

Intelligent Systems (AI-2)

Computer Science cpssc422, Lecture 10

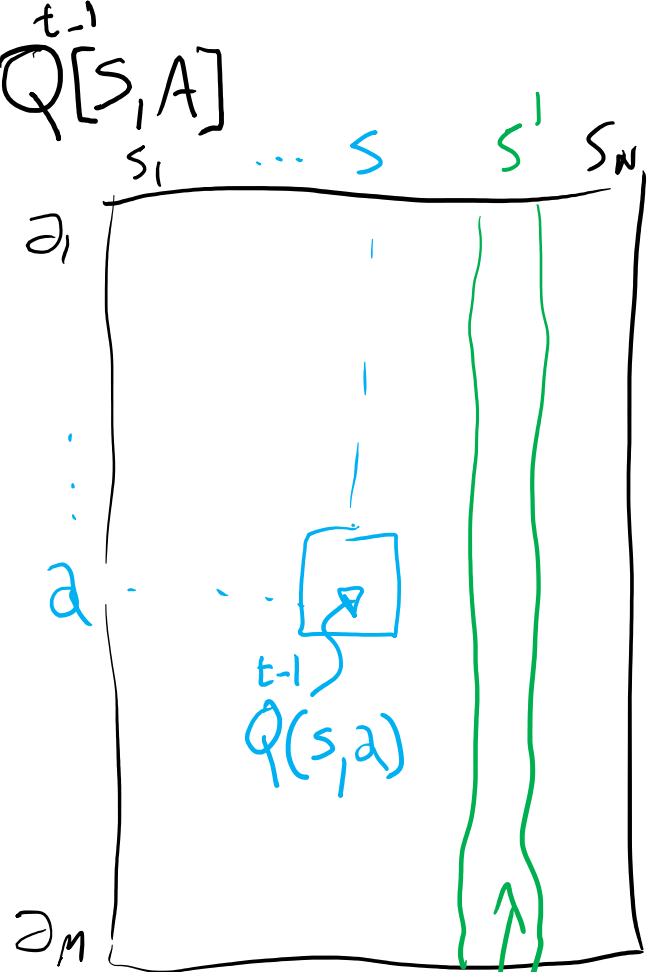
Sep, 25, 2019



Lecture Overview

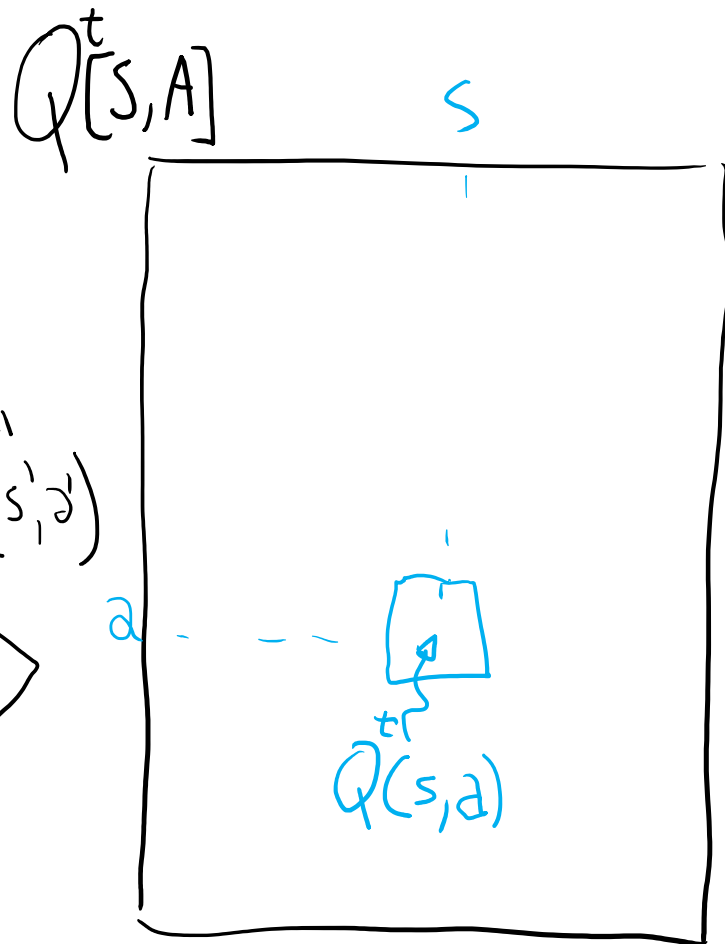
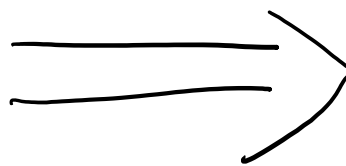
Finish Reinforcement learning

