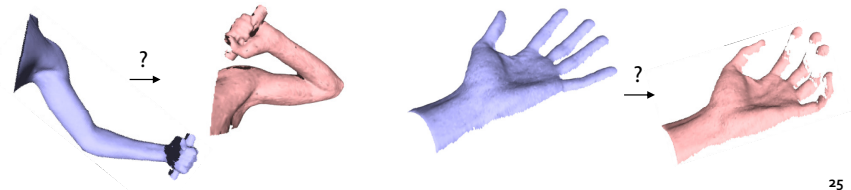


# Automatic Registration for Articulated Shapes

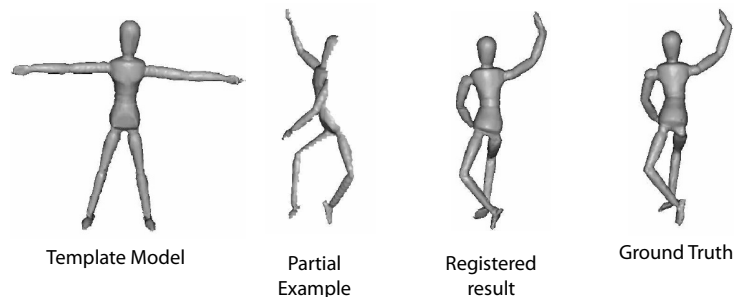
## Problem Statement

- Solve pairwise registration problem
  - ▣ Develop robust method independent of initial pose
  - ▣ Do not require markers or a template
- Contributions:
  - ▣ Useful for initialization: used as preprocessing step
  - ▣ Focus on registration: does not solve for a reduced motion model



## Related Work

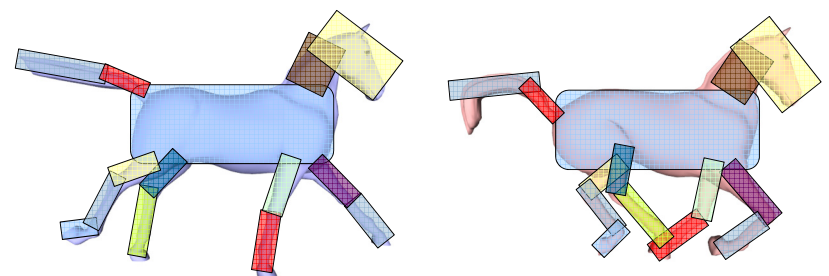
- Correlated correspondence algorithm, requires a template (Anguelov et al. 2004)



(from Anguelov et al. 2004) 26

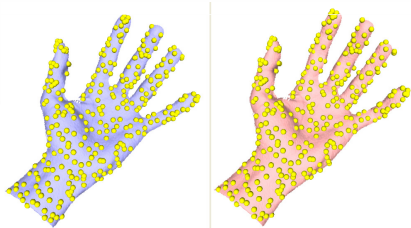
## Algorithm Overview

- Articulated motion → small set of transformations
- **Predetermine** a set of transformations describing the motion
- **Optimize assignment** of transformations to the points

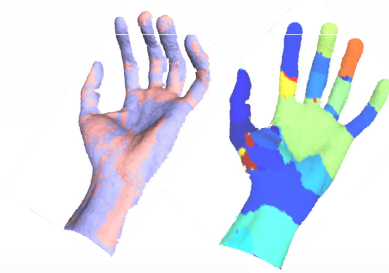


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## Algorithm Description



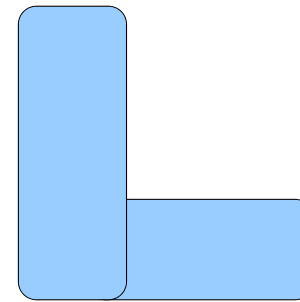
**Motion Sampling**



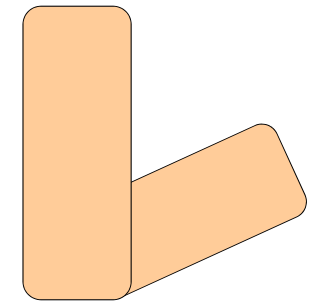
Global Motion Optimization

## Motion Sampling Illustration

- Find transformations that move parts of the source to parts of the target



Source Shape

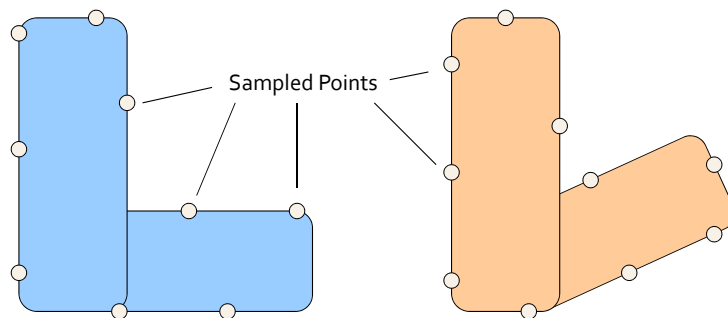


Target Shape

29

## Motion Sampling Illustration

- Find transformations that move parts of the source to parts of the target



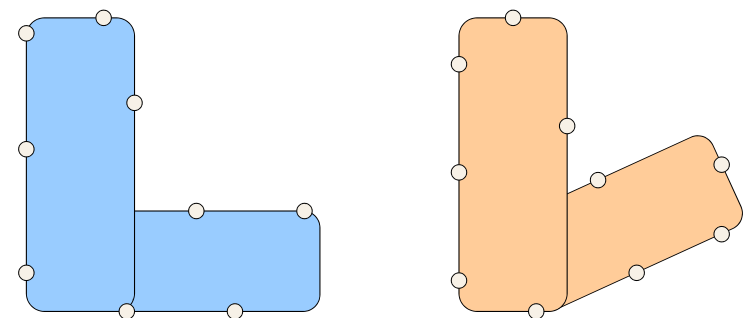
Source Shape

Target Shape

30

## Motion Sampling Illustration

- Find transformations that move parts of the source to parts of the target



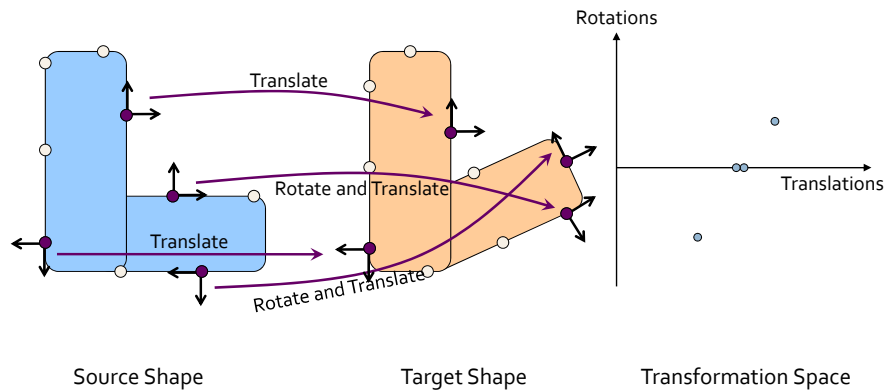
Source Shape

Target Shape

31

# Motion Sampling Illustration

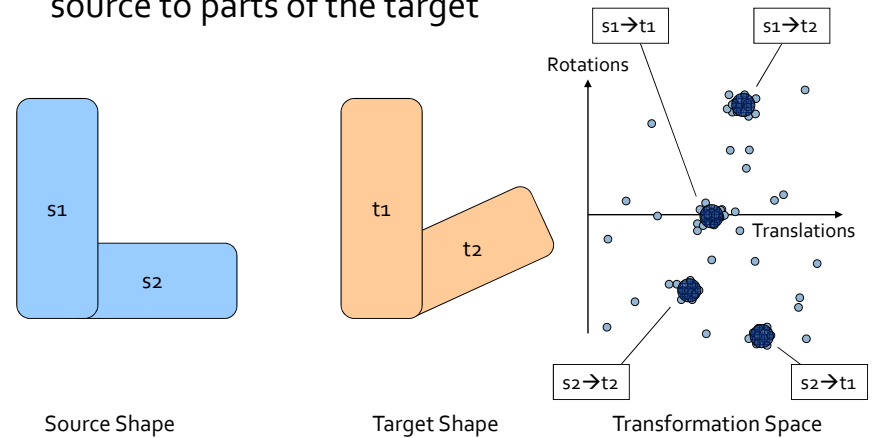
- Find transformations that move parts of the source to parts of the target



