# Probability and Time: Markov Models

# Computer Science cpsc322, Lecture 31

#### (Textbook Chpt 6.5.1)

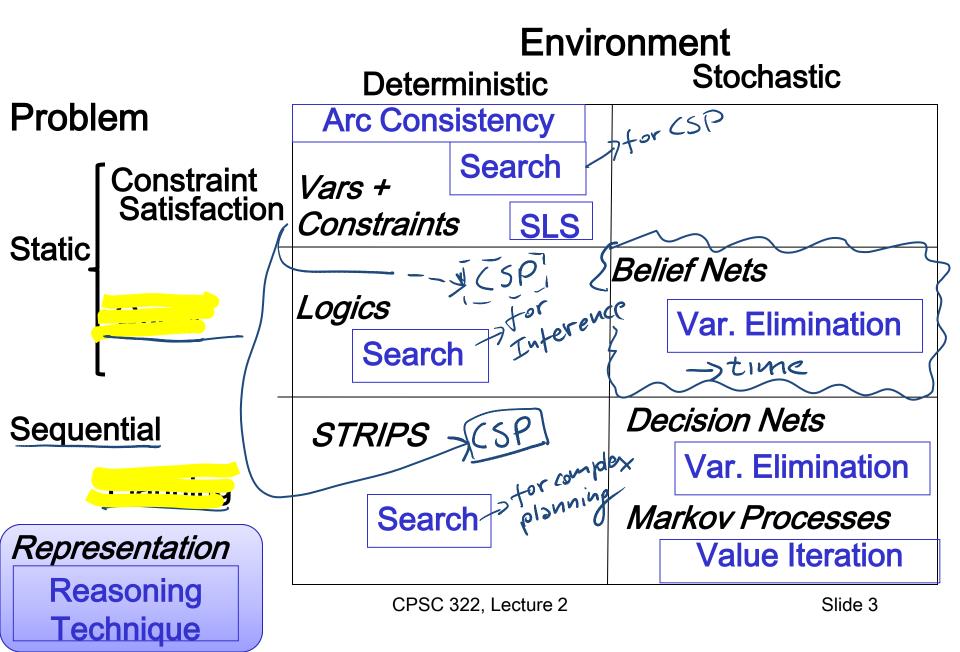
March, 31, 2010

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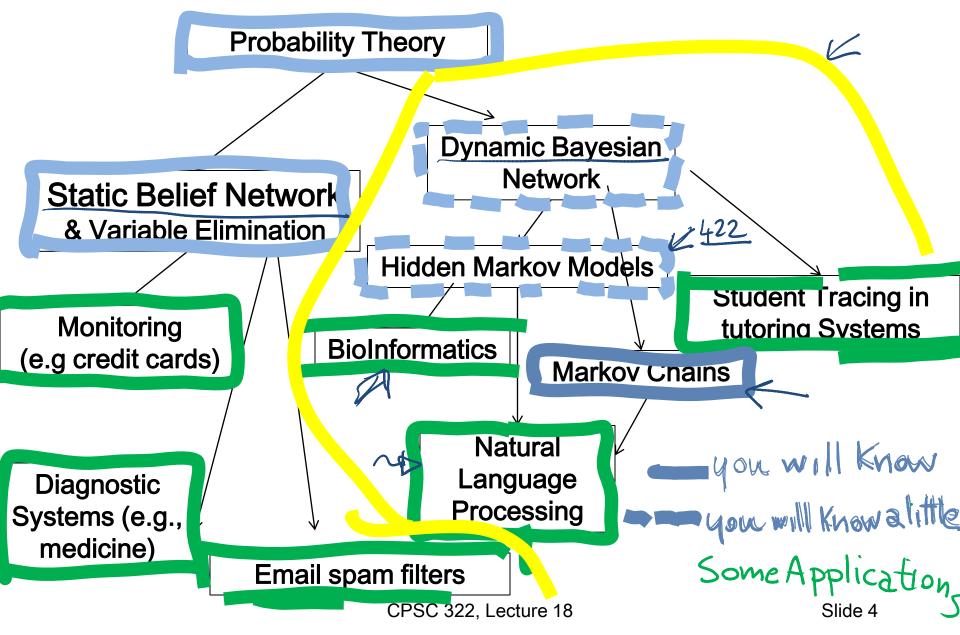
# Recap