- **Exploration vs. Exploitation**
- On-policy Learning (SARSA)
- Scalability



Sars'

$$Q(s, a) = r + \gamma \max_{a'} Q(s', a')$$



TD

$$A^t = A^{t-1} + \alpha_k (v^t - A^{t-1})$$

$$Q(s, a)^t = Q(s, a)^{t-1} + \alpha_k ((r + \gamma \max_{a'} Q(s', a')^{t-1}) - Q(s, a)^{t-1})$$

Also keep the α_k

$$s_a = \frac{1}{K_{s_a}}$$

$K[s, a]$

a

s

K_{s_a}

of
experiences
 $s_a \dots$

What Does Q-Learning learn

Q-learning does not explicitly tell the agent what to do....

Given the Q-function the agent can.....

... either exploit it or explore more....

Any effective strategy should be *greedy in the limit of infinite exploration* (**GLIE**)

- Try each action an unbounded number of times
- Choose the predicted best action in the limit

We will look at two exploration strategies

- ϵ -greedy
- soft-max

ϵ -greedy

- Choose a **random action with probability ϵ** and choose **best action with probability $1 - \epsilon$**

$$P(\text{random action}) = \epsilon$$

$$P(\text{best action}) = 1 - \epsilon$$

- First GLIE condition (try every action an unbounded number of times) is satisfied via the ϵ random selection
- What about second condition?
 - Select predicted best action in the limit.
- reduce ϵ overtime!

Soft-Max

if $Q[s,a]$ close to 0 each action

selected with prob $\frac{1}{\text{\# of actions}}$

UNIFORM DISTRIB.

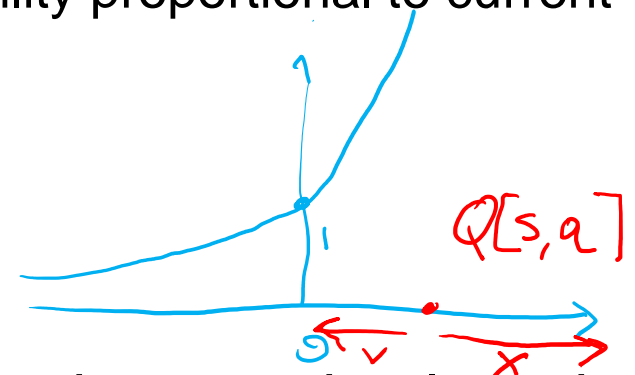
➤ Takes into account improvement in estimates of expected reward function $Q[s,a]$

- Choose action **a** in state **s** with a probability proportional to current estimate of **Q[s,a]**

$$\frac{e^{Q[s,a]}}{\sum_a e^{Q[s,a]}}$$

or controlled by τ parameter

$$\frac{e^{Q[s,a]/\tau}}{\sum_a e^{Q[s,a]/\tau}}$$



➤ τ (tau) in the formula above influences how randomly actions should be chosen

- ✓ if τ is high, the exponentials approach 1, the fraction approaches $1/(\text{number of actions})$, and each action has approximately the same probability of being chosen (exploration or exploitation?)
- ✗ as $\tau \rightarrow 0$, the exponential with the highest $Q[s,a]$ dominates, and the current best action is always chosen (exploration or exploitation?)

Soft-Max example

Assume only 3 actions

$Q[s_i, a]$	s_i	$Q[s_i, a] / \tau$	$\tau = 100$	$\tau = .5$
a_1	2\$.02	4
a_2	3\$.03	6
a_3	1\$.01	2

prob of selecting action a

$$p(a_1) = \frac{e^{Q[s, a_1]}}{\sum_a e^{Q[s, a]}}$$

$$p(a_2) = \frac{e^3}{e^1 + e^2 + e^3}$$

$$p(a_3) = \frac{e^1}{e^1 + e^2 + e^3}$$

$\tau = 100$

$$\frac{e^{Q[s, a] / \tau}}{\sum_a e^{Q[s, a] / \tau}}$$

$$\frac{e^{.02}}{e^{.01} + e^{.02} + e^{.03}}$$

→ same

$$\frac{e^{.03}}{e^{.01} + e^{.02} + e^{.03}}$$

$$\frac{e^{.01}}{e^{.01} + e^{.02} + e^{.03}}$$

$\tau = .5$

$$\frac{e^{Q[s, a] / \tau}}{\sum_a e^{Q[s, a] / \tau}}$$

$$\frac{e^4}{e^2 + e^4 + e^6}$$

$$\frac{e^6}{e^2 + e^4 + e^6}$$

$$\frac{e^2}{e^2 + e^4 + e^6}$$

Soft-Max

➤ When in state **s**, Takes into account improvement in estimates of expected reward function $Q[s,a]$ for all the actions

