# **Uniformed Search (cont.)**

#### Computer Science cpsc322, Lecture 6

#### (Textbook finish 3.5)

Sept, 17, 2012



#### **Lecture Overview**

- Recap DFS vs BFS
- Uninformed Iterative Deepening (IDS)
- Search with Costs

## **Recap: Graph Search Algorithm**

- **Input:** a graph, a start node, Boolean procedure *goal(n)* that tests if *n* is a goal node
- frontier:=[<s>: s is a start node]; While frontier is not empty: select and remove path  $< n_o, ..., n_k >$  from frontier; If goal( $n_k$ ) return  $< n_o, ..., n_k >$ ; For every neighbor n of  $n_k$  push add  $< n_o, ..., n_k$ , n> to frontier; DFS end

In what aspects DFS and BFS differ when we look at the generic graph search algorithm?

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## When to use BFS vs. DFS?

- The search graph has cycles or is infinite
  BFS DFS
- We need the shortest path to a solution
  BFS DFS
- There are only solutions at great depth



• There are some solutions at shallow depth



• Memory is limited



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#### Iterative Deepening (sec 3.6.3)

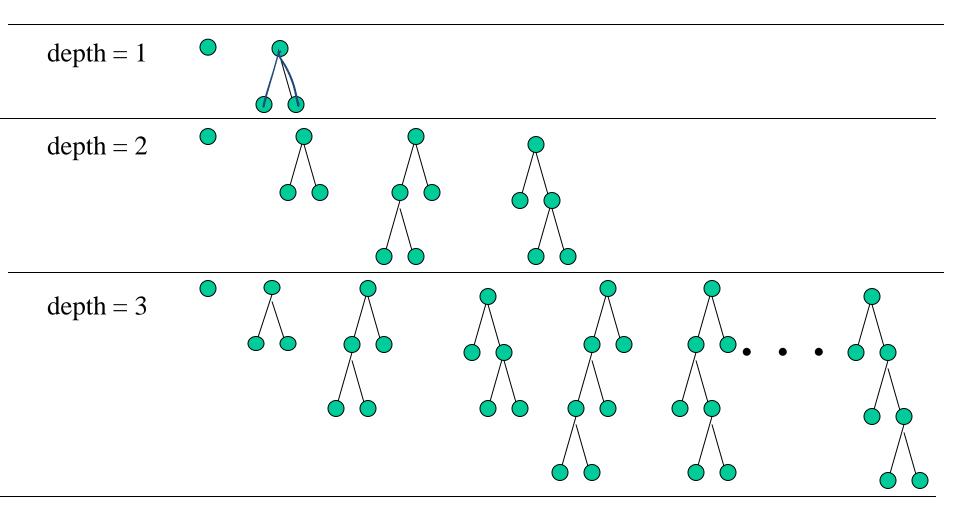
How can we achieve an acceptable (linear) space complexity maintaining completeness and optimality?

