Department of Computer Science Undergraduate Events More details @ <u>https://www.cs.ubc.ca/students/undergrad/life/upcoming-events</u>

SAP Code Slam

Sat. Oct 13 noon to Sun. Oct 14 noon DMP 110

IBM Info Session Tues. Oct 16 5:30 pm Wesbrook 100

Global Relay Open House

Thurs. Oct 18 4:30 – 6:30 pm 220 Cambie St. 2nd Floor

Stochastic Local Search

Computer Science cpsc322, Lecture 15

(Textbook Chpt 4.8)

Oct, 10, 2012

Announcements

- Thanks for the feedback, we'll discuss it on Mon
- Assignment-2 on CSP will be out on Fri (programming!)

Lecture Overview

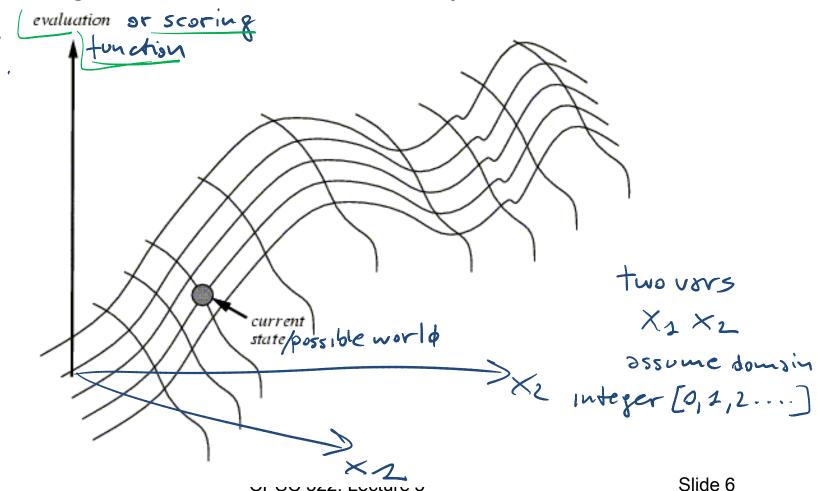
- Recap Local Search in CSPs
- Stochastic Local Search (SLS)
- Comparing SLS algorithms

Local Search: Summary

- A useful method in practice for large CSPs
 - Start from a possible world (randomly chosen)
 - Generate some neighbors ("similar" possible worlds) e.g. differ from current poss. world only by one variable's value
 - Move from current node to a neighbor, selected to _minimize/maximize a scoring function which combines:
 - ✓ Info about how many constraints are violated
 - Information about the cost/quality of the solution (you want the best solution, not just a solution)

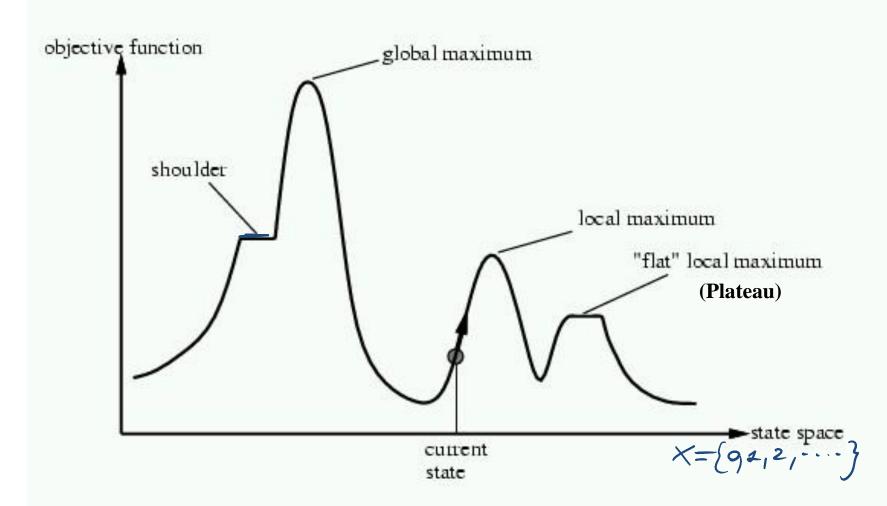
Hill Climbing

NOTE: Everything that will be said for Hill Climbing is also true for Greedy Descent

