Uniformed Search (cont.)

Computer Science cpsc322, Lecture 6

(Textbook finish 3.5)

January, 15, 2010



Lecture Overview

Recap DFS vs BFS

Uninformed Iterative Deepening (IDS)

Search with Costs

Recap: Graph Search Algorithm

```
Input: a graph, a start node, Boolean procedure goal(n) that tests if n is a
   goal node
frontier:=[<s>: s is a start node];
While frontier is not empty:
    select and remove path \langle n_0, ..., n_k \rangle from frontier;
    If goal(n_k)
           return \langle n_0, \dots, n_k \rangle;
     For every neighbor n of n_k push add < n_o, ..., n_k, n >  to frontier;
end
```

In what aspects <u>DFS</u> and <u>BFS</u> differ when we look at the generic graph search algorithm?

CPSC 322, Lecture 6

Slide 3

Recap: Comparison of DFS and BFS

	Complete	Optimal	Time	Space
DFS	- N (Y tho andes		0(6m)	(m d)
BFS	7		0(64)	O(6 M)

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Iterative Deepening (sec 3.6.3)

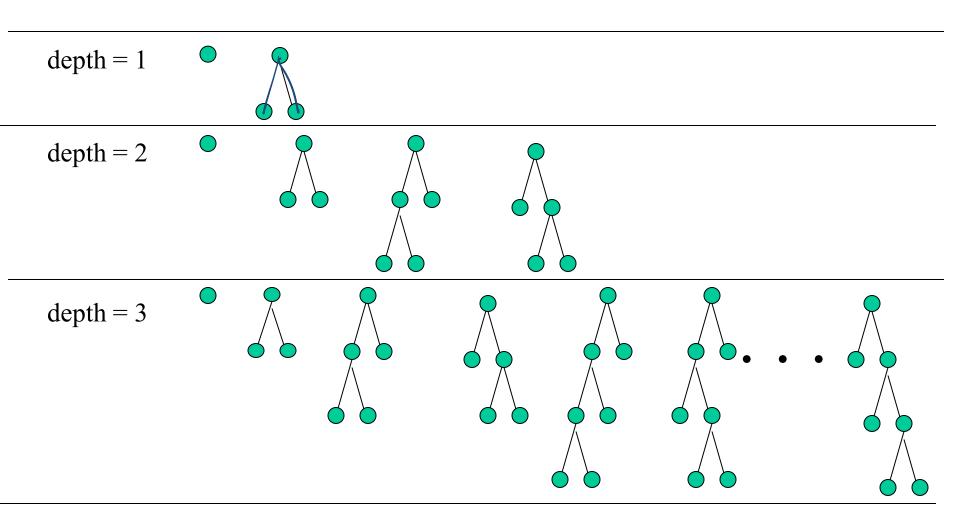
How can we achieve an acceptable (linear) space complexity maintaining completeness and optimality?

	Complete	Optimal	Time	Space
DFS	\sim	\mathcal{N}	6 W	m 5
BFS	R	Y	bm	5 m
LIDS	Y	Y	6 m	mb

Key Idea: let's re-compute elements of the frontier rather than saving them.

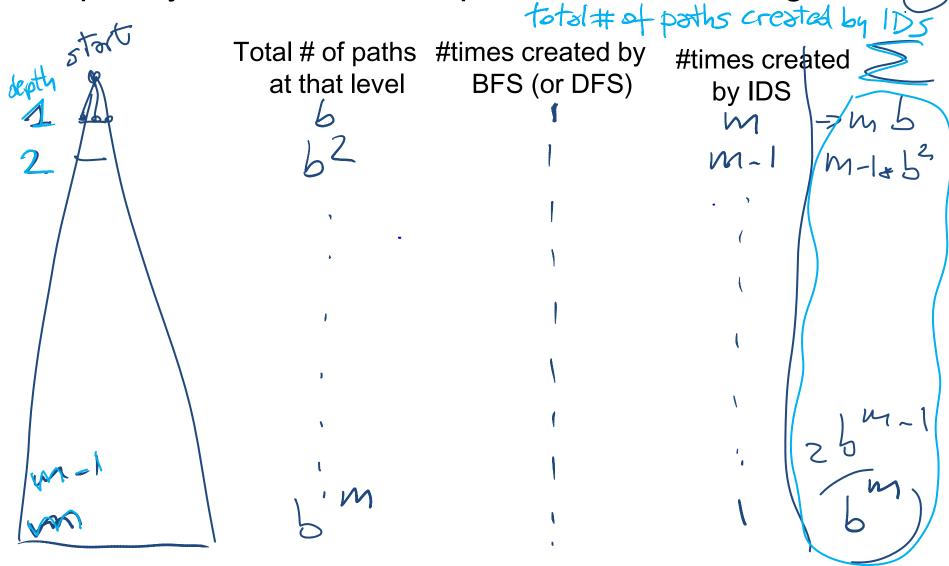
Iterative Deepening in Essence

- Look with DFS for solutions at depth 1, then 2, then 3, etc.
- If a solution cannot be found at depth D, look for a solution at depth D + 1.
- You need a depth-bounded depth-first searcher.
- Given a bound B you simply assume that paths of length B cannot be expanded....



