Lecture 10: High Dimensionality Information Visualization CPSC 533C, Fall 2007

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**UBC** Computer Science

15 October 2007

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#### **Readings Covered**

Hyperdimensional Data Analysis Using Parallel Coordinates. Edward J. Wegman. Journal of the American Statistical Association, Vol. 85, No. 411. (Sep., 1990), pp. 664-675.

Visualizing Proximity Data. Rich DeJordy, Stephen P. Borgatti, Chris Roussin and Daniel S. Halgin. Field Methods, 19(3):239-263, 2007.

Fast Multidimensional Scaling through Sampling, Springs and Interpolation. Alistair Morrison, Greg Ross, Matthew Chalmers, Information Visualization 2(1) March 2003, pp. 68-77.

Cluster Stability and the Use of Noise in Interpretation of Clustering. George S. Davidson, Brian N. Wylie, Kevin W. Boyack, Proc InfoVis 2001.

Interactive Hierarchical Dimension Ordering, Spacing and Filtering for Exploration Of High Dimensional Datasets. Jing Yang, Wei Peng, Matthew O. Ward and Elke A. Rundensteiner. Proc. InfoVis 2003.

#### **Further Reading**

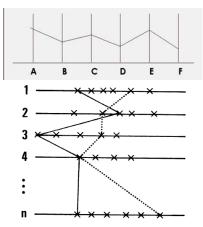
Visualizing the non-visual: spatial analysis and interaction with information from text documents. James A. Wise et al, Proc. InfoVis 1995

Hierarchical Parallel Coordinates for Visualizing Large Multivariate Data Sets Ying-Huey Fua, Matthew O. Ward, and Elke A. Rundensteiner, IEEE Visualization '99.

Parallel Coordinates: A Tool for Visualizing Multi-Dimensional Geometry. Alfred Inselberg and Bernard Dimsdale, IEEE Visualization '90.

#### Parallel Coordinates

- only 2 orthogonal axes in the plane
- instead, use parallel axes!



[Hyperdimensional Data Analysis Using Parallel Coordinates. Edward J. Wegman. Journal of the American Statistical Association, 85(411), Sep 1990, p 664-675.]

#### **PC: Correllation**

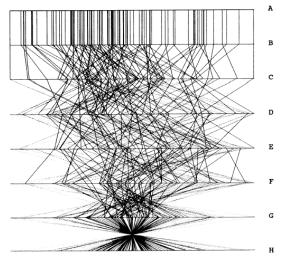
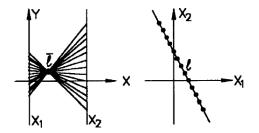


Figure 3. Parallel Coordinate Plot of Six-Dimensional Data Illustrating Correlations of  $\rho = 1, .8, .2, 0, -.2, -.8,$  and -1.

[Hyperdimensional Data Analysis Using Parallel Coordinates. Edward J. Wegman. Journal of the American Statistical Association, 85(411), Sep 1990, p 664-675.]

### PC: Duality

- rotate-translate
- point-line
  - pencil: set of lines coincident at one point



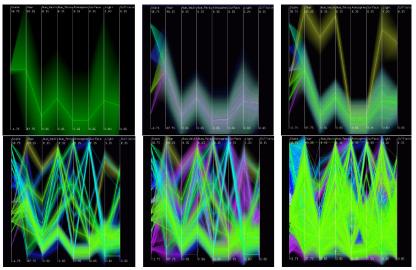
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[Parallel Coordinates: A Tool for Visualizing Multi-Dimensional Geometry. Alfred Inselberg and Bernard Dimsdale, IEEE Visualization '90.]

### PC: Axis Ordering

- geometric interpretations
  - hyperplane, hypersphere
  - points do have intrinsic order
- infovis
  - no intrinsic order, what to do?
  - indeterminate/arbitrary order
    - weakness of many techniques
    - downside: human-powered search
    - upside: powerful interaction technique
- most implementations
  - user can interactively swap axes
- Automated Multidimensional Detective
  - Inselberg 99
  - machine learning approach

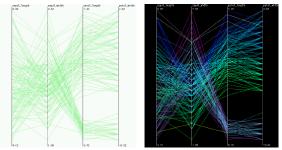
#### Hierarchical Parallel Coords: LOD



[Hierarchical Parallel Coordinates for Visualizing Large Multivariate Data Sets. Fua, Ward, and Rundensteiner, IEEE Visualization 99.]