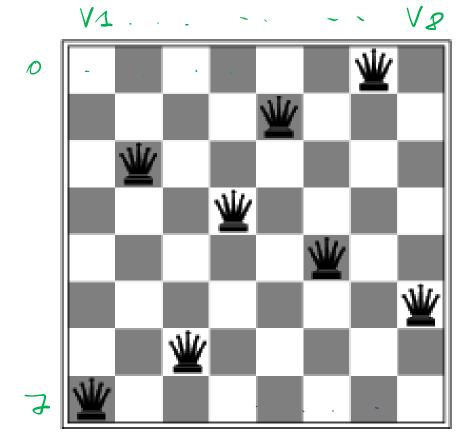


Problems with Hill Climbing

Local Maxima. Plateau - Shoulders



Corresponding problem for GreedyDescent Local minimum example: 8-queens problem

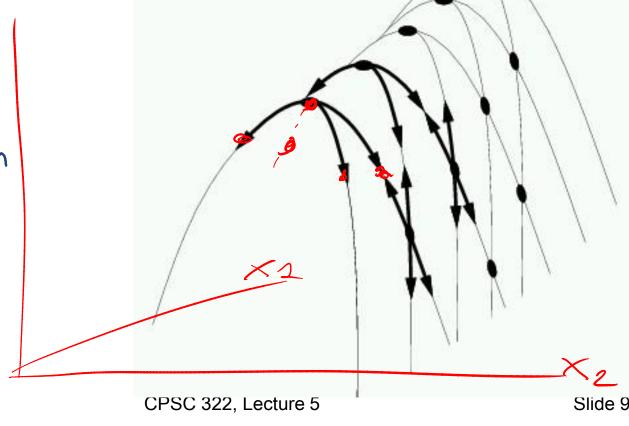


A local minimum with h = 1

Even more Problems in higher dimensions

E.g., Ridges – sequence of local maxima not directly connected to each other
From each local maximum you can only go downhill





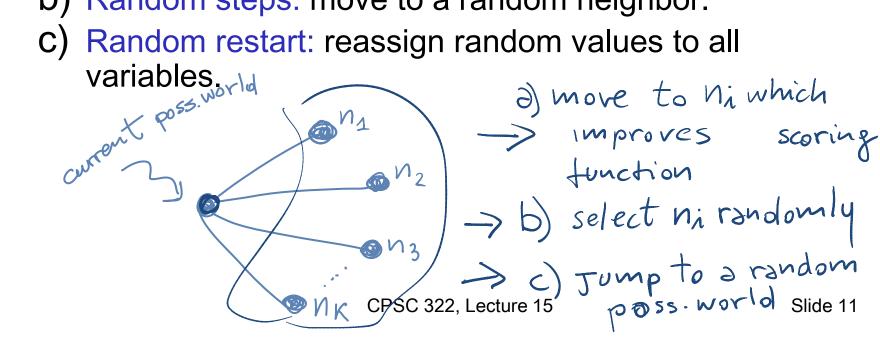
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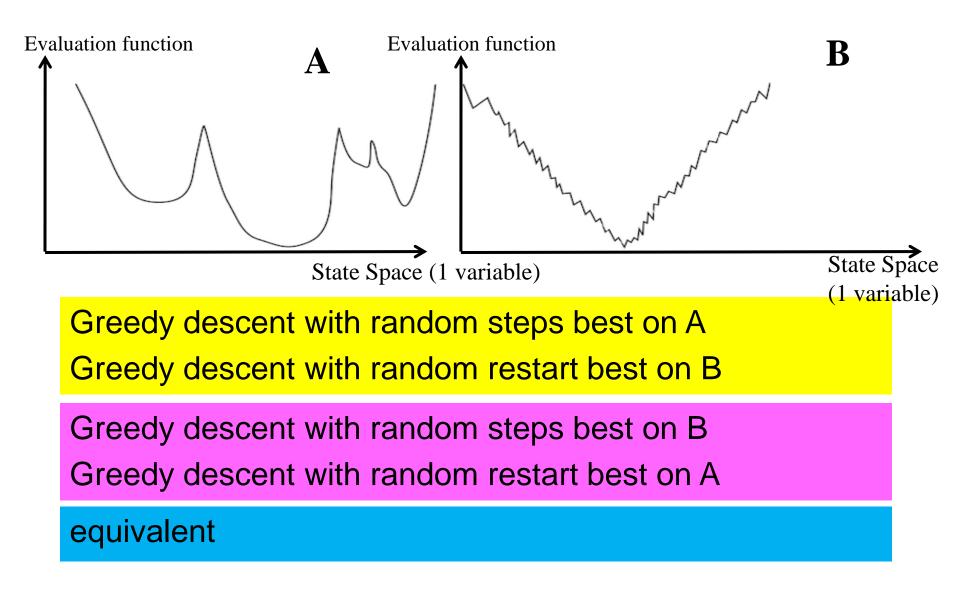
Stochastic Local Search