32

# Motion Sampling Illustration

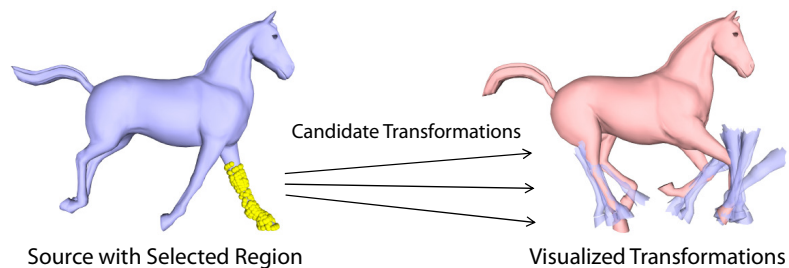
- Find transformations that move parts of the source to parts of the target



33

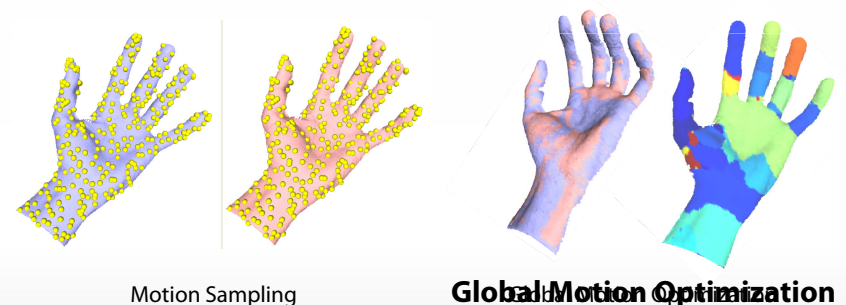
# Limitations of Motion Sampling

- Final Output*: finite set of rigid transformations
- If there are multiple similar parts
  - Does not figure out the correct part
  - Disambiguate in the optimization step



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# Algorithm Description



Motion Sampling

Global Motion Optimization

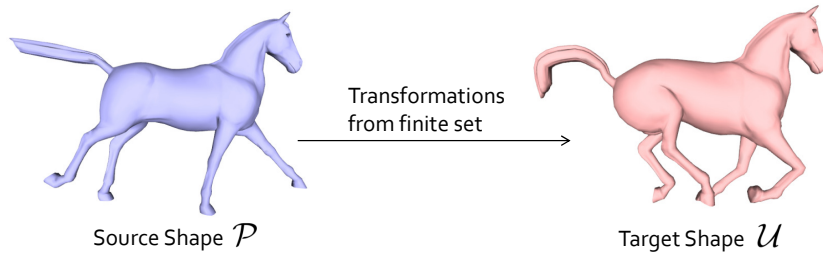
# Global Motion Optimization

- Optimize an *assignment* from a finite set of transformations

**argmin** Data Cost + Smoothness Cost

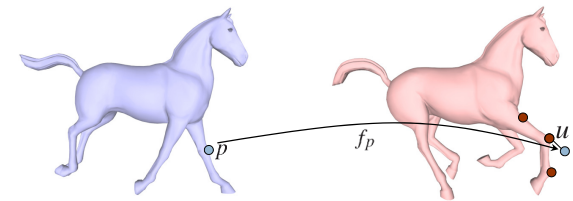
Assignment from a set of transformations

- A discrete labelling problem → Graph Cuts for optimization



# Data Term

- Move all points as close as possible to the target
- How to measure distance to target?
  - Apply selected transformation  $f_p$  for all  $p = f_p(p)$
  - Measure distance to closest point  $u$  in target

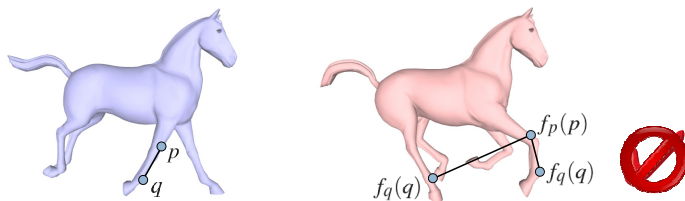


# Smoothness Term

- Preserve edge length between neighboring points

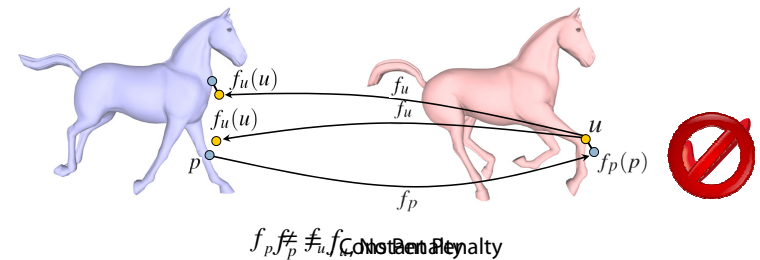
$$V(p, q, f_p, f_q) = \left| \underbrace{\|p - q\|}_{\text{Original Length}} - \underbrace{\|f_p(p) - f_q(q)\|}_{\text{Transformed Length}} \right|$$

- Disambiguates multiple possible mappings



# Symmetric Cost Function

- Swapping source / target can give different results
  - Optimize assignment in both meshes (forward & backward)
  - Enforce consistent assignment: penalty when  $f_p \neq f_u$



# Optimization Using Graph Cuts

$$\underset{\text{Assignment from a set of transformations}}{\operatorname{argmin}} \quad \text{Data}_{\text{Source}} + \text{Smoothness}_{\text{Source}} + \text{Data}_{\text{Target}} + \text{Smoothness}_{\text{Target}} + \text{Symmetric Consistency}_{\text{Source \& Target}}$$

- Data and smoothness terms apply to both shapes
- Additional symmetric consistency term
- Weights to control relative influence of each term
- Use "graph cuts" to optimize assignment
  - [Boykov, Veksler & Zabih PAMI '01]

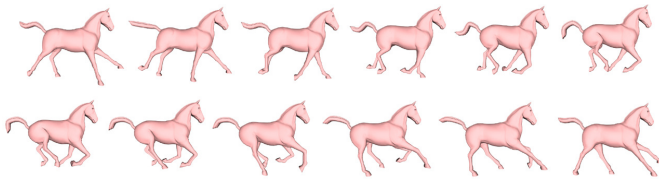
40

## Results

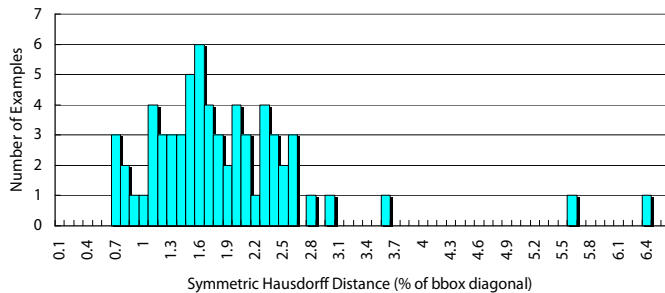
Horse Dataset  
Arm Dataset  
Hand Dataset

## Horse Dataset Results

12 poses of galloping horse: total of 66 pairs, correct leg matched in 64 pairs

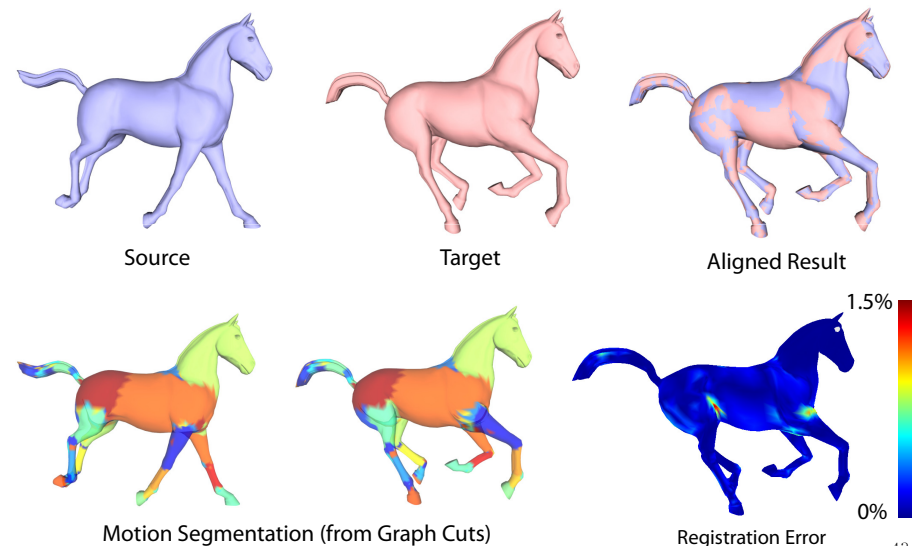


Histogram of Error in Galloping Horse Dataset (minimum over 3 trials)



