

- Project #2 - should be well underway...
- Practice exam questions on web page.

“Once you replace negative thoughts with positive ones, you’ll start having positive results.”

Willie Nelson, 2006 in “The Tao of Willie”

Since Midterm

- difference lists, definite clause grammars and natural language interfaces to databases
- computer algebra and calculus
- Triples are universal representations of relations, and are the basis for RDF, and knowledge graphs
- URIs/IRIs provide constants that have standard meanings
- Ontologies define the meaning of symbols
- You should know what the following mean: RDF, IRI, `rdf:type`, `rdfs:subClassOf`, `rdfs:domain`, `rdfs:range`
- Complete Knowledge Assumption, Negation as failure, unique names assumption

To do:

- Negation-as-failure (cont)
- Extra-logical predicates
- Proofs

Clark Normal Form

The **Clark normal form** of the clause

$$p(t_1, \dots, t_k) :- B.$$

is the clause

$$p(V_1, \dots, V_k) :- \exists W_1 \dots \exists W_m V_1 = t_1, \dots, V_k = t_k, B.$$

where

- V_1, \dots, V_k are k variables that did not appear in the original clause
- W_1, \dots, W_m are the original variables in the clause.
- When the clause is an atomic clause, B is *true*.
- Often can be simplified by replacing $\exists W V = W \wedge p(W)$ with $P(V)$.

Clark normal form

For the clauses

student(mary).

student(sam).

student(X) :- undergrad(X).

the Clark normal form is

student(V) :- V = mary.

student(V) :- V = sam.

student(V) :- $\exists X$ V = X \wedge undergrad(X).

Clark's Completion

Suppose all of the clauses for p are put into Clark normal form, with the same set of introduced variables, giving

$$p(V_1, \dots, V_k) :- B_1.$$

\vdots

$$p(V_1, \dots, V_k) :- B_n.$$

which is equivalent to

$$p(V_1, \dots, V_k) :- B_1 \vee \dots \vee B_n.$$

Clark's completion of predicate p is the equivalence

$$\forall V_1 \dots \forall V_k p(V_1, \dots, V_k) \leftrightarrow B_1 \vee \dots \vee B_n$$

If there are no clauses for p , the completion results in

$$\forall V_1 \dots \forall V_k p(V_1, \dots, V_k) \leftrightarrow \textit{false}$$

Clark's completion of a knowledge base consists of the completion of every predicate symbol along the unique names assumption.

Clark normal form

For the clauses

$student(mary).$

$student(sam).$

$student(X) :- undergrad(X).$

the Clark normal form is

$student(V) :- V = mary.$

$student(V) :- V = sam.$

$student(V) :- \exists X V = X \wedge undergrad(X).$

which is equivalent to

$student(V) :- V = mary \vee V = sam \vee \exists X V = X \wedge undergrad(X).$

The completion of the *student* predicate is

$\forall V student(V) \leftrightarrow V = mary \vee V = sam$
 $\vee \exists X V = X \wedge undergrad(X).$

Completion Example

Consider the recursive definition:

$$\begin{aligned} & \textit{passed_each}([], St, MinPass). \\ & \textit{passed_each}([C|R], St, MinPass) :- \\ & \quad \textit{passed}(St, C, MinPass), \\ & \quad \textit{passed_each}(R, St, MinPass). \end{aligned}$$

In Clark normal form, this can be written as

$$\begin{aligned} & \textit{passed_each}(L, S, M) :- L = []. \\ & \textit{passed_each}(L, S, M) :- \\ & \quad \exists C \exists R L = [C|R], \textit{passed}(S, C, M), \textit{passed_each}(R, S, M). \end{aligned}$$

Here we renamed the variables as appropriate. Thus, Clark's completion of *passed_each* is

$$\begin{aligned} & \forall L \forall S \forall M \textit{passed_each}(L, S, M) \leftrightarrow L = [] \vee \\ & \quad \exists C \exists R L = [C|R], \textit{passed}(S, C, M), \textit{passed_each}(R, S, M). \end{aligned}$$

Clark's Completion of a KB

- Clark's completion of a knowledge base consists of the completion of every predicate.
- The completion of an n -ary predicate p with no clauses is $p(V_1, \dots, V_n) \leftrightarrow \text{false}$.
- You can interpret negations in the body of clauses.
 - $\setminus+ a$ means a is false under the complete knowledge assumption. $\setminus+ a$ is replaced by $\neg a$ in the completion.
 - This is **negation as failure**.

