

Intelligent Systems (AI-2)

Computer Science cpsc422, Lecture 19

Oct, 18, 2019



Slide Sources

Raymond J. Mooney University of Texas at Austin

D. Koller, Stanford CS - Probabilistic Graphical Models

D. Page, Whitehead Institute, MIT

Several Figures from

“Probabilistic Graphical Models: Principles and Techniques” *D. Koller, N. Friedman* 2009

Lecture Overview

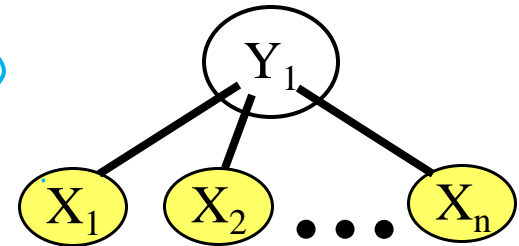
- Recap: Naïve Markov – Logistic regression (simple CRF)
- CRFs: high-level definition
- CRFs Applied to sequence labeling
- NLP Examples: Name Entity Recognition, joint POS tagging and NP segmentation
- CFR + deep learning Example

Let's derive the probabilities we need

$$\phi_i(X_i, Y_1) = \exp\{w_i \mathbb{1}\{X_i = 1, Y_1 = 1\}\}$$

how strongly $Y_1 = 1$ given that $X_i = 1$

$$\phi_0(Y_1) = \exp\{w_0 \mathbb{1}\{Y_1 = 1\}\}$$



$$P(Y_1 \mid \underbrace{x_1, \dots, x_n}_B) =$$

$$\frac{\tilde{P}(Y_1, x_1, \dots, x_n)}{\tilde{P}(x_1, \dots, x_n)}$$

$$\tilde{P}(Y_1, x_1, \dots, x_n) = \phi_0(Y_1) \prod_{i=1}^n \phi_i(x_i, Y_1)$$

$$\tilde{P}(Y_1 = 0, x_1, \dots, x_n) = 1$$

$$\tilde{P}(Y_1 = 1, x_1, \dots, x_n) =$$

$$e^{w_0 + \sum w_i x_i}$$

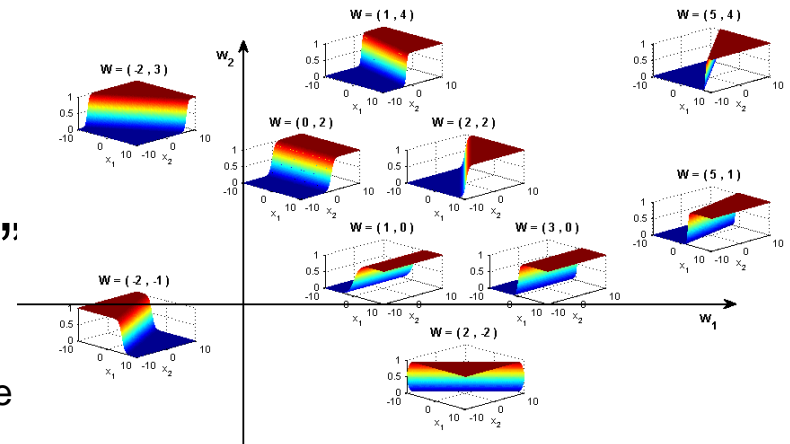
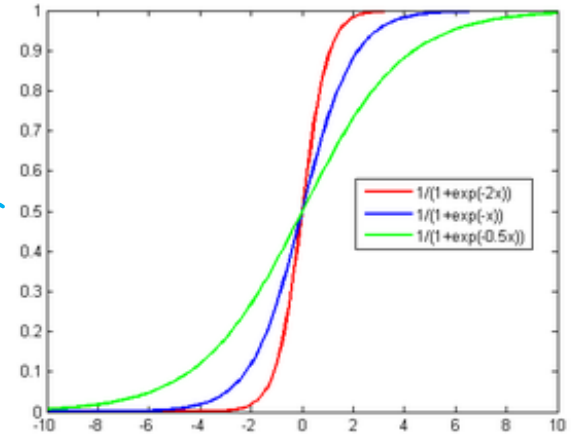
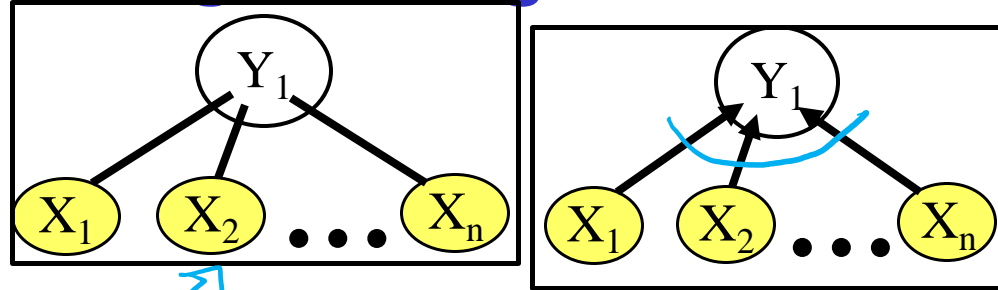
Continue.....

$$P(Y_1 = 1 | X_1, \dots, X_n) = \frac{e^{w_0 + \sum w_i x_i}}{1 + e^{w_0 + \sum w_i x_i}}$$
$$= \frac{e^z}{1 + e^z} \frac{e^{-z}}{e^{-z}} = \frac{1}{e^{-z} + 1}$$

$$P(Y_1 | X_1, \dots, X_n) = \left\{ \frac{1}{e^{-z} + 1}, \frac{e^{-z}}{e^{-z} + 1} \right\}$$