### **Hierarchical Clustering**

- proximity-based coloring
- interaction lecture later:
  - structure-based brushing
  - extent scaling



[Hierarchical Parallel Coordinates for Visualizing Large Multivariate Data Sets. Fua, Ward, and Rundensteiner, IEEE Visualization 99.]

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#### **Dimensionality Reduction**

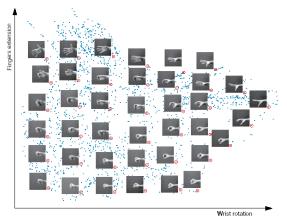
- mapping multidimensional space into
- space of fewer dimensions
  - typically 2D for infovis
  - keep/explain as much variance as possible

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- show underlying dataset structure
- multidimensional scaling (MDS)
- MDS: minimize differences between interpoint distances in high and low dimensions

#### **Dimensionality Reduction: Isomap**

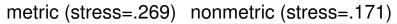
- 4096 D: pixels in image
- 2D: wrist rotation, fingers extension



[A Global Geometric Framework for Nonlinear Dimensionality Reduction. J. B. Tenenbaum, V. de Silva, and J. C. Langford. Science 290(5500), pp 2319–2323, Dec 22 2000]

### Visualizing Proximity Data

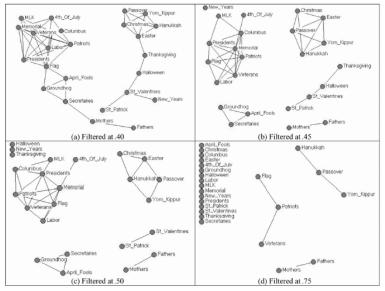
- characterizing MDS vs. graph layout
  MDS
  - nonmetric: ordering preserved, not exact distances
  - general clusters meaningful, specific local distances less so





[Visualizing Proximity Data. DeJordy, Borgatti, Roussin and Halgin. Field Methods, 19(3):239-263, 2007. ]

#### From Matrix To Graph



[Visualizing Proximity Data. DeJordy, Borgatti, Roussin and Halgin. Field Methods, 19(3):239-263, 2007.]

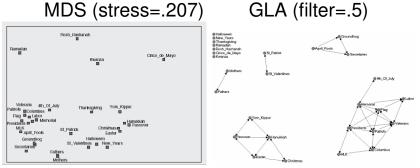
#### MDS vs GLA: Dimensionality

- MDS better when dim = 2D/3D
  - Iow stress
- GLA better when dim > 2D
  - 2D MDS shows MLK intermediate
  - GLA shows MLK part of patriotic group
  - 3D MDS also shows MLK part of patritioc

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#### MDS vs GLA: Outliers

- outliers distort with MDS
- outliers automatically handled with GLA



[Visualizing Proximity Data. DeJordy, Borgatti, Roussin and Halgin. Field Methods, 19(3):239-263, 2007. ]

#### MDS vs GLA

- intransitivity (triangle inequality doesn't hold): GLA better
- data asymmetric: GLA better
- interactive exploration (changing filter): GLA allows
- manual node repositioning: GLA allows
- existence/absence of relationships at precise levels: GLA
- overview of all relationships at once: MDS

# Critique

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#### Critique

somewhat evangelical pro-graph stance

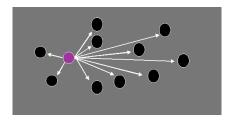
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 but we could use more such characterizations

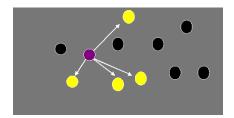
#### Spring-Based MDS: Naive

- repeat for all points
  - compute spring force to all other points
  - difference between high dim, low dim distance
  - move to better location using computed forces

- compute distances between all points
  - $O(n^2)$  iteration,  $O(n^3)$  algorithm



