Reasoning Under Uncertainty: Belief Networks

Computer Science cpsc322, Lecture 27 (Textbook Chpt 6.3)

Nov, 9, 2012



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Slide 1

Big Picture: R&R systems



Answering Query under Uncertainty



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Key points Recap

- We model the environment as a set of $\underline{X_{n}}$ was $X_{n} \xrightarrow{} X_{n} \xrightarrow{} \mathbb{T}^{PD} \mathbb{P}(X_{1} \cdots X_{n})$
- Why the joint is not an adequate representation ?

Solution: Exploit marginal&conditional independence P(X|Y) = P(X) P(X|YZ) = P(X|Z)

But how does independence allow us to simplify the joint?

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Lecture Overview

Belief Networks

- Build sample BN
- Intro Inference, Compactness, Semantics
- More Examples

Belief Nets: Burglary Example

There might be a **burglar** in my house

The anti-burglar alarm in my house may go off

I have an agreement with two of my neighbors, John and Mary, that they call me if they hear the alarm go off when I am at work

Minor earthquakes may occur and sometimes the set off the alarm.

Variables: BAMJE N=5Joint has $2^{5}-1$ entries/probs $2^{N}-1$

Belief Nets: Simplify the joint

- Typically order vars to reflect causal knowledge (i.e., causes *before effects*)
 - A burglar (B) can set the alarm (A) off
 - An earthquake (E) can set the alarm (A) off
 - The alarm can cause Mary to call (M)
 - The alarm can cause John to call (J)

• Apply Chain Rule marginal indep-

• Simplify according to marginal&conditional independence

Belief Nets: Structure + Probs $\rightarrow P(B) * P(E) * P(A|B,E) * P(M|A) * P(J|A)$

- Express remaining dependencies as a network
 - Each var is a node
 - For each var, the conditioning vars are its parents
 - Associate to each node corresponding conditional probabilities $E^{P(E)^{c}}$ $P(A|B,E)^{c}$

A

Directed Acyclic Graph (DAG)

P(MA)



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Burglary Example: Bnets inference

Our BN can answer any probabilistic query that can be answered by processing the joint!

(Ex1) I'm at work,

- neighbor John calls to say my alarm is ringing,
 - neighbor Mary doesn't call.
- No news of any earthquakes.
 - Is there a burglar?

(Ex2) I'm at work, Try tus

- Receive message that neighbor John called ,
- News of minor earthquakes.
- Is there a burglar?

Set digital places to monitor to 5





Bayesian Networks – Inference Types



BNnets: Compactness

P(B=T) F			P(E=T)	P(E=F)						
.001	.999	Butalary		(E	orthquake		.002	.998]	
1										
				Ε	P(A=T B,E)	<i>P(A</i> =	:F <mark>B,E</mark>)			
V.C.			Т	Т	.95		.05			
(Alarm)			Т	F	.94		.06	< 4	_	
				Т	.29		.71	\leq		
				F	.001		.999 🧲			
(John Calls) Mars Calls										
					orycans) A	P(M=T /	A) P(M=	=F <mark>A</mark>)	
A	<i>P(J=T A)</i>	P(J=F A)				Т	.70		.30	
Т	.90	.10	2		2	F	.01		.99	
F	.05	.95	1	_						
BNet										
2+2+4+1+1=1									10	
JFP J = Z - I						Slide 13				



For *k*<< *n*, this is a substantial improvement,

 the numbers required grow linearly with n, vs. O(2ⁿ) for the full joint distribution

BNets: Construction General Semantics

The full joint distribution can be defined as the product of conditional distributions:

$$P(X_1, \dots, X_n) = \prod_{i=1}^n P(X_i | X_1, \dots, X_{i-1})$$
 (chain rule)

Simplify according to marginal&conditional independence

- Express remaining dependencies as a network
 - Each var is a node
 - For each var, the conditioning vars are its parents
 - Associate to each node corresponding conditional probabilities

$$P(X_1, \dots, X_n) = \prod_{i=1}^n P(X_i | Parents(X_i))$$

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BNets: Construction General Semantics (cont')

$$P(X_1, \ldots, X_n) = \Pi_{i=1} P(X_i | Parents(X_i))$$

n

 Every node is independent from its non-descendants given it parents \bigcirc \bigcirc (1)

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Other Examples: Fire Diagnosis (textbook Ex. 6.10)

- Suppose you want to diagnose whether there is a fire in a building
- you receive a <u>noisy report</u> about whether everyone is <u>leaving the building</u>.
- if everyone is leaving, this may have been caused by a fire alarm.
- if there is a fire alarm, it may have been caused by a fire or by tampering
- if there is a fire, there may be smoke raising from the bldg.



Other Examples (cont')

- Make sure you explore and understand the Fire Diagnosis example (we'll expand on it to study Decision Networks)
- Electrical Circuit example (textbook ex 6.11)



- Patient's wheezing and coughing example (ex. 6.14)
- Several other examples on





Realistic BNet: Liver Diagnosis

Source: Onisko et al., 1999



Learning Goals for today's class

You can: Build a Belief Network for a simple domain

Classify the types of inference Diagnostic, Predictive, Intercousal, Mixed

Compute the representational saving in terms on number of probabilities required

Next Class (Wednesday!)

Bayesian Networks Representation

- Additional Dependencies encoded by BNets
- More compact representations for CPT
- Very simple but extremely useful Bnet (Bayes Classifier)

Belief network summary

- A belief network is a directed acyclic graph (DAG) that effectively expresses independence assertions among random variables.
- The parents of a node X are those variables on which X directly depends.
- Consideration of causal dependencies among variables typically help in constructing a Bnet