- Choose action a in state s with a probability proportional to current estimate of $Q[s,a]$

$$\frac{e^{Q[s,a]}}{\sum_a e^{Q[s,a]}}$$

$$\frac{e^{Q[s,a]/\tau}}{\sum_a e^{Q[s,a]/\tau}}$$

➤ τ (tau) in the formula above influences how randomly values should be chosen

- if τ is high, $\gg Q[s,a]$?



A. It will mainly exploit

B. It will mainly explore

C. It will do both with equal probability

Soft-Max

$$\frac{e^{Q[s,a]/\tau}}{\sum_a e^{Q[s,a]/\tau}}$$

all very close to 1



➤ τ (tau) in the formula above influences how randomly values should be chosen

- if τ is high, the exponentials approach 1, the fraction approaches $1/(\text{number of actions})$, and each action has approximately the same probability of being chosen (exploration or exploitation?)
- as $\tau \rightarrow 0$, the exponential with the highest $Q[s,a]$ dominates, and the current best action is always chosen (exploration or exploitation?)

Lecture Overview

Finish Reinforcement learning

- Exploration vs. Exploitation
- **On-policy Learning (SARSA)**
- **RL scalability**

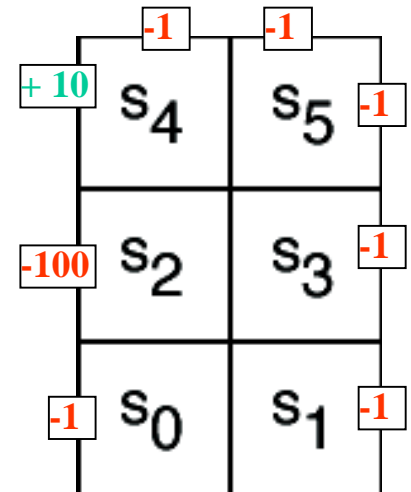
Learning before vs. during deployment

- Our learning agent can:
 - A. act in the environment to learn how it works (before deployment)
 - B. Learn as you go (after deployment)
- If there is time to learn before deployment, the agent should try to do its best to learn as much as possible about the environment
 - even engage in locally suboptimal behaviors, because this will guarantee reaching an optimal policy in the long run
- If learning while “at work”, suboptimal behaviors could be costly

Example

➤ Consider, for instance, our sample grid game:

- the optimal policy is to go *up* in S_0
- But if the agent includes some exploration in its policy (e.g. selects 20% of its actions randomly), exploring in S_2 could be dangerous because it may cause hitting the **-100** wall
- No big deal if the agent is not deployed yet, but not ideal otherwise



➤ Q-learning would not detect this problem

- It does *off-policy learning*, i.e., it focuses on the optimal policy

➤ *On-policy* learning addresses this problem

On-policy learning: SARSA

- On-policy learning learns the value of **the policy being followed**.
 - e.g., act greedily 80% of the time and act randomly 20% of the time
 - Better to be aware of the consequences of exploration as it happens, and avoid outcomes that are too costly while acting, rather than looking for the true optimal policy
- SARSA
 - So called because it uses *<state, action, reward, state, action>* experiences rather than the *<state, action, reward, state>* used by Q-learning
 - Instead of looking for the best action at every step, **it evaluates the actions suggested by the current policy**
 - Uses this info to revise it

On-policy learning: SARSA

- Given an experience $\langle s, a, r, s', a' \rangle$, SARSA updates $Q[s, a]$ as follows

$$Q[s, a] \leftarrow Q[s, a] + \alpha((r + \gamma Q[s', a']) - Q[s, a])$$

What's different from Q-learning?

