Local Search

Computer Science cpsc322, Lecture 14
(Textbook Chpt 4.8)

February, 3, 2010

Announcements

Assignment1 due now!

- I will be away this Fri (attending conference in HK)
 - Postdoc Gabriel Murray will give lecture
 - TA will offer my office hour (in X150)

Lecture Overview

- Recap solving CSP systematically
- Local search
- Constrained Optimization
- Greedy Descent / Hill Climbing: Problems

Systematically solving CSPs: Summary

- Build Constraint Network
- Apply Arc Consistency
 - One domain is empty → ¼₂ テਂ।
 - ► Each domain has a single value → unque sol
 - Some domains have more than one value → ? I may or maynot have a solution
- Apply Depth-First Search with Pruning
 - Split the problem in a number of disjoint cases
 - Apply Arc Consistency to each case

Lecture Overview

- Recap
- Local search
- Constrained Optimization
- Greedy Descent / Hill Climbing: Problems

Local Search motivation: Scale

- Many CSPs (scheduling, DNA computing, more later) are simply too big for systematic approaches
- If you have $10^5 \text{ vars with dom(var}_i) = 10^4$
 - Systematic Search

$$b = 10^4$$

$$d = 10^5$$

$$depth$$
branching depth

Constraint Network

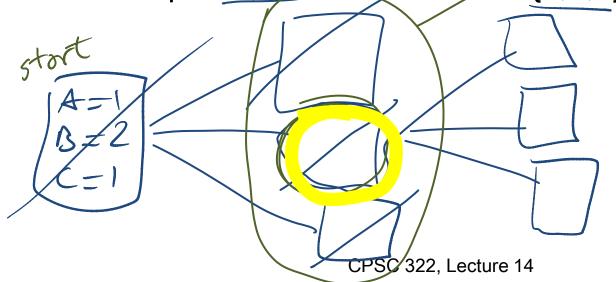
but if solutions are densely distributed......

Local Search: General Method

Remember, for CSP a solution is ... Possible world

- Start from a possible world
- Generate some neighbors ("similar" possible worlds)
- Move from the current node to selected according to a particular strategy

Example: A,B,C same domain {1,2,3}



Slide 7

(not a path)

Local Search: Selecting Neighbors

How do we determine the neighbors?

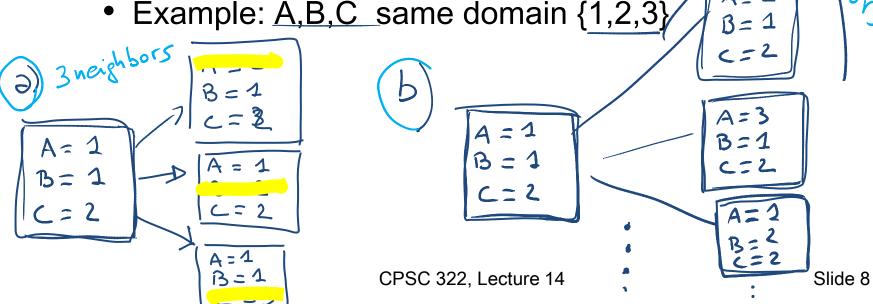
Usually this is simple: some small incremental change to the variable assignment

a) assignments that differ in one variable's value, by (for instance) a → value difference of +1

assignments that differ in one variable's value

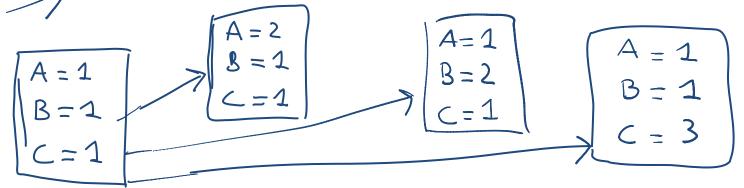
assignments that differ in two variables' values, etc. 6

• Example: A,B,C same domain {1,2,3}



Selecting the best neighbor

• Example: A,B,C same domain {1,2,3}, (A=B, A>1, C≠3)

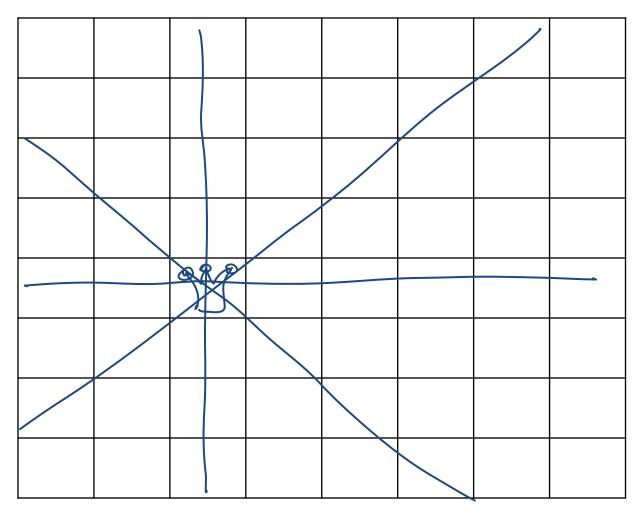


A common component of the scoring function (heuristic) => select the neighbor that results in the