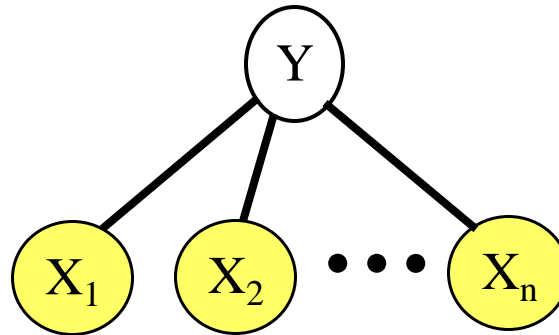
Sigmoid Function used in Logistic Regression

- Great practical interest
- Number of param w_i is linear instead of exponential in the number of parents
- Natural model for many real-world applications
- Naturally aggregates the influence of different “parents”



Logistic Regression as a Markov Net (CRF)

Logistic regression is a simple Markov Net (a CRF) *aka naïve markov model*



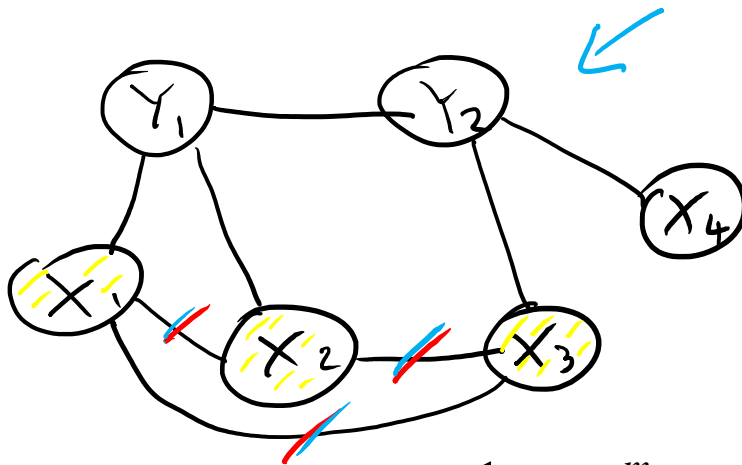
- But only models the **conditional distribution**, $P(Y | \mathbf{X})$ and not the full joint $P(\mathbf{X}, Y)$

Let's generalize

Assume that you always observe a set of variables $\mathbf{X} = \{X_1 \dots X_n\}$ and you want to predict one or more variables $\mathbf{Y} = \{Y_1 \dots Y_k\}$

A **CRF** is an undirected graphical model whose nodes corresponds to $\mathbf{X} \cup \mathbf{Y}$.

$\phi_1(D_1) \dots \phi_m(D_m)$ represent the factors which annotate the network (but we disallow factors involving only vars in \mathbf{X} – why?)



They would be

- A. too large
- B. constant**
- C. difficult to acquire

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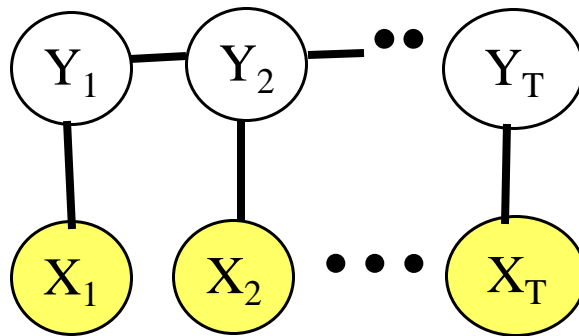
$$P(\mathbf{Y} | \mathbf{X}) = \frac{1}{Z(\mathbf{X})} \left(\prod_{i=1}^m \phi_i(D_i) \right)$$

$$Z(\mathbf{X}) = \sum_{\mathbf{Y}} \left(\prod_{i=1}^m \phi_i(D_i) \right)$$

Lecture Overview

- Recap: Naïve Markov – Logistic regression (simple CRF)
- CRFs: high-level definition
- **CRFs Applied to sequence labeling**
- NLP Examples: **Name Entity Recognition**, joint POS tagging and NP segmentation
- CFR + deep learning Example