On-policy learning: SARSA

- Given an experience $\langle s, a, r, s', a' \rangle$, SARSA updates $Q[s, a]$ as follows

$$Q[s, a] \leftarrow Q[s, a] + \alpha((r + \gamma Q[s', a']) - Q[s, a])$$

- While Q-learning was using

$$Q[s, a] \leftarrow Q[s, a] + \alpha((r + \gamma \max_{a'} Q[s', a']) - Q[s, a])$$

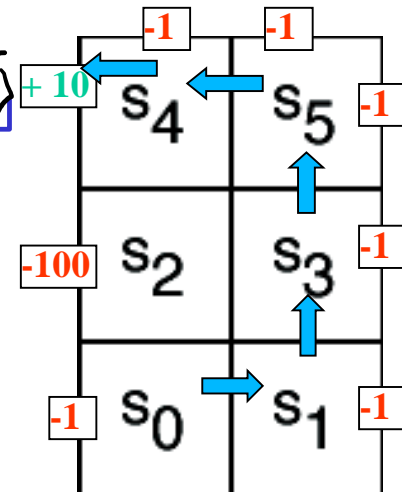
- There is no more **max** operator in the equation, there is instead the Q-value of the action suggested by the current policy

$\langle s_0, right, 0, s_1, upCareful, -1, s_3, upCareful, -1, s_5, left, 0, s_4, left, 10, s_0, right \rangle$

$$Q[s, a] \leftarrow Q[s, a] + \alpha(r + \gamma Q[s', a'] - Q[s, a])$$

k=1

Q[s,a]	s_0	s_1	s_2	s_3	s_4	s_5
<i>upCareful</i>	0	0	0	0	0	0
<i>Left</i>	0	0	0	0	0	0
<i>Right</i>	0	0	0	0	0	0
<i>Up</i>	0	0	0	0	0	0



$$Q[s_0, right] \leftarrow Q[s_0, right] + \alpha_k(r + 0.9Q[s_1, UpCareful] - Q[s_0, right]);$$

$$Q[s_0, right] \leftarrow$$

$$Q[s_1, upCarfull] \leftarrow Q[s_1, upCarfull] + \alpha_k(r + 0.9Q[s_3, UpCareful] - Q[s_1, upCarfull]);$$

$$Q[s_1, upCarfull] \leftarrow$$

$$Q[s_3, upCarfull] \leftarrow Q[s_3, upCarfull] + \alpha_k(r + 0.9Q[s_5, Left] - Q[s_3, upCarfull]);$$

$$Q[s_3, upCarfull] \leftarrow 0 + 1(-1 + 0.9 * 0 - 0) = -1$$

$$Q[s_5, Left] \leftarrow Q[s_5, Left] + \alpha_k(r + 0.9Q[s_4, left] - Q[s_5, Left]);$$

$$Q[s_5, Left] \leftarrow 0 + 1(0 + 0.9 * 0 - 0) = 0$$

$$Q[s_4, Left] \leftarrow Q[s_4, Left] + \alpha_k(r + 0.9Q[s_0, Right] - Q[s_4, Left]);$$

$$Q[s_4, Left] \leftarrow 0 + 1(10 + 0.9 * 0 - 0) = 10$$

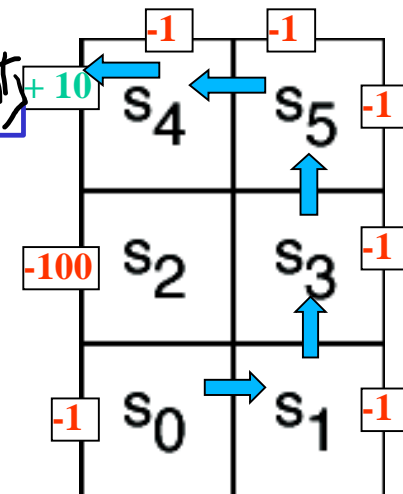
**Only immediate rewards
are included in the update,
as with Q-learning**

$\langle s_0, right, 0, s_1, upCareful, -1, s_3, upCareful, -1, s_5, left, 0, s_4, left, 10, s_0, right \rangle$

$$Q[s, a] \leftarrow Q[s, a] + \alpha(r + \gamma Q[s', a'] - Q[s, a])$$

k=2

Q[s,a]	s_0	s_1	s_2	s_3	s_4	s_5
<i>upCareful</i>	0	-1	0	-1	0	0
<i>Left</i>	0	0	0	0	10	0
<i>Right</i>	0	0	0	0	0	0
<i>Up</i>	0	0	0	0	0	0



$$Q[s_0, right] \leftarrow Q[s_0, right] + \alpha_k(r + 0.9Q[s_1, UpCareful] - Q[s_0, right]);$$

