Search: Advanced Topics

Computer Science cpsc322, Lecture 9

(Textbook Chpt 3.6)

Sept, 24, 2010





- Recap A*
- Branch & Bound
- A^{*} tricks
- Other Pruning

Branch-and-Bound Search

• What is the biggest advantage of A*?

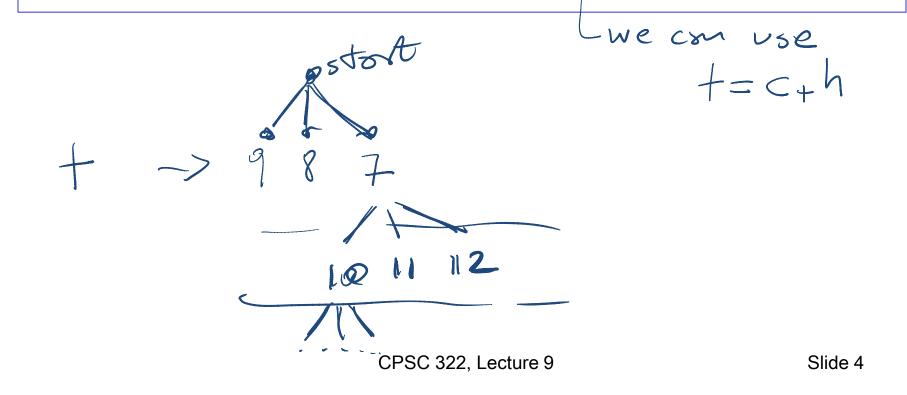
• What is the biggest problem with A*?

• Possible Solution:

DFS + h

Branch-and-Bound Search Algorithm

- Follow exactly the same search path as depth-first search
 - treat the <u>frontier as a stack</u>: expand the most-recently added path first
 - the order in which neighbors are expanded can be governed by some arbitrary node-ordering heuristic

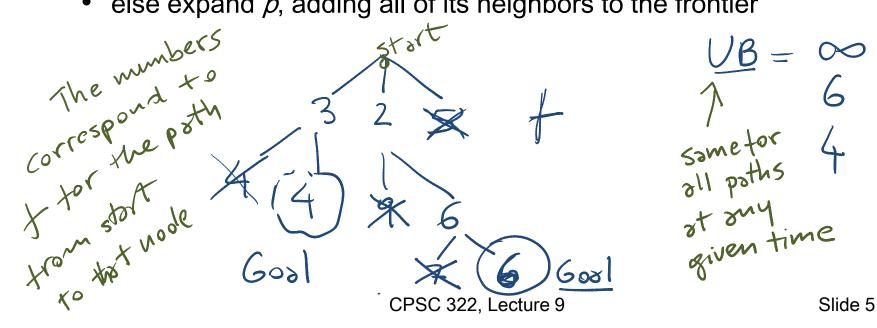


Branch-and-Bound Search Algorithm

- Keep track of a lower bound and upper bound on solution cost at each path
 - lower bound: LB(p) = f(p) = cost(p) + h(p)
 - upper bound: UB = cost of the best solution found so far.

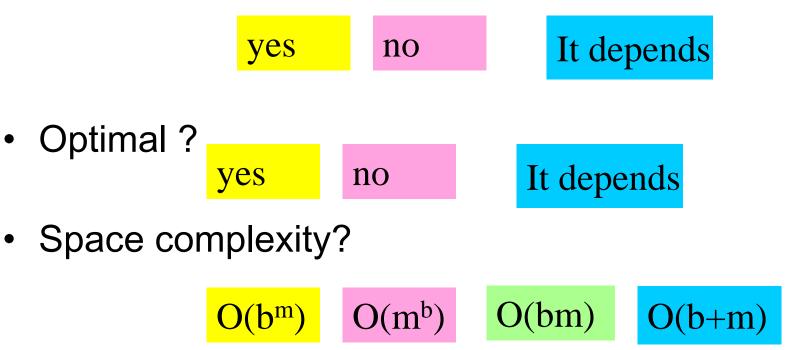
 \checkmark if no solution has been found yet, set the upper bound to ∞ .