# compare distances only with a few points maintain small local neighborhood set

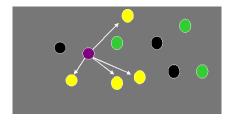


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#### compare distances only with a few points

- maintain small local neighborhood set
- each time pick some randoms, swap in if closer

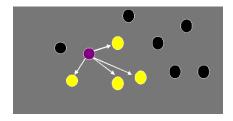
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#### compare distances only with a few points

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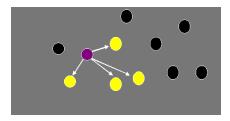


compare distances only with a few points

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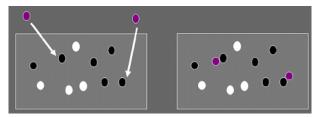
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- small constant: 6 locals, 3 randoms typical
  - O(n) iteration,  $O(n^2)$  algorithm



## Parent Finding [Morrison 02, 03]

- lay out a  $\sqrt{n}$  subset with [Chalmers 96]
- for all remaining points
  - find "parent": laid-out point closest in high D
  - place point close to this parent
- $O(n^{5/4})$  algorithm



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#### Issues

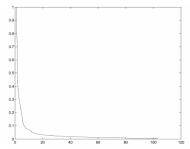
which distance metric: Euclidean or other?

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- computation
  - ▶ naive: *O*(*n*<sup>3</sup>)
  - better:  $O(n^2)$  Chalmers 96
  - hybrid:  $O(n\sqrt{n})$

### True Dimensionality: Linear

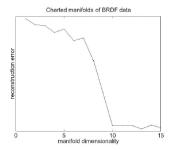
- how many dimensions is enough?
  - could be more than 2 or 3
  - knee in error curve
- example
  - measured materials from graphics
  - linear PCA: 25
  - get physically impossible intermediate points



[A Data-Driven Reflectance Model, SIGGRAPH 2003, W Matusik, H. Pfister M. Brand and L. McMillan, graphics.lcs.mit.edu/~wojciech/pubs/sig2003.pdf]

#### True Dimensionality: Nonlinear

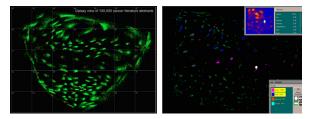
- nonlinear MDS: 10-15
  - all intermediate points possible
- categorizable by people
  - red, green, blue, specular, diffuse, glossy, metallic, plastic-y, roughness, rubbery, greasiness, dustiness...



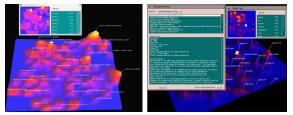
[A Data-Driven Reflectance Model, SIGGRAPH 2003, W Matusik, H. Pfister M. Brand and L. McMillan, graphics.lcs.mit.edu/~wojciech/pubs/sig2003.pdf]

#### **MDS Beyond Points**

#### galaxies: aggregation



#### themescapes: terrain/landscapes



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[www.pnl.gov/infoviz/graphics.html]

### **Cluster Stability**

#### display

- also terrain metaphor
- underlying computation
  - energy minimization (springs) vs. MDS
  - weighted edges
- do same clusters form with different random start points?

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- "ordination"
  - spatial layout of graph nodes

# Approach

Gene Names	Attributes	.6	2 1	-
Element 1		$1 \qquad \qquad$	(3) ~	
Element 2				
Element 3		l⇒ . ୬ ⇒		the parts
Element 4			(5) (4) <sup></sup>	and the second
Element 5		(5) (4)	(6)	
Element 6		.8 6 .6		Prove State
			v	

- normalize within each column
- similarity metric
  - discussion: Pearson's correllation coefficient
- threshold value for marking as similar
  - discussion: finding critical value

### **Graph Layout**

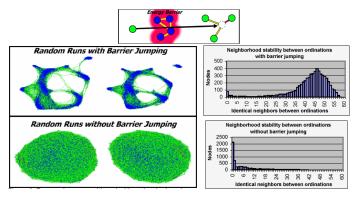
- criteria
  - geometric distance matching graph-theoretic distance