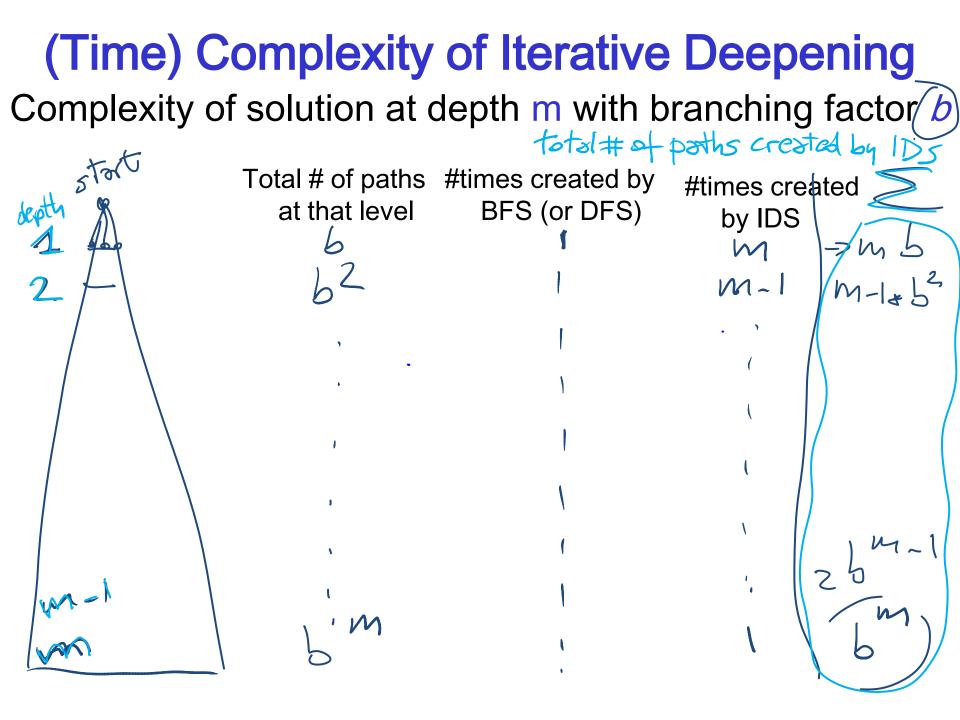
	Complete	Optimal	Time	Space
DFS	N		6 m	m 5
BFS	R	Y	bm	5 m
L'IDS	Y	Y	6 m	mb

Key Idea: let's re-compute elements of the frontier rather than saving them.

#### **Iterative Deepening in Essence**

- Look with DFS for solutions at depth 1, then 2, then 3, etc.
- If a solution cannot be found at depth D, look for a solution at depth D + 1.
- You need a depth-bounded depth-first searcher.
- Given a bound B you simply assume that paths of length B cannot be expanded....



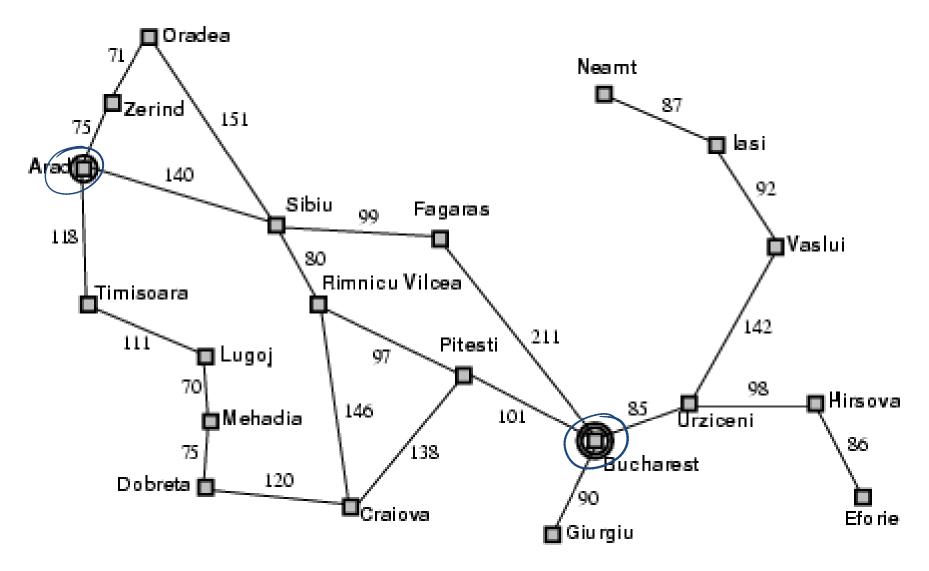


# (Time) Complexity of Iterative Deepening Complexity of solution at depth m with branching factor b Total # of paths generated ALB $b^{m} + 2b^{m-1} + 3b^{m-2} + ..+ mb = A$ $(1+2b^{-1}+3b^{-2}+..+mb^{1-m})$ CPSC 322, Lecture 6 Slide 10

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#### **Example: Romania**



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#### **Search with Costs**

Sometimes there are costs associated with arcs.