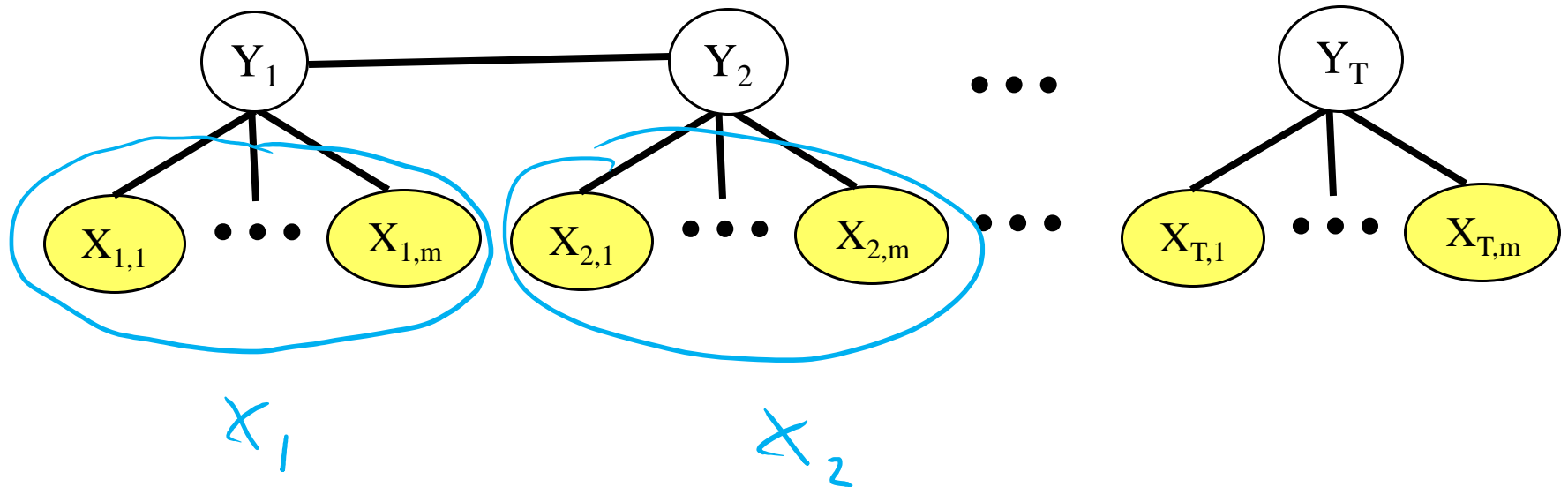
Sequence Labeling



Linear-chain CRF

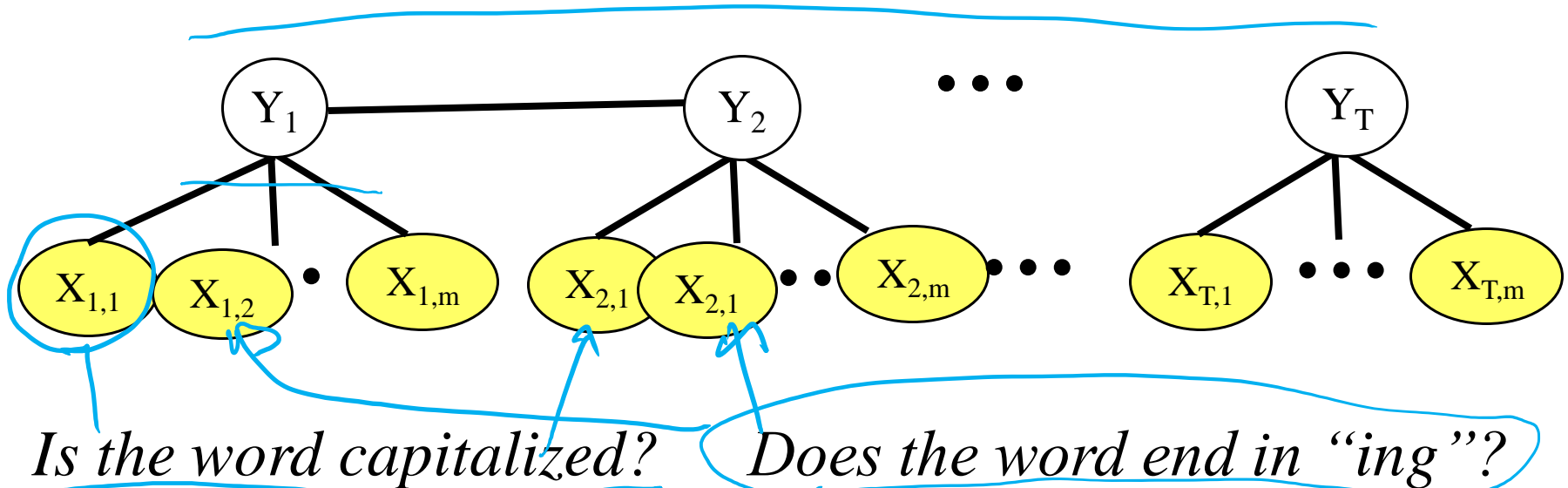
Increase representational Complexity: Adding Features to a CRF

- Instead of a single observed variable X_i we can model multiple features X_{ij} of that observation.



CRFs in Natural Language Processing

- One target variable Y for each word X , encoding the possible labels for X
- Each target variable is connected to a set of feature variables that capture properties relevant to the target distinction



Named Entity Recognition Task

- Entity often span multiple words “*British Columbia*”
- Type of an entity may not be apparent for individual words “*University of British Columbia*”
- Let’s assume three categories: **Person, Location, Organization**
- BIO notation (for sequence labeling)

possible B-PER I-PER B-LOC I-LOC
labels B-ORG I-ORG OTHER

O B-ORG I-ORG I-ORG I-ORG
The University of British Columbia

O O B-LOC I-LOC
is in Vancouver B.C.

Linear chain CRF parameters


With two factors “types” for each word

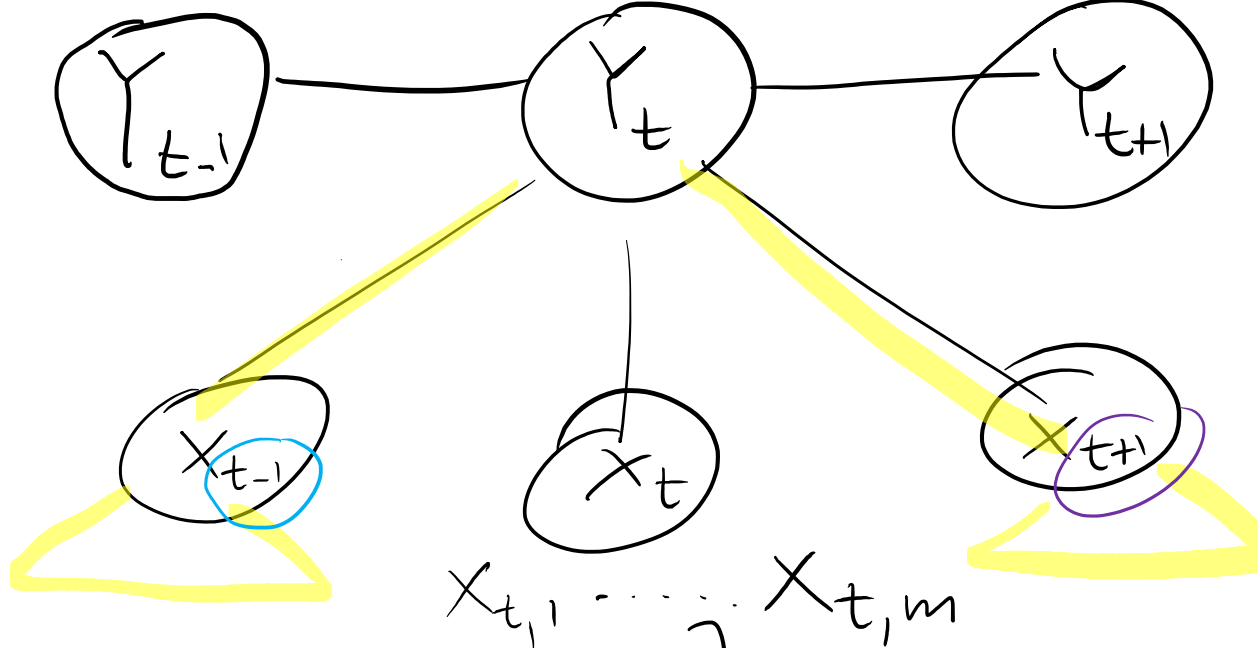
$\phi_t^1(Y_t, Y_{t-1}) \phi_t^1(Y_t, Y_{t+1})$ Dependency between neighboring target vars 