Defining *empty_course*

Given database of:

- *course*(*C*) that is true if *C* is a course
- *enrolled*(*S*, *C*) that is true if student *S* is enrolled in course *C*.

Define *empty_course*(*C*) that is true if there are no students enrolled in course *C*.

- Using negation as failure, *empty_course*(*C*) can be defined by
$$\begin{aligned} \text{empty_course}(C) &:- \text{course}(C), \quad \backslash+ \text{has_enrollment}(C). \\ \text{has_enrollment}(C) &:- \text{enrolled}(S, C). \end{aligned}$$

- The completion of this is:

$$\forall C \text{ empty_course}(C) \iff \text{course}(C), \neg \text{has_enrollment}(C).$$

$$\forall C \text{ has_enrollment}(C) \iff \exists S \text{ enrolled}(S, C).$$

Problem Cases

- $p :- p.$
- $r :- \backslash + r.$
- $a :- \backslash + b.$
 $b :- \backslash + a.$
- $c :- \backslash + d.$
 $d :- c.$
- It isn't clear what the semantics should be.
Prolog goes into an infinite loop.
Avoid cycles!

Problematic Cases

$p(X) :- \setminus + q(X)$

$q(X) :- \setminus + r(X)$

$r(a)$

$?- p(X).$

- What is the answer?
- How can this be implemented?

Asserting and retracting clauses

New clauses can be added using

- `assertz(atom)` adds `atom` as the last clause.
`atom` must be declared dynamic.
- `assertz((h :- b))` adds `h :- b` as the last clause
(note double parentheses). `h` must be declared dynamic.
- `asserta` adds a clause as the first clause.

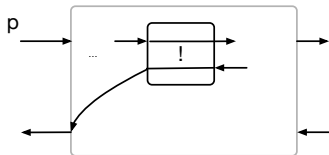
These are not undone by backtracking.

Example: count the number of times `countthis` is called:

```
:- dynamic countn/1.  
countn(0).  
countthis :-  
    retract(countn(N)),  
    N1 is N+1,  
    assertz(countn(N1)).
```

cut, or **commit**, written as **!**

- when called, exits
- when retried, fails the atom it is used in



Example: implementing negation as failure

```
mynot(A) :- call(A), !, fail.  
mynot(A).
```

bagof, setof, findall

`setof(t(Xs), Ys^foo(Xs, Ys, Zs), L)`

where $t(Xs)$ is a term containing variables Xs .

Ys is a set of existential variables

Zs is the other variable in *foo*

is true when $L = \{t(Xs) \mid \exists Y \text{ foo}(X, Y, Z)\} \neq \{\}$

there is an answer for each Z .

`bagof(t(Xs), Ys^foo(Xs, Ys, Zs), L)` returns a list not a set
Try from `cs312_2024`:

```
bagof(P, D^S^F^office_hour(P, D, S, F), Bag).
```

```
setof(P, D^S^F^office_hour(P, D, S, F), Bag).
```

```
bagof(P, S^F^office_hour(P, D, S, F), Bag).
```

```
bagof(P, office_hour(P, D, S, F), Bag).
```

```
bagof(s(P,S), F^office_hour(P, D, S, F), Bag).
```

`findall(t(Xs), foo(Xs, Ys, Zs), L)` like

```
bagof(t(Xs), Ys^Zs^foo(Xs, Ys, Zs), L)
```