**Definition (cost of a path)** The cost of a path is the sum of the costs of its arcs:  $\operatorname{cost}(\langle n_0, \dots, n_k \rangle) = \sum_{i=1}^k \operatorname{cost}(\langle n_{i-1}, n_i \rangle)$ 

In this setting we often don't just want to find just any solution

we usually want to find the solution that minimizes cost

**Definition (optimal algorithm)** 

A search algorithm is optimal if it is complete, and only returns cost-minimizing solutions.

#### Lowest-Cost-First Search

- At each stage, lowest-cost-first search selects a path on the frontier with lowest cost.
  - The frontier is a priority queue ordered by path cost
  - We say ``a path" because there may be ties
- Example of one step for LCFS:
  - the frontier is  $[\langle p_2, 5 \rangle, \langle p_3, 7 \rangle, \langle p_1, 11 \rangle, ]$
  - (p) is the lowest-cost node in the frontier
  - "neighbors" of *p*<sub>2</sub> are {(*p*<sub>9</sub>, 10), (*p*<sub>10</sub>, 15)}
- What happens?
  - $p_2$  is selected, and tested for being a goal.
  - Neighbors of  $p_2$  are inserted into the frontier
  - Thus, the frontier is now [(p<sub>3</sub>, 7), (p<sub>9</sub>, 10), (p<sub>1</sub>, 11), (p<sub>10</sub>, 15)].
  - ?  $\rho_3$  ? is selected next.
  - Etc. etc. CPSC 322, Lecture 6



• When arc costs are equal LCFS is equivalent to...



#### None of the above



## Analysis of Lowest-Cost Search (1)

- Is LCFS complete?
  - not in general: a cycle with zero or negative arc costs could be followed forever.
  - yes, as long as arc costs are strictly positive

- Is LCFS optimal?
  - Not in general. Why not?
  - Arc costs could be negative: a path that initially looks high-cost could end up getting a ``refund".
  - However, LCFS *is* optimal if arc costs are guaranteed to be non-negative.

#### **Analysis of Lowest-Cost Search**

- What is the time complexity, if the maximum path length is *m* and the maximum branching factor is *b*?
  - The time complexity is *O(b<sup>m</sup>)*: must examine every node in the tree.
  - Knowing costs doesn't help here.

- What is the space complexity?
  - Space complexity is  $O(b^m)$  we must store the whole frontier in memory.

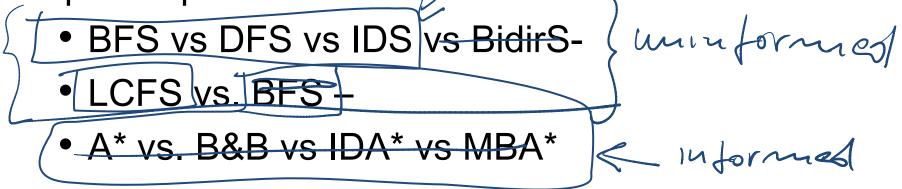
## Learning Goals for Search (up to today)

 Apply basic properties of search algorithms: completeness, optimality, time and space complexity of search algorithms.

	Complete	Optimal	Time	Space
DFS	$\sim$	$\sim$	bm	bu
BFS	Y	Y	N	bm
IDS	Y	Y	11	bm
LEPS	Y it c>0	N $Y_1 + C > C$	p b	5m

## Learning Goals for Search (cont') (up to today)

Select the most appropriate search algorithms for specific problems.



- Define/read/write/trace/debug different search algorithms
  - With / Without cost
  - Informed / Uninformed

#### Beyond uninformed search....

• So far the selection of the next path to examine (and possibly expand) is based on

. . . .

#### **Next Class**

# • Start Heuristic Search (textbook.: start 3.6)