$\phi_t^2(Y_t, X_1, \dots, X_T)$ Dependency between target variable and its context in the word sequence, which can include also **features of the words** (capitalized, appear in an atlas of location names, etc.)

Factors are similar to the ones for the Naïve Markov (logistic regression)

$$\phi_t(Y_t, X_{tk}) = \exp\{w_{tk} \times \uparrow \{Y_t = I-LOC, X_{tk} = 1\}\}$$

 appears in atlas of location names



$X_{t,1} \dots X_{t,m}$

$\uparrow \{ Y_t = \text{I-ORG}, X_{t,k} = \text{"Times"} \}$

$\uparrow \{ Y_t = \text{I-PER}, X_{t+1,k} = \text{"spoke"} \}$

$\uparrow \{ Y_t = \text{I-PER}, X_{t-1,k} = \text{"Mrs."} \}$

Features can also be

- The word
- Following word
- Previous word

More on features

Including features that are **conjunctions of simple features** increases accuracy

$$\uparrow \left\{ Y_t = 1\text{-PER}, X_{t+1, k} = \text{"spoke"} \right\}$$

$$\uparrow \left\{ Y_t = 1\text{-PER}, X_{t-1, k} = \text{"Mrs."} \right\}$$

\hat{Y}_t

Total number of features can be 10^5 - 10^6

However features are sparse i.e. most features are 0 for most words

Linear-Chain Performance

Per-token/word accuracy in the high 90% range for many natural datasets *label is wrong for 2 words out of 9*

Per-field precision and recall are more often around 80-95% , depending on the dataset. Entire Named Entity Phrase must be correct

only one is correct out of 2

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\checkmark O \checkmark B-ORG \checkmark I-ORG \times B-LOC \times I-LOC
 The University of British Columbia

\checkmark O \checkmark O \checkmark B-LOC \checkmark I-LOC
 is in Vancouver B.C.

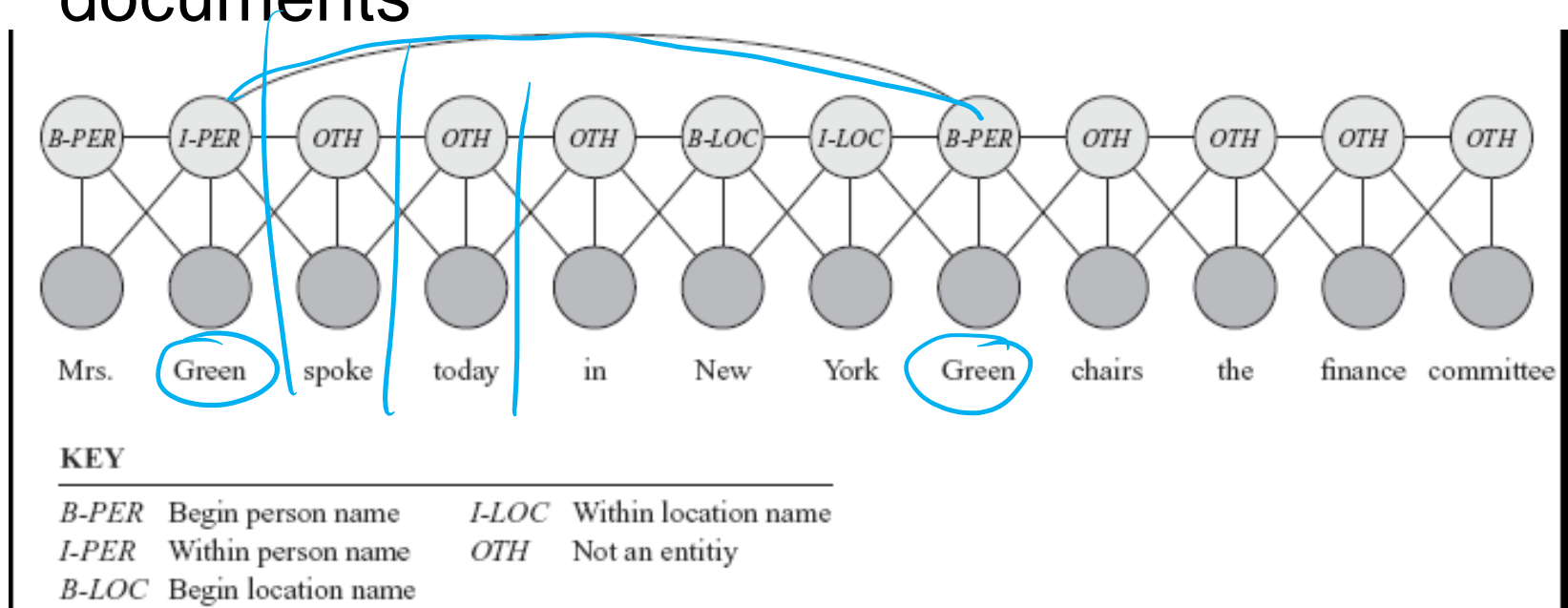
\checkmark Per-word accuracy?
 \checkmark Per-field precision?