GOAL: We want our local search

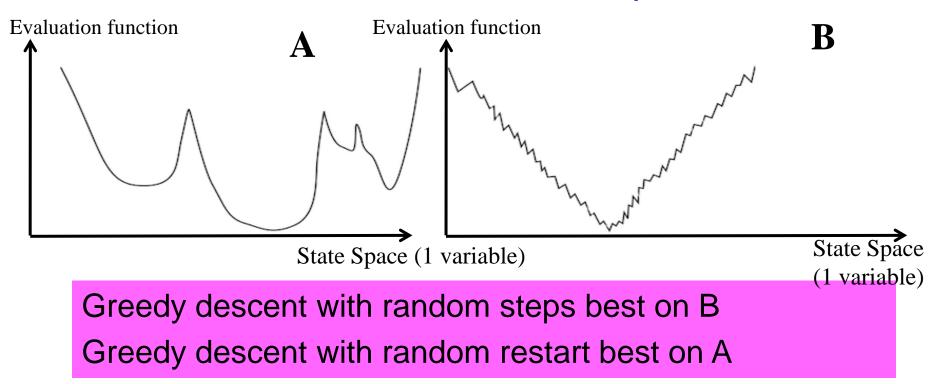
- to be guided by the scoring function
- Not to get stuck in local maxima/minima, plateaus etc.
- SOLUTION: We can alternate
 - a) Hill-climbing steps
 - Random steps: move to a random neighbor. b)
 - Random restart: reassign random values to all



Which randomized method would work best in each of these two search spaces?



Which randomized method would work best in each of the these two search spaces?



- But these examples are simplified extreme cases for illustration
 - in practice, you don't know what your search space looks like
- Usually integrating both kinds of randomization works best

Random Steps (Walk)

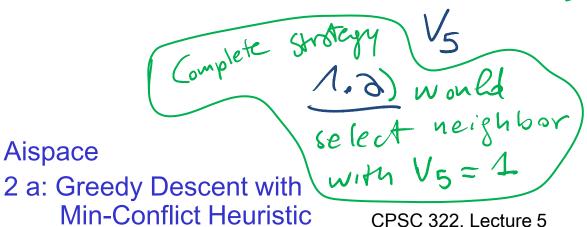
Let's assume that neighbors are generated as

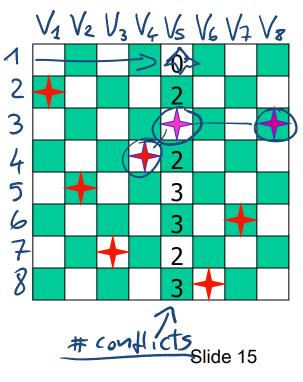
- <u>assignments</u> that differ in one variable's value
- How many neighbors there are given n variables with domains with d values? -1)One strategy to add randomness to the growthes selection variable-value pair. Sometimes choose the pair V1 V2 V3 V4 V5 V6 V2 V8 C According to the scoring function 18 12 13 12 14 13 14 14 15 16 13 16 A random one 12 18 13 15 12 14 How many neighbors? 8.7=56 volues E.G in 8-queen 16 13 13 16 14 17 16 15 16 • 1 choose one of the circled ones fuds 18 15 16 7 15 18 15 16 2 choose roudomlyone of the 14 17 13 18 CPSC 322. Lecture 5 Slide 14

Random Steps (Walk): two-step

Another strategy: select a variable first, then a value:

- Sometimes select variable:
- \rightarrow 1. that participates in the largest number of conflicts. V_5
 - 2. at random, any variable that participates in some conflict.
 - 3. <u>at random</u> $\sqrt{1}$ $(\sqrt{4} \sqrt{5} \sqrt{8})$
 - Sometimes choose value
 - a) That minimizes # of conflicts \swarrow
 - b) at random / MeAL 1 selects





Successful application of SLS

 Scheduling of Hubble Space Telescope: reducing time to schedule 3 weeks of observations:
 from one week to around 10 sec.