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- vertices one hop away close
- vertices many hops away far
- insensitive to random starting positions
  - major problem with previous work!
- tractable computation
- force-directed placement
  - discussion: energy minimization
  - others: gradient descent, etc
  - discussion: termination criteria

### **Barrier Jumping**

- same idea as simulated annealing
  - but compute directly
  - just ignore repulsion for fraction of vertices
- solves start position sensitivity problem

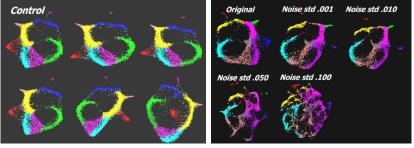


#### Results

#### efficiency

- naive approach: O(V<sup>2</sup>)
- approximate density field: O(V)
- good stability
  - rotation/reflection can occur

#### different random start adding noise



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# Critique

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### Critique

#### real data

- suggest check against subsequent publication!
- give criteria, then discuss why solution fits
- visual + numerical results
  - convincing images plus benchmark graphs

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- detailed discussion of alternatives at each stage
- specific prescriptive advice in conclusion

### **Dimension Ordering**

- in NP, like most interesting infovis problems heuristic
- divide and conquer
  - iterative hierarchical clustering
  - representative dimensions
- choices
  - similarity metrics
  - importance metrics
    - variance
  - ordering algorithms
    - optimal
    - random swap
    - simple depth-first traversal

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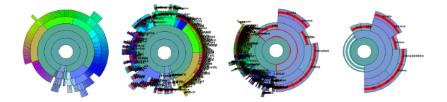
# Spacing, Filtering

- same idea: automatic support
- interaction
  - manual intervention
  - structure-based brushing
  - focus+context, next week

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### **Results: InterRing**

#### raw, order, distort, rollup (filter)

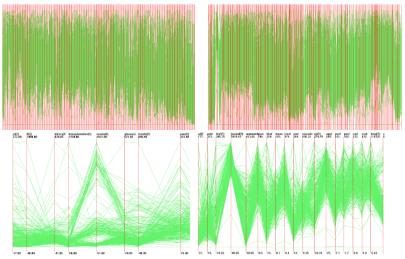


[Interactive Hierarchical Dimension Ordering, Spacing and Filtering for Exploration Of High Dimensional Datasets. Yang Peng, Ward, and Rundensteiner. Proc. InfoVis 2003]

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#### **Results: Parallel Coordinates**

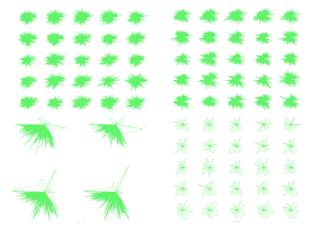
raw, order/space, zoom, filter



[Interactive Hierarchical Dimension Ordering, Spacing and Filtering for Exploration Of High Dimensional Datasets. Yang Peng, Ward, and Rundensteiner. Proc. InfoVis 2003]

#### **Results: Star Glyphs**

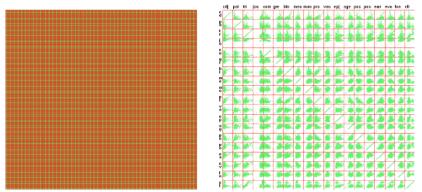
raw, order/space, distort, filter



[Interactive Hierarchical Dimension Ordering, Spacing and Filtering for Exploration Of High Dimensional Datasets. Yang Peng, Ward, and Rundensteiner. Proc. InfoVis 2003]

#### **Results: Scatterplot Matrices**

raw, filter



[Interactive Hierarchical Dimension Ordering, Spacing and Filtering for Exploration Of High Dimensional Datasets. Yang Peng, Ward, and Rundensteiner. Proc. InfoVis 2003]

# Critique

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### Critique

#### pro

- approach on multiple techniques,
- real data!
- con
  - always show order then space then filter
    - hard to tell which is effective
    - show ordered vs. unordered after zoom/filter?

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#### Software, Data Resources

#### www.cs.ubc.ca/~tmm/courses/infovis/resources.html

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