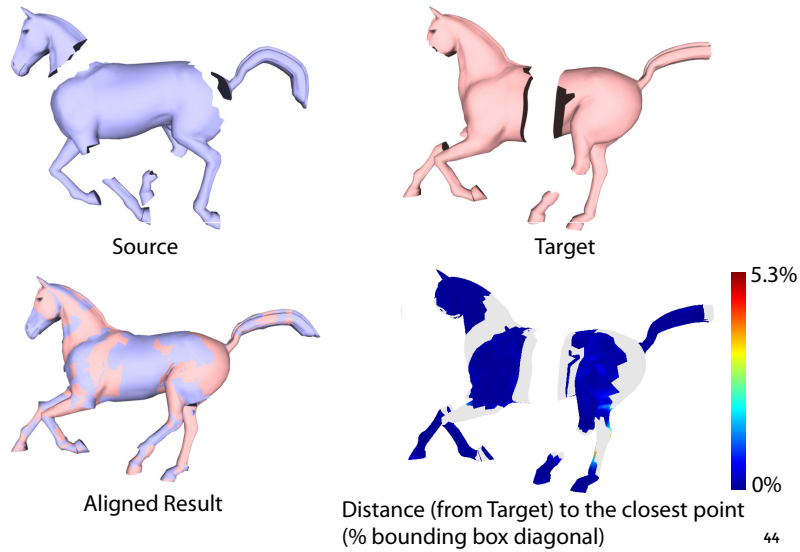
42

## Synthetic Dataset Example



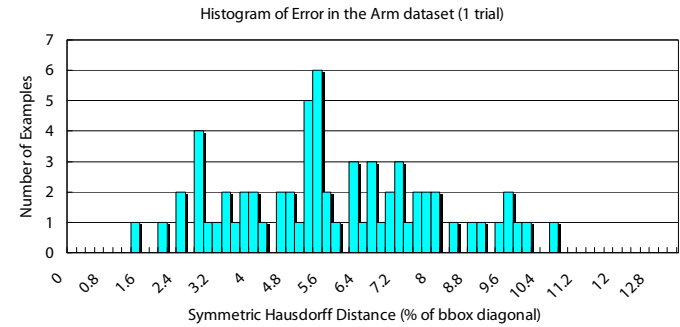
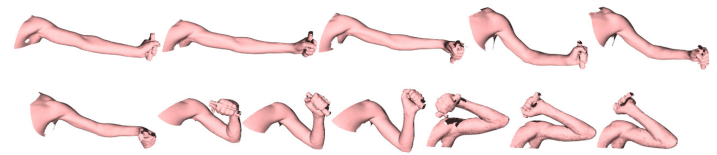
43

# Synthetic Dataset w/ Holes

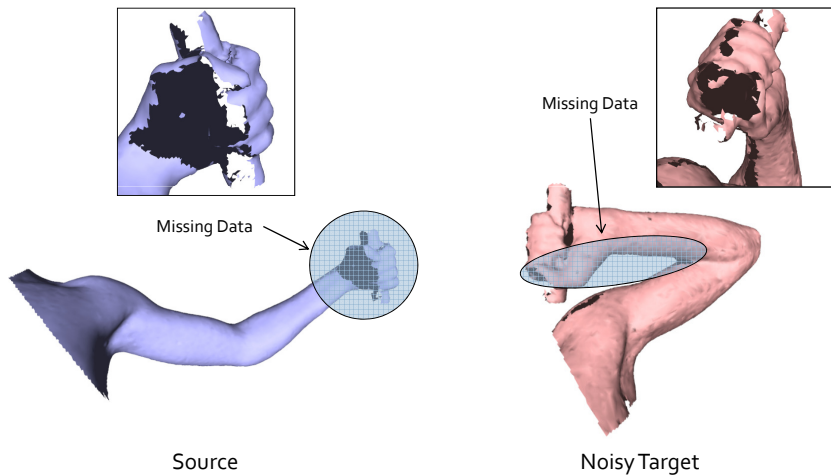


# Arm Dataset Results

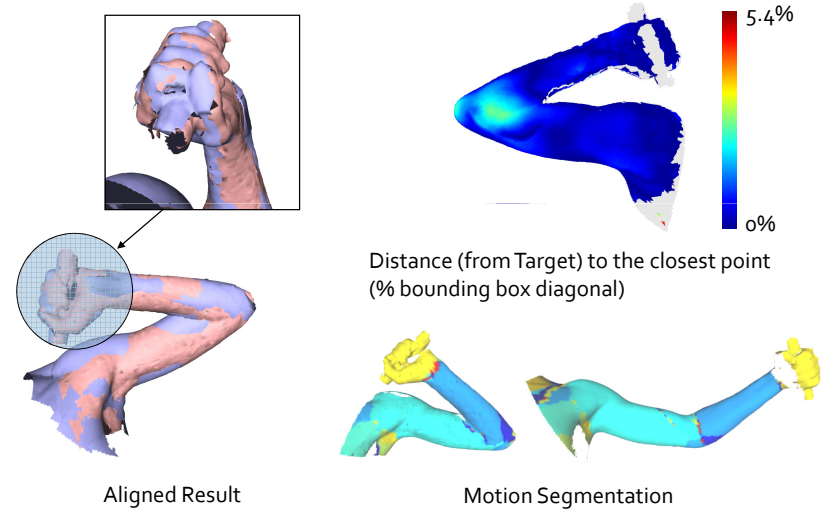
12 poses of arm scans: total of 66 pairs, arm & hand orientation matched in all pairs