Example: SLS for RNA secondary structure design

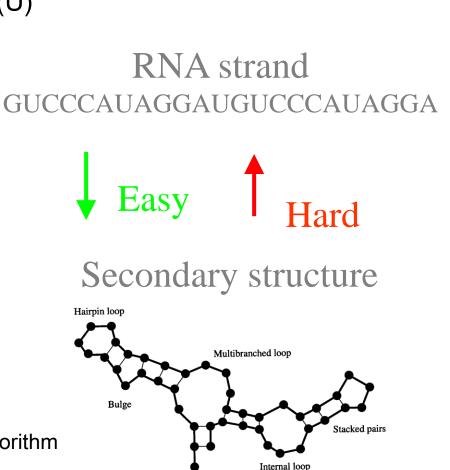
RNA strand made up of four bases: cytosine (C), guanine (G), adenine (A), and uracil (U) 2D/3D structure RNA strand folds into

is important for its function

Predicting structure for a strand is "easy": O(n³)

But what if we want a strand that folds into a certain structure?

- Local search over strands
 - ✓ Search for one that folds into the right structure
- Evaluation function for a strand
 - ✓ Run O(n^3) prediction algorithm
 - Evaluate how different the result is from our target structure
 - Only defined implicitly, but can be evaluated by running the prediction algorithm



External base

Best algorithm to date: Local search algorithm RNA-SSD developed at UBC [Andronescu, Fejes, Hutter, Condon, and Hoos, Journal of Molecular Biology, 2004]

CSP/logic: formal verification





Hardware verification (e.g., IBM) Software verification (small to medium programs)

Most progress in the last 10 years based on: Encodings into propositional satisfiability (SAT) CPSC 322, Lecture 1

(Stochastic) Local search advantage: Online setting

- When the problem can change (particularly important in scheduling)
- E.g., schedule for airline: thousands of flights and thousands of personnel assignment
 - Storm can render the schedule infeasible
- Goal: Repair with minimum number of changes
- This can be easily done with a local search starting form the current schedule
- Other techniques usually:
 - require more time
 - might find solution requiring many more changes

SLS limitations

- Typically no guarantee to find a solution even if one exists
 - SLS algorithms can sometimes stagnate
 - \checkmark Get caught in one region of the search space and never terminate
 - Very hard to analyze theoretically
- Not able to show that no solution exists
 - SLS simply won't terminate
 - You don't know whether the problem is infeasible or the algorithm has stagnated

SLS Advantage: anytime algorithms

- When should the algorithm be stopped ?
 - When a solution is found (e.g. no constraint violations)
 - Or when we are out of time: you have to act NOW
 - Anytime algorithm:
 - ✓ maintain the node with best h found so far (the "incumbent")
 - \checkmark given more time, can improve its incumbent

Lecture Overview

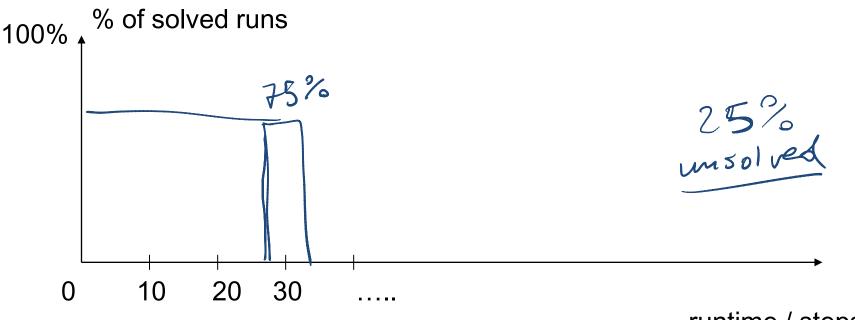
- Recap Local Search in CSPs
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Evaluating SLS algorithms