- When a path *p* is selected for expansion:
 - if $LB(p) \ge UB$, remove p from frontier without expanding it (pruning)
 - else expand *p*, adding all of its neighbors to the frontier



Branch-and-Bound Analysis

• Complete ?



• Time complexity?

Branch-and-Bound Analysis

- Completeness: no, for the same reasons that DFS isn't complete
 - however, for many problems of interest there are no infinite paths and no cycles
 - hence, for many problems B&B is complete
- Time complexity: $O(b^m)$
- Space complexity: O(bm)
 - Branch & Bound has the same space complexity as.
 - this is a big improvement over …A[★].....!
- Optimality: 4es

Lecture Overview

- Recap A*
- Branch & Bound
- A* tricks
- Pruning Cycles and Repeated States

Other A* Enhancements

The main problem with A^* is that it uses exponential space. Branch and bound was one way around this problem. Are there others?

Itenshve Deepeng AX INA*

• Memory-bounded A^{*}

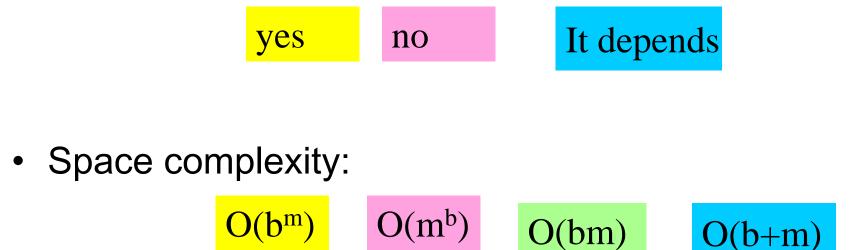
(Heuristic) Iterative Deepening – IDA*

- **B & B** can still get stuck in infinite (extremely long) paths
- Search depth-first, but to a fixed depth/bound
 - if you don't find a solution, increase the depth tolerance and try again

 - depth is measured inf. stort mode + (stort) = ha(stort)
 - Then update with the lowest f..... that passed the previous bound

Analysis of Iterative Deepening A* (IDA*)

• Complete and optimal:



• Time complexity:



(Heuristic) Iterative Deepening – IDA*

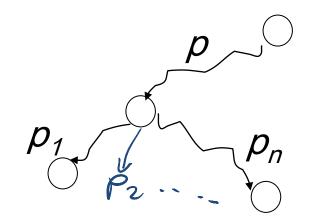
 Counter-intuitively, the asymptotic complexity is not changed, even though we visit paths multiple times (<u>go back to slides on uninformed ID</u>)



Memory-bounded A*

- Iterative deepening A* and B & B use a tiny amount of memory
- what if we've got more memory to use?
- keep as much of the fringe in memory as we can
- if we have to delete something:

 - ``back them up" to a common ancestor



MBA*: Compute New h(p) p_n New $h(p) = min \max[(cost(p_i) - cost(p)) + h(p_i)], Old h(p)$ New $h(p) = max \lim_{i \to i} [(cost(p_i) - cost(p)) + h(p_i)], Old h(p)$

Memory-bounded A*

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• "back them up" to a common ancesto min max p_1 p_n p_n h(p) = 1 $cost(p_1) - cost(p) + h(p_1)$ p_2 p_2 p_n h(p) = 1 $cost(p_1) - cost(p) + h(p_2)$ p_1 p_2 p_2

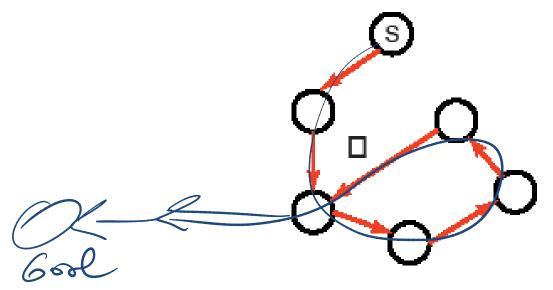
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Slide 15

Lecture Overview

- Recap A*
- Branch & Bound
- A* tricks
- Pruning Cycles and Repeated States

Cycle Checking



You can prune a path that ends in a node already on the path. This pruning cannot remove an optimal solution.