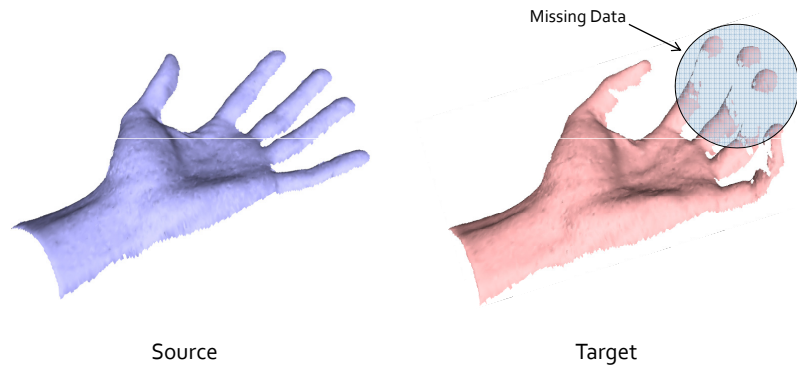
# Arm Dataset Example



# Arm Dataset Example

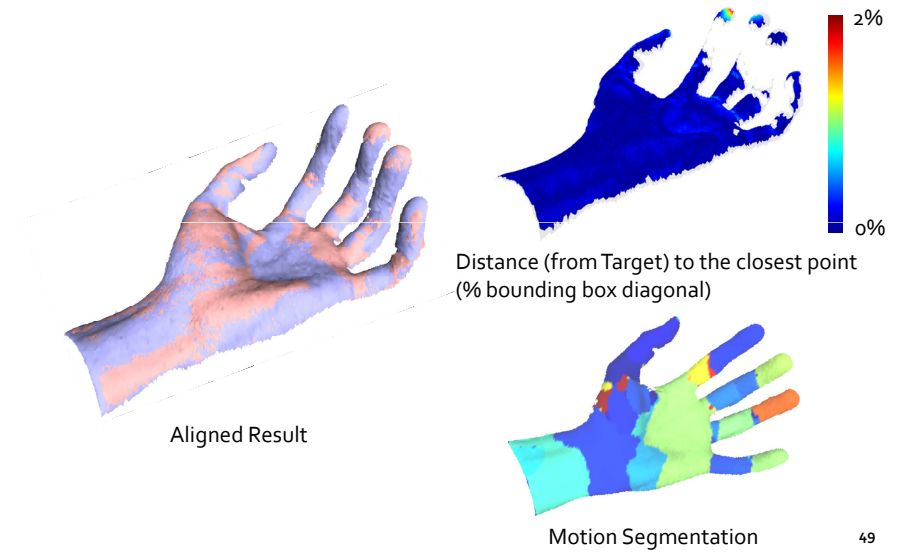


# Hand Dataset Example



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# Hand Dataset Example



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# Performance

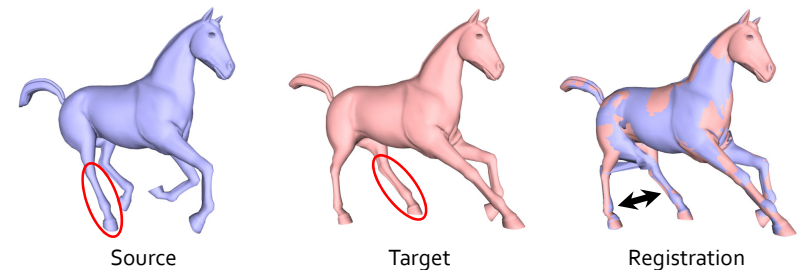
Dataset	#Points	# Labels	Matching	Clustering	Pruning	Graph Cuts
Horse	8431	1500	2.1 min	3.0 sec	(skip) 1.6 sec	1.1 hr
Arm	11865	1000	55.0 sec	0.9 sec	12.4 min	1.2 hr
Hand (Front)	8339	1500	14.5 sec	0.7 sec	7.4 min	1.2 hr
Hand (Back)	6773	1500	17.3 sec	0.9 sec	9.4 min	1.6 hr

- Graph cuts optimization is most time-consuming step
  - ▣ Symmetric optimization doubles variable count
  - ▣ Symmetric consistency term introduces many edges

50

# Limitations

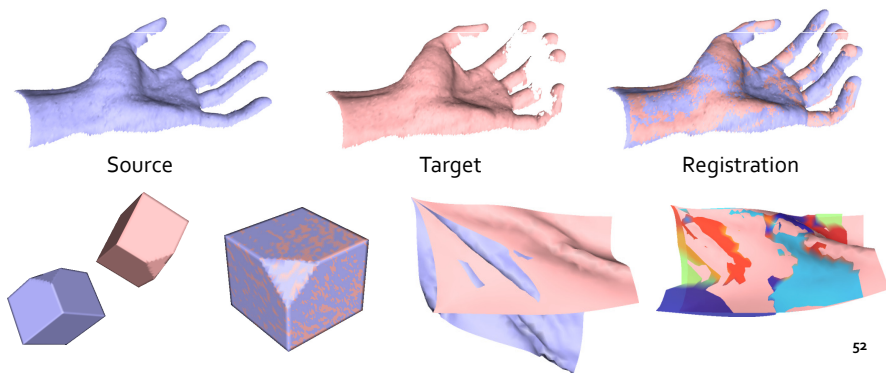
- Errors in registration
  - ▣ Trade-off between data and smoothness costs
    - Data weight too high → May break smoothness
    - Smoothness weight too high → Prefer bad alignment



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## Limitations

- Errors in registration
  - Motion sampling: may fail to sample properly when too much missing data, non-rigid motion
  - Hard assignment of transformations



## Conclusions

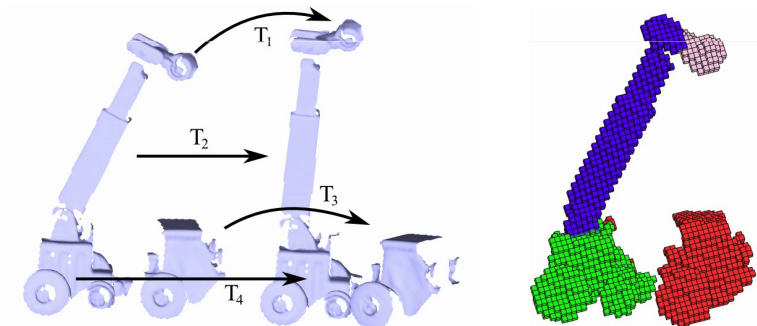
- Automatic method for registering articulated shapes
  - No template, markers, or manual segmentation needed
  - Explicitly sample a discrete set of motion
  - Optimize the assignment of transformations
  - Graph cut result gives intuitive segmentation
- Useful for obtaining a robust initialization of the registration
  - Does not provide an articulated motion model

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## Range Scan Registration Using Reduced Deformable Models

## Problem Statement

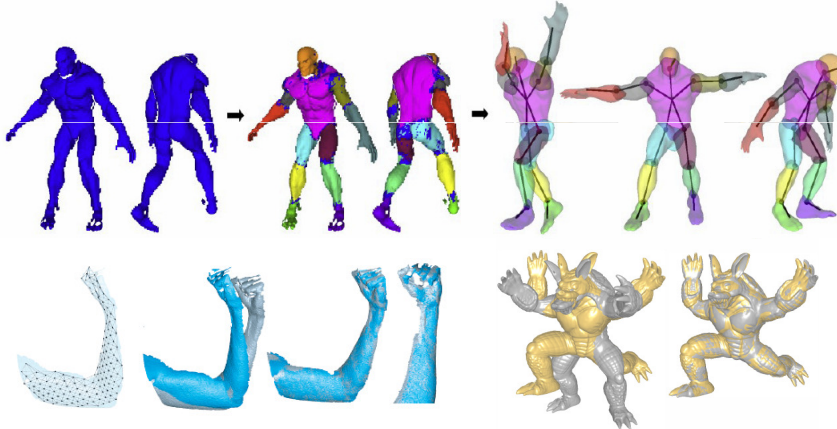
- Fit a model of the surface motion to a pair of scans
  - Articulated model (e.g. joints, smooth weights)
  - Serves as the basis for fitting on multiple frames





## Related Work

- User provided segmentation: Pekelnyc8
- Unsupervised pairwise registration: Lio8, Huango8

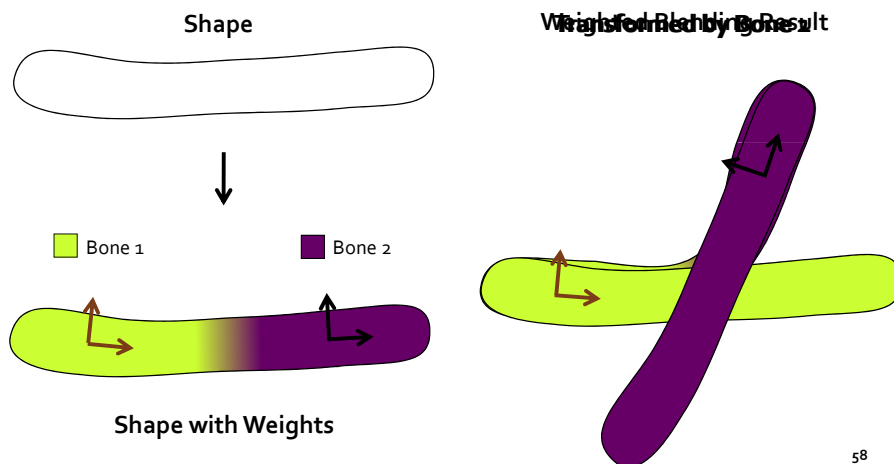


(from Pekelnyc and Gotsman 2008, Li et al. 2008 and Huang et al. 2008) 56

## Problem Formulation

## Model: Linear Blend Skinning

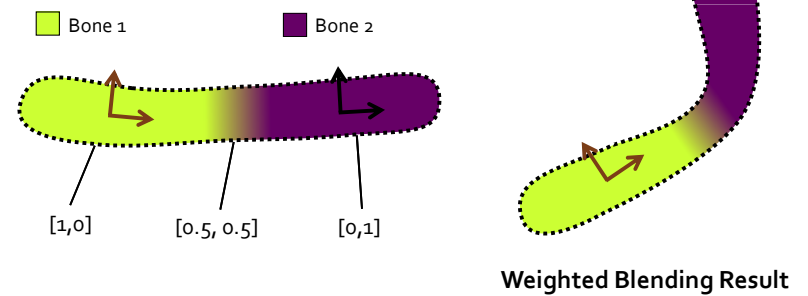
- Transformations (bones) and weights



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## Model: Linear Blend Skinning