A.	B	C.
$\frac{1}{2}$	$\frac{7}{9}$	$\frac{7}{9}$
$\frac{1}{2}$	$\frac{3}{9}$	$\frac{1}{2}$

Skip-Chain CRFs

Include additional factors that connect non-adjacent target variables

E.g., When a word occur multiple times in the same documents



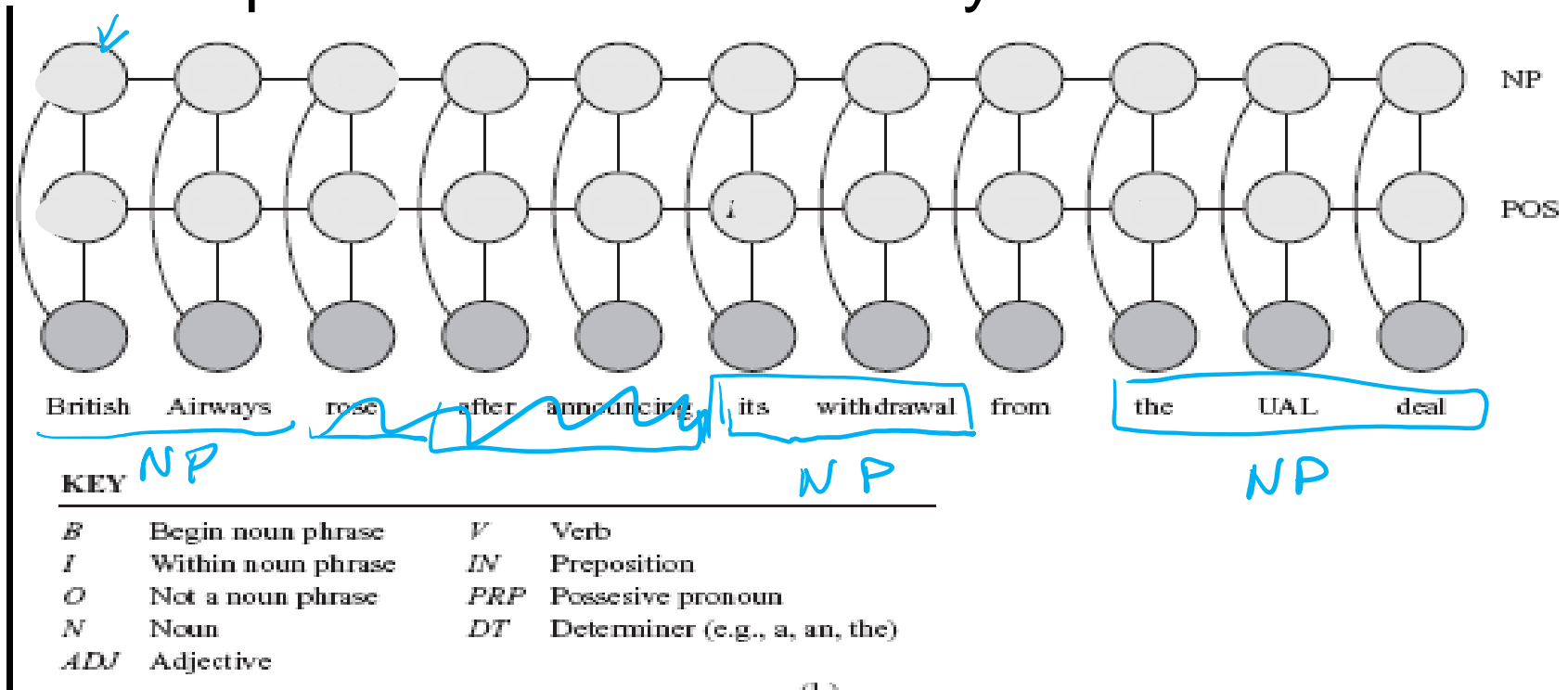
Graphical structure over Y can depend on the values of the Xs ! CPSC 422, Lecture 19

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Coupled linear-chain CRFs

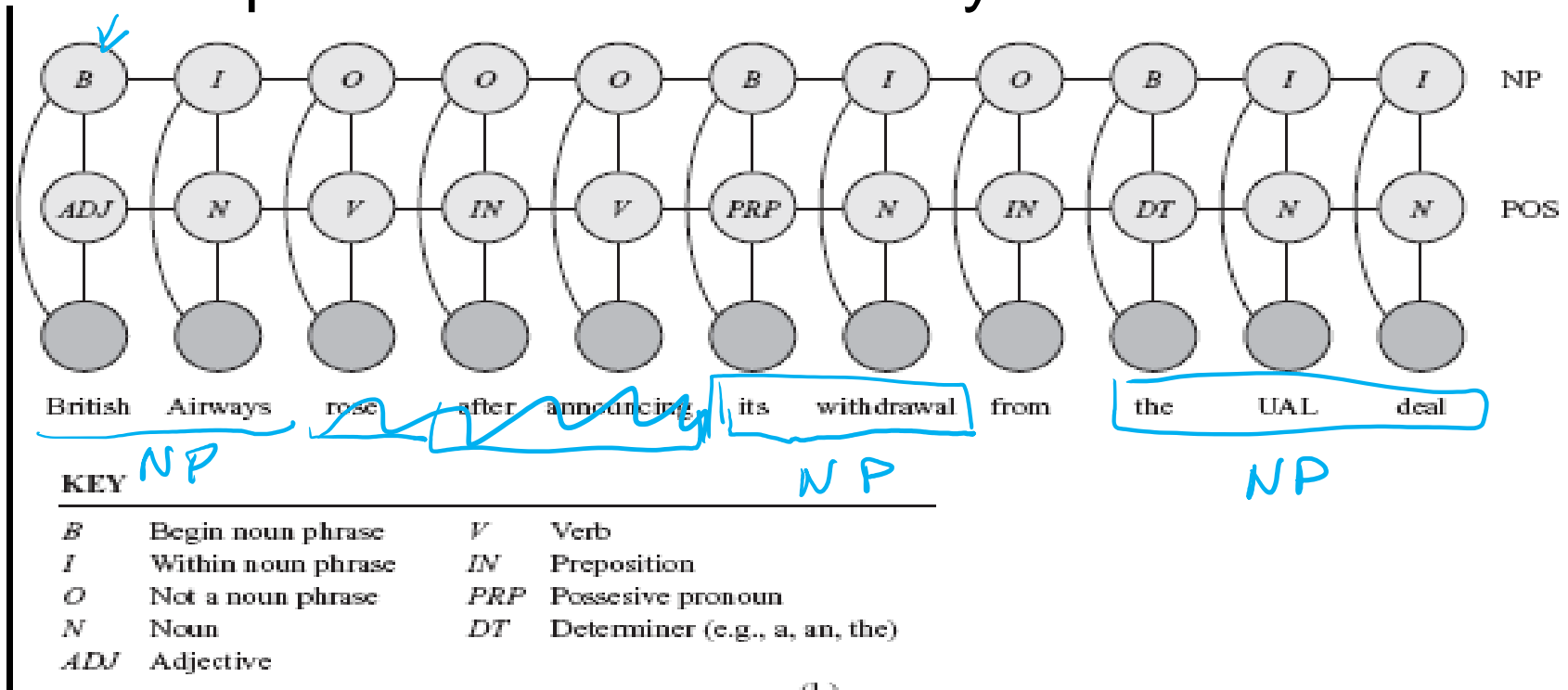
- Linear-chain CRFs can be combined to perform multiple tasks simultaneously