- SLS algorithms are randomized
 - The time taken until they solve a problem is a random variable
 - It is entirely normal to have runtime variations of 2 orders of magnitude in repeated runs!
 - \checkmark E.g. 0.1 seconds in one run, 10 seconds in the next one
 - \checkmark On the same problem instance (only difference: random seed)
 - Sometimes SLS algorithm doesn't even terminate at all: stagnation
- If an SLS algorithm sometimes stagnates, what is its mean runtime (across many runs)?
 - Infinity!
 - In practice, one often counts timeouts as some fixed large value X
 - Still, summary statistics, such as **mean** run time or **median** run time, don't tell the whole story
 - E.g. would penalize an algorithm that often finds a solution quickly but sometime stagnates

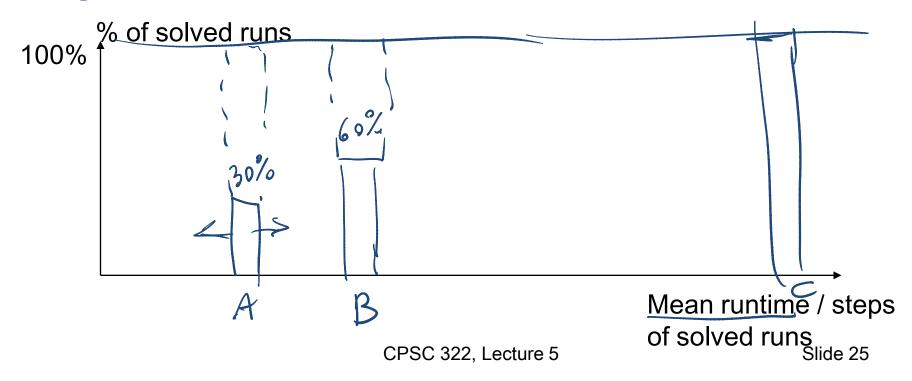
Comparing Stochastic Algorithms: Challenge

- Summary statistics, such as **mean** run time, **median** run time, and **mode** run time don't tell the whole story
 - What is the running time for the runs for which an algorithm *never* finishes (infinite? stopping time?)



First attempt....

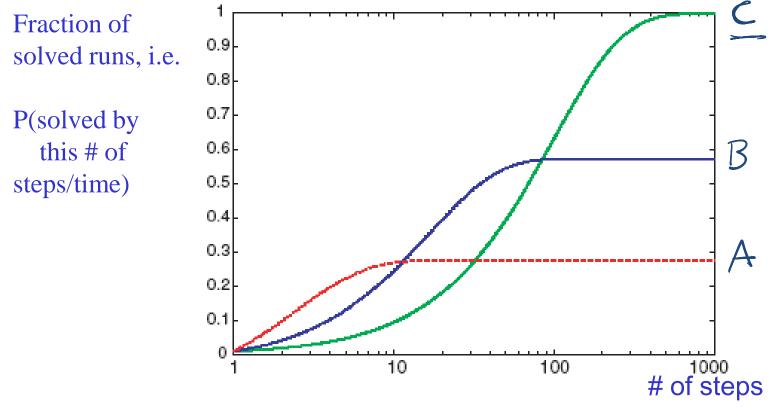
- How can you compare three algorithms when
 - A. one solves the problem 30% of the time very quickly but doesn't halt for the other 70% of the cases
 - B. one solves 60% of the cases reasonably quickly but doesn't solve the rest
 - \underline{C} . one solves the problem in 100% of the cases, but slowly?



Runtime Distributions are even more effective

Plots runtime (or number of steps) and the proportion (or number) of the runs that are solved within that runtime.

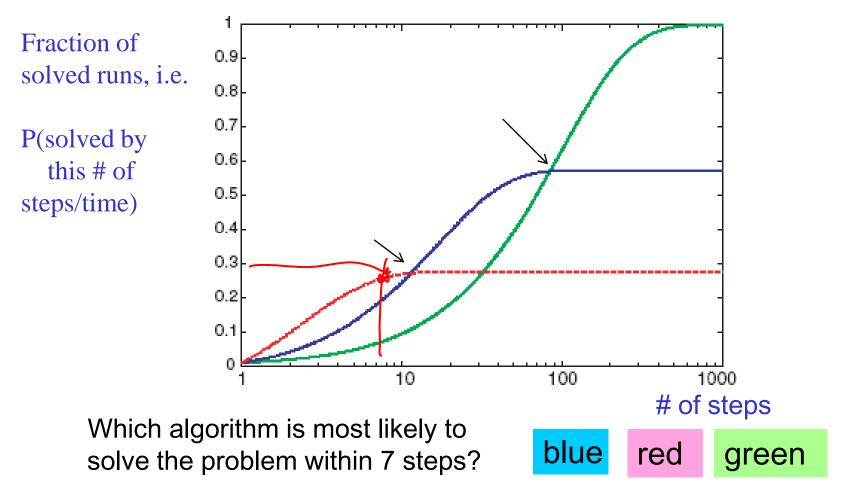
• log scale on the x axis is commonly used