(Time) Complexity of Iterative Deepening

Complexity of solution at depth m with branching factor b



(Time) Complexity of Iterative Deepening

Complexity of solution at depth m with branching factor b

Total # of paths generated
$$b^{m} + 2b^{m-1} + 3b^{m-2} + .. + mb = A$$

$$b^{m} (1+2b^{-1} + 3b^{-2} + .. + mb^{1-m}) \le A$$

$$b^{m} \sum_{i=1}^{\infty} b^{i} b^{-1} = 2(b^{m})$$

$$b^{m} \sum_{i=1}^{\infty} b^{-1} b^{-1} = 2(b^{m})$$

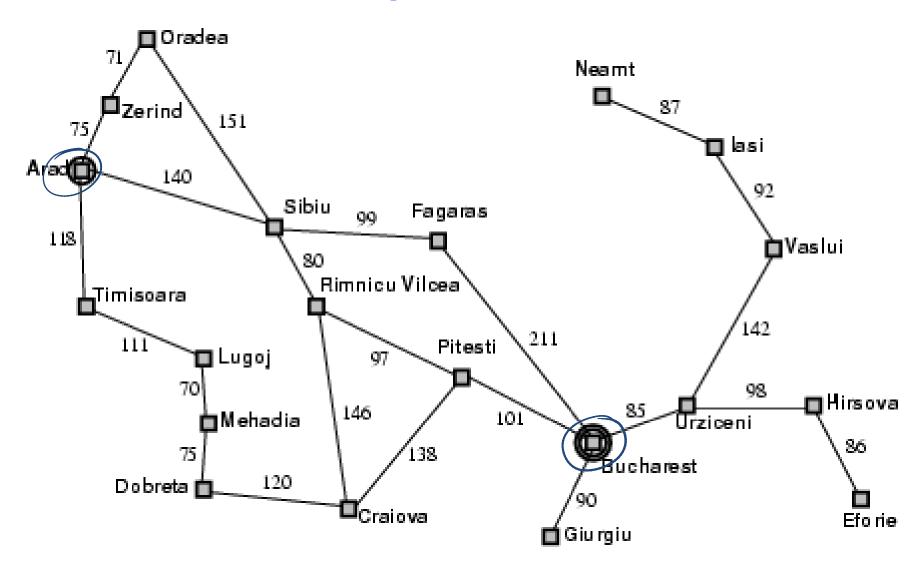
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Example: Romania



Search with Costs

Sometimes there are costs associated with arcs.

Definition (cost of a path)

The cost of a path is the sum of the costs of its arcs:

$$\operatorname{cost}(n_0, \dots, n_k) = \sum_{i=1}^k \operatorname{st}(\langle n_{i-1}, n_i \rangle)$$

In this setting we often don't just want to find just any solution

we usually want to find the solution that minimizes cost

Definition (optimal algorithm)

A search algorithm is optimal if it is complete, and only returns cost-minimizing solutions.

Lowest-Cost-First Search

- At each stage, lowest-cost-first search selects a path on the frontier with lowest cost.
 - The frontier is a priority queue ordered by path cost
 - We say ``a path" because there may be ties
- When all arc costs are equal, LCFS is equivalent to ? BFS ?
- Example of one step for LCFS:
 - the frontier is $\lfloor \langle p_2, 5 \rangle, \langle p_3, 7 \rangle, \langle p_1, 11 \rangle, \rfloor$
 - (p) is the lowest-cost node in the frontier
 - "neighbors" of p_2 are $\{\langle p_9, 10 \rangle, \langle p_{10}, 15 \rangle\}$
- What happens?
 - p_2 is selected, and tested for being a goal.
 - Neighbors of p_2 are inserted into the frontier
 - Thus, the frontier is now $\lfloor \langle p_3, 7 \rangle$, $\langle p_9, 16 \rangle$, $\langle p_1, 11 \rangle$, $\langle p_{10}, 15 \rangle \rfloor$.
 - ? ? ? is selected next.
 - Etc. etc.



Analysis of Lowest-Cost Search (1)

- Is LCFS complete?
 - not in general: a cycle with zero or negative arc costs could be followed forever.
 - yes, as long as arc costs are strictly positive

- Is LCFS optimal?
 - Not in general. Why not?
 - Arc costs could be negative: a path that initially looks high-cost could end up getting a ``refund".
 - However, LCFS is optimal if arc costs are guaranteed to be non-negative.

Analysis of Lowest-Cost Search

- What is the time complexity, if the maximum path length is m and the maximum branching factor is b?
 - The time complexity is $O(b^m)$: must examine every node in the tree.
 - Knowing costs doesn't help here.

- What is the space complexity?
 - Space complexity is $O(b^m)$: we must store the whole frontier in memory.

Learning Goals for Search (up to today)

 Apply basic properties of search algorithms: completeness, optimality, time and space complexity of search algorithms.

	Complete	Optimal	Time	Space
DFS	\sim	\sim	6 m	bus
BFS	Y	4	N	bm
105		\(\frac{1}{2}\)	11	bm
LERS	X 1+ C>0	N Y1+ C>1	b b	5m

Learning Goals for Search (cont') (up to today)

 Select the most appropriate search algorithms for specific problems.

- BFS vs DFS vs IDS vs BidirS-
- LCFS vs. BFS
- A* vs. B&B vs IDA* vs MBA*

- Define/read/write/trace/debug different search algorithms
 - With / Without cost
 - Informed / Uninformed

Beyond uninformed search....

 So far the selection of the next path to examine (and possibly expand) is based on

Next Class

Start Heuristic Search

(textbook.: start 3.6)