- Performs part-of-speech labeling and noun-phrase segmentation

Coupled linear-chain CRFs

- Linear-chain CRFs can be combined to perform multiple tasks simultaneously



- Performs part-of-speech labeling and noun-phrase segmentation

Inference in CRFs (just intuition)

An HMM can be viewed as a factor graph
 $p(\mathbf{y}, \mathbf{x}) = \prod_t \Psi_t(y_t, y_{t-1}, x_t)$ where $Z = 1$, and the factors are defined as:

$$\Psi_t(j, i, x) \stackrel{\text{def}}{=} p(y_t = j | y_{t-1} = i) p(x_t = x | y_t = j). \quad (4.1)$$

Forward / Backward / Smoothing and Viterbi can be rewritten (not trivial!) using these factors

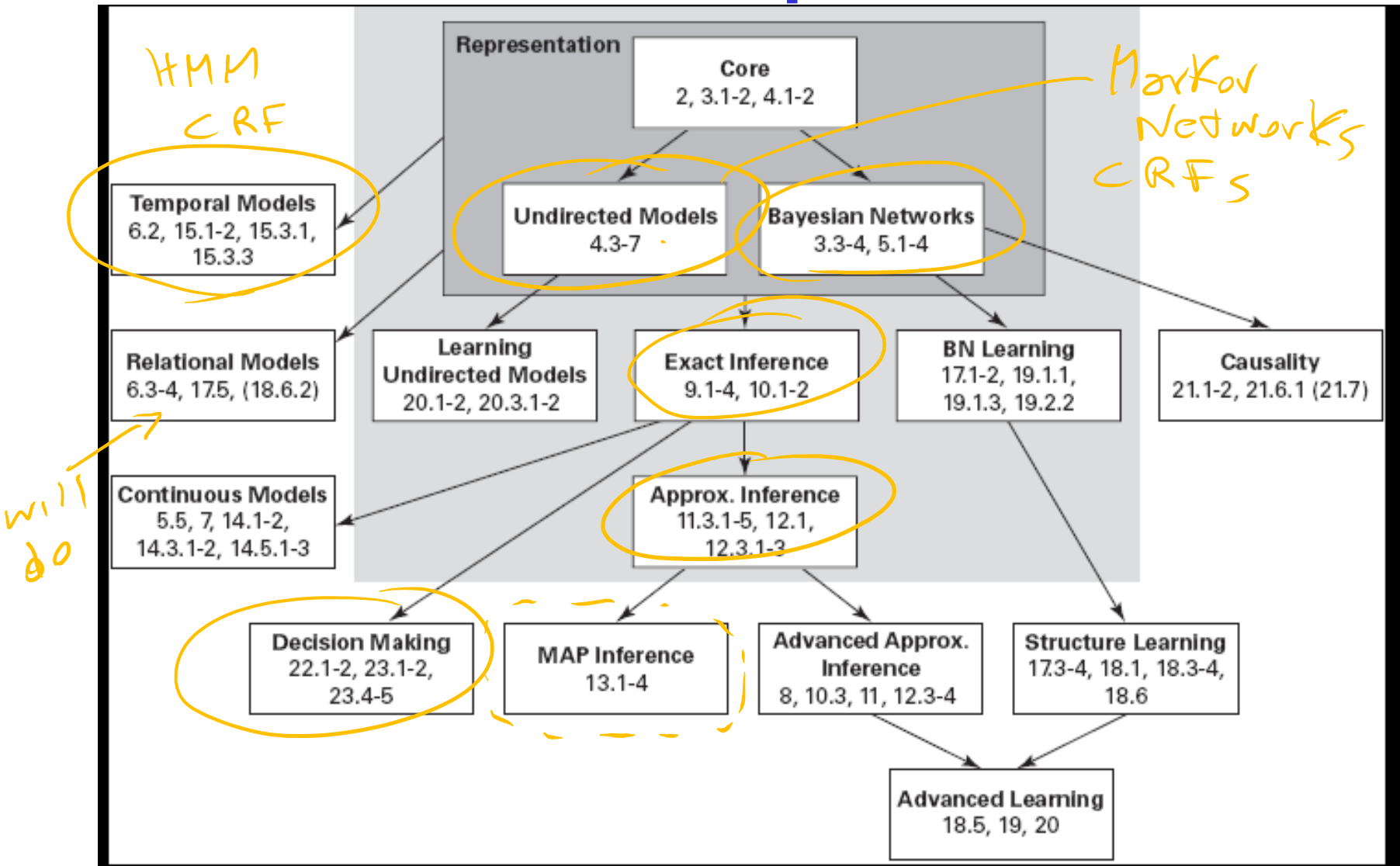
Then you plug in the factors of the CRFs and all the algorithms work fine with CRFs! 😊