- Temporal Probabilistic Models
- Start Markov Models
  - Markov Chain
  - Markov Chains in Natural Language Processing

# **Big Picture: R&R systems**



#### **Answering Query under Uncertainty**



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# **Modelling static Environments**

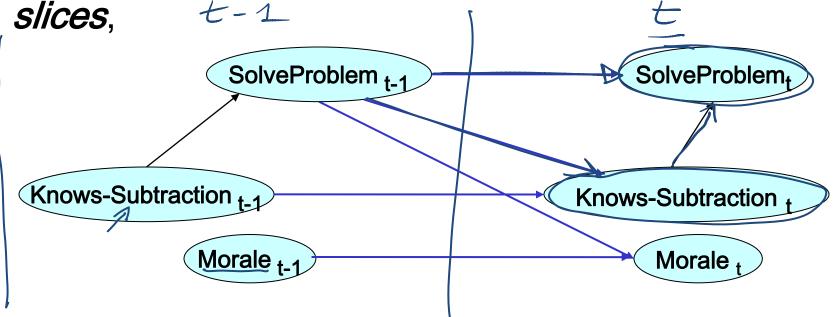
- So far we have used Bnets to perform inference in **static** environments
- For instance, the system keeps collecting evidence to diagnose the cause of a fault in a system (e.g., a car).
- The environment (values of the evidence, the true cause) does not change as I gather new evidence

• What does change?

The system's beliefs over possible causes

#### **Modeling Evolving Environments**

- Often we need to make inferences about evolving environments.
- Represent the state of the world at each specific point in time via a series of snapshots, or *time* slices

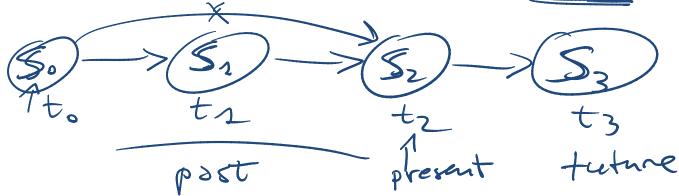


Tutoring system tracing student knowledge and morale

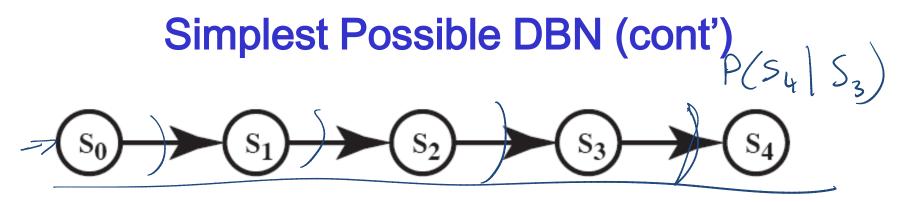
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# Simplest Possible DBN

• One random variable for each time slice: let's assume  $S_t$  represents the state at time *t*. with domain  $\{s_1 \dots s_n\}$ 



- Each random variable depends only on the previous one
- Thus  $(S_{t+1}|S_{\bullet}\cdots S_t) = P(S_{t+1}|S_t)$
- Intuitively S<sub>t</sub> conveys all of the information about the history that can affect the future states.
- "The future is independent of the past given the present."