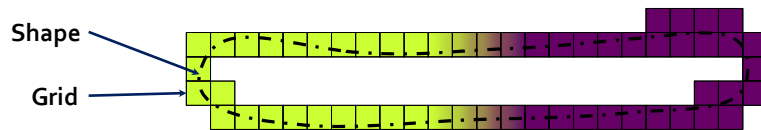
- Each point assigned weights in reference pose
- Transformations move each point according to its weights



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## Weight Grid

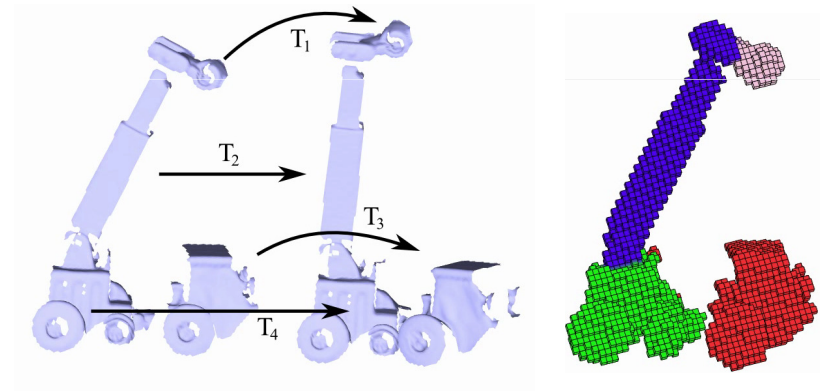
- Define weights on grid enclosing surface
  - Covers small holes, reduces variables
  - Provides regular structure for optimization



60

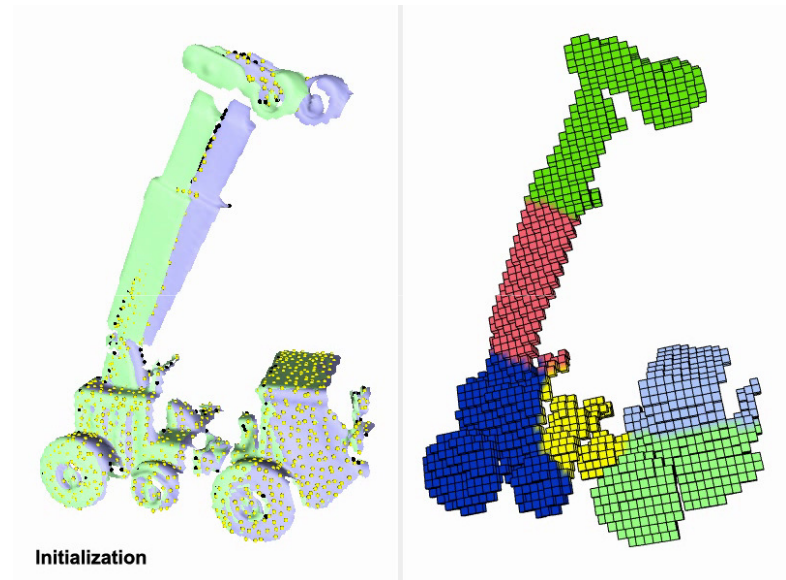
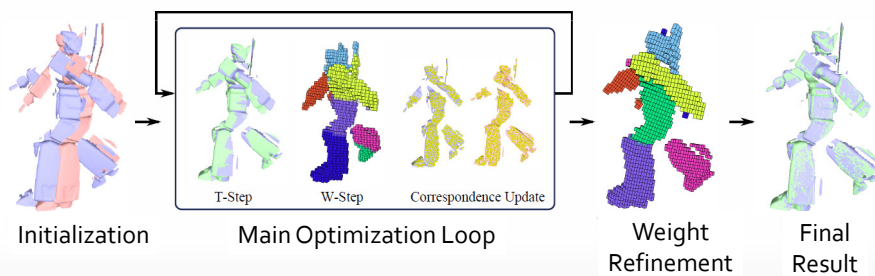
## LBS for scan registration

- Fit the transformations and weights to align a pair of range scans



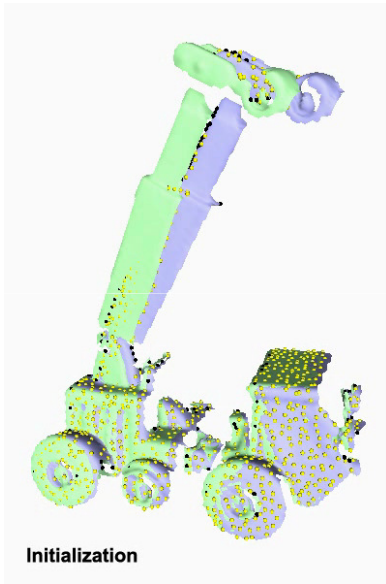
61

## Algorithm Description

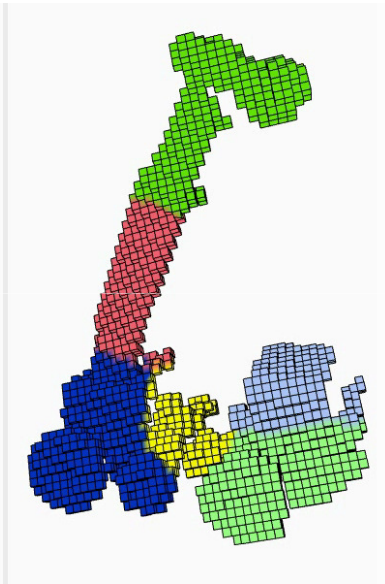


Initialization

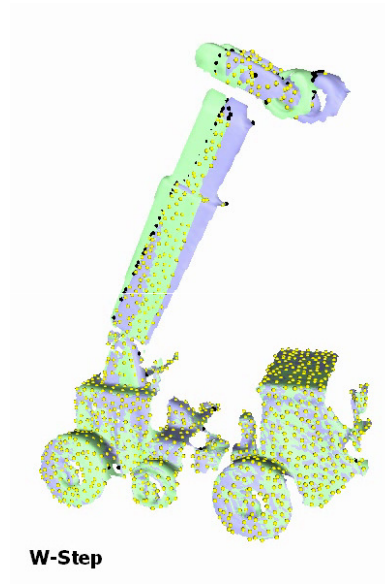
63



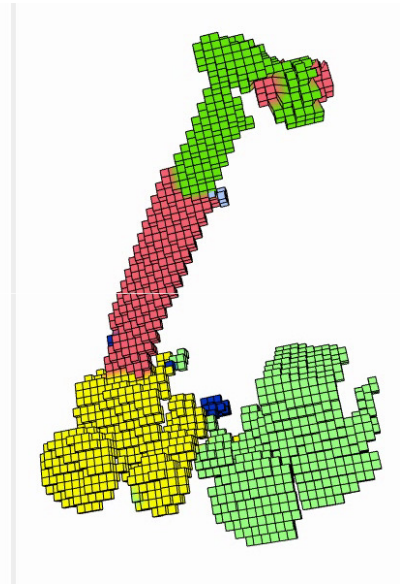
Initialization  
(Converged)