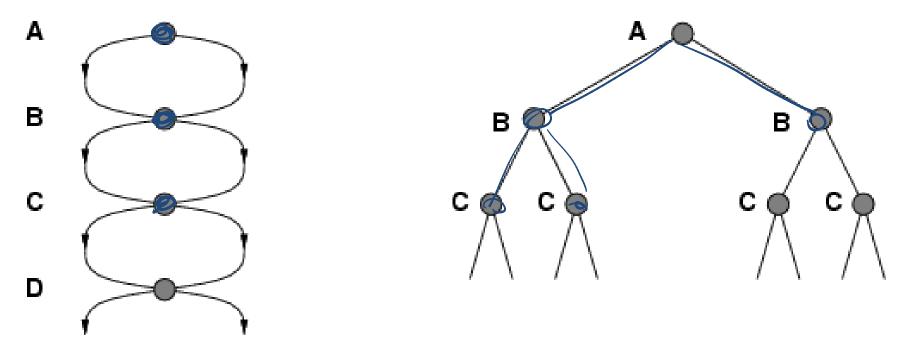
• The time is <u>line</u> in path length.



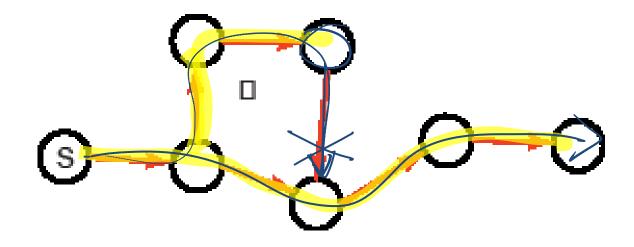
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Repeated States / Multiple Paths

Failure to detect repeated states can turn a linear problem into an exponential one!



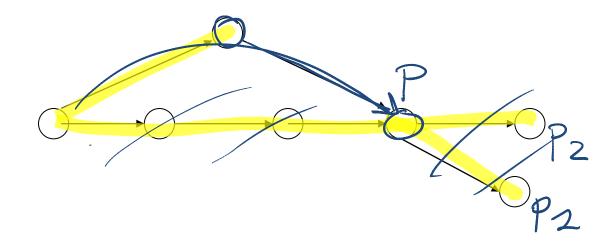
Multiple-Path Pruning



- •You can prune a path to node *n* that you have already found a path to
- (if the new path is longer more costly).

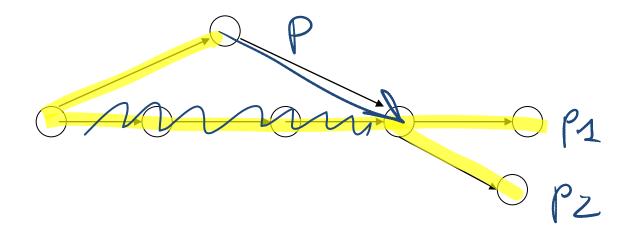
Multiple-Path Pruning & Optimal Solutions

- Problem: what if a subsequent path to *n* is shorter than the first path to *n*?
- You can remove all paths from the frontier that use the longer path. (as these can't be optimal)



Multiple-Path Pruning & Optimal Solutions

- Problem: what if a subsequent path to *n* is shorter than the first path to *n*?
- You can change the initial segment of the paths on the frontier to use the shorter path.



Learning Goals for today's class

•Define/read/write/trace/debug different search algorithms

- •With / Without cost
- Informed / Uninformed
- Pruning cycles and Repeated States

Next class

- Dynamic Programming
- Recap Search
- Start Constraint Satisfaction Problems (CSP)
- Chp 4.

• Start working on assignment-1 !