- How many CPTs do we need to specify?  $4 P(s_1|s_0) P(s_2|s_1) etc.$
- Stationary process assumption: the mechanism that regulates how state variables change overtime is stationary, that is it can be described by a single transition model
- · P(St |St-1) is the same for all t

#### Stationary Markov Chain (SMC)

$$(s_0 \rightarrow s_1 \rightarrow s_2 \rightarrow s_3 \rightarrow s_4)$$

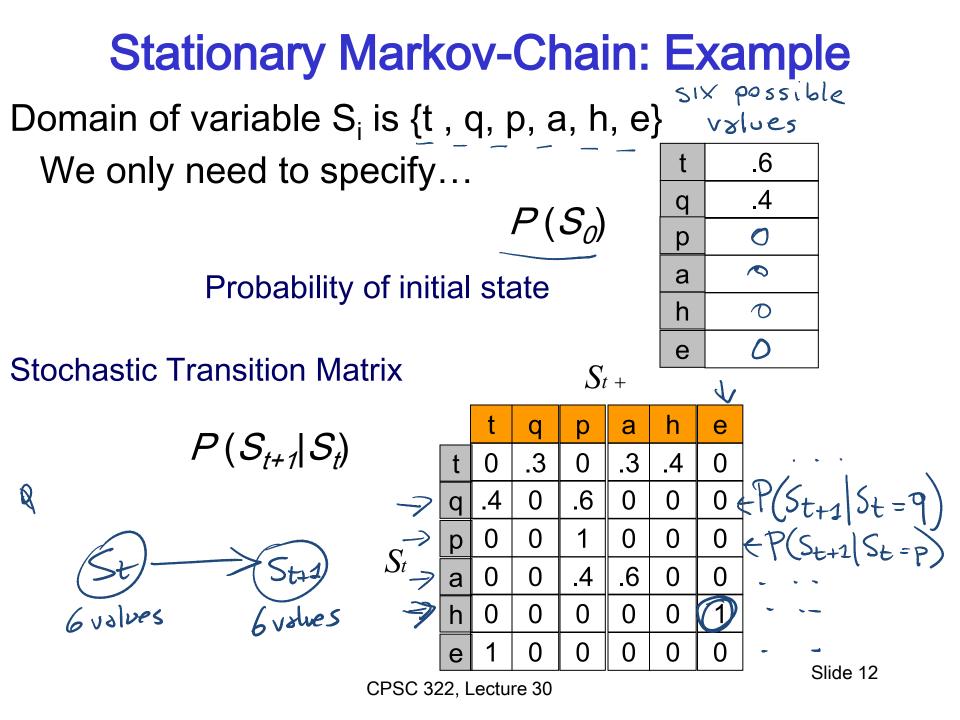
A stationary Markov Chain : for all t >0

- $P(S_{t+1} | S_{0}, \dots, S_{t}) = P(S_{t+1} | S_{t})$  and Markov assumption
- $P(S_{t+1}|S_t)$  is the same stationary

We only need to specify  $\mathcal{P}(\mathcal{S}_{\bullet})$  and  $\mathcal{P}(\mathcal{S}_{\bullet})$ 

$$S_{t+1}(S_t)$$

- Simple Model, easy to specify
- Often the natural model <</li>
- The network can extend indefinitely
- Variations of SMC are at the core of most Natural in the Language Processing (NLP) applications! also used by Google to Bage Ronk algo (used by Web pages)