CPSC 322, Lecture 5

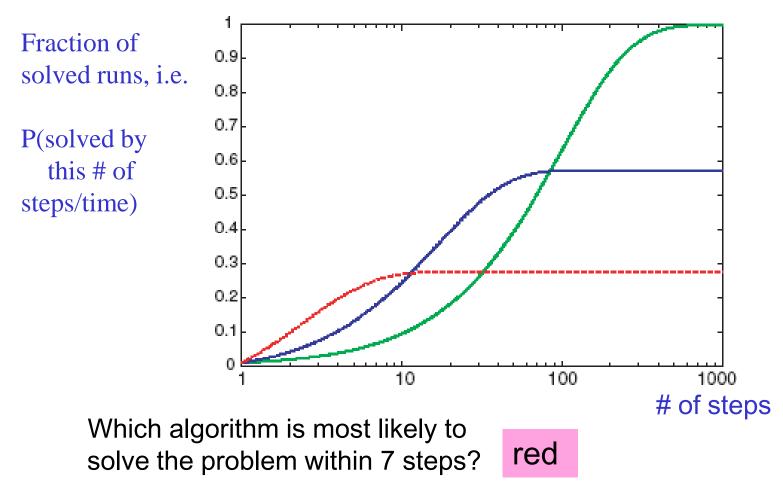
x axis: runtime (or number of steps) y axis: proportion (or number) of runs solved in that runtime

• Typically use a log scale on the x axis

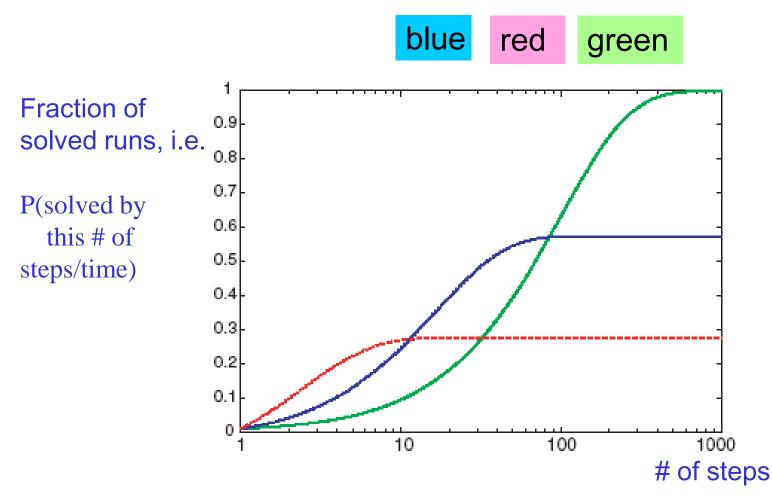


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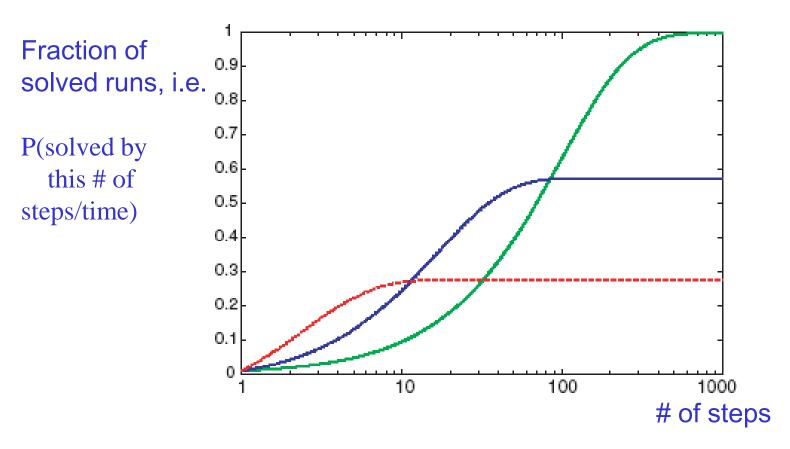
• Typically use a log scale on the x axis



- Which algorithm has the best median performance?
 - I.e., which algorithm takes the fewest number of steps to be successful in 50% of the cases?