$$Q[s_0, right] \leftarrow$$

SARSA backs up the expected reward of the next action, rather than the max expected reward

$$Q[s_1, upCarfull] \leftarrow Q[s_1, upCarfull] + \alpha_k(r + 0.9Q[s_3, UpCareful] - Q[s_1, upCarfull]);$$

$$Q[s_1, upCarfull] \leftarrow$$

$$Q[s_3, upCarfull] \leftarrow Q[s_3, upCarfull] + \alpha_k(r + 0.9Q[s_5, Left] - Q[s_3, upCarfull]);$$

$$Q[s_3, upCarfull] \leftarrow -1 + 1/2(-1 + 0.9*0 + 1) = -1$$

$$Q[s_5, Left] \leftarrow Q[s_5, Left] + \alpha_k(r + 0.9Q[s_4, left] - Q[s_5, Left]);$$

$$Q[s_5, Left] \leftarrow 0 + 1/2(0 + 0.9*10 - 0) = 4.5$$

$$Q[s_4, Left] \leftarrow Q[s_4, Left] + \alpha_k(r + 0.9Q[s_0, Right] - Q[s_4, Left]);$$

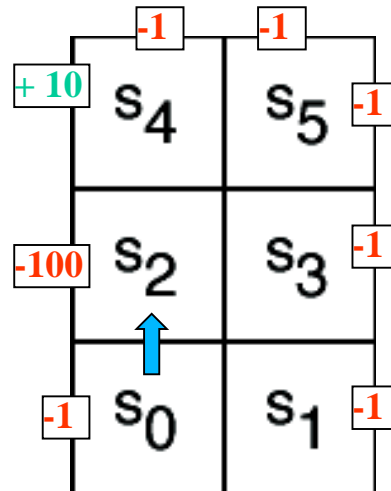
$$Q[s_4, Left] \leftarrow 10 + 1/2(10 + 0.9*0 - 10) = 10$$

Comparing SARSA and Q-learning

➤ For the little 6-states world

➤ Policy learned by **Q-learning** 80% greedy is to go *up* in s_0 to reach s_4 quickly and get the big +10 reward

Iterations	$Q[s_0, \text{Up}]$	$Q[s_1, \text{Up}]$	$Q[s_2, \text{UpC}]$	$Q[s_3, \text{Up}]$	$Q[s_4, \text{Left}]$	$Q[s_5, \text{Left}]$
40000000	19.1	17.5	22.7	20.4	26.8	23.7

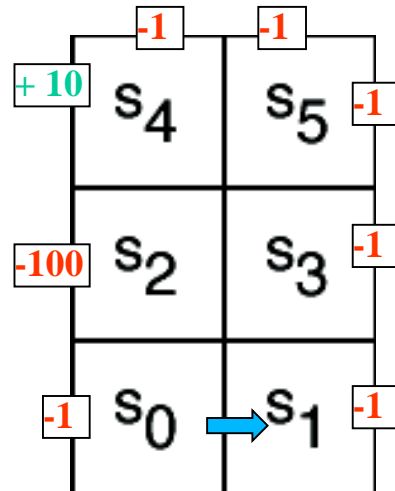


- Verify running full demo, see <http://www.cs.ubc.ca/~poole/aibook/demos/rl/tGame.html>

Comparing SARSA and Q-learning

- Policy learned by **SARSA** 80% greedy is to go *right* in s_0
- Safer because avoid the chance of getting the -100 reward in s_2
- but non-optimal \Rightarrow lower Q-values

Iterations	$Q[s_0, \text{Right}]$	$Q[s_1, \text{Up}]$	$Q[s_2, \text{UpC}]$	$Q[s_3, \text{Up}]$	$Q[s_4, \text{Left}]$	$Q[s_5, \text{Left}]$
40000000	6.8	8.1	12.3	10.4	15.6	13.2



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- Verify running full demo, see <http://www.cs.ubc.ca/~poole/aibook/demos/rl/tGame.html>

SARSA Algorithm

begin

initialize $Q[S, A]$ arbitrarily

observe current state s

select action a using a policy based on Q

repeat forever:

carry out an action a

observe reward r and state s'

select action a' using a policy based on Q

$Q[s, a] \leftarrow Q[s, a] + \alpha (r + \gamma Q[s', a'] - Q[s, a])$

$s \leftarrow s'$;