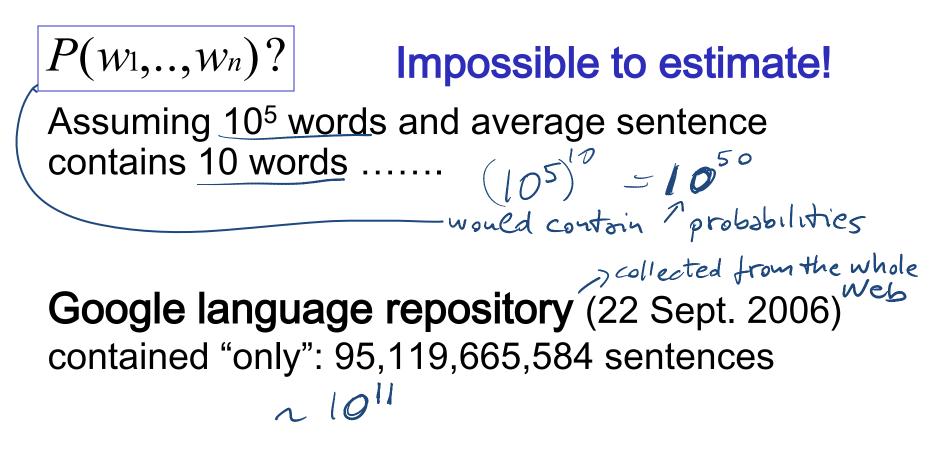
Markov-Chain: Inference Probability of a sequence of states  $S_0 \dots S_T$  $P(S_0,...,S_T) = P(S_0) P(S_1|S_0) P(S_2|S_1) -$ 71  $P(S_{t+1}|S_t)$  $S_2$ e а  $P(S_0)$ .3 ⇒ t P(M,ee) .4 0 .6  $\mathbf{0}$ ()6 q Example: 0 0  $\mathbf{0}$ 0 0 6 0 al а 0 P(t, q, p) =h 0 0 0  $\mathbf{0}$  $\mathbf{0}$ e  $\neq P(q)$ 1t) \* P. - .108 . 6 R . 3

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# Key problems in NLP

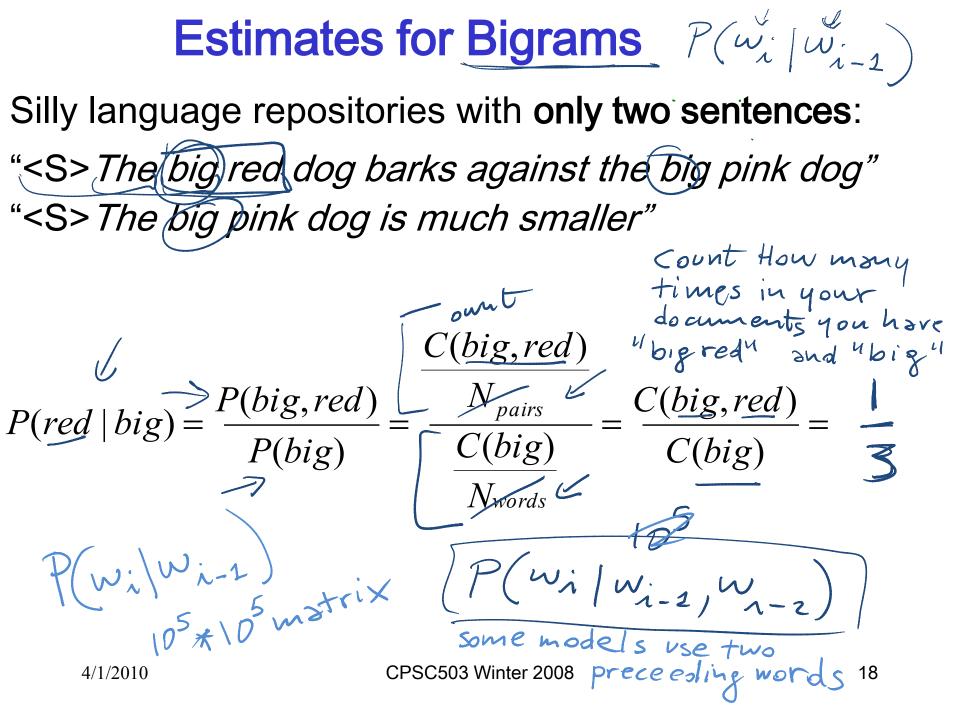
Nour verb  $\begin{array}{c} \text{"Book me a room near UBC"} \\ \text{$W_1$,$W_2$,$W_3$,$W_4$,$W_5$,$W_6$} \\ \text{Assign a probability to a sentence} \\ \text{$Book me a room near UBC"} \\ \text{$W_1$,$W_1$,$W_1$,$W_1$,$W_2$,$W_3$,$W_4$,$W_5$,$W_6$} \\ \text{$Assign a probability to a sentence} \\ \text{$Book me a room near UBC"} \\ \text{$W_1$,$W_1$,$W_1$,$W_2$,$W_6$} \\ \text{$Assign a probability to a sentence} \\ \text{$Book me a room near UBC"} \\ \text{$W_1$,$W_1$,$W_2$,$W_6$} \\ \text{$M_1$,$W_2$,$W_6$,$W_6$} \\ \text{$M_2$,$W_2$,$W_6$,$W$  $P(w_1,..,w_n)?$ Part-of-speech tagging \_\_\_\_ Symmarization, Machine → • Word-sense disambiguation, → *Translation*...... Probabilistic Parsing Predict the next word  $\mathcal{L}$   $P(w_n | w_1 \dots w_{N-1}) =$ • Speech recognition • Hand-writing recognition  $= P(w_1 \dots w_N) / P(w_1 \dots w_{N-1})$ Augmentative communication for the disabled Impossible to  $P(w_1,\ldots,w_n)?$ CPSC503 Winter 2008 estimate 🙁 15 4/1/2010



Most sentences will not appear or appear only once  $\otimes$ 

# What can we do?

Make a strong simplifying assumption! Sentences are generated by a Markov Chain W1 st the beginning of a sentence  $P(w_1,...,w_n) = P(w_1 | < S > \prod_{k=1}^{n} P(w_k | w_{k-1})$ =  $P(w_1 | < S >) P(w_2 | w_2) P(w_3 | w_2) ... P(w_k | w_{k-1})$ P(The big red dog barks)= SP(The|<S>)\* P(big | the) & P(red | big) X.... X P(dog | red) & P(borks | dog) These probs can be assessed in practice!

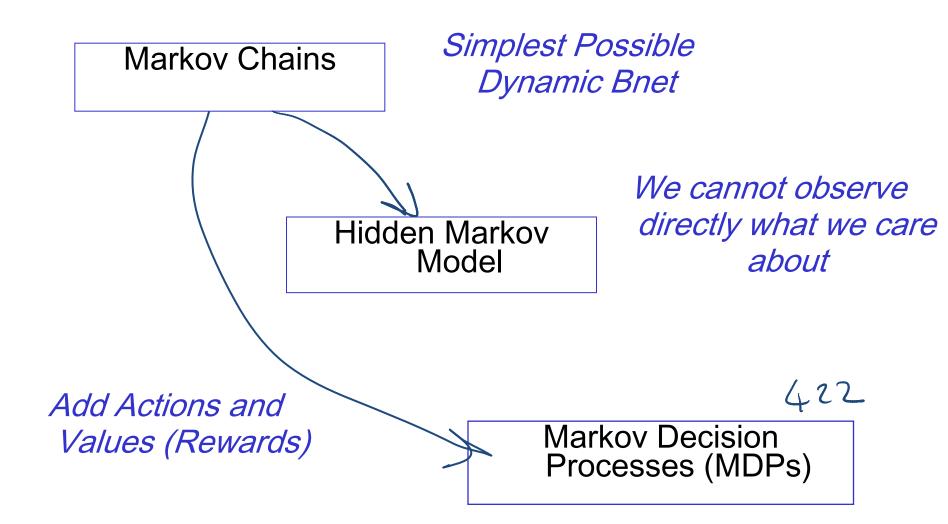


# Learning Goals for today's class

### You can:

- Specify a Markov Chain and compute the probability of a sequence of states
- Justify and apply Markov Chains to compute the probability of a Natural Language sentence (NOT to compute the conditional) probabilities - slide 18

# **Markov Models**



### **Next Class**

- Finish Probability and Time: Hidden Markov Models (HMM) (TextBook 6.5.2)
- Start Decision networks (TextBook chpt 9)

### **Course Elements**

- Assignment 4 is available on webCT. It is due on Apr the 14<sup>th</sup> (last class).
  - You can now work on the first 3 questions. For the 4<sup>th</sup> one you have to wait until we cover decision networks.