

Uniformed Search (cont.)

Computer Science cpsc322, Lecture 6

(Textbook finish 3.5)

May, 18, 2017



Lecture Overview

- **Recap DFS vs BFS**
- Uninformed Iterative Deepening (IDS)
- Search with Costs



Search Strategies



Search Strategies are different with respect to how they:

- A. Check what node on a path is the goal
- B. Initialize the frontier
- C. Add/remove paths from the frontier
- D. Check if a state is a goal

Recap: Graph Search Algorithm

Input: a graph, a start node, Boolean procedure $goal(n)$ that tests if n is a goal node

$frontier := [\langle s \rangle: s \text{ is a start node}]$;

While $frontier$ is not empty:

select and remove path $\langle n_o, \dots, n_k \rangle$ from $frontier$;

If $goal(n_k)$

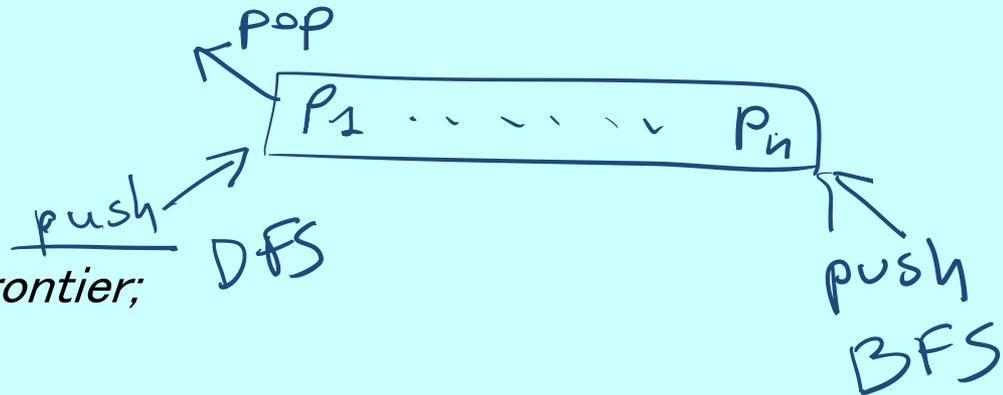
return $\langle n_o, \dots, n_k \rangle$;

For every neighbor n of n_k

add $\langle n_o, \dots, n_k, n \rangle$ to $frontier$;

end

No solution found



In what aspects DFS and BFS differ when we look at the generic graph search algorithm?

When to use BFS vs. DFS?

- The search graph has cycles or is infinite

BFS

DFS

- We need the shortest path to a solution

BFS

DFS

- There are only solutions at great depth

BFS

DFS

- There are some solutions at shallow depth

BFS

DFS

- Memory is limited

BFS

DFS

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Iterative Deepening (sec 3.6.3)

How can we achieve an acceptable (linear) space complexity maintaining completeness and optimality?

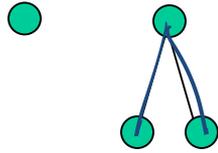
	Complete	Optimal	Time	Space
DFS	\mathcal{N}	\mathcal{N}	b^m	$m b$
BFS	\mathcal{Y}	\mathcal{Y}	b^m	b^m
$\hat{\mathcal{I}}$ IDS	\mathcal{Y}	\mathcal{Y}	b^m	$m b$

Key Idea: let's re-compute elements of the frontier rather than saving them.

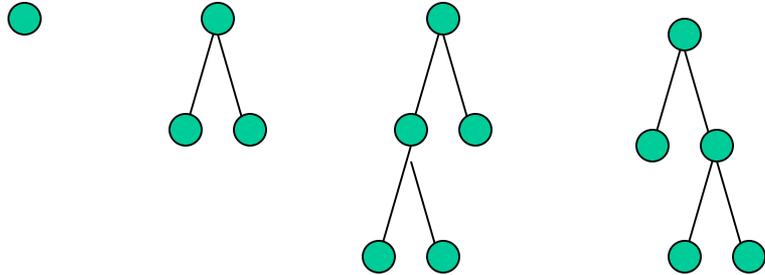
Iterative Deepening in Essence

- **Look with DFS** for solutions at depth 1, then 2, then 3, etc.
- If a solution cannot be found at depth D , look for a solution at depth $D + 1$.
- You need a **depth-bounded depth-first searcher**.
- Given a bound B you simply assume that paths of length B cannot be expanded...