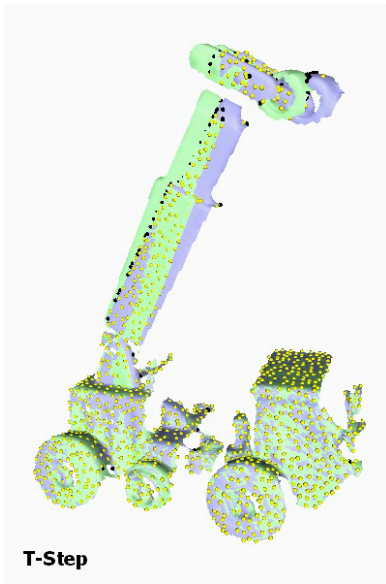
64



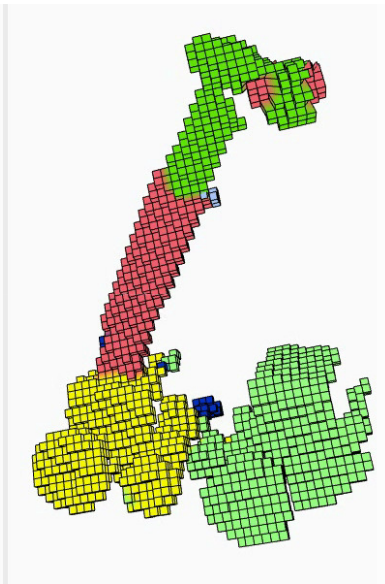
W-Step



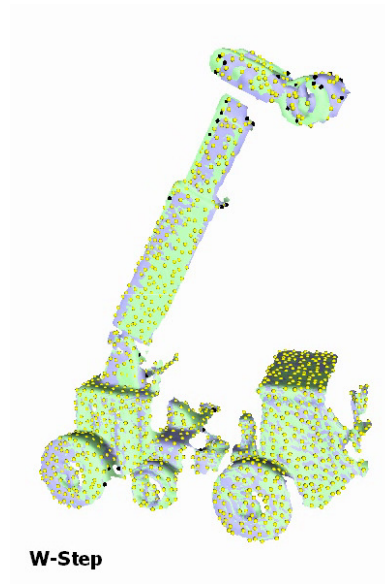
65



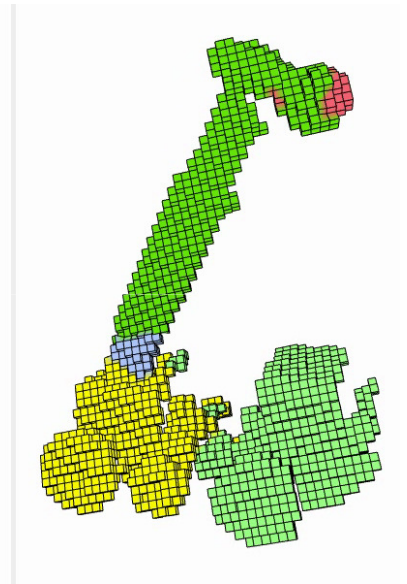
T-Step  
(Converged)



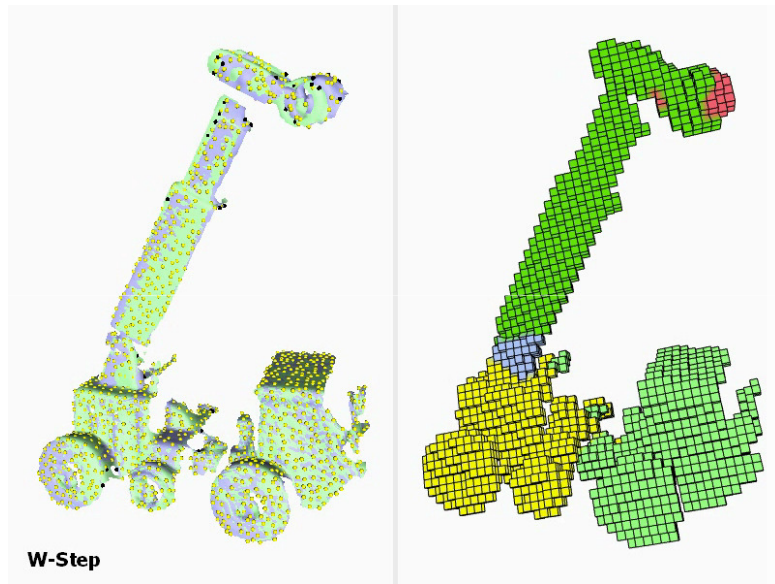
66



W-Step

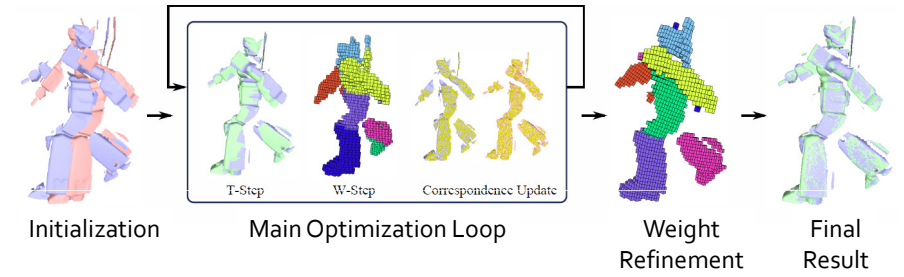


67

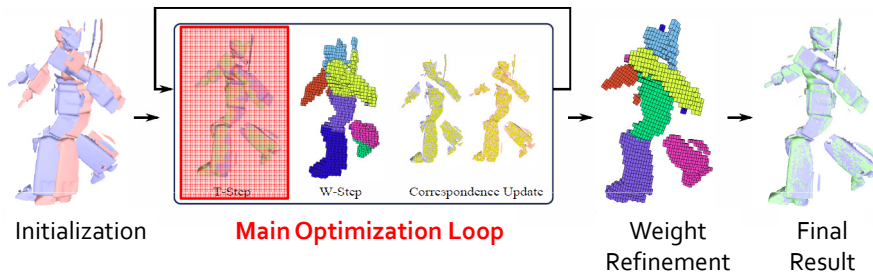


**W-Step**  
(Finished)

## Optimization overview



## Optimization overview

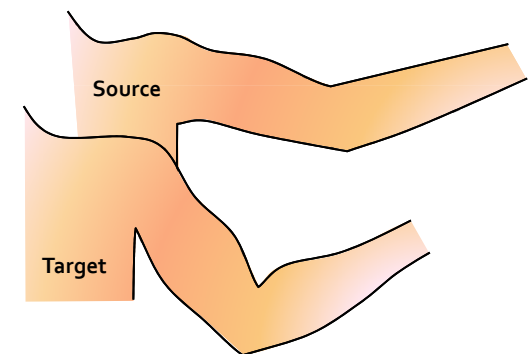


### □ T-Step: Optimize Alignment

- ▣ Distance Term
- ▣ Joint Constraint Term

## T-Step: Distance Term

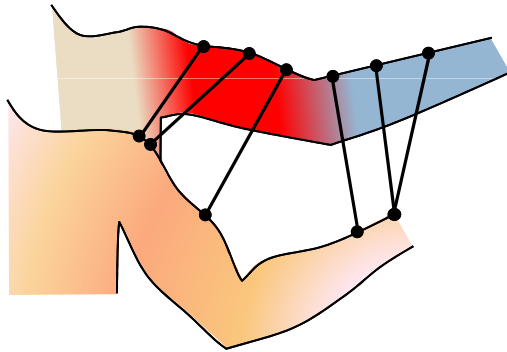
- Fix weights & solve for transformations



## T-Step: Distance Term

- Fix weights & solve for transformations
  - ▣ Use closest point correspondences

- Bone 1
- Bone 2
- Bone 3

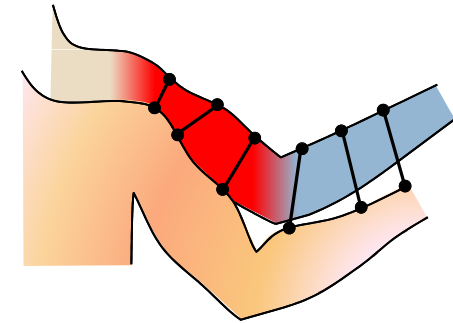


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## T-Step: Distance Term

- Fix weights & solve for transformations
  - ▣ Use closest point correspondences

- Bone 1
- Bone 2
- Bone 3

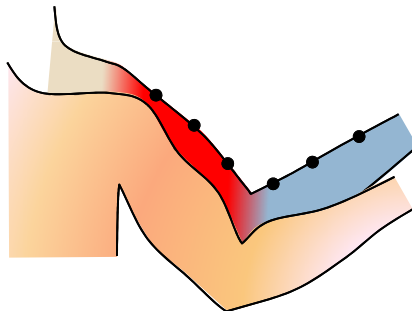


73

## T-Step: Distance Term

- Fix weights & solve for transformations
  - ▣ Use closest point correspondences
  - ▣ Iterate further until convergence