$a \leftarrow a'$;

end-repeat

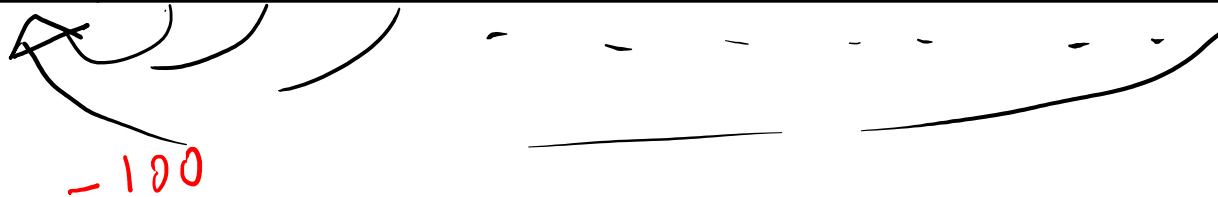
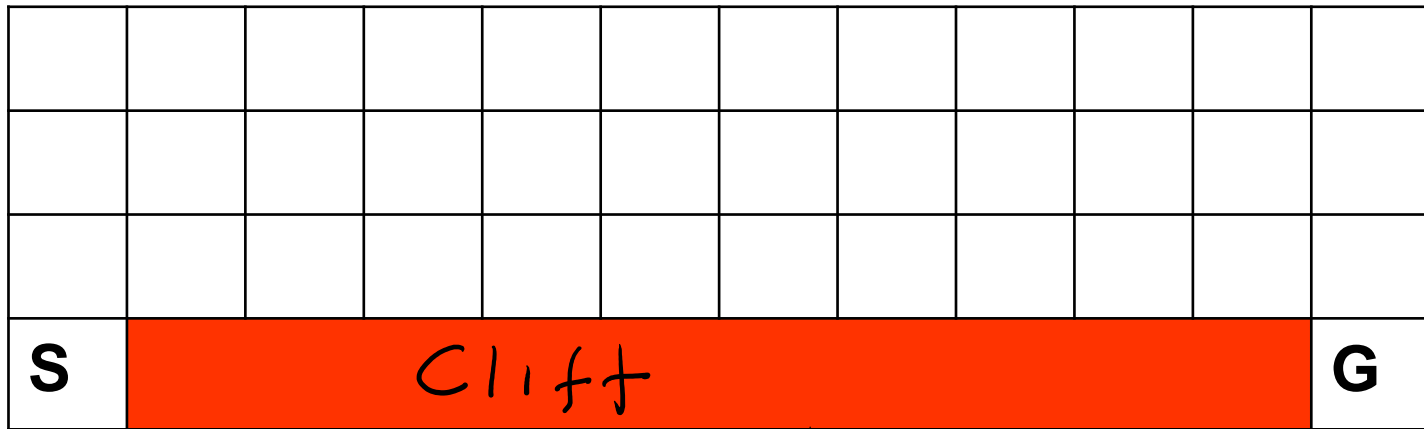
end

This could be, for instance any ϵ -greedy strategy:
-Choose random ϵ times, and max the rest

Another Example

➤ Gridworld with:

- Deterministic actions *up, down, left, right*
- Start from **S** and arrive at **G** (terminal state with reward > 0)
- **Reward is -1 for all transitions**, except those into the **region marked “Cliff”**
 - ✓ Falling into the cliff causes the agent to be sent back to start: **$r = -100$**



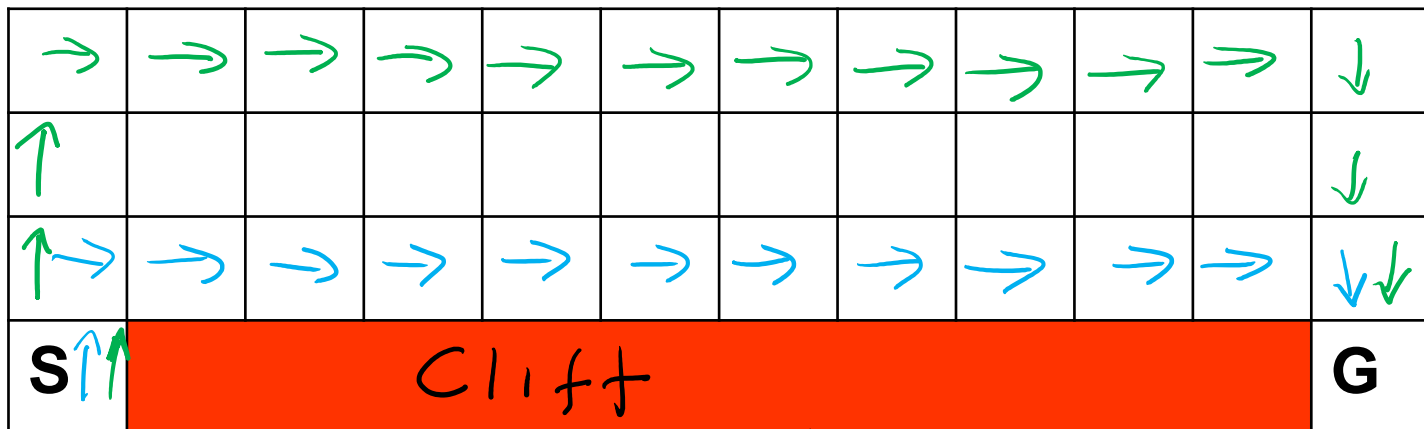
➤ With an ϵ -greedy strategy (e.g., $\epsilon = 0.1$)