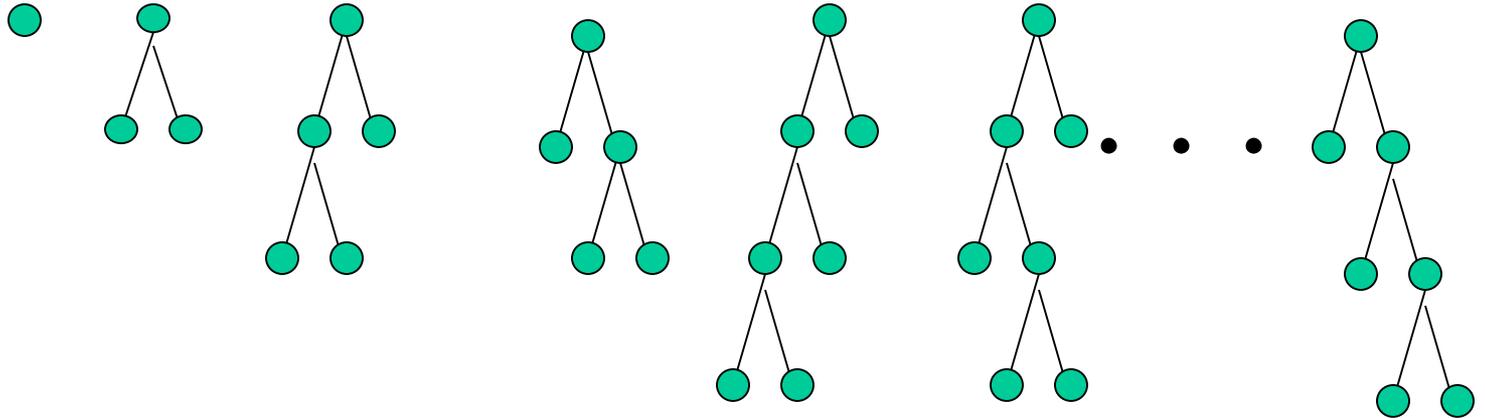
depth = 1



depth = 2



depth = 3



(Time) Complexity of Iterative Deepening

Complexity of solution at depth m with branching factor b

Total # of paths generated

$$b^m + 2b^{m-1} + 3b^{m-2} + \dots + mb = A$$

$A < B$

$$b^m (1 + 2b^{-1} + 3b^{-2} + \dots + mb^{1-m}) \leq B$$

$$b^m \left(\sum_{i=1}^{\infty} ib^{1-i} \right) = b^m \left(\frac{b}{b-1} \right)^2 = O(b^m)$$