- Bone 1
- Bone 2
- Bone 3

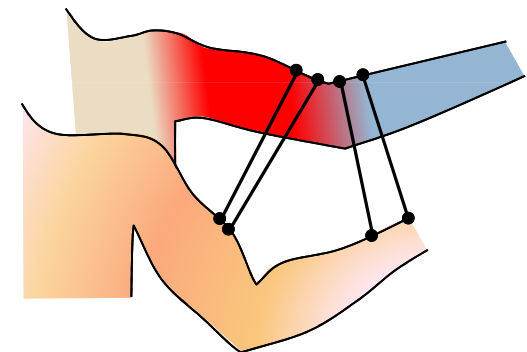


74

## T-Step: Joint Constraint Term

- Prevent neighboring bones from separating

- Bone 1
- Bone 2
- Bone 3

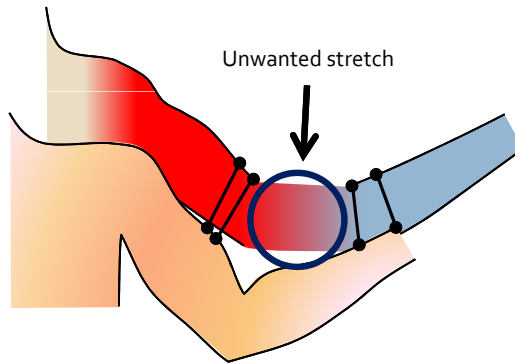


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## T-Step: Joint Constraint Term

- Prevent neighboring bones from separating
  - ▣ Constrain overlapping weight regions

- Bone 1
- Bone 2
- Bone 3

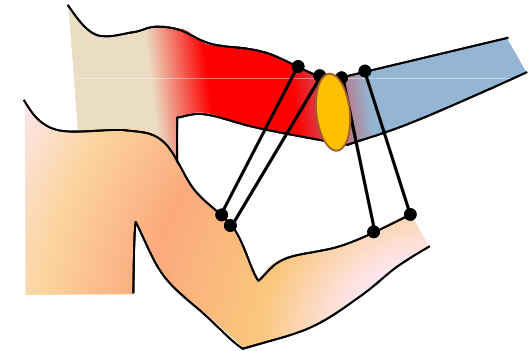


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## T-Step: Joint Constraint Term

- Prevent neighboring bones from separating
  - ▣ Constrain overlapping weight regions

- Bone 1
- Bone 2
- Bone 3

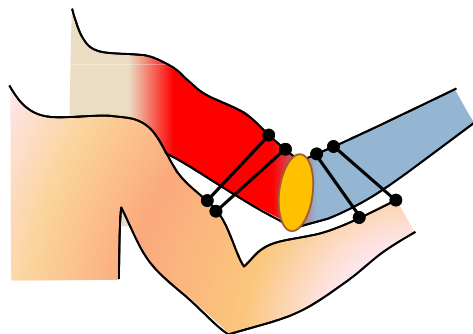


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## T-Step: Joint Constraint Term

- Prevent neighboring bones from separating
  - ▣ Constrain overlapping weight regions

- Bone 1
- Bone 2
- Bone 3



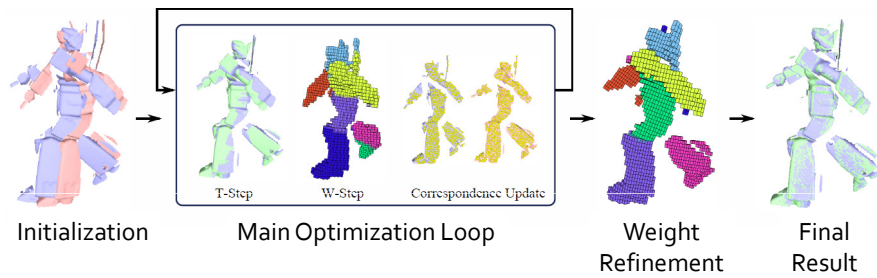
78

## T-Step: Optimization summary

- Like rigid registration
  - ▣ Except multiple parts & joint constraints
- Non-linear least squares optimization
  - ▣ Solving for a rotation matrix
  - ▣ Gauss-Newton algorithm
  - ▣ Solve by iteratively linearizing solution
- Few variables → Fast performance
  - ▣ # variables =  $6 \times \text{\#bones}$
  - ▣ Typically 5~10 bones in our examples

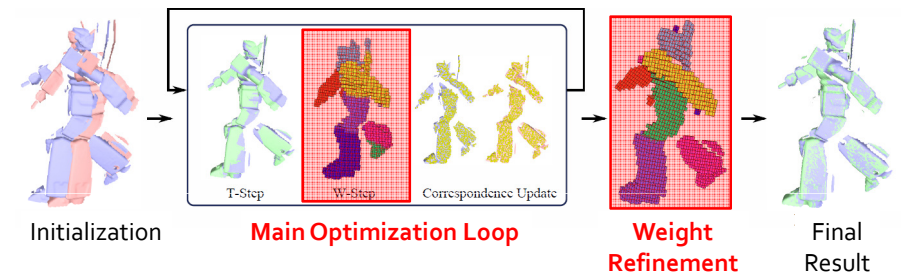
79

## Optimization overview



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## Optimization overview



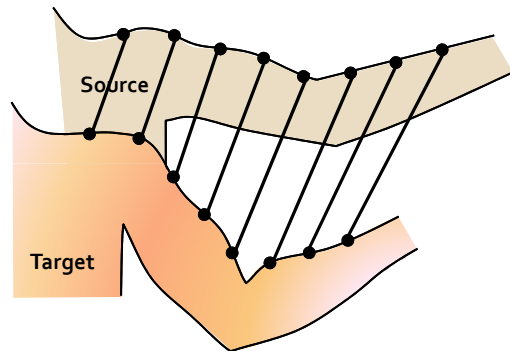
### □ W-Step: Optimize Weights

- Use Discrete Labelling
- Continuous Weight Refinement

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## W-Step: Optimizing weights

- Fix transformations, solve for continuous weights

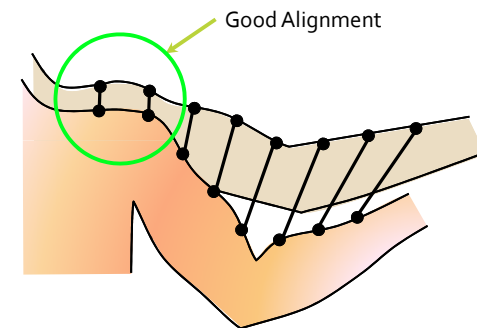


Correspondences from last T-Step

82

## W-Step: Optimizing weights

- Fix transformations, solve for continuous weights

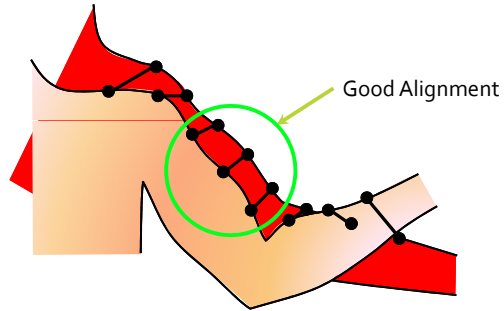


Bone 1  
(Applied to entire shape)