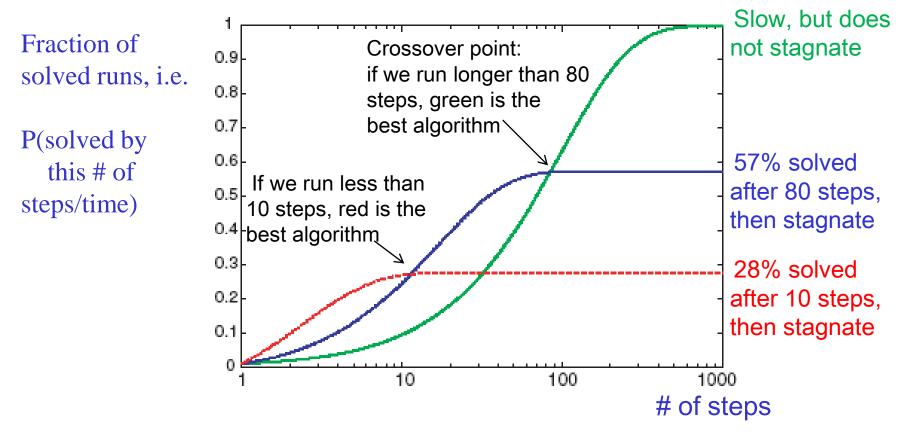


- Which algorithm has the best median performance?
 - I.e., which algorithm takes the fewest number of steps to be successful in 50% of the cases?



x axis: runtime (or number of steps) y axis: proportion (or number) of runs solved in that runtime

• Typically use a log scale on the x axis



Runtime distributions in Alspace

- Let's look at some algorithms and their runtime distributions:
 - 1. Greedy Descent
 - 2. Random Sampling
 - 3. Random Walk
 - 4. Greedy Descent with random walk



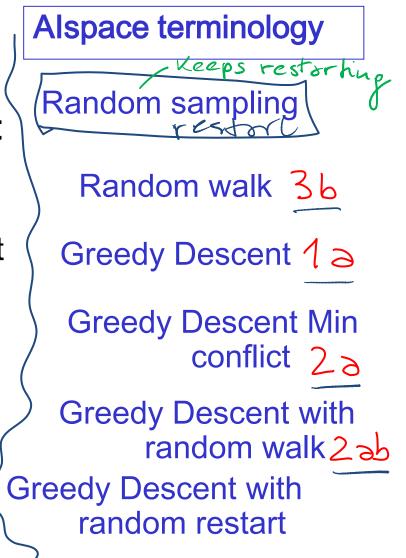
• Simple scheduling problem 2 in Alspace:

What are we going to look at in Alspace

When selecting a variable first followed by a value:

- Sometimes select variable:
 - 1. that participates in the largest number of conflicts.
 - 2. at random, any variable that participates in some conflict.
 - 3. at random
- Sometimes choose value

 a) That minimizes # of conflicts
 b) at random



Stochastic Local Search

- Key Idea: combine greedily improving moves with randomization
 - As well as improving steps we can allow a "small probability" of:
 - <u>Random steps:</u> move to a random neighbor. 1%
 - Random restart: reassign random values to all 5% variables.
 - Always keep best solution found so far
 - Stop when
 - Solution is found (in vanilla CSP . pw. skifging all C)
 - Run out of time (return best solution so far)

Learning Goals for today's class

You can:

- Implement SLS with
 - random steps (1-step, 2-step versions)
 - random restart
- Compare SLS algorithms with runtime distributions

Assign-2

- Will be out on Tue
- Assignments will be weighted: A0 (12%), A1...A4 (22%) each

Next Class

- More SLS variants
- Finish CSPs
- (if time) Start planning