A. SARSA will learn policy p1 while Q-learning will learn p2

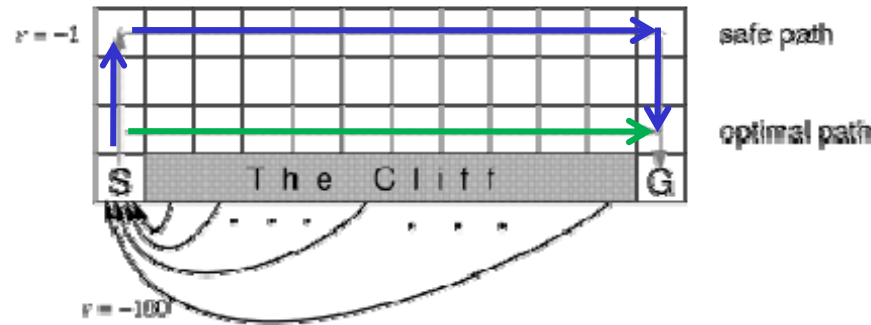
B. Q-learning will learn policy p1 while SARSA will learn p2

C. They will both learn p1

D. They will both learn p2

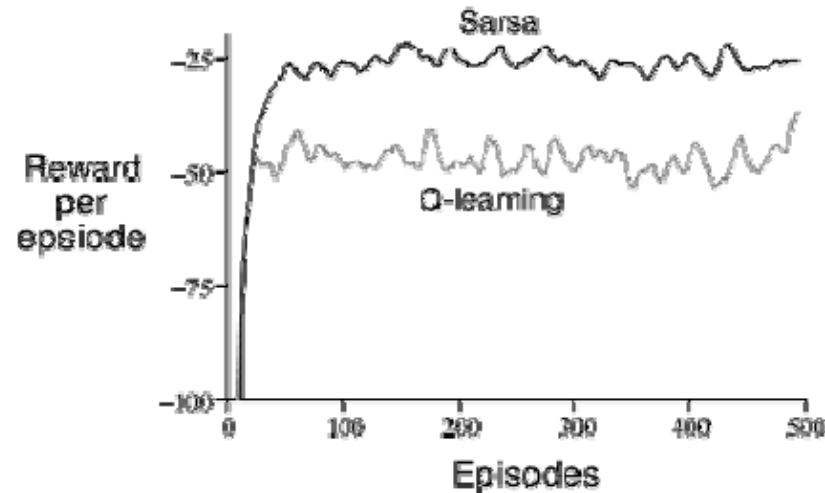


Cliff Example



- Because of **negative reward for every step taken**, the optimal policy over the four standard actions is to take the shortest path along the cliff
- But if the agents adopt an ϵ -greedy action selection strategy with $\epsilon=0.1$, walking along the cliff is dangerous
 - The optimal path that considers exploration is to go around as far as possible from the cliff