83

## W-Step: Optimizing weights

- Fix transformations, solve for continuous weights

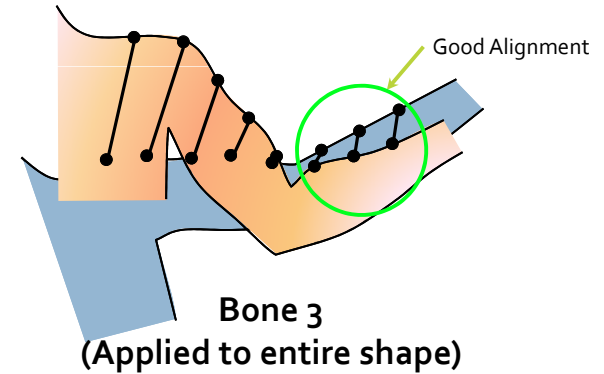


**Bone 2**  
(Applied to entire shape)

84

## W-Step: Optimizing weights

- Fix transformations, solve for continuous weights

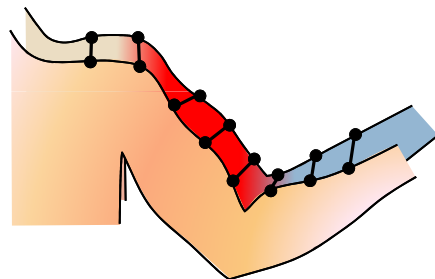


**Bone 3**  
(Applied to entire shape)

85

## W-Step: Optimizing weights

- Fix transformations, solve for continuous weights



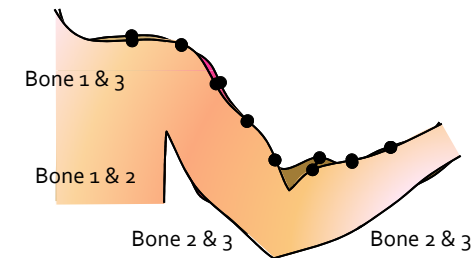
**"Ideal" solved result**

- Bone 1
- Bone 2
- Bone 3

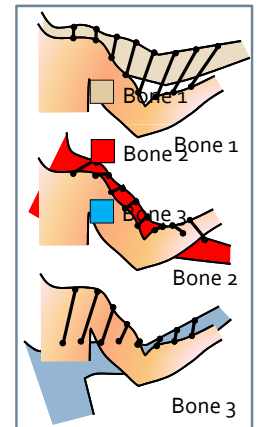
86

## W-Step: Optimizing weights

- Without additional constraints, problem is underconstrained



**Typical solved result**

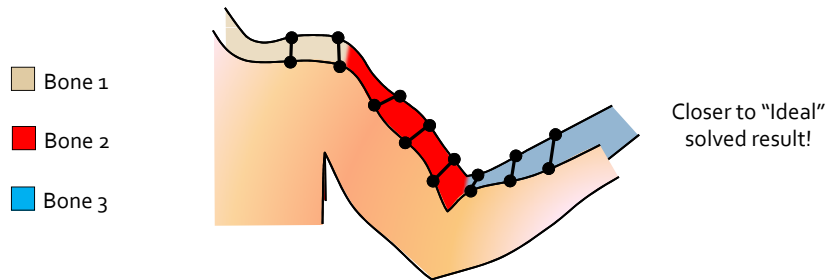


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## Use discrete labeling

- **Our solution:** one transformation per location
  - ▣ Bones = labels
  - ▣ Becomes discrete labeling problem



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## W-Step: Optimization Summary

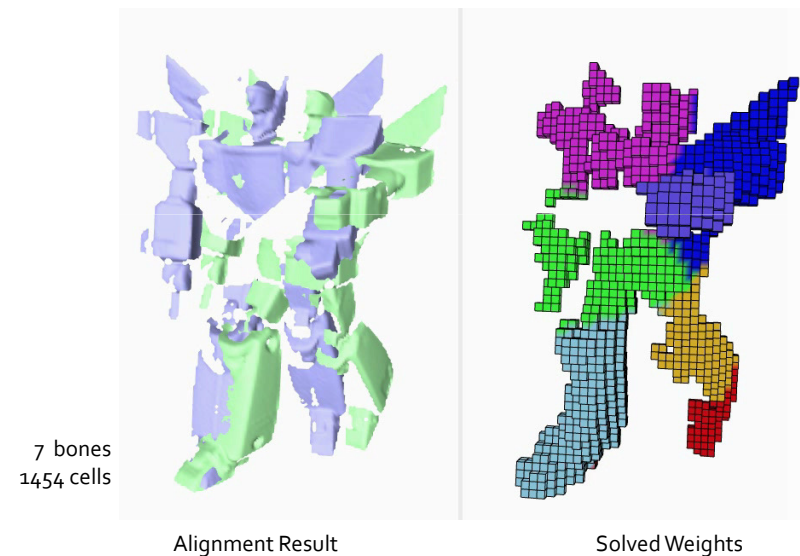
- Use "graph cuts" to optimally label grid cells
  - ▣ [Boykov, Veksler & Zabih PAMI '01]
- Distance term + Smoothness term
  - ▣ Distance: measures alignment for a given label
  - ▣ Smoothness: penalizes different labels for adjacent cells
- Good Performance
  - ▣ Only ~ 1000 grid cells (graph nodes) in our examples
  - ▣ Fast performance for graph cuts

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## Results

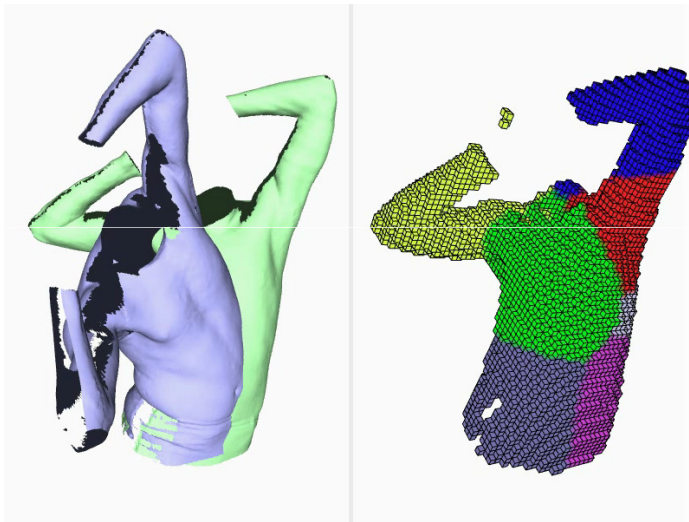
Robot, torso video  
Interactive posing video  
Additional results & statistics

## Robot video (real-time recording)



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## Torso video (2x speed recording)



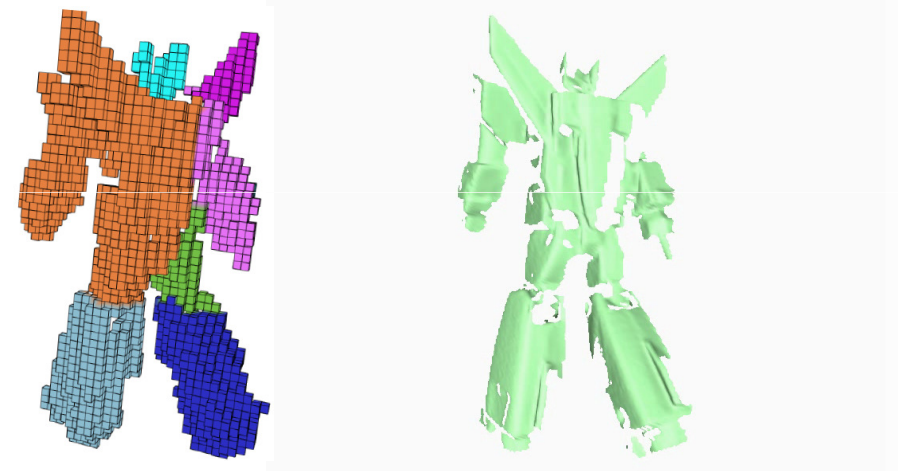
7 bones  
4890 cells

Alignment Result

Solved Weights

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## Interactive posing (real-time recording)



Solved Weights  
(7 bones, 1598 cells)

Interactive Posing Result

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## Average performance statistics

	Car	Robot	Walk	Hand
<b>Bones</b>	7	7	10	12
<b>Corresp.</b>	1200	1200	1000	1500
<b>Vertices</b>	5389	9377	4502	34342
<b>Max Dist</b>	20	40	20	30
<b>Grid Res</b>	60	65	50	40
<b>Grid Cells</b>	1107	1295	1014	814
<b>Grid Points</b>	2918	3366	2553	1884
<b>Setup</b>	0.185 sec	0.234 sec	0.1365 sec	0.078 sec
<b>RANSAC</b>	8.089 sec	20.001 sec	5.517 sec	N/A
<b>Align</b>	9.945 sec	19.644 sec	23.092 sec	49.918 sec
<b>Weight</b>	6.135 sec	10.713 sec	10.497 sec	3.689 sec
<b>Total Time</b>	24.355 sec	50.591 sec	39.242 sec	53.684 sec

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## Limitations

- Discussion
  - ▣ Topology issues with grid
    - Improve in next section using graph-based approach
  - ▣ Limited to a pair of scans
    - Simultaneously register multiple frames in next section
  - ▣ Limitations with LBS
    - Optimize better model (e.g. DLB)

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# Conclusion

- A new algorithm to align range scans by modeling the motion with a reduced deformable model
  - Use LBS to represent the motion
  - Represent weight function using a 3D grid
  - Solve for the parameters using alternating optimization
  - No marker, template, segmentation information
  - Robust to occlusion & missing data
- **Next:** extend this method to handle multiple frames