CRFs Summary

- Ability to incorporate arbitrary overlapping local and global features
- Graphical structure over Y can depend on the values of the X s (see slide 17)
- Can perform multiple tasks simultaneously (see slide 19)
- *Standard Inference algorithm* for HMM can be applied
- *Practical Learning algorithms exist*
- State-of-the-art on many labeling tasks (*deep learning recently shown to be often better when large training data are available... current research on ensembling them!*)

See MALLET package for CRF implementation

Probabilistic Graphical Models



From "Probabilistic Graphical Models: Principles and Techniques" D. Koller, N. Friedman 2009

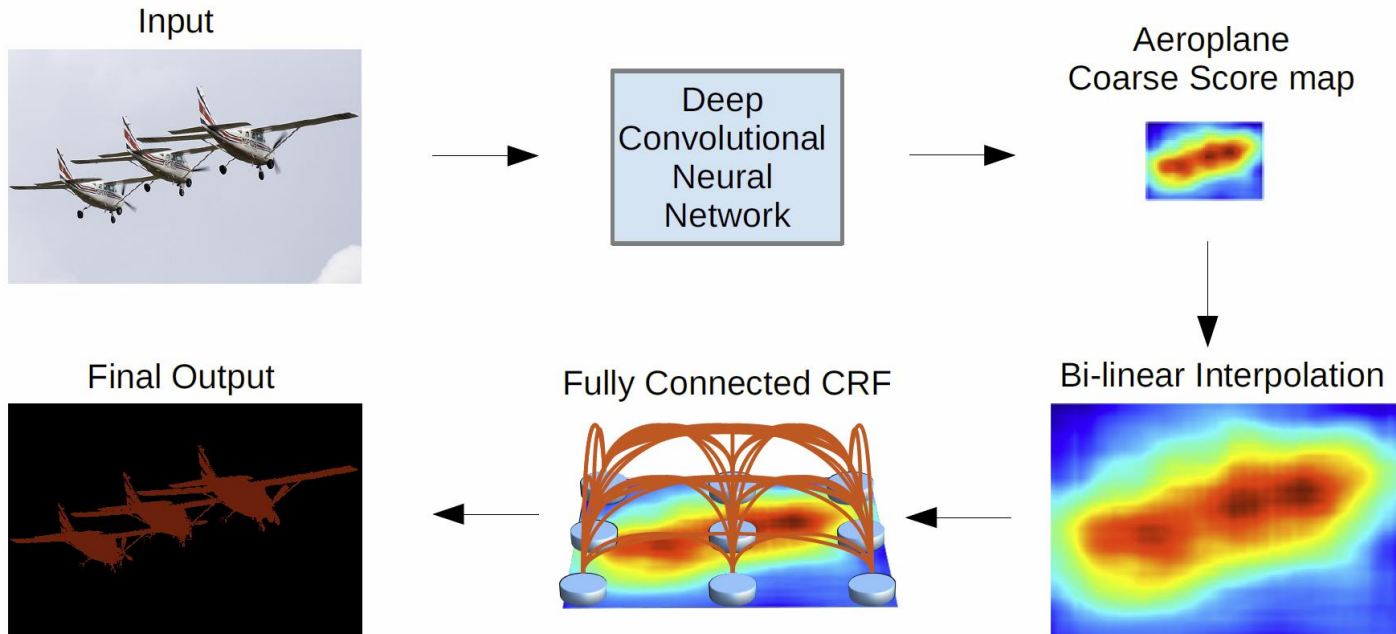
Combining CRFs and Neural Models

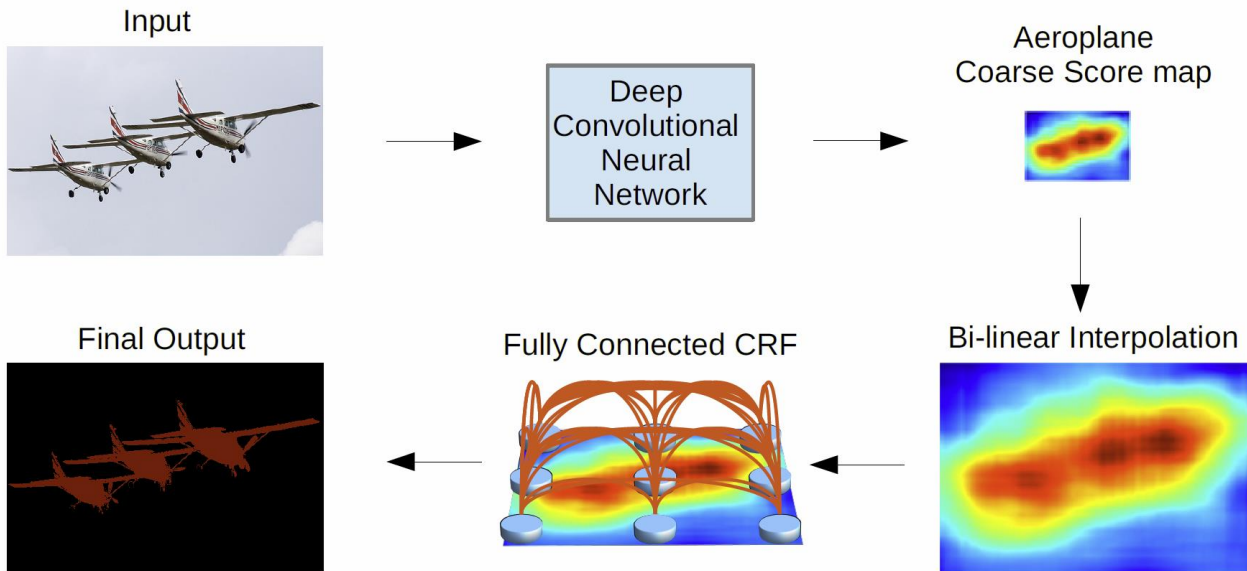
SEMANTIC IMAGE SEGMENTATION WITH DEEP CONVOLUTIONAL NETS AND FULLY CONNECTED CRFS

International Conference on Learning Representations (ICLR), San Diego, California, USA, May 2015.