$$b = 2$$

$$\boxed{4}$$

$$b = 3$$

$$\frac{9}{4} = \boxed{2.25}$$

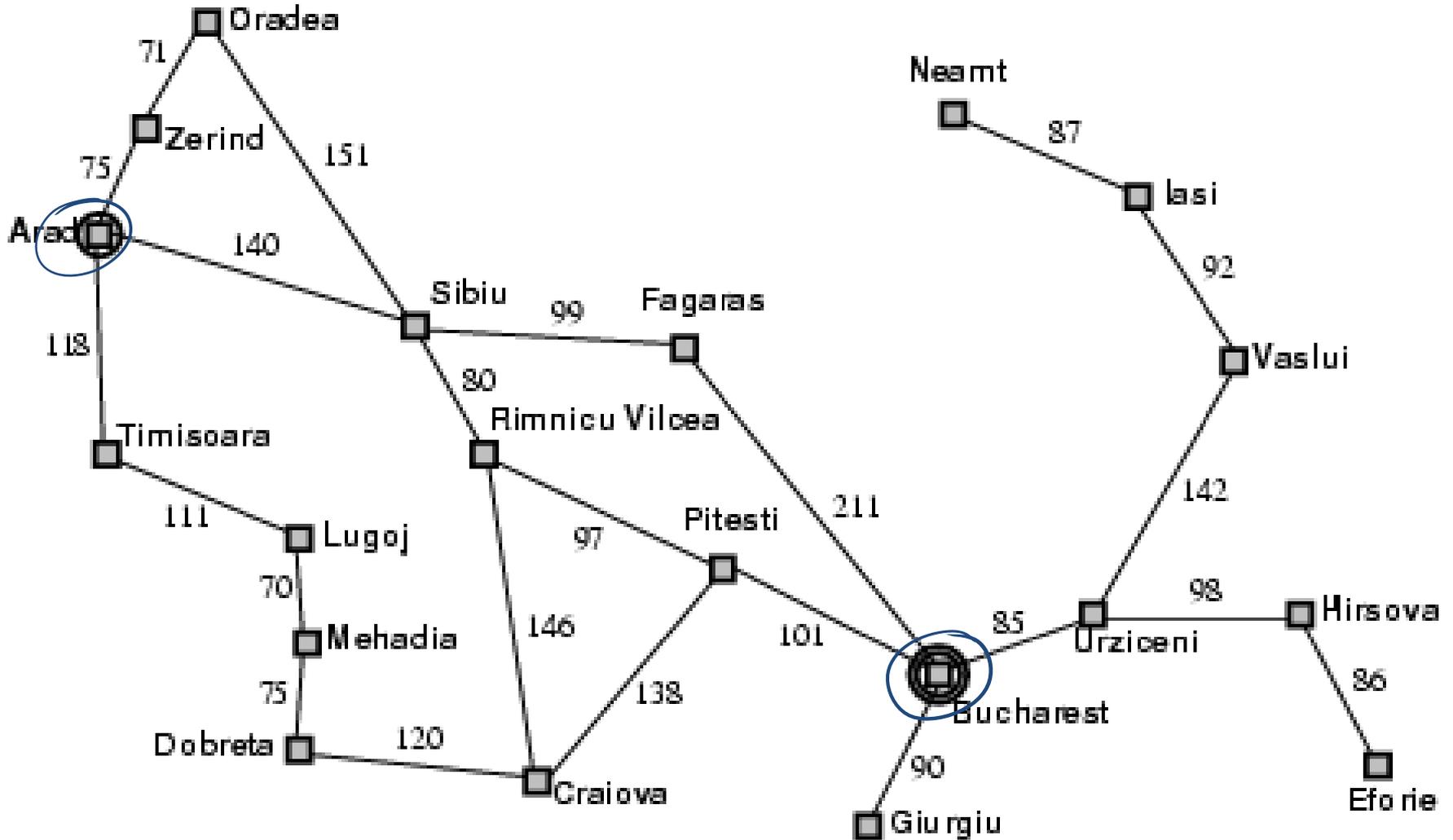
$$b = 4$$

$$\boxed{\frac{16}{4} < 2}$$

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Example: Romania



Search with Costs

Sometimes there are **costs** associated with arcs.

Definition (cost of a path)

The cost of a path is the sum of the costs of its arcs:

$$\text{cost}(\langle n_0, \dots, n_k \rangle) = \sum_{i=1}^k \text{cost}(\langle n_{i-1}, n_i \rangle)$$

In this setting we often don't just want to find just any solution

- we usually want to find the solution that **minimizes cost**

Definition (optimal algorithm)

A search algorithm is **optimal** if, when it returns a solution, it is the one with minimal cost.