Q-learning vs. SARSA

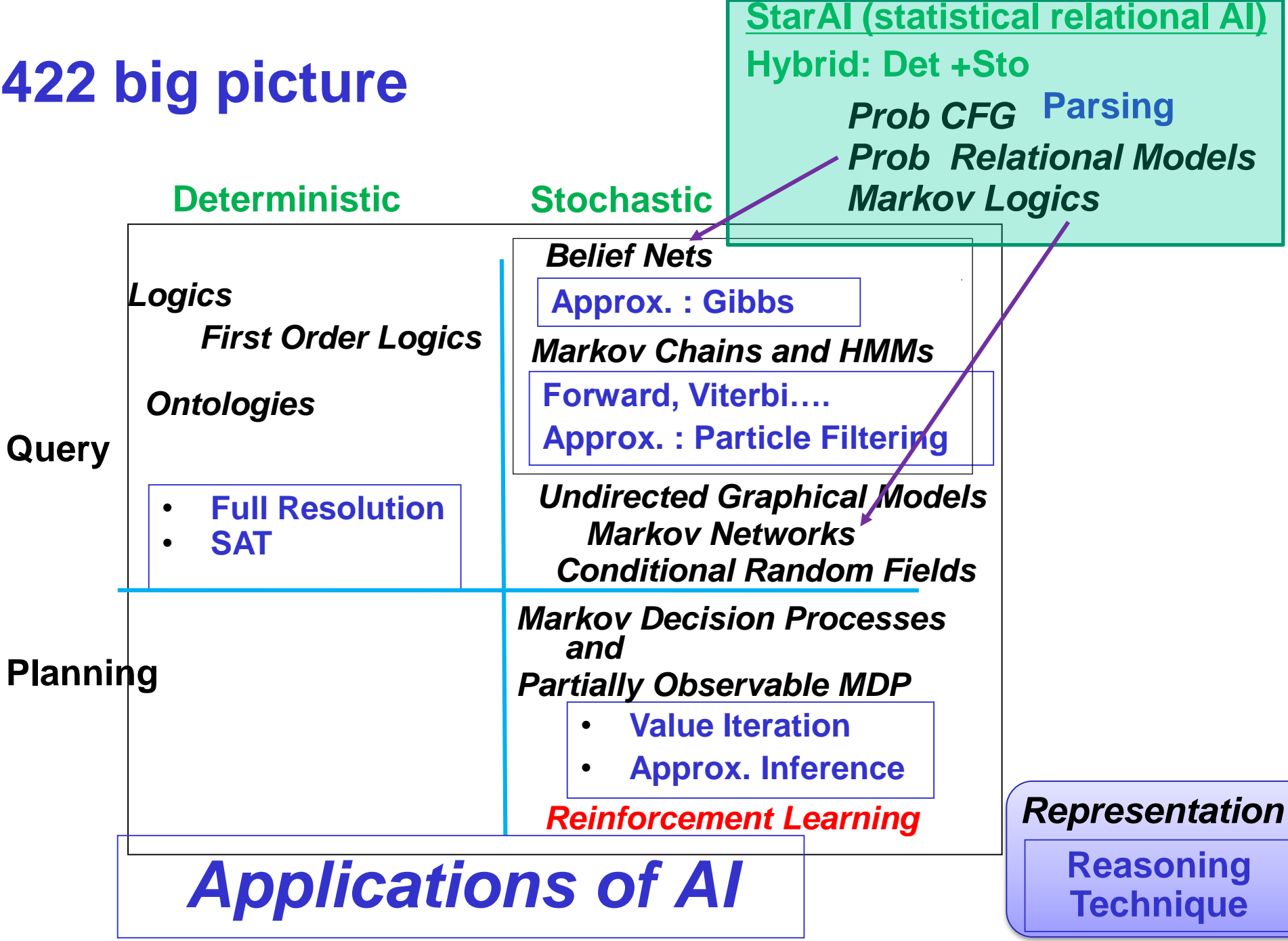


- Q-learning learns the optimal policy, but because it does so **without taking exploration into account**, it does not do so well while the agent is exploring
 - It occasionally falls into the cliff, so its reward per episode is not that great
- SARSA has better on-line performance (reward per episode), because it learns to stay away from the cliff while exploring
 - But note that if $\epsilon \rightarrow 0$, SARSA and Q-learning would asymptotically converge to the optimal policy

Final Recommendation

- If agent is **not deployed** it should do
 - random all the time ($\epsilon=1$) and **Q-learning**
 - When Q values have converged then deploy
- If the agent is **deployed** it should
 - apply one of the explore/exploit strategies (e.g., $\epsilon=.5$) and do Sarsa
 - Decreasing ϵ over time

422 big picture



Learning Goals for today's class

➤ You can:

- Describe and compare techniques to combine exploration with exploitation
- On-policy Learning (SARSA)
- Discuss trade-offs in RL scalability (not required)

TODO for Fri

- Read textbook 6.4.2
- Next research paper will be next Wed
- Practice Ex 11.B
- Assignment 1 due on Fri