Liang-Chieh Chen Univ. of California, Los Angeles; George Papandreou Google Inc. ; Iasonas Kokkinos INRIA ; Kevin Murphy Google Inc. ; Alan L. Yuille Univ. of California, Los Angeles

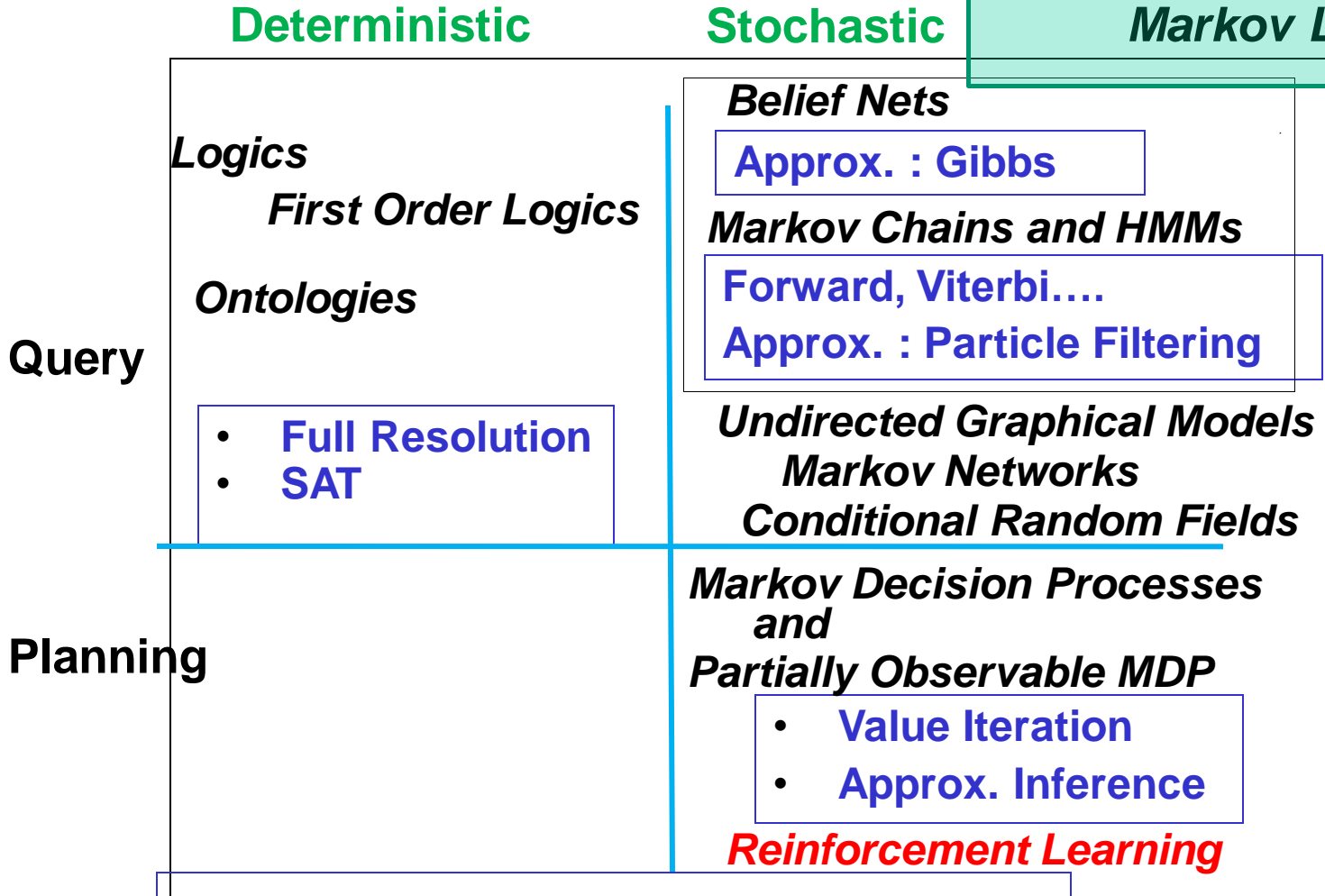
1. Use CNN to generate a rough prediction of segmentation (smooth, blurry heat map)
2. Refine this prediction with a conditional random field (CRF)





422 big picture

StarAI (statistical relational AI)
 Hybrid: Det +Sto
 Prob CFG
 Prob Relational Models
 Markov Logics



Applications of AI

Representation
 Reasoning
 Technique

Learning Goals for today's class

You can:

- Provide general definition for CRF
- Apply CRFs to sequence labeling
- Describe and justify features for CRFs applied to Natural Language processing tasks
- Explain benefits of CRFs

**Midterm, Fri, Oct 25,
we will start at 4pm sharp**

How to prepare...

- Go to **Office Hours**
- **Learning Goals** (look at the end of the slides for each lecture – complete list has been posted)
- Revise all the **clicker questions** and **practice exercises**
- **More practice material** has been posted
- Check questions and answers on Piazza

Next class Mon

- Start Logics
- Revise Logics from 322!