Lowest-Cost-First Search

- At each stage, lowest-cost-first search selects a path on the frontier with **lowest cost**.
 - The frontier is a **priority queue ordered by path cost**
 - We say “a path” because there may be ties

- **Example of one step for LCFS:**

- the frontier is $[\langle p_2, 5 \rangle, \langle p_3, 7 \rangle, \langle p_1, 11 \rangle,]$
- p_2 is the lowest-cost node in the frontier
- “neighbors” of p_2 are $\{\langle p_9, 10 \rangle, \langle p_{10}, 15 \rangle\}$
- What happens?
 - p_2 is selected, and tested for being a goal (its end).
 - (if not a goal) Neighbors of p_2 are inserted into the frontier
 - Thus, the frontier is now $[\langle p_3, 7 \rangle, \langle p_9, 10 \rangle, \langle p_1, 11 \rangle, \langle p_{10}, 15 \rangle]$.
 - ? p_3 ? is selected next.
 - Etc. etc.

- When arc costs are equal LCFS is equivalent to..
 - A. DFS
 - B. BFS**
 - C. IDS
 - D. None of the Above

Analysis of Lowest-Cost Search (1)

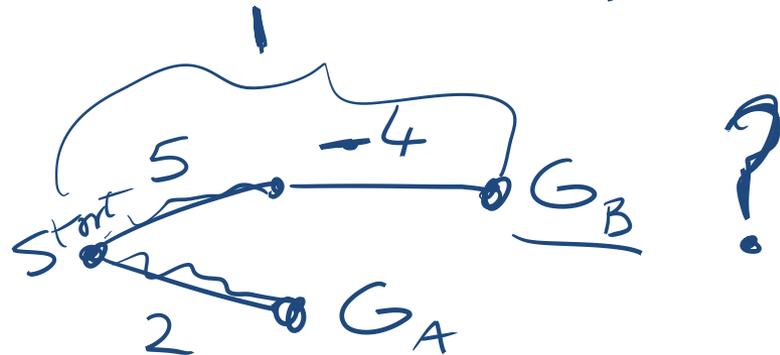
- Is LCFS **complete**?

- not in general: a cycle with zero or negative arc costs could be followed forever

AI space

- yes, as long as arc costs are strictly positive

cost > 0



- Is LCFS **optimal**?

- Not in general. Why not?

- Arc costs could be negative: a path that initially looks high-cost could end up getting a “refund”.

- However LCFS *is* optimal if arc costs are guaranteed to be non-negative.

cost ≥ 0

Analysis of Lowest-Cost Search

- What is the **time complexity**, if the maximum path length is m and the maximum branching factor is b ?
 - The time complexity is $O(b^m)$. must examine every node in the tree.
 - Knowing costs doesn't help here.
- What is the **space complexity**?
 - Space complexity is $O(b^m)$. we must store the whole frontier in memory.

Learning Goals for Search (up to today)

- Apply basic properties of search algorithms: completeness, optimality, time and space complexity of search algorithms.

	Complete	Optimal	Time	Space
DFS	N	N	b^m	$b \cdot m$
BFS	Y	Y	n	b^m
ID3	Y	Y	1	$b \cdot m$
LEFS	N Y if $c > 0$	N Y if $c \geq 0$	b^m b	b^m b

Learning Goals for Search (cont') (up to today)

- Select the most appropriate search algorithms for specific problems.

• ~~BFS vs DFS vs IDS vs BidirS~~

• ~~LCFS vs. BFS =~~

• ~~A* vs. B&B vs IDA* vs MBA*~~

uninformed

informed

- Define/read/write/trace/debug different search algorithms
 - With / Without cost
 - ~~Informed~~ / Uninformed

Beyond uninformed search...



What information we could use to better select paths from the frontier

- A. an estimate of the distance from the last node on the path to the goal
- B. an estimate of the distance from the start state to the goal
- C. an estimate of the cost of the path
- D. None of the above

Next Class on Tue

- **Heuristic Search**

(read textbook.: 3.6)

- Best-First Search
- Combining LCFS and BFS: A* (finish 3.6)
- A* Optimality

Finish Search (finish Chpt 3)

- Branch-and-Bound
- A* enhancements
- Non-heuristic Pruning
- Dynamic Programming