- the min conflicts heuristics

Queens in Chess

Positions a queen can attack



Example: *n*-queens

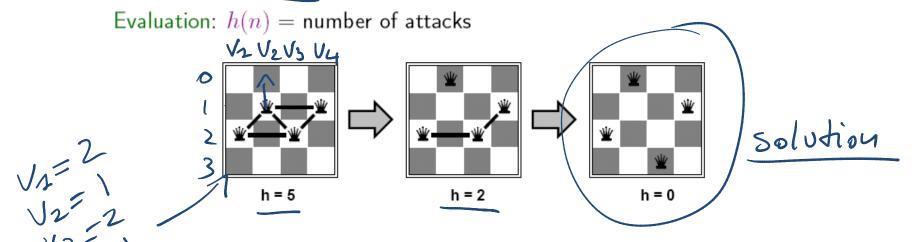
Put *n* queens on an *n* board with no two queens on the same row, column, or diagonal (i.e attacking each other)

Example: 4-Queens

Seems: 4 queens in 4 columns ($4^4 = 256$ states)

Operators: move queen in column (to generate neighbors)

Goal test: no attacks



CPSC 322, Lecture 14

Slide 11



Why this problem?

Lots of research in the 90' on local search for CSP was generated by the observation that the runtime of local search on n-queens problems is independent of problem size!

Given random initial state, can solve n-queens in almost constant time for arbitrary n with high probability (e.g., n=10,000,000)

Lecture Overview

- Recap
- Local search
- Constrained Optimization
- Greedy Descent / Hill Climbing: Problems

Constrained Optimization Problems

So far we have assumed that we just want to find a possible world that satisfies all the constraints.

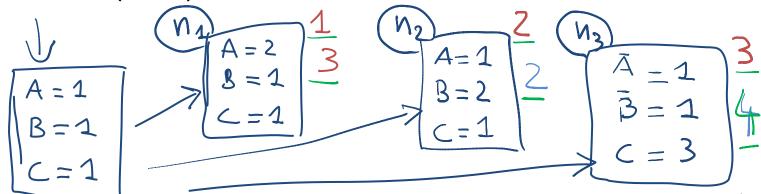
But sometimes solutions may have different values / costs

- We want to find the optimal solution that
 - maximizes the value or
 - minimizes the cost

Constrained Optimization Example

• Example: A,B,C same domain {1,2,3} , (A=B, A>1, C≠3)

• Value = (C+A) so we want a solution that maximize that



The scoring function we'd like to maximize might be: Select 41

$$f(n) = (C + A) - \#-of-conflicts + (u_1) = 2 + (u_2) = 0 + (u_3) = 1$$

Hill Climbing means selecting the neighbor which best improves a (value-based) scoring function.

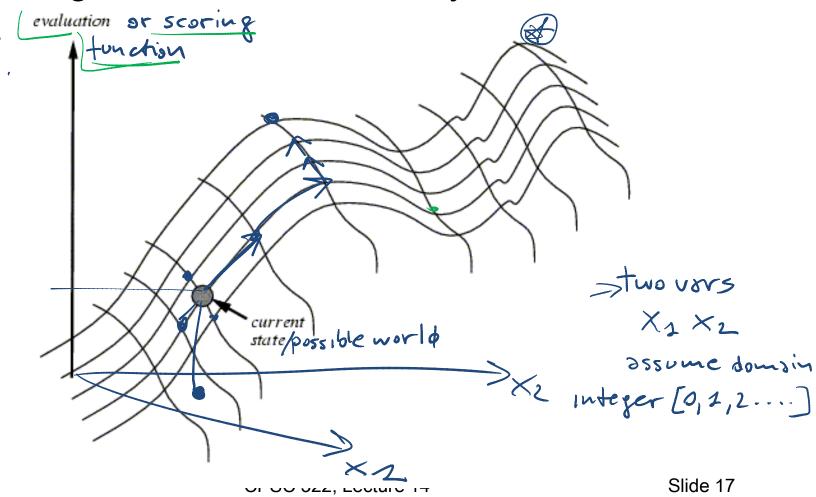
Greedy Descent means selecting the neighbor which minimizes a (cost-based) scoring function.

Lecture Overview

- Recap
- Local search
- Constrained Optimization
- Greedy Descent / Hill Climbing: Problems

Hill Climbing

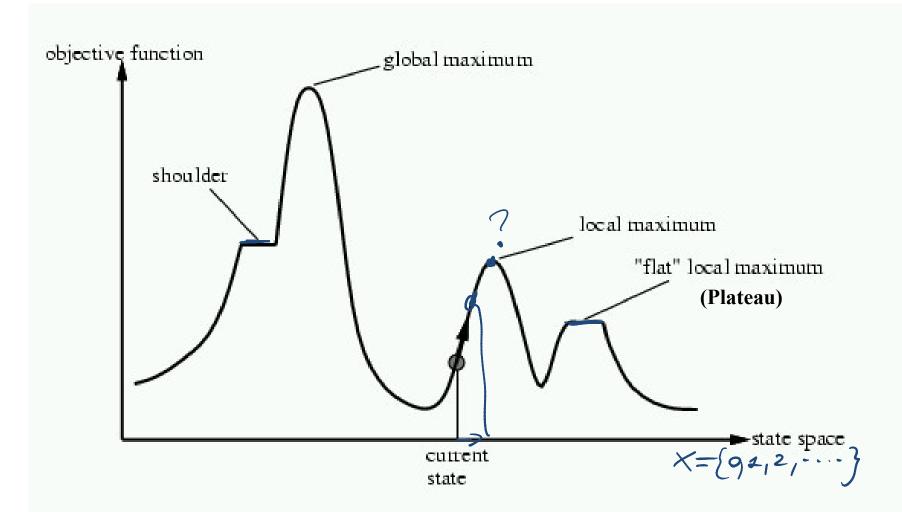
NOTE: Everything that will be said for Hill Climbing is also true for Greedy Descent



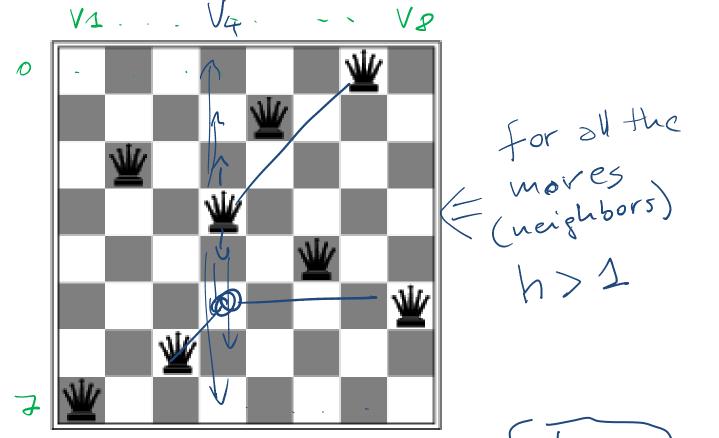
Problems with Hill Climbing

Local Maxima.

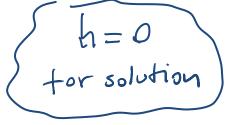
Plateau - Shoulders



Corresponding problem for GreedyDescent Local minimum example: 8-queens problem

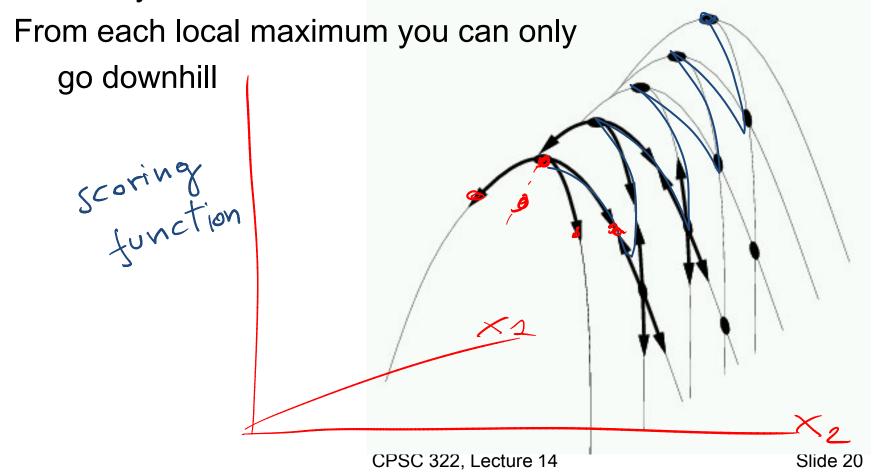


A local minimum with h = 1



Even more Problems in higher dimensions

E.g., Ridges – sequence of local maxima not directly connected to each other



Learning Goals for today's class

You can:

Implement local search for a CSP.

- Implement different ways to generate neighbors
- Implement scoring functions to solve a CSP by local search through either greedy descent or hill-climbing.

Next Class

 How to address problems with Greedy Descent / Hill Climbing?

Stochastic Local Search (SLS)

322 Feedback © or 8

- Lectures
- Slides
- Practice
 Exercises
- Assignments
- Alspace
- •

- Textbook
- Course Topics / Objectives
- TAs
- Learning Goals
-