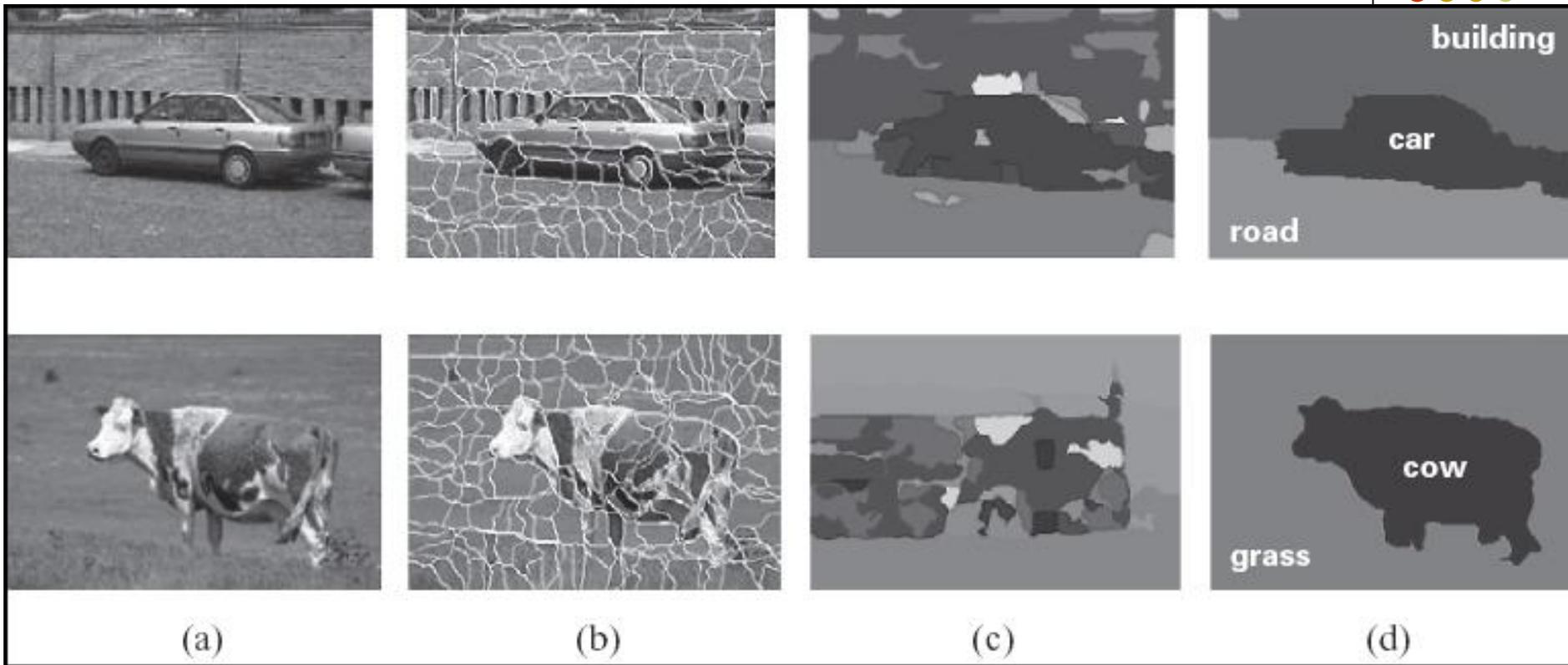
- performs *collective* entity resolution, where resolving one pair of entities helps to resolve pairs of related entities

e.g., inferring that a pair of citations are equivalent can provide evidence that the names *AAAI-06* and *21st Natl. Conf. on AI* refer to the same venue, even though they are superficially very different. This equivalence can then aid in resolving other entities.

# Similar to.....



# Image segmentation



classifying  
each superpixel  
independently

with a  
Markov  
Random  
Field!



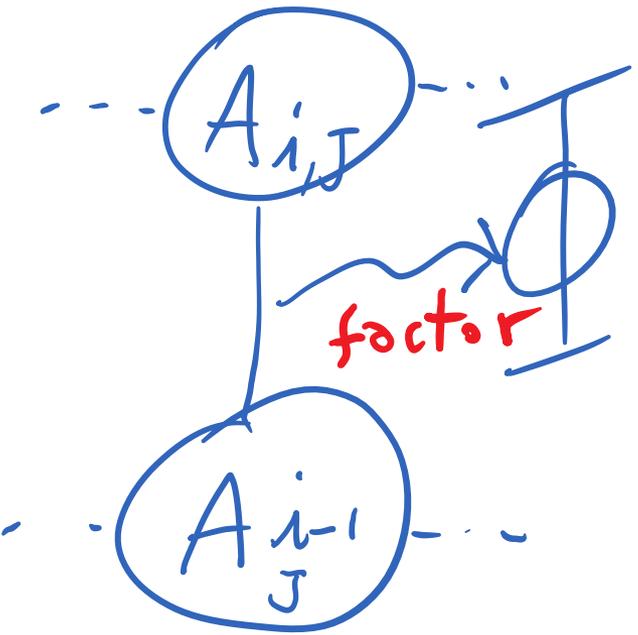
# Markov Networks Applications (1): Computer Vision

- Each vars correspond to a *pixel* (or *superpixel*)
- Edges (factors) correspond to interactions between adjacent pixels in the image
- E.g., in segmentation: from generically penalize discontinuities, to road under car

favor continuities

discontinuities, to road under car

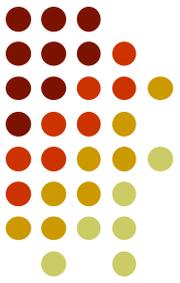
## SIMPLE EXAMPLE



$A_{ij}$

	road	car
$A_{i-1,j}$ road	100	50
$A_{i-1,j}$ car	1	100

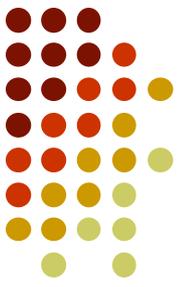
# Other MLN applications



- **Information Extraction**
- **Co-reference Resolution Robot Mapping**  
(infer the map of an indoor environment from laser range data)
- **Link-based Clustering** (uses relationships among the objects in determining similarity)
- **Ontologies extraction from Text**
- .....

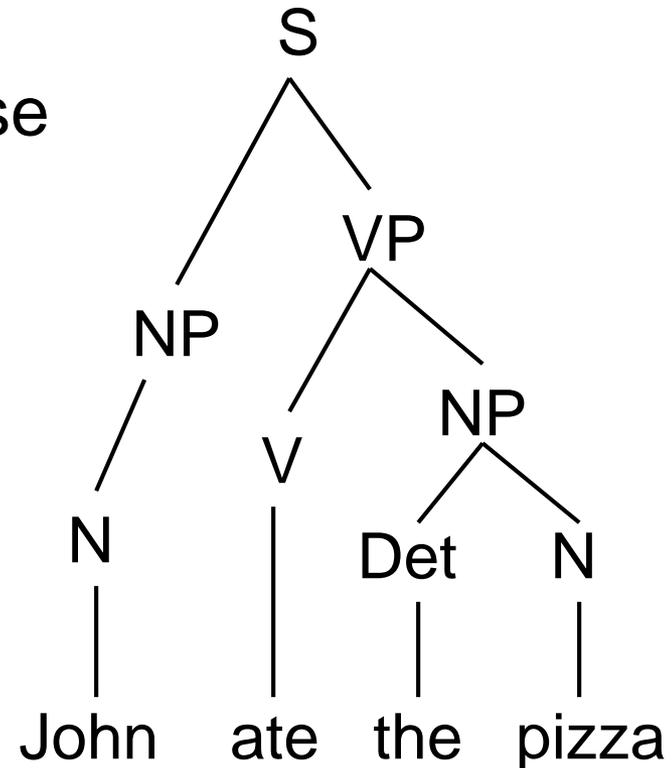
# Lecture Overview

- Recap of MLN
- **Markov Logic: applications**
  - Entity resolution
  - **Statistical Parsing!**



# Statistical Parsing

- **Input:** Sentence
- **Output:** Most probable parse
- **PCFG:** Production rules with probabilities  
E.g.: 0.7  $NP \rightarrow N$   
0.3  $NP \rightarrow Det N$
- **WCFG:** Production rules with weights (equivalent)
- Chomsky normal form:  
 $A \rightarrow BC$  or  $A \rightarrow a$





# Logical Representation of CFG

→ rewrites as

⇒ logical implication

$S \rightarrow NP VP$       (A)  $NP \wedge VP \Rightarrow S$

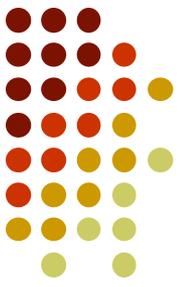
(B)  $NP(i,j) \wedge VP(j,k) \Rightarrow S(i,k)$

(C)  $S(i,k) \Rightarrow NP(i,j) \wedge VP(j,k)$

Which one would be a reasonable representation in logics?



0 the 1 dog 2 chases 3 the 4 cat 5



# Logical Representation of CFG

$S \rightarrow NP VP$

$NP(i,j) \wedge VP(j,k) \Rightarrow S(i,k)$

$NP \rightarrow Adj N$

$Adj(i,j) \wedge N(j,k) \Rightarrow NP(i,k)$

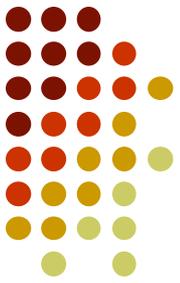
$NP \rightarrow Det N$

$Det(i,j) \wedge N(j,k) \Rightarrow NP(i,k)$

$VP \rightarrow V NP$

$V(i,j) \wedge NP(j,k) \Rightarrow VP(i,k)$

# Lexicon....



// Determiners

Token("a",i) => Det(i,i+1)

Token("the",i) => Det(i,i+1)

// Adjectives

Token("big",i) => Adj(i,i+1)

Token("small",i) => Adj(i,i+1)

// Nouns

Token("dogs",i) => N(i,i+1)

Token("dog",i) => N(i,i+1)

Token("cats",i) => N(i,i+1)

Token("cat",i) => N(i,i+1)

Token("fly",i) => N(i,i+1)

Token("flies",i) => N(i,i+1)

// Verbs

Token("chase",i) => V(i,i+1)

Token("chases",i) => V(i,i+1)

Token("eat",i) => V(i,i+1)

Token("eats",i) => V(i,i+1)

Token("fly",i) => V(i,i+1)

Token("flies",i) => V(i,i+1)

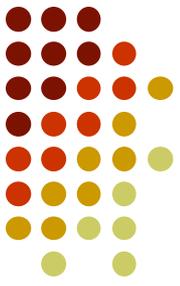
Det(0,1) N(1,2)

the cat ate the mouse

0 1 2 3 4 5

0 1 2 3 4 5

# Avoid two problems (1)

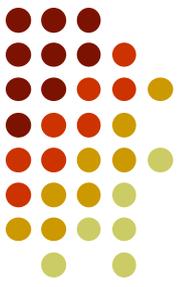


- If there are two or more rules with the same left side (such as **NP**  $\rightarrow$  **Adj N** and **NP**  $\rightarrow$  **Det N**) need to enforce the constraint that only one of them fires :

**NP(i,k) ^ Det(i,j) => ¬Adj(i,j)**

``If a noun phrase results in a determiner and a noun, it cannot result in and adjective and a noun".

# Avoid two problems (2)



- **Ambiguities in the lexicon.**

homonyms belonging to different parts of speech,  
e.g., *fly* (noun or verb),

only one of these parts of speech should be assigned.

We can enforce this constraint in a general manner by making mutual exclusion rules for each part of speech pair, i.e.:

$\neg \text{Det}(i,j) \vee \neg \text{Adj}(i,j)$

$\neg \text{Det}(i,j) \vee \neg \text{N}(i,j)$

$\neg \text{Det}(i,j) \vee \neg \text{V}(i,j)$

$\neg \text{Adj}(i,j) \vee \neg \text{N}(i,j)$

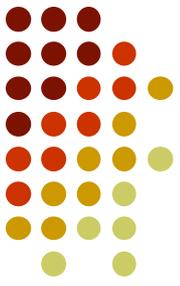
$\neg \text{Adj}(i,j) \vee \neg \text{V}(i,j)$

$\neg \text{N}(i,j) \vee \neg \text{V}(i,j)$

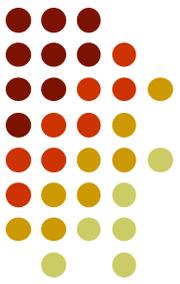
$\neg (A \wedge B)$

# Statistical Parsing

## Representation: Summary



- For each rule of the form  $A \rightarrow B C$ :  
Formula of the form  $B(i, j) \wedge C(j, k) \Rightarrow A(i, k)$   
E.g.:  $NP(i, j) \wedge VP(j, k) \Rightarrow S(i, k)$
- For each rule of the form  $A \rightarrow a$ :  
Formula of the form  $Token(a, i) \Rightarrow A(i, i+1)$   
E.g.:  $Token("pizza", i) \Rightarrow N(i, i+1)$
- For each nonterminal: state that exactly one production holds (solve problem 1)
- Mutual exclusion rules for each part of speech pair (solve problem 2)

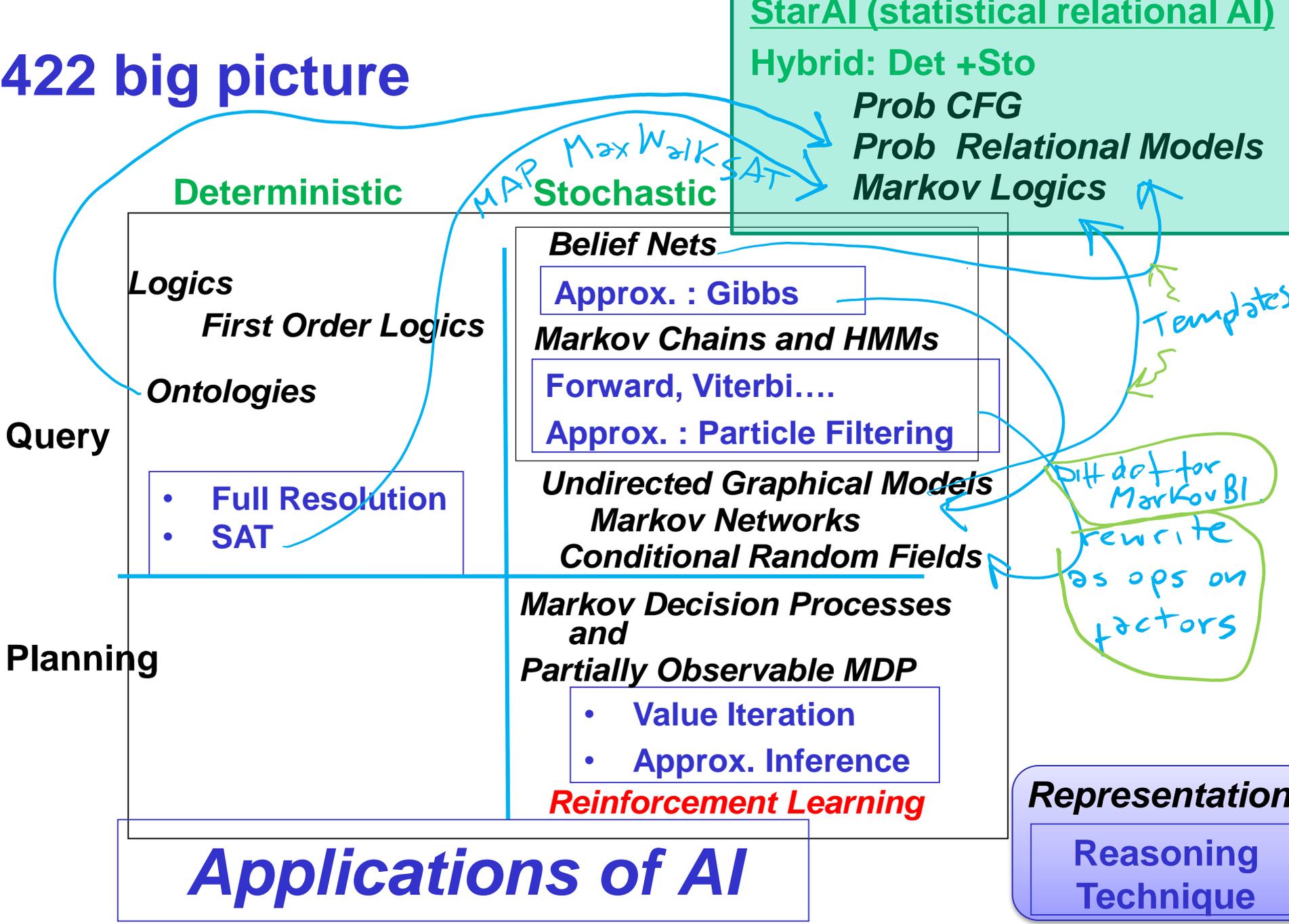


# Statistical Parsing : Inference

- Evidence predicate: `Token(token, position)`  
E.g.: `Token("pizza", 3)` etc.
- Query predicates:  
`Constituent(position, position)`  
E.g.: `S(0, 7)` "is this sequence of seven words a sentence?" but also `NP(2, 4)`
- What inference yields the most probable parse?

MAP! Find the most likely interpretation

# 422 big picture



# Learning Goals for today's class

## **You can:**

- Describe the entity resolution application of ML and explain the corresponding representation
- Probabilistic parsing as MLN not required

# Next Class on Mon

- **Start Probabilistic Relational Models**

Keep working on **Assignment-4**

**Due Apr 14**

In the past, a similar hw took students between 8 - 15 hours to complete. Please